

ĐẠI HỌC BÁCH KHOA HÀ NỘI VIỆN CÔNG NGHỆ THÔNG TIN VÀ TRUYỀN THÔNG



# Electronics for Information Technology

(Điện tử cho Công nghệ Thông tin)

**IT3420E** 

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Department of Computer Engineering

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#### General Information

- Course: Electronics for Information Technology
- ID Number: IT3420
- Credits: 2 (2-1-0-4)
- Lecture/Exercise: 32/16 hours (48 hours, 16 weeks)
- Evaluation:
  - Midterm examination and weekly assignment: 50%
  - Final examination: **50%**
- Learning Materials:
  - Lecture slides
  - Textbooks
    - *Introductory Circuit Analysis* (2015),  $10^{th} 13^{th}$  ed., Robert L. Boylestad
    - *Electronic Device and Circuit Theory* (2013), 11<sup>th</sup> ed., Robert L. Boylestad, Louis Nashelsky
    - *Microelectronics Circuit Analysis and Design* (2006), 4<sup>th</sup> ed., Donald A. Neamen
    - Digital Electronics: Principles, Devices and Applications (2007), Anil K. Maini



#### Contact Your Instructor

- You can reach me through office in **Room 802, B1 Building**, HUST.
  - You should make an appointment by email before coming.
  - If you have urgent things, just come and meet me!
- You can also reach me at the following **email** any time. This is the best way to reach me!
  - thuandc@soict.hust.edu.vn



#### **Course Contents**

- The Concepts of Electronics for IT
- Chapter 1: Passive Electronic Components and Applications
- Chapter 2: Semiconductor Components and Applications
- Chapter 3: Operational Amplifiers
- Chapter 4: Fundamentals of Digital Circuits
- Chapter 5: Logic Gates
- Chapter 6: Combinational Logic
- Chapter 7: Sequential Logic



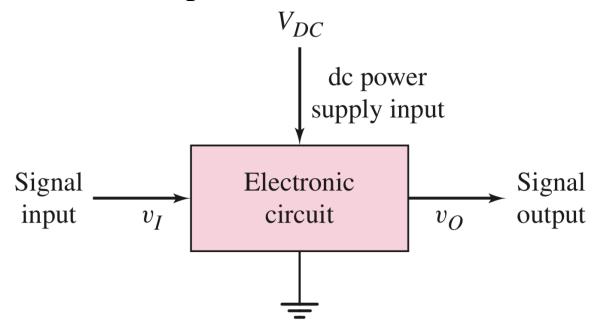
# Chapter 2: Semiconductor Components and Applications

- Semiconductor Materials
- Diodes and Applications
- Transistors and Applications



#### **Analog Circuits**

- A signal contains some type of information.
  - Ex: a sound wave produced by a speaking human
- Electronic circuits that process analog signals are called analog circuits.
  - Ex: a linear amplifier





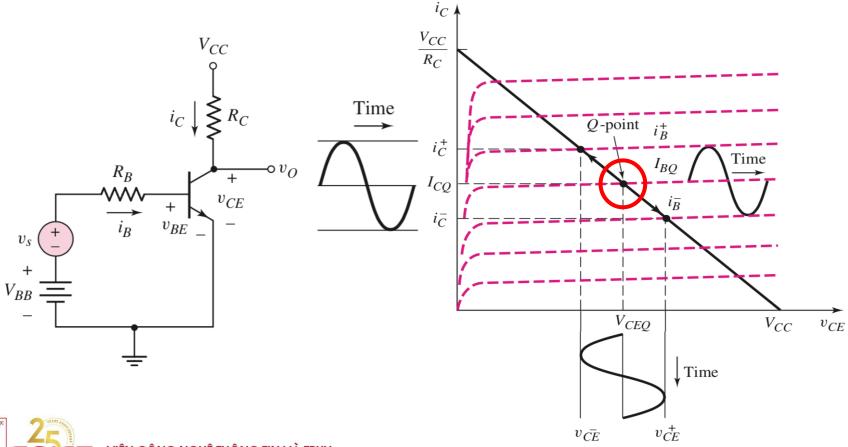
#### Analysis Method

- Using a small-signal analysis → a linear model
  - Doing the DC analysis to establish the Q-point of the transistor in the linear amplifier
  - Doing the AC analysis to determine the relationships between the time-varying output and input signals
  - Applying the superposition principle (thanks to the linear model)
    - "The response of a linear circuit excited by multiple independent input signals is the sum of the responses of the circuit to each of the input signals alone."

