Package 'Rbmop'

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Type Package

Title B-spline MoPs densities and conditional densities

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Description Handling, estimation and comparison functions for B-spline MoPs densities and conditional densities (bmop).
License GPL-3
Imports stats
Suggests rgl, cubature
R topics documented:
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 ${\tt add_knots.bmop}$

Add a new knot to a bmop object

Description

Add a new knot to a bmop object

Usage

```
add_knots.bmop(bmop, value, MARGIN = 1)
```

Arguments

bmop a bmop object

value the new knot to be added

MARGIN the dimension where the new knot has to be added

Value

a bmop object

AIC.bmop 3

AIC.bmop Akaike Informat	tion Criteria for bmop
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Description

Akaike Information Criteria for bmop

Usage

```
## S3 method for class 'bmop'
AIC(object, data, corrected = F, ..., k = 2)
```

Arguments

object a bmop object

data data.frame, matrix, vector of observations

corrected logical ... see AIC

k penalization coefficients, see AIC

as.bins Bins grouping

Description

This function extend the histogram class for multi-dimensional datasets

Usage

```
as.bins(data, breaks = nclass.FD, ...)
```

Arguments

data a dataset

breaks function or positive integer
... additional parameters

Value

an object bins, the data are grouped into bins uniformly

BIC.bmop

as.function.bmop

Convert an bmop object to a function

Description

Convert an bmop object to a function

Usage

```
## S3 method for class 'bmop'
as.function(x, MIN = 0, ...)
```

Arguments

```
x an bmop object
```

MIN non negative number, MIN value for evaluation of x

... compatibility with as.function

Examples

```
bmop<-bmop_fit(rnorm(200))
fun<-as.function(bmop)
fun(0)
fun(3)
plot(fun,from=-2,to=+2)</pre>
```

BIC.bmop

Bayesian Information Criteria for bmop

Description

Bayesian Information Criteria for bmop

Usage

```
## S3 method for class 'bmop'
BIC(object, data, corrected = F, ...)
```

Arguments

```
object a bmop object
```

data data.frame, matrix, vector of observations

corrected logical ... see BIC

bmopPar 5

bmopPar

Set Rbmop parameters

Description

Set appropriate global parameters to be used by Rbmop functions. This is the appropriate way to change those parameters. The use is similar to par() in package graphics.

Usage

```
bmopPar(...)
```

Arguments

... see details.

Details

This function set parameters used for estimation. The call values of the parameters.

bmopPar() just print the

mle=FALSE: logical. If use maximum-likelihood estimation of bmop coefficient, setting mle=TRUE just force repMax=1.

N=NA: If present, the number of knots in every dimensions. Vector of positive integer, if needed values will be recycled.

order=3: The order of the B-spline in every dimensions, vector of positive integer, if needed values will be recycled.

alpha=3: The penalization exponent to compute the number of knots. This is the default method to compute the number of knots, with the formula: $floor(n^(1/alpha))$, where n is the number of observations in the dataset. If !is.na(N) then the number of knots will be set to N^d where d is the number of dimensions in the dataset (num. of variables).

knotsMethod="uniform": "uniform" or "quantiles" knots, how knots are computed by generate_knots.

k=2: Coefficient of AIC (penalized likelihood), positive integer or "BIC" string. This is used by search_bmop.

toll=10^{-10}: Tollerance for the increment of the likelihood in the mle estimation of the coefficient.

repMax=100: maximum number of iteration in the mle estimation of the coefficient

MIN=10^{-10}: This is not a learning parameter but instead define the MIN parameter in the evaluation of bmop object. Observe that some functions like logLik or plot, set this parameter independently.

autoReduce=200: This value set the maximum dimension of an accepted dataset as raw-data, for larger dataset, functions bmop_fit and search_bmop will be applied over the reduced bins (histogram). Setting it to Inf disable this features.

