ELECTRONICS FOR INFORMATION TECHNOLOGY

IT3420E

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ONE LOVE. ONE FUTURE.

General Information

- Course Name: Electronics for Information Technology
- ID Number: **IT3420**
- Credit Hour: 2 (2-1-0-4)
- Lecture/Exercise: 16.5 weeks
- Evaluation:
 - Midterm examination, assignment, attendance: 50%
 - Final examination: 50%
- Learning Materials:
 - Lecture slides
 - Textbooks:
 - Electronics A Systems Approach (2017), 6th ed., Neil Storey
 - *Introductory Circuit Analysis* (2015), 10th 13th ed., Robert L. Boylestad
 - *Electronics Fundamentals Circuits Devices and Applications* (2014), 8th ed., David M Buchla, Thomas L Floyd
 - Electronic Device and Circuit Theory (2013), 11th ed., Robert L. Boylestad, Louis Nashelsky
 - Digital Electronics: Principles, Devices and Applications (2007), Anil K. Maini
 - Microelectronics Circuit Analysis and Design (2006), 4th ed., Donald A. Neamen



Contact Your Instructor

Đỗ Công Thuần, Ph.D.

Department of Computer Engineering, SoICT, HUST

- You can reach me through office in **Room 803, B1 Building**, HUST.
 - You should make an appointment by email before coming.
 - If you have urgent things, just come and meet me!
- You can also reach me at the following **email** any time. This is the best way to reach me!
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Course Contents

- The Concepts of Electronics for IT
- Chapter 1: Passive Electronic Components and Applications
- Chapter 2: Semiconductor Components and Applications
- Chapter 3: Operational Amplifiers
- Chapter 4: Fundamentals of Digital Circuits
- Chapter 5: Boolean Algebra and Logic Gates
- Chapter 6: Combinational Logic
- Chapter 7: Sequential Logic



Chapter 4:

Fundamentals of Digital Circuits

- 1. Introduction to Number Systems
- 2. Number Systems
- 3. Digital Arithmetic



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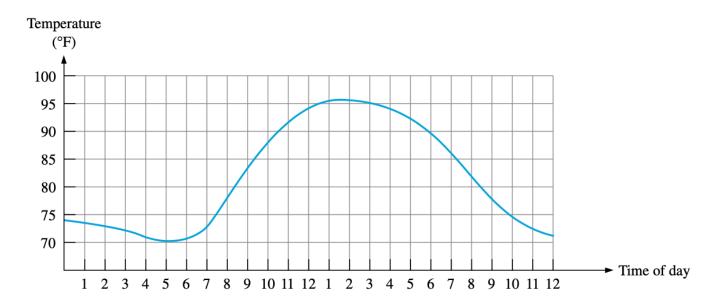
Introduction to Number Systems

- Electronic circuits can be divided into 2 broad categories: **digital** and **analog**.
- Digital electronics involves quantities with descrete values.
- Analog electronics involves quantities with continuous values.



Analog Quantity

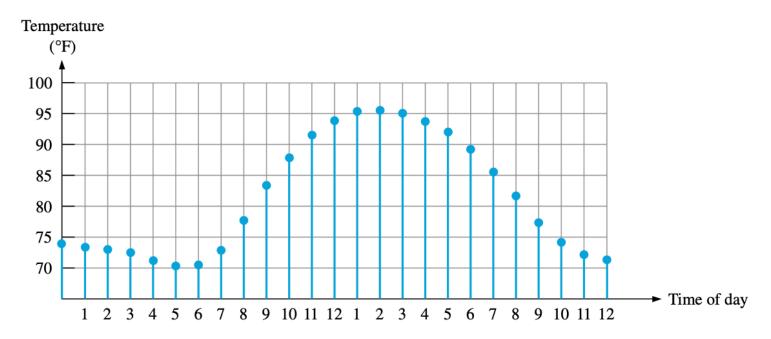
- An analog quantity is one having continuous value.
- Example: the air temperature changes over a continuous range of values.
 - Infinite values between 70° 71°





Digital Quantity

- A digital quantity is one having a discrete set of values.
- Example: taking a temperature reading every hour





