

**COMPLEX
NETWORKS**

Mirko Lai, Salvatore Vilella, Giancarlo Ruffo, and Federica Cena



UPO

UNIVERSITÀ DEL PIEMONTE ORIENTALE



UNIVERSITÀ
DI TORINO

A Complex Networks Approach to Evaluate the 15-Minute City Paradigm and Urban Segregation

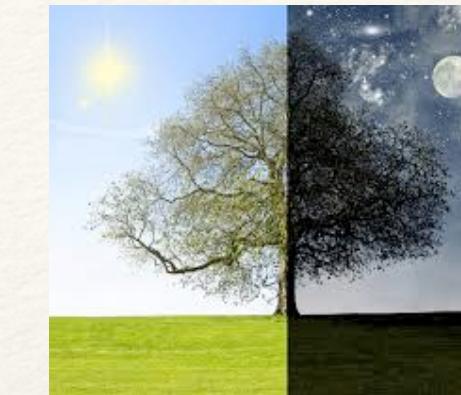
Exploring Urban Accessibility,
Connectivity, and Segregation Through
Network Science

Bright and dark sides of the "15 minute" city



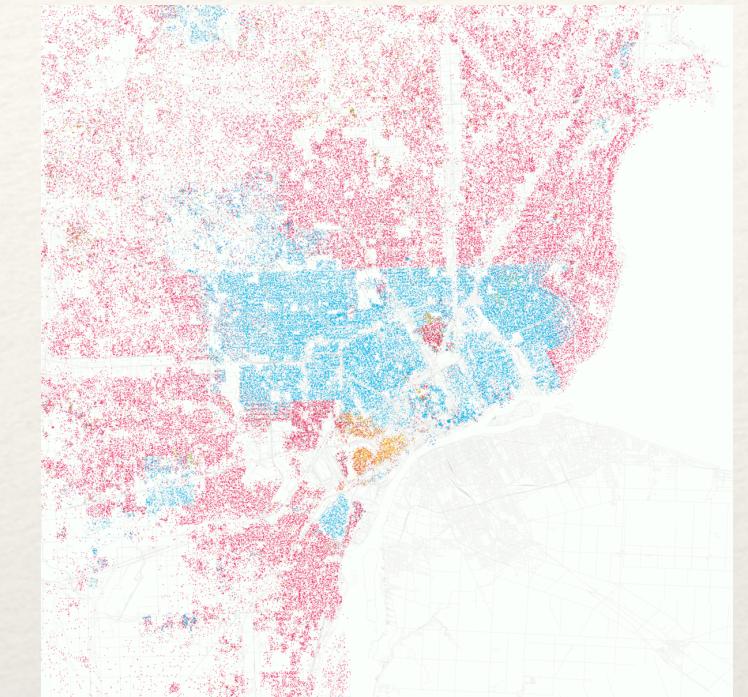
❖ **Walkable and accessible** cities:
everything you *really* need is **close**:

- ❖ healthcare
- ❖ arts, museums, theaters
- ❖ education
- ❖ parks
- ❖ shopping
- ❖ (work)
- ❖ *water supply*
- ❖ *electricity*



❖ Self-sufficiency can accelerate
urban segregation:

- ❖ no cars: you are dependent on public transport for medium-long trips
- ❖ smaller urban areas self-organize and are governed by homophily
- ❖ but larger districts are more heterogeneous in terms of social class, education, income



Is the ‘15-minute city’ idea a utopian ideal or dystopian nightmare?

AP

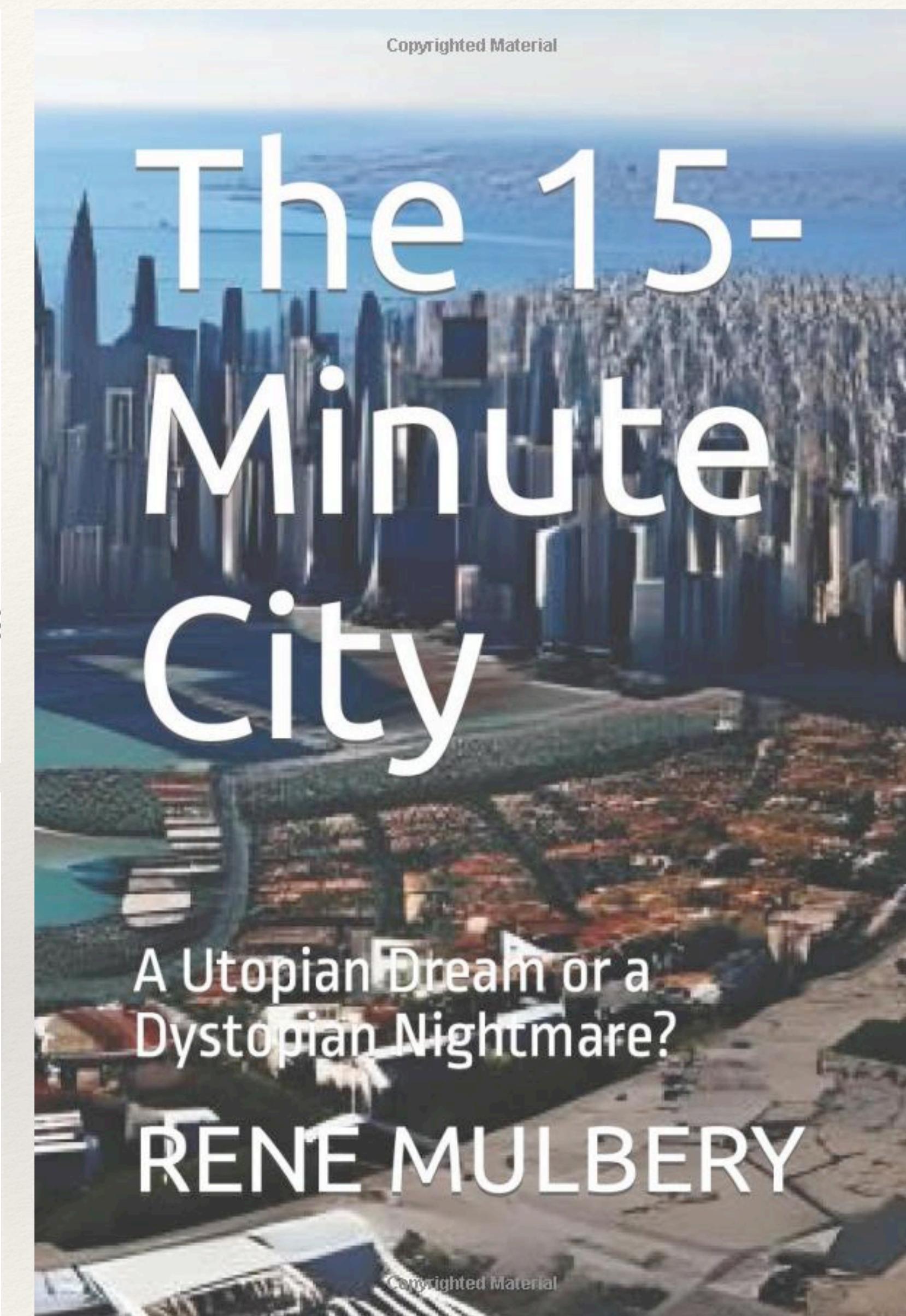
By Philip Marcelo

3 Mar, 2023 03:46 AM ⏳ 5 mins to read

15-minute cities: Path to dystopia or storm in a side street?

Urban planners and transportation professionals will need to address wild accusations about the motives behind 15-minute cities - and relevant criticisms too - if the concept is to scale to its potential

Air Quality & Weather Systems / June 5, 2023



Research questions

1. What patterns emerge when using complex network measures?
2. How does accessibility relate to urban connectivity and segregation?
3. Can I use accessibility and connectivity metrics for comparative purposes at different scales (i.e., cities, districts, census areas, residential addresses)?

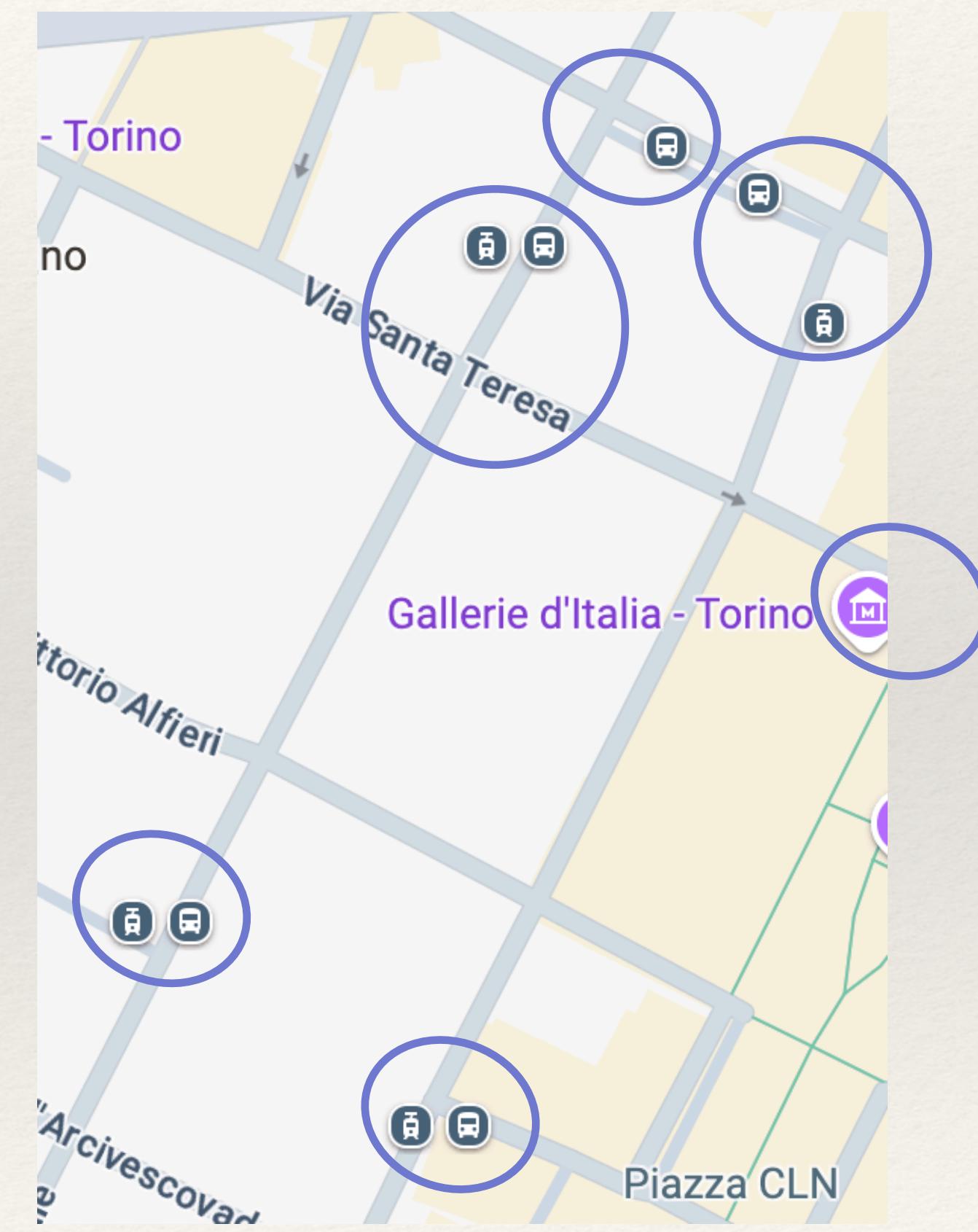
Methods

- ❖ Data sources: OpenStreetMap, GTFS data, and Census data
 - ❖ Socio-demographic data when available
- ❖ Network construction (given a city c):
 - ❖ We map every **PoI** (including bus/metro/train stops) and every **residential address** to the closest intersection
 - ❖ **nodes**: intersections; **links**: streets segments
weights: distance and transit time
 - ❖ **Pedestrian networks** for calculating accessibility to services and amenities
 $G_c^{\text{ped}} = (N_c, E_c)$
 - ❖ **Urban transport networks** for city scale connectivity
 $G_c^{\text{urb}} = (N_c, L_c)$



