



NumPy Notes

What is NumPy?

NumPy (Numerical Python) is a **powerful library** for numerical computations in Python. It provides:

- **Multidimensional arrays** (ndarray)
 - **Mathematical functions** (like mean, sum, sqrt, etc.)
 - **Linear algebra, Fourier transform, random number generation**, and more.
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Why Use NumPy?

Feature	Benefit
Faster	NumPy uses C under the hood, making array operations much faster than regular Python loops or lists.
Memory Efficient	Stores data in contiguous memory locations.
Convenient	Supports broadcasting, vectorization, slicing, reshaping, etc.
Rich Ecosystem	Used in Pandas, Matplotlib, Scikit-learn, TensorFlow , etc.

Difference Between NumPy Arrays and Python Data Structures

Feature	NumPy Array	Python List / Tuple
Speed	Very fast (uses C)	Slower
Memory	Less memory	More memory
Operations	Vectorized (e.g., $a + 1$)	Requires loops
Data Type	Homogeneous (all elements same type)	Heterogeneous
Functionality	Mathematical operations	Limited math support



NumPy Array Creation Methods

1. np.array()

Creates an array from a **Python list or tuple**.

```
import numpy as np  
  
arr = np.array([1, 2, 3])  
  
print(arr) # [1 2 3]
```

2. dtype (Data Type of Array Elements)

Specify or check the **data type** of elements in an array.

```
arr = np.array([1, 2, 3], dtype=float)  
  
print(arr)      # [1. 2. 3.]  
  
print(arr.dtype) # float64
```

3. np.arange(start, stop, step)

Creates a range of numbers with a given step.

```
arr = np.arange(0, 10, 2)  
  
print(arr) # [0 2 4 6 8]
```

4. np.ones(shape)

Creates an array filled with **1s**.

```
arr = np.ones((2, 3))  
  
print(arr)  
  
# [[1. 1. 1.]  
  
#  [1. 1. 1.]]
```

5. np.zeros(shape)

Creates an array filled with **0s**.

```
arr = np.zeros((3, 2))

print(arr)

# [[0. 0.]
# [0. 0.]
# [0. 0.]]
```

6. np.eye(N)

Creates an **identity matrix** of size N x N.

```
arr = np.eye(3)

print(arr)

# [[1. 0. 0.]
# [0. 1. 0.]
# [0. 0. 1.]]
```

7. np.random.rand(shape)

Generates an array of **random numbers** between 0 and 1.

```
arr = np.random.rand(2, 3)

print(arr)
```

8. np.linspace(start, stop, num)

Generates num **evenly spaced values** between start and stop.

```
arr = np.linspace(0, 1, 5)

print(arr) # [0. 0.25 0.5 0.75 1.]
```

NumPy Array Attributes

These attributes help you understand the **structure and memory** details of a NumPy array.

1. ◆ **ndim – Number of Dimensions**

Returns how many dimensions (axes) the array has.

```
import numpy as np
```

```
a = np.array([[1, 2, 3], [4, 5, 6]])
```

```
print(a.ndim) # Output: 2
```

2. ◆ **shape – Shape of the Array**

Returns a **tuple** showing the size of each dimension (rows, columns).

```
print(a.shape) # Output: (2, 3) → 2 rows, 3 columns
```

3. ◆ **size – Total Number of Elements**

Returns the **total number of elements** in the array.

```
print(a.size) # Output: 6 → because  $2 \times 3 = 6$  elements
```

4. ◆ **itemsize – Memory Size of One Element (in Bytes)**

Tells how many **bytes** each **element** takes in memory.

```
print(a.itemsize) # Output: 4 (if dtype is int32)
```

5. ◆ **dtype – Data Type of Array Elements**

Returns the **data type** (int32, float64, etc.) of array elements.

```
print(a.dtype) # Output: int32 or int64 (depends on your system)
```

All Together Example

```
a = np.array([[10, 20, 30], [40, 50, 60]], dtype=np.int32)
```

```
print("ndim:", a.ndim)      # 2
print("shape:", a.shape)    # (2, 3)
print("size:", a.size)      # 6
print("itemsize:", a.itemsize) # 4 bytes
print("dtype:", a.dtype)    # int32
```

Changing Data Type in NumPy Arrays

NumPy allows you to **change or convert** the data type (dtype) of array elements using several methods.

1. Using astype() Method

The astype() function is used to **explicitly convert** an array to a different data type.

