

“Measurements of nuclear **fragmentation**
differential **cross section** of a ^{16}O beam
in an energy range between 200 MeV/n and 400 MeV/n
at the FOOT experiment”

Thesis description presentation

Candidate:
Giacomo Ubaldi

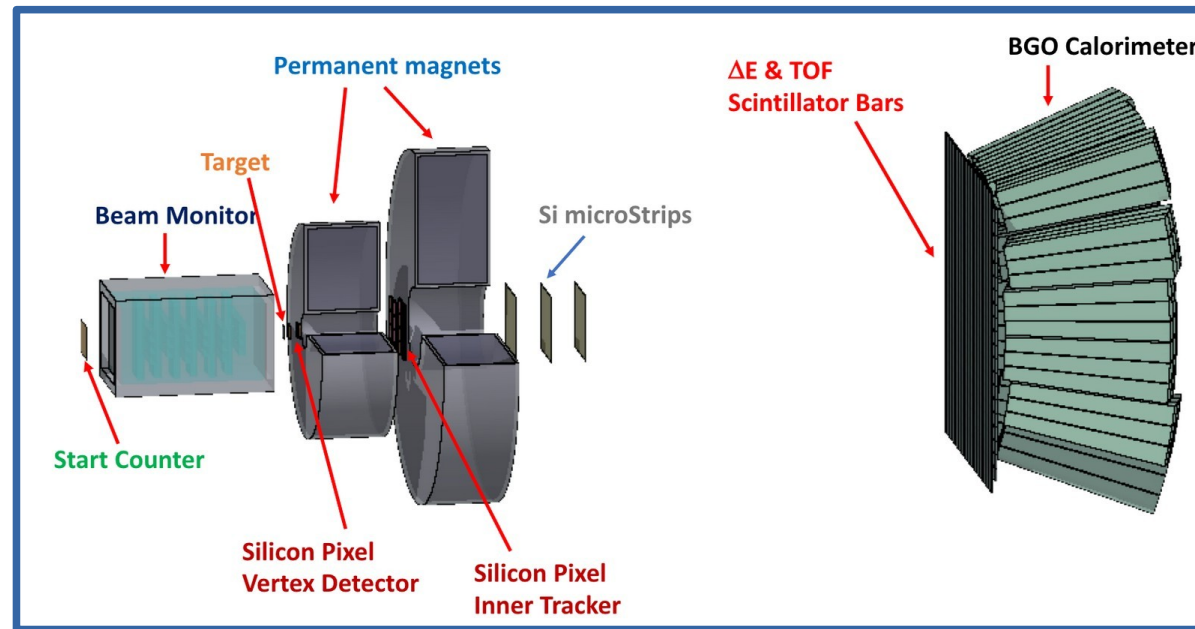
28/06/2022

The FOOT experiment



Fixed target experiment with **scintillators**, **magnetic spectrometer**, **calorimeter**

- Beams of p,C,O between 200 MeV/u and 700 MeV/u for **hadrontherapy** and **space radioprotection** topics
- Particle identification by measuring all kinematic quantities



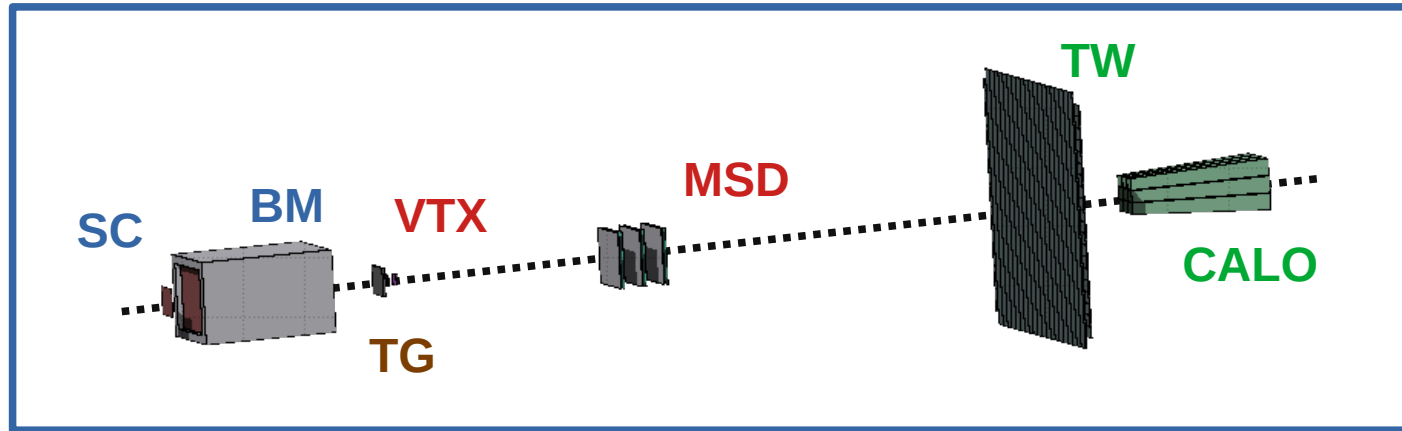
Goal:

Differential **fragmentation cross sections** measurements:

$$\frac{d^2\sigma}{d\Omega \cdot dE_{kin}}$$

My work

- Analysis of data taken at GSI in 2021 of ^{16}O 400 MeV/u and 200 MeV/u against C as target
- Analysis integrated in **SHOE** and optimization for specific data
- Partial setup: no tracker, only one module of calorimeter



Specific goal:

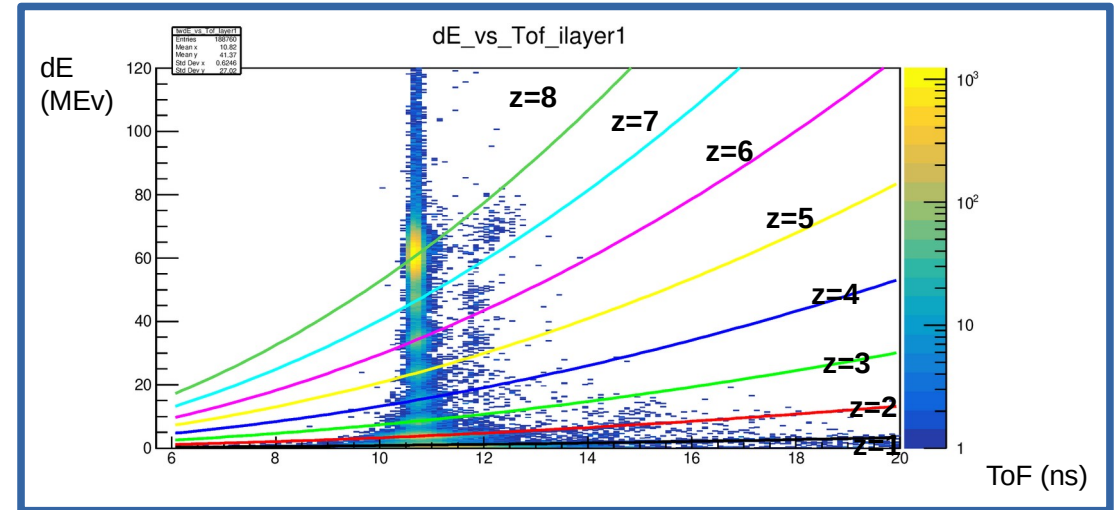
Differential fragment cross section:

$$\frac{d\sigma}{d\theta} = \frac{(Y_f - B_f)^u}{N_{beam} \cdot N_{target} \cdot \Delta\theta \cdot \epsilon}$$