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Estimation of bmop density or conditional density

Description

Estimation of bmop density or conditional density

Usage

```
bmop_fit(data, conditional = F, Min = NULL, Max = NULL, ...)
```

Arguments

data.frame, matrix, vector or object of class "histogram" or "bins"

conditional logic, if TRUE a conditional density is learned

Min vector of lower bounds

Max vector of upper bounds

... see bmopPar

Value

a bmop object, a density if conditional=FALSE or a conditional density if conditional=TRUE. In the latter case the first variable of the dataset is considered as a de conditioned one and the rest of the variables as the conditioning ones. If the dataset has only one variable a normal density is generated discarding the value of conditional.

Examples

```
plot(bmop_fit(rnorm(100)))
plot(bmop_fit(hist(rnorm(100000))))
############################
Data<-data.frame(rnorm(100),rexp(100))
bmop<-bmop_fit(Data)
plot(bmop)
########################
X<-rnorm(100)
Y<-rnorm(100,mean=X)
Data<-data.frame(X,Y)
bmopPar(mle=TRUE)
bmopC<-bmop_fit(Data,conditional=TRUE)
plot(bmopC)</pre>
```

bmop_fit.bins 7

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bmop) † 1	t.	b1	ns

Estimation of bmop density or conditional density

Description

Estimation of bmop density or conditional density

Usage

```
## S3 method for class 'bins'
bmop_fit(data, conditional = F, Min = NULL, Max = NULL,
   bmop = NULL, ...)
```

Arguments

data histogram or bins object the variables must be in the right order

conditional logic, if TRUE a conditional density is learned

Min vector of lower bounds

Max vector of upper bounds

bmop a bmop object
... see bmopPar

Value

a bmop object

bmop_fit.data.frame

Estimation of bmop density or conditional density

Description

Estimation of bmop density or conditional density

```
## S3 method for class 'data.frame'
bmop_fit(data, conditional = F, Min = NULL,
    Max = NULL, bmop = NULL, ...)
```

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Arguments

data.frame, matrix or vector the variables must be in the right order (the columns

of data)

conditional logic, if TRUE a conditional density is learned

Min vector of lower bounds

Max vector of upper bounds

bmop a bmop object
... see bmopPar

Value

a bmop object

bmop_fit.default

Estimation of bmop density or conditional density

Description

Estimation of bmop density or conditional density

Usage

```
## Default S3 method:
bmop_fit(data, conditional = F, Min = NULL, Max = NULL,
...)
```

Arguments

data.frame, matrix, vector or object of class "histogram" or "bins"

conditional logic, if TRUE a conditional density is learned

Min vector of lower bounds

Max vector of upper bounds

... see bmopPar

Value

a bmop object

bmop_fit.histogram 9

bmop_fit.histogram

Estimation of bmop density or conditional density

Description

Estimation of bmop density or conditional density

Usage

```
## S3 method for class 'histogram'
bmop_fit(data, conditional = F, Min = NULL,
    Max = NULL, bmop = NULL, ...)
```

Arguments

data histogram or bins object the variables must be in the right order

conditional logic, if TRUE a conditional density is learned

Min vector of lower bounds

Max vector of upper bounds

bmop a bmop object ... see bmopPar

Value

a bmop object

clean.bmop

Clean a bmop object

Description

remove extra informations from bmop object

Usage

```
clean.bmop(object)
```

Arguments

object

a bmop object

Value

a bmop object

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compare.bmop

Compare bmop with true density

Description

Compare bmop with true density

Usage

```
compare.bmop(object, dtrue, measure = "MSE", ...)
```

Arguments

```
object bmop object dtrue function
```

measure string, "MSE", "MAE", "MAX"

... optional arguments to be passed to dtrue

Examples

```
data<-rnorm(200)
bmop1<-bmop_fit(data)
bmopPar(mle=TRUE)
bmop2<-bmop_fit(data)
compare.bmop(bmop1,dtrue=dnorm)</pre>
```

comparison_plot

Plot several bmops and true density

Description

Plot several bmops and true density

```
comparison_plot(bmop.list, dtrue = NULL, colors = NULL, lwd = 3,
  type = "1", type.true = "1", col.true = "red",
  names.bmop = 1:length(bmop.list), legend.display = T,
  legend.pos = "topleft", file = NULL, ylim = c(0, 1), ...)
```