Digital Signal and Modulation

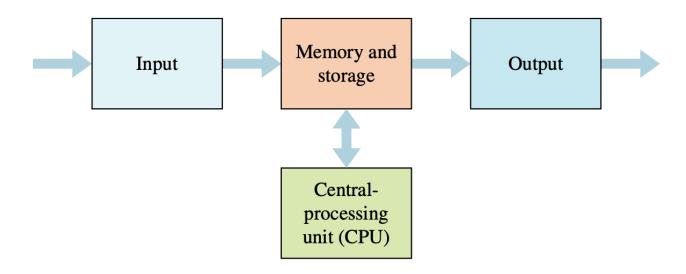
- A digital signal is encoded into sequences of 0's and 1's.
- The sequence is then transmitted as a sequence of voltage pulses of equal width that represent bit '1' and bit '0'.





Digital System

- A digital system contains devices that process the physical quantities represented in digital form.
- Example: personal computer (PC)





The Digital Advantage

- Digital data can be processed and transmitted more efficiently and reliably than analog data.
- Digtal data can be stored more compactly and preprocued with great accuracy and clarity.
- Noise does not affect digital data as much as analog data.
- Digital systems are more programmable and much easier to design.



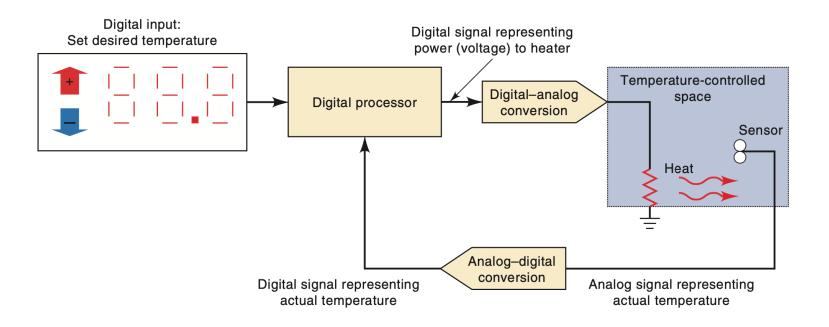
The Digital Disadvantage

- Most physical quantities (e.g., position, velocity, acceleration, force, pressure, temperature and flowrate, ...) are analogue in nature.
- A/D conversion takes time and causes error!
 - Physical quantities (variables) to analog signal (voltage, current) conversion
 - Analog-to-Digital conversion
 - Digital processing
 - Digital-to-Analog conversion



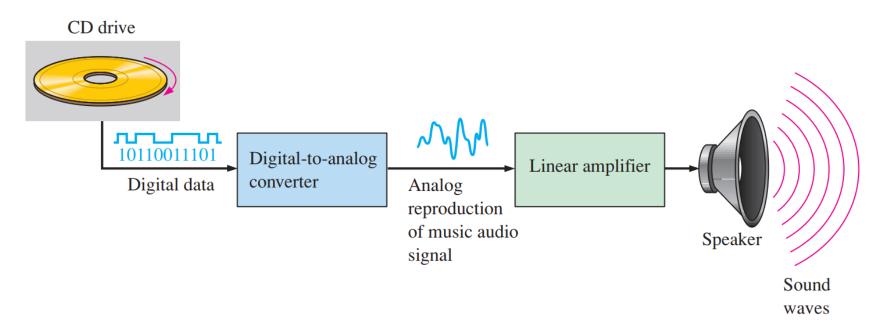
Combining Digital and Analog Methods

• Most of real applications use both digital and analog systems.





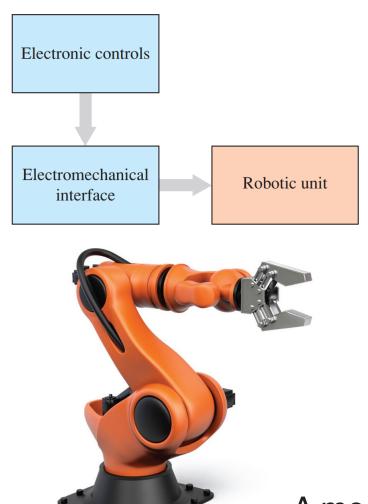
Combining Digital and Analog Methods

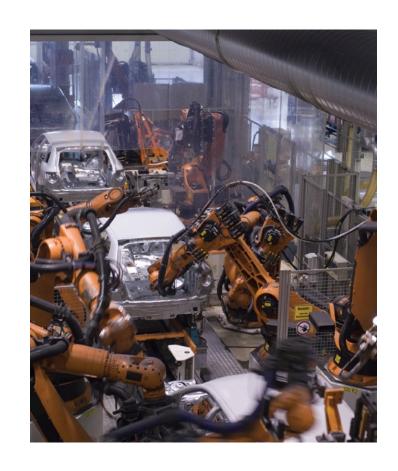


Basic block diagram of a CD player



Combining Digital and Analog Methods





A mechatronic system: Robotic arm



Chapter 4:

Fundamentals of Digital Circuits

- 1. Introduction to Number Systems
- 2. Number Systems
- 3. Digital Arithmetic



Number System

- A number system includes the number of independent digits (or symbols) used in the number system, the place values of the different digits constituting the number, and the maximum numbers that can be written with the given number of digits.
 - Symbol in Roman numerals: I, V, X, L, C,...
 - Standard form: IX, XV, XXX
- The number of independent digits used in the number system is called radix or base (denoted as r).
 - **Example:** the decimal system has a radix of 10 (0,1,2...,9).



Number System

- Base-r Number System
- Common Number Systems
- Representation of Negative Numbers
- Conversion between Two Number Systems
- Floating-Point Numbers



Base-r Number System

- A radix of r digits, $0 \rightarrow (r-1)$
- A number, N, in the base-r number system is represented in the form: $a_5 a_4 a_3 a_2 a_1 a_0$. $a_{-1} a_{-2} a_{-3}$
- In general, N is written as:

$$N = a_{n-1} \times r^{n-1} + \dots + a_0 \times r^0 + a_{-1} \times r^{-1} + \dots + a_{-m} \times r^{-m}$$
$$= \sum_{n=1}^{-m} a_i \times r^i$$

- Weights of whole numbers: r⁰, r¹, r²...
- Weights of fractional numbers: r⁻¹, r⁻², r⁻³...



Common Number Systems

- Decimal System
 - → For human beings
- Binary System
 - \rightarrow For machine (e.g. PC)
- Octal System
 - → A convenient way to abbreviate binary numbers
- Hexadecimal System
 - → A convenient way to abbreviate binary numbers



Decimal System (base 10)

- A radix of 10 digits: 0, 1, 2, 3, 4, 5, 6, 7, 8, 9
- Weights of whole numbers: 10⁰, 10¹, 10², 10³...
- Weights of fractional numbers: 10⁻¹, 10⁻², 10⁻³...
- Standard form: (3456.265)₁₀

Decimal point



Binary System (base 2)

- A radix of 2 digits: 0, 1
- Weights of whole numbers: 2^0 , 2^1 , 2^2 , 2^3 ...
- Weights of fractional numbers: 2⁻¹, 2⁻², 2⁻³...
- Standard form: $(0011.0111)_2$



Octal System (base 8)

- A radix of 8 digits: 0, 1, 2, 3, 4, 5, 6, 7
- Weights of whole numbers: 8⁰, 8¹, 8², 8³...
- Weights of fractional numbers: 8⁻¹, 8⁻², 8⁻³...
- Standard form: $(123)_8$



Hexadecimal System (base 16)

- A radix of 16 digits: $0\rightarrow 9$, A, B, C, D, E, F
- Weights of whole numbers: 16⁰, 16¹, 16², 16³...
- Weights of fractional numbers: 16⁻¹, 16⁻², 16⁻³...
- Standard form: (2ABE)₁₆



Basic Concepts – Binary System

- Bit: 0 and 1, the smallest unit of information.
- Byte: a string of 8 bits, the basic unit of data operated as a single unit in computers.
- Word: a string of bits whose size is fixed for a specified computer (1 byte, 2 bytes, 3 bytes, 4 bytes or even larger).
- 1's complement of a binary number is obtained by complementing all its bits.
 - E.g.: 1's complement of $(10010110)_2$ is $(01101001)_2$
- 2's complement of a binary number is obtained by adding '1' to its 1's complement.
 - E.g.: 2's complement of $(10010110)_2$ is $(01101010)_2$



Basic Concepts – Decimal System

- 9's complement of a given decimal number is obtained by subtracting each digit from 9.
 - E.g.: 9's complement of $(2496)_{10}$ is $(7503)_{10}$