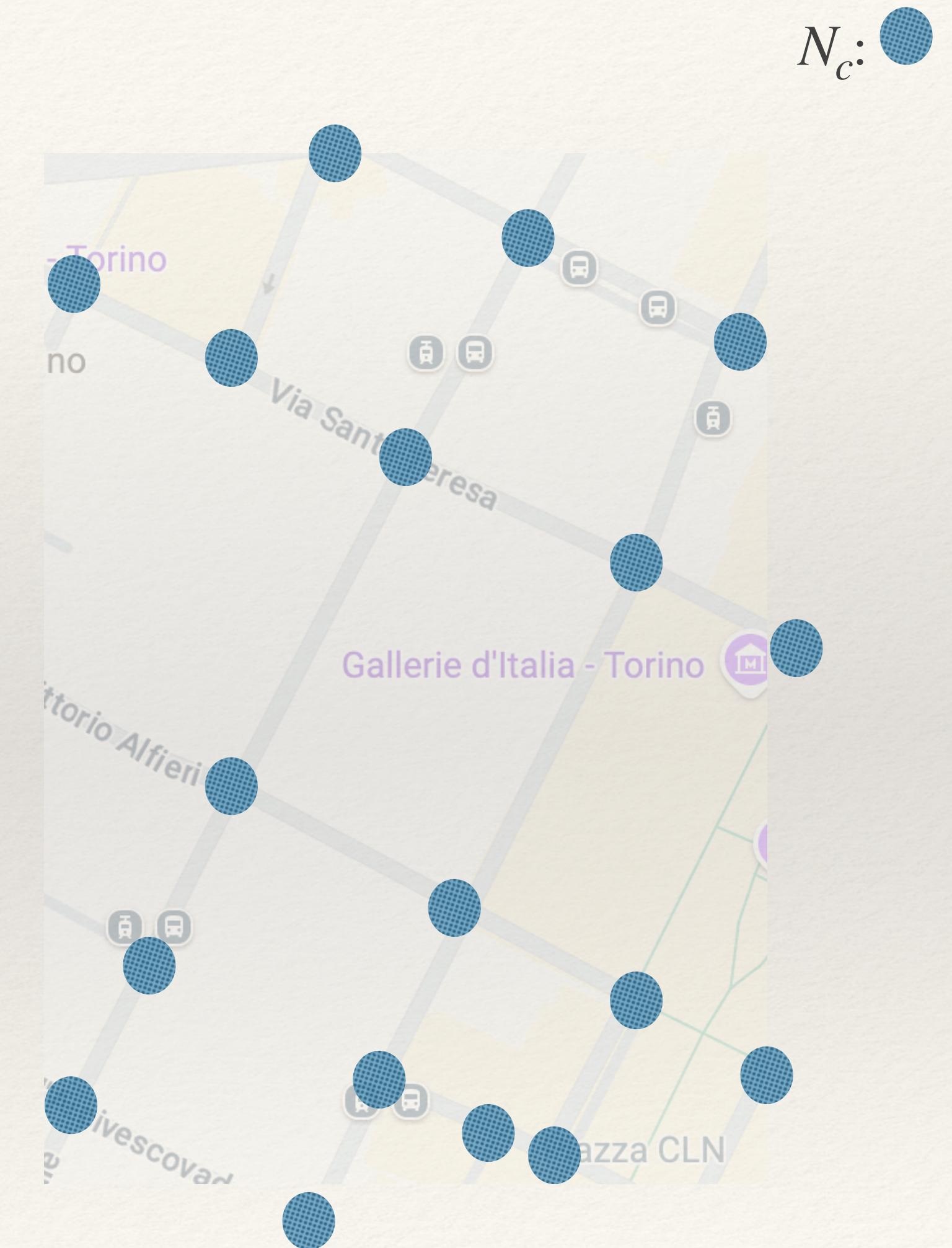
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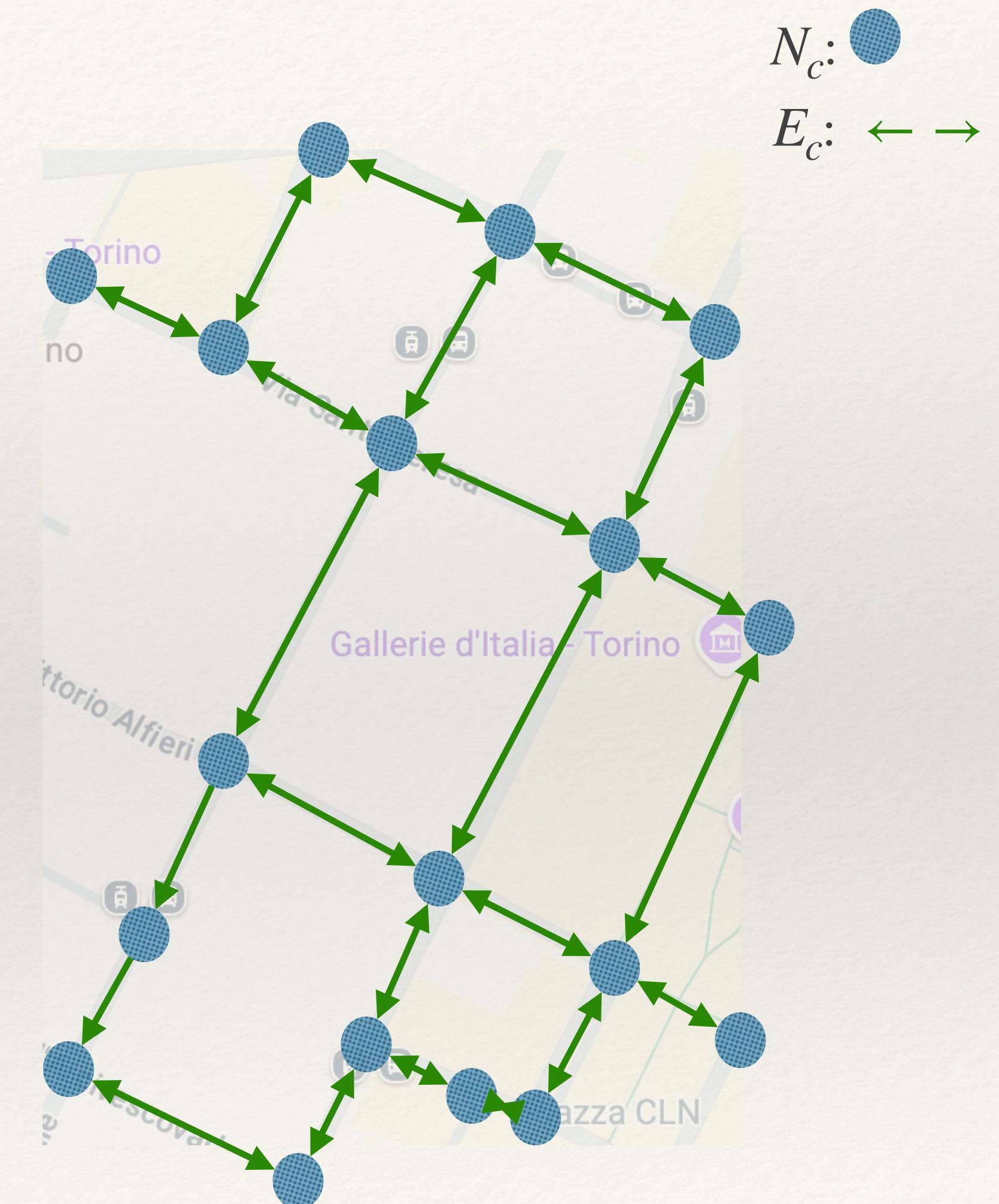


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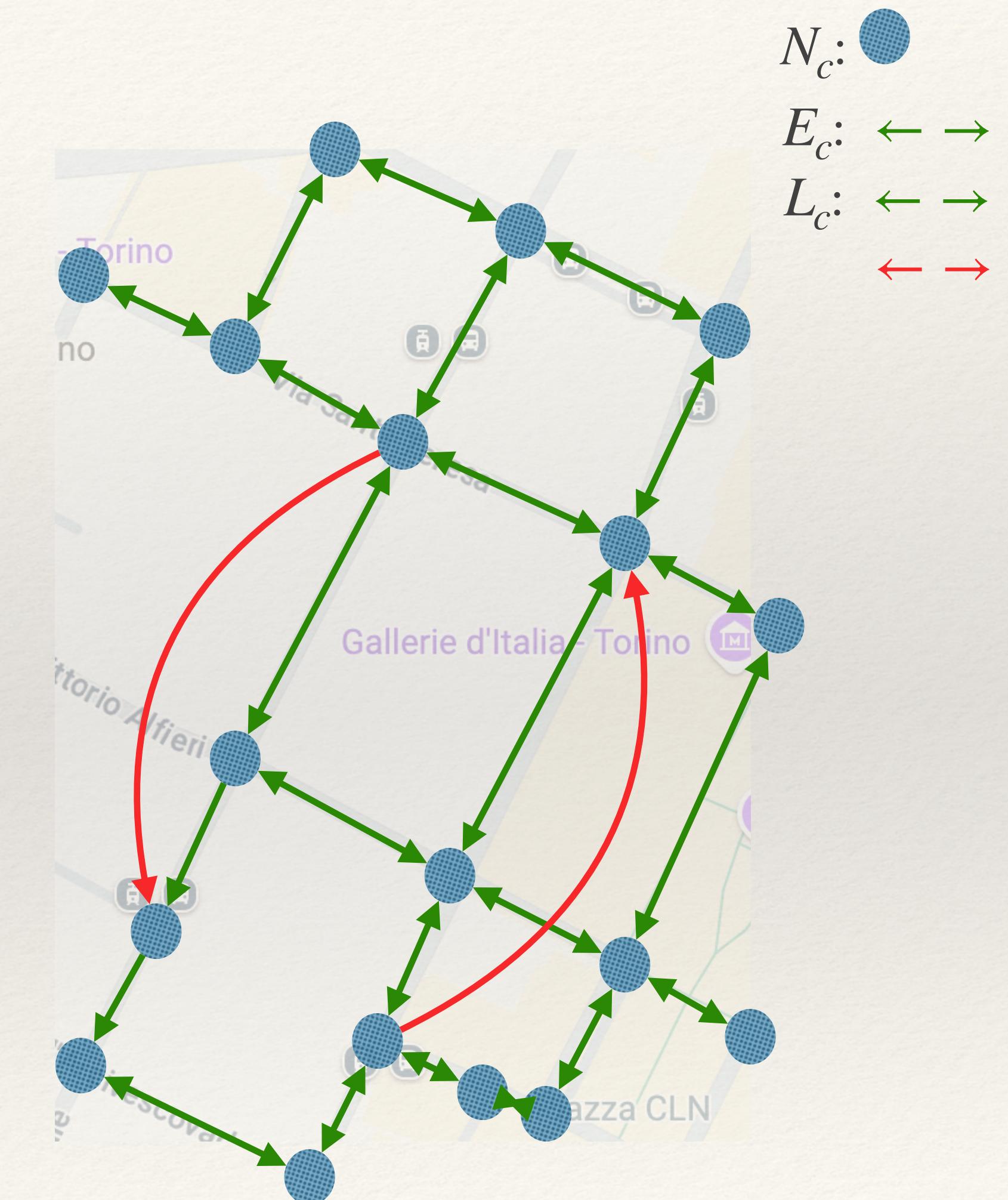