Syntax:

```
array.astype(new_dtype)
```

Example:

```
import numpy as np
arr = np.array([1, 2, 3])
new_arr = arr.astype(float)
print(new_arr)      # [1. 2. 3.]
print(new_arr.dtype) # float64
```

2. Converting from Float to Integer

This **truncates** the decimal values.

```
arr = np.array([1.5, 2.7, 3.2])
int_arr = arr.astype(int)
```

```
print(int_arr)    # [1 2 3]
print(int_arr.dtype) # int32 or int64
```

3. Converting to String Type

```
arr = np.array([10, 20, 30])
str_arr = arr.astype(str)

print(str_arr)    # ['10' '20' '30']
print(str_arr.dtype) # <U2 (Unicode string)
```

4. Converting Boolean to Integer or Float

```
bool_arr = np.array([True, False, True])
```

```
int_arr = bool_arr.astype(int)
float_arr = bool_arr.astype(float)

print(int_arr) # [1 0 1]
print(float_arr) # [1. 0. 1.]
```

5. Checking the Data Type Before and After Conversion

```
arr = np.array([1, 2, 3])
print("Before:", arr.dtype)

arr = arr.astype('float32')
print("After:", arr.dtype)
```

Why Change Data Types?

Purpose	Example
Save memory	Use float32 instead of float64
Prepare data for ML models	Convert strings/booleans to numbers
Avoid errors during calculations	Convert strings to numeric types

NumPy Array Operations

1. Scalar Operations

These are operations where a single scalar value is applied to each element of the array.

Let:

```
a = np.array([1, 2, 3, 4])
```

Arithmetic with Scalar:

- $a + 5 \rightarrow [6, 7, 8, 9]$
- $a - 2 \rightarrow [-1, 0, 1, 2]$
- $a * 3 \rightarrow [3, 6, 9, 12]$
- $a / 2 \rightarrow [0.5, 1.0, 1.5, 2.0]$
- $a ** 2 \rightarrow [1, 4, 9, 16]$

Relational with Scalar:

- $a > 2 \rightarrow [\text{False}, \text{False}, \text{True}, \text{True}]$
- $a < 4 \rightarrow [\text{True}, \text{True}, \text{True}, \text{False}]$
- $a == 3 \rightarrow [\text{False}, \text{False}, \text{True}, \text{False}]$
- $a != 1 \rightarrow [\text{False}, \text{True}, \text{True}, \text{True}]$
- $a >= 2 \rightarrow [\text{False}, \text{True}, \text{True}, \text{True}]$
- $a <= 3 \rightarrow [\text{True}, \text{True}, \text{True}, \text{False}]$

These operations are **element-wise**, meaning they apply to each value in the array.

2. Vector (Element-wise) Arithmetic

These operations are performed between two arrays of the same shape.

Let:

```
x = np.array([1, 2, 3])
```

```
y = np.array([4, 5, 6])
```

Arithmetic:

- $x + y \rightarrow [5, 7, 9]$
 - $x - y \rightarrow [-3, -3, -3]$
 - $x * y \rightarrow [4, 10, 18]$
 - $x / y \rightarrow [0.25, 0.4, 0.5]$
 - $x ** y \rightarrow [1, 32, 729]$
-

3. Vector Relational Operations

These comparisons are done element by element between two arrays.

Let:

```
x = np.array([10, 20, 30])
```

```
y = np.array([15, 20, 25])
```

Relational:

- $x > y \rightarrow [\text{False}, \text{False}, \text{True}]$
- $x < y \rightarrow [\text{True}, \text{False}, \text{False}]$
- $x == y \rightarrow [\text{False}, \text{True}, \text{False}]$
- $x != y \rightarrow [\text{True}, \text{False}, \text{True}]$
- $x >= y \rightarrow [\text{False}, \text{True}, \text{True}]$
- $x <= y \rightarrow [\text{True}, \text{True}, \text{False}]$

These return **Boolean arrays** used for filtering or logical operations.



NumPy Array Functions

```
=====
```

◆ Max, Min, Sum, Prod

These functions return **summary values** from the array.

✓ Basic Usage:

Let arr = np.array([[1, 2], [3, 4]])

- np.max(arr) → 4
- np.min(arr) → 1
- np.sum(arr) → 10
- np.prod(arr) → 24

✓ With axis:

- np.sum(arr, axis=0) → [4, 6] → (column-wise sum)
- np.sum(arr, axis=1) → [3, 7] → (row-wise sum)

Explanation:

- axis=0: Works **vertically** (down columns)
 - axis=1: Works **horizontally** (across rows)
-

◆ Mean, Median, Std, Var (Statistics Functions)

✓ Basic Usage:

Let arr = np.array([[1, 2], [3, 4]])

- np.mean(arr) → 2.5
- np.median(arr) → 2.5
- np.std(arr) → 1.118
- np.var(arr) → 1.25

✓ With axis:

- np.mean(arr, axis=0) → [2.0, 3.0]
 - np.mean(arr, axis=1) → [1.5, 3.5]
-

◆ Trigonometric Functions

These work **element-wise** on angle values in **radians**.

