

KNN Formalization (For binary class & 2 features)

- Input: $\vec{x} \in \mathcal{X}$ where $\vec{x} \in \mathbb{R}^2$. Thus \vec{x} has 2 features x_1, x_2 .
- Output: $\vec{y} \in \mathcal{Y}$ where $\vec{y} \in \{0, 1\} = \mathbb{R}$ \vec{y} is 0 or 1.
- Unknown Ground truth function: $f: \mathcal{X} \rightarrow \mathcal{Y}$ where $\vec{x} \mapsto \vec{y}$
- Data: $\mathcal{D} = \{(\vec{x}^{(1)}, \vec{y}^{(1)}), (\vec{x}^{(2)}, \vec{y}^{(2)}) \dots (\vec{x}^{(m)}, \vec{y}^{(m)})\}$
- Hypothesis set: $\mathcal{H} = \{h_1, h_2, \dots, h_m\}$ if and only if our KNN has a fixed distance metric d and dataset.
- Hypothesis function: $h \in \mathcal{H}$ i.e. any one in \mathcal{H} .
- Learning Algorithm & best hypothesis function.

From \mathcal{H} , perform our learning A on \mathcal{D} & find best $h \in \mathcal{H}$,
call the best h to be g .

Now our h should take the form of
 $h(x; \theta)$ where $\theta = k$ and

best is based on
your evaluating
metric.

★ Then the decision boundary is the set of $\vec{x} = (x_1, x_2)$
such that $h(\vec{x}; \theta) = ???$ not sure.

see Voronoi diagram