## **Session 09: Integer Arithmetic**

#### **Learning Objectives**

- a. Shift & rotate Instructions
- b. Multiplication and Division
- c. Extended Addition and Subtraction

#### **Shift and Rotate Instructions**

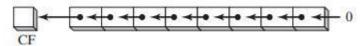
The 8086-based processors provide a complete set of instructions for shifting and rotating bits.

#### • Shift Instructions:

Shift instructions move bits a specified number of places to the right or left. The last in the direction of the shift goes into the carry flag, and the first bit is filled with 0 or with the previous value of the first bit.

## • SHL Instruction

This instruction performs a logical left shift on the destination operand, filling the lowest bit with 0. The highest bit is moved to the Carry flag, and the bit that was in the Carry flag is discarded.



Syntax: SHL destination, count

The following lists the types of operands permitted by this instruction:

SHL reg,imm8

SHL mem,imm8

SHL reg,CL

SHL mem,CL

Example:

mov bl,8Fh ;BL=10001111b

SHL bl,1 ;CF=1, BL=00011110b

mov al,10000000b ;AL=10000000b

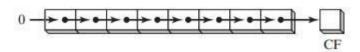
SHL al,2 ;CF=0, AL=00000000b

Bit Multiplication Example: SHL can perform multiplication by powers of 2. Shifting any operand left by n bits multiplies the operand by  $2^n$ . For example, shifting the integer 5 left by 1 bit yields the product of  $5 \times 2^1 = 10$ :

 $mov \ dl, 5$  ; DL=00000101b = 5 SHL dl, 1 ; CF=0, DL=00001010b = 10

#### • SHR Instruction

The SHR (shift right) instruction performs a logical right shift on the destination operand, replacing the highest bit with a 0. The lowest bit is copied into the Carry flag, and the bit that was previously in the Carry flag is lost.



Examples:

 $mov \ al, 0D0h$  ; AL = 11010000b

 $shr\ al, 1$ ; AL = 01101000b, CF = 0

mov al,00000010b

 $shr\ al,2$ ;  $AL = 00000000b,\ CF = 1$ 

#### **Bitwise Division**

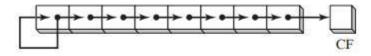
Bitwise Division Logically shifting an unsigned integer right by n bits divides the operand by  $2^n$ . In the following statements, we divide 32 by  $2^1$ , producing 16:

mov dl,32 ;DL=00100000b =32 SHR dl,1 ;DL=00010000b, CF=0 =16

#### • SAL and SAR Instructions.

The SAL (shift arithmetic left) instruction works the same as the SHL instruction.

The SAR (shift arithmetic right) works like:



The following example shows how SAR duplicates the sign bit. AL is negative before and after it is shifted to the right:

mov al, 0F0h ; AL = 11110000b (-16)

sar al,1 ; AL = 11111000b (-8), CF = 0

## Sign division:

mov dl,-128 ; DL = 10000000bsar dl,3 ; DL = 11110000b

#### **Sign-Extend AX into EAX:**

mov ax,-128 ; EAX = ????FF80h shl eax,16 ; EAX = FF800000h sar eax,16 ; EAX = FFFFFF80h

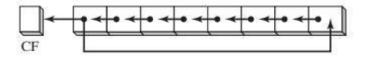
Instruction	CL	Initial	Contents	ontents Final Co		ntents	
		Decimal	Binary	Decimal	Binary	CF	
SHR AL,1		250	11111010	125	01111101	0	
SHR AL,CL	3	250	11111010	31	00011111	0	
SHL AL,1		23	00010111	46	00101110	0	
SHL BL,CL	2	23	00010111	92	01011100	0	
SAL BL,1	Î	+23	00010111	+46	00101110	0	
SAL DL,CL	4	+3	00000011	+48	00110000	0	
SAR AL,1		-126	10000010	-63	11000001	0	
SAR AL,CL	2	-126	10000010	-32	11100000	1	

#### • Rotate Instructions:

Rotate instructions also move bits a specified number of places to the right or left. For each bit rotated the last bit in the direction of the rotate operation moves into the first bit position at the other end of the operand. With some variations, the carry bit is used as an additional bit of the operand. **RCR** (Rotate Carry Right) and **RCL** (Rotate Carry Left) instructions carry values from the first register to the second by passing the leftmost or rightmost bit through the carry flag.