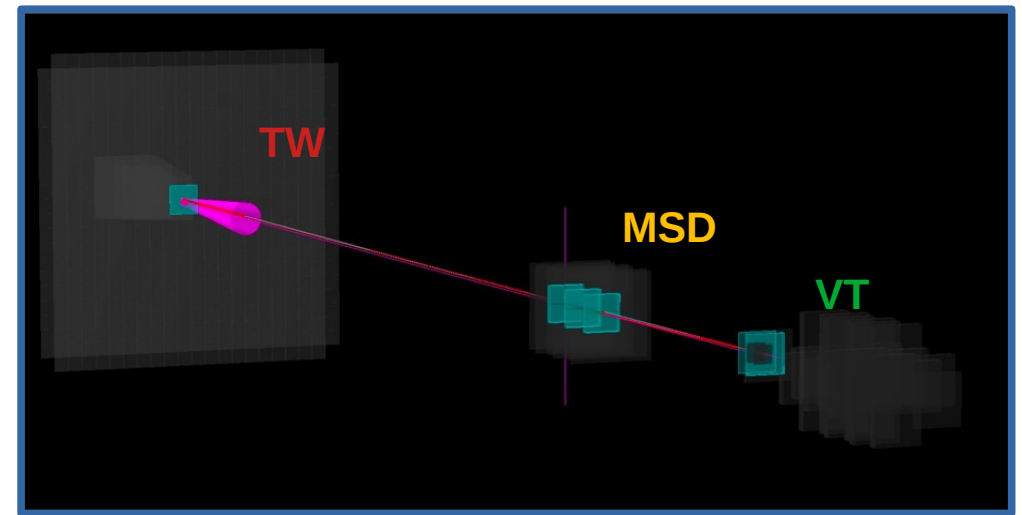
Event reconstruction

$$\frac{d\sigma}{d\theta} = \frac{(Y_f - B_f)^u}{N_{beam} \cdot N_{target} \cdot \Delta\theta \cdot \epsilon}$$

TW charge reconstruction algorithm



Kalman Filter reconstruction of a track



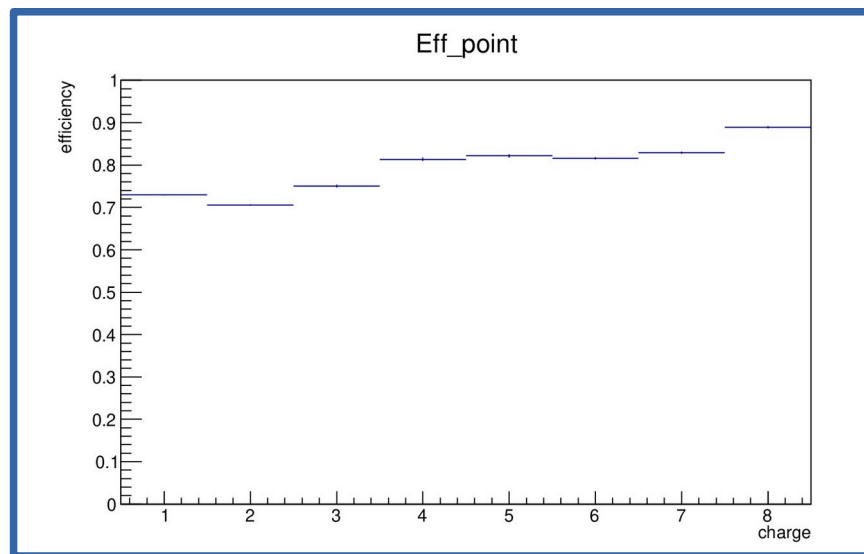
Efficiencies

$$\frac{d\sigma}{d\theta} = \frac{(Y_f - B_f)^u}{N_{beam} \cdot N_{target} \cdot \Delta\theta} \epsilon$$

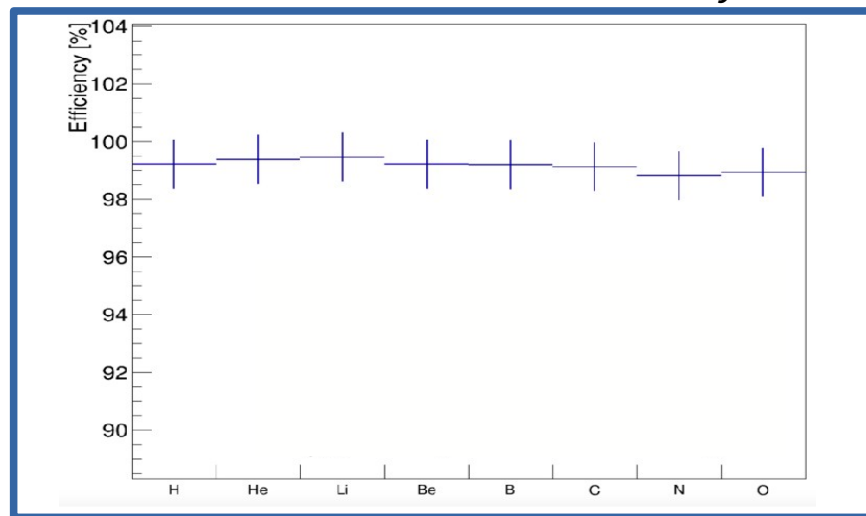
$$\epsilon(Z) = \frac{N_{TW}(Z) + 1}{N_{track}(Z) + 2}$$

$$\epsilon(Z) = \frac{N_{Z,conv}}{N_{Z,tot}}$$

charge reconstruction efficiency



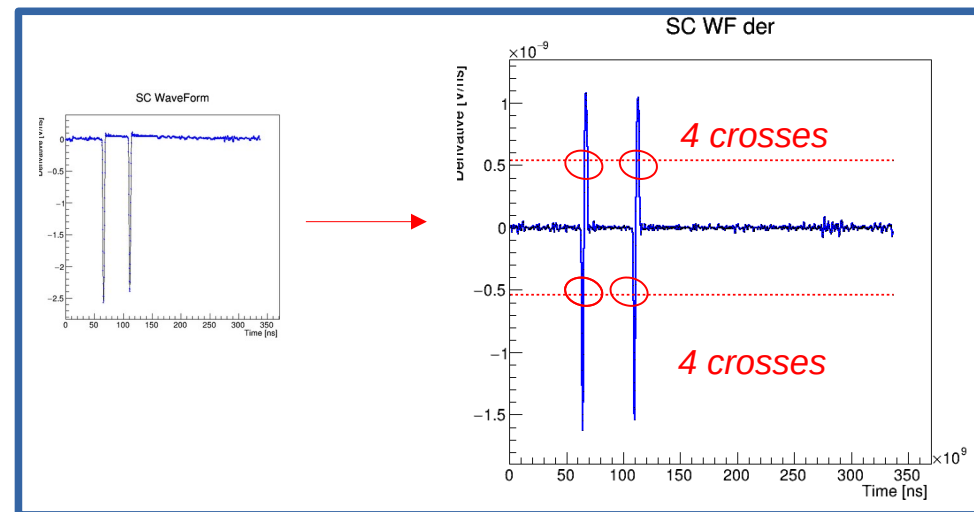
Track reconstruction efficiency



Pile-up removal

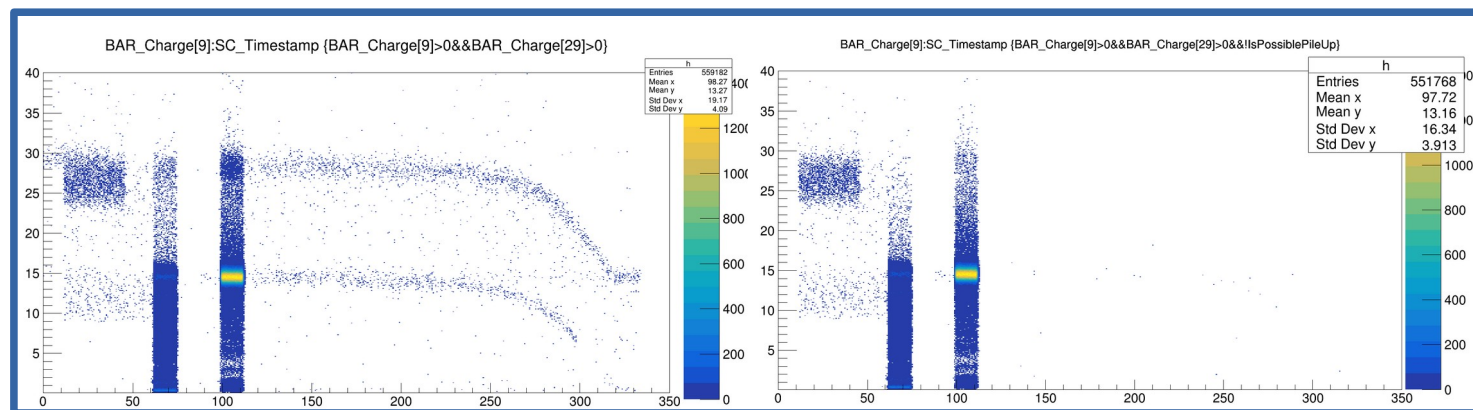
$$\frac{d\sigma}{d\theta} = \frac{(Y_f - \textcircled{B_f})^u}{N_{beam} \cdot N_{target} \cdot \Delta\theta \cdot \epsilon}$$

