

Artificial Intelligence

Lecturer 5 - Advanced search methods

School of Information and Communication Technology - HUST

Outline

- Memory-bounded heuristic search
- Hill-climbing search
- Simulated annealing search



Memory-bounded heuristic search

- Some solutions to A* space problems (maintain completeness and optimality)
 - Iterative-deepening A* (IDA*)
 - Here cutoff information is the f-cost (g+h) instead of depth
 - Recursive best-first search(RBFS)
 - Recursive algorithm that attempts to mimic standard best-first search with linear space.
 - (simple) Memory-bounded A* ((S)MA*)
 - Drop the worst-leaf node when memory is full

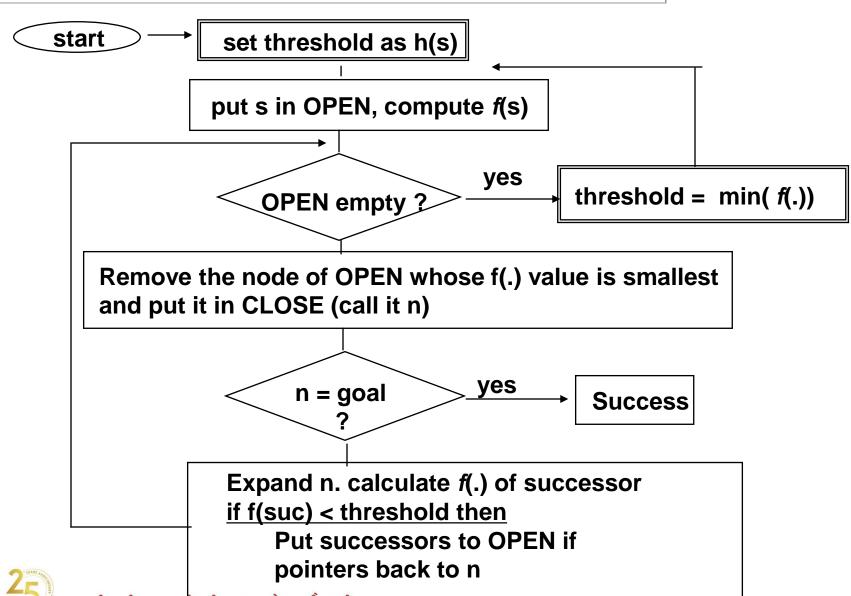


Iterative Deeping A*

- Iterative Deeping version of A*
 - use threshold as depth bound
 - To find solution under the threshold of *f*(.)
 - increase threshold as minimum of f(.) of
 - previous cycle
- Still admissible
- same order of node expansion
- Storage Efficient practical
 - but suffers for the real-valued *f*(.)
 - large number of iterations



Iterative Deepening A* Search Algorithm (for tree search)



Recursive best-first search

- A variation of Depth-first search
- Keep track of *f*-value of the best alternative path
- Unwind if *f*-value of all children exceed its best alternative
- When unwind, store *f*-value of best child as its *f*-value
- When needed, the parent regenerate its children again.



Recursive best-first search

function RECURSIVE-BEST-FIRST-SEARCH(*problem*) **return** a solution or failure **return** RBFS(*problem*,MAKE-NODE(INITIAL-STATE[*problem*]),∞)

```
function RBFS (problem, node, f_limit) return a solution or failure and a new f-cost limit
if GOAL-TEST[problem](STATE[node]) then return node
successors \leftarrow \text{EXPAND}(node, problem)
if successors is empty then return failure, \infty
for each s in successors do
         f[s] \leftarrow \max(g(s) + h(s), f[node])
repeat
         best \leftarrow \text{the lowest } f\text{-value node in } successors
         if f[best] > f\_limit then return failure, f[best]
         alternative \leftarrow the second lowest f-value among successors
         result, f[best] \leftarrow RBFS(problem, best, min(f_limit, alternative))
         if result \neq failure then return result
```



Recursive best-first search

- Keeps track of the f-value of the best-alternative path available.
 - If current f-values exceeds this alternative f-value then backtrack to alternative path.
 - Upon backtracking change f-value to best f-value of its children.
 - Re-expansion of this result is thus still possible.