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Accessibility Metrics

- ❖ Given $n \in N_c$
 - ❖ PoI-Proximity $\mathcal{P}(n) = t$
 - ❖ PoI-Density $\mathcal{D}(n, t)$
 - ❖ PoI-Entropy $\mathcal{E}(n, t)$
 - ❖ PoI-Accessibility $\mathcal{A}(n, t)$

PoI's categories:

Mobility



Active Living



Entertainment



Food Choices



Community



Education



Health and Well-being



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n

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Active Living



Entertainment



Food Choices



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Education

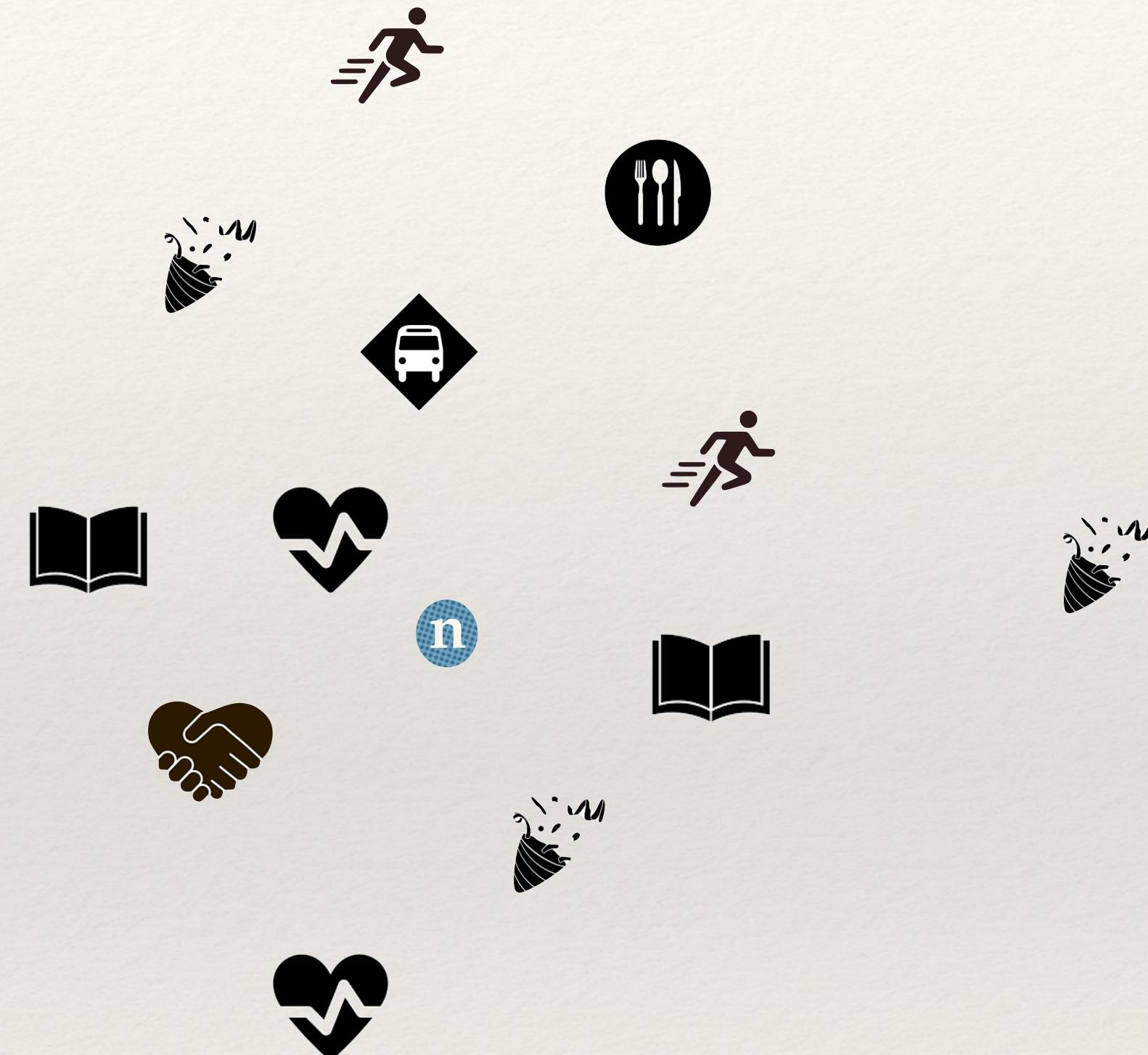


Health and Well-being



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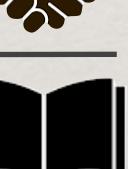
Food Choices



Community



Education



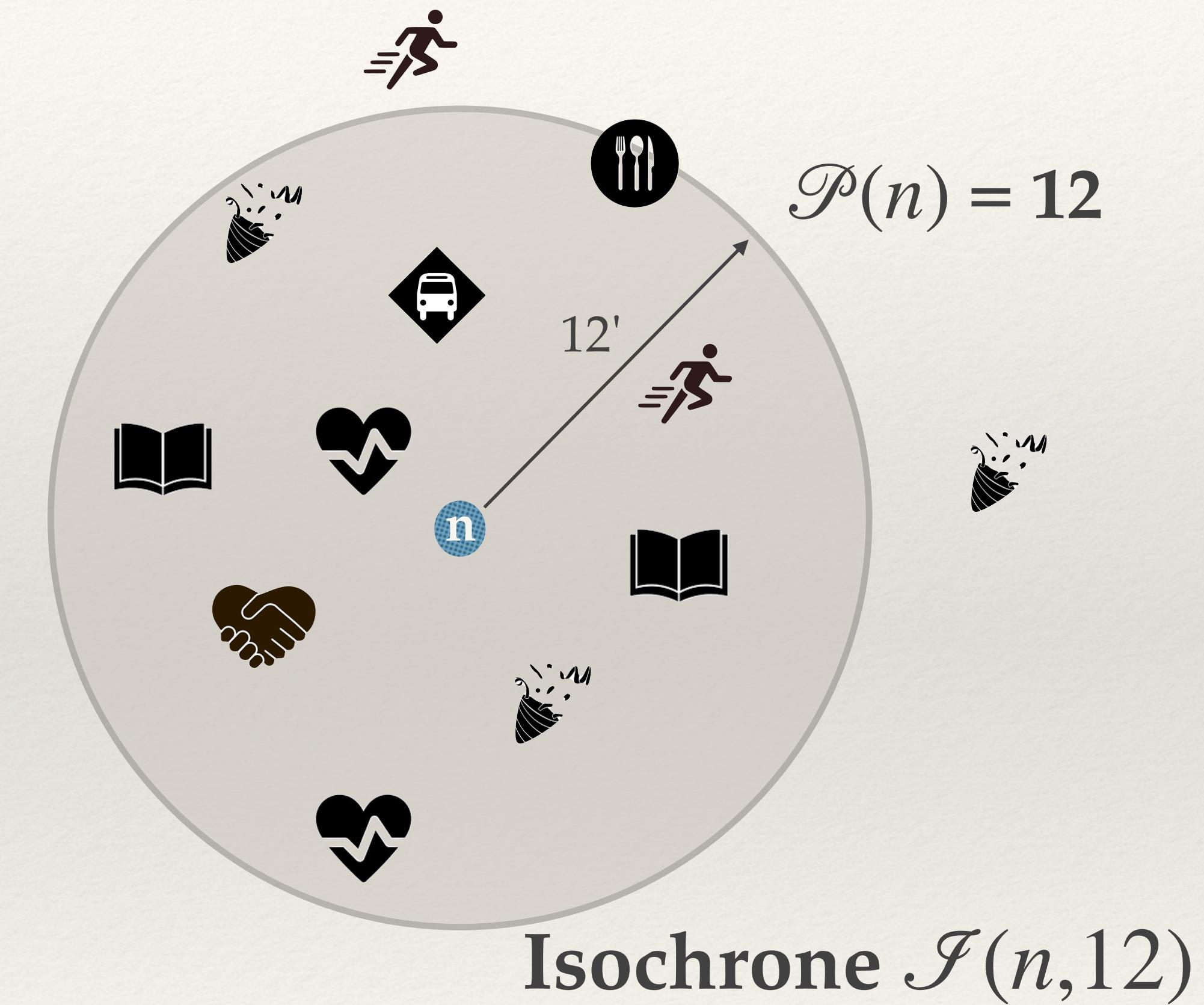
Health and Well-being



$\mathcal{P}(n) = t$: at least one PoI for each category is within t minutes walk

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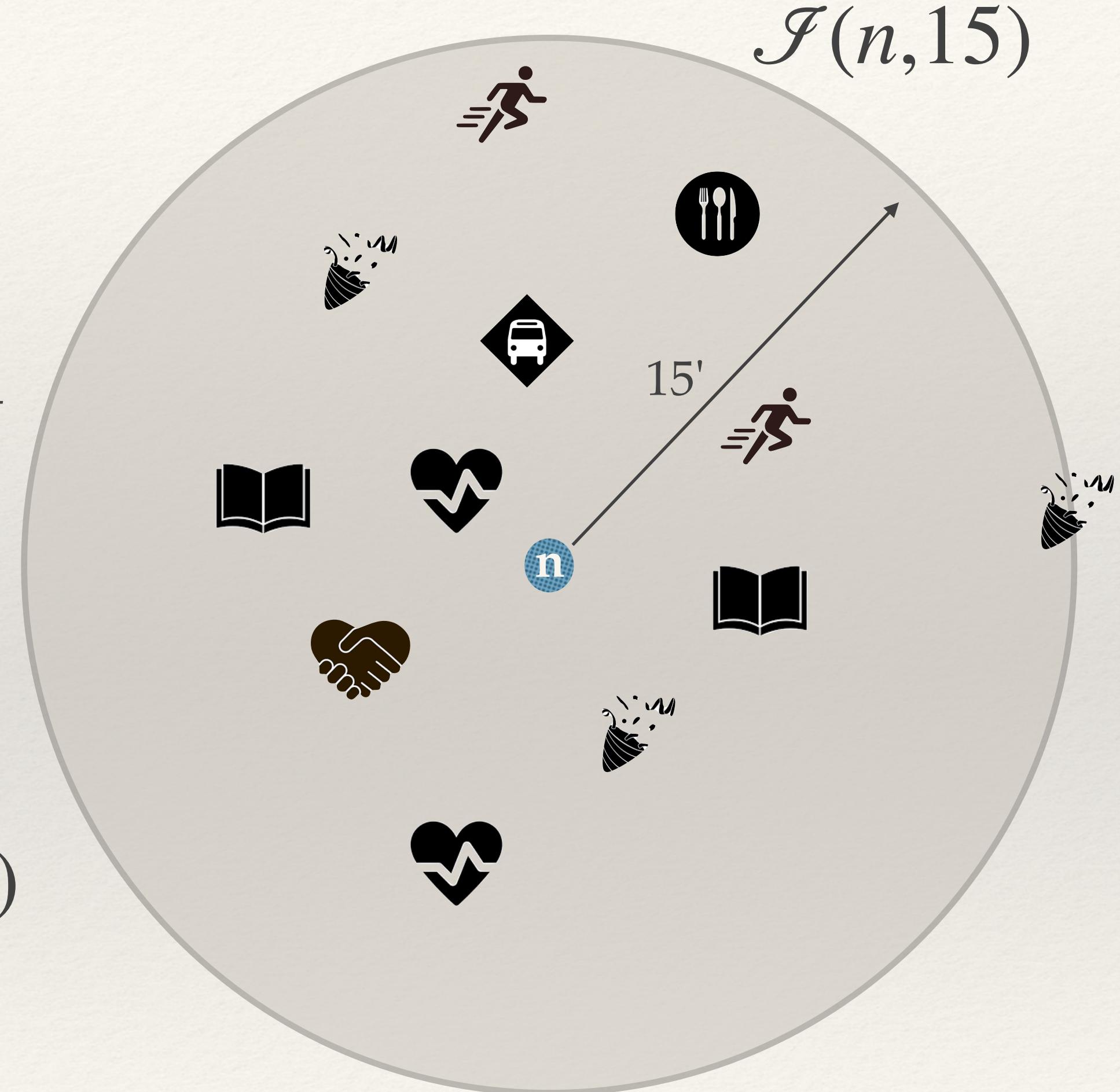
Health and Well-being



