

Simultaneous Localisation and Mapping (SLAM)

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Autonomous Mobile Robots

- The three key questions [Leonard and Durrant-Whyte 1991]
 - Where am I?
 - Where am I going?
 - How do I get there ?



- Know its environment => Mapping.
- Perceive and analyze the environment => e.g. vision, lidar.
- Find its position within the environment => Localization.
- Plan and execute the movement => Path Planning.







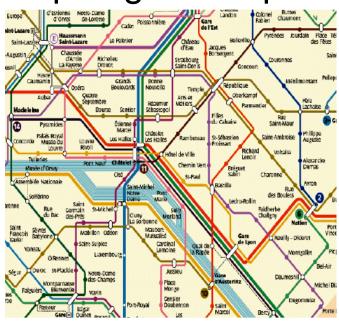
Robot Mapping and Localisation

Mapping – modelling the environment.

Geometric map



Topological map

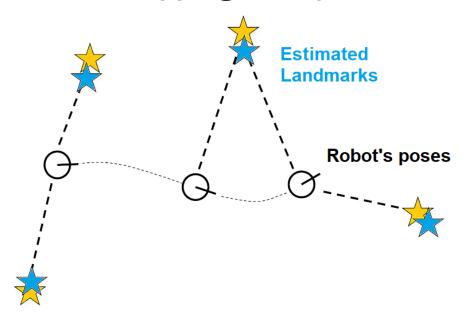


Localization: estimating the robot's location.

Courtesy of Wolfram Burgard

Robot Mapping and Localisation

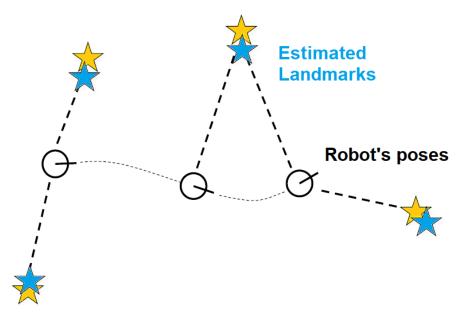
Mapping Example



- Robot knows its pose and sees landmarks.
- Robot estimates landmarks on the map
 - to create / update / extend the map.

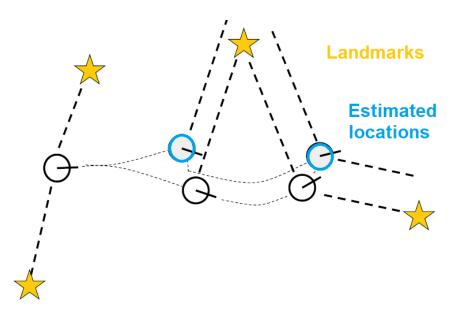
Robot Mapping and Localisation

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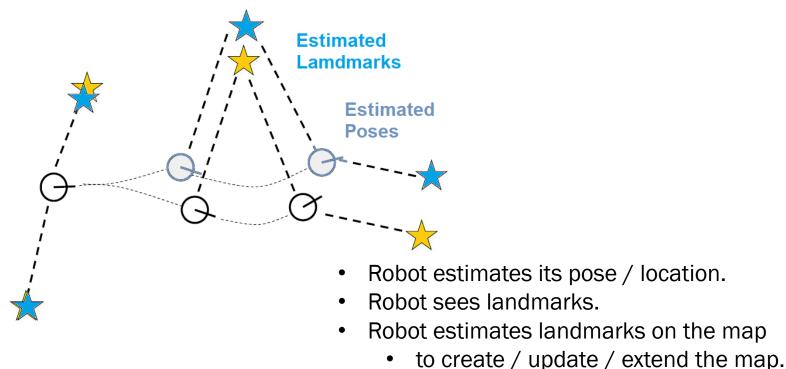
Localisation Example



- Robot knows landmarks on map and sees landmarks.
- Robot estimates its pose / location.

Simultaneous Localisation and Mapping (SLAM)

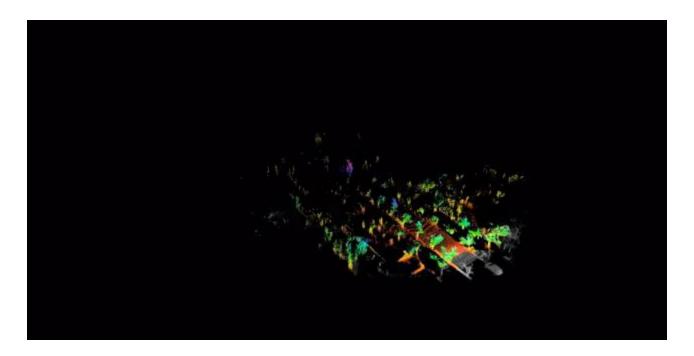
- Estimate the robot's poses /locations and the landmarks at the same time.
 - building a map and locating the robot simultaneously.



Courtesy of Cyrill Stachniss, Robot Mapping, http://ais.informatik.uni-freiburg.de/teaching/ws12/mapping/pdf/slam01-intro.pdf, 2019

Simultaneous Localisation and Mapping (SLAM)

- Estimate the robot's poses /locations and the landmarks at the same time.
 - building a map and locating the robot simultaneously.

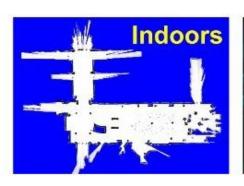


Courtesy https://www.youtube.com/watch?v=1pt3wuQMRDk

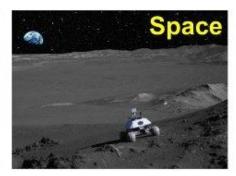


SLAM

- SLAM is considered as a fundamental problem for autonomous mobile robots.
- It is basis for most navigation systems.
 - building a map of an unknown environment by a mobile robot while at the same time navigating the environment using the map.
- Wide range of applications.
- Highly relevant for all kinds of applications that involve moving robots.









vacuum cleaner

reef monitoring

terrain mapping for localisation

exploration of mines

Courtesy of H. Durrant-Whyte, NASA, S. Thrun



SLAM in AR/VR

- Project Tango (Google)
- AR/ VR Glasses
 - Hololens (Microsoft)
 - Oculus Rift (Facebook)

- Apple (metaio)
- Oculus (surreal Vision) ..







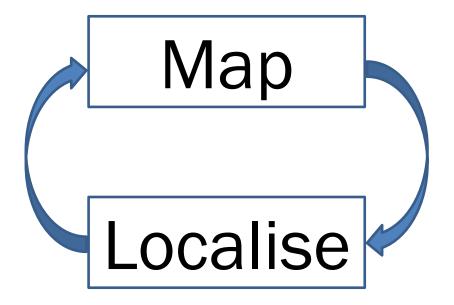






The SLAM Problem

- SLAM is a chicken-or-egg problem.
 - Map is needed for localisation.
 - Pose estimate is necessary for mapping.





