



HUST

ĐẠI HỌC BÁCH KHOA HÀ NỘI
HANOI UNIVERSITY OF SCIENCE AND TECHNOLOGY

ONE LOVE. ONE FUTURE.



DATA STRUCTURES AND ALGORITHMS BASIC LAB



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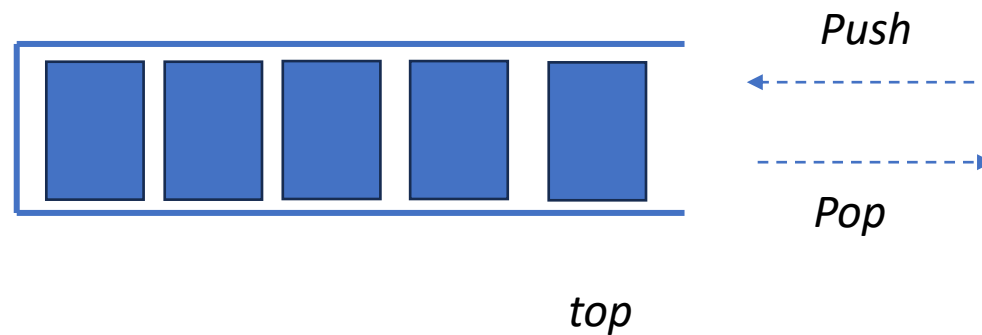
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STACK AND QUEUE

A stack:

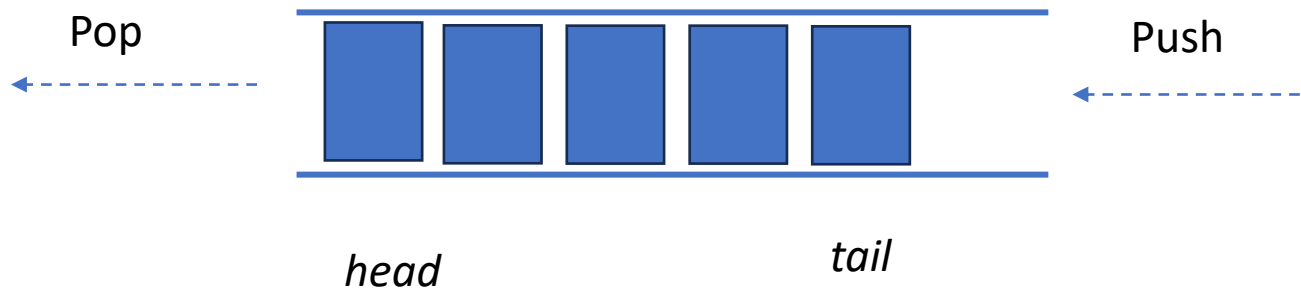
- A linear list of object
- Push and Remove are operated at top (head) of the list (First-In-Last-Out)
- Commonly used operations:
 - $\text{Push}(x, S)$: Insert an element x into stack S
 - $\text{Pop}(S)$: Remove an element from S
 - $\text{Top}(S)$: Access the element on the top of S
 - $\text{Empty}(S)$: Return true if S is empty



STACK AND QUEUE

A Queue:

- Is a linear list of objects. A queue has two pointers: *head* and *tail*
- Inserting a new element is operated at *tail* and removing is at *head* (First-In-First-Out)
- Commonly used operations:
 - Enqueue(x,Q) (Push): Insert a new element x into Q
 - Dequeue(Q) (Pop): Remove an element from Q
 - Empty(Q): Return true if Q is empty



EXERCISE 1: SIMULATION STACK

- Perform a sequence of operations over a stack, each element is an integer:
 - PUSH v: push a value v into the stack
 - POP: remove an element out of the stack and print this element to stdout (print NULL if the stack is empty)
- Input
 - Each line contains a command (operation) of type
 - PUSH v
 - POP
- Output
 - Write the results of POP operations (each result is written in a line)

EXERCISE 1: SIMULATION STACK

Example:

stdin	stdout
PUSH 1	3
PUSH 2	2
PUSH 3	5
POP	
POP	
PUSH 4	
PUSH 5	
POP	
#	

EXERCISE 1: SIMULATION STACK - PSEUDOCODE

- Using a singly linked list (pointed by *top*) to implement a stack:
 - Pop: remove an element on the *top*.
 - Push: add a new element to the *top*.

```
struct Node{  
    int value;  
    struct Node* next;  
}
```

```
makeNode(x){  
    p = new Node();  
    p -> value = x;  
    return p;  
}
```

```
Pop(){  
    if top==NULL return NULL;  
    x = top;  
    top = top-> next;  
    return x;  
}
```

```
Push(x){  
    p = makeNode(x);  
    p->next= top;  
    top = p;  
}
```