$\mathcal{P}(n) = 12$: at least one PoI for each category is within 12 minutes walk

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PoI's categories:

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Food Choices



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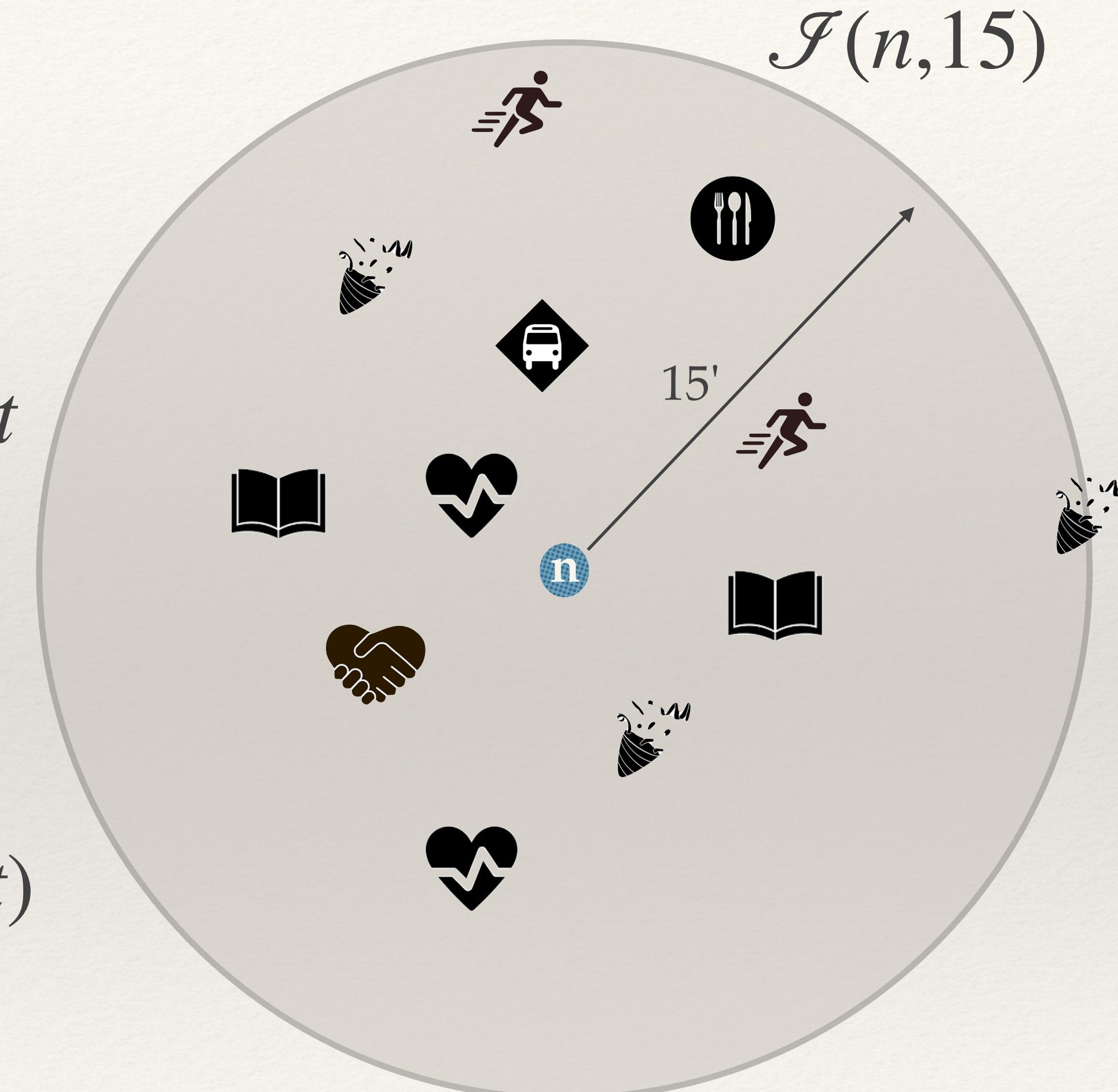
Health and Well-being



$$\mathcal{P}(n) = 12$$

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PoI's categories:

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Food Choices



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Education



Health and Well-being

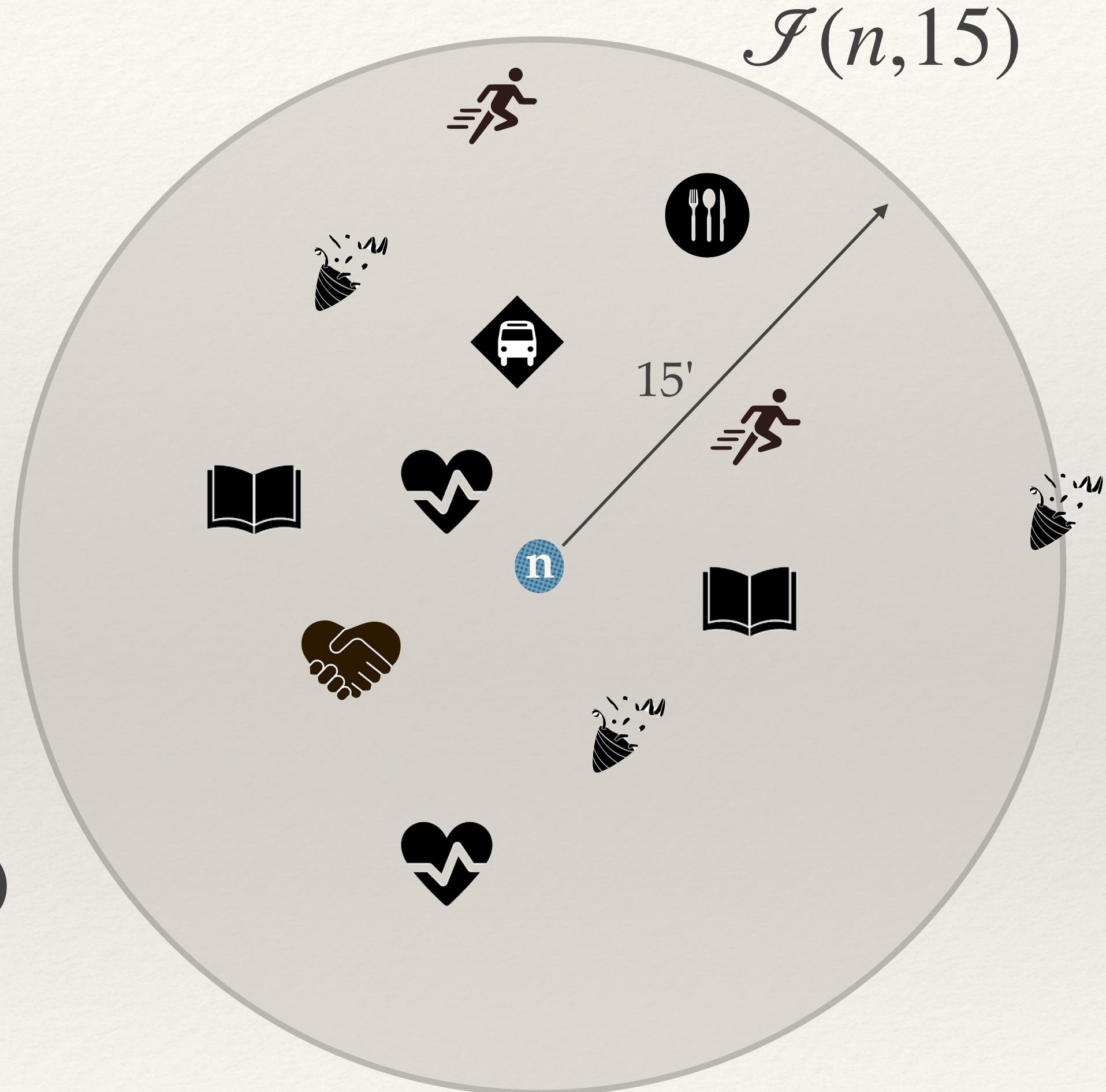


$$\mathcal{P}(n) = 12$$

$$\mathcal{D}(n, 15) = \frac{|\text{PoIs} \in \mathcal{J}(15)|}{\text{Area of } \mathcal{J}(n, 15)} = \frac{12}{7\text{km}^2} = 1.71$$

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PoI's categories:

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Food Choices



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Education



Health and Well-being

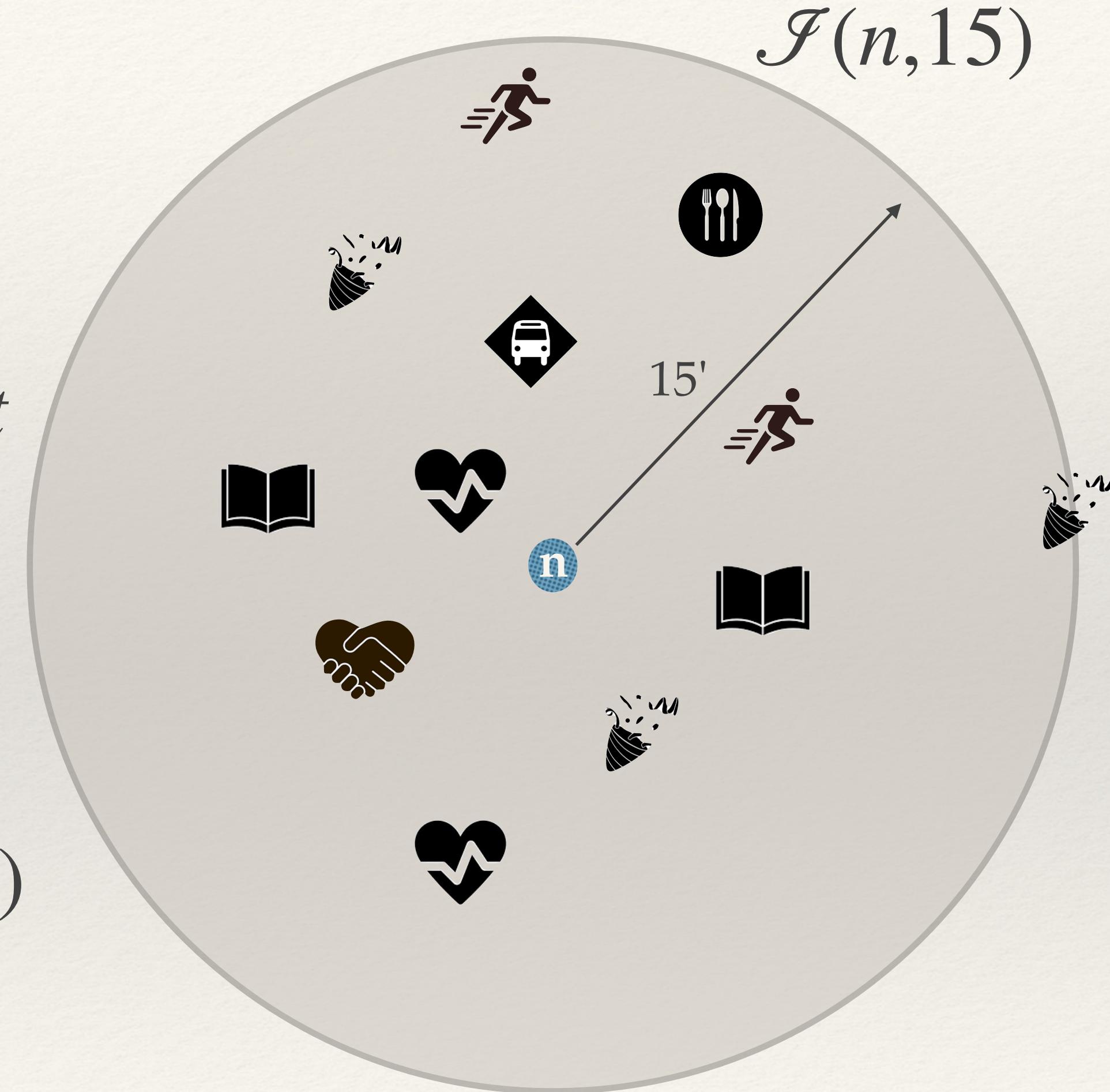


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PoI's categories:

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Entertainment



Food Choices



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Health and Well-being



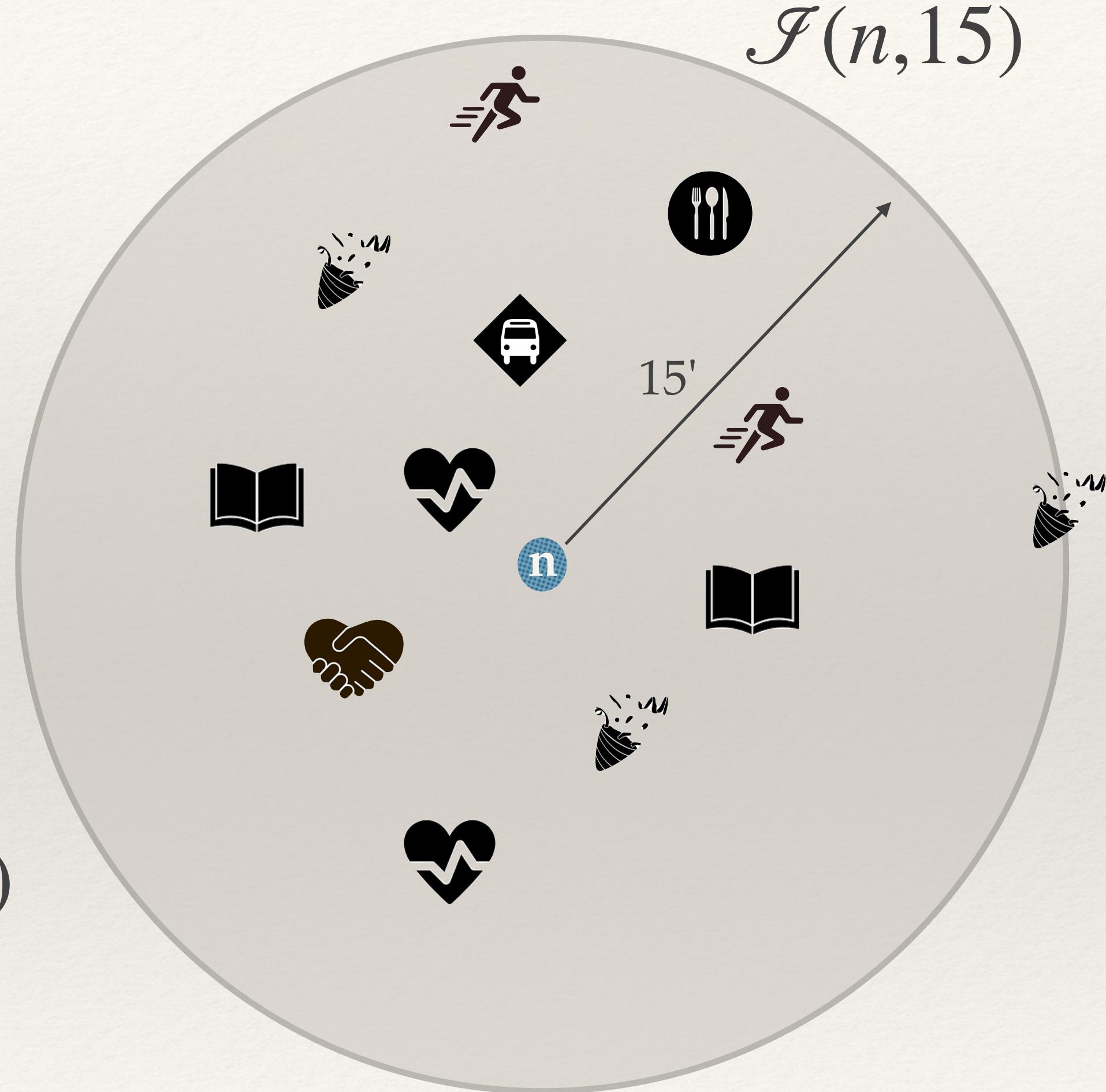
$$\mathcal{P}(n) = 12$$

$$\mathcal{D}(n, 15) = 1.71$$

$\mathcal{E}(n, 15)$ = the entropy of the distribution of PoIs' categories within $\mathcal{J}(n, 15) = 2.69$

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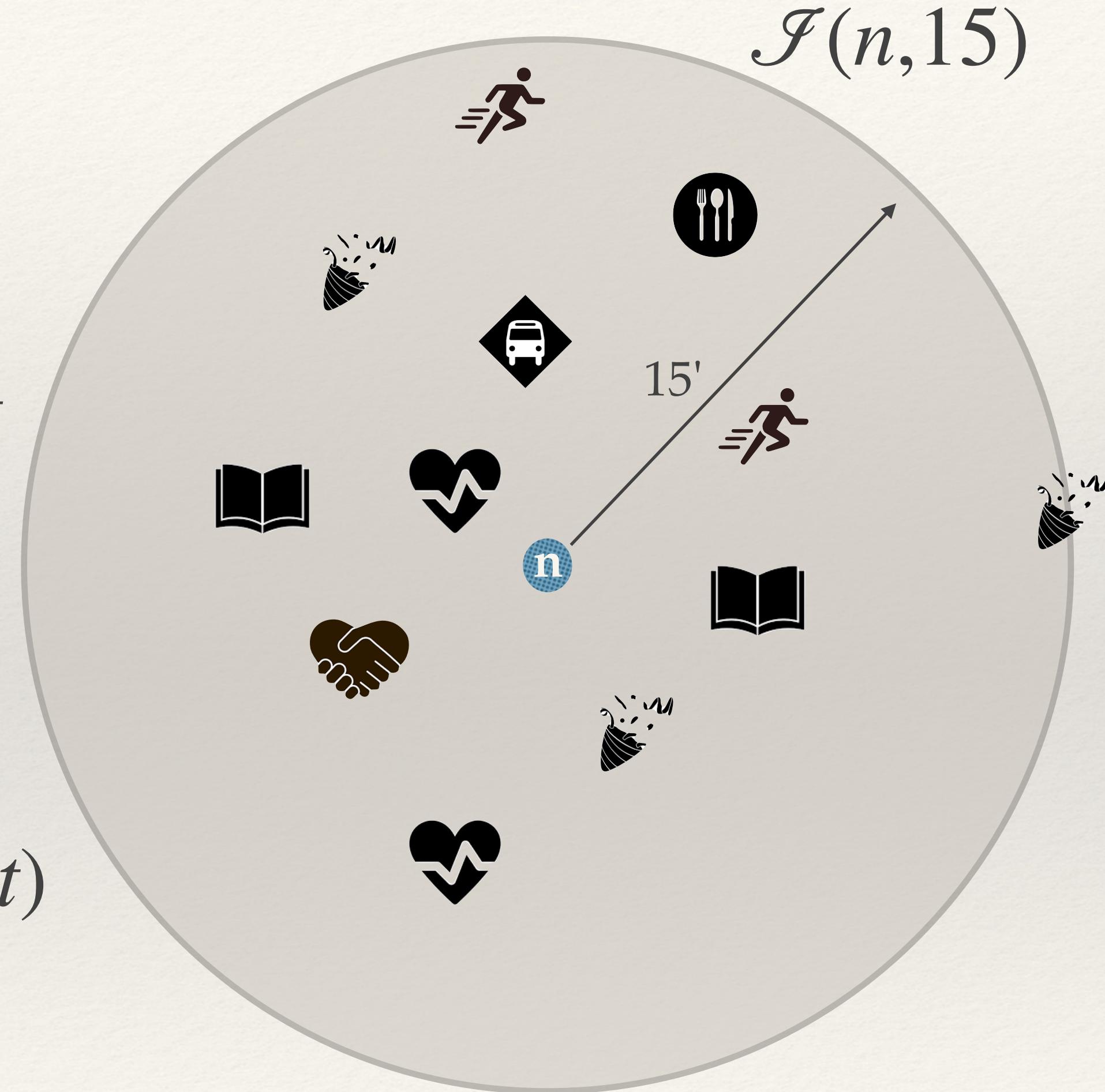
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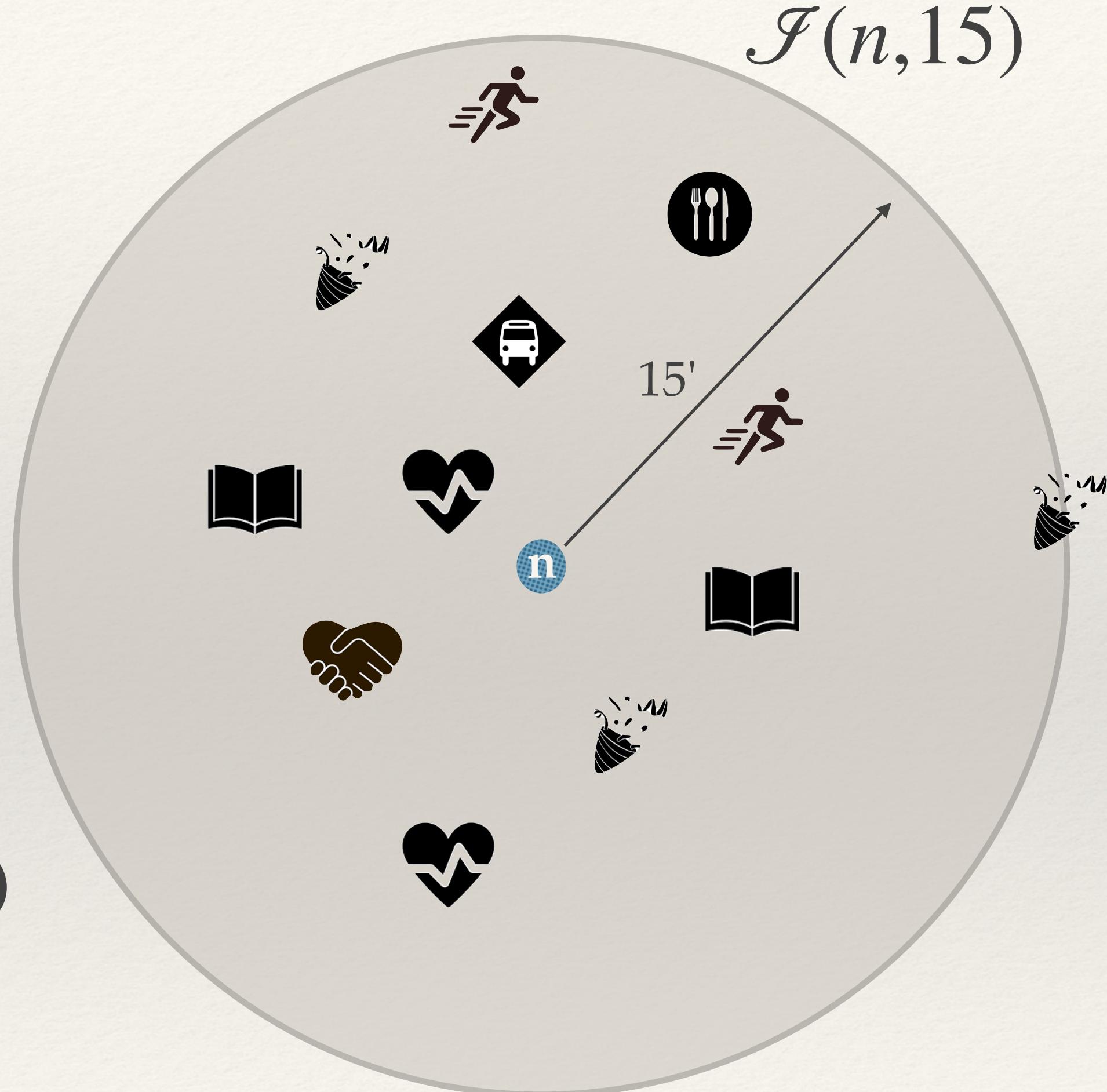
$$\mathcal{D}(n, 15) = 1.71$$