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Arguments

bmop.list list of bmop objects (1 dimensional)
dtrue function, true density function
colors NULL or vector of colors
lwd graphical parameter see par
type graphical parameter see par

type. true as type, but just for true density plot

col.true as col graphical parameter but for dtrue density plot

names.bmop vector for the names showed in legend legend.display logical, to show or not the legend

legend.pos string for the position of the legend "top", "left", "topright", etc.

file an optional file name to save the plot

ylim parameter to set the plot correctly, set to NULL for automatic setting

... more parameters to be passed to dtrue

Value

invisible()

Examples

dim.bmop

Dimension of bmop

Description

Dimension of bmop

Usage

```
## S3 method for class 'bmop'
dim(x)
```

Arguments

x a bmop object

Value

the number of free parameters of x

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Envelop of estimated bmop

Description

This function plots various bmop estimations, from differents datasets.

Usage

```
envelope_plot(n = 100, N = 50, rtrue = rnorm, fun = bmop_fit,
   dtrue = dnorm, lwd = 3, type = "1", col.true = "red", ...)
```

Arguments

n	number of bmop densities to learn from different datasets
N	number of observations in every dataset
rtrue	function to generate samples, see rnorm
fun	a learning function of bmop as bmop_fit
dtrue	true density function, see dnorm
lwd	graphical par
type	graphical par
col.true	the color for the true density

additional parameters to be passed to rtrue and dtrue

Value

```
invisible()
```

Examples

```
envelope_plot(n=50,N=50,rtrue=rexp,dtrue=dexp)
```

evaluate.bmop

Evaluation of a bmop object

Description

Evaluation of a bmop object

```
evaluate.bmop(x, object, MIN = bmopPar()$MIN)
```

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Arguments

V	numeric,	vector	matrix
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object bmop object MIN numeric

Details

The deBoor algorithm is used, implemented in C.

Value

Numeric value (values) of the computed bspline at point (points) x.

References

```
Carl de Boor, On calculating with B-splines, Journal of Approximation Theory, Volume 6, Issue 1, July 1972, Pages 50-62, http://www.sciencedirect.com/science/article/pii/0021904572900809.
```

Examples

```
bmop<-bmop_fit(rnorm(100))
evaluate.bmop(0,bmop)
evaluate.bmop(c(-1,0,+1),bmop)</pre>
```

Examples_bmop

Examples of bmop density estimations

Description

Various examples to show the capabilities of bmop estimations.

Usage

```
ex_bmop_gaussian2Mixture(N = 1000, m1 = -3, m2 = 0, lambda = 0.5)
ex_bmop_gaussian3Mixture(N = 1000, m1 = -3, m2 = 0, m3 = +3,
    lambda = c(1, 1, 1))
ex_bmop_gaussianBetaGamma(N = 1000, m1 = -3, m2 = 2, m3 = 3,
    lambda = c(1, 1, 1))
```

Arguments

N positive integer, the number of observations

m1, m2, m3 location parameters

lambda mixing coefficient, vector or double

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Details

This functions generate datasets of N observations. The function bmop_fit is then used to estimate the density. A comparative plot is then returned.

- ex_bmop_gaussian2Mixture lambda-mixture of two Gaussian densities with unitary variance and means m1 and m3.
- ex_bmop_gaussian3Mixture lambda-mixture of three Gaussian densities with unitary variance and means m1, m2 and m3.
- ex_bmop_gaussianBetaGamma lambda-mixture of a Gaussian density with unitary variance and mean m1, a Beta density with shape1=2 shape2=5 ncp=m2 and a Gamma density with shape=9 scale=m3/9.

Value

All the functions return an invisible list contating the generated dataset, the estimated bmops and the true density function. See example on how, for example, plot the default kernel density estimation on the same dataset.

