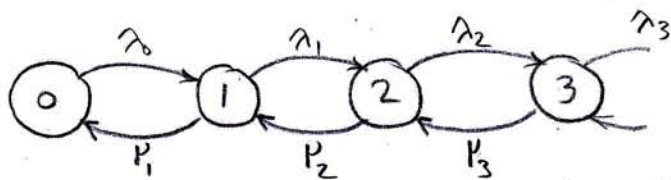


3.16



Global balance equations

$$0: \quad \boxed{\lambda_0 p_0 = p_1 p_1}$$

$$1: \quad (p_1 + \lambda_1) p_1 = p_2 p_2 + \lambda_0 p_0 \quad \text{but } \because \lambda_0 p_0 = p_1 p_1 \quad \therefore \boxed{\lambda_1 p_1 = p_2 p_2}$$

$$2: \quad (p_2 + \lambda_2) p_2 = p_3 p_3 + \lambda_1 p_1 \quad \text{but } \because \lambda_1 p_1 = p_2 p_2 \quad \therefore \boxed{\lambda_2 p_2 = p_3 p_3}$$

⋮

$$k: \quad \Rightarrow \quad \boxed{\lambda_k p_k = p_{k+1} p_{k+1}}$$

define  $\rho_k = \frac{\lambda_k}{p_{k+1}}$

$$p_{k+1} = \rho_k p_k \quad \forall k \geq 0 \quad \Rightarrow \quad p_{k+1} = p_k p_{k-1} \dots p_0 p_0 \quad \forall k \geq 1$$

$p_0$  is determined using:  $\sum_{k=0}^{\infty} p_k = 1$

$$p_0 + p_0 p_0 + p_0 p_1 p_0 + \dots + (p_0 p_1 \dots p_k) p_0 + \dots = 1$$

$$p_0 = \left[ 1 + \sum_{k=0}^{\infty} \prod_{i=1}^k \rho^i \right]^{-1}$$