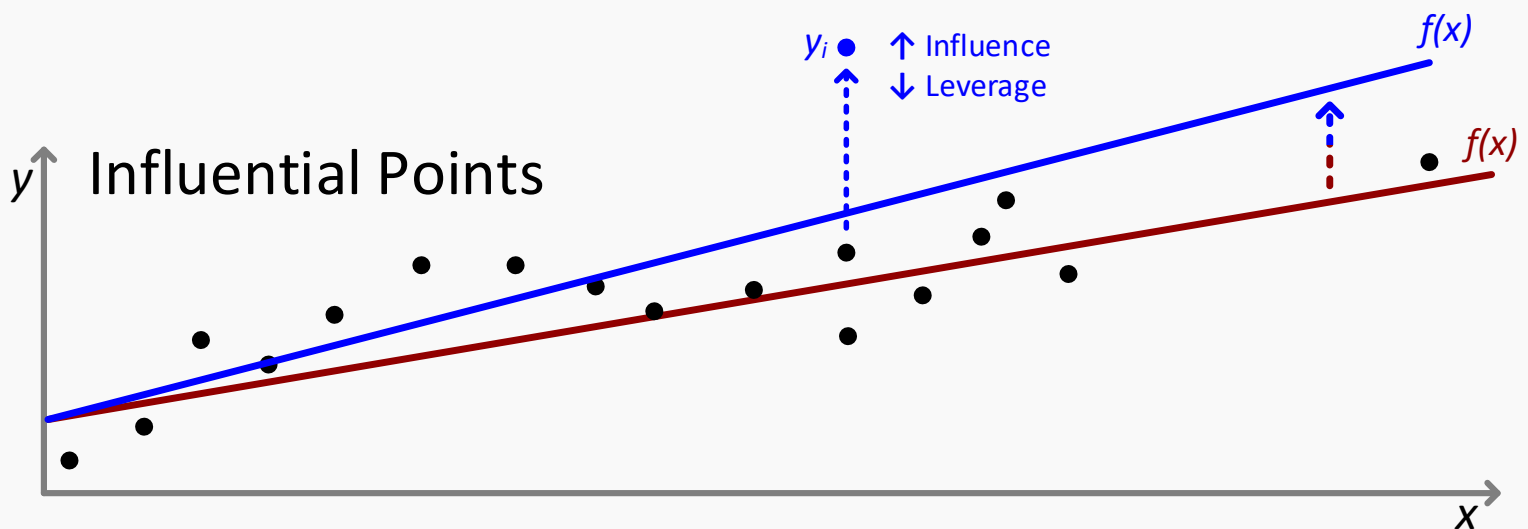
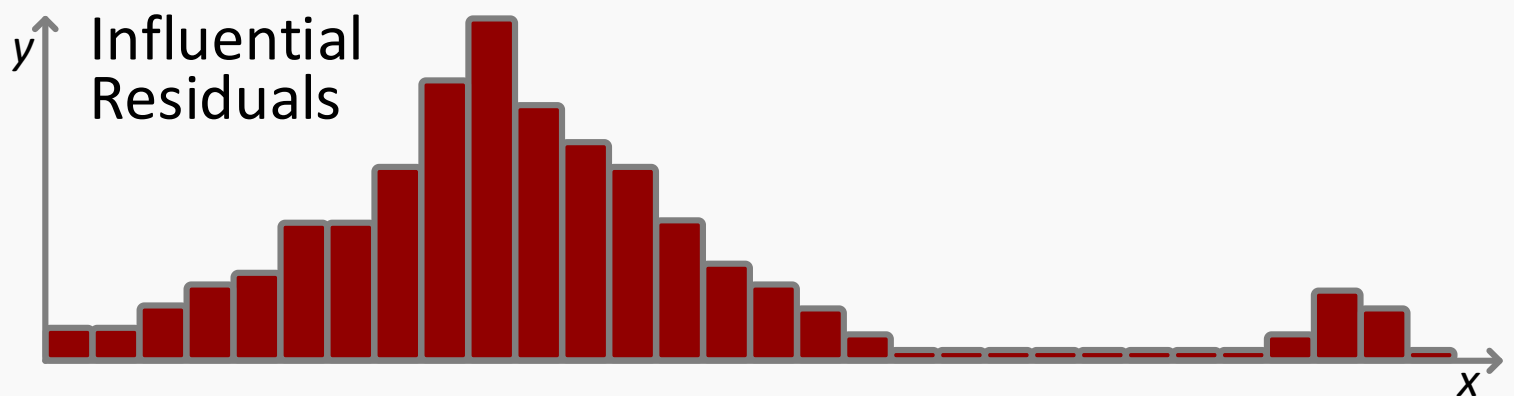