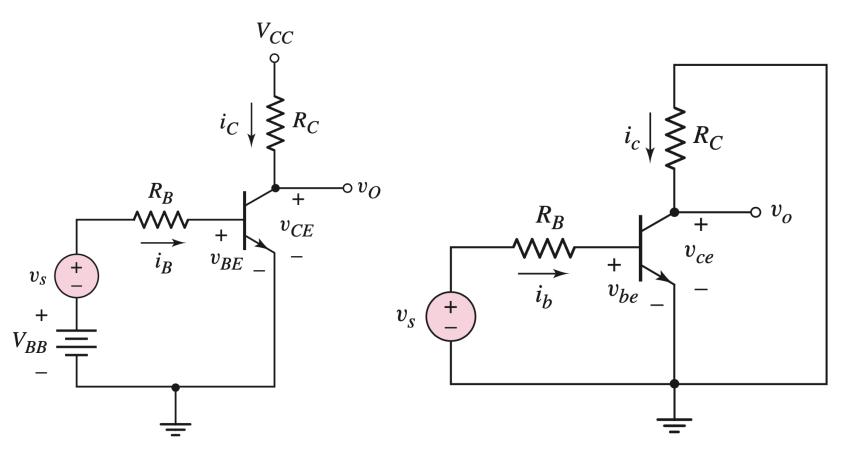


# Graphical Analysis

- DC Analysis: to find the desired Q-point
- AC Analysis: to determine the relationships between the timevarying output and input signals



#### AC Equivalent Circuit

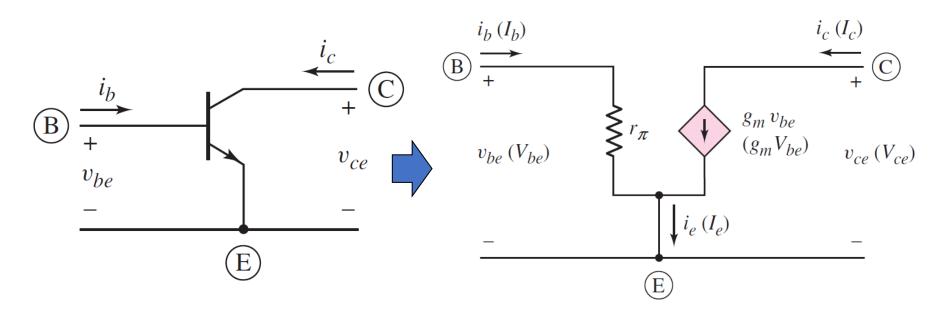


Common-Emitter Circuit

AC equivalent circuit



#### Small-Signal Hybrid-π Equivalent Circuit



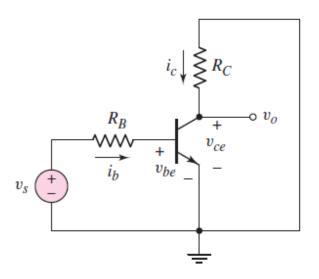
Can treat the bipolar transistor as a two-port network

