

## **Thesis description presentation**

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“Measurements of nuclear fragmentation differential cross section in an energy range between 200 MeV/n and 400 MeV/n at the FOOT experiment”

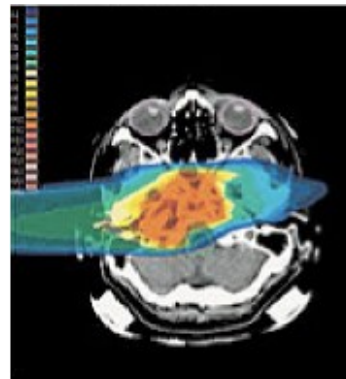
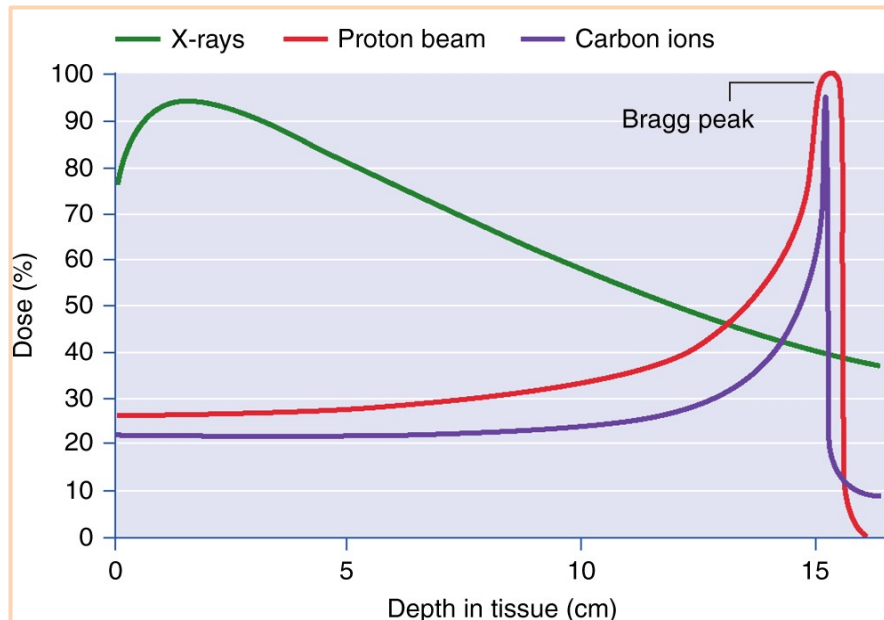
Candidate:  
Giacomo Ubaldi

28/06/2022

# The FOOT experiment



## *hadrontherapy*



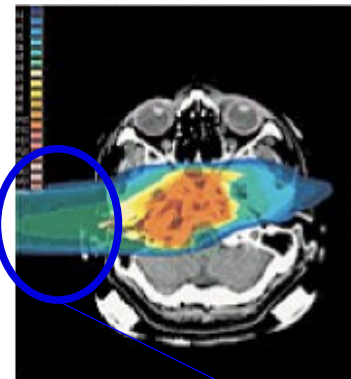
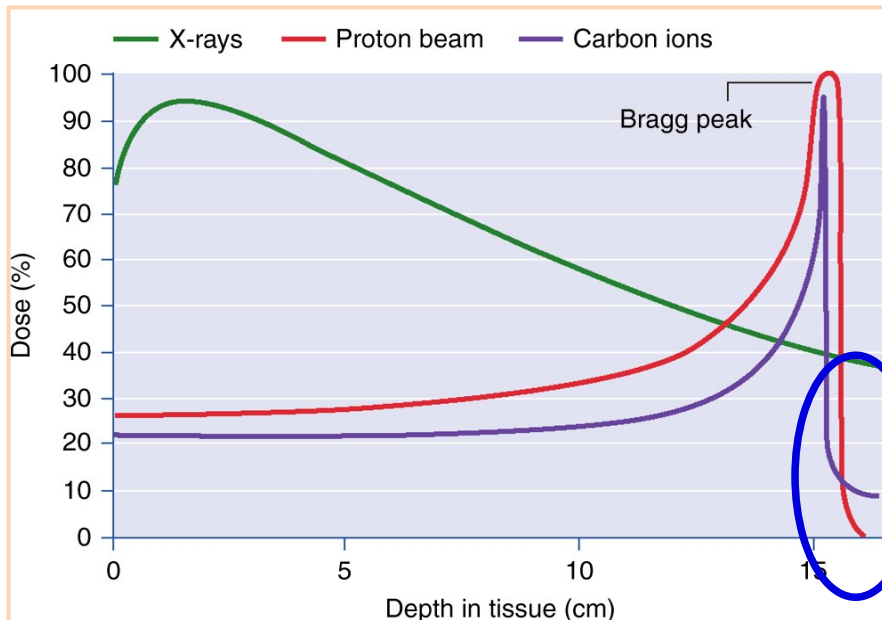
## *Space radioprotection*



# The FOOT experiment

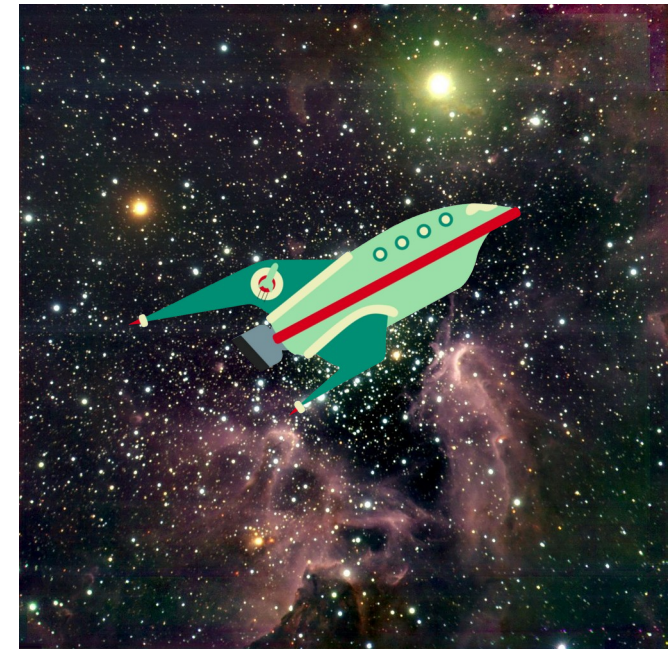


## *hadrontherapy*



Fragmentation!

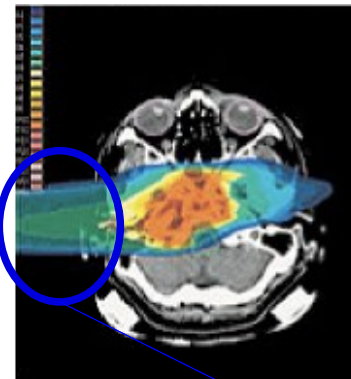
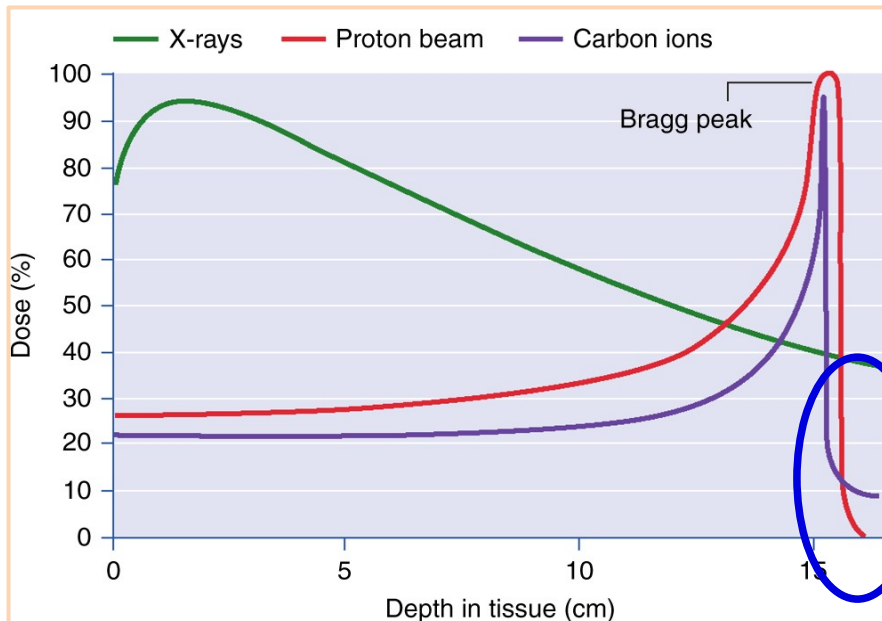
## *Space radioprotection*



# The FOOT experiment

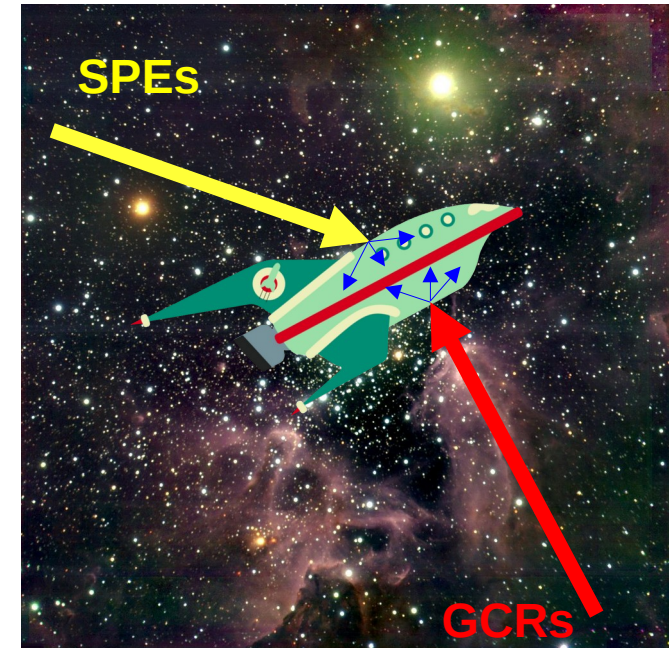


## hadrontherapy



Fragmentation!