- 10's complement of a given decimal number is obtained by adding '1' to its 9's complement.
 - E.g.: 10's complement of $(2496)_{10}$ is $(7504)_{10}$



Basic Concepts – Octal System

- 7's complement of a given octal number is obtained by subtracting each digit from 7.
 - E.g.: 7's complement of $(562)_8$ is $(215)_8$

- 8's complement of a given decimal number is obtained by adding '1' to its 7's complement.
 - E.g.: 8's complement of $(562)_8$ is $(216)_8$



Basic Concepts – Hexadecimal System

- 15's complement of a given octal number is obtained by subtracting each digit from 15.
 - E.g.: 15's complement of $(3BF)_{16}$ is $(C40)_{16}$

- 16's complement of a given decimal number is obtained by adding '1' to its 15's complement.
 - E.g.: 16's complement of $(2AE)_{16}$ is $(D52)_{16}$



Example 4.1

- The 7's complement of an octal number is $(5264)_8$. Determine the binary and hexa equivalent of the octal number.
 - The 7's complement: $(5264)_8$
 - The octal number = $(2513)_8$
 - The binary number $= (010\ 101\ 001\ 011)_2$ $= (10101001011)_2$
 - The hexa decimal number $= (10101001011)_2$ $= (101 0100 1011)_{16}$ $= (54B)_{16}$



Conversion btw. Two Number Systems

The integer and fractional parts of the given number should be treated separatedly.

- 1. To find the decimal equivalent of a number in a base r:
 - Represent the integer part in the form: r^0 , r^1 , r^2 , r^3 ...
 - Represent the fractional part in the form: r^{-1} , r^{-2} , r^{-3} ...



Binary-to-Decimal Conversion

- Example: $(1101.0101)_2 = (13.3125)_{10}$
- The whole part: $(1101)_2$
 - The decimal equivalent:

$$= 1x2^0 + 0x2^1 + 1x2^2 + 1x2^3$$

$$= 1 + 0 + 4 + 8 = 13$$

- The fractional part: $(.0101)_2$
 - The decimal equivalent:

$$= 0x2^{-1} + 1x2^{-2} + 0x2^{-3} + 1x2^{-4}$$

$$= 0 + 0.25 + 0 + 0.0625 = 0.3125$$



Octal-to-Decimal Conversion

- Example: $(135.21)_8 = (93.265625)_{10}$
- The whole part: $(135)_8$
 - The decimal equivalent:

$$= 5x8^0 + 3x8^1 + 1x8^2$$

$$= 5 + 24 + 64 = 93$$

- The fractional part: $(.21)_8$
 - The decimal equivalent:

$$= 2x8^{-1} + 1x8^{-2}$$

$$= 0.25 + 0.015625 = 0.265625$$



Hexadecimal-to-Decimal Conversion

- Example: $(1BF.A1)_{16} = (447.62890625)_{10}$
- The whole part: $(1BF)_{16}$
 - The decimal equivalent:

$$= 15x16^0 + 11x16^1 + 1x16^2$$

$$= 15 + 176 + 256 = 447$$

- The fractional part: $(.A1)_{16}$
 - The decimal equivalent:

$$= 10x16^{-1} + 1x16^{-2}$$

$$= 0.625 + 0.00390625 = 0.62890625$$



Conversion btw. Two Number Systems

The integer and fractional parts of the given number should be treated separatedly.

- 1. To find the decimal equivalent of a number in a base r:
 - Represent the integer part in the form: r^0 , r^1 , r^2 , r^3 ...
 - Represent the fractional part in the form: r⁻¹, r⁻², r⁻³...
- 2. To convert a decimal number to its equivalent in a base r:
 - For the integer part, successively divide the integer part by $r \rightarrow$ record the remainders until the quotient becomes '0'. The remainders written in reverse order constitute the equivalent (in a base r).
 - For the fractional part, successively multiply the fractional part by $r \rightarrow$ record the carry until the result of multiplication is '0'. The carry sequence written in forward order constitutes the equivalent (in a base r).