$$\mathcal{E}(n, 15) = 2.69$$

$$\mathcal{A}(n, t) = w_1 \mathcal{P}'(n) + w_2 \mathcal{D}'(n, t) + w_3 \mathcal{E}'(n, t) \quad \text{e.g., } w_1 = w_2 = w_3 = 1/3, \text{ and } t = 15$$

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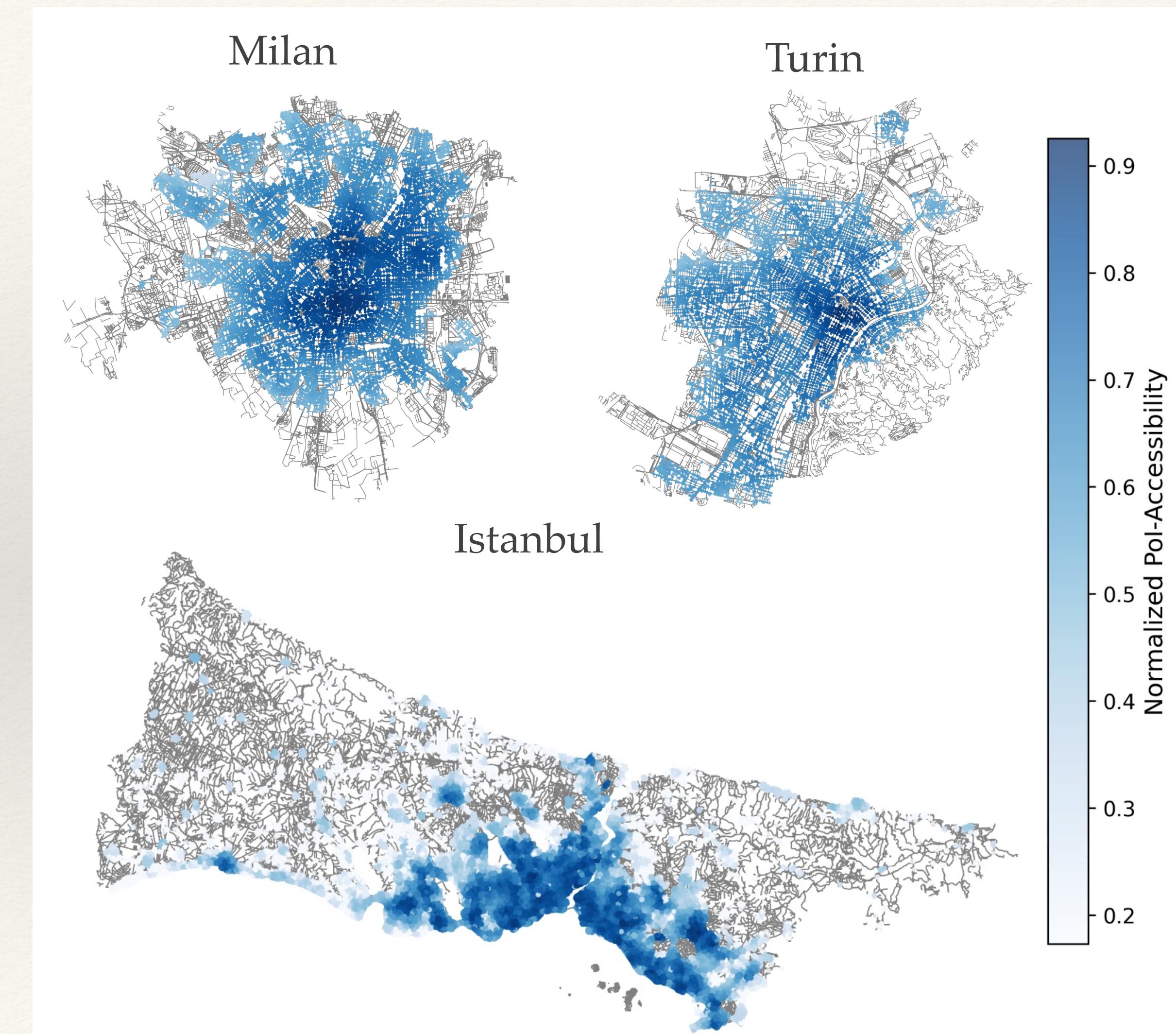
$$\mathcal{D}(n, 15) = 1.71$$

$$\mathcal{E}(n, 15) = 2.69$$

$$\mathcal{A}(n, 15) \in [0, 1]$$

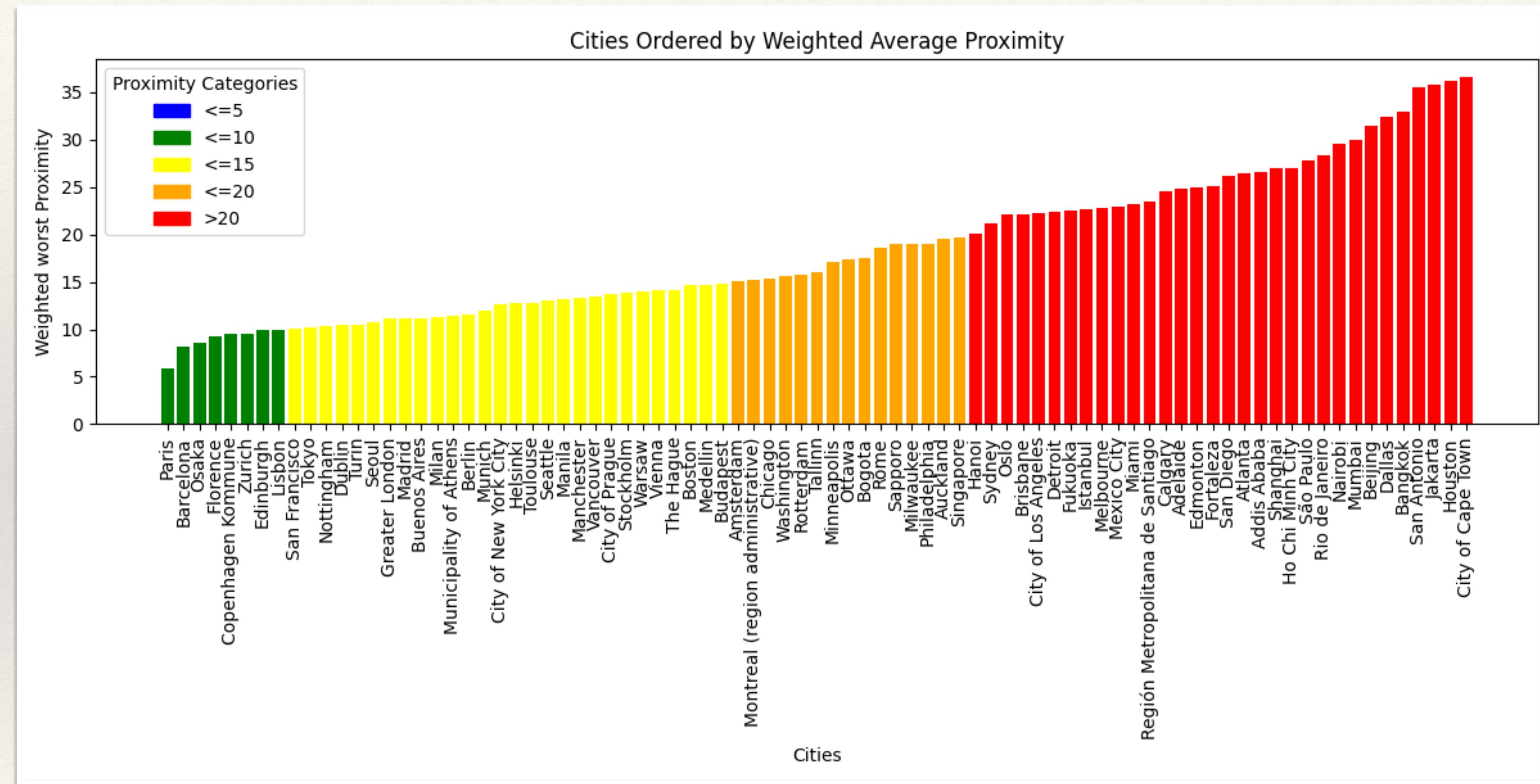
Accessibility metrics at different scales

- ❖ All the above metrics can be calculated for every node $n \in N_c$
- ❖ RQ1: we can calculate a range of metrics' statistics:
 - ❖ scales: census area, network clusters (e.g., by infomap), administrative districts, the city as whole
 - ❖ statistics: min, max, average, std, ...
 - ❖ other:
 - ❖ how much people live in residential addresses with $\mathcal{P}(n) = t$?
 - ❖ Do income/education/immigration rate correlate with accessibility?
 - ❖ ...