#### • **ROL Instruction**

The ROL (rotate left) instruction shifts each bit to the left. The highest bit is copied into the Carry flag and the lowest bit position. The instruction format is the same as for SHL:



Example:

mov al,40h ; AL = 01000000b

rol al,1 ; AL = 10000000b, CF = 0

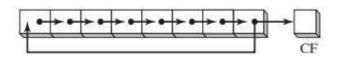
rol al,1 ; 
$$AL = 00000001b$$
,  $CF = 1$  rol al,1 ;  $AL = 00000010b$ ,  $CF = 0$ 

Exchanging Groups of Bits You can use ROL to exchange the upper (bits 4–7) and lower (bits 0–3) halves of a byte. For example, 26h rotated four bits in either direction becomes 62h:

rol al,4 ; AL = 62h

## • ROR Instruction

The ROR (rotate right) instruction shifts each bit to the right and copies the lowest bit into the Carry flag and the highest bit position.



Example:

mov al,01h ; AL = 00000001b

ror al,1 ; AL = 10000000b, CF = 1ror al,1 ; AL = 01000000b, CF = 0

## • RCL Instructions

The RCL (rotate carry left) instruction shifts each bit to the left, copies the Carry flag to the LSB, and copies the MSB into the Carry flag:



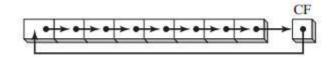
#### **Example:**

clc :CF=0

mov bl,88h ; CF, BL = 0 10001000b rcl bl,1 ; CF,BL = 1 00010000b

#### • RCR Instruction:

The RCR (rotate carry right) instruction shifts each bit to the right, copies the Carry flag into the MSB, and copies the LSB into the Carry flag



Example:

stc ;CF=1

mov ah,10h ; AH, CF = 00010000 1 rer ah,1 ; AH, CF = 10001000 0

Instruction	CL	Initial Contents		Final Contents	
		CF	Binary	Binary	CF
ROR AL,1		0	11111010	01111101	0
ROR AL,CL	3	1	11111010	01011111	0
ROL AL,1		0	00010111	00101110	0
ROL BL,CL	2	1	00010111	01011100	0
RCL BL,1		0	00010111	00101110	0
RCL DL,CL	4	1	00000011	00111000	0
RCR AL,1		1	10000010	11000001	0
RCR AL,CL	2	0	10000010	00100000	1

# **APPLICATIONS:**

# 1. Binary Multiplication

EAX \* 36 = EAX \* 
$$(2^5 + 2^2)$$
  
= EAX \*  $(32 + 4)$   
=  $(EAX * 32) + (EAX * 4)$ 

.code

mov eax,123  $\times \begin{array}{c} 01111011 & 123 \\ \times & 00100100 & 36 \end{array}$ 

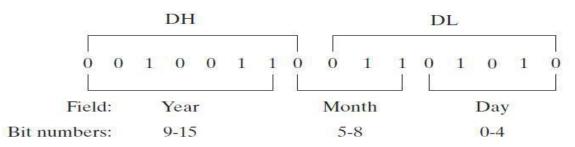
mov ebx,eax 0 1 1 1 1 0 1 1 123 SHL 2 + 0 1 1 1 1 0 1 1 123 SHL 5

shl eax,5; mult by 25; 0001000101001100 4428

shl ebx,2; mult by 22

add eax,ebx ; add the products

## 2. <u>Isolating Data Fields</u>



The following code example extracts the day number field of a date stamp integer by making a copy of DL and masking off bits not belonging to the field:

```
mov al,dl ; make a copy of DL and al,00011111b ; clear bits 5-7 mov day,al ; save in day
```

To extract the month number field, we shift bits 5 through 8 into the low part of AL before masking off all other bits. AL is then copied into a variable:

```
mov ax,dx ; make a copy of DX shr ax,5 ; shift right 5 bits and al,00001111b ; clear bits 4-7 mov month,al ; save in month
```

The year number (bits 9 through 15) field is completely within the DH register. We copy it to AL and shift right by 1 bit:

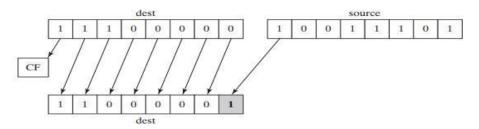
```
mov al,dh ; make a copy of DH shr al,1 ; shift right one position mov ah,0 ; clear AH to zeros add ax,1980 ; year is relative to 1980 mov year,ax ; save in year
```

#### • SHLD Instruction

The SHLD (shift left double) instruction shifts a destination operand a given number of bits to the left. The bit positions opened up by the shift are filled by the most significant bits of the source operand.