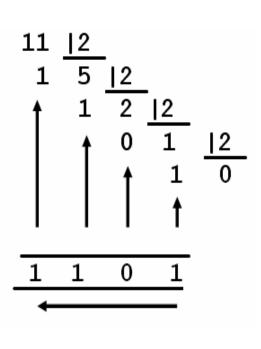


Decimal-to-Binary Conversion

• Example: $(11.73)_{10} = (1011.1011)_2$

- The whole part: $(11)_{10}$
- The fractional part: $(0.73)_{10}$

	0.73	
1	0.46	
0	0.92	
1	0.84	
1	0.68	
0.1011	0.1011	





Decimal-to-Octal Conversion

• Example: $(23.75)_{10} = (27.6)_8$

- The whole part: $(23)_{10}$
 - The octal equivalent: $(27)_8$
- The fractional part: $(0.75)_{10}$
 - The octal equivalent: $(0.6)_8$



Decimal-to-Hexadecimal Conversion

• Example: $(23.75)_{10} = (17.12)_{16}$

- The whole part: $(23)_{10}$
 - The hexadecimal equivalent: $(17)_{16}$
- The fractional part: $(0.75)_{10}$
 - The hexadecimal equivalent: $(0.12)_{16}$



Conversion btw. Two Number Systems

The integer and fractional parts of the given number should be treated separatedly.

- 1. To find the decimal equivalent of a number in a base r:
 - Represent the integer part in the form: r^0 , r^1 , r^2 , r^3 ...
 - Represent the fractional part in the form: r⁻¹, r⁻², r⁻³...
- 2. To convert a decimal number to its equivalent in a base r:
 - For the integer part, successively divide the integer part by $r \rightarrow$ record the remainders until the quotient becomes '0'. The remainders written in reverse order constitute the equivalent (in a base r).
 - For the fractional part, successively multiply the fractional part by $r \rightarrow$ record the carry until the result of multiplication is '0'. The carry sequence written in forward order constitutes the equivalent (in a base r).
- 3. For octal—binary/binary—octal conversion:
 - Replace each octal digit with its 3-bit binary equivalent.
 - Split the integer and fractional parts into groups of 3 bits, starting from the binary point on both sides. The 0s can be added to complete the outside groups if needed.
- 4. For hexadecimal-octal/octal-hexadecimal conversion:
 - The hex number \rightarrow its binary equivalent \rightarrow its octal equivalent. (An alternative approach: the given hex number \rightarrow its decimal equivalent \rightarrow its octal equivalent.)
 - The octal number \rightarrow its binary equivalent \rightarrow its hex equivalent.



Binary-to-Octal/Octal-to-Binary Conversion

- Example: $(375.2)_8 = (?)_2$ $(1100110001.0111)_2 = (?)_8$
- Octal-to-Binary conversion: $(375.2)_8 = (?)_2$

$$(375.2)_8 = (011\ 111\ 101.010)_2$$

= $(0111111101.010)_2$
= $(111111101.01)_2$

• Binary-to-Octal conversion:

```
(1100110001.0111)_2 = (1\ 100\ 110\ 001.011\ 1)_2
= (001\ 100\ 110\ 001.011\ 100)_2
= (1461.34)_8
```



Hex-to-Octal/Octal-to-Hex Conversion

- Example: $(375.2)_8 = (?)_{16}$ $(3BF.1A)_{16} = (?)_8$
- Octal-to-Hex conversion: $(375.2)_8 = (?)_{16}$

$$(375.2)_8 = (011\ 111\ 101.010)_2$$

= $(0111111101.010)_2$
= $(1111\ 1101.0100)_2 = (FD.4)_{16}$

• Hex-to-Octal conversion: $(3BF.1A)_{16} = (?)_8$

$$(3BF.1A)_{16} = (0011\ 1011\ 1111.0001\ 1010)_2$$

= $(1110111111.0001101)_2$
= $(001\ 110\ 111\ 111.000\ 110\ 100)_2$
= $(1677.064)_8$



Representation of Negative Numbers

- Several most common methods:
 - Sign and magnitude
 - 2's complement
 - 1's complement
- In each of these methods, the leftmost bit of a number is 0 for positive numbers and 1 for negative numbers.