The SLAM Problem

GIVEN

The robot's controls

$$u_{1:T} = \{u_1, u_2, \dots, u_T\}$$

Observations

$$z_{1:T} = \{z_1, z_2, \dots, z_T\}$$

Note: The controls and observations are both noisy.

ESTIMATE

Path of the robot => sequence of poses and locations,

$$x_{0:T} = \{x_0, x_1, x_2, \dots, x_T\}$$

Map of the environment

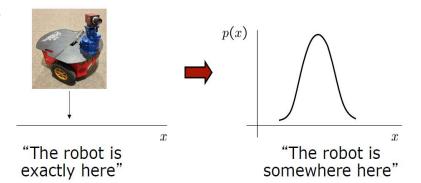
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Probabilistic Approaches

 Use the probability theory to explicitly represent the uncertainty.



In Probabilistic Terms

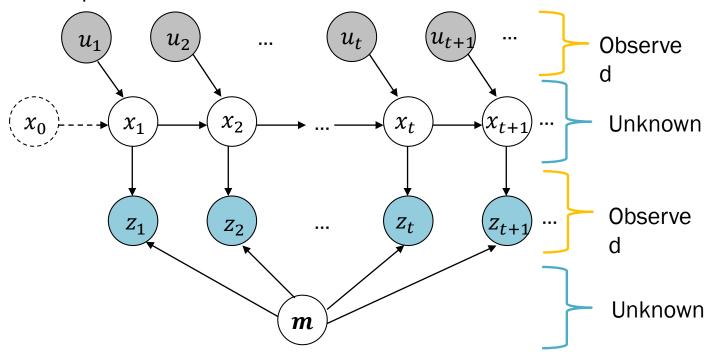
Estimate the robot's path and the map

$$p(x_{0:T}, m|z_{1:T}, u_{1:T})$$
distribution path map given observations controls



Graphical Model

Markov assumption



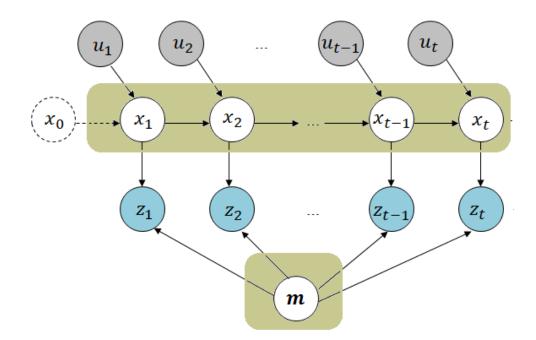
- SLAM as a state estimation Problem
 - Estimate the state of a system given observations and controls. i.e. p(x|z,u)

State transition: $p(x_t|x_{t-1}, u_t)$ Observation function: $p(z_t|x_t)$



Full SLAM

• Estimates the entire path and map $p(x_{0:T}, m|z_{1:T}, u_{1:T})$





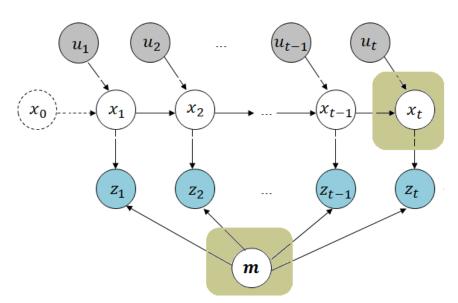
Online SLAM

Estimates only the most recent pose and map.

$$p(\mathbf{x_t}, m | \mathbf{z_{1:t}}, u_{1:t}) = \iint \dots \int p(\mathbf{x_{1:t}}, m | \mathbf{z_{1:t}}, u_{1:t}) dx_1 dx_2 \dots dt_{t-1}$$

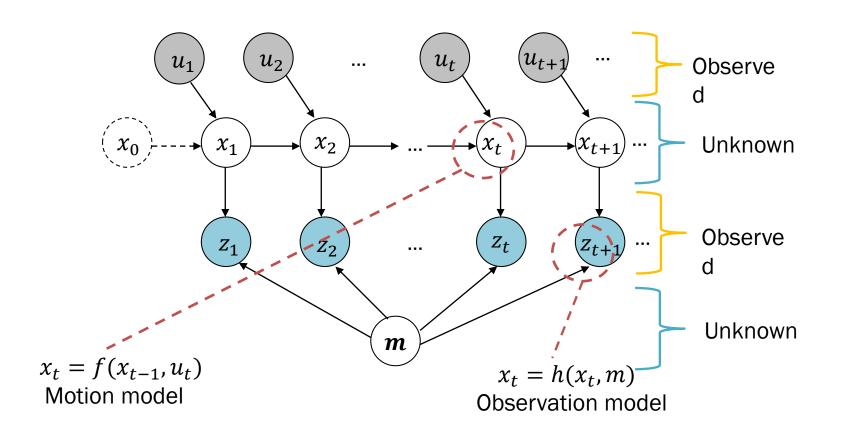
Integrations typically done recursively, one at a

time.





Motion and Observation Model

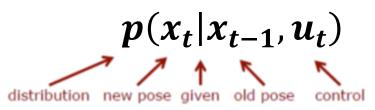


- SLAM as a state estimation Problem
 - Estimate the state of a system given observations and controls. i.e. p(x|z,u)

Motion and Observation Model

Motion Model

describes the relative motion of the robot.



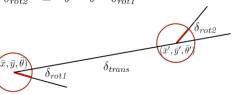
Odometry Model

- Robot moves from $(\bar{x}, \bar{y}, \bar{\theta})$ to $(\bar{x}', \bar{y}', \bar{\theta}')$
- Odometry information $u = (\delta_{rot1}, \delta_{trans}, \delta_{rot2})$

$$\delta_{trans} = \sqrt{(\bar{x}' - \bar{x})^2 + (\bar{y}' - \bar{y})^2}$$

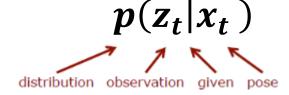
$$\delta_{rot1} = \operatorname{atan2}(\bar{y}' - \bar{y}, \bar{x}' - \bar{x}) - \bar{\theta}$$

$$\delta_{rot2} = \bar{\theta}' - \bar{\theta} - \delta_{rot1}$$



Observation Model

 The observation or sensor model relates measurements with the robot's pose.