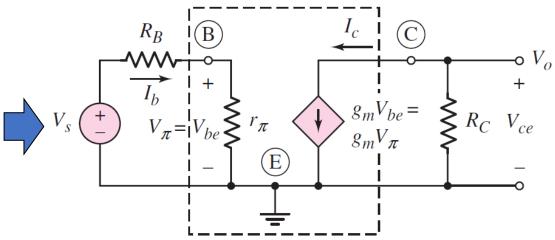
Hybrid- $\pi$  equivalent circuit with small time-varying signals

$$r_{\pi} = rac{V_T}{I_{BO}}$$
 Diffusion resistance or B-E input resistance

$$g_m = \frac{I_{CQ}}{V_T}$$
 Transconductance

# Hybrid-π Equivalent Circuit





Output signal voltage

Small-signal B-E voltage

Small-signal voltage gain

$$V_o = V_{ce} = -(g_m V_\pi) R_C$$

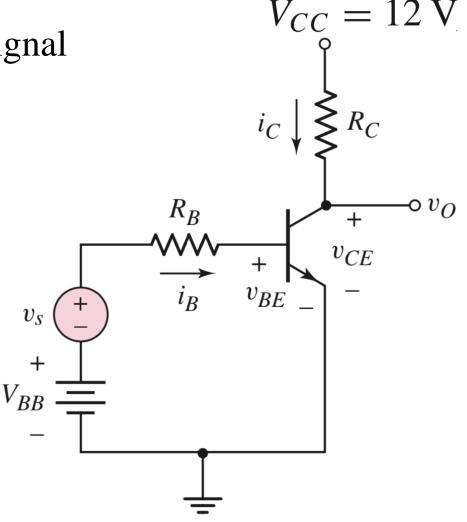
$$V_\pi = \left(\frac{r_\pi}{r_\pi + R_B}\right) \cdot V_s$$

$$A_v = \frac{V_o}{V_s} = -(g_m R_C) \cdot \left(\frac{r_\pi}{r_\pi + R_B}\right)$$



- Calculate the small-signal voltage gain.
- Assume:

$$eta = 100$$
 $V_{BE} = 0.7 \text{ V}$ 
 $R_C = 6 \text{ k}\Omega$ 
 $R_B = 50 \text{ k}\Omega$ 
 $V_{BB} = 1.2 \text{ V}$ 





# Example 2.13: DC Analysis

• DC equivalent circuit:

$$I_{BQ} = \frac{V_{BB} - V_{BE}(on)}{R_B} = \frac{1.2 - 0.7}{50} = 10 \,\mu\text{A}$$

$$I_{CQ} = \beta I_B = 100 * 0.01 = 1 \text{mA}$$

$$V_{CEQ} = V_{CC} - I_C R_C$$

$$= 12 - 1 * 6 = 6V$$

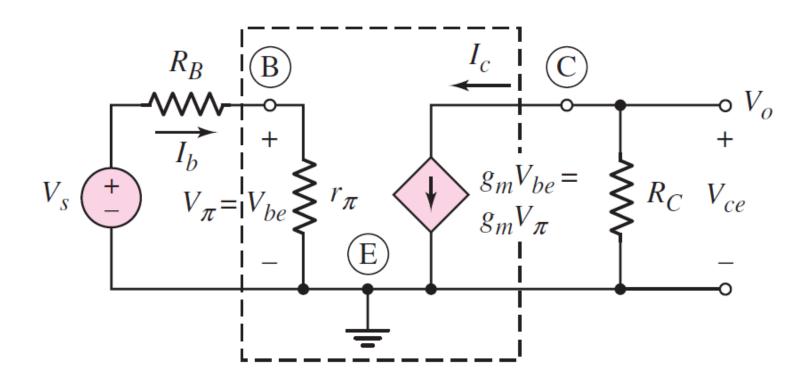
$$\downarrow I_{BQ} = 10 \,\mu\text{A}$$

$$V_{CEQ} = 6V$$

$$\downarrow I_{BQ} = 10 \,\mu\text{A}$$

$$V_{CEQ} = 6V$$
The transistor is biased in the forward-active mode

#### Example 2.13: Hybrid-π Equivalent Circuit



$$A_v = \frac{V_o}{V_s} = -(g_m R_C) \cdot \left(\frac{r_\pi}{r_\pi + R_B}\right)$$



