O given cend?:
$$\{x_{k}\}$$
 covariance relationary $\{x_{k}\}$ covariance $\{x_{k}\}$ cova

< = + (n-k) & < 6

 $\Rightarrow \frac{1}{N} \sum_{i=1}^{N-1} \lambda(i) \rightarrow 0 \quad \text{as} \quad \lambda \rightarrow A$

$$V(\bar{X}_{N}) = \frac{1}{N} \sum_{|h| < N} \left(1 - \frac{|h|}{N} \right) Y_{h}$$

$$= \left| \frac{1}{N} \sum_{|h| < N} \left(1 - \frac{|h|}{N} \right) Y_{h} \right|$$

$$\leq \frac{1}{N} \sum_{|h| < N} \left| Y_{h} \right|$$

$$= \frac{2}{N} \sum_{|h| < N} |Y_{h}| - \frac{1}{N} |Y_{0}|$$

$$\leq \frac{2}{N} \sum_{|h| < N} |Y_{h}| \rightarrow 0 \text{ as } N \Rightarrow 4 \text{ as } Y_{h} \rightarrow 0$$

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Comber example: Converse is NOT true

$$\bar{X}_n = \begin{cases} 0, & \text{nin even} \\ -\frac{z}{n}, & \text{nin odd} \end{cases}$$

$$V(\bar{X}_n) = \{0, n \text{ is even} \}$$

$$\left\{\frac{1}{n^2}, n \text{ is odd}\right\}$$

$$\rightarrow 0 \quad \text{on} \quad n \rightarrow d$$

$$Y_h = Cov(x_b, x_{b+h}) = (-1)^h +> 0$$
 as $h \rightarrow d$

(3)
$$(x_1, \dots, x_{100})$$
 from AR(1) with unknown mean μ

$$\widehat{x}_{100} = 0.157, \ \widehat{\phi} = 0.6, \ \widehat{\nabla}^{\perp} = 2$$

using asymptotic result

$$\sqrt{n}\left(\overline{X}_{n}-u\right)\stackrel{\angle}{\longrightarrow} N\left(0,\frac{\tau}{2}x_{n}=\frac{\sigma^{2}}{(1-\phi)^{2}}\right)$$

Almo
$$Z = \frac{\sqrt{n}(\bar{X}_n - 0)}{\sqrt{\frac{\hat{q}^2}{(1 - \hat{\varphi})^2}}}$$
 asym $N(0, 1)$ under the

Reject Ho at 5% level of significance if Shod 121 > 70.05/2

$$\frac{121 = \sqrt{100} (0.157)}{\sqrt{\frac{4}{(1-.6)^{2}}}} \approx -31 \neq 1.96 (\gamma_{0.05/1})$$

100(1-a)/, asymptotic Confidence internal

$$\overline{\chi}_{n} \mp \gamma_{\alpha/2} \sqrt{\frac{\hat{\tau}^{2}}{(1-\hat{\phi})^{2}}}$$

$$X_{t} = 0 + \ell_{t} + \frac{1}{2} \ell_{t-1} + \frac{1}{2} \ell_{t-2}; \quad \ell_{t} \sim 0 \quad N(0,1)$$

$$Y_{h} = \begin{cases} 1 + \frac{1}{4} + \frac{1}{4} = \frac{3}{2}, & h = 0 \\ \frac{1}{2} + \frac{1}{4} = \frac{3}{4}, & h = \pm 1 \\ 0, & h = \pm 2 \end{cases}$$

$$V_{h} = \begin{cases} 1 \times \frac{1}{4} = \frac{3}{4}, & h = \pm 1 \\ 0, & h = \pm 2 \end{cases}$$

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(5)
$$\lim_{n \to 1} n \vee (\bar{x}_n) = \sum_{-1} \gamma_n$$

$$= \sum_{-1} \left(\cdot \cdot \cdot \cdot \cdot \cdot \cdot + 2 \cdot (0.3)^{|h|} + (0.1)^{|h|} \right) - (x)$$

$$\left(\sum_{-1} \alpha^{|h|} = 2 \sum_{0} \alpha^{h} - 1 \right) = \frac{2}{1 - \alpha} - 1 = \frac{1 + \alpha}{1 - \alpha}$$

$$|\alpha| < 1$$

$$(x) = \frac{1.6}{.4} + 2 \frac{1.3}{.7} + \frac{1.1}{.9} \approx 8.93$$

$$\sqrt{n}(\overline{X}_{n} - \mu) \stackrel{\text{onym}}{\sim} N(0, 8.93) - (*)$$

$$P(\overline{X}_{n} - 0.49 \leq \mu \leq \overline{X}_{n} + 0.49)$$

$$= P(|\overline{X}_{n} - \mu| \leq 0.49) \geq 0.95 - (i)$$

Using (*1)
$$P\left(\frac{1\bar{x}_n - u}{\sqrt{\frac{8.93}{n}}} \le 1.96\right) = 0.95$$