Model for Laser Scanners

Scan z consists of K measurements.

$$z_t = \{z_t^1, \dots, z_t^k\}$$

 Individual measurements are independent given the robot position

$$p(z_t \mid x_t, m) = \prod_{i=1}^k p(z_t^i \mid x_t, m)$$

Courtesy of Cyrill Stachniss, Robot Mapping, http://ais.informatik.uni-freiburg.de/teaching/ws12/mapping/pdf/slam02-bayes-filter-short.pdf, 2019

Motion and Observation Model

- Sequentially estimate p(x|z,u) and update the map
- Using Bayer's filter

$$bel(x_t) = p(x_t|z_{1:t}, u_{1:t}) =$$
 belief

Prediction Step

$$\overline{bel}(x_t) = \int \underline{p(x_t|u_t, x_{t-1})} bel(x_{t-1}) dx_{t-1}$$
motion model

Correction Step

$$bel(x_t) = \eta \underline{p}(\underline{z_t}|\underline{x_t}) \overline{bel}(x_{t-1})$$
observation model

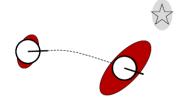


SLAM

- Kalman Filter => Bayer's Filter
 - Gaussian distributions and noise
 - Linear motion and observation model.
- Most realistic problems in robotics involve nonlinear functions.
 - The non-linear functions lead to non Gaussian distributions.
- Non-Gaussian Distributions
 - Local linearization by first order Taylor series expansion as in Extended Kalman Filter (EKF).
 - EKF SLAM is the first SLAM solution.
- Non parametric and Arbitrary models
 - Particle Filter based localisation (Monte-Carlo localization)
 - Particle Filters => non-parametric, recursive Bayes filters.

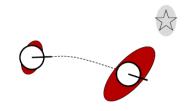


1. State prediction (e.g. odometry)



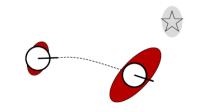


- 1. State prediction (e.g. odometry)
- 2. Measurement prediction





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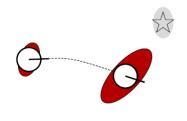


3. Measurement

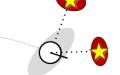




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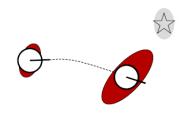


- 4. Data association
 - Associates predicted measurements with observation

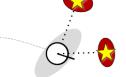




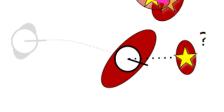
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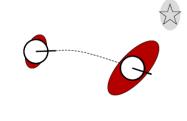


5. Update





- 1. State prediction (e.g. odometry)
- 2. Measurement prediction



- 3. Measurement
- 4. Data association
 - Associates predicted measurements with observation



- 5. Update
- 6. Integration of new landmarks



Courtesy of Cyrill Stachniss, EKF SLAM, http://ais.informatik.uni-freiburg.de/teaching/ws12/mapping/pdf/slam04-ekf-slam.p



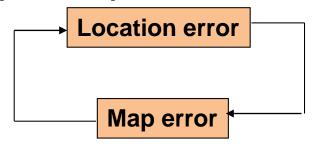
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Suggested Readings

- Thrun et al. "Probabilistic Robotics"
- Course: Introduction to Mobile Robotics SS 2019
- Siciliano et al. "Springer Handbook of Robotics"

Why is SLAM a hard problem?

- Robot path and map are both unknown.
- Errors in map and pose estimates correlate.



- The mapping between observations and the map is unknown.
- Picking wrong data associations can lead to divergence.



SLAM: Loop Closure

Recognizing an already mapped area.

 By revisiting already mapped areas, uncertainties in robot and landmark estimates can be reduced.

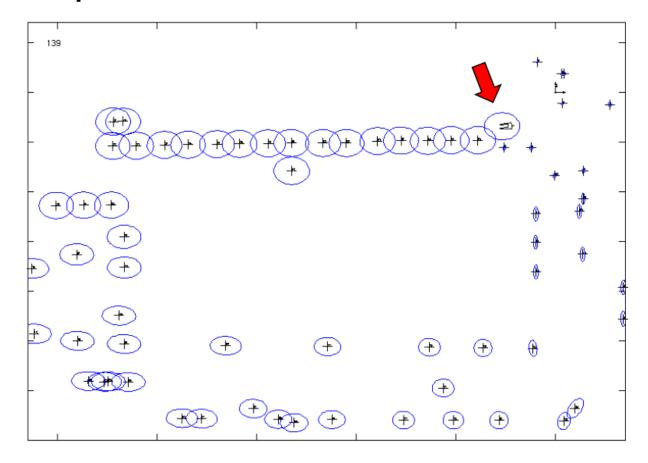
 This can be exploited when exploring an environment for the sake of better (e.g. more accurate) maps.

Courtesy of Cyrill Stachniss, EKF SLAM, http://ais.informatik.uni-freiburg.de/teaching/ws12/mapping/pdf/slam04-ekf-slam.pdf



SLAM: Loop Closure

Before loop closure

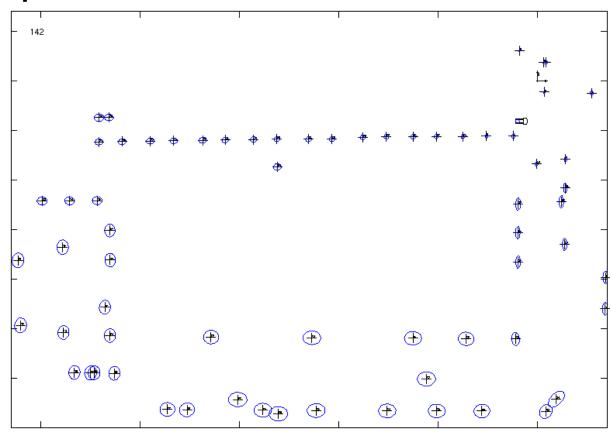


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SLAM: Loop Closure

After loop closure

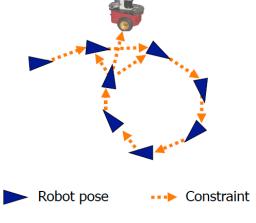


Courtesy of Cyrill Stachniss, EKF SLAM, http://ais.informatik.uni-freiburg.de/teaching/ws12/mapping/pdf/slam04-ekf-slam.pdf



Graph-Based SLAM

- Use a graph to represent the problem.
- Every node in the graph corresponds to a pose of the robot during mapping.
- Every edge between two nodes corresponds to a spatial constraint between them.
- Goal: Build the graph and find a node configuration that minimize the error introduced by the constraints.
 - Least squares approach to SLAM.