# Example 2.13: AC Analysis

• The small-signal hybrid- $\pi$  parameters are:

$$r_{\pi} = \frac{\beta V_T}{I_{CQ}} = \frac{(100)(0.026)}{1} = 2.6 \text{ k}\Omega$$

$$g_m = \frac{I_{CQ}}{V_T} = \frac{1}{0.026} = 38.5 \text{ mA/V}$$

$$A_v = \frac{V_o}{V_s} = -(g_m R_C) \cdot \left(\frac{r_{\pi}}{r_{\pi} + R_B}\right)$$

$$= -(38.5)(6) \left(\frac{2.6}{2.6 + 50}\right)$$



# Example 2.13: Sinusoidal Input Voltage

• Considering a specific sinusoidal input voltage:

$$v_s = 0.25 \sin \omega t \text{ V}$$

• The sinusoidal base current is given by:

$$i_b = \frac{v_s}{R_B + r_\pi} = \frac{0.25 \sin \omega t}{50 + 2.6} \to 4.75 \sin \omega t \ \mu A$$

• The sinusoidal base current is given by:

$$i_c = \beta i_b = (100)(4.75 \sin \omega t) \to 0.475 \sin \omega t \text{ mA}$$

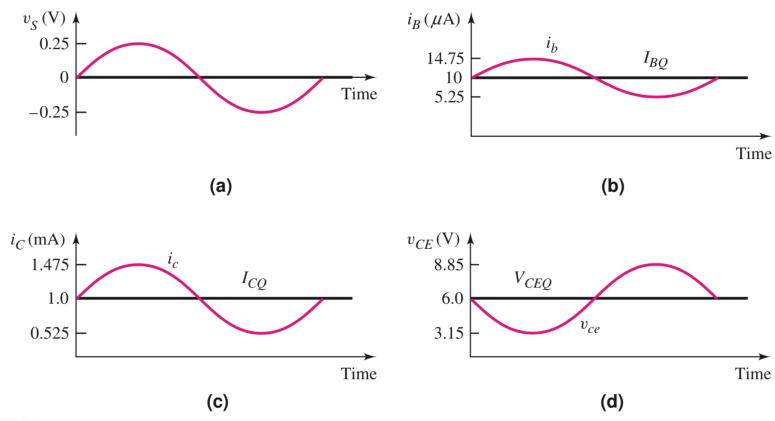
• The sinusoidal C-E voltage is:

$$v_{ce}=-i_cR_C=-(0.475)(6)\sin\omega t=-2.85\sin\omega t~{
m V}$$
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#### Example 2.13: Sinusoidal Input Voltage

• The DC and AC signals in the common-emitter circuit:





#### Problem-Solving Technique: AC Analysis

- Step 1: Analyze the circuit with only the dc sources present → Q-point. The transistor must be biased in the forward-active region to produce a linear amplifier.
- Step 2: Replace each element in the circuit with its small-signal model. Apply the small-signal hybrid- $\pi$  model to the transistor.
- Step 3: Analyze the small-signal equivalent circuit, setting the dc source components equal to zero, to produce the response of the circuit to the time-varying input signals only.
- Step 4: Apply the principle of superposition.



# Transformation of Elements in DC and Small-Signal Analysis

Element	<i>I–V</i> relationship	DC model	AC model
Resistor	$I_R = \frac{V}{R}$	R	R
Capacitor	$I_C = sCV$	Open	C
		<b>→</b>	
Inductor	$I_L = \frac{V}{sL}$	Short ———	L
Diode	$I_D = I_S(e^{v_D/V_T} - 1)$	$+V_{\gamma}-r_f$	$r_d = V_T/I_D$ $-\!$
Independent voltage source	$V_S = \text{constant}$	$+V_S -$	Short →⊶—
Independent current source	$I_S = \text{constant}$	$I_S$	Open →



