## Math 115 Worksheet Section 3.9

## Warm-up question

The linear approximation or local linearization of f(x) at x = a is given by L(x) =

**Problem 1.** (a) Find the linear approximation of ln(x) at x = 1.

- (b) Use your approximation to approximate ln(1.1)
- (c) Is your answer an underestimate or overestimate of  $\ln(1.1)$ ? Why?

**Problem 2.** Find the linear approximation of cos(x) at x = 0.

**Problem 3.** (Winter 2017 Exam 2) A group of biology students is studying the length L of a newborn corn snake (in cm) as a function of its weight w (in grams). That is, L = G(w). A table of values of G(w) is shown below.

w	5	10	15	20	25
G(w)	24.5	31.6	38.7	44.7	50
G'(w)	2.23	1.58	1.30	1.12	1.05

Assume that G'(w) is a differentiable and decreasing function for 0 < w < 25.

- (a) Find a formula for H(w), the tangent line approximation of G(w) near w=20.
- (b) Use the tangent line approximation of G(w) near w = 20 to approximate the length of a corn snake that weighs 22 grams.
- (c) Is your answer in part (b) an overestimate or an underestimate? Write a sentence to justify your answer.
- (d) In their study of the growth of corn snakes, they found the results of a recent article that states that the average weight w of a corn snake (in grams) t weeks after being born is given by  $w = \frac{1}{5}t^2$ . Let  $S(t) = G(\frac{1}{5}t^2)$  be the length of a corn snake t weeks after being born. Find a formula for P(t), the tangent line approximation of S(t) near t = 5.

**Problem 4.** (Fall 2016 Exam 2) Let  $h(x) = x^x$ . For this problem, it may be helpful to know the following formula:

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$$h'(x) = x^x(\ln(x) + 1)$$

Write a formula for p(x), the local linearization of h(x) near x = 1.

**Problem 5.** (Fall 2017 Exam 2) Let g be a twice differentiable function defined on -1 < x < 11. Some values of g(x), g'(x) and g''(x) are shown in the table below.

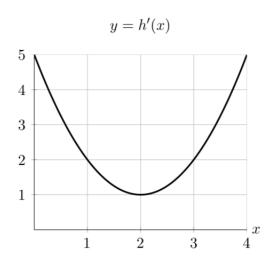
x	0	2	4	6	8	10
g(x)	-2	-1	3	4	5	6
g'(x)	0.5	2	?	5	1	2
g''(x)	2	1	5	-3	-1	0.5

Let j(x) = g(14 - 4x).

- (a) Use the values from the table to find a formula for L(x), the linear approximation to j(x) at x=2.
- (b) Find an approximate value for j(2.25) using your formula for L(x).
- (c) Is your approximation in part (b) an overestimate or an underestimate? Circle your answer and give a justification of your answer.

Overestimate Underestimate Not enough information

**Problem 6.** (Winter 2018 Exam 2) Below is the graph of h'(x).



- (a) Find a formula for the tangent line approximation L(x) to the function h(x) near x = 2 if the point (2, -3) lies on the graph of y = h(x). Your answer should not include the letter h.
- (b) Use the tangent line approximation to h(x) near x=2 to approximate the value of h(1.6).
- (c) Is your approximation in part (b) an overestimate, an underestimate or is there not enough information to determine that?