

Topology, Munkres

Chapter 4

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Exercise Set 1

Problem 1. 1. A G_δ set in a space X is a set A that equals a countable intersection of open sets of X . Show that in a first-countable T_1 space, every one-point set is a G_δ set.

2. There is a familiar space in which every one-point set is a G_δ set, which nevertheless does not satisfy the first countability axiom. What is it?

The terminology here comes from the German. The “ G ” stands for “Gebiet,” which means “open set,” and the “ δ ” for “Durchschnitt,” which means “intersection.”

Solution :