From Prime (1) A (11)

Comparing (1) A (11)

$$0.49 > \sqrt{\frac{8.93}{N}} 1.96$$

$$\Rightarrow M > 16 \times 8.93 = 142.88$$

$$X_{E} = M + \frac{1}{2}X_{E-1} + E_{E}$$

$$\Rightarrow M_{X} = 2M ; Y_{X}(L) = \frac{4}{1-\frac{1}{4}} \cdot (\frac{1}{2})^{|L|} = \frac{1}{3} \sigma^{2} (\frac{1}{2})^{|L|}$$

$$Y_{E} = M + \frac{1}{3} Y_{E-1} + E_{E}$$

$$M_{Y} = \frac{3}{2} M ; Y_{Y}(L) = \frac{9}{8} \sigma^{2} (\frac{1}{3})^{|L|}$$

$$Z_{E} = X_{E} + Y_{E} ; M_{Z} = 2M + \frac{3M}{2} = \frac{7M}{2}$$

$$\sqrt{n} \left(\frac{2}{2}n - \frac{7M}{2} \right) \xrightarrow{L} N \left(0, \frac{5}{2} Y_{Z}(L) \right)$$

$$Y_{Z}(L) = Y_{X}(L) + Y_{Y}(L)$$

$$= \frac{\sigma^{2}}{(1 - \frac{1}{2})^{2}} + \frac{\sigma^{3}}{(1 - \frac{1}{3})^{2}} = 4 \sigma^{3} + \frac{9}{4} \sigma^{2} = \frac{2M}{4} \sigma^{2}$$

$$1.8. \sqrt{n} \left(\overline{X}_{n} - \frac{7M}{2} \right) \xrightarrow{L} N \left(0, \frac{2M}{4} \sigma^{2} \right)$$

$$P \left(|\overline{Z}_{n} - \frac{7M}{2}| \le \frac{5}{2} \frac{1.96}{\sqrt{n}} \right) = 0.95$$

given condition

$$P(|\overline{z}_n - \frac{7\mu}{2}| \le 0.098) \ge 0.95$$

$$\Rightarrow$$
 0.098 $\geq \frac{5}{2} \frac{1.96}{\sqrt{n}}$

$$X_{t} = A + \phi \times_{t-1} + \epsilon_{t} \qquad |\phi| < 1$$

$$Y_{t} = \delta + \chi_{t} + \delta \chi_{t-1} + \epsilon_{t} \qquad |\phi| < 1$$

$$\{\epsilon_{t}\} \land \{\delta_{t}\} \quad \text{are in-def}.$$

$$Z_{t} = \chi_{t} + \chi_{t}$$

$$\chi_{2}(\lambda) = \chi_{x}(\lambda) + \chi_{y}(\lambda)$$

$$\chi_{x}(\lambda) = \frac{\sigma^{2}}{1 - \phi^{2}} \phi^{1\lambda}; \quad \chi_{y}(\lambda) = \begin{cases} \sigma^{2}(1 + \delta^{2}), & \lambda = 0 \\ \delta \sigma^{2}, & \lambda = \pm 1 \end{cases}$$

$$\chi_{x}(\lambda) = \frac{\sigma^{2}}{1 - \phi^{2}} \phi^{1\lambda}; \quad \chi_{y}(\lambda) = \begin{cases} \sigma^{2}(1 + \delta^{2}), & \lambda = 0 \\ \delta \sigma^{2}, & \lambda = \pm 1 \end{cases}$$

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(8)
$$P(x_1, x_n) = a_1 x_1 + \cdots + a_n x_n$$
 $V(2 - P_{(-)} + 2) = V(2) + V(P_{(-)} + 2) - 2 \text{ for } \{2, P_{(-)} + 2\}$
 $a_1, \dots, a_n = 3$
 $E(2 - P_{(-)} + 2) \times i = 0 + i$
 $\Rightarrow E(2 - P_{(-)} + 2) \times i = 0 + i$
 $\Leftrightarrow V(2 - P_{(-)} + 2) \times i = 0 + i$
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$$\Rightarrow \alpha_{1} + \alpha_{3} + \dots + \alpha_{h-1} = 0$$

$$& \alpha_{2} + \alpha_{h+1} - \dots + \alpha_{h-2} = 1$$

$$P(x_{h}, x_{h-1}, \dots x_{2}) \times_{h+1} = \overline{Z}_{2} (\alpha_{k} + \alpha_{h+1} + \dots + \alpha_{h-2}) = \overline{Z}_{2}$$

$$P(x_{h}, x_{h-1}, \dots x_{2}) \times_{h+1} = \overline{Z}_{2} (\alpha_{k} + \alpha_{h+1} + \dots + \alpha_{h-2}) = \overline{Z}_{2}$$