RBFS evaluation

- RBFS is a bit more efficient than IDA*
 - Still excessive node generation (mind changes)
- Like A^* , optimal if h(n) is admissible
- Space complexity is O(bd).
 - IDA* retains only one single number (the current f-cost limit)
- Time complexity difficult to characterize
 - Depends on accuracy if h(n) and how often best path changes.
- IDA* and RBFS suffer from *too little* memory.



(simplified) memory-bounded A*

- Use all available memory.
 - I.e. expand best leafs until available memory is full
 - When full, SMA* drops worst leaf node (highest *f*-value)
 - Like RBFS, we remember the best descendant in the branch we delete
- What if all leafs have the same *f*-value?
 - Same node could be selected for expansion and deletion.
 - SMA* solves this by expanding *newest* best leaf and deleting *oldest* worst leaf.
- The deleted node is regenerated when all other candidates look worse than the node.
- SMA* is complete if solution is reachable, optimal if optimal solution is reachable.
- Time can still be exponential.

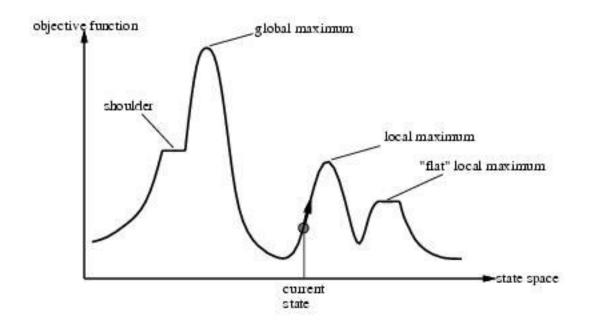


Local search algorithms

- In many optimization problems, the path to the goal is irrelevant; the goal state itself is the solution
- State space = set of "complete" configurations
- Find configuration satisfying constraints, e.g., n-queens
- In such cases, we can use local search algorithms
- Local search= use single current state and move to neighboring states.
- Advantages:
 - Use very little memory
 - Find often reasonable solutions in large or infinite state spaces.
- Are also useful for pure optimization problems.
 - Find best state according to some *objective function*.



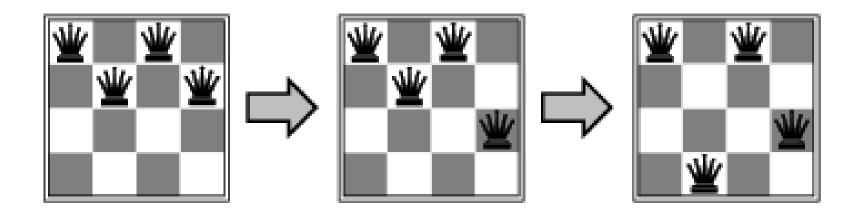
Local search and optimization





Example: *n*-queens

• Put n queens on an $n \times n$ board with no two queens on the same row, column, or diagonal



Hill-climbing search

- Simple, general idea:
 - Start wherever
 - Always choose the best neighbor
 - If no neighbors have better scores than current, quit
- Hill climbing does not look ahead of the immediate neighbors of the current state.
- Hill-climbing chooses randomly among the set of best successors, if there is more than one.
- Some problem spaces are great for hill climbing and others are terrible.



Hill-climbing search

function HILL-CLIMBING(*problem*) **return** a state that is a local maximum

input: problem, a problem

local variables: current, a node.

neighbor, a node.