## influential $\approx$ points

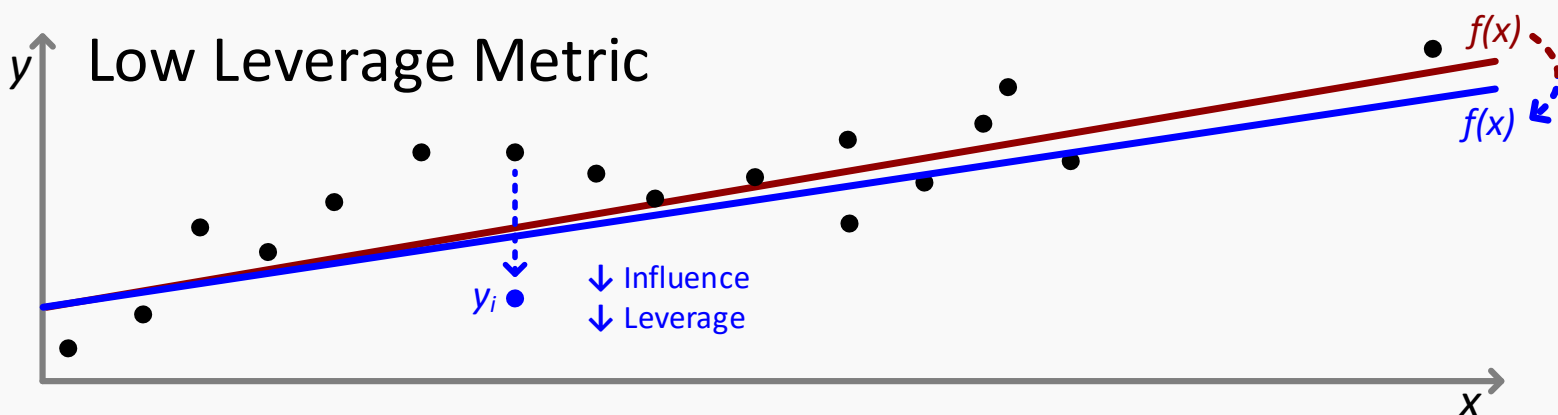
An **Influential Point** changes a model's predicted values significantly when omitted or altered:



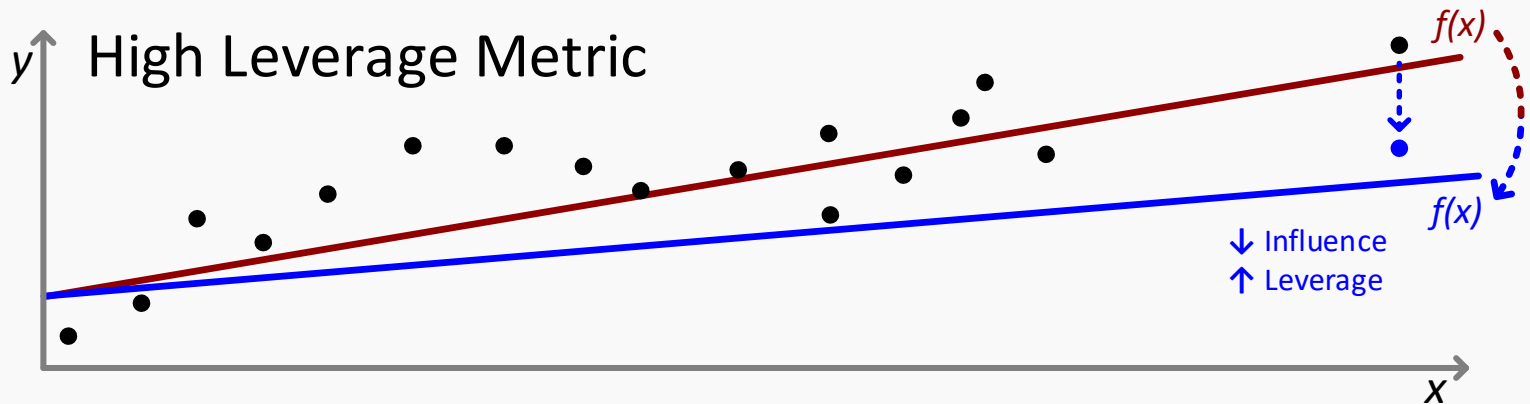
Equally, **Influential Points** significantly impact a plot of residuals seen in the histogram below:



Alternatively, **Leverage** is where a point can be altered in multiple ways without having a significant impact on the model's predictions or the plotted residual distribution as seen in the illustration below:



However, depending on the location of the point in question, **Leverage** can be substantially increased. Any alteration of such a point will cause the model to alter in a more significant nature seen below:



Formally, if point  $x_i$  is moved, and  $f(x_i)$  moves proportionally, the proportionality constant is referred to as the leverage of point  $i$ .

Leverage depends on  $x_i$  but does not depend on  $y_i$ . Leverage depends on how far away  $x_i$  is from the mean of the points  $x_i$ 's.

It is important to note the **Influential Points** do not necessarily have a high amount of **Leverage**. Alternatively, High **Leverage** points are not necessarily **Influential Points**.

Ultimately, the **Leverage** of point  $x_i$  measures the impact of  $x_i$  on  $f(x_i)$ .

Investigating the nature of outliers typically involves asking questions such as:

- Is the data correct and represented as such?
- Is the model complete and performing sufficiently?