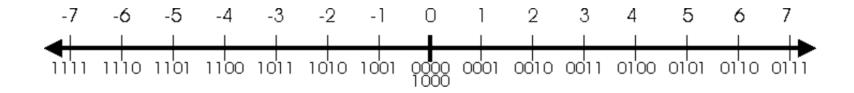
Sign and Magnitude

- In an n-bit *sign and magnitude* system, a number is represented by a sign bit (0 for '–' and 1 for '+'), followed by n-1 bits that represent the magnitude of the number.
- Example: in an 8-bit sign & magnitude number system
 - +9 is represented by $(00001001)_2$
 - -9 is represented by $(10001001)_2$
- Range of representation: $-(2^{n-1}-1)$ to $+(2^{n-1}-1)$, including a positive and negative zero (+0 & -0)
 - Example: in an 8-bit S&M number system, the range is from -127_{10} to $+127_{10}$, including 00000000 (+0) and 10000000 (-0)



Sign and Magnitude

- Advantage: easily determine whether a number is negative or positive by testing the MSB
- Disadvantage :
 - 2 zero representations (-0 and +0)



- Binary addition and subtractions are difficult!



- A negative number (-N) is represented by the 1's complement of its positive number (N).
- Example: in an 8-bit 1's complement number system
 - +9 is represented by $(00001001)_2$
 - -9 is represented by $(11110110)_2$
- Range of representation: $-(2^{n-1}-1)$ to $+(2^{n-1}-1)$, including a positive and negative zero (+0 & -0)
 - Example: in an 8-bit 1's complement number system, the range is from -127 to +127



• Advantage:

- Easily determining whether a number is negative or positive by testing the MSB
- Quite convenient for the computer to perform arithmetic

• Disadvantage:

- 2 zero representations (-0 and +0)
- Binary multiplication and division are inefficient!



• Advantage:

- Easily determining whether a number is negative or positive by testing the MSB
- Quite convenient for the computer to perform arithmetic

• Disadvantage:

- 2 zero representations (-0 and +0)
- Binary multiplication and division are inefficient!



- A negative number (-N) is represented by the 2's complement of its positive number (N):
 - The MSB is the sign bit (0 = '+' & 1 = '-')
 - The following bits are used to represent the magnitude.
- Example: in an 8-bit 2's complement number system
 - +9 is represented by $(00001001)_2$
 - -9 is represented by $(11110111)_2$
- Range of representation: $-(2^{n-1})$ to $+(2^{n-1}-1)$, including only one zero representation.
 - Example: in an 8-bit 2's complement number system, the range is from -128 đến +127



Advantage:

- Only one representation of zero, 000...0 (all zeroes)
- Discard last carry-out bit

• Disadvantage:

- Not work for multiplication and division

• Binary subtraction:

- Converting subtraction to addition of 2's complement numbers

```
- Discarding the last carry 11111000 (-8) 00010011 + 19 (1)00001011 = +11 (1)00001011 = +11
```



Chapter 4:

Fundamentals of Digital Circuits

- 1. Introduction to Number Systems
- 2. Number Systems
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Digital Arithmetic

- Basic Rules of Binary Addition and Subtraction
- Addition of Larger-Bit Binary Numbers
- Subtraction of Larger-Bit Binary Numbers
- Binary Multiplication
- Binary Division
- Floating-Point Arithmetic



Basic Rules of Binary Addition

- 1. 0+0=0
- 2. 0 + 1 = 1
- 3. 1 + 0 = 1
- 4. 1 + 1 = 0 (with a carry of '1' to the next more significant bit)
- 5. 1 + 1 + 1 = 1 (with a carry of '1')



Addition of Larger-Bit Binary Numbers

$$A + B + C_{in}$$

A	В	Carry- in (C_{in})	Sum	Carry- out (C_0)
0	0	0	0	0
0	0	1	1	0
0	1	0	1	0
0	1	1	0	1
1	0	0	1	0
1	0	1	0	1
1	1	0	0	1
1	1	1	1	1



- 1. Both the numbers are positive
- 2. The larger of the two numbers is positive
- 3. The larger of the two numbers is negative
- 4. Both numbers are negative



- Case 1: Consider $+37_{10}$ and $+18_{10}$
 - 2's complement representation of +37 in 8 bits = 00100101
 - 2's complement representation of +18 = 00010010
 - Result = $(00110111)_2 = (+55)_{10}$

- Case 2: Consider $+37_{10}$ and -18_{10}
 - 2's complement representation of + 37 = 00100101
 - 2's complement representation of -18 = 111011110
 - Result = $(00010011)_2 = (+19)_{10}$