constant threshold **discrimination method**



pileup projectile: >4 crosses

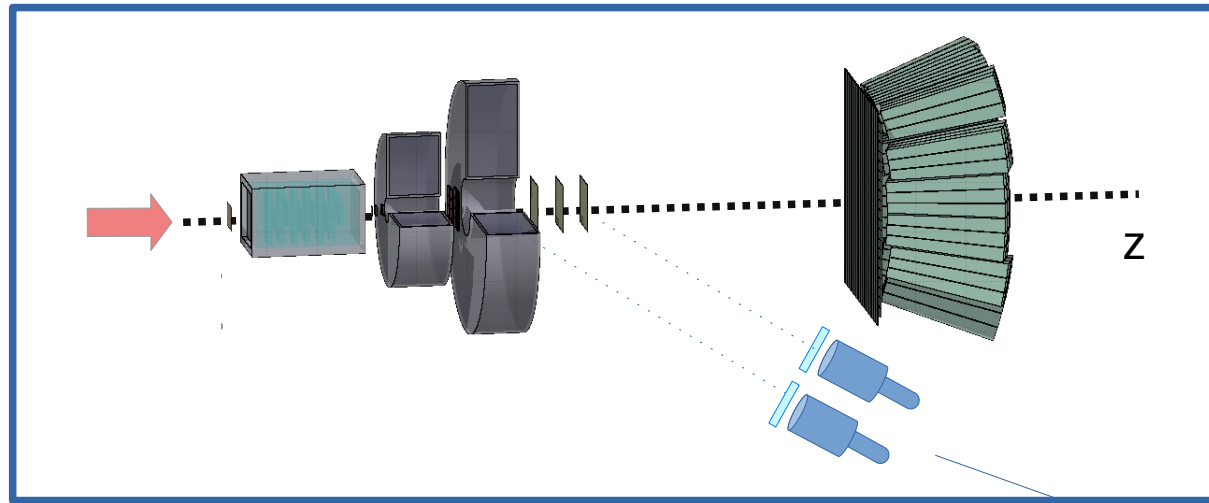
Pile-up rejection ~ 1%



Future prospects

Foreseen:

- New data taking with beam of ^4He , ^{12}C , ^{16}O at energies of 200 MeV/u, 400 MeV/n, 800 MeV/n



- Analysis optimization for all the setup
- Implementation of neutron detectors in analysis software
- Inverse kinematic application



BC-501A liquid scintillator

Back up slides

Isotopic identification

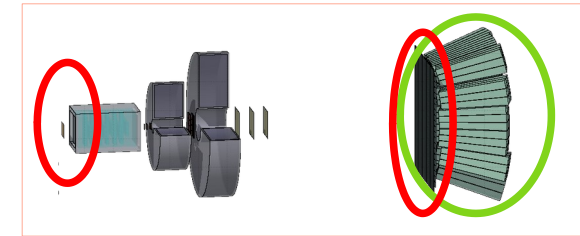
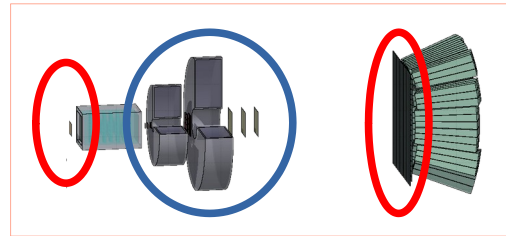
$$\frac{d\sigma}{d\theta} = \frac{(Y_f - B_f)^u}{N_{beam} \cdot N_{target} \cdot \Delta\theta \cdot \epsilon}$$

- MC data

Mass reconstruction using all FOOT subdetectors:

$$A_1 = \frac{p}{U\beta c\gamma}$$

$$A_2 = \frac{E_k}{Uc^2(\gamma - 1)}$$



$$A_3 = \frac{p^2 c^2 - E_k^2}{2Uc^2 E_k}$$



Isotopic identification

$$\frac{d\sigma}{d\theta} = \frac{(Y_f - B_f)^u}{N_{beam} \cdot N_{target} \cdot \Delta\theta \cdot \epsilon}$$

- MC data

Augmented Lagrangian Method

- Minimization of

$$L(\vec{x}, \lambda, \mu) \equiv f(\vec{x}) - \sum_a \lambda_a c_a(\vec{x}) + \frac{1}{2\mu} \sum_a c_a^2(\vec{x})$$

where

$$f(\vec{x}) = \left(\frac{TOF - T}{\sigma_{TOF}} \right)^2 + \left(\frac{p - P}{\sigma_p} \right)^2 + \left(\frac{E_k - K}{\sigma_{E_k}} \right)^2$$