Format:

```
SHLD reg16, reg16, CL/imm8
SHLD mem16, reg16, CL/imm8
SHLD reg32, reg32, CL/imm8
SHLD mem32, reg32, CL/imm8
```



## Example:

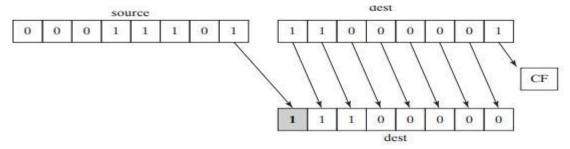
.data a WORD 9BA6h .code mov ax, 0AC36h

mov ax, 0AC36h shld a, ax, 4

;a=BA6Ah

## • SHRD Instruction

The SHRD (shift right double) instruction shifts a destination operand a given number of bits to the right. The bit positions opened by the shift are filled by the least significant bits of the source operand.



# Example:

.code

mov ax,234Bh mov dx,7654h shrd ax,dx,4

;ax=4234h

#### • MUL Instruction

The MUL instruction is for unsigned multiplication. Operands are treated as unsigned numbers. The three formats accept register and memory operands, but not immediate operands. The Carry flag is clear (CF = 0) because AH (the upper half of the product) equals zero. Syntax:

MUL reg/mem8 MUL reg/mem16 MUL reg/mem32

## • The table represents MUL operands

Multiplicand	Multiplier	Product	
AL	reg/mem8	AX	
AX	reg/mem16	DX:AX	
EAX	reg/mem32	EDX:EAX	

#### **EXAMPLE # 01:**

INCLUDE Irvine32.inc

.code

main PROC

mov eax,0

mov ebx,0

mov al,5h

mov bl,10h

mul bl

AX = 0050h, CF = 0

call crlf

call dumpregs

exit

main ENDP

END main

## EXAMPLE # 02:

.data

val1 WORD 2000h val2 WORD 0100h

.code

mov ax,val1 ; AX = 2000h

mul val2 ; DX:AX = 00200000h, CF = 0

## **EXAMPLE # 03:**

mov eax,12345h

mov ebx,1000h

mul ebx; EDX:EAX = 0000000012345000h, CF = 0

#### • **IMUL Instruction**

The **IMUL** instruction is for signed multiplication. Operands are treated as signed numbers and result is positive or negative depending on the signs of the operands.

The x86 instruction set supports three formats for the IMUL instruction: one operand, two operands, and three operands.

## One-Operand Formats:

IMUL reg/mem8 ; AX = AL \* reg/mem8

IMUL reg/mem16 ; DX:AX = AX \* reg/mem16 IMUL reg/mem32 ; EDX:EAX = EAX \* reg/mem32

## - Two-Operand Formats

```
IMUL reg16, reg/mem16
IMUL reg16, imm8
IMUL reg16, imm16
```

## - Three-Operand Formats

```
IMUL reg16, reg/mem16, imm8
IMUL reg16, reg/mem16, imm16
IMUL reg32, reg/mem32, imm8
IMUL reg32, reg/mem32, imm32
```

# Example:

The following instructions multiply 48 by 4, producing +192 in AX. Although the product is correct, AH is not a sign extension of AL, so the Overflow flag is set:

```
mov al,48

mov bl,4

imul bl ;AX = 00C0h, OF = 1
```

The following instructions multiply -4 by 4, producing -16 in AX. AH is a sign extension of AL so the Overflow flag is clear:

```
.code
main PROC
mov eax,0
mov ebx,0
mov edx,0
mov ax,-2
mov bx,4
; EDX:EAX = FFFFFF8h, OF = 0
imul bx
call crlf
call dumpregs
```

The following instructions demonstrate two-operand formats:

## **EXAMPLE:**

```
call dumpregs
       imul bx,ax
                                                        ;BX = -8
       call dumpregs
       imul bx,2
                                                        ;BX=-16
       call dumpregs
       imul bx,word1
                                                        :BX = -64
       mov eax.-16
       mov ebx,2
       call dumpregs
       imul ebx,eax
       call dumpregs
       imul ebx,2
       call dumpregs
       imul ebx,dword1
       call dumpregs
main ENDP
END main
```

The following instructions demonstrate three-operand formats:

## **Example:**

exit

```
INCLUDE Irvine32.inc
.data
     word1 SWORD 4
     dword1 SDWORD 4
.code
main PROC
mov ebx,0
imul bx,word1,-2
call dumpregs
imul ebx,dword1,-5
call dumpregs
exit
main ENDP
END main
```

#### **DIV Instruction**

The DIV (unsigned divide) instruction performs 8-bit, 16-bit, and 32-bit unsigned integer division. The single register or memory operand is the divisor. The formats are

DIV reg/mem8 DIV reg/mem16

## DIV reg/mem32

The following table shows the relationship between the dividend, divisor, quotient, and remainder:

Dividend	Divisor	Quotient	Remainder  AH  DX	
AX	reg/mem8	AL		
DX:AX	reg/mem16	AX		
EDX:EAX	reg/mem32	EAX	EDX	

## Example:

mov ax,0083h ; dividend mov bl,2 ; divisor

div bl; AL = 41h, AH = 01h

mov dx,0; clear dividend, high

mov ax,8003h ; dividend, low

mov cx, 100h; divisor

div cx ; AX = 0080h, DX = 0003h

## <u>Sign Extension Instructions(CBW,CWD,CDQ):</u>

Dividends of signed integer division instructions must often be sign-extended before the division takes place. Intel provides three useful sign extension instructions: CBW, CWD, and CDQ.

The CBW instruction (convert byte to word) extends the sign bit of AL into AH, preserving the number's sign. In the next example, 9Bh (in AL) and FF9Bh (in AX) both equal -101 decimal:

#### **EXAMPLE:**

.data

byteVal SBYTE -101 ; 9Bh

.code

mov al,byteVal ; AL = 9Bh cbw ; AX = FF9Bh

# The CWD (convert word to doubleword) instruction extends the sign bit of AX into DX:

.data

wordVal SWORD -101 ; FF9Bh

.code

mov ax, word Val ; AX = FF9Bh

cwd; DX:AX = FFFFFF9Bh

# The CDQ (convert doubleword to quadword) instruction extends the sign bit of EAX into EDX:

.data

dwordVal SDWORD -101 ; FFFFF9Bh

.code

mov eax,dwordVal

cdq; EDX:EAX = FFFFFFFFFFFF9Bh

# • <u>IDIV Instruction</u>

The IDIV (signed divide) instruction performs signed integer division, using the same operands as DIV.

Example: The following instructions divide -48 by 5.

.data

byteVal SBYTE -48 ; D0 hexadecimal

.code

mov al,byteVal ; lower half of dividend cbw ; extend AL into AH

mov bl,+5 ; divisor

idiv bl ;AL=-9,AH=-3

## • ADC Instructions:

The ADC (add with carry) instruction adds both a source operand and the contents of the Carry flag to a destination operand.

**Syntax:** *ADC Destination, source* 

ADC reg,reg ADC mem,reg ADC reg,mem ADC mem,imm ADC reg,imm

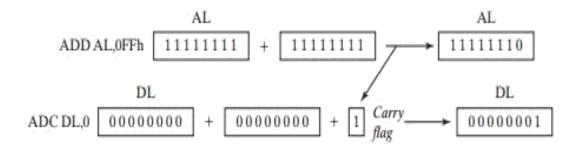
# EXAMPLE # 01:

mov dl,0

mov al,0FFh

add al,0FFh ; AL = FEh

adc dl,0 ; DL/AL = 01FEh



## • SBB Instructions:

The SBB (subtract with borrow) instruction subtracts both a source operand and the value of the Carry flag from a destination operand.

**Syntax:** SBB Destination, source

## **EXAMPLE:**

mov edx,7; upper halfmov eax,1; lower halfsub eax,2; subtract 2sbb edx,0; subtract upper half