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$$P(x_{h}, x_{h}, \dots x_{h+1}, \dots x_{h+1}) \times_{h+1} \times_{h+1} = \overline{Z}_{2} (\alpha_{k} + \alpha_{h+1}, \dots x_{h+1}) \times_{h+1} \times_{h+1} = \overline{Z}_{2}$$

$$P(x_{h}, x_{h}, \dots x_{h+1}, \dots x_{h+1}) \times_{h+1} \times_$$

The above can also be derived wring Yule-Walker eg, ~ argument.

$$\begin{array}{lll}
Y_{E} = X_{2E} = \varphi X_{2E-1} + \varepsilon_{2E}; & \varepsilon_{E} \sim WN[0,\sigma^{2}]; | \varphi | < 1 \\
Y_{E} = \varphi (\varphi X_{2E-2} + \varepsilon_{2E-1}) + \varepsilon_{2E} \\
&= \varphi^{2} \times_{2E-2} + \varphi \varepsilon_{2E-1} + \varepsilon_{2E} \\
Y_{E} = \varphi^{2} \times_{2E-2} + \varphi \varepsilon_{2E-1} + \varepsilon_{2E} \\
Y_{E} = \varphi^{2} \times_{2E-1} + \varphi_{2E};
\end{array}$$
Let $all P_{E} = \varphi \varepsilon_{2E-1} + \varepsilon_{2E} \sim WN[0,\sigma^{2}(1+\varphi^{2})]$

$$\Rightarrow \{Y_{E}\} \sim \text{distinctly } AR(1)$$

$$\Rightarrow \begin{cases} \lambda^{+} : \Rightarrow \lambda^{+} : \Rightarrow$$

min mean of prediction error $E(\lambda^{p+1} - b^{-2}\lambda^{p+1}) = E(\lambda^{p+1} - b_{-1}\lambda^{p})$ = E (2 = 1) = 2, (1+ d)

(2)
$$X_{E} = \phi_{X} X_{E-1} + z_{E} \qquad z_{E} \sim HN(0, T_{D}^{2}) > indep.$$

$$Y_{E} = \phi_{Y} Y_{E-1} + z_{E} + U_{E} \qquad U_{E} \sim HN(0, T_{D}^{2}) > indep.$$

$$|\phi_{X}|, |\phi_{Y}| \leq 1$$

$$P_{Y_E} \times_{E+1} = \alpha Y_E$$

$$\alpha = \frac{E(X_{E+1} Y_E)}{E Y_E} - (*)$$

Note that

 Π

$$Y_{t} - \phi_{y} Y_{t-1} = \frac{1}{2} + 0$$

$$(1 - \phi_{y} B) Y_{t} = \frac{1}{2} + 0$$

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$$A = \frac{(\Delta_{r}^{F} + \Delta_{r}^{A})(1 - \phi^{A})_{-1}}{\phi^{A}} = \frac{(\Delta_{r}^{F} + \Delta_{r}^{A})}{\phi^{A}(1 - \phi^{A})_{-1}} = \frac{(\Delta_{r}^{F} + \Delta_{r}^{A})}{\phi^{A}(1 - \phi^{A})} = \frac{(\Delta_{r}^{F} + \Delta_{r}^{A})}{(\Delta_{r}^{F} + \Delta_{r}^{A})} = \frac{(\Delta_{r}^{F} + \Delta_{r}^{A})}{(\Delta_{r}^{F} + \Delta_{r}^{F})} = \frac{(\Delta_{r}^{F} + \Delta_{r}^{A})}{(\Delta_{r}^{F} + \Delta_{r}^{A})} = \frac{(\Delta_{r}^{F} + \Delta_{r}^{A})}{$$

3
$$X_{t} = \frac{1}{2}X_{t-1} + E_{t} ; E_{t} \sim WN(0,1)$$

$$Y_{t} = X_{t} + Y_{t} ; Y_{t} \sim WN(0,0)$$

$$Y_{t} = X_{t} + Y_{t} ; Y_{t} \sim WN(0,0)$$

$$\{E_{t}\} \times \{Y_{t}\} \text{ index} \Rightarrow \{X_{t}\} \times \{Y_{t}\} \text{ are index}.$$

$$Y_{t} \approx WN(0,0) \times \{Y_{t}\} \times \{Y_{t}\} \text{ are index}.$$

$$Y_{t} \approx WN(0,0) \times \{Y_{t}\} \times \{$$

 $\begin{pmatrix} \chi_{BLP} \\ \beta_{BLP} \end{pmatrix} = \begin{pmatrix} \chi_0 & \chi_1 \\ \chi_1 & \chi_0 \end{pmatrix} \begin{pmatrix} \chi_1 \\ \chi_2 \end{pmatrix}$

use (1) to get ro, r, r2 and simplify.

