

Week 1 questions

Ex1 Find the domain of the following functions

a) $\ln(1 - \cos 2x)$.

c) $\arcsin(\sinh(x))$

b) $\tan \frac{2x}{x+1}$

d) $\sqrt{\tan x - 1}$.

Ex2 Determine the parity (odd-even) of following functions

a) $y = \sin(\sin x)$

c) $\sinh^{-1}(x)$

b) $y = \tan(\cos x)$

d) $\arcsin(\sin x)$

Ex3 Study the following functions

a) $y = \arcsin x + \arccos x$

b) $y = \arcsin(\sin x)$

c) $y = \arccos(\cos x)$

d) $y = \arctan(\tan x)$

e) $y = \arctan x - \operatorname{arccot} \frac{1}{x}$.

Hints: Domain? Range? Parity? Periodicity?

Boundedness? Graph?

Ex 4 Compute the limits (if exists)

a) $\lim_{n \rightarrow +\infty} (n^2 + \cos(\pi n))$

d) $\lim_{n \rightarrow +\infty} \frac{\cos(\pi n)}{n^2}$

b) $\lim_{n \rightarrow +\infty} (n^2 \cdot \cos(\pi n))$

e) $\lim_{n \rightarrow +\infty} (n^2 - \cos(\pi n))$

c) $\lim_{n \rightarrow +\infty} \frac{n^2}{\cos(\pi n)}$

f) $\lim_{n \rightarrow +\infty} n^{2 + \cos(\pi n)}$

Remark Given a sequence u_n , the case $\lim_{n \rightarrow +\infty} u_n = +\infty$ is different to the case $\lim_{n \rightarrow +\infty} u_n$ does not exist.

Ex 5 Show that $\lim_{n \rightarrow +\infty} \cos(n)$ does not exist.

Ex 6 (hard)

a) Show that $\sin(x) + \sin(\pi x)$ is not periodic

b) Show that $A \sin(mx) + B \sin(nx)$, $A, B \in \mathbb{R}$
 $m, n \in \mathbb{Z}$ is periodic. Compute the smallest period.