EXERCISE 2: SIMULATION QUEUE (P.03.08.02)

- Perform a sequence of operations over a queue, each element is an integer:
 - PUSH v: push a value v into the queue
 - POP: remove an element out of the queue and print this element to stdout (print NULL if the queue is empty)
- Input
 - Each line contains a command (operation) of type
 - PUSH v
 - POP
- Output
 - Write the results of POP operations (each result is written in a line)

EXERCISE 2: SIMULATION QUEUE

Example 2.1:

stdin	stdout
PUSH 1	1
PUSH 2	2
PUSH 3	3
POP	
POP	
PUSH 4	
PUSH 5	
POP	
#	

EXERCISE 2: SIMULATION QUEUE

Example 2.2:

stdin	stdout
PUSH 1	1
POP	NULL
POP	4
PUSH 4	
POP	
#	

EXERCISE 2: SIMULATION QUEUE - PSEUDOCODE

- Using a singly link list pointed by *head* và *tail* to implement a queue:
 - Pop: remove the element at *head*
 - Push: add a new element to *tail*

```
struct Node{  
    int value;  
    struct Node* next;  
}
```

```
Pop(){  
    if head = tail = NULL return ‘’;  
    v=head->value  
    head = head->next  
    return v  
}
```

```
makeNode(x){  
    p = new Node();  
    p -> value = x;  
    return p;  
}
```

```
Push(x){  
    p = makeNode(x)  
    if head=tail=NULL then  
        head=tail=p; return;  
    tail->next = p  
    tail = p  
    return  
}
```

EXERCISE 3: CHECK PARENTHESIS

- Given a string containing only characters (,), [,] {, }. Write a program that checks whether the string is correct in expression.

Example:

- `([]{}())`: correct
 - `([]{})([])`: incorrect
- Input
 - One line contains the string (the length of the string is less than or equal to 10^6)
- Output
 - Write 1 if the sequence is correct, and write 0, otherwise

stdin	stdout
<code>(([][]){}{}[]([]{}))</code>	1

EXERCISE 3: CHECK PARENTHESIS - PSEUDOCODE

- Using a stack, from left to right, if meet an open parenthesis then push to the stack, otherwise (a close parenthesis):
 - If the top of the stack is the matched open parenthesis then pop from stack
 - Otherwise: return false

```
match(a,b){  
  if (a=='(' and b ==')') or (a=='{' and  
    b=='}')  
  or (a=='[' and b == ']') return true;  
  return false;  
}
```

```
Check(s){  
  stack h;  
  for i = 1...len(s){  
    if s[i] in ('(', '[', '{') then push(s[i]);  
    else if (s[i] match top(h)) then pop(h);  
    else return false;  
  }  
  if h is empty return true;  
  return false;  
}
```

EXERCISE 4: WATER JUGS (P.03.08.04)

- There are two jugs, a-litres jug and b-litres jug (a, b are positive integers). There is a pump with unlimited water. Given a positive integer c, how to get exactly c litres.
- Input
 - Line 1: contains positive integers a, b, c ($1 \leq a, b, c \leq 900$)
- Output
 - Write the number of steps or write -1 (if no solution found)

Example:

stdin	stdout
6 8 4	4

EXERCISE 4: WATER JUGS - PSEUDOCODE

Idea: Enumerating the amount of water in the jugs (a pair of two integer x,y) using a queue with the shortest steps.

- Mark (x,y) if visited
- Pop each (x,y) at the head of the queue then push to the tail the new states not visited yet but can be reached from (x,y) by 1 step. Increase `num_steps` by 1.
- If reach to the target state then return `num_steps`, otherwise return -1 when finish.

```
mark(t){  
    m[t] = 1;  
}
```

```
is_mark(t){  
    return m[t] == 1;  
}
```

```
target(t){  
    return c in t;  
}
```

```
update_num_steps(t,r){  
    num[t] = r + 1;  
}
```

```
next_steps(t){  
    r = list_of_next_1_step_from(t);  
    return r;  
}
```

```
Check(a,b,c){  
    (x,y) = (0,0); mark((0,0));  
    queue q; q.push((x,y))  
    while not empty(q){  
        t = pop(q);  
        for ti in next_steps(t){  
            if target(ti) then return num[t]+1;  
            if not is_mark(ti) then {push(ti); mark(ti);  
update_num_steps(ti, num[t]);}  
        }  
    }  
    return -1;  
}
```



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THANK YOU !