a)
$$\operatorname{rand}(\hat{\sigma}), \mathcal{T}_{\hat{\sigma}} \neq 0$$

$$\mathcal{I}_{\ell} = \{(\hat{\sigma}_{1}, \dots, \hat{\sigma}_{\ell})\} \quad \forall \ell$$

$$\mathcal{I}_{\ell} = \{(\hat{\sigma}_{\ell+1}, \dots, \hat{\sigma}_{\mathcal{L}})\} \quad \forall \ell$$

$$\mathcal{I}_{\ell} = \{(\hat{\sigma}_{\ell+1}, \dots, \hat{\sigma}_{\ell+1}, \dots, \hat{\sigma}_{\ell+1}, \dots, \hat{\sigma}_{\ell+1}, \dots, \hat{\sigma}_{\ell+1}, \dots, \hat{\sigma}_{\ell+1}, \dots, \hat{\sigma}_{\ell+1}$$