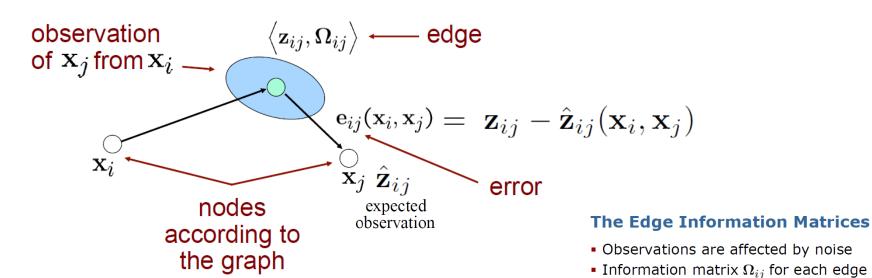


Courtesy of Wolfram Burgard, Graph-Based SLAM, http://ais.informatik.uni-freiburg.de/teaching/ss19/robotics/slides/16-graph-slam.pdf, 2019



Pose Graph

The problem can be described by a graph.



Goal

$$x^* = \underset{x}{\operatorname{argmin}} \sum_{ij} e_{ij}^T \Omega_{ij} e_{ij}$$

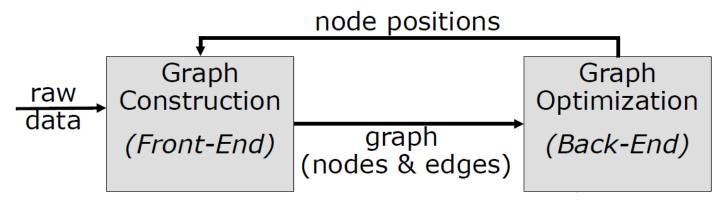
Courtesy of Wolfram Burgard, Graph-Based SLAM, http://ais.informatik.uni-freiburg.de/teaching/ss19/robotics/slides/16-graph-slam.pdf, 2019

to encode its uncertainty

• The "bigger" Ω_{ij} , the more the edge "matters" in the optimization



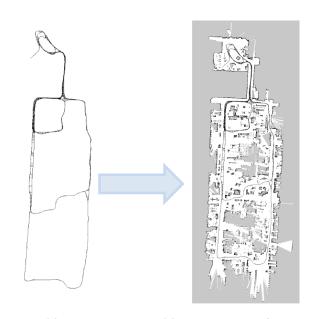
The overall SLAM system



- Once we have the graph, we determine the most likely map by correcting the nodes.
- Then, we can render a map based on the known poses.

Suggested Reading:

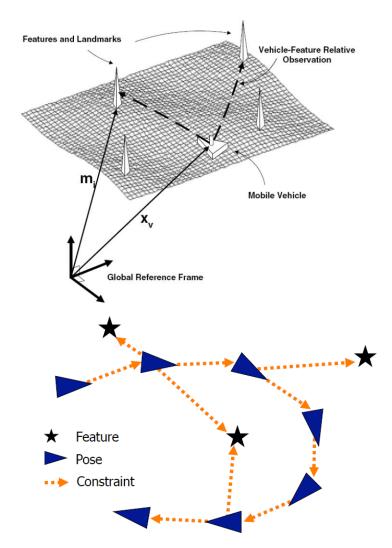
Grisetti, Kümmerle, Stachniss, Burgard: "A Tutorial on Graph-based SLAM", 2010



Courtesy of Wolfram Burgard, Graph-Based SLAM, http://ais.informatik.uni-freiburg.de/teaching/ss19/robotics/slides/16-graph-slam.pdf, 2019

Graph-Based SLAM with Landmarks

- Nodes can represent:
 - Robot poses.
 - Landmark locations.
- Edges can represent:
 - Landmark observations.
 - Odometry measurements.
- The minimization optimizes the landmark locations and robot poses.



Courtesy of Cyrill Stachniss, Graph-Based SLAM with Landmarks, http://ais.informatik.uni-freiburg.de/teaching/ws12/mapping/pdf/slam17-ls-landmarks.pdf

Graph-Based SLAM with Landmarks

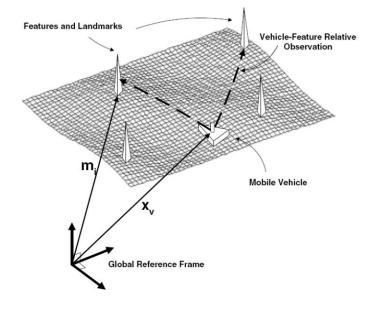
Landmark is a (x, y)-point in the world Relative observation in (x, y)

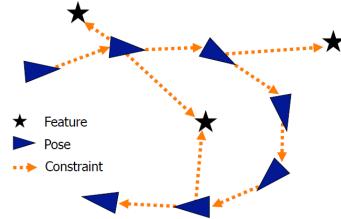
Expected observation (x-y sensor)

$$\hat{\mathbf{z}}_{ij}(\mathbf{x}_i, \mathbf{x}_j) = \mathbf{R}_i^T(\mathbf{x}_j - \mathbf{t}_i)$$
robot landmark robot translation



$$\mathbf{e}_{ij}(\mathbf{x}_i, \mathbf{x}_j) = \hat{\mathbf{z}}_{ij} - \mathbf{z}_{ij}$$
$$= \mathbf{R}_i^T(\mathbf{x}_j - \mathbf{t}_i) - \mathbf{z}_{ij}$$



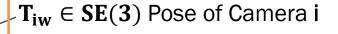


Courtesy of Cyrill Stachniss, Graph-Based SLAM with Landmarks, http://ais.informatik.uni-freiburg.de/teaching/ws12/mapping/pdf/slam17-ls-landmarks.pdf



Feature-Based Visual SLAM





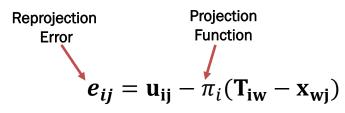
 $\mathbf{x}_{\mathrm{wj}} \in \mathbb{R}^3$ Coordinates of Point **j**

Measurements

$$\mathbf{u_{ij}} = \begin{bmatrix} u_{ij} \\ v_{ij} \end{bmatrix}$$
 Observation of Point **j** from camera **i**

$$T_{iw} = \begin{cases} R_{iw} \in SO(3) & \text{Rotation Matrix} \\ t_{iw} \in \mathbb{R}^3 & \text{Translation Vector} \end{cases}$$