## Space radioprotection





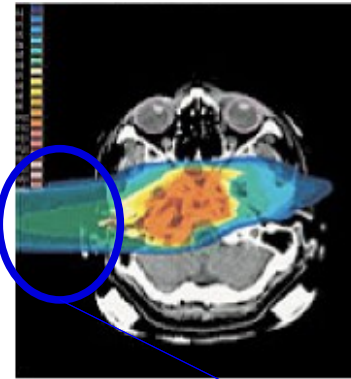
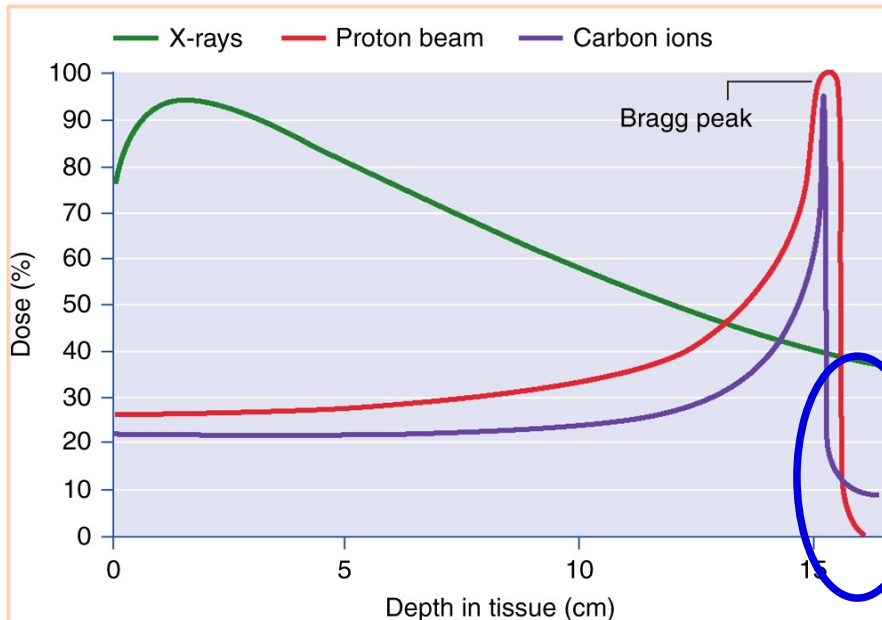
# The FOOT experiment



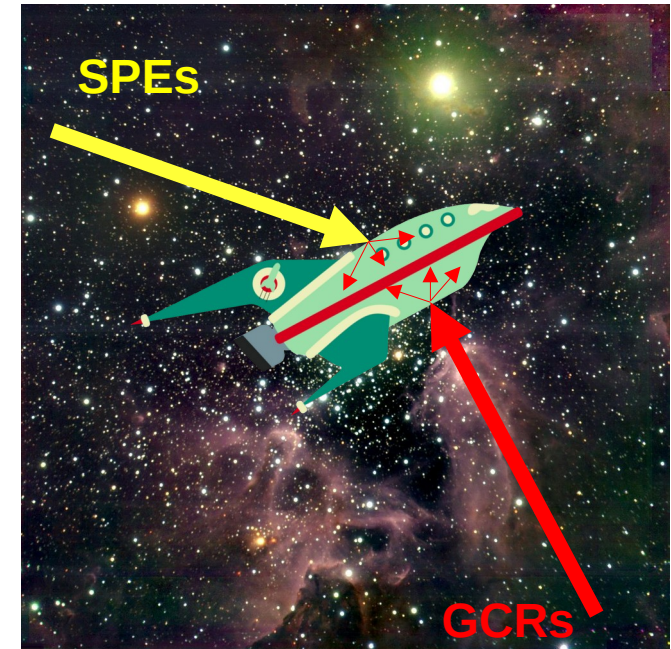
## Goal:

double differential projectile and target **nuclear cross sections** measurements with  $\sigma < 5\%$

- Fixed target collisions
- Beam energies between 200 MeV/u and 700 MeV/u for **hadrontherapy** and **space radioprotection** topics
- **table top setup** to be moved according to beam facility availability
- Particle identification by measuring all kinematic quantities

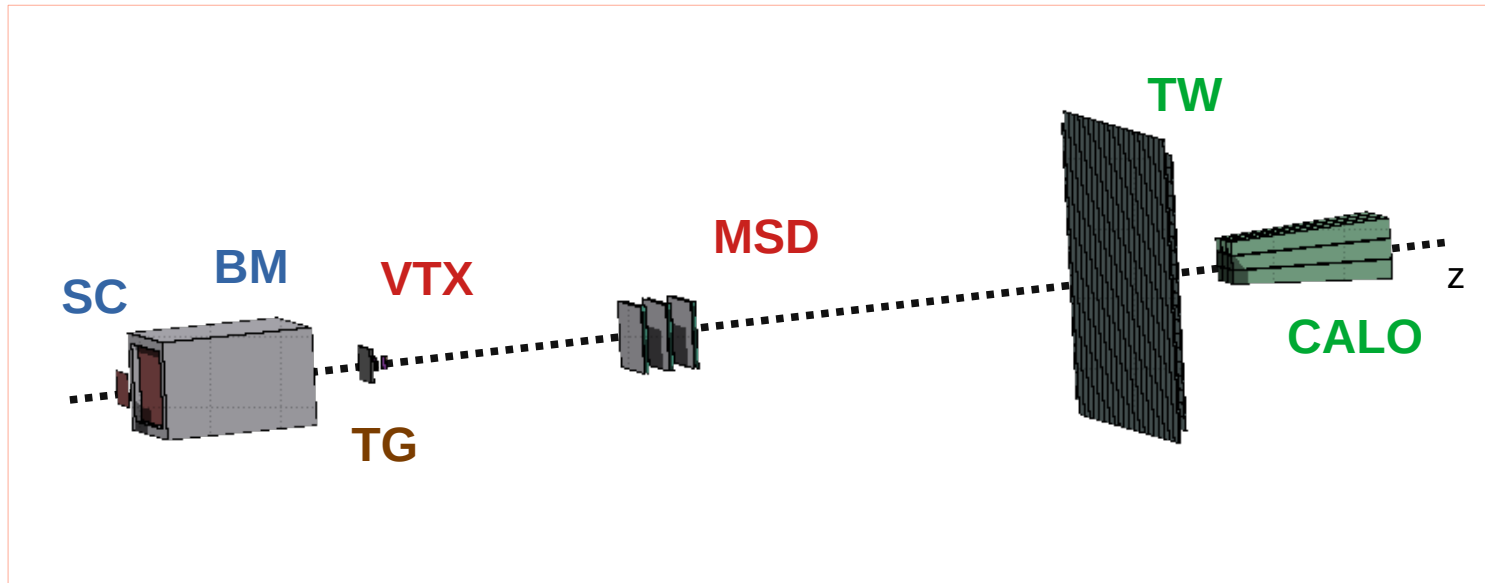


Fragmentation!

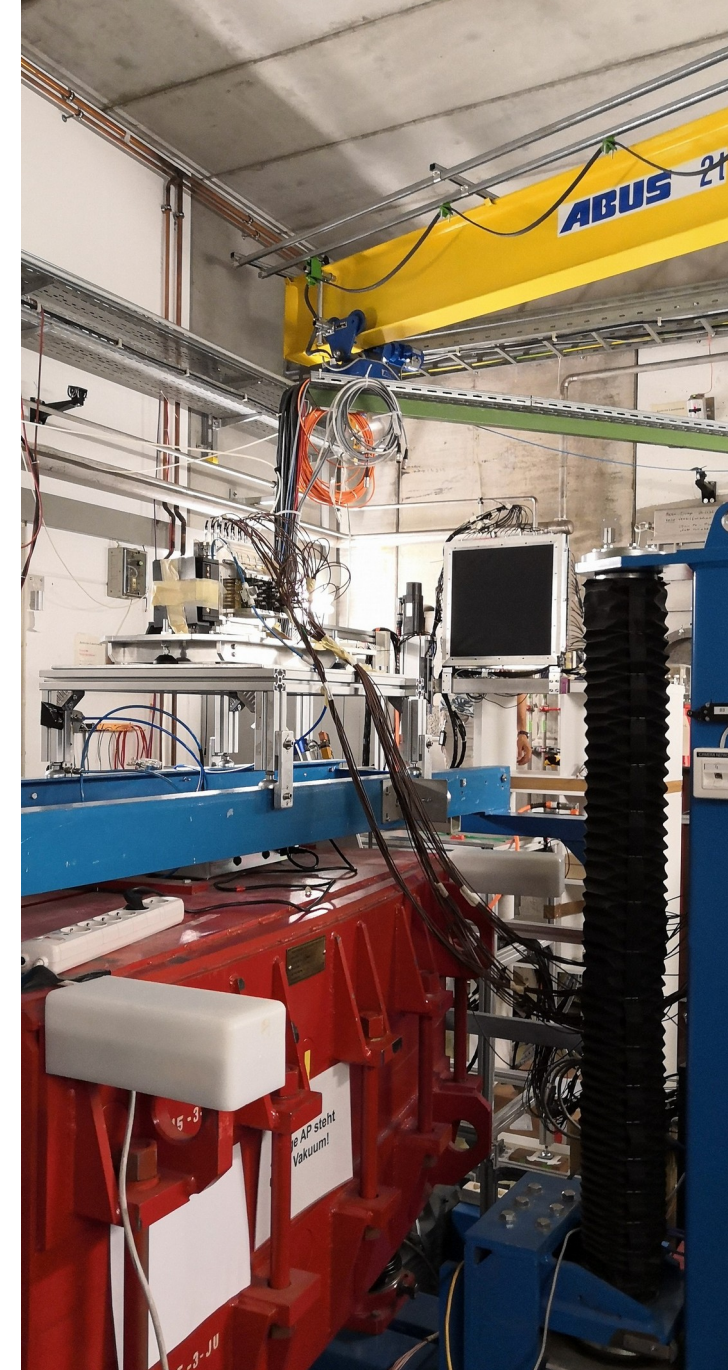


# GSI 2021 analysis

- $^{16}\text{O}$  400 MeV/u on 5 mm C target
- Real data taken at GSI in 2021
- Analysis implemented in **SHOE**
- Partial setup: no tracker, only one module of calorimeter



