

**STAT 2131:**  
**Applied Statistical Methods I**  
**HW #3**  
**Due Thursday, Sep 10**

1. KNNL 3.14. See slides 15-18 of Lecture 5 for a review of how to apply an F test when  $X$  takes discrete values.
2. KNNL 3.18. The data for this problem has been uploaded to blackboard. In part d, a normal probability plot refers to a normal Q-Q plot (standard normal quantiles vs. data quantiles).

3.14. Refer to **Plastic hardness** Problem 1.22.

- a. Perform the  $F$  test to determine whether or not there is lack of fit of a linear regression function; use  $\alpha = .01$ . State the alternatives, decision rule, and conclusion.
- b. Is there any advantage of having an equal number of replications at each of the  $X$  levels? Is there any disadvantage?
- c. Does the test in part (a) indicate what regression function is appropriate when it leads to the conclusion that the regression function is not linear? How would you proceed?

- 3.18. **Production time.** In a manufacturing study, the production times for 111 recent production runs were obtained. The table below lists for each run the production time in hours ( $Y$ ) and the production lot size ( $X$ ).

$i$ :	1	2	3	...	109	110	111
$X_i$ :	15	9	7	...	12	9	15
$Y_i$ :	14.28	8.80	12.49	...	16.37	11.45	15.78

- Prepare a scatter plot of the data. Does a linear relation appear adequate here? Would a transformation on  $X$  or  $Y$  be more appropriate here? Why?
- Use the transformation  $X' = \sqrt{X}$  and obtain the estimated linear regression function for the transformed data.
- Plot the estimated regression line and the transformed data. Does the regression line appear to be a good fit to the transformed data?
- Obtain the residuals and plot them against the fitted values. Also prepare a normal probability plot. What do your plots show?
- Express the estimated regression function in the original units.