 $x_{ij} = R_{iw}x_{wj} + t_{iw}$ Coordinates of point j wr. t. camera i



Courtesy of Juan D. Tardos, Feature-Based Visual SLAM, http://www.dis.uniroma1.it/~labrococo/tutorial_icra_2016/icra16_slam_tutorial_tardos.pdf

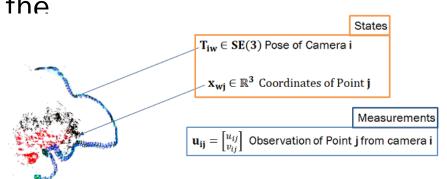


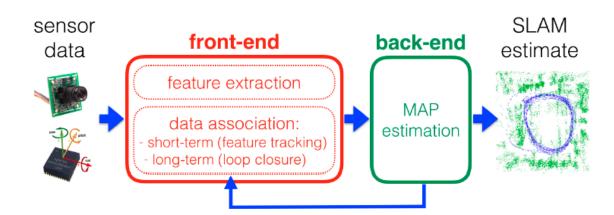
Feature-Based Visual SLAM

Find the state values minimizing the reprojection error.

$$e_{ij} = \mathbf{u_{ij}} - \pi_i (\mathbf{T_{iw}} - \mathbf{x_{wj}})$$

By Bundle Adjustment





Courtesy of Juan D. Tardos, Feature-Based Visual SLAM, http://www.dis.uniroma1.it/~labrococo/tutorial_icra_2016/icra16_slam_tutorial_tardos.pdf



Data Association (DA)

- Data association is the process of associating uncertain measurements to known tracks.
 - Does the current observation belong to a known landmark or a new landmark needs to be added?
- Why is it difficult?
 - complicated by sensor noise, dynamics, uncertainty in robot motion, static world assumption.
 - correct DA essential for getting correct estimates of landmarks as well as robot motion.

Lowry, Stephanie, et al. "Visual place recognition: A survey." IEEE Transactions on Robotics 32.1 (2016): 1-19



DA in Modern Visual SLAM

- Visual Landmarks
 - Features
 - Corners => Harris, FAST, ORB
 - Blobs like SIFT, SURF
 - Line segment => LSD, ED
 - Feature Descriptors like HoG, DoG, KAZE, BRIEF
- The aim is to track the patch over time
 - Assumption: descriptors vary very little between frames.
 - The scene is static, occlusions are limited, no rapid motion.



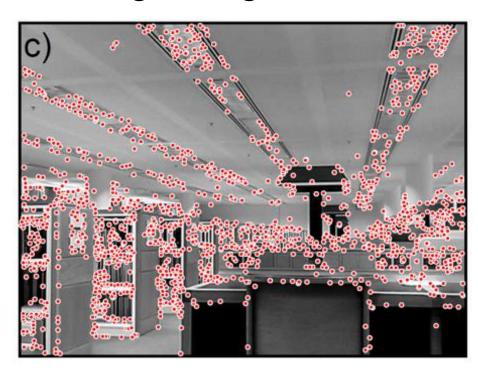
 Task: Find matches for a reference image in current image.

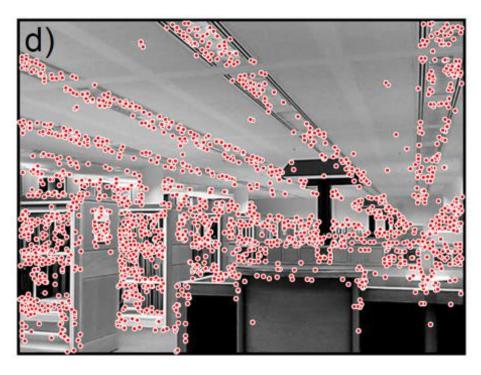






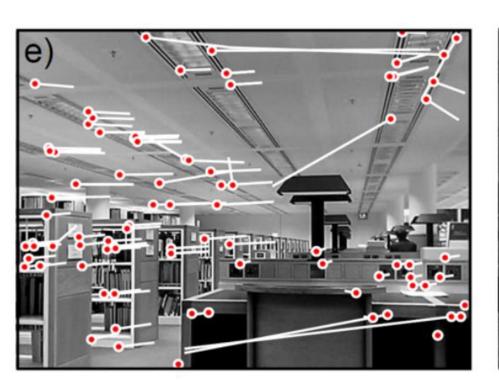
- Find features
 - e.g. using a corner detection algorithm.

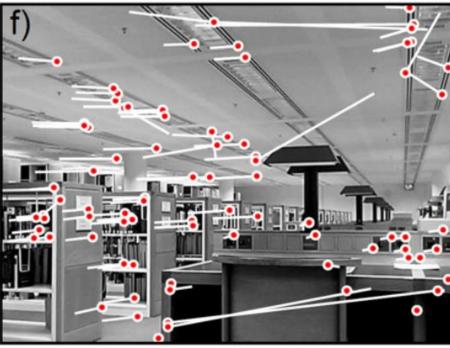






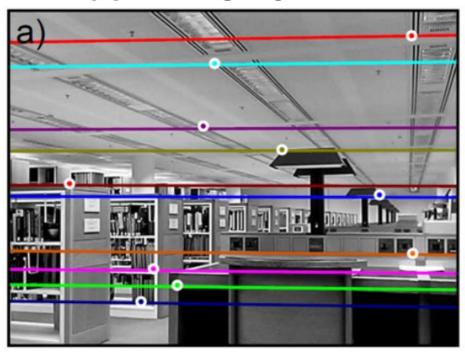
Match features.

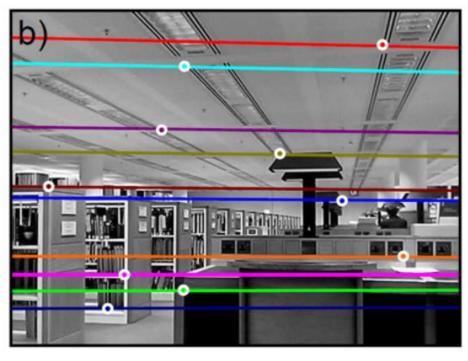






- Remove Outliers
 - Fit fundamental matrix using robust algorithm such as RANSAC

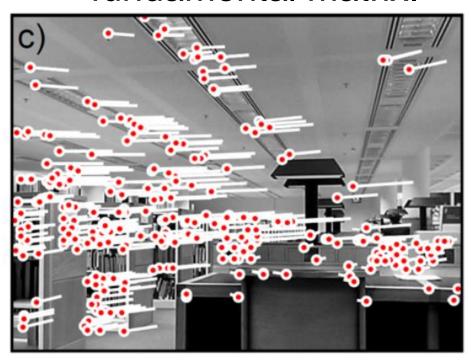


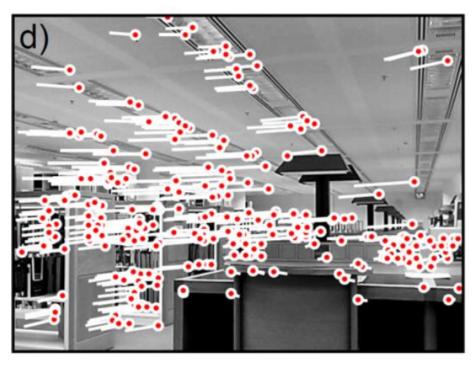


Courtesy of Simon Lucey, http://16623.courses.cs.cmu.edu/slides/Lecture_18.pdf



- Keep Inliers
 - Find matching points that agree with the fundamental matrix.