- Case 3: Consider $+18_{10}$ and -37_{10}
 - 2's complement <u>representation</u> of -37 = 11011011
 - 2's complement representation of +18 = 00010010
 - Result = $(11101101)_2$ = $(-19)_{10}$

- Case 4: Consider -18_{10} and -37_{10}
 - 2's complement representation of -18 = 111011110
 - 2's complement <u>representation</u> of -37 = 11011011
 - Result = $(11001001)_2 = (-55)_{10}$



Addition Using 2's Complement Arithmetic

Steps to do addition in 2's complement arithmetic:

- 1. Represent the two numbers to be added in 2's complement form
- 2. Do the addition using basic rules of binary addition
- 3. Disregard the final carry, if any
- 4. The result of addition is in 2's complement form



• When overflow occurs, the result is wrong:

$$X = 0100 \ 1011 = +75$$
 $+ Y = 0101 \ 0001 = +81$
 $S = 1001 \ 1100 \neq +156$
 $(S = -2^7 + 2^4 + 2^3 + 2^2 = -100)$
 $X = 1001 \ 1000 = -104$
 $Y = 1011 \ 0110 = -74$
 $S = 0100 \ 1110 \neq -178$
 $C_{out} = 1 \rightarrow Discard$
 $(S = 2^6 + 2^3 + 2^2 + 2^1 = 78)$



Basic Rules of Binary Subtraction

- 1. 0 0 = 0
- $2. \quad 1 0 = 1$
- 3. 1 1 = 0
- 4. 0 1 = 1 (with a borrow of 1 from the next more significant bit)



Subtraction of Larger-Bit Binary Numbers

$$A - B - B_{in}$$

Inputs			Outputs	
Minuend (A)	Subtrahend (B)	Borrow-in $(B_{\rm in})$	Difference (D)	Borrow-out (B_0)
0	0	0	0	0
0	0	1	1	1
0	1	0	1	1
0	1	1	0	1
1	0	0	1	0
1	0	1	0	0
1	1	0	0	0
1	1	1	1	1



- 1. Both minuend and subtrahend are positive. The subtrahend is the smaller of the two.
- 2. Both minuend and subtrahend are positive. The subtrahend is the larger of the two.
- 3. The minuend is positive. The subtrahend is negative and smaller in magnitude.
- 4. The minuend is positive. The subtrahend is negative and greater in magnitude.
- 5. Both minuend and subtrahend are negative. The minuend is the smaller of the two.n
- 6. Both minuend and subtrahend are negative. The minuend is the larger of the two.



- Case 1: +24 (+14)
 - 2's complement representation of +24 = 00011000
 - 2's complement representation of +14 = 00001110
 - 2's complement of the subtrahend (i.e. +14) = 11110010 (i.e. -14)
 - Result = $(00001010)_2$ = $(+10)_{10}$
- Case 2: +14 (+24)
 - 2's complement representation of +24 = 00011000
 - 2's complement representation of +14 = 00001110
 - 2's complement of the subtrahend (i.e. +24) = 11101000 (i.e. -24)
 - Result = $(11110110)_2$ = $(-10)_{10}$



- Case 3: +24 (-14)
 - 2's complement representation of +24 = 00011000
 - 2's complement representation of -14 = 11110010
 - 2's complement of the subtrahend (i.e. -14) = 00001110 (i.e. +14)
 - Result = $(00100110)_2 = (+38)_{10}$
- Case 4: +14 (-24)
 - 2's complement <u>representation</u> of -24 = 11101000
 - 2's complement representation of +14 = 00001110
 - 2's complement of the subtrahend (i.e. -24) = 00011000 (i.e. +24)
 - Result = $(00100110)_2 = (+38)_{10}$



- Case 5: -24 (-14)
 - 2's complement representation of -24 = 11101000
 - 2's complement representation of -14 = 11110010
 - 2's complement of the subtrahend (i.e. -14) = 00001110 (i.e. +14)
 - Result = $(11110110)_2$ = $(-10)_{10}$
- Case 6: -14 (-24)
 - 2's complement <u>representation</u> of -14 = 11110010
 - 2's complement <u>representation</u> of -24 = 11101000
 - 2's complement of the subtrahend (i.e. -24) = 00011000 (i.e. +24)
 - Result = $(00001010)_2$ = $(+10)_{10}$



Steps to do substraction in 2's complement arithmetic:

- 1. Represent the minuend and subtrahend in 2's complement form
- 2. Find the 2's complement of the subtrahend
- 3. Add the 2's complement of the subtrahend to the minuend
- 4. Disregard the final carry, if any
- 5. The result is in 2's complement form
- 6. 2's complement notation can be used to perform subtraction when the expected result of subtraction lies in the range from -2^{n-1} to $+(2^{n-1}-1)$, n being the number of bits used to represent the numbers.