**First preliminary goal:**  
charge changing angular differential cross section



# Differential cross section

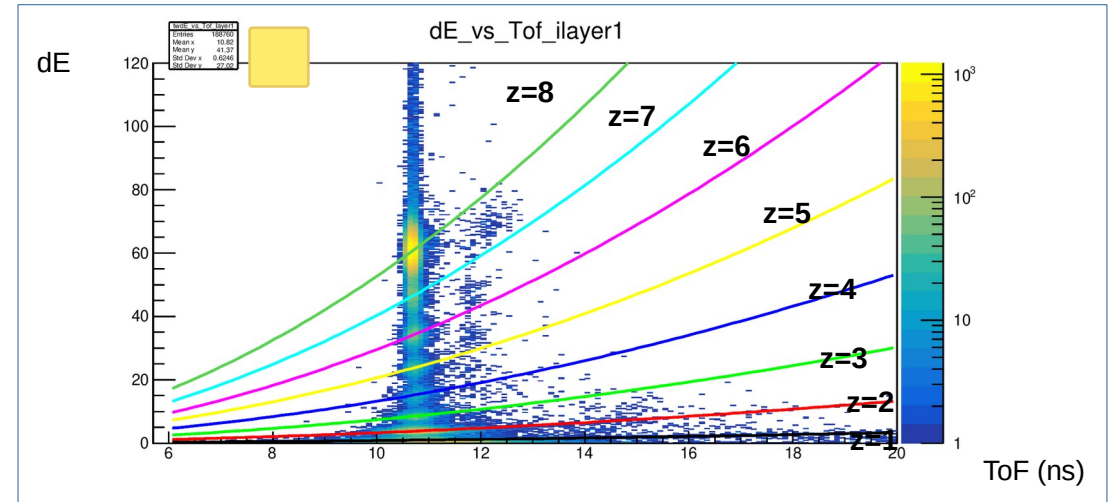
$$\frac{d\sigma}{d\theta} = \frac{(Y_f - B_f)^u}{N_{beam} \cdot N_{target} \cdot \Delta\theta \cdot \epsilon}$$

# Fragment identification

$$\frac{d\sigma}{d\theta} = \frac{(Y_f - B_f)^u}{N_{beam} \cdot N_{target} \cdot \Delta\theta \cdot \epsilon}$$

- MC data

*TW charge reconstruction algorithm*



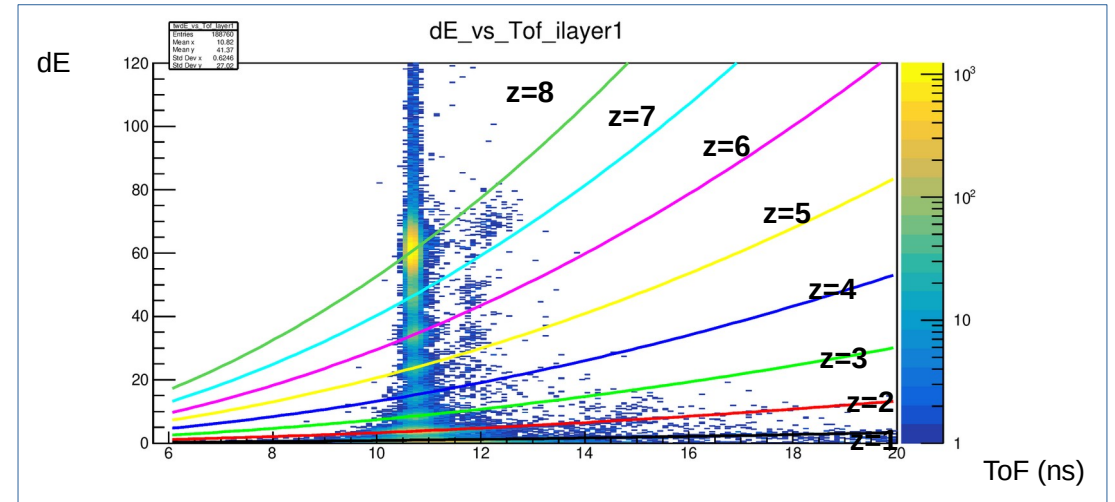


# Fragment identification

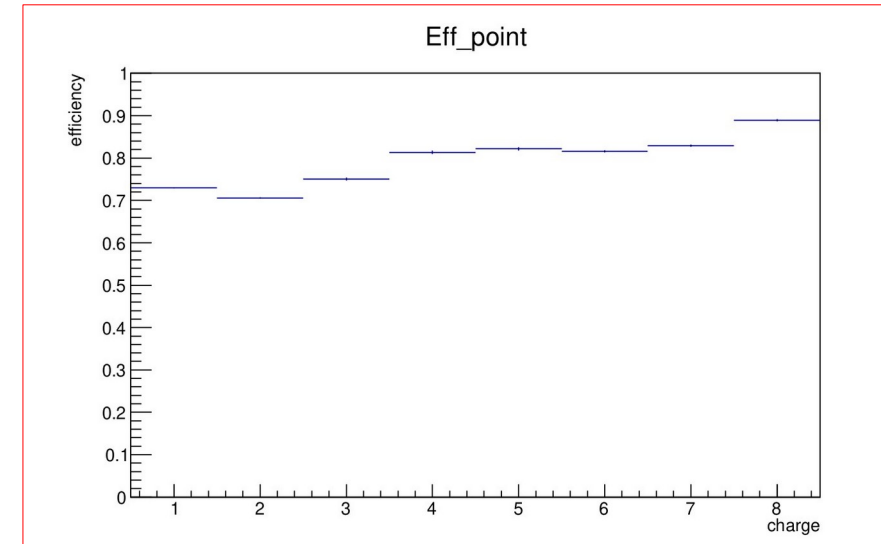
$$\frac{d\sigma}{d\theta} = \frac{(Y_f - B_f)^u}{N_{beam} \cdot N_{target} \cdot \Delta\theta \cdot \epsilon}$$

- MC data

*TW charge reconstruction algorithm*



*charge reconstruction efficiency*

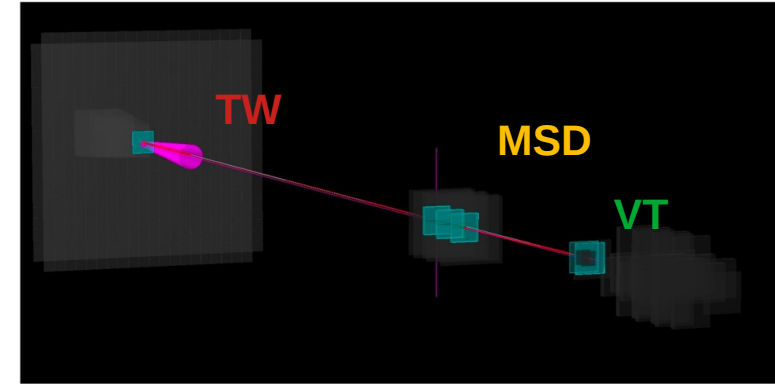


# Track reconstruction

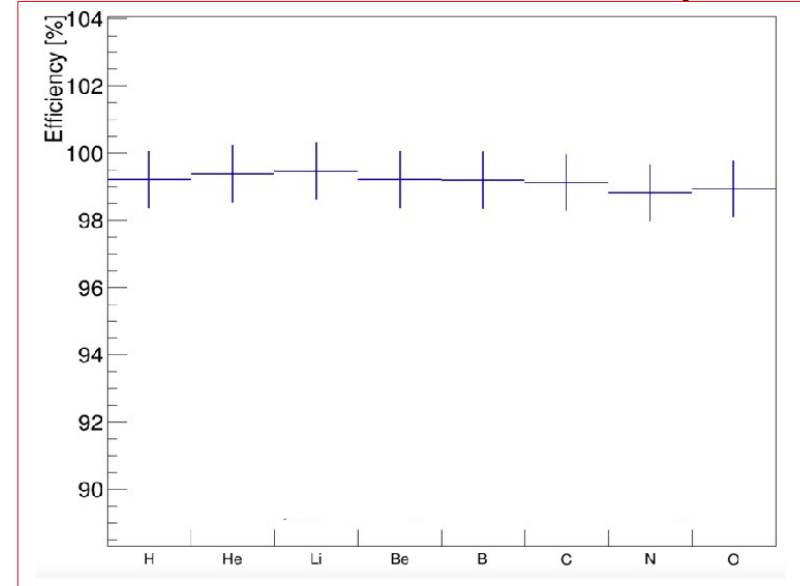
$$\frac{d\sigma}{d\theta} = \frac{(Y_f - B_f)^u}{N_{beam} \cdot N_{target} \cdot \Delta\theta \cdot \epsilon}$$