Comparing and ranking cities

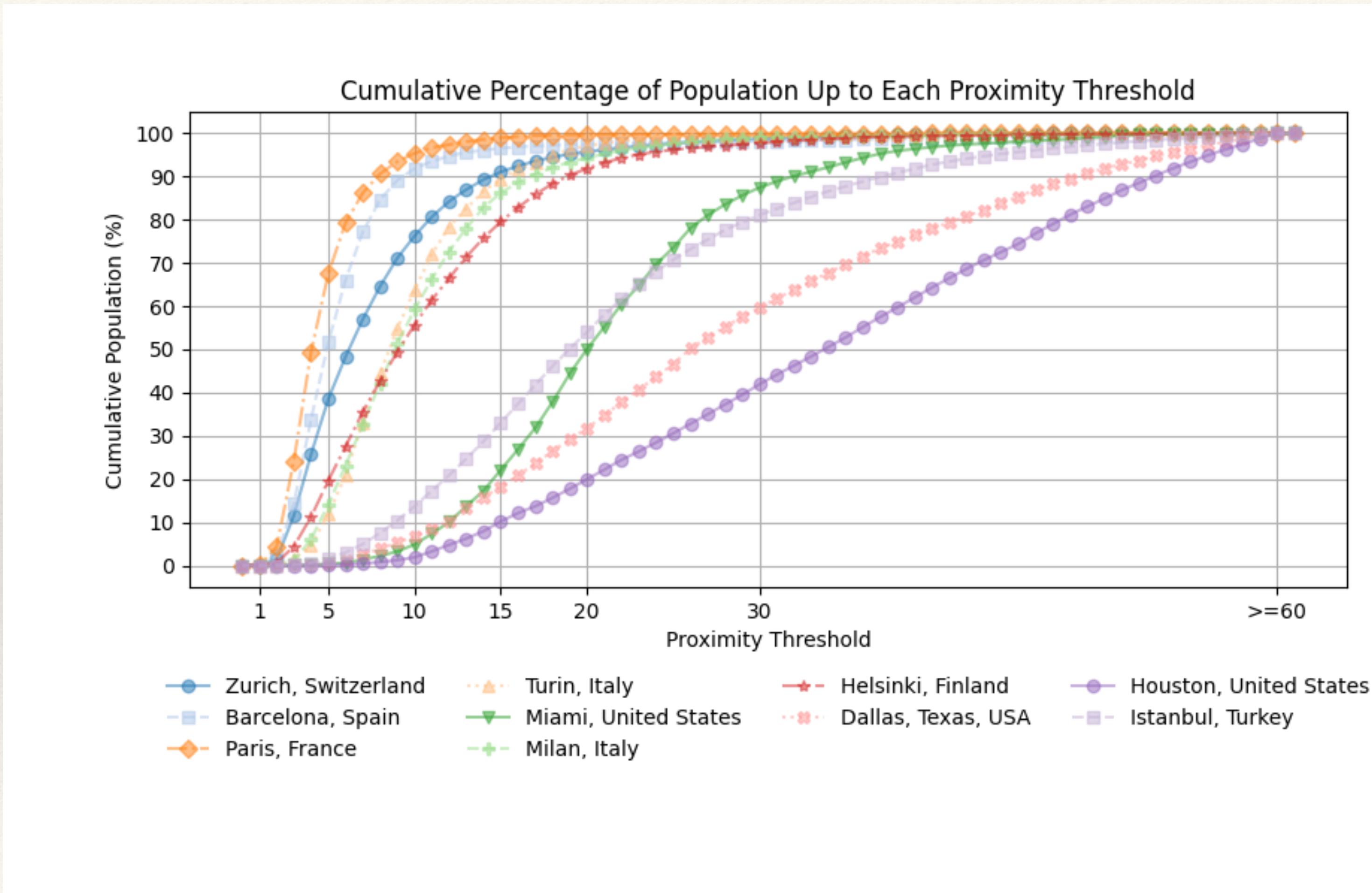
- ❖ High correlation
(Kendall's $\tau > 0.6$)
with other rankings
based on variants of
this proximity
measure [1, 2]



[1] Nicoletti, L., et al. (2023). Disadvantaged communities have lower access to urban infrastructure. Environment and Planning B: Urban Analytics and City Science, 50(3), 831-849.

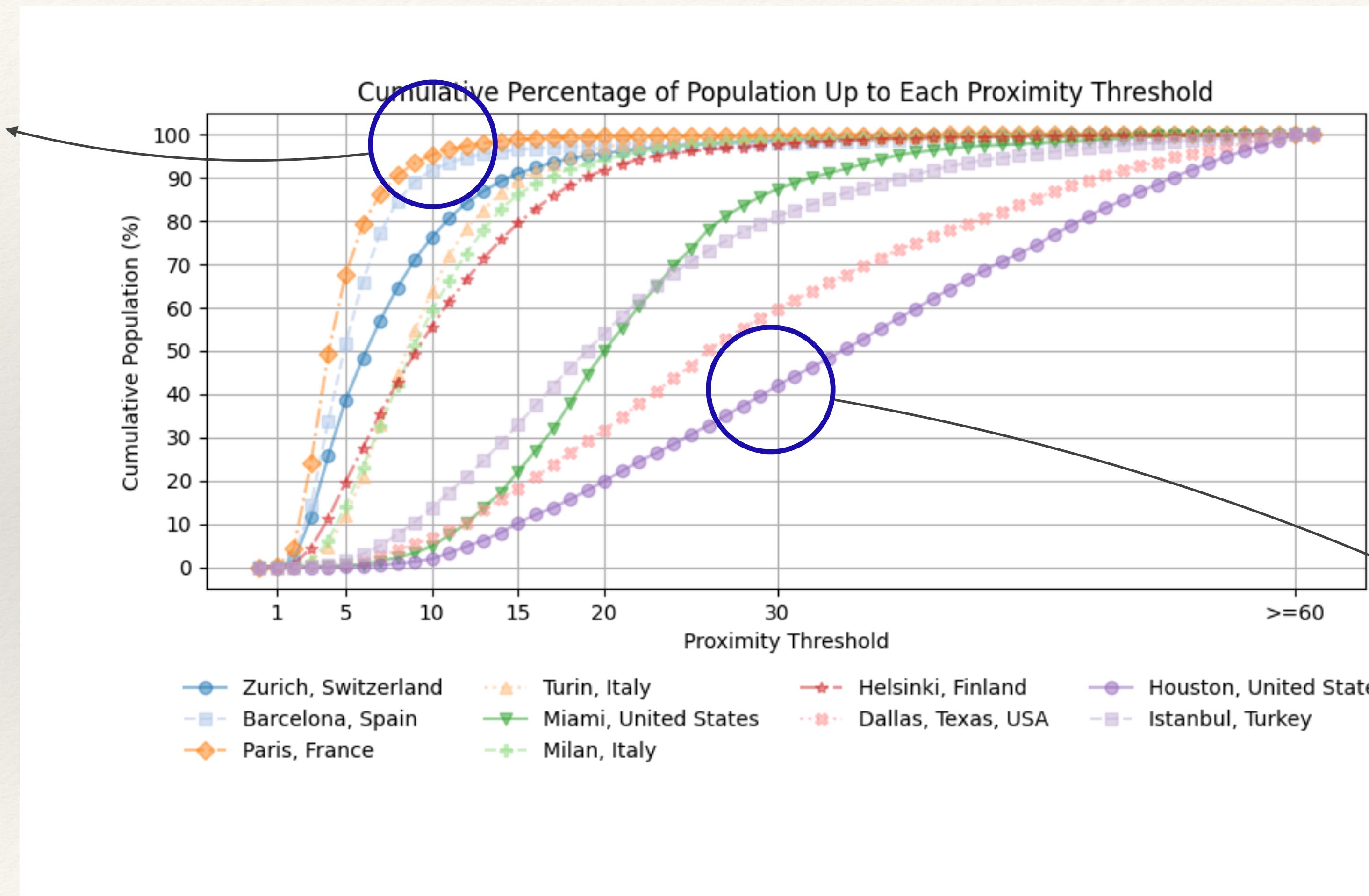
[2] Bruno, M., et al. A universal framework for inclusive 15-minute cities. Nat Cities 1, 633–641 (2024).