Binary Multiplication

- The basic rules of multiplication:
- 1. $0 \times 0 = 0$
- 2. $0 \times 1 = 0$
- 3. $1 \times 0 = 0$
- 4. $1 \times 1 = 1$

- Computers use the following algorithms to do binary multiplication:
- 1. Repeated Left-Shift and Add Algorithm
- 2. Repeated Right-Shift and Add Algorithm



Repeated Left-Shift and Add Algorithm



Repeated Right-Shift and Add Algorithm

1 0 1 1 1 1 1 1 0	Multiplicand Multiplier
00000	Start
0 0 0 0 0	Result of first addition
00000 + 10111	0 (Result of addition shifted one bit to right)
1 0 1 1 1	Result of second addition
0 1 0 1 1 + 1 0 1 1 1	10 (Result of addition shifted one bit to right)
1 0 0 0 1 0	Result of third addition
010001	010 (Result of addition shifted one bit to right)



Binary Division

- Binary division can be performed by using either:
- 1. Repeated Right-Shift and Substract Algorithm, or
- 2. Repeated Left-Shift and Substract Algorithm



Repeated Right-Shift and Substract Algorithm

• Dividend: 100110

• Divisor: 1100

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U	uo	ш	лп
•			

First step	0	1 0 0 1 1 0 -1 1 0 0	Dividend Divisor
Second step	1	1 0 0 1 1 -1 1 0 0	First five MSBs of dividend Divisor shifted to right
Third step	1	0 1 1 1 0 1 1 1 0 -1 1 0 0	First subtraction remainder Next MSB appended Divisor right shifted
		0010	Second subtraction remainder



Repeated Left-Shift and Substract Algorithm

Quotient	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	1 0
0	1 1 0 1 +1 1 0 0	Borrow exists
	1 0 0 1	Final carry ignored
	1 0 0 1 1 -1 1 0 0	Next MSB appended
1	0 1 1 1	No borrow
	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	Next MSB appended
1	00010	No borrow



Floating-Point Numbers

- Floating-point notation can be used conveniently to represent both large as well as small fractional or mixed numbers.
- Floating-point numbers are in general expressed in the form: $N=M \times b^{E}$

M: Mantissa (bits)

b: **b**ase (bits)

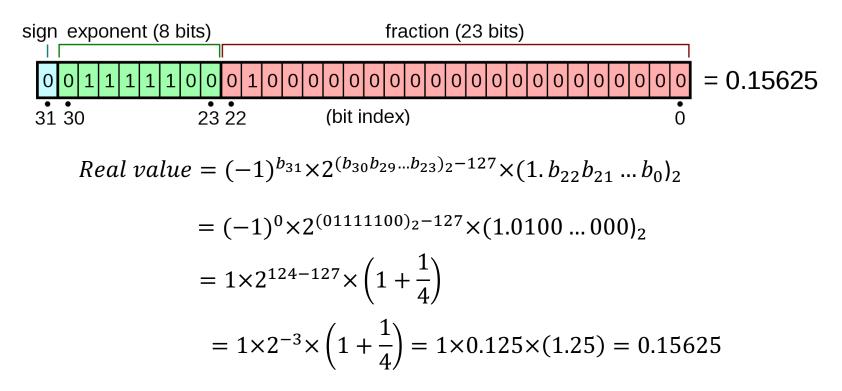
E: **E**xponent (bits)

- Decimal system: $N= M \times 10^E$
- Hexadecimal system: N= M x 16^E
- Binary system: $N = M \times 2^{E}$



Floating-Point Numbers

• Example: 32-bit single-precision floating point (IEEE 754 Std.)



Read textbooks for more details.