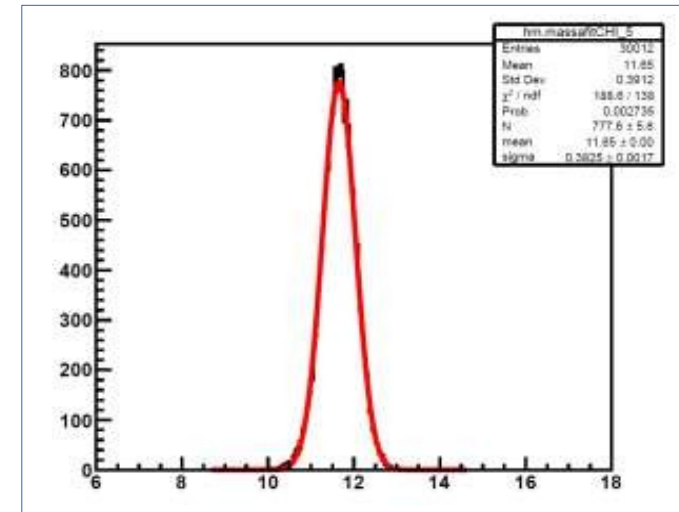
$$c_a(\vec{x}) = A - A_a$$

Es. **A = 12**

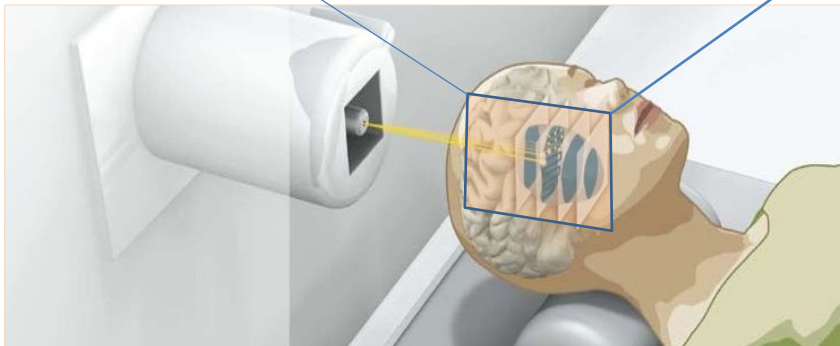
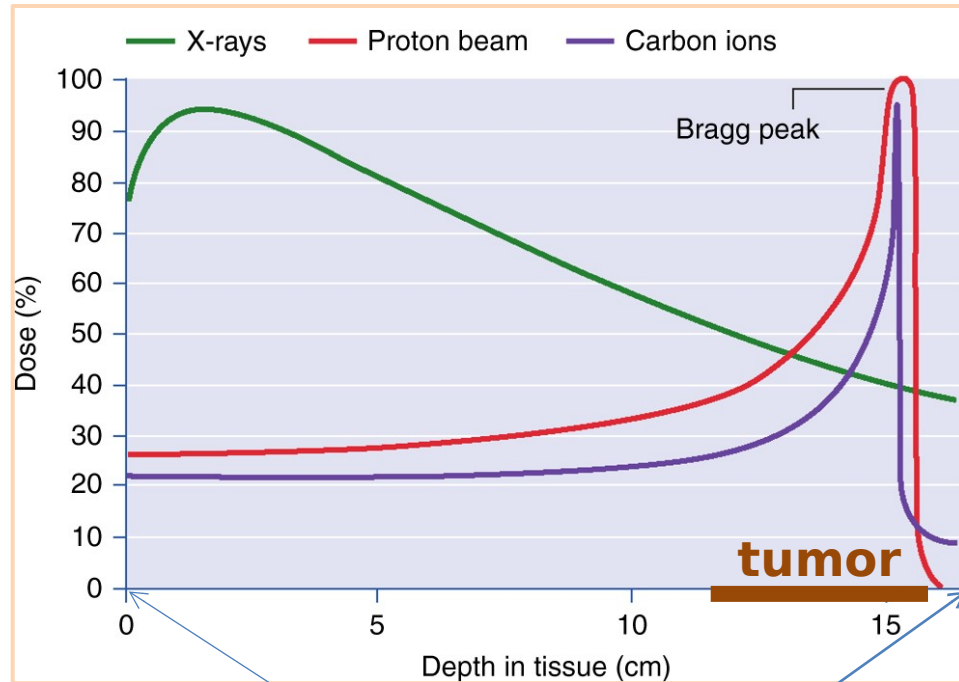
$$A_{ALM} = 11.66 \pm 0.38$$

$$A/\sigma_A = 3.2 \%$$

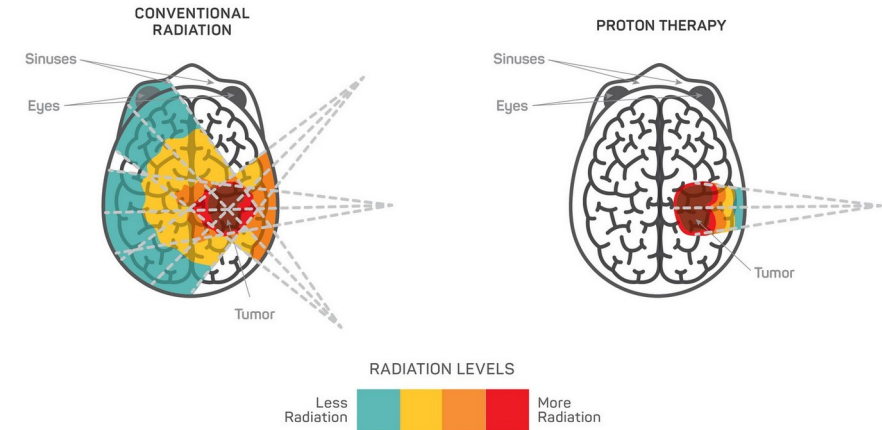
$$\chi^2 < 5$$



Hadrontherapy



depth- dose profile for X-rays and charged particles as a beam

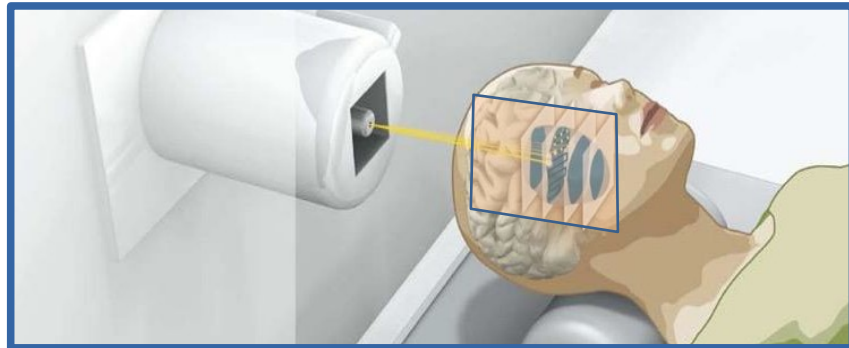
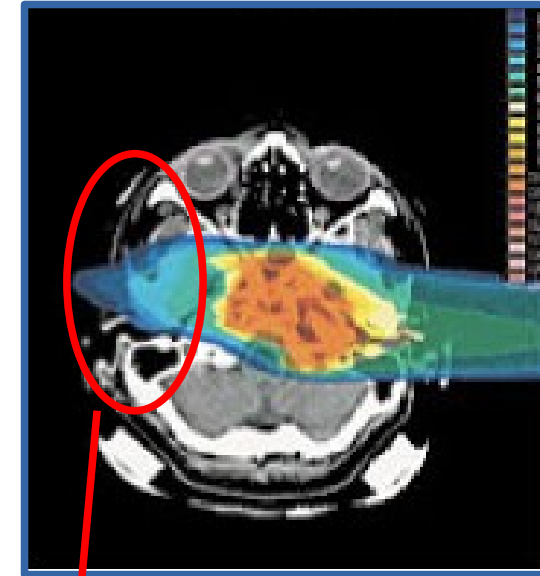
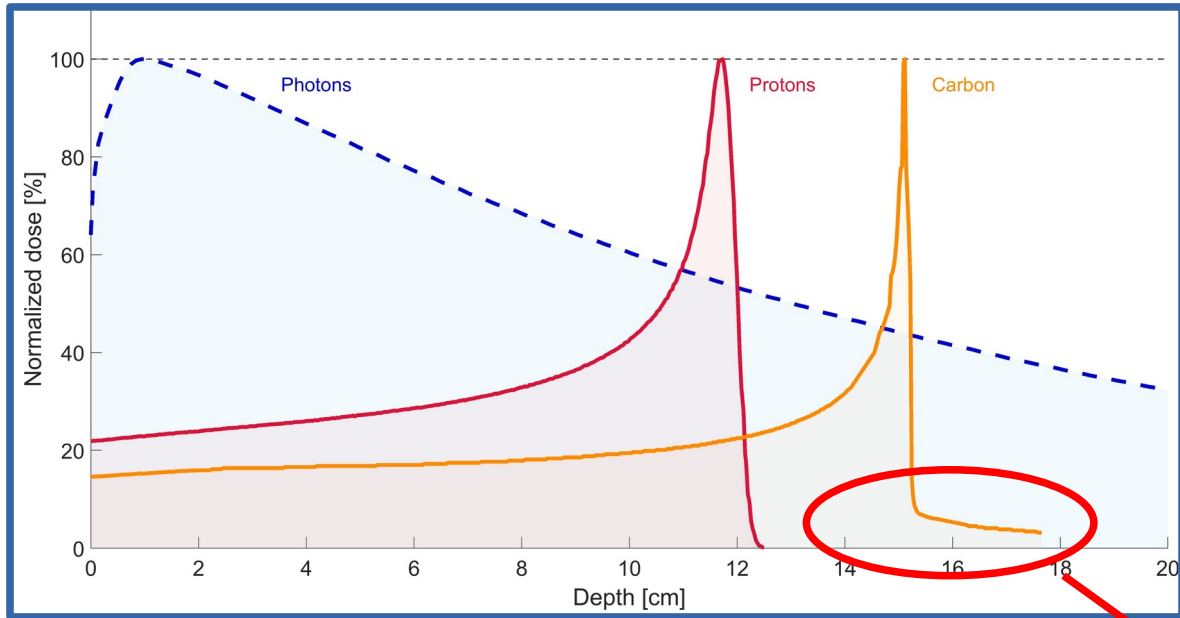


Sketch of a treatment planning system on brain-located tumor

Hadrontherapy vs radiotherapy:

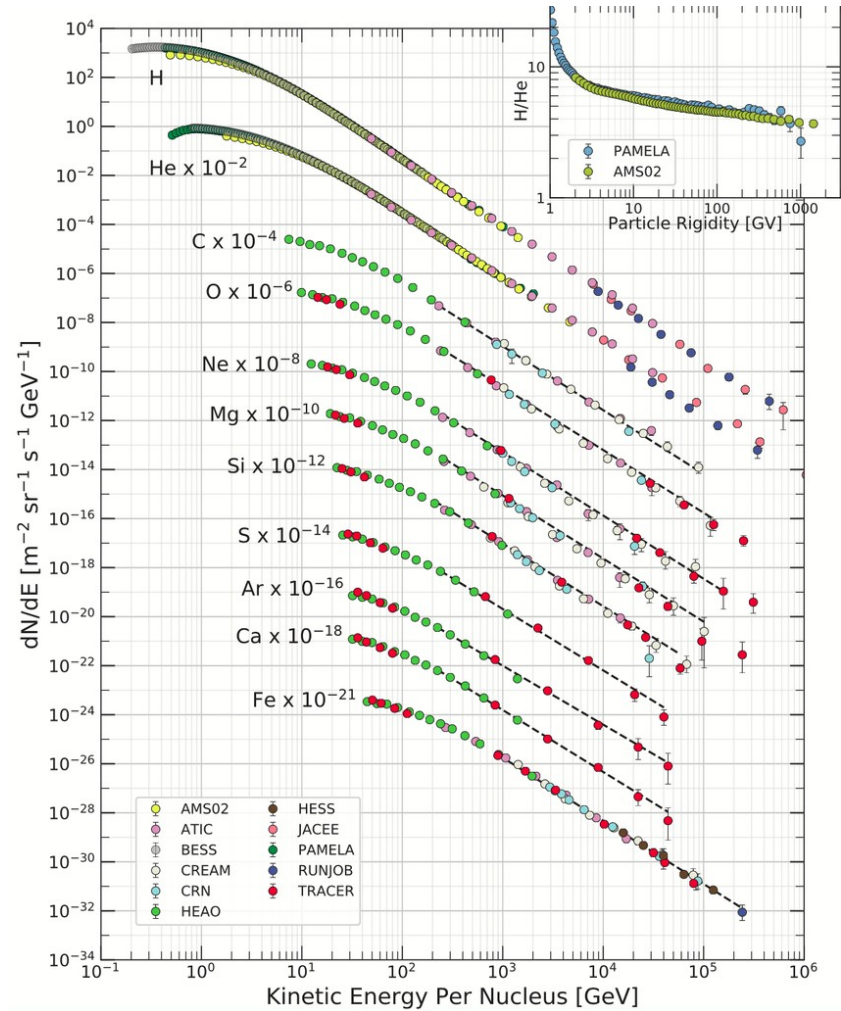
- **Finite range**
- **Localized dose profile**
- **Nuclear fragmentation**

Hadrontherapy

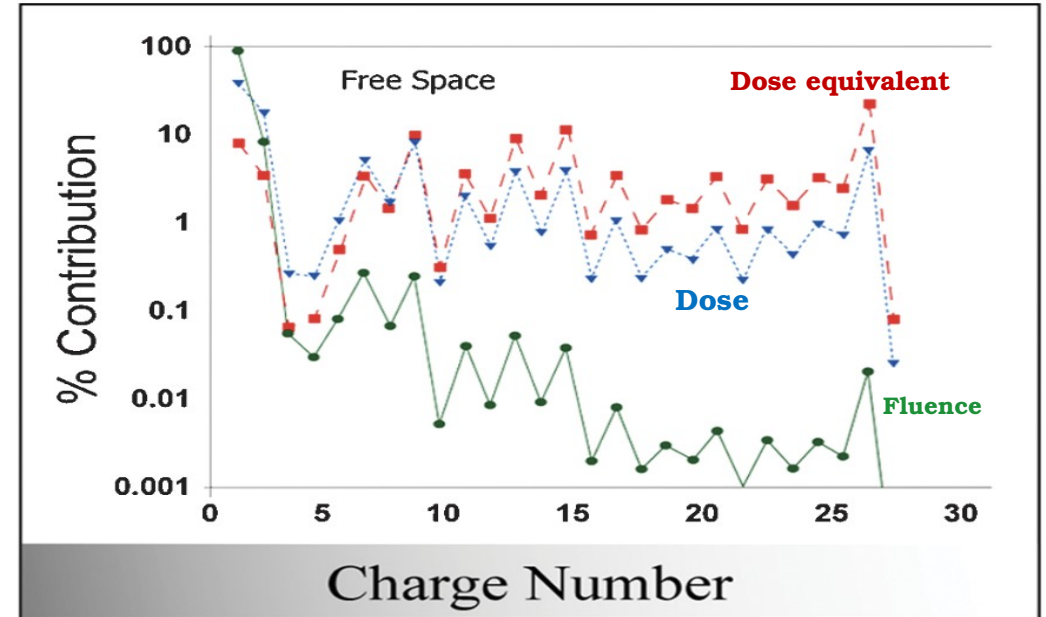


**Tail after Bragg peak:
nuclear fragmentation!**

Space radioprotection



GCR fluence

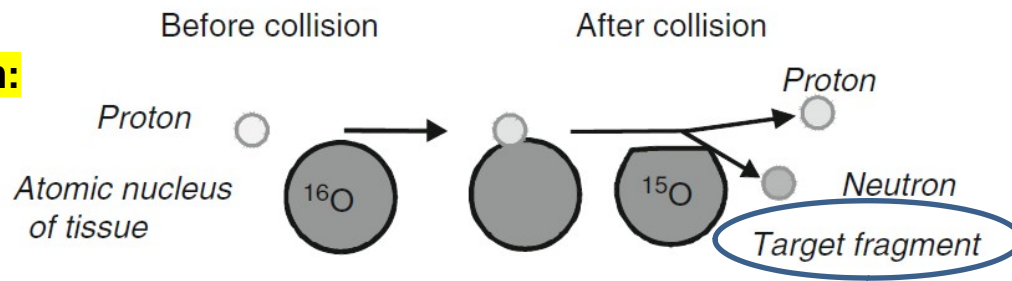


Particles contribution in
Fluence, dose and equivalent dose

Nuclear Fragmentation

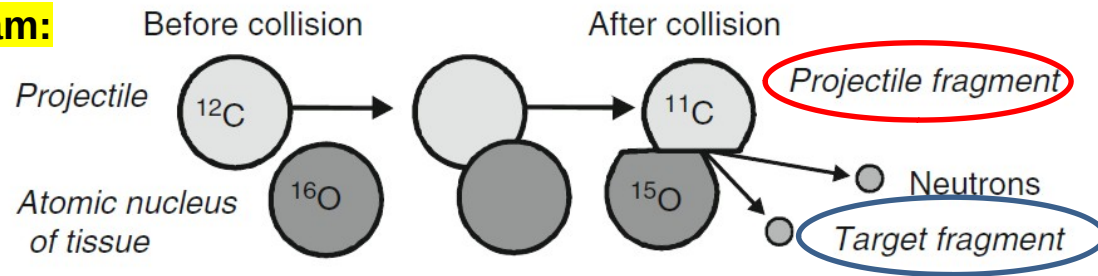
Proton beam:

~ 200 MeV

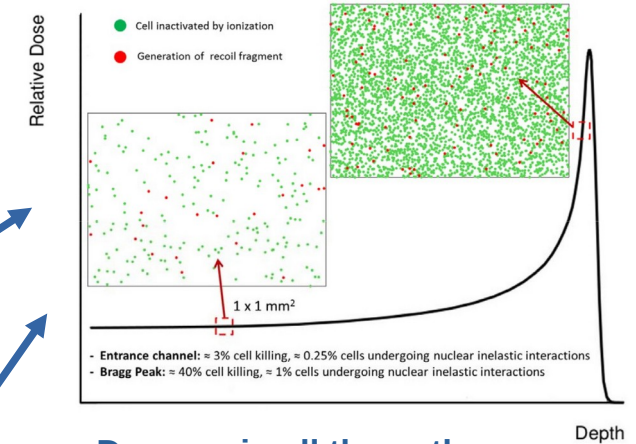


Carbon beam:

