

```
fun append (xs,ys) =  
  if xs=[]  
  then ys  
  else (hd xs)::append(tl xs,ys)  
  
fun map (f,xs) =  
  case xs of  
    [] => []  
  | x::xs' => (f x)::(map(f,xs'))  
  
val a = map (increment, [4,8,12,16])  
val b = map (hd, [[8,6],[7,5],[3,0,9]])
```

Programming Languages

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Partial Application

“Too Few Arguments”

- Previously used currying to simulate multiple arguments
- But if caller provides “too few” arguments, we get back a closure “waiting for the remaining arguments”
 - Called partial application
 - Convenient and useful
 - Can be done with any curried function
- No new semantics here: a pleasant idiom

Example

```
fun fold f acc xs =  
  case xs of  
    []      => acc  
  | x::xs' => fold f (f(acc,x)) xs'  
  
fun sum_inferior xs = fold (fn (x,y) => x+y) 0 xs  
  
val sum = fold (fn (x,y) => x+y) 0
```

As we already know, `fold (fn (x,y) => x+y) 0`
evaluates to a closure that given `xs`, evaluates the case-expression
with `f` bound to `fold (fn (x,y) => x+y)` and `acc` bound to 0

Unnecessary function wrapping

```
fun sum_inferior xs = fold (fn (x,y) => x+y) 0 xs  
  
val sum = fold (fn (x,y) => x+y) 0
```

- Previously learned not to write `fun f x = g x` when we can write `val f = g`
- This is the same thing, with `fold (fn (x,y) => x+y) 0` in place of `g`

Iterators

- Partial application is particularly nice for iterator-like functions
- Example:

```
fun exists predicate xs =  
  case xs of  
    []      => false  
  | x::xs' => predicate x  
              orelse exists predicate xs'  
  
val no = exists (fn x => x=7) [4,11,23]  
val hasZero = exists (fn x => x=0)
```

- For this reason, ML library functions of this form usually curried
 - Examples: `List.map`, `List.filter`, `List.foldl`

The Value Restriction Appears ☹

If you use partial application to *create a polymorphic function*, it may not work due to the **value restriction**

- Warning about “type vars not generalized”
 - And won’t let you call the function
- This should surprise you; you did nothing wrong 😊 but you still must change your code
- See the code for workarounds
- Can discuss a bit more when discussing type inference