Courtesy of Simon Lucey, http://16623.courses.cs.cmu.edu/slides/Lecture_18.pdf



Extract essential matrix from fundamental matrix.

Extract rotation R and translation t from essential matrix.

Reconstruct the 3D positions x of points.

$$\lambda \tilde{\mathbf{x}} = R\mathbf{x} + \mathbf{t}$$



Relocation and Loop Closing

- Relocation problem:
 - During SLAM tracking can be lost: occlusions, low texture, quick motions, ...
 - Re-acquire camera pose and continue.



- SLAM is working, and we come back to a previously mapped area.
 - Loop detection: to avoid map duplication.
 - Loop correction: to compensate the accumulated drift => reduces overall uncertainty.
- In both cases we need a place recognition technique.



(a) Aerial view of the courtyard.



b) Before loop closure.



(c) After loop closure.

Courtesy of Juan D. Tardos, Feature-Based Visual SLAM, http://www.dis.uniroma1.it/~labrococo/tutorial_icra_2016/icra16_slam_tutorial_tardos.pdf



Why is loop closing difficult?

- Similar place can look different over time (day/night, weather, construction, etc).
- Perceptual aliasing: Different places can "look" similar to the sensor.





Why is loop closing difficult?

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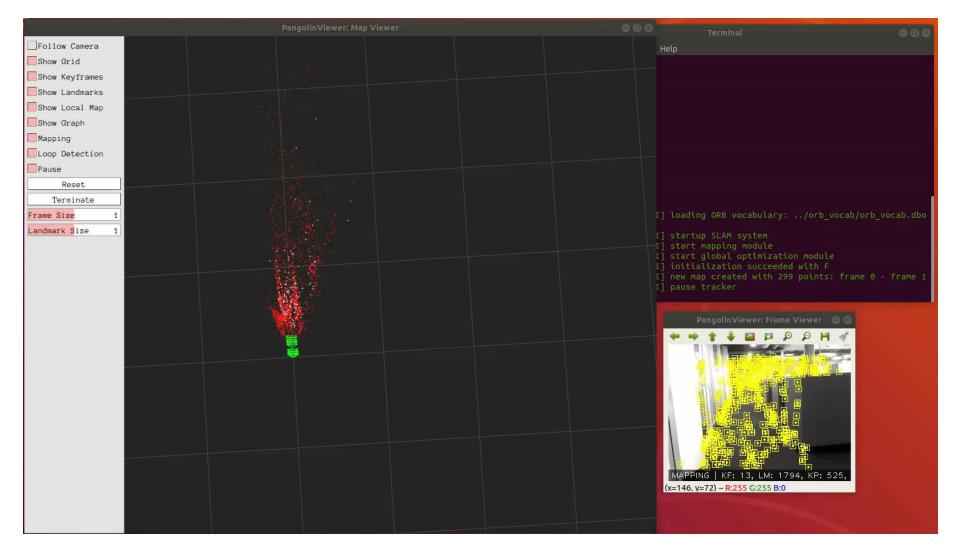
Loop Closing

 Visual similarity can be computed using global image descriptors (GIST descriptors) or local image descriptors (e.g., ORB features).

- Image retrieval is the problem of finding the most similar image of a template image in a database of billion images (image retrieval).
- This can be solved efficiently with Bag of Words.



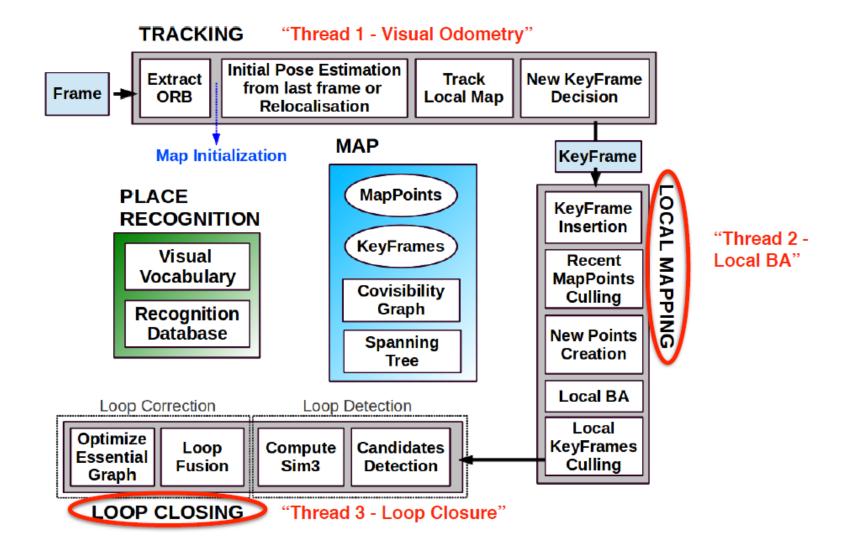
Loop Closing



ORB-SLAM: Feature-Based SLAM

- Use the same features for:
 - Tracking
 - Mapping
 - Loop closing
 - Relocation
- ORB: FAST corner+ Oriented Rotated Brief descriptor
 - Binary descriptor
 - Very fast to compute and compare
- Real-time, large scale operation
- ORB-SLAM => monocular
- ORB-SLAM2 => for Monocular, Stereo, and RGB-D
- Raul Mur-Artal, Jose M. M. Montiel and Juan D. Tard6s, ORB-SLAM: A Versatile and Accurate Monocular SLAM System, IEEE Trans. on Robotics 31(5): 1147-1163, Oct 2015
- R. Mur-Artal and J. D. Tardós, "ORB-SLAM2: An Open-Source SLAM System for Monocular, Stereo, and RGB-D Cameras," in *IEEE Transactions on Robotics*, vol. 33, no. 5, pp. 1255-1262, Oct. 2017.
- https://webdiis.unizar.es/~raulmur/orbslam/