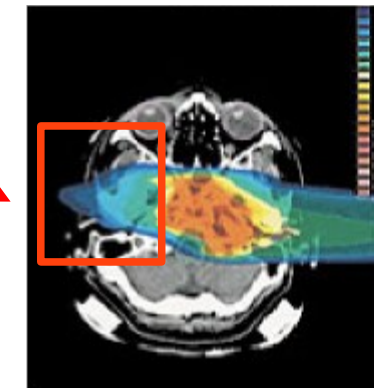
~ 400 MeV/u



Sketch of Nuclear fragmentation

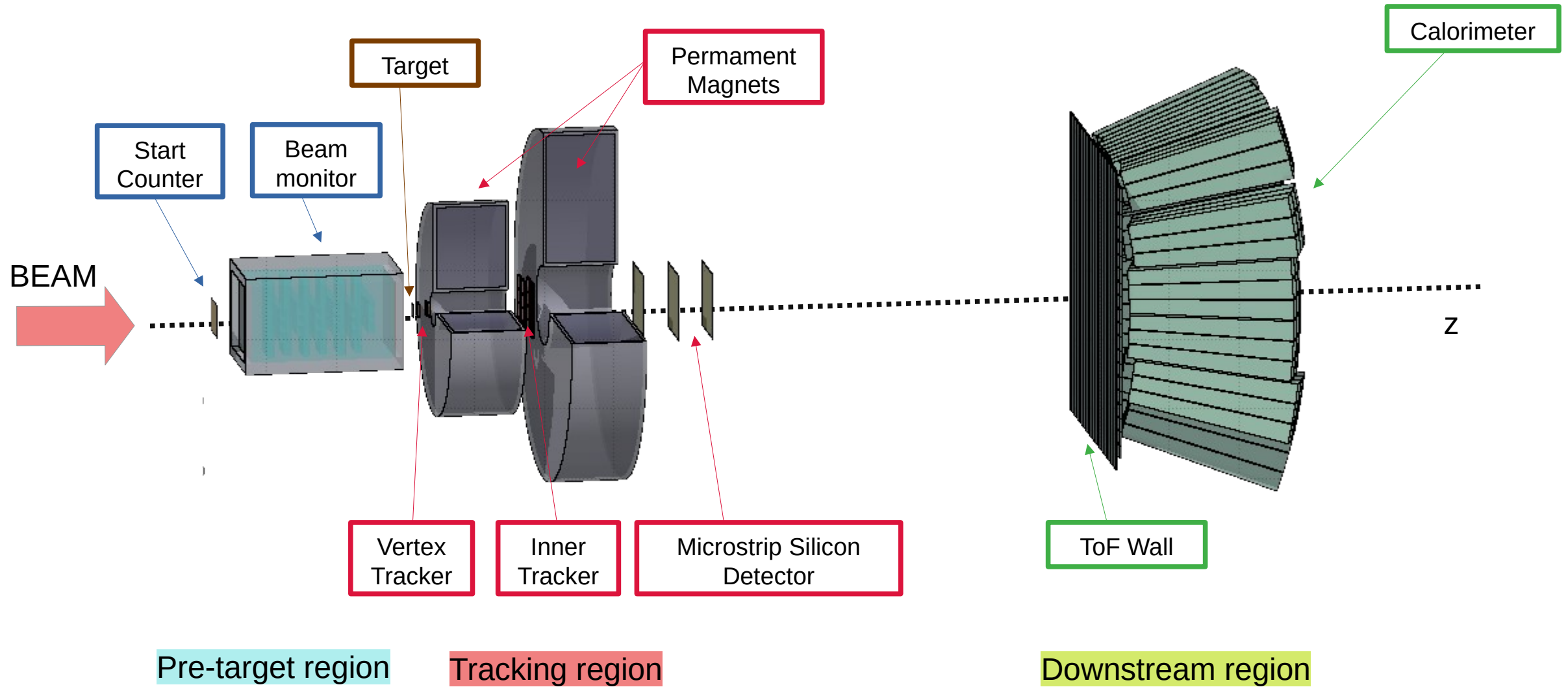


Damage in all the path



Damage after the BP

The FOOT detector



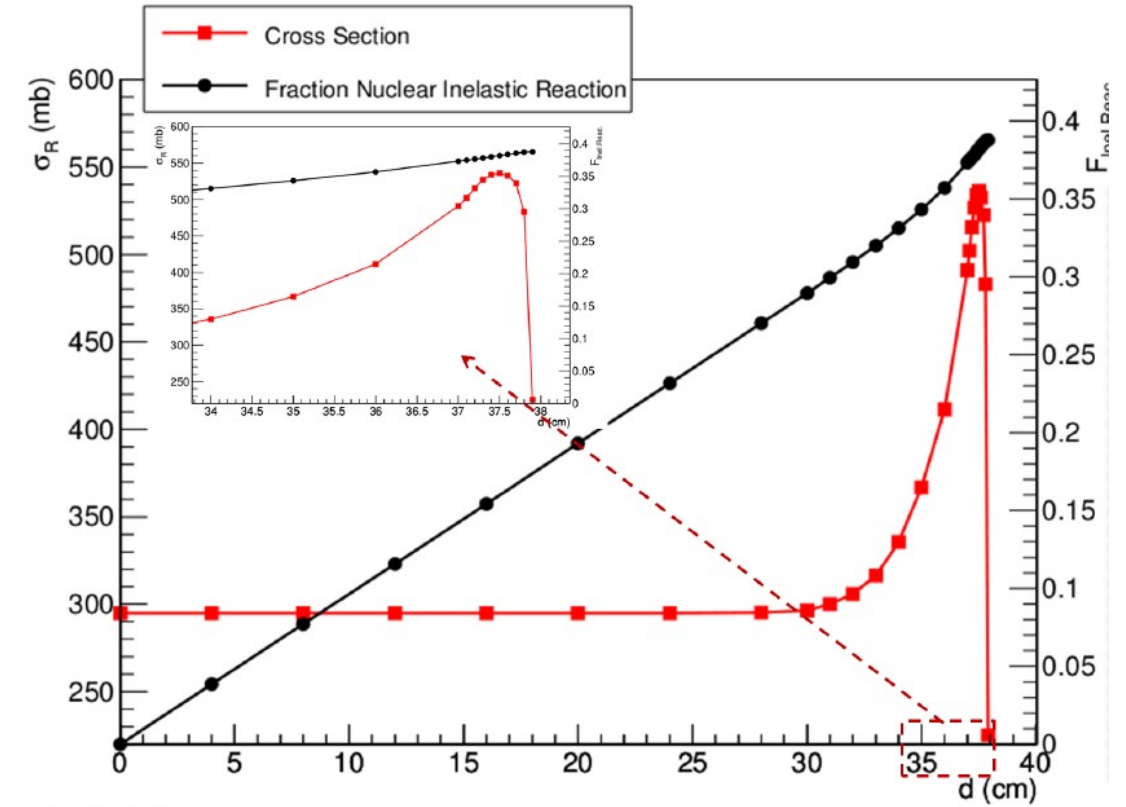
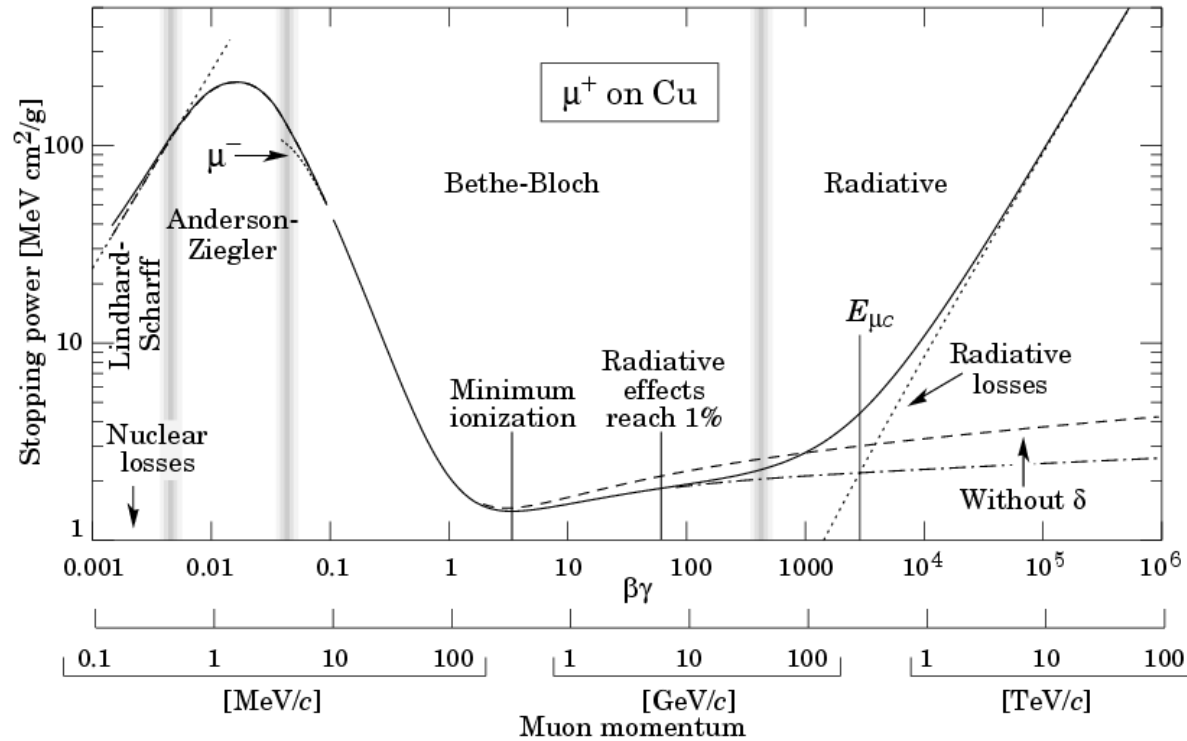
Differential Cross section