#### Superposition Principle

• The time-varying signals are superimposed on dc values:

$$i_B = I_{BQ} + i_b$$
  
 $i_C = I_{CQ} + i_c$   
 $v_{CE} = V_{CEQ} + v_{ce}$   
 $v_{BE} = V_{BEQ} + v_{be}$ 

Variable	Meaning
$i_B,v_{BE}$	Total instantaneous values
$I_B,V_{BE}$	DC values
$i_b,v_{be}$	Instantaneous ac values
$I_b, V_{be}$	Phasor values



# Example 2.13: Superposition Principle

• The total instantaneous base current is given by:

$$i_B = I_{BQ} + i_b$$

$$= 10 + 4.75 sin\omega t \mu A$$

• The total instantaneous collector current is given by:

$$i_C = I_{CQ} + i_c$$
$$= 1 + 0.475 sin\omega t mA$$

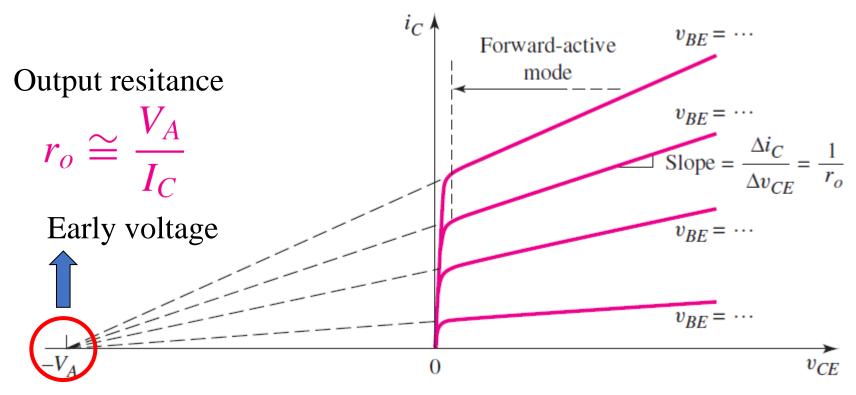
• The total instantaneous C-E voltage is given by:

$$v_{CE} = V_{CEQ} + v_{ce}$$
$$= 6 - 2.85 sin \omega t V$$



# Hybrid-π Equivalent Circuit, Including the Early Effect

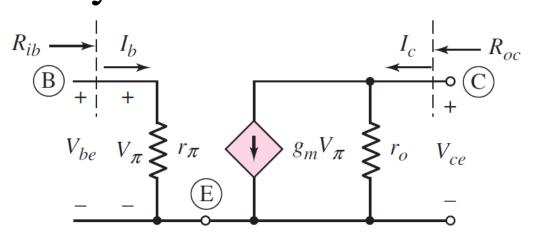
• When the curves are extrapolated to zero current, they meet at a point on the negative voltage axis, at  $v_{CE} = -V_A$ .



• Typical values of  $V_A$ :  $50 < V_A < 300 \text{ V}$ 

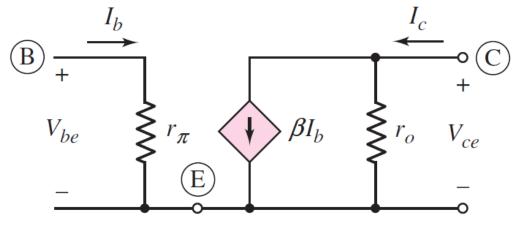


# Hybrid-π Equivalent Circuit, Including the Early Effect



The small-signal equivalent circuit, including the output resistance when the circuit contains the transconductance parameter.