Let arr = np.array([0, np.pi/2])

- np.sin(arr) → [0.0, 1.0]
 - np.cos(arr) → [1.0, 0.0]
 - np.tan(arr) → [0.0, undefined]
-

◆ Dot Product

Used for **matrix multiplication** or **inner product** of vectors.

✓ Example:

Let

a = np.array([1, 2])

b = np.array([3, 4])

- np.dot(a, b) → 11 (1×3 + 2×4)

For matrices:

Let

A = np.array([[1, 2], [3, 4]])

B = np.array([[5, 6], [7, 8]])

- np.dot(A, B) →

lua

CopyEdit

[[19, 22],

[43, 50]]

◆ Logarithm & Exponential Functions

Let arr = np.array([1, 2])

- np.log(arr) → [0.0, 0.693]
 - np.exp(arr) → [2.718, 7.389]
-

◆ Rounding Functions

Let arr = np.array([1.4, 2.6, 3.5])

- np.round(arr) → [1.0, 3.0, 4.0]

- `np.floor(arr) → [1.0, 2.0, 3.0]`
- `np.ceil(arr) → [2.0, 3.0, 4.0]`

NumPy Indexing and Slicing

◆ 1D Array

Let:

```
arr = np.array([10, 20, 30, 40, 50])
```

Indexing:

- `arr[0] → 10`
- `arr[-1] → 50 (last element)`
- `arr[2] → 30`

Slicing:

- `arr[1:4] → [20, 30, 40]`
- `arr[:3] → [10, 20, 30]`
- `arr[2:] → [30, 40, 50]`
- `arr[::-2] → [10, 30, 50] (every 2nd element)`

◆ 2D Array

Let:

```
arr = np.array([[1, 2, 3], [4, 5, 6], [7, 8, 9]])
```

Indexing:

- `arr[0][1] or arr[0, 1] → 2`
- `arr[2][2] or arr[2, 2] → 9`
- `arr[-1, -1] → 9 (last row, last column)`

Row Access:

- `arr[0] → [1, 2, 3] (first row)`

- $\text{arr}[1, :] \rightarrow [4, 5, 6]$ (second row, all columns)

Column Access:

- $\text{arr}[:, 0] \rightarrow [1, 4, 7]$ (first column)
- $\text{arr}[:, 2] \rightarrow [3, 6, 9]$ (third column)

Slicing:

- $\text{arr}[0:2, 1:3] \rightarrow$

$[[2, 3],$

$[5, 6]]$

- $\text{arr}[:2, :] \rightarrow$ first 2 rows
 - $\text{arr}[:, 1:] \rightarrow$ all rows, columns from index 1 onward
-

◆ 3D Array

Let:

```
arr = np.array([
    [[1, 2], [3, 4]],
    [[5, 6], [7, 8]]
])
```

Shape: (2, 2, 2)

Indexing:

- $\text{arr}[0, 0, 0] \rightarrow 1$
- $\text{arr}[1, 1, 1] \rightarrow 8$
- $\text{arr}[0] \rightarrow$

$[[1, 2],$

$[3, 4]]$

Slicing:

- $\text{arr}[0, :, :] \rightarrow$ 2D slice from first block
 $\rightarrow [[1, 2], [3, 4]]$
- $\text{arr}[:, 1, :] \rightarrow$ second row from all blocks
 $\rightarrow [[3, 4], [7, 8]]$

- arr[:, :, 0] → first column from every 2x2
→ [[1, 3], [5, 7]]
-

NumPy Iteration (1D, 2D, 3D Arrays)

◆ 1D Array Iteration

Let:

```
arr = np.array([10, 20, 30])
```

Iterating:

```
for i in arr:
```

```
    print(i)
```

Output:

```
10  
20  
30
```

Each element is directly accessed one by one.