The diagram illustrates the formula for the differential cross-section, $\frac{d\sigma}{d\theta}$, with various components labeled in boxes and connected to the formula by arrows:

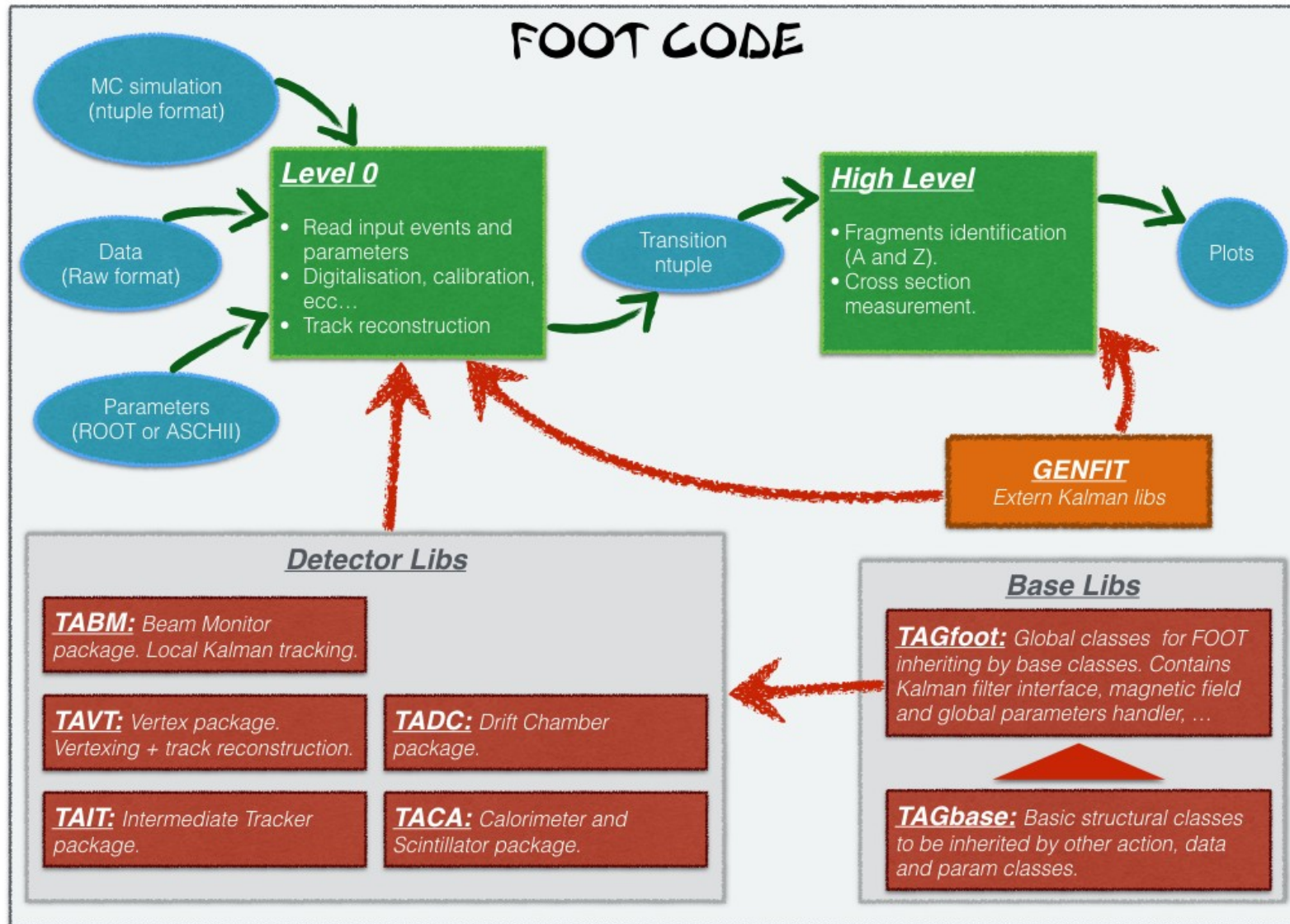
- Yield of all fragments** (brown box) points to Y_f in the numerator.
- Background** (black box) points to B_f in the numerator.
- unfolding** (black box) points to the superscript u in the numerator.
- efficiency** (red box) points to ϵ in the denominator.
- N° of primary events** (blue box) points to N_{beam} in the denominator.
- N° of scattered centers** (blue box) points to N_{target} in the denominator.
- Phase space** (green box) points to $\Delta\theta$ in the denominator.

$$\frac{d\sigma}{d\theta} = \frac{(Y_f - B_f)^u}{N_{beam} \cdot N_{target} \cdot \Delta\theta \cdot \epsilon}$$

Bethe Bloch vs nuclear cross section

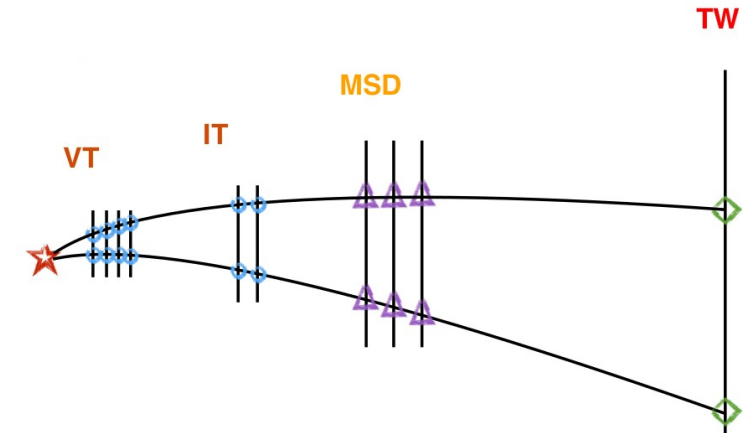
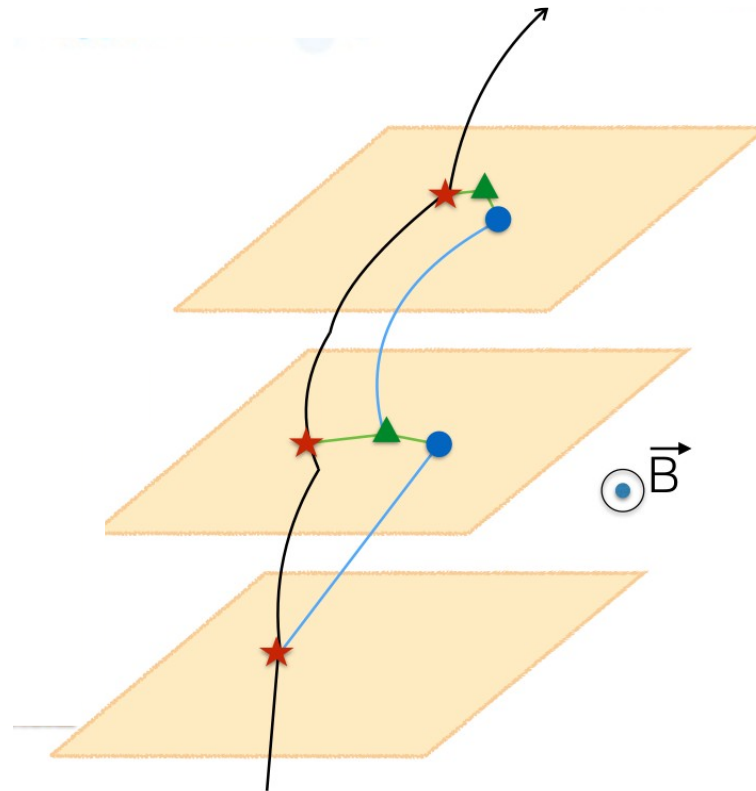