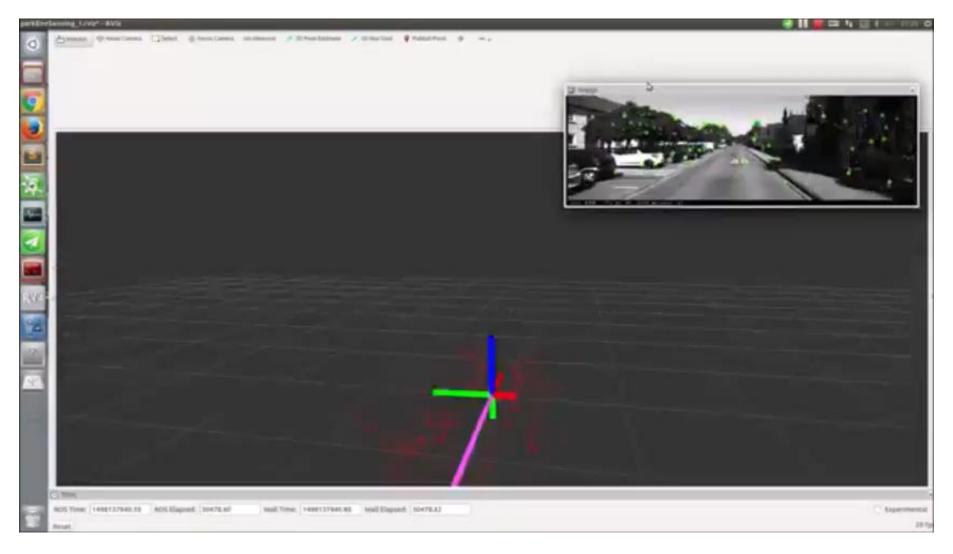
ORB-SLAM: Real-Time Monocular SLAM



Courtesy of Juan D. Tardos, Feature-Based Visual SLAM, http://www.dis.uniroma1.it/~labrococo/tutorial_icra_2016/icra16_slam_tutorial_tardos.pdf



ORB SLAM demo



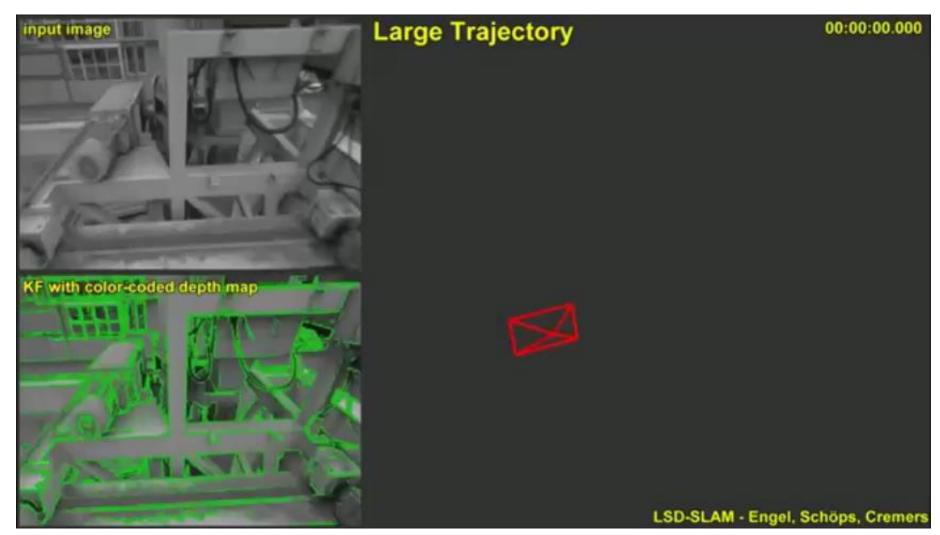
Feature-Based vs Direct SLAM

Feature-Based Direct Input Input **Images** Images Extract & Match Features (SIFT / SURF / ...) abstract image to feature observations keep full images (no abstraction) Track: Track: min. photometric error min. reprojection error (intensity differences) (point distances) est. feature-parameters est. per-pixel depth (3D points / normals) (semi-dense depth map

https://medium.com/@j.zijlmans/lsd-slam-vs-orb-slam2-a-literature-based-comparison-20732df431d



Direct SLAM

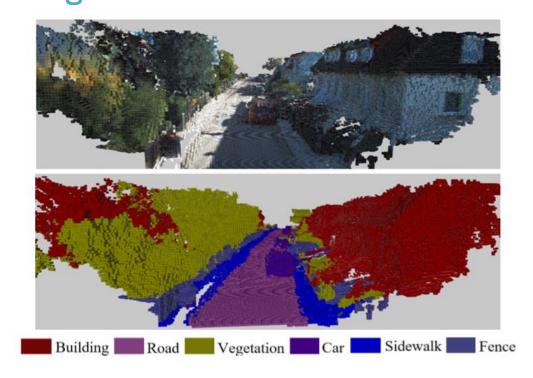


https://vision.in.tum.de/research/vslam/lsdslam



Semantic Mapping

"The goal of semantic mapping is to create maps that include meanings, both to robots and human. Maps that include semantic information make it easier for robots and human to communicate and reason about goals."

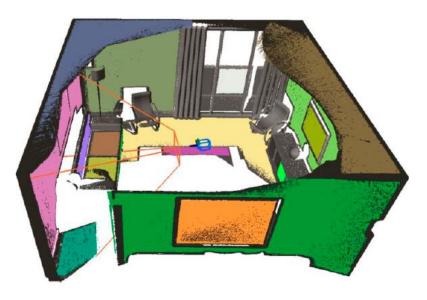


Trevor et al. "Tables, Counters, and Shelves: Semantic Mapping of Surfaces in 3D", IROS 2010



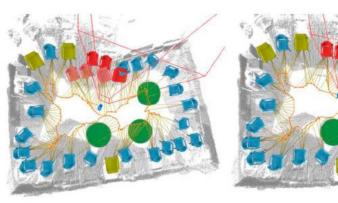
Map Optimisation

 Objects (Semantics) often provide extra constraints that can be used to optimise the map.



Every detected plane imposes constraints on the 3D points lying on the plane. Instead of saying that the 3D points are **independent**, they have to satisfy the plane equation.

