```
fun append (xs,ys) =
    if xs=[]
    then ys
    else (hd xs)::append(tl xs,ys)

fun map (f,xs) =
    case xs of
      [] => []
      | x::xs' => (f x)::(map(f,xs'))

val a = map (increment, [4,8,12,16])
val b = map (hd, [[8,6],[7,5],[3,0,9]])
```

Programming Languages Dan Grossman

Introduction to First-Class Functions

What is functional programming?

"Functional programming" can mean a few different things:

- Avoiding mutation in most/all cases (done and ongoing)
- 2. Using functions as values (this section)

. . .

- Style encouraging recursion and recursive data structures
- Style closer to mathematical definitions
- Programming idioms using laziness (later topic, briefly)
- Anything not OOP or C? (not a good definition)

Not sure a definition of "functional language" exists beyond "makes functional programming easy / the default / required"

No clear yes/no for a particular language

First-class functions

- First-class functions: Can use them wherever we use values
 - Functions are values too
 - Arguments, results, parts of tuples, bound to variables, carried by datatype constructors or exceptions, ...

```
fun double x = 2*x
fun incr x = x+1
val a_tuple = (double, incr, double(incr 7))
```

- Most common use is as an argument / result of another function
 - Other function is called a higher-order function
 - Powerful way to factor out common functionality

Function Closures

- Function closure: Functions can use bindings from outside the function definition (in scope where function is defined)
 - Makes first-class functions much more powerful
 - Will get to this feature in a bit, after simpler examples
- Distinction between terms first-class functions and function closures is not universally understood
 - Important conceptual distinction even if terms get muddled

Onward

Most of this section of course:

- How to use first-class functions and closures
- The precise semantics
- Multiple powerful idioms