 $current \leftarrow MAKE-NODE(INITIAL-STATE[problem])$

loop do

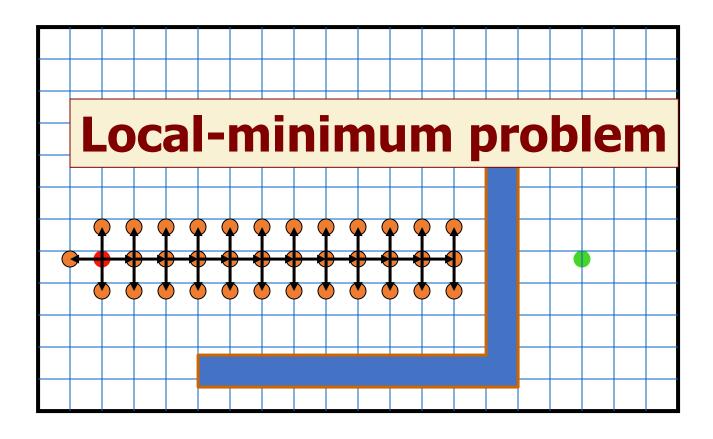
 $neighbor \leftarrow$ a highest valued successor of *current*

if VALUE [neighbor] < VALUE[current] then return STATE[current]</pre>

 $current \leftarrow neighbor$



Robot Navigation



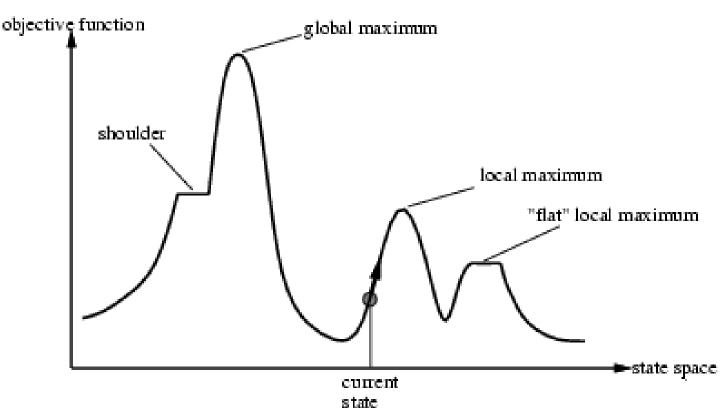
f(N) = h(N) = straight distance to the goal



Drawbacks of hill climbing

- Problems:
 - Local Maxima: depending on initial state, can get stuck in local maxima
 - **Plateaus:** the space has a broad flat region that gives the search algorithm no direction (random walk)
 - **Ridges:** flat like a plateau, but with dropoffs to the sides; steps to the North, East, South and West may go down, but a combination of two steps (e.g. N, W) may go up

Introduce randomness





Hill-climbing variations

- Stochastic hill-climbing
 - Random selection among the uphill moves.
 - The selection probability can vary with the steepness of the uphill move.
- First-choice hill-climbing
 - Stochastic hill climbing by generating successors randomly until a better one is found.
- Random-restart hill-climbing
 - Tries to avoid getting stuck in local maxima.
 - If at first you don't succeed, try, try again...

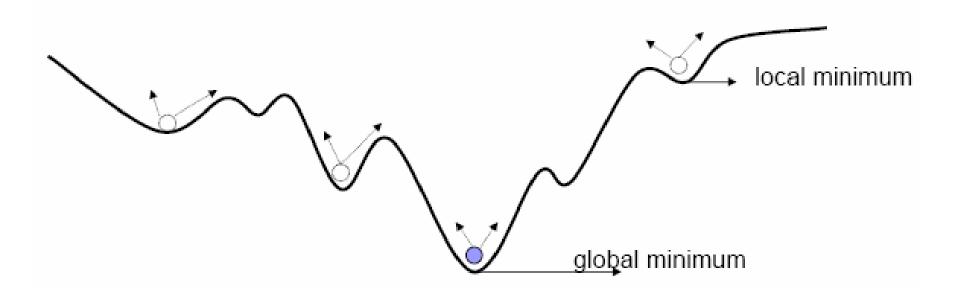


Simulated Annealing

- Simulates slow cooling of annealing process
- Applied for combinatorial optimization problem by S. Kirkpatric ('83)
- What is annealing?
 - Process of slowly cooling down a compound or a substance
 - Slow cooling let the substance flow around → thermodynamic equilibrium
 - Molecules get optimum conformation