- MC data

*Kalman Filter reconstruction of a track*



*Track reconstruction efficiency*



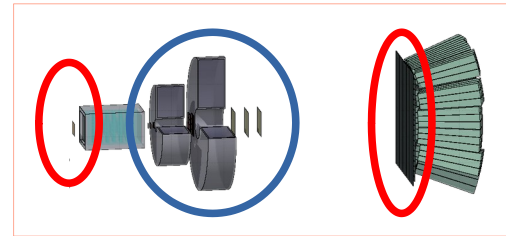
# Isotope identification

$$\frac{d\sigma}{d\theta} = \frac{(Y_f - B_f)^u}{N_{beam} \cdot N_{target} \cdot \Delta\theta \cdot \epsilon}$$

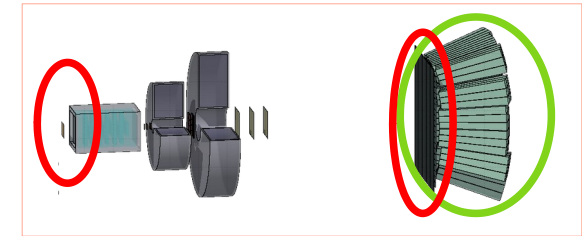
- MC data

*Mass reconstruction using all FOOT subdetectors:*

$$A_1 = \frac{p}{U\beta c\gamma}$$



$$A_2 = \frac{E_k}{Uc^2(\gamma - 1)}$$



$$A_3 = \frac{p^2c^2 - E_k^2}{2Uc^2E_k}$$



# Isotope identification

$$\frac{d\sigma}{d\theta} = \frac{(Y_f - B_f)^u}{N_{beam} \cdot N_{target} \cdot \Delta\theta \cdot \epsilon}$$

- MC data

## Augmented Lagrangian Method

- Minimization of

$$L(\vec{x}, \lambda, \mu) \equiv f(\vec{x}) - \sum_a \lambda_a c_a(\vec{x}) + \frac{1}{2\mu} \sum_a c_a^2(\vec{x})$$

where

$$f(\vec{x}) = \left( \frac{TOF - T}{\sigma_{TOF}} \right)^2 + \left( \frac{p - P}{\sigma_p} \right)^2 + \left( \frac{E_k - K}{\sigma_{E_k}} \right)^2$$

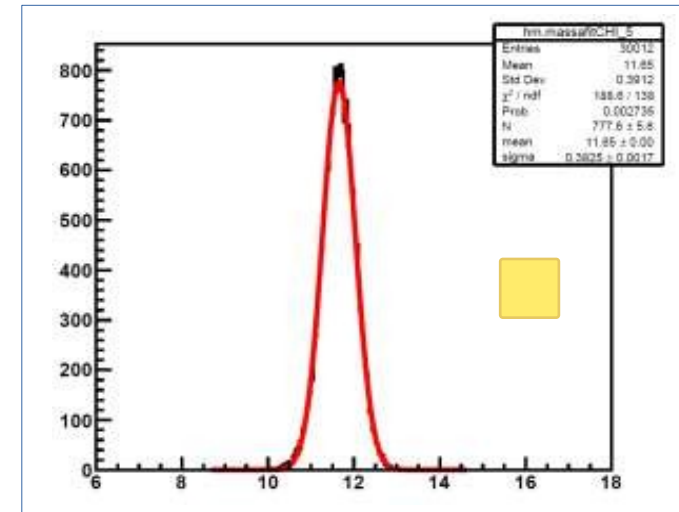
$$c_a(\vec{x}) = A - A_a$$

Es. **A = 12**

$$A_{ALM} = 11.66 \pm 0.38$$

$$A/\sigma_A = 3.2 \%$$

$$\chi^2 < 5$$



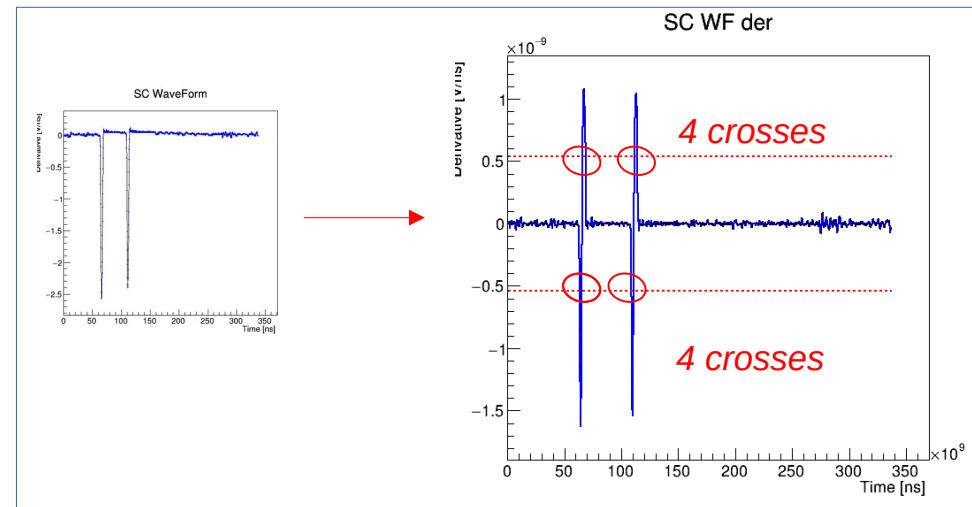


# Pile-up removal

$$\frac{d\sigma}{d\theta} = \frac{(Y_f - \textcircled{B_f})^u}{N_{beam} \cdot N_{target} \cdot \Delta\theta \cdot \epsilon}$$

