$\ell \in \{1, \ldots, \mathcal{L}\}:$