◆ 2D Array Iteration

Let:

```
arr = np.array([[1, 2, 3], [4, 5, 6]])
```

Iterating Row by Row:

```
for row in arr:
```

```
    print(row)
```

Output:

```
[1 2 3]  
[4 5 6]
```

Iterating Each Element (Nested Loop):

```
for row in arr:
```

```
for item in row:
```

```
    print(item)
```

Output:

```
1 2 3 4 5 6
```

Using .flat to Flatten:

```
for item in arr.flat:
```

```
    print(item)
```

◆ **3D Array Iteration**

Let:

```
arr = np.array([
```

```
    [[1, 2], [3, 4]],
```

```
    [[5, 6], [7, 8]]
```

```
])
```

Shape: (2, 2, 2)

Iterating Block by Block:

```
for block in arr:
```

```
    print(block)
```

Output:

```
[[1 2]
```

```
[3 4]]
```

```
[[5 6]
```

```
[7 8]]
```

Nested Loop for All Elements:

```
for block in arr:
```

```
    for row in block:
```

```
        for item in row:
```

```
            print(item)
```

Output:

```
1 2 3 4 5 6 7 8
```

Flattened Iteration:

```
for item in arr.flat:
```

```
    print(item)
```

Note on .nditer()

NumPy also provides `np.nditer()` for efficient and flexible iteration over arrays of any shape.

```
for x in np.nditer(arr):
```

```
    print(x)
```

Works for **1D, 2D, 3D** arrays and simplifies nested loops.

NumPy: reshape, transpose, and ravel

◆ **1. reshape()**

Used to change the **shape** of the array **without changing data**.

Syntax:

```
array.reshape(new_shape)
```

Example:

```
arr = np.array([1, 2, 3, 4, 5, 6])
```

```
reshaped = arr.reshape(2, 3)
```

Output:

```
[[1, 2, 3],
```

```
[4, 5, 6]]
```

- The **total number of elements** must remain the same.
- You can use `-1` to auto-calculate one dimension:
- `arr.reshape(3, -1) → shape will be (3, 2)`

◆ 2. transpose()

Used to **swap the axes** of an array. Commonly used to **convert rows to columns and vice versa**.

✓ Syntax:

```
array.transpose()
```

✓ Example:

```
arr = np.array([[1, 2], [3, 4]])
```

```
transposed = arr.transpose()
```

Output:

```
[[1, 3],
```

```
[2, 4]]
```

For 2D: switches rows and columns.

For 3D: can rearrange multiple axes using:

```
arr.transpose(1, 0, 2)
```

◆ 3. ravel()

Returns a **flattened 1D array** from any n-dimensional array. Unlike reshape, ravel() is often a **view** (no copy).

✓ Syntax:

```
array.ravel()
```

✓ Example:

```
arr = np.array([[1, 2], [3, 4]])
```

```
flattened = arr.ravel()
```

Output:

```
[1, 2, 3, 4]
```

- Similar to flatten(), but ravel() is **faster** and uses less memory.

NumPy: vstack, hstack, vsplit, hsplit

=====

◆ 1. np.vstack() – Vertical Stacking

Stacks arrays **vertically** (along rows). The arrays are stacked **one on top of the other**.

Syntax:

```
np.vstack((arr1, arr2, ...))
```

Example:

```
arr1 = np.array([1, 2, 3])  
arr2 = np.array([4, 5, 6])  
stacked = np.vstack((arr1, arr2))
```

Output:

```
[[1, 2, 3],  
 [4, 5, 6]]
```

- The **number of columns** must be the same.
-

◆ 2. np.hstack() – Horizontal Stacking

Stacks arrays **horizontally** (along columns). The arrays are stacked **side by side**.

Syntax:

```
np.hstack((arr1, arr2, ...))
```

Example:

```
arr1 = np.array([1, 2, 3])  
arr2 = np.array([4, 5, 6])  
stacked = np.hstack((arr1, arr2))
```

Output:

```
[1, 2, 3, 4, 5, 6]
```

- The **number of rows** must be the same.

◆ 3. np.vsplit() – Vertical Splitting

Splits the array **vertically** (along rows). The array is split into **multiple sub-arrays** along the first axis (rows).

✓ Syntax:

```
np.vsplit(arr, indices_or_sections)
```

✓ Example:

```
arr = np.array([[1, 2, 3], [4, 5, 6], [7, 8, 9]])
```

```
split_arr = np.vsplit(arr, 3)
```

Output:

```
[array([[1, 2, 3]]),
```

```
array([[4, 5, 6]]),
```

```
array([[7, 8, 9]])]
```

- **Divides the array** into the specified number of **rows**.
-

◆ 4. np.hsplit() – Horizontal Splitting

Splits the array **horizontally** (along columns). The array is split into **multiple sub-arrays** along the second axis (columns).

✓ Syntax:

```
np.hsplit(arr, indices_or_sections)
```

✓ Example:

```
arr = np.array([[1, 2, 3], [4, 5, 6], [7, 8, 9]])
```

```
split_arr = np.hsplit(arr, 3)
```

Output:

```
[array([[1], [4], [7]]),
```

```
array([[2], [5], [8]]),
```

```
array([[3], [6], [9]])]
```

- **Divides the array** into the specified number of **columns**.
-

