```
#pragma once
#include <stdexcept>
#include <algorithm>
template<typename T>
struct BinaryTreeNode
{
    using BNode = BinaryTreeNode<T>;
    using BTreeNode = BNode*;
    T key;
    BTreeNode left;
    BTreeNode right;
    static BNode NIL;
    const T& findMax() const
        if (empty())
        {
            throw std::domain_error("Empty tree encountered.");
        return right ->empty() ? key : right ->findMax();
    }
    const T& findMin() const
        if (empty())
        {
            throw std::domain_error("Empty tree encountered.");
        }
        return left ->empty() ? key : left ->findMin();
    }
    bool remove(const T& akey, BTreeNode aParent)
    {
        BTreeNode x = this;
        BTreeNode y = aParent;
        while (!x->empty())
            if (akey == x->key)
            {
                break;
            }
            y = x;
            x = aKey < x->key ? x->left : x->right;
```

}

```
return true;
}
   BinaryTreeNode() :key(T()), left(&NIL), right(&NIL)
   }
   BinaryTreeNode(const T & akey) :key(akey), left(&NIL), right(&NIL)
   }
   BinaryTreeNode(T && aKey) :key(std::move(aKey)), left(&NIL), right >
      (&NIL)
    {
   }
   ~BinaryTreeNode()
    {
        if (!left->empty())
            delete left;
        if (!right->empty())
            delete right;
   }
   bool empty() const
        return this == &NIL;
    }
   bool leaf() const
    {
        return left->empty() && right->empty();
    }
   size_t height() const
    {
        if (empty())
            throw std::domain_error("Empty Tree encountered");
        if (leaf())
            return 0;
        const size_t lLeftHeight = left->empty() ? 1 : left->height() + >
        const size_t lRightHeight = right->empty() ? 1 : right->height() >
        return std::max(lLeftHeight, lRightHeight);
```

```
bool insert(const T & akey)
        {
            if (empty())
                return false;
            if (aKey > key)
                if (right->empty())
                    right = new BNode(aKey);
                else return right->insert(aKey);
                return true;
            }
            if (aKey < key)</pre>
                if (left->empty())
                    left = new BNode(aKey);
                else return left->insert(aKey);
                return true;
            }
            return false;
        }
};
template<typename T>
BinaryTreeNode<T> BinaryTreeNode<T>::NIL;
```