

ESc 201  
Full Marks: 15

Quiz 1A

30.8.18  
Total Time: 30 mins.

Name Key Section No. \_\_\_\_\_ Roll No. \_\_\_\_\_

- a) Determine  $I_1$ ,  $I_2$ , and  $I_3$ , using the *mesh current technique*. 8
- b) Using the results of part a), calculate the node voltages at nodes A, B, and C, with respect to the reference node G (ground). 4.5
- c) Hence, determine the voltage dropped across the 5 A current source ( $I_s$ ), clearly specifying its polarity. 2.5

a) Due to presence of  $I_s$ , mesh eqns for meshes ① and ② can be written. But  $I_1 - I_2 = 5A \Rightarrow \underline{I_1 = I_2 + 5}$

Invoke Supermesh 1: DACGD

$$\Rightarrow 10 = 6I_1 + 2I_2 + I_3 + 4I_1$$

$$\Rightarrow \underline{12I_2 + I_3 = -40} \quad \text{or} \quad \underline{12I_1 + I_3 = 20} \quad \dots \quad \text{①}$$

Supermesh 2: DACBGD

$$\Rightarrow 10 = 6I_1 + 2I_2 + 3(I_2 - I_3) + 4(I_1 - I_3) \Rightarrow \underline{15I_2 - 7I_3 = -40} \quad \text{or} \quad \underline{15I_1 - 7I_3 = 35} \quad \dots \quad \text{②}$$

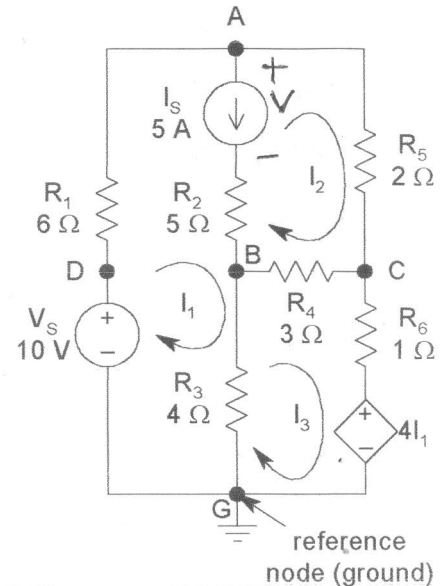
$$\text{Mesh 3: } \underline{GBCG} \Rightarrow 4(I_3 - I_1) + 3(I_3 - I_2) + I_3 + 4I_1 = 0 \Rightarrow \underline{-3I_2 + 8I_3 = 0} \quad \dots \quad \text{③}$$

Any 2 among Eqs. (1)-(3) would be enough.

Solving any pair,  $\underline{I_1 = 1.77A}$      $\underline{I_2 = -3.23A}$      $\underline{I_3 = -1.24A}$

b)  $V_A = V_s - I_1 R_1 = \underline{-0.62V}$      $V_B = R_3(I_1 - I_3) = \underline{12.04V}$      $V_C = V_A - R_5 I_2 = \underline{5.84V}$

c)  $V_A - V_B = V + R_2 I_s \Rightarrow \underline{V = -37.66V}$ , with polarity as shown in the fig.



ESc 201  
Full Marks: 15

Quiz 1B

30.8.18  
Total Time: 30 mins.

Name Key Section No. \_\_\_\_\_ Roll No. \_\_\_\_\_

- a) Determine  $I_1$ ,  $I_2$ , and  $I_3$ , using the *mesh current technique*. 8
- b) Using the results of part a), calculate the node voltages at nodes A, B, and C, with respect to the reference node G (ground). 4.5
- c) Hence, determine the voltage dropped across the 5 A current source ( $I_s$ ), clearly specifying its polarity. 2.5

a)  $I_2 - I_1 = 5A \Rightarrow I_2 = I_1 + 5$

Supermesh 1:  $DACGD \Rightarrow 10 = 6I_1 + 2I_2 + I_3 + 3I_2$   
 $\Rightarrow 11I_1 + I_3 = -15$  or  $11I_2 + I_3 = 40$  ①

Supermesh 2:  $DACBGD \Rightarrow 10 = 6I_1 + 2I_2 + 3(I_2 - I_3) + 4(I_1 - I_3)$   
 $\Rightarrow 15I_1 - 7I_3 = -15$  or  $15I_2 - 7I_3 = 60$  ②

Mesh 3:  $GBCG \Rightarrow 4(I_3 - I_1) + 3(I_3 - I_2) + I_3 + 3I_2 = 0$   
 $\Rightarrow -I_1 + 2I_3 = 0$  or  $-I_2 + 2I_3 = -5$  ③

Solving:  $I_1 = -1.3A$   $I_2 = 3.7A$   $I_3 = -0.7A$

b)  $V_A = V_S - I_1 R_1 = 17.8V$   $V_B = R_3(I_1 - I_3) = -2.4V$   $V_C = V_A - I_2 R_5 = 10.4V$

c)  $V_A - V_B = V - R_2 I_s \Rightarrow V = 45.2V$ , with polarity as shown in the fig.