SHOE organization



Kalman filter in pills

1. Take an ideal particle in vacuum. If we add air + detector layers, trajectory changes due to M.S. and energy loss.
2. We'll see some measurement hits on the detector layers (considering finite detector uncertainty).
3. Propagate the first hit to the next layer. Propagator Matrix F .
4. Find the best compromise between the propagated point and the closest hit on the 2nd layer. Use a Chi2 and a Projection Matrix H .
5. Iterate 3 and 4 for the next layers.

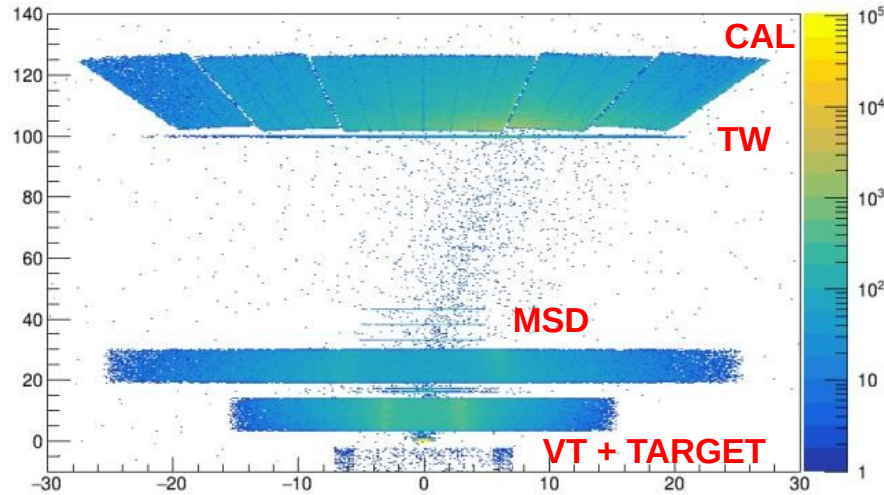


Kalman Filter reconstruction of a track

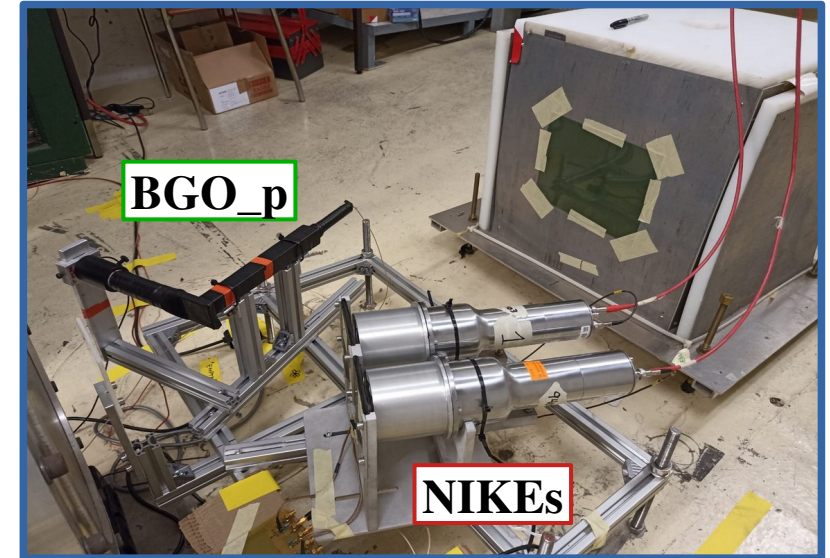
- Start from VT tracklets
- Projection to possible planes of IT
- KF extrapolation to MSD
- KF extrapolation to TW
- Fit the track candidates and extract reconstructed quantities: es. **momentum**

Fast neutrons detectors

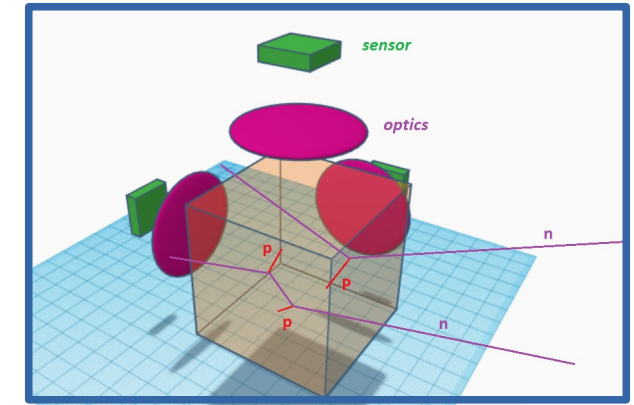
High **neutron production** as a consequence of fragmentation with detectors



Purpose to
Add neutron
detectors:



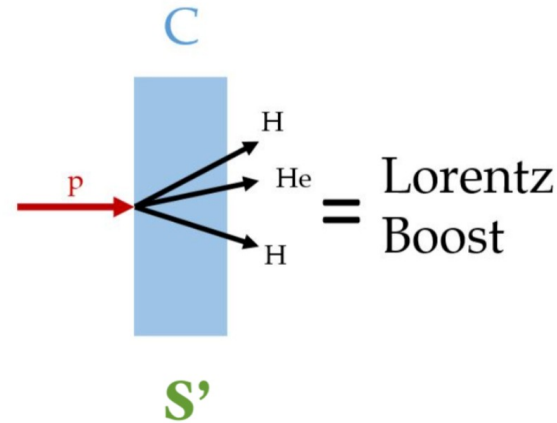
- BC-501A liquid scintillator
- BGO Phoswich



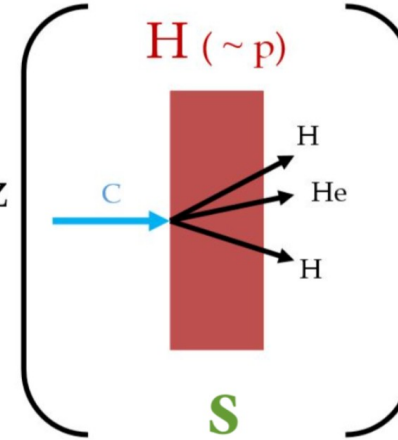
- recoil-proton track
imaging detector

Inverse kinematics

Proton beam on patient-target
(Patient frame of reference)



Patient-target on Proton beam
(Laboratory frame of reference)



= Lorentz
Boost

$$ct' = \gamma(ct - \beta z)$$

$$x' = x$$

$$y' = y$$

$$z' = \gamma(z - \beta ct)$$

$$E'/c = \gamma(E/c - \beta p_z)$$

$$p'_x = p_x$$

$$p'_y = p_y$$

$$p'_z = \gamma(p_z - \beta E/c)$$