

Prob 1.6:

Solution:

a, We have:

- P1: Clock rate = 3 GHz, CPI = 1.5
- P2: Clock rate = 2.5 GHz, CPI = 1.0
- P3: Clock rate = 4 GHz, CPI = 2.2

$IPS = \text{Clock rate} / \text{CPI}$

$IPS_{P1} = 3 \text{ GHz} / 1.5 = 2 * 10^9 \text{ instruction per sec.}$

$IPS_{P2} = 2.5 \text{ GHz} / 1.0 = 2.5 * 10^9 \text{ instruction per sec.}$

$IPS_{P3} = 4 \text{ GHz} / 2.2 = \text{approximately } 1.82 * 10^9 \text{ instruction per sec.}$

\Rightarrow P2 has the highest performance at $2.5 * 10^9 \text{ instruction per sec.}$

b, We have:

$\text{Total Cycle} = \text{Clock Rate} * \text{Execution Time}$

Given Execution Time = 10 sec.

$\text{Total Cycle}_{P1} = 3 \text{ GHz} * 10 \text{ sec} = 30 * 10^9 \text{ cycles.}$

$\text{Total Cycle}_{P2} = 2.5 \text{ GHz} * 10 \text{ sec} = 25 * 10^9 \text{ cycles.}$

$\text{Total Cycle}_{P3} = 4.5 \text{ GHz} * 10 \text{ sec} = 45 * 10^9 \text{ cycles.}$

$\text{Instructions} = \text{Total Cycle} / \text{CPI}$

$\text{Instructions}_{P1} = 30 * 10^9 \text{ cycles} / 1.5 = 20 * 10^9 \text{ instructions.}$

$\text{Instructions}_{P2} = 25 * 10^9 \text{ cycles} / 1.0 = 25 * 10^9 \text{ instructions.}$

$\text{Instructions}_{P3} = 45 * 10^9 \text{ cycles} / 2.2 = \text{approximately } 18.2 * 10^9 \text{ instructions.}$

c, Because we reduce the execution time by 30% so the new execution time is:

$T_{\text{New}} = T_{\text{old}} * (1 - 0.3) = 7 \text{ sec.}$

The original CPI increases by 20%, so the new CPI will be:

$\text{CPI}_{\text{New}} = \text{CPI}_{\text{old}} * 1.2.$

Suppose we apply to P1:

$$CPI_{P1\ New} = 1.5 * 1.2 = 1.8$$

We have the formula:

$$T_{New} = (CPI_{New} * Instructions) / Clock\ Rate_{New}$$

$$\Rightarrow Clock\ Rate_{new} = (CPI_{New} * Instructions) / T_{New} = (1.8 * 20 * 10^9) / 7 = \text{approximately } 5.14\ \text{Ghz}$$

Prob 1.7:

We have:

- **P1:** Clock rate = 2.5 GHz
 - CPI (Class A) = 1
 - CPI (Class B) = 2
 - CPI (Class C) = 3
 - CPI (Class D) = 3
- **P2:** Clock rate = 3 GHz
 - CPI (Class A) = 2
 - CPI (Class B) = 2
 - CPI (Class C) = 2
 - CPI (Class D) = 2

The instruction mix for the program is:

- 10% of instructions from Class A
- 20% from Class B
- 50% from Class C
- 20% from Class D

Total instruction count = $1.0 * 10^6$ instructions.

a, We have the formula for global CPI is:

$$CPI_{Global} = \sum (\text{Fraction of Instructions}) * (\text{CPI for that class})$$

$$\Rightarrow \text{CPI}_{\text{Global P1}} = (0.1 * 1) + (0.2 * 2) + (0.5 * 3) + (0.2 * 3) = 2.6$$

$$\Rightarrow \text{CPI}_{\text{Global P2}} = (0.1 * 2) + (0.2 * 2) + (0.5 * 2) + (0.2 * 2) = 2.0$$

b, We have the formula:

$$\text{Total Cycles} = \text{CPI}_{\text{Global}} * \text{Instruction Count}$$

$$\Rightarrow \text{Total Cycles}_{\text{P1}} = 2.6 * 1.0 * 10^6 = 2.6 * 10^6 \text{ cycles.}$$

$$\Rightarrow \text{Total Cycles}_{\text{P2}} = 2.0 * 1.0 * 10^6 = 2.0 * 10^6 \text{ cycles.}$$

To compare between P1 and P2 which one has the better performance, we have the formula:

$$\text{Execution Time} = \text{Total Cycles} / \text{Clock Rate}$$

$$\Rightarrow \text{Execution Time}_{\text{P1}} = (2.6 * 10^6) / (2.5 * 10^9) = 1.04 \text{ ms.}$$

$$\Rightarrow \text{Execution Time}_{\text{P2}} = (2.0 * 10^6) / (3 * 10^9) = 0.6667 \text{ ms.}$$

Conclusion, P2 is faster than P1 with 0.6667 ms to 1.04 ms.