BLP & X2 bosed on X1, X3, X4 P(X1, X3, X4) = x, X1 + x2 X3 + x3 X4 d1, d2, d3 3 E(X2-d,X1-d2X3-d3X4) is min w.r.t. x1,d3,d4 E(X2- x, X, - x2 X3- x3 X4) X; = 0 i=1,3,4 Y1 - d, r0 - d2 r2 - d3 r3 =0 Y, - d, 82 - d2 To - d3 Y, =0 V(.) Mindres of MA! $\chi = \begin{cases} 0.7 & h = 11 \\ 0.7 & h = 11 \end{cases}$ $B L P eq": \begin{pmatrix} x_1 \\ x_1 \end{pmatrix} = \begin{pmatrix} x_0 & 0 & 0 \\ 0 & x_0 & x_1 \\ 0 & x_1 & x_2 \end{pmatrix} \begin{pmatrix} x_1 \\ x_2 \\ x_3 \end{pmatrix}$ $\begin{pmatrix} d_{1}(BLP) \\ d_{2}(BLP) \end{pmatrix} = \begin{pmatrix} \sigma_{0} & 0 & 0 \\ 0 & \begin{pmatrix} r_{0} & r_{1} \\ r_{1} & r_{0} \end{pmatrix} \end{pmatrix} \begin{pmatrix} \sigma_{1} \\ \sigma_{1} \\ 0 \end{pmatrix}$

use ACVF structure of MA(1) to simplify.

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i.e.
$$Cov(x_{n+1}, y_{i}) = a_{1} Y_{y}(i-1) + \cdots + a_{n} Y_{y}(i-n)$$

i.e. $Cov(x_{n+1}, y_{i}) = a_{1} Y_{y}(0) + a_{2} Y_{y}(1) + \cdots + a_{n} Y_{y}(n-1)$

$$Cov(x_{n+1}, y_{n}) = a_{1} Y_{y}(n-1) + \cdots + a_{n} Y_{y}(n-1)$$

$$Cov(x_{n+1}, y_{i}) = a_{1} Y_{y}(n-1) + \cdots + a_{n} Y_{y}(0)$$

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$$Cov(x_{n+1}, y_{i}) = a_{1} Y_{y}(n) + a_{2} Y_{y}(n) + \cdots + a_{n} Y_{y}(n-1)$$

$$A_{1} Y_{y}(n) = a_{1} Y_{y}(n) + \cdots + a_{n} Y_{y}(n)$$

$$Cov(x_{n+1}, y_{i}) = a_{1} Y_{y}(n) + \cdots + a_{n} Y_{y}(n)$$

$$A_{1} Y_{y$$

use (1), (2), (3) in (4) to other (2)

(d)

$$BLP = \begin{pmatrix} x_{y(0)} & x_{y(1)} \\ x_{y(1)} & x_{y(0)} \end{pmatrix}^{-1} \begin{pmatrix} x_{x}(2) \\ x_{x}(3) \end{pmatrix}$$

(b) PACF at $\log 2 \Re \{y_{t}\}$
 $M(2) = \log ((y_{3} - P_{y_{2}})^{3}, y_{1} - P_{y_{2}}) - (*)$
 $P_{y_{2}} = P_{y_{1}} (y_{2}) + P_{y_{2}} (y_{3}) + P_{y_{2}} (y_{1}) + P_{y_{2}} (y$

$$\Rightarrow \begin{array}{c} 0 = 6 \, \alpha \\ -1 = 6 \, \beta \end{array} \Rightarrow \begin{array}{c} x = 0 \, ; \beta = -\frac{1}{6} \\ (x_{4}, x_{3}) \end{array}$$

(a)

(b)
$$E\left(X_{5} + \frac{1}{6}X_{3}\right)^{2}$$

 $= EX_{5}^{2} + \frac{1}{36}EX_{3}^{2} + 2 \cdot \frac{1}{6}EX_{5}X_{3}$
 $= Y_{0} + \frac{1}{36}Y_{0} + \frac{1}{3}Y_{2}$
 $= 6 + \frac{1}{36}6 + \frac{1}{3}(-1)$

(c) PACF at leg 2 =
$$\chi(2)$$

= $Lord^n \left(x_1 P_{\chi_2} X_1, \chi_3 P_{\chi_2} X_3 \right) = Lord^n \left(\chi_1 - P(1) \chi_2, \chi_3 - P(1) \chi_2 \right)$
= $Lord^n \left(\chi_1, \chi_3 \right) = \frac{\chi_2}{\chi_0} = -\frac{1}{6}$