Examples

```
Ex<-ex_bmop_gaussian2Mixture()
points(density(Ex$data),type="1",col="blue",lwd=3)</pre>
```

generate_knots

Generate sequence of knots for bmop objects

Description

Generate sequence of knots for bmop objects

Usage

```
generate_knots(data = NULL, N = 5, method = "uniform", Min = NULL, Max = NULL)
```

Arguments

data data.frame matrix vector

N positive integer, the number of knots

method string "uniform" or "quantiles"

Min numeric
Max numeric

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Examples

```
data<-rnorm(200)
bmopE<-bmop_fit(data)
bmopS<-search_bmop(data)
plot(bmopE)
points(bmopS,type="1",col="red")</pre>
```

integrate.bmop

Integrate bmop object over the support

Description

Integrate bmop object over the support

Usage

```
integrate.bmop(object)
```

Arguments

object

bmop object

Examples

```
data<-rnorm(200)
bmop<-bmop_fit(data)
integrate.bmop(bmop)</pre>
```

is.bmop

Check if an object's class is bmop

Description

Check if an object's class is bmop

Usage

```
is.bmop(object)
```

Arguments

object

an R object

Details

```
Just a call of inherits(object, "bmop")
```

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Value

logical, TRUE if "bmop" is present among class(object), FALSE otherwise

Examples

```
bmop<-bmop_fit(rexp(100))
is.bmop(bmop)</pre>
```

logLik.bmop

Log-Likelihood of bmop object

Description

Log-Likelihood of bmop object

Usage

```
## S3 method for class 'bmop'
logLik(object, data, ...)
```

Arguments

object a bmop object

data matrix, data.frame or vector of observation

... some methods require additional arguments, see AIC

See Also

AIC.bmop

lower.bmop

Lower Limit of bmop

Description

Lower Limit of bmop

Usage

```
lower.bmop(object)
```

Arguments

object a bmop object

Value

numeric value

marginalize.bmop 17

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Description

marginalize a bmop object, that is integrate a bmop multivariate density over some of its dimension.

Usage

```
marginalize.bmop(object, MARGIN = 1, ...)
```

Arguments

object a bmop object

MARGIN positive integer or vector of positive integer, the dimensions that has to be marginal-

ized

... additional parameters

Value

a bmop object over a space of dimension length (MARGIN) the result of integrating over the -MARGIN other dimensions.

Examples

```
data<-data.frame(rnorm(100),rnorm(100))
bmop2d<-bmop_fit(data)
bmop1d<-bmop_fit(data[,1])
bmop1dmargin<-marginalize.bmop(bmop2d,MARGIN=1)
comparison_plot(list(bmop1d,bmop1dmargin),true=dnorm,
names.bmop=c("direct est.","marginalized"))</pre>
```

mean.bmop

Mean value for a bmop density

Description

Mean value for a bmop density

```
## S3 method for class 'bmop' mean(x, ...)
```

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Arguments

x a bmop object

... for compatibility with mean

Value

numeric value, the mean of the bmop density

Examples

```
bmop<-bmop_fit(rnorm(100))
mean(bmop)</pre>
```

new_bmop

New bmop object

Description

Constructor of bmop object.

Usage

```
new_bmop(knots, order, ctrpoints = NULL, nk = FALSE)
```

Arguments

knots list of numeric vector, knots of the B-spline basis

order vector order of the B-spline for each variable, values will be recycled eventually

ctrpoints array of control points

nk logical, parameter used internally see details on how to use it

Details

The function create an object of class bmop, that is, a list with components

- order vector of orders
- knots list, every element of the list is the vector of knots in one dimension, knots are ordered but can be repeted.
- · ctropoints An array of control points

If nk==FALSE (default method) the knots provided are sorted and the unique function is applied. Then the appropriate knots are computed, repeating the first and last knots many times as the order in the considered dimension, with this choice the bmop object represent a B-spline function regular up to the order-1 derivate in every dimension. If nk==TRUE the bmop object will be created without any check on the knots, use carefully this option as it could result in a wrong defined bmop object.

Value

An object of class bmop, a list with elements order, knots, ctrpoints,

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normalize.bmop	Normalize a bmop
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Description

Normalize a bmop object, makes it integrate to one.