Dense Planar SLAM (Salas-Moreno 2014)



Before loop closure

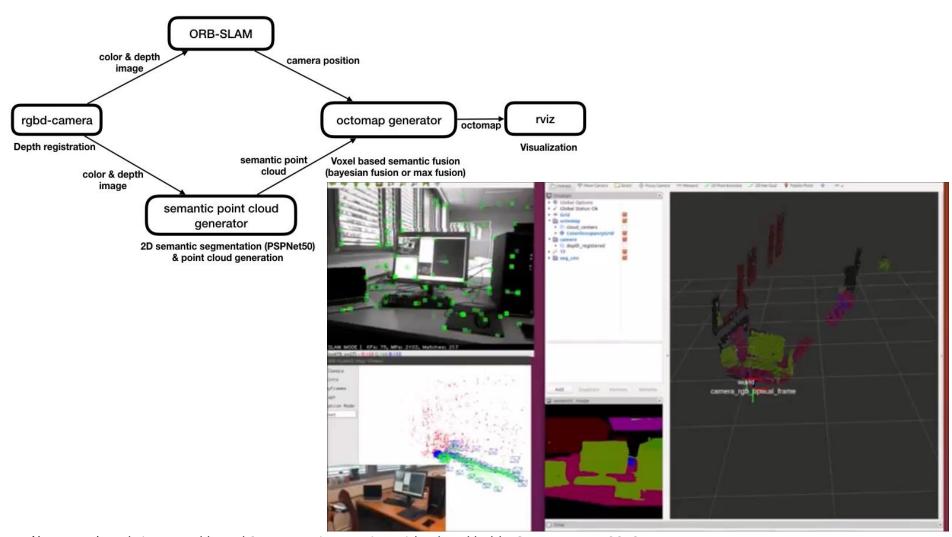
After loop closure

Instead of having a pose graph with edges containing relative camera transformations, have a pose graph with edges containing relative camera and relative object transformations.

SLAM++ (Salas-Moreno et al. 2013)



Semantic SLAM

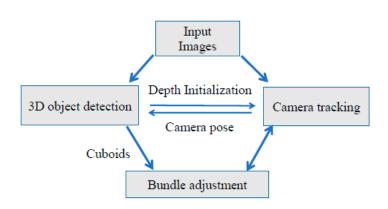


Xuan et al Real-time voxel based 3D semantic mapping with a hand held RGB-D camera, 2018

https://github.com/floatlazer/semantic_slam



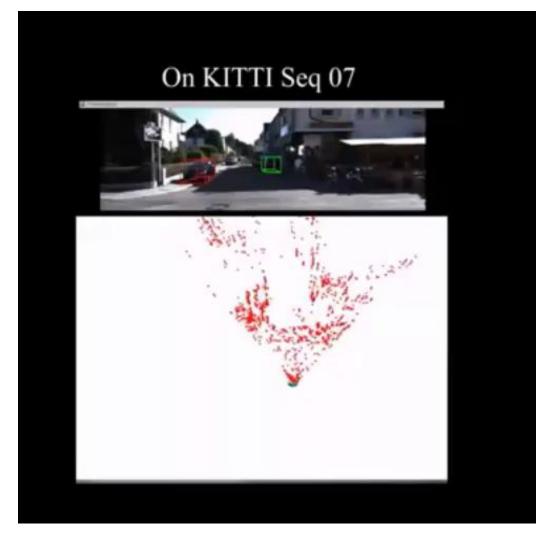
Object SLAM



Single view object detection provides cuboid landmark and depth initialization for SLAM while SLAM can estimate camera pose for more accurate object detection. Object detection and SLAM complements each other.

Yang S, Scherer S. CubeSLAM: Monocular 3-D Object SLAM. IEEE Transactions on Robotics. 2019 May 7.

https://github.com/shichaoy/cube_slam





Open Issues in SLAM

- Dynamic environments.
- Systematically changing environments.
- Seasonal changes.
- Online solutions.
- Life-long operation.
- Resource-constraint systems.
- Failure recovery/zero user intervention.
- Exploiting prior knowledge.
- Robots sharing maps.

 $\underline{\text{http://ais.informatik.uni-freiburg.de/teaching/ws12/mapping/pdf/slam21-summary.pdf}}$



Sensor-Related Issues

- Efficient data association.
 - Deep learning can help.

- Sensor-related limitations such as:
 - Poorly structured scenes.
 - Missing light for vision.

Monocular SLAM (in large environments).



Resources/ References

- H. F. Durrant-Whyte and T. Bailey. Simultaneous Localisation and Mapping (SLAM): Part I. IEEE Robotics and Automation Magazine, 13(2):99–110, 2006.
- T. Bailey and H. F. Durrant-Whyte. Simultaneous Localisation and Mapping (SLAM): Part II. Robotics and Autonomous Systems (RAS), 13(3):108–117, 2006.
- J. Aulinas, Y. Petillot, J. Salvi, and X. Llado. The SLAM Problem: A ´Survey. In Proceedings of the International Conference of the Catalan Association for Artificial Intelligence, pages 363–371. IOS Press, 2008
- Taketomi T, Uchiyama H, Ikeda S. Visual SLAM algorithms: a survey from 2010 to 2016. IPSJ Transactions on Computer Vision and Applications. 2017 Dec 1;9(1):16.
- Younes G, Asmar D, Shammas E, Zelek J. Keyframe-based monocular SLAM: design, survey, and future directions. Robotics and Autonomous Systems. 2017 Dec 1;98:67-88.
- Cadena C, Carlone L, Carrillo H, Latif Y, Scaramuzza D, Neira J, Reid I, Leonard JJ. Past, present, and future of simultaneous localization and mapping: Toward the robust-perception age. IEEE Transactions on robotics. 2016 Dec;32(6):1309-32.



Resources/ References

- https://github.com/ckddls1321/SLAM_Resources
- https://openslam-org.github.io/
- https://pythonrobotics.readthedocs.io/en/latest/
- https://www.mrpt.org/tutorials/slam-algorithms/slam-simultaneous-localization-and-mapping-for-beginners-the-basics/
- https://github.com/xdspacelab/openvslam
- http://www.semanticslam.ai/
- Scene Understanding Challenge
 - https://nikosuenderhauf.github.io/roboticvisionchallenges/scene-understanding
 - https://www.youtube.com/watch?v=xOGzJ6QVVYU
- ROS
 - https://www.ros.org/
- Robot Academy (open online robotics education resource)
 - https://robotacademy.net.au/



Thank you

























DEMO: SLAM Map Building with TurtleBot

http://wiki.ros.org/Robots/TurtleBot

- http://wiki.ros.org/turtlebot_navigation
- Build a map with SLAM
 - You will have live demo



Autonomously navigate in a known map