The small-signal equivalent circuit, including the output resistance when the circuit contains the current gain parameter.



$$r_{o} = \frac{V_{A}}{I_{CO}}$$

Small-signal transistor output resistance

• Determine the small-signal voltage gain, including the effect of the transistor output resistance  $r_0$ , with the parameters:

$$\beta = 100$$

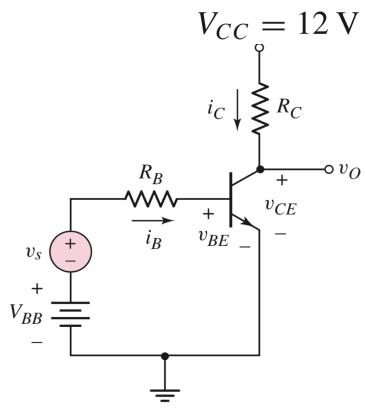
$$V_{BE} = 0.7 \text{ V}$$

$$R_C = 6 \text{ k}\Omega$$

$$R_B = 50 \text{ k}\Omega$$

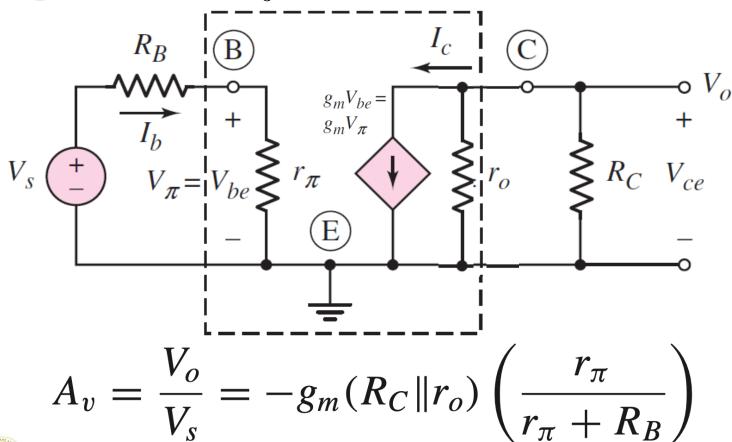
$$V_{BB} = 1.2 \text{ V}$$

$$V_A = 50 \text{ V}$$





• The small-signal equivalent circuit, including the output resistance r<sub>o</sub>:





• The output resistance is given by:

$$r_o = \frac{V_A}{I_{CQ}} = \frac{50}{1 \text{ mA}} = 50 \text{ k}\Omega$$

• The small-signal voltage gain is therefore:

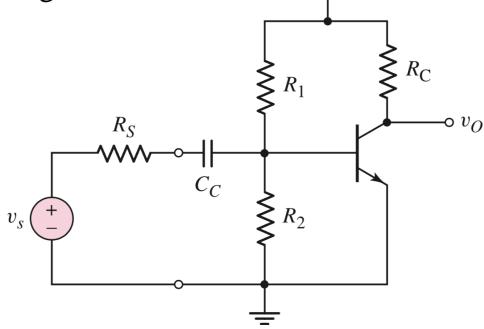
$$A_v = \frac{V_o}{V_s} = -g_m(R_C || r_o) \left(\frac{r_\pi}{r_\pi + R_B}\right)$$
$$= -(38.5)(6||50) \left(\frac{2.6}{2.6 + 50}\right)$$
$$= -10.2$$



r<sub>o</sub> reduces the magnitude of the small-signal voltage gain

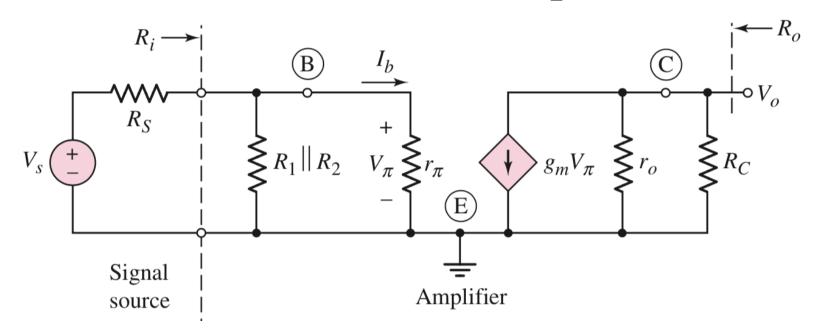


- Basic common-emitter circuit with voltage-divider biasing:
  - Do the dc analysis (to find the Q-point).
  - Do the ac analysis using the small-signal model.