Usage

```
normalize.bmop(object, ...)
```

Arguments

```
object a bmop object ... additional parameters
```

Value

a bmop object proportional to object, but such that integrates to one.

plot.bmop Plot of bmop object

Description

Plot of bmop object

Usage

```
## S3 method for class 'bmop'
plot(x, N = 1000, type = "1", contour = TRUE,
    persp = FALSE, file = NULL, MIN = 0, ...)
```

Arguments

X	bmop object
N	positive integer
type	graphical parameter, see par
contour	graphical parameter, see par
persp	logical
file	optional file name, where to save a pdf copy of the plot
MIN	parameter of evaluate.bmop
	graphical parameters as col, main,, see plot or filled.contour

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Details

For the 2-d persp (persp==TRUE) plot the rgl package is needed. In order to obtain a nicer result in the contour plot, try to supply a col or color.palette parameter, like in the example below (RColorBrewer package is needed).

Value

plot of 1-d or 2-d (contour and perspective) bmop, an empty plot and a warning message are returned if the bmop object has more than 2 dimensions.

See Also

```
points.bmop
```

Examples

```
## Not run:
bmop<-bmop_fit(data.frame(rnorm(100),rnorm(100)))
colFun<-
grDevices::colorRampPalette(RColorBrewer::brewer.pal(9,name="YlGnBu"))
plot(bmop,color.palette=colFun)
## End(Not run)</pre>
```

points.bmop

Plot points from bmop

Description

Plot points from bmop

Usage

```
## S3 method for class 'bmop'
points(x, N = 100, ...)
```

Arguments

x bmop objectN number of points to plot... graphical parameters see par

Details

As points, this functions provide a way to add the plot of a bmop to an existing plot.

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See Also

```
plot.bmop.
```

Examples

```
data<-rnorm(200)
bmopE<-bmop_fit(data)
bmopS<-search_bmop(data)
plot(bmopE)
points(bmopS,type="1",col="red")</pre>
```

print.bmop

Print bmop objects

Description

Print bmop objects

Usage

```
## S3 method for class 'bmop'
print(x, ...)
```

Arguments

x bmop object ... see print

put_evidence.bmop

Put evidence on a conditional bmop

Description

Instantiate evidence on a bmop conditional density.

```
put_evidence.bmop(object, evidence, evd.pos = NULL, MIN = 0,
    normalize = FALSE, ...)
```

Rbmop

Arguments

object a bmop object
evidence the value of evidence
evd.pos the position of evidence
MIN the MIN value as in bmopPar
normalize logical, if TRUE the final bmop object will be normalized (usually it is not needed since this function is applied to conditional densities)
... additional parameters

Value

a bmop object, the result of imposing some evidence

Rbmop: A package for handling and estimating densities and conditional densities with B-spline.

Description

The main functions of Rbmop package are the following:

- bmop_fit for estimation of density or conditional density.
- bmopPar function for changing the parameter of the package.
- compare.bmop and comparison_plot comparison functions.
- Moreover the package provide base functions as plot, print and conversion methods as . function.bmop.

Author(s)

Gherardo Varando <gherardo.varando@gmail.com>, Concha Bielza and Pedro Larranaga

Examples

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search_bmop

Greedy penalized log-likelihood search

Description

Approximation of a density $f(x_1, \ldots, x_n)$ or conditional density

Usage

```
search_bmop(data, conditional = F, k = Rbmop::bmopPar()$k,
    corrected = FALSE, knotsMethod = Rbmop::bmopPar()$knotsMethod, ...)
```

Arguments

data.frame, matrix or vector, the variables must be in the right order (the columns

of data)

conditional logical

k positive number or "BIC"

corrected logical

knotsMethod the method to use in knots generation

... additional parameters

Value

A bmop object, the approximations of f.

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Examples

```
data<-rnorm(100)
bmopS<-search_bmop(data=data)
plot(bmopS)</pre>
```

summary.bmop

Summary of a bmop object

Description

Summary of a bmop object

Usage

```
## S3 method for class 'bmop'
summary(object, ...)
```

Arguments

object bmop object

... compatibility with summary

Examples

```
data(trees)
bmop<-bmop_fit(data=trees$Height)
summary(bmop)</pre>
```

upper.bmop

Upper Limit of bmop

Description

Upper Limit of bmop

Usage

```
upper.bmop(object)
```

Arguments

object

a bmop object

Value

numeric value

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