Simulated annealing



gradually decrease shaking to make sure the ball escape from local minima and fall into the global minimum



Simulated annealing

- Escape local maxima by allowing "bad" moves.
 - Idea: but gradually decrease their size and frequency.
- Origin; metallurgical annealing
- Implement:
 - Randomly select a move instead of selecting best move
 - Accept a bad move with probability less than 1 (p<1)
 - p decreases by time
- If T decreases slowly enough, best state is reached.
- Applied for VLSI layout, airline scheduling, etc.



Simulated annealing

What's the probability when: $\Delta=0$?

s the probability when: $\Delta \rightarrow -\infty$?

function SIMULATED-ANNEALING(problem, schedule) **return** a solution state **input:** problem, a problem schedule, a mapping from time to temperature **local variables:** current, a node; next, a node. T, a "temperature" controlling the probability of downward steps $current \leftarrow MAKE-NODE(INITIAL-STATE[problem])$ Similar to hill climbing, for $t \leftarrow 1$ to ∞ do but a **random** move $T \leftarrow schedule[t]$ instead of best move **if** T = 0 **then return** *current* $next \leftarrow$ a randomly selected successor of *current* $\Delta E \leftarrow \text{VALUE}[next] - \text{VALUE}[current]$ case of improvement, make the move if $\Delta E > 0$ then current \leftarrow next **else** *current* \leftarrow *next* only with probability $e^{\Delta E/T}$ What's the probability when: $T \rightarrow \inf$? Otherwise, choose the move with What's the probability when: $T \rightarrow 0$? probability that decreases exponentially

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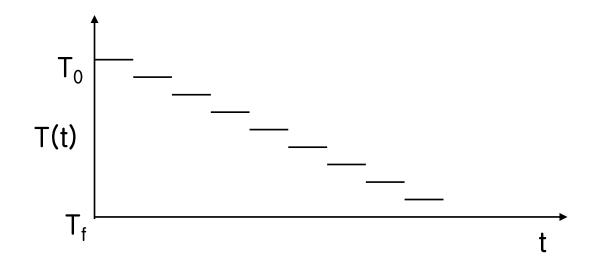
with the "badness" of the move

Simulated Annealing parameters

- Temperature T
 - Used to determine the probability
 - High T : large changes
 - Low T : small changes
- Cooling Schedule
 - Determines rate at which the temperature T is lowered
 - Lowers T slowly enough, the algorithm will find a global optimum
- In the beginning, aggressive for searching alternatives, become conservative when time goes by



Simulated Annealing Cooling Schedule



- if Ti is reduced too fast, poor quality
- if Tt >= T(0) / log(1+t)

- Geman
- System will converge to minimun configuration
- Tt = k/1+t

- Szu
- Tt = a T(t-1) where a is in between 0.8 and 0.99



Tips for Simulated Annealing

- To avoid of entrainment in local minima
 - Annealing schedule : by trial and error
 - Choice of initial temperature
 - How many iterations are performed at each temperature
 - How much the temperature is decremented at each step as cooling proceeds
- Difficulties
 - Determination of parameters
 - If cooling is too slow → Too much time to get solution
 - If cooling is too rapid → Solution may not be the global optimum



Properties of simulated annealing

• Theoretical guarantee:

• Stationary distribution:

$$p(x) \alpha e^{\frac{E(x)}{kT}}$$

- If T decreased slowly enough, will converge to optimal state!
- Is this an interesting guarantee?
- Sounds like magic, but :
 - The more downhill steps you need to escape, the less likely you are to every make them all in a row
 - People think hard about *ridge operators* which let you jump around the space in better ways