 $V_{CC}$ 





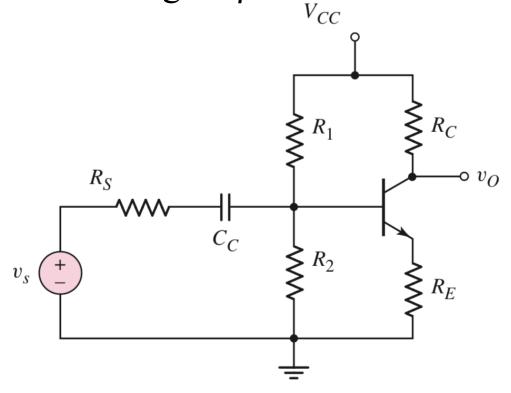
Output voltage: 
$$V_o = -g_m V_\pi (r_o || R_C)$$

Control voltage: 
$$V_{\pi} = \frac{R_1 || R_2 || r_{\pi}}{R_1 || R_2 || r_{\pi} + R_S} \cdot V_s$$

Voltage gain: 
$$A_v = \frac{V_o}{V_s} = -g_m(r_o || R_C) \left( \frac{R_1 || R_2 || r_\pi}{R_1 || R_2 || r_\pi + R_S} \right)$$

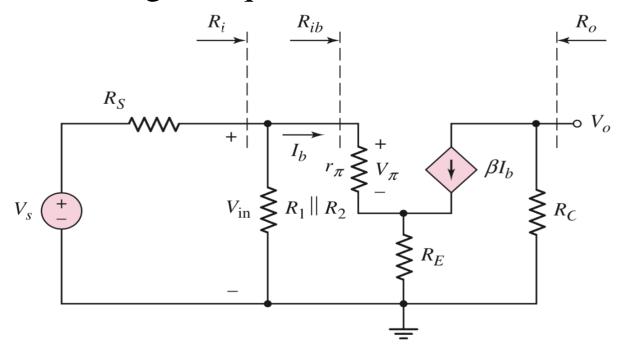


• Using the Emitter resistor ( $R_E$ ) so that the voltage gain of the amplifier circuit will be less dependent on the transistor current gain  $\beta$ .





• The small-signal equivalent circuit:



Output voltage:  $V_o = -(\beta I_b)R_C$ 

Input resistance:  $R_{ib} = \frac{V_{\text{in}}}{I_b} = r_{\pi} + (1 + \beta)R_E$ 



• Input resistance to the amplifier:  $R_i = R_1 || R_2 || R_{ib}$ 

• Input voltage: 
$$V_{\text{in}} = \left(\frac{R_i}{R_i + R_S}\right) \cdot V_s$$

• The small-signal voltage gain is:

$$A_v = \frac{V_o}{V_s} = \frac{-(\beta I_b)R_C}{V_s} = -\beta R_C \left(\frac{V_{\text{in}}}{R_{ib}}\right) \cdot \left(\frac{1}{V_s}\right)$$

or:

$$A_v = \frac{-\beta R_C}{r_\pi + (1+\beta)R_E} \left(\frac{R_i}{R_i + R_S}\right)$$



• Voltage gain is:

$$A_v = \frac{-\beta R_C}{r_\pi + (1+\beta)R_E} \left(\frac{R_i}{R_i + R_S}\right)$$

• If:

$$\begin{cases} R_i \gg R_S \\ (1+\beta)R_E \gg r_\pi \end{cases}$$

• Voltage gain is approximately:

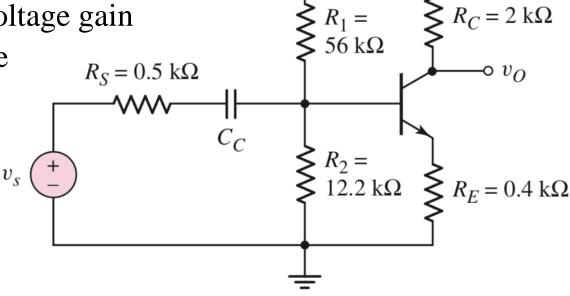
$$A_v \cong \frac{-\beta R_C}{(1+\beta)R_E} \cong \frac{-R_C}{R_E}$$

• For the circuit in the figure:

$$V_{BE}(\text{on}) = 0.7 \text{ V}$$

$$\beta = 100 \quad V_A = \infty$$

- Determine:
  - Small-signal voltage gain
  - Input resistance



 $V_{CC} = 10 \text{ V}$ 



# Example 2.15: DC Analysis

• DC solution:

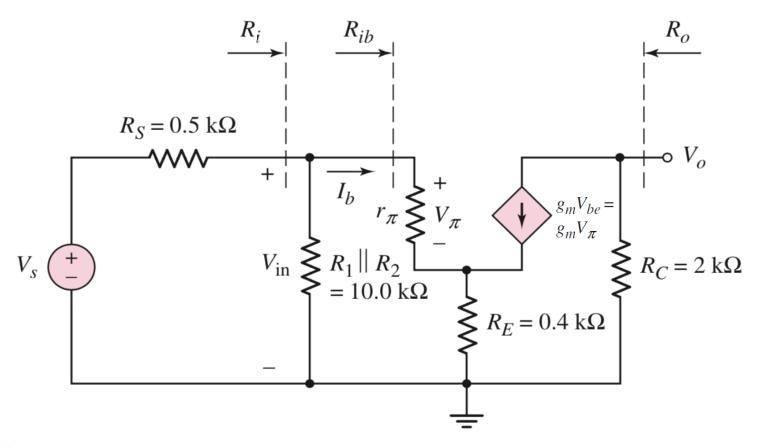
$$V_{CEQ} = 4.81 \text{ V}$$
  
 $I_{CQ} = 2.16 \text{ mA}$ 



The transistor is biased in the forward-active mode

#### Example 2.15: AC Analysis

• The small-signal equivalent circuit:





# Example 2.15: AC Analysis

• The small-signal hybrid- $\pi$  parameters:

$$r_{\pi} = \frac{V_T \beta}{I_{CQ}} = \frac{(0.026)(100)}{(2.16)} = 1.20 \,\mathrm{k}\Omega$$
 $g_m = \frac{I_{CQ}}{V_T} = \frac{2.16}{0.026} = 83.1 \,\mathrm{mA/V}$ 

• The input resistance to the base:

$$R_{ib} = r_{\pi} + (1 + \beta)R_E = 1.20 + (101)(0.4) = 41.6 \text{ k}\Omega$$

• The input resistance to the amplifier:

$$R_i = R_1 || R_2 || R_{ib} = 10 || 41.6 = 8.06 \text{ k}\Omega$$



# Example 2.15: AC Analysis

• Voltage gain:

$$A_v = \frac{-(100)(2)}{1.20 + (101)(0.4)} \left(\frac{8.06}{8.06 + 0.5}\right)$$
$$= -4.53$$

Approximate voltage gain:

$$A_v \cong \frac{-\beta R_C}{(1+\beta)R_E} \cong \frac{-R_C}{R_E}$$

• Obtain:

$$A_v = \frac{-R_C}{R_E} = \frac{-2}{0.4} = -5.0$$



#### Example 2.15: Comment

- The magnitude of the voltage gain is substantially reduced when an emitter resistor  $(R_E)$  is included.
  - Because of the  $(1 + \beta)R_E$  term in the denominator
- $-R_C/R_E$  can be used in the initial design of a commonemitter circuit with an emitter resistor.
- The amplifier gain is nearly independent of changes in the current gain parameter  $\beta$ .

β	$A_v$
50	-4.41
100	-4.53
150	-4.57

