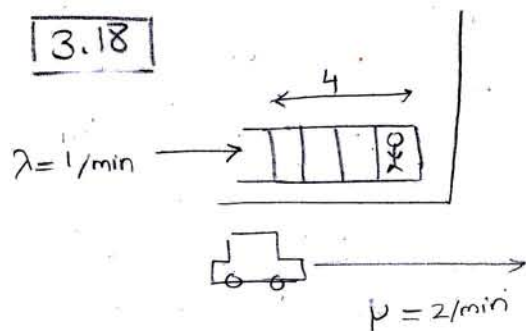
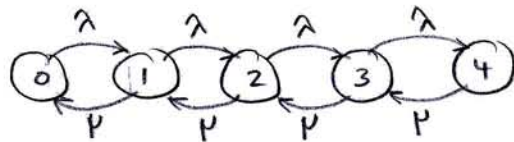


3.18



The problem can be modeled by :



$$\rho = \frac{\lambda}{\mu} = \frac{1}{2}$$

$$P_i = P_0 \rho^i \quad i = 0, 1, \dots, 4$$

(where  $P_i$  is the probability of  $i$  persons waiting for a taxi)

$$\sum_{i=0}^4 P_i = 1 \Rightarrow P_0 \left( 1 + \frac{1}{2} + \frac{1}{4} + \frac{1}{8} + \frac{1}{16} \right) = 1 \Rightarrow P_0 = \frac{16}{31}$$

$$\therefore P_i = \frac{16}{31} \left( \frac{1}{2} \right)^i \quad i = 0, 1, \dots, 4$$

$$\text{Average number of persons waiting} = N = \sum_{i=1}^4 i P_i$$

$$\begin{aligned} N &= \frac{16}{31} \left[ 1 \times \frac{1}{2} + 2 \times \frac{1}{4} + 3 \times \frac{1}{8} + 4 \times \frac{1}{16} \right] \\ &= \frac{16}{31} \times \frac{(8+8+6+4)}{16} \\ &= \frac{26}{31} \end{aligned}$$

$$N = \frac{26}{31}$$

$$\begin{aligned} \lambda_q &= \text{rate of passengers that join the queue} \\ &= \lambda \times (1 - P_4) = 1 \times \frac{30}{31} \end{aligned}$$

$$\text{Little's thm : } T = \frac{N}{\lambda_q} = \frac{26/31}{30/31} = \frac{13}{15}$$