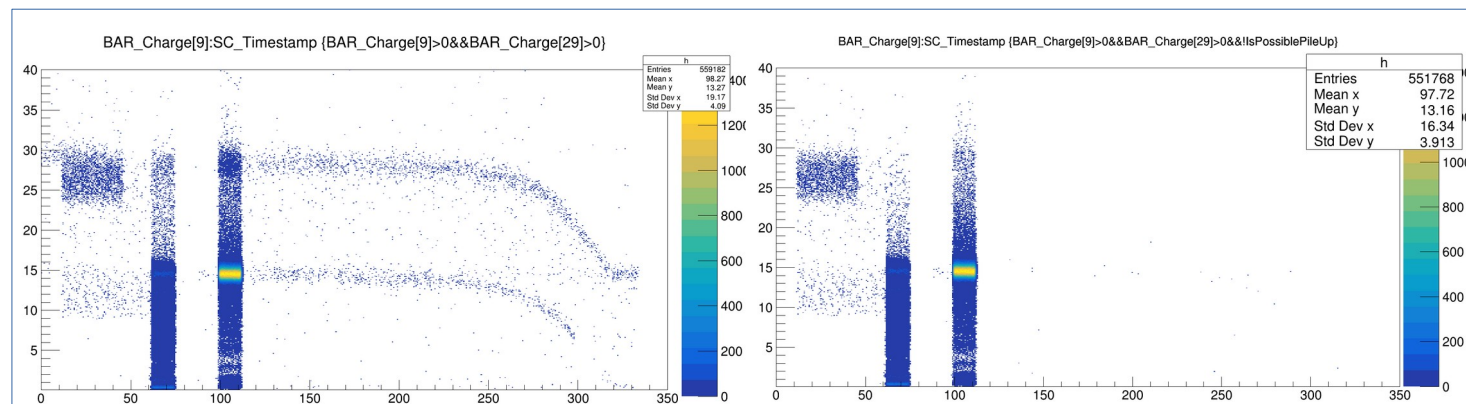
- Real data

constant threshold **discrimination method**



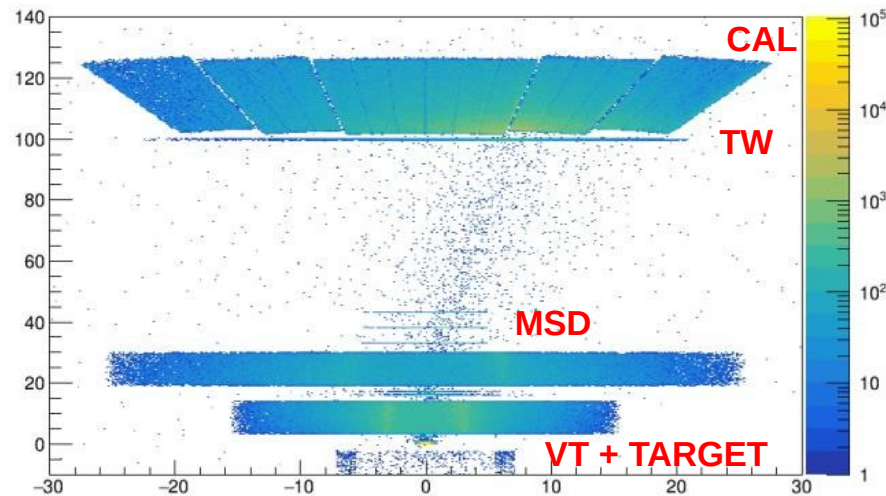
**pileup projectile:** >4 crosses

**Pile-up rejection ~ 1%**

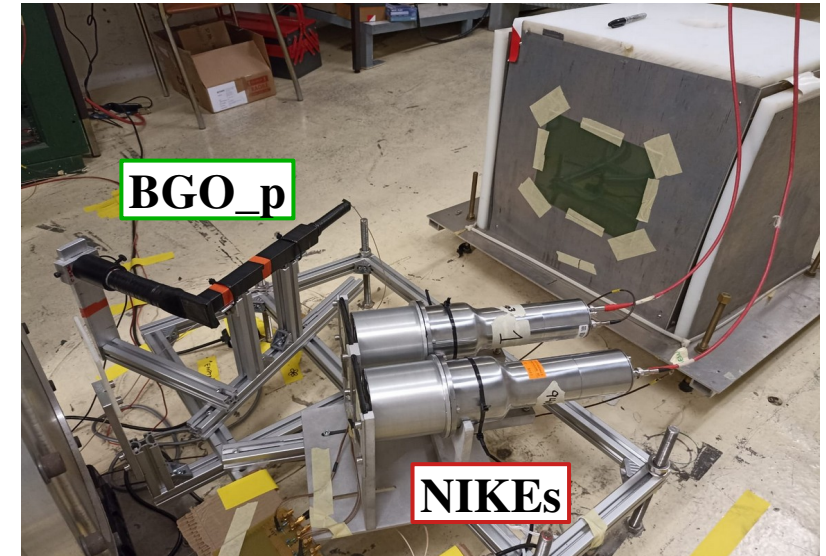


# Fast neutrons detectors

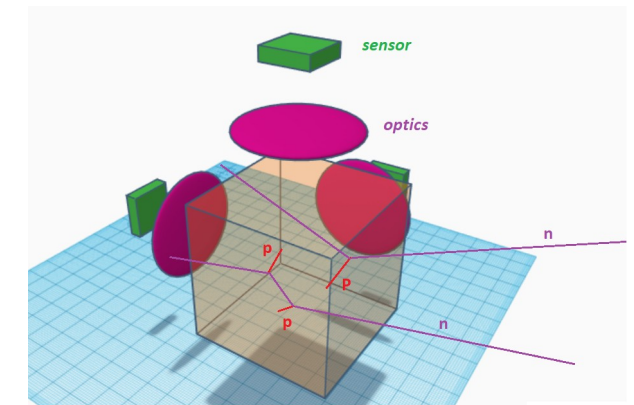
High **neutron production** as a consequence of fragmentation with detectors



Purpose to  
Add neutron  
detectors:



- BC-501A liquid scintillator
- BGO Phoswich



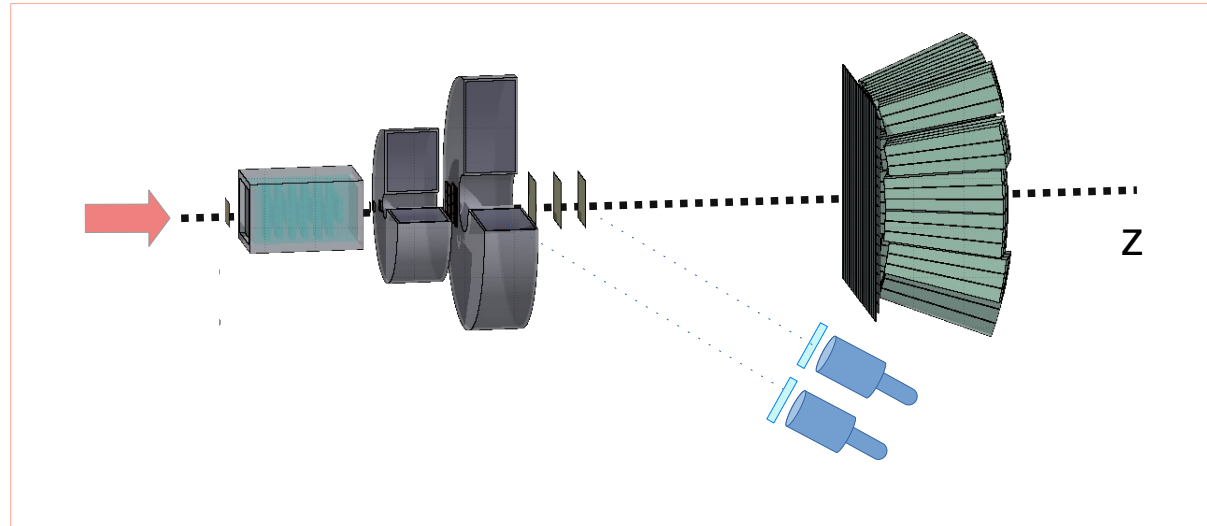
- recoil-proton track  
imaging detector

# Future data taking

Foreseen within 2023 – 2024



- All detectors will be present

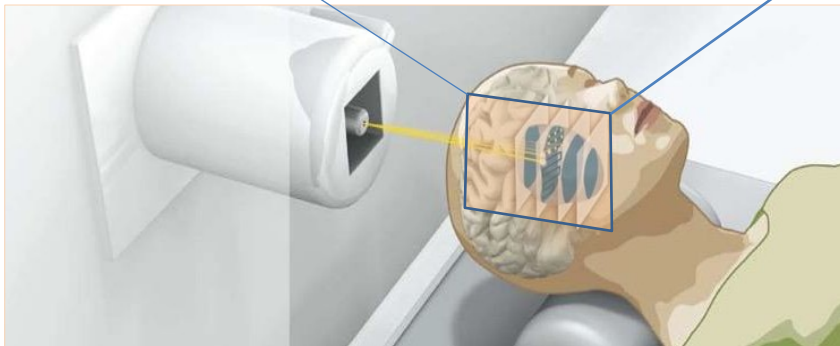
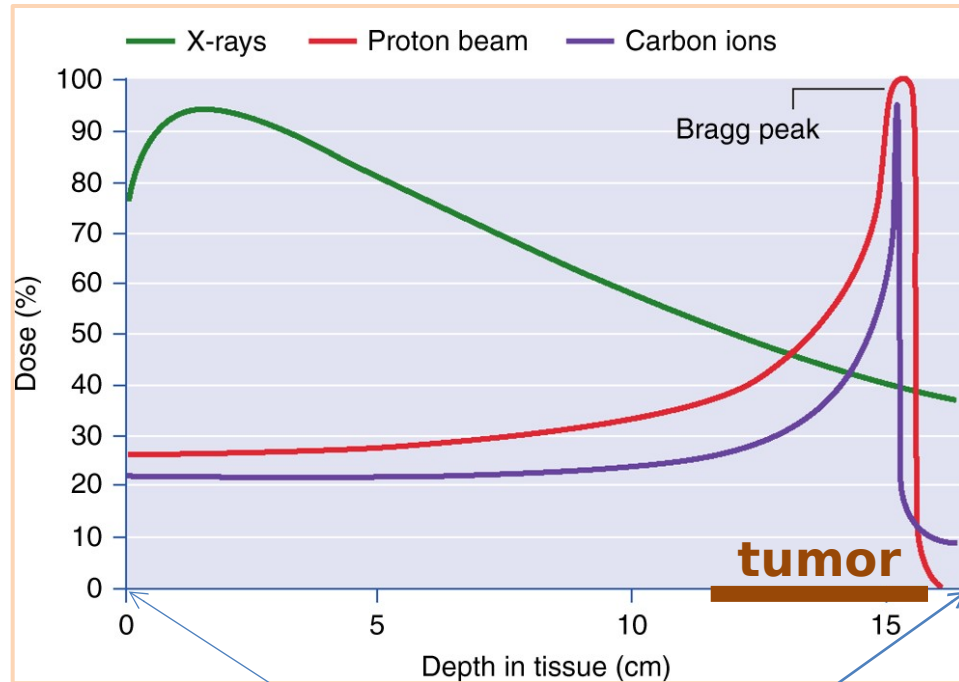


- Beam tests for calibration of all detectors together
- Compact analysis strategy needed
- Implementation of neutron detectors in analysis software
- Inverse kinematic application

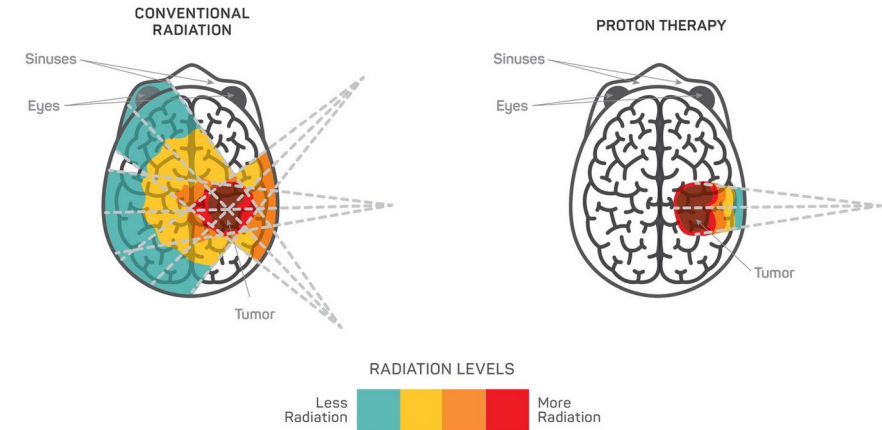
# Back up slides



# Hadrontherapy



depth- dose profile for X-rays and charged particles as a beam

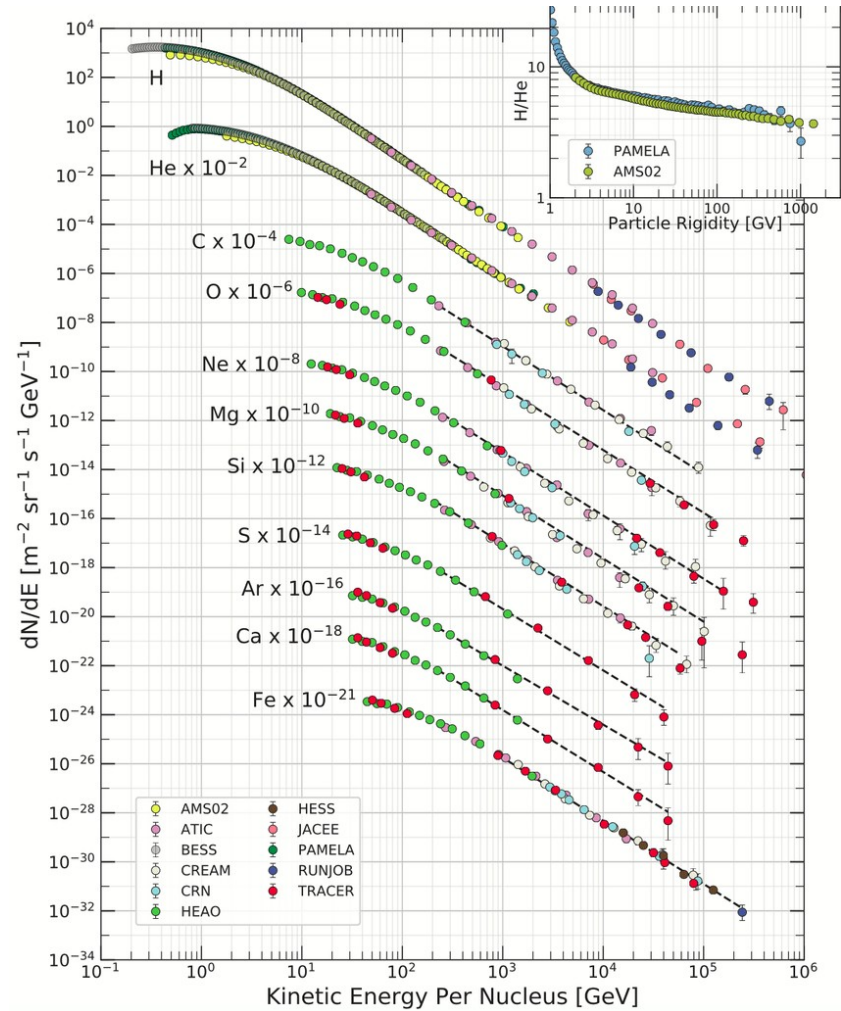


Sketch of a treatment planning system on brain-located tumor

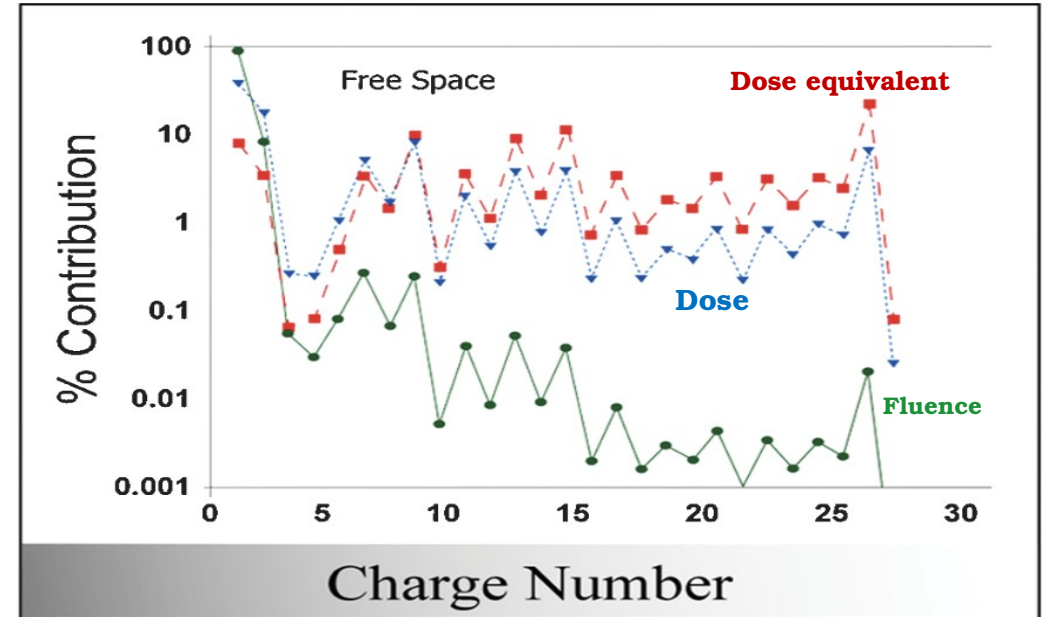
Hadrontherapy vs radiotherapy:

- **Finite range**
- **Localized dose profile**
- **Nuclear fragmentation**

# Space radioprotection



GCR fluence

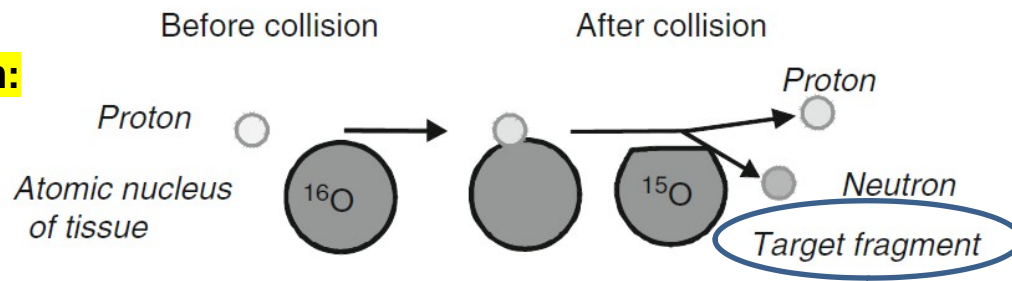


Particles contribution in Fluence, dose and equivalent dose

# Nuclear Fragmentation

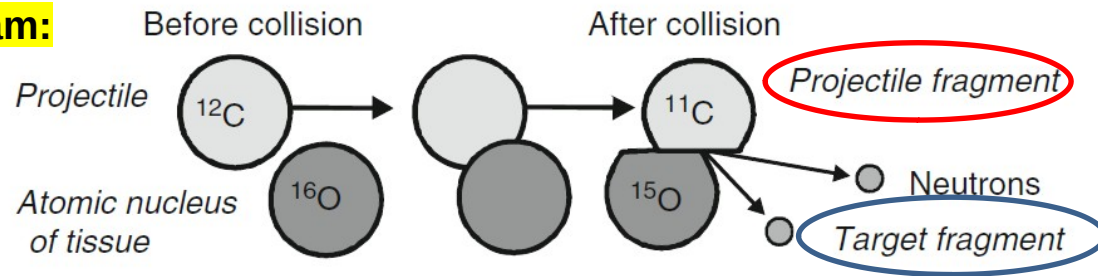
## Proton beam:

~ 200 MeV

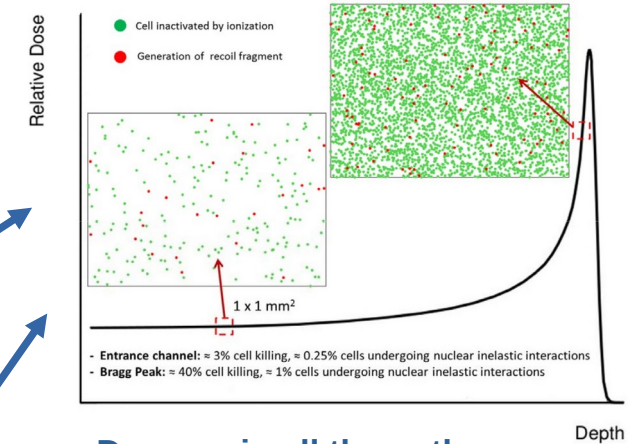


## Carbon beam:

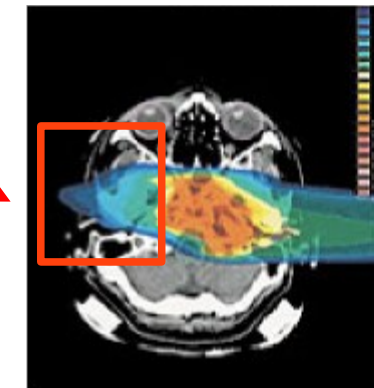
~ 400 MeV/u



Sketch of Nuclear fragmentation



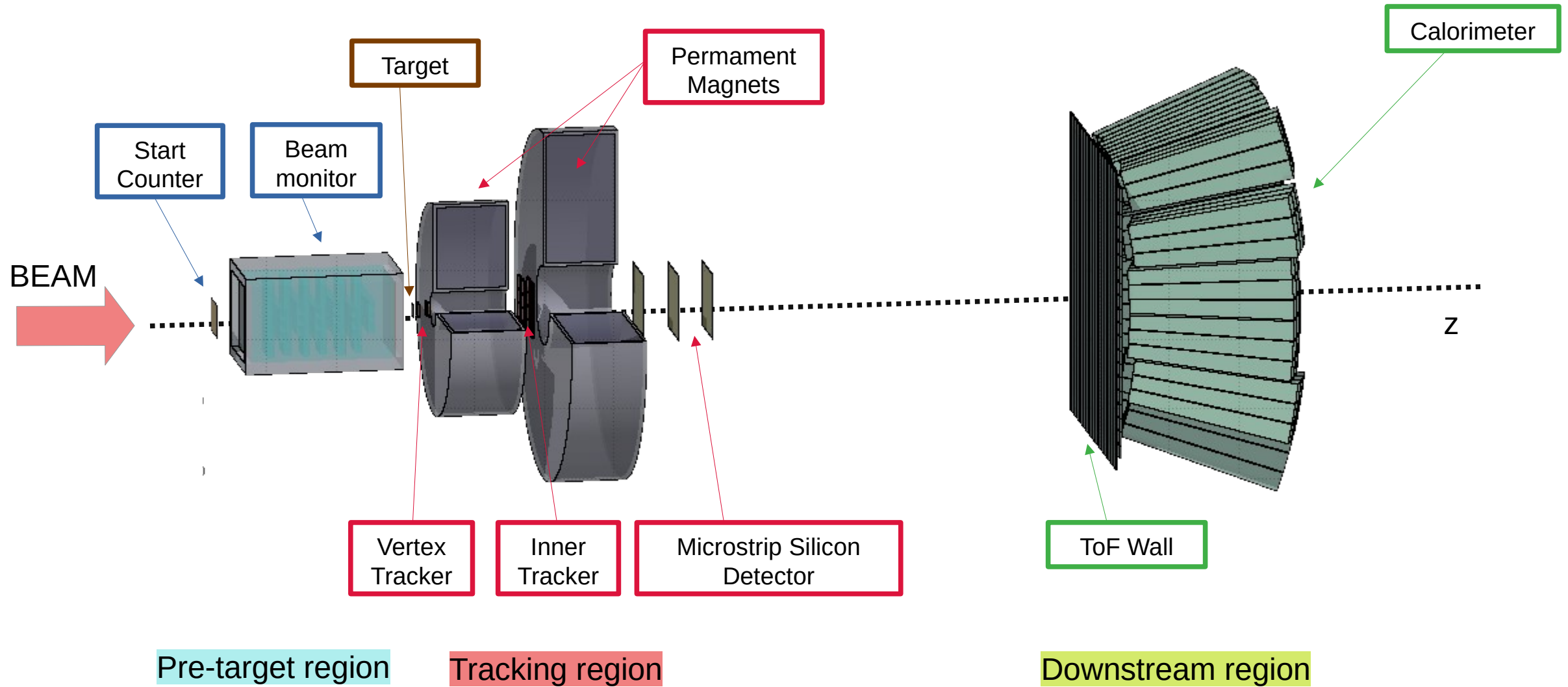
Damage in all the path



BEAM

Damage after the BP

# The FOOT detector





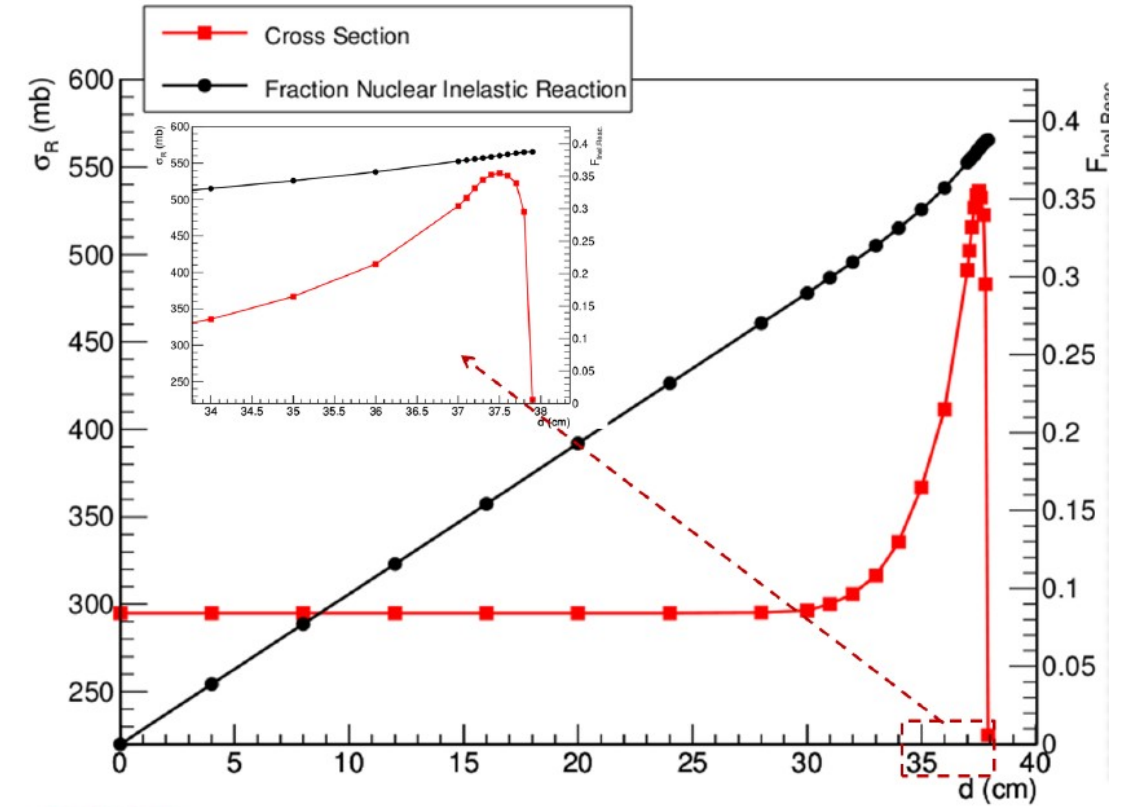
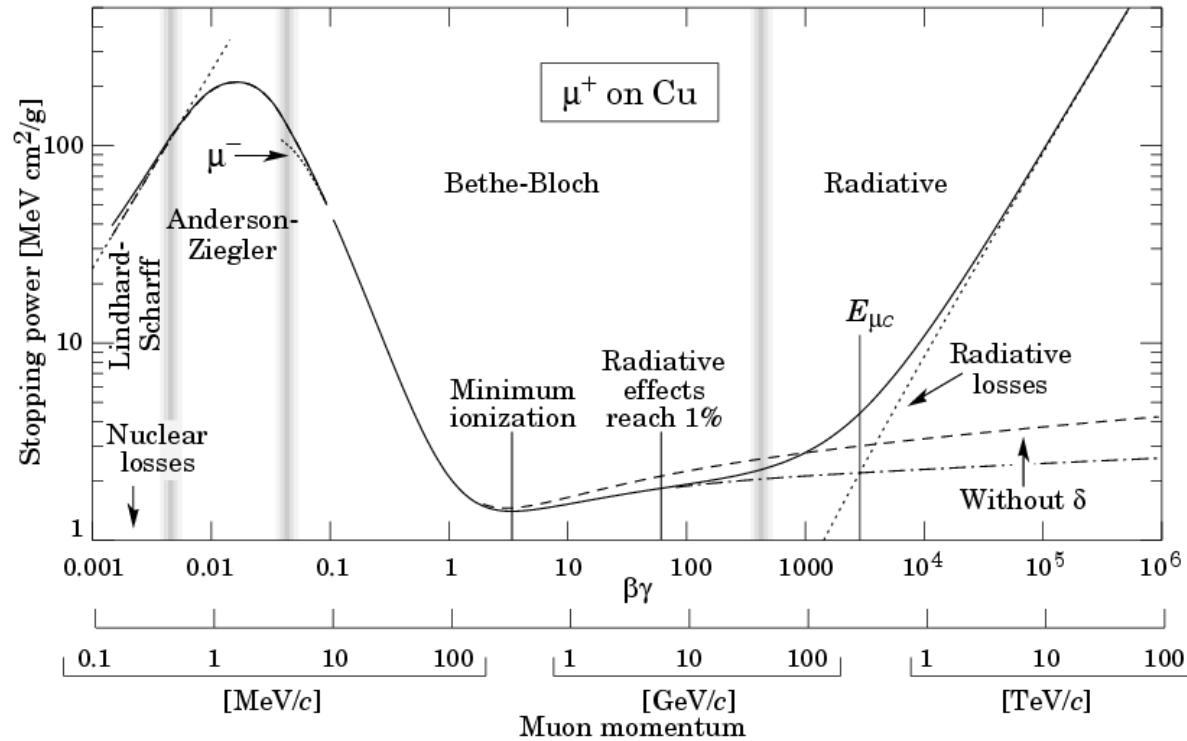
# Differential Cross section

The diagram illustrates the formula for the differential cross-section,  $\frac{d\sigma}{d\theta}$ , with various components labeled in boxes and connected to the formula by arrows:

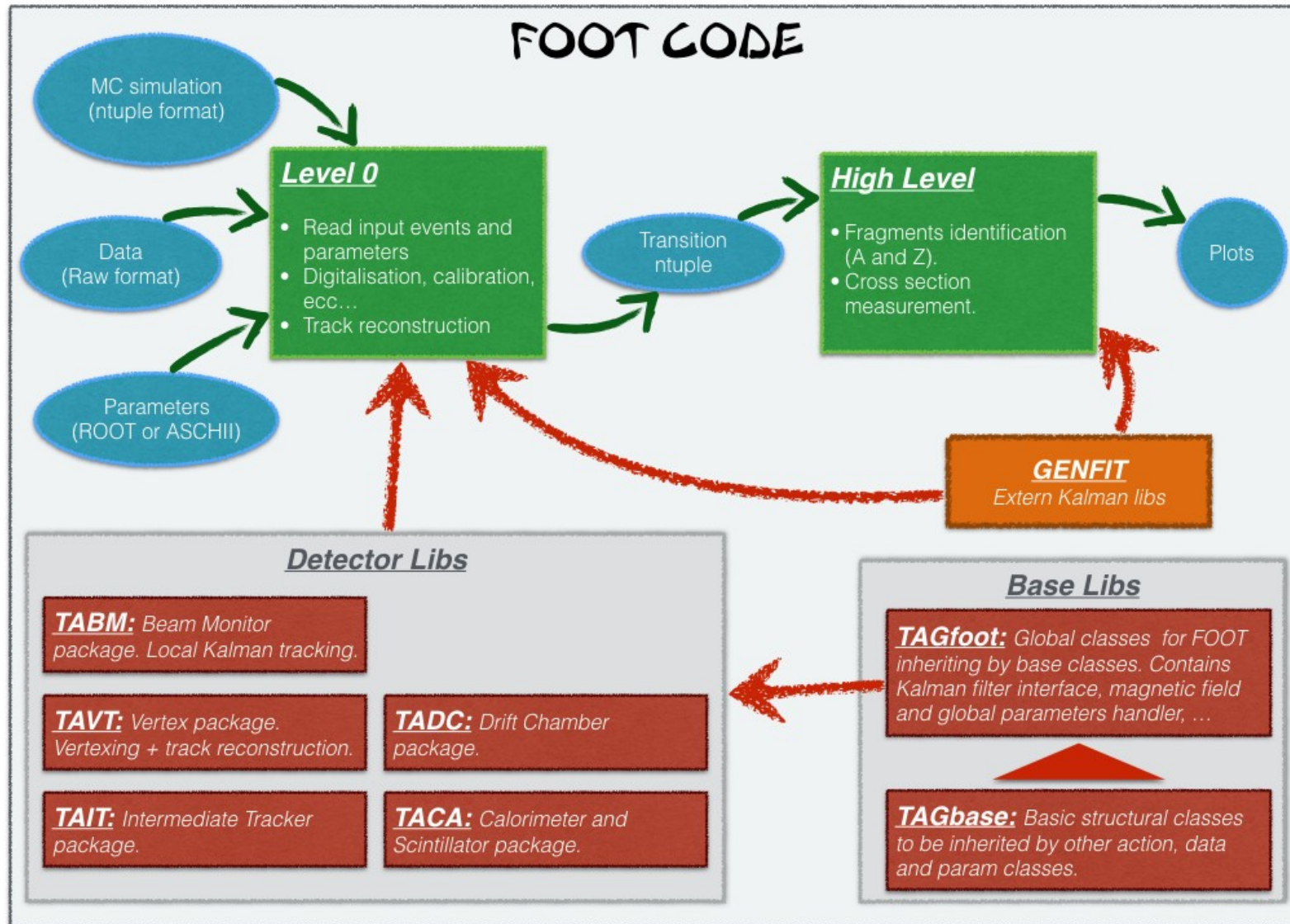
- Yield of all fragments** (red box) points to  $Y_f$  in the numerator.
- Background** (black box) points to  $B_f$  in the numerator.
- unfolding** (black box) points to the superscript  $u$  in the numerator.
- efficiency** (red box) points to  $\epsilon$  in the denominator.
- N° of primary events** (blue box) points to  $N_{beam}$  in the denominator.
- N° of scattered centers** (blue box) points to  $N_{target}$  in the denominator.
- Phase space** (green box) points to  $\Delta\theta$  in the denominator.

$$\frac{d\sigma}{d\theta} = \frac{(Y_f - B_f)^u}{N_{beam} \cdot N_{target} \cdot \Delta\theta \cdot \epsilon}$$

# Bethe Bloch vs nuclear cross section



# SHOE organization



# Kalman filter in pills

1. Take an ideal particle in vacuum. If we add air + detector layers, trajectory changes due to M.S. and energy loss.

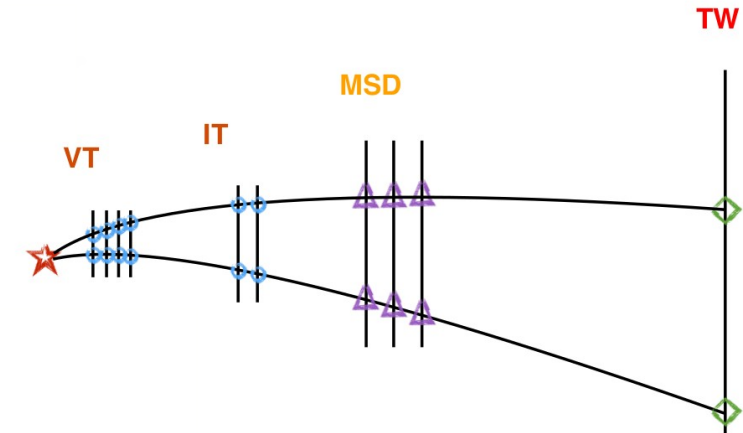
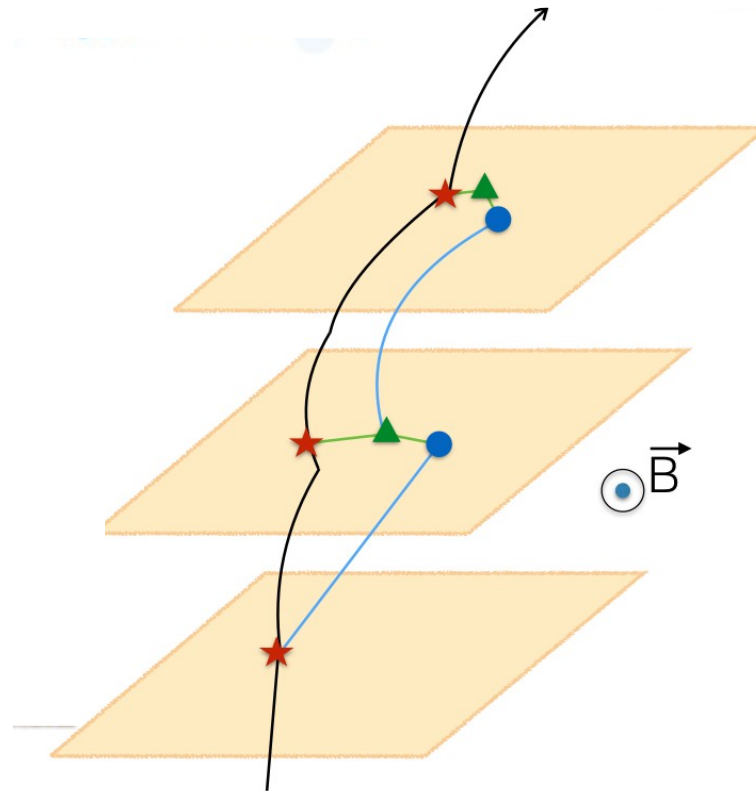
2. We'll see some measurement hits on the detector layers (considering finite detector uncertainty).

Filtering

3. Propagate the first hit to the next layer. Propagator Matrix  $F$ .

4. Find the best compromise between the propagated point and the closest hit on the 2 nd layer. Use a Chi2 and a Projection Matrix  $H$ .

5. Iterate 3 and 4 for the next layers.



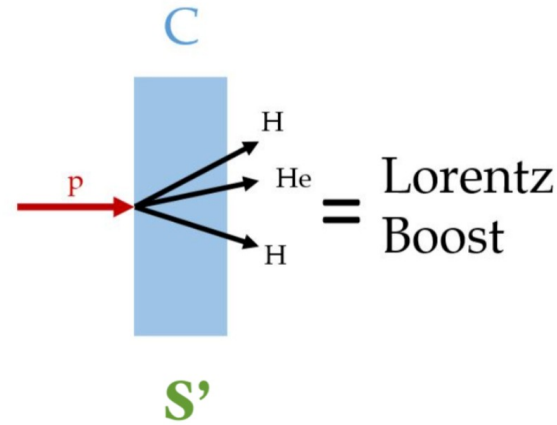
Kalman Filter reconstruction of a track

- Start from VT tracklets
- Projection to possible planes of IT
- KF extrapolation to MSD
- KF extrapolation to TW
- Fit the track candidates and extract reconstructed quantities: **Z, momentum ...**

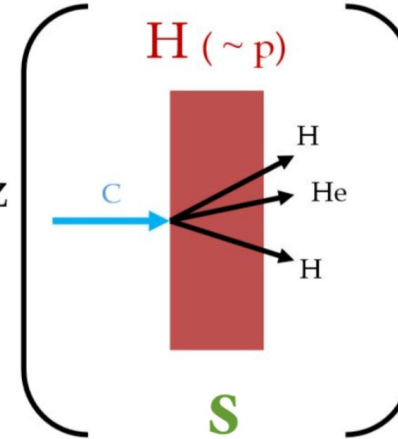


# Inverse kinematics

Proton beam on patient-target  
(Patient frame of reference)



Patient-target on Proton beam  
(Laboratory frame of reference)



= Lorentz  
Boost

$$ct' = \gamma(ct - \beta z)$$

$$x' = x$$

$$y' = y$$

$$z' = \gamma(z - \beta ct)$$

$$E'/c = \gamma(E/c - \beta p_z)$$

$$p'_x = p_x$$

$$p'_y = p_y$$

$$p'_z = \gamma(p_z - \beta E/c)$$