Comparing and ranking cities



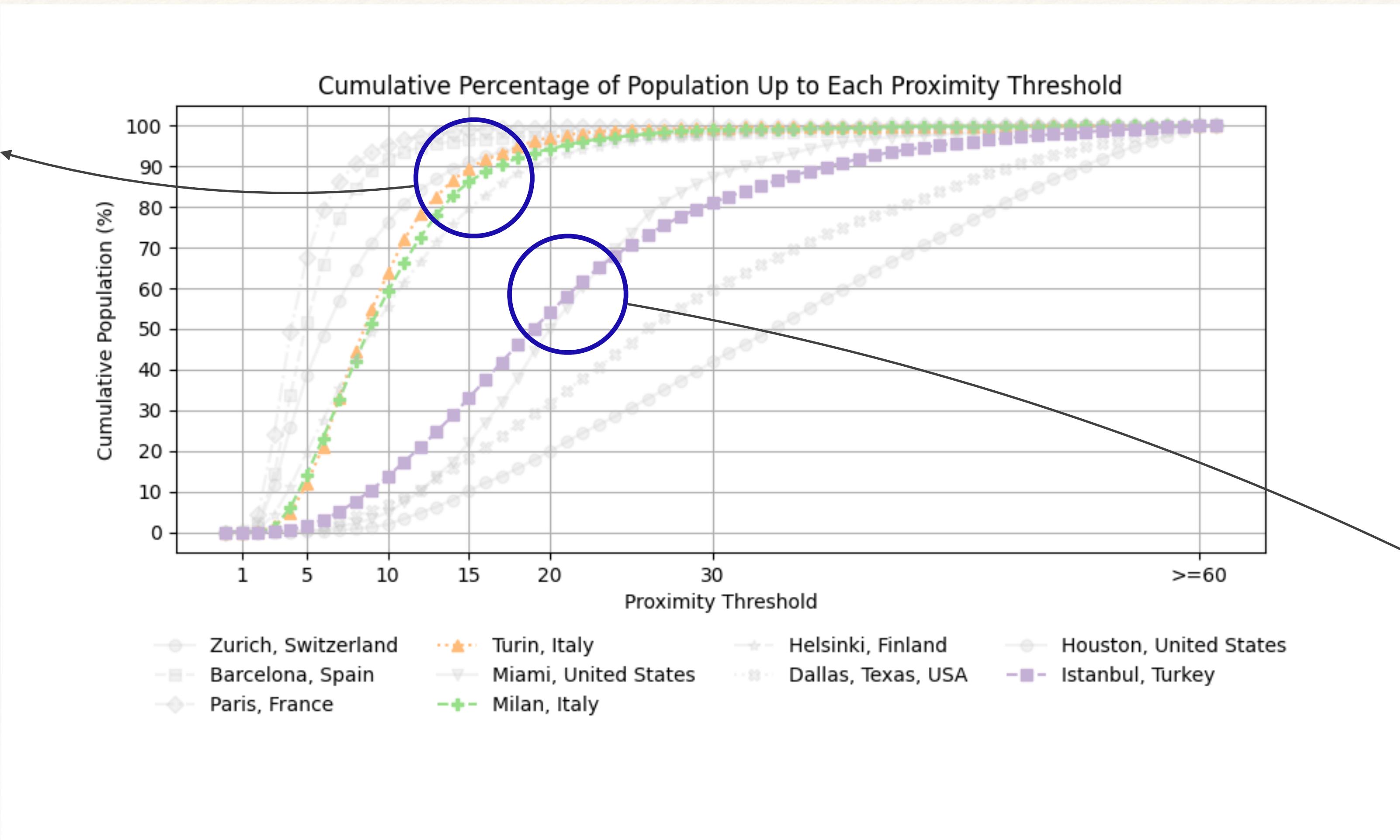
Comparing and ranking cities

> 90% of Paris citizens
live in places with
 $\mathcal{P}(n) \leq 10!$



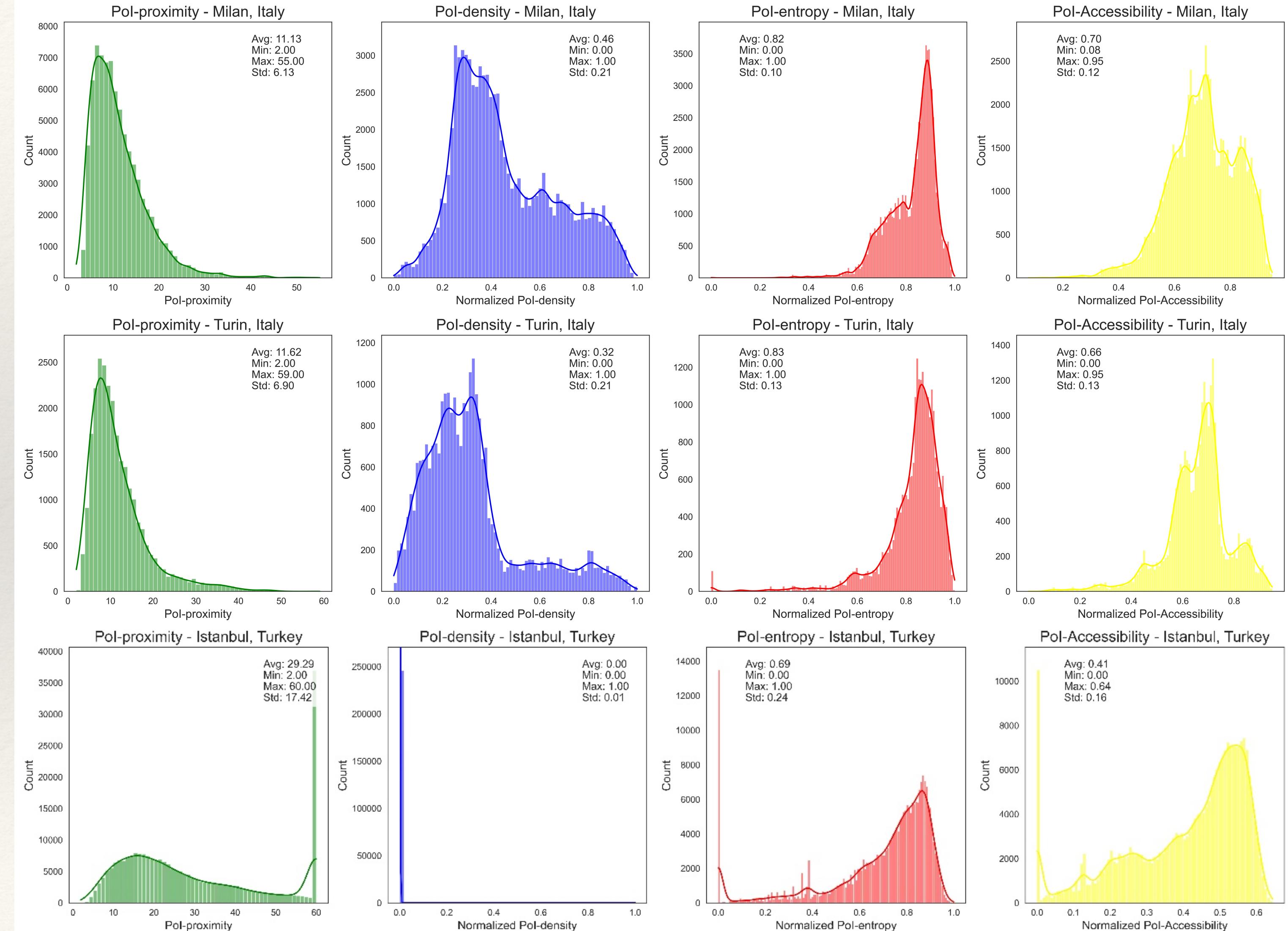
Comparing and ranking cities

$\sim 90\%$ of Milan
and Turin citizens
live in places with
 $\mathcal{P}(n) \leq 15$



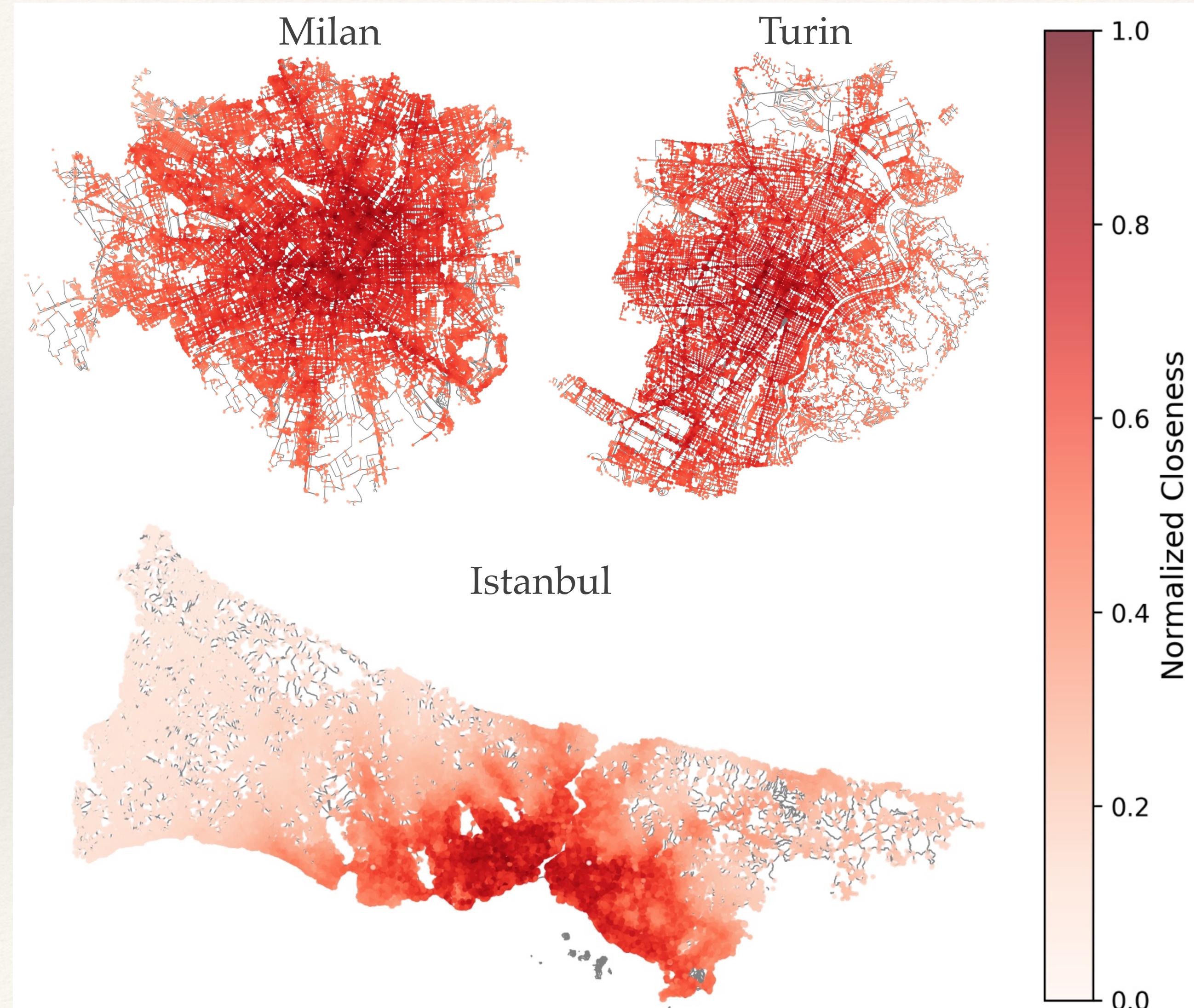
Comparing and ranking cities

$t = 15'$ for
Pol-{density, entropy, accessibility})



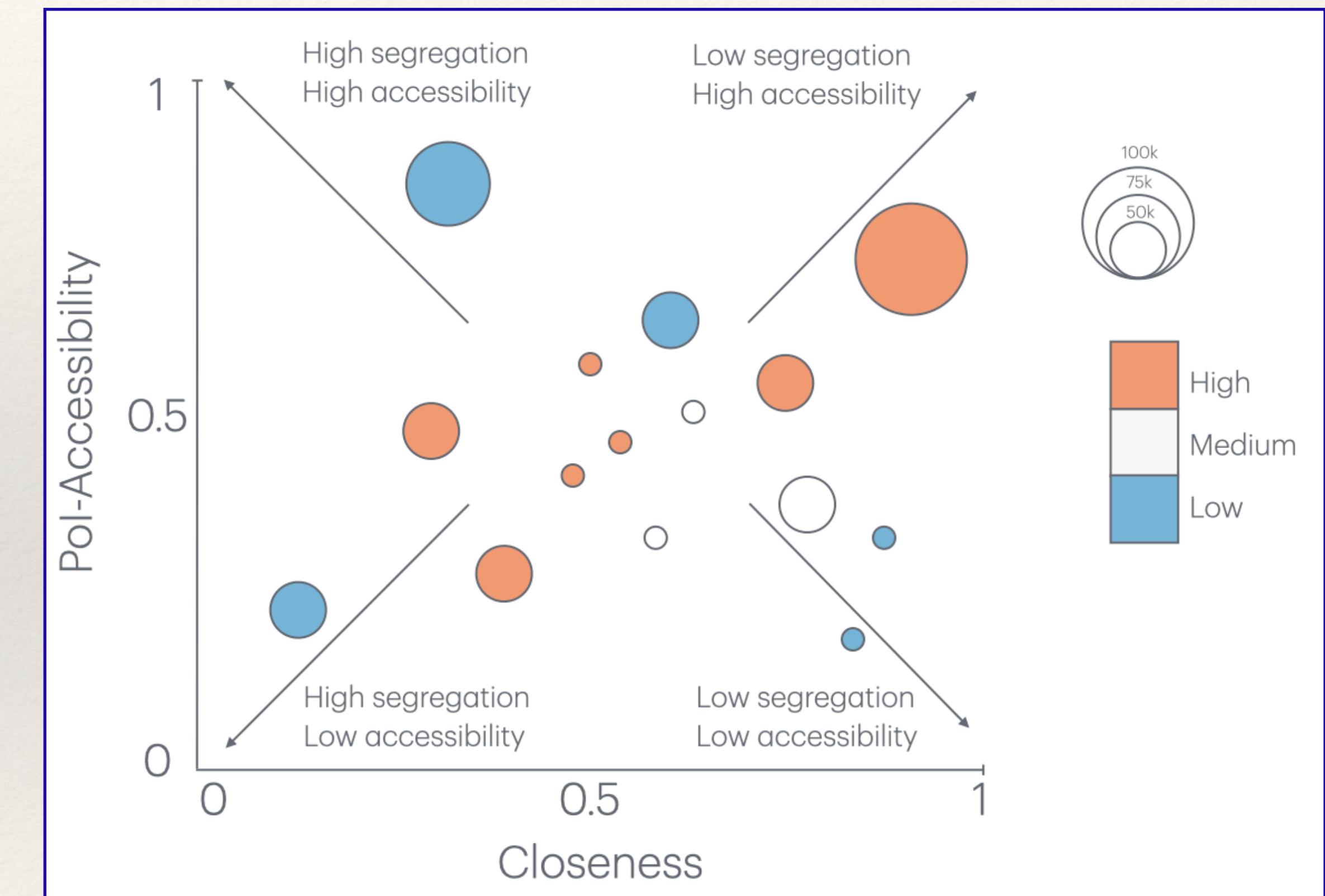
Connectivity metrics

- ❖ Given $n \in N_c$
 - ❖ (normalized) **Closeness**
$$\mathcal{C}(n) = \frac{|N_c| - 1}{\sum_{m \neq n: m \in N_c} t(n, m)}$$
 - ❖ $t(n, m)$ is the shortest path length (i.e., temporal distance) that it takes to go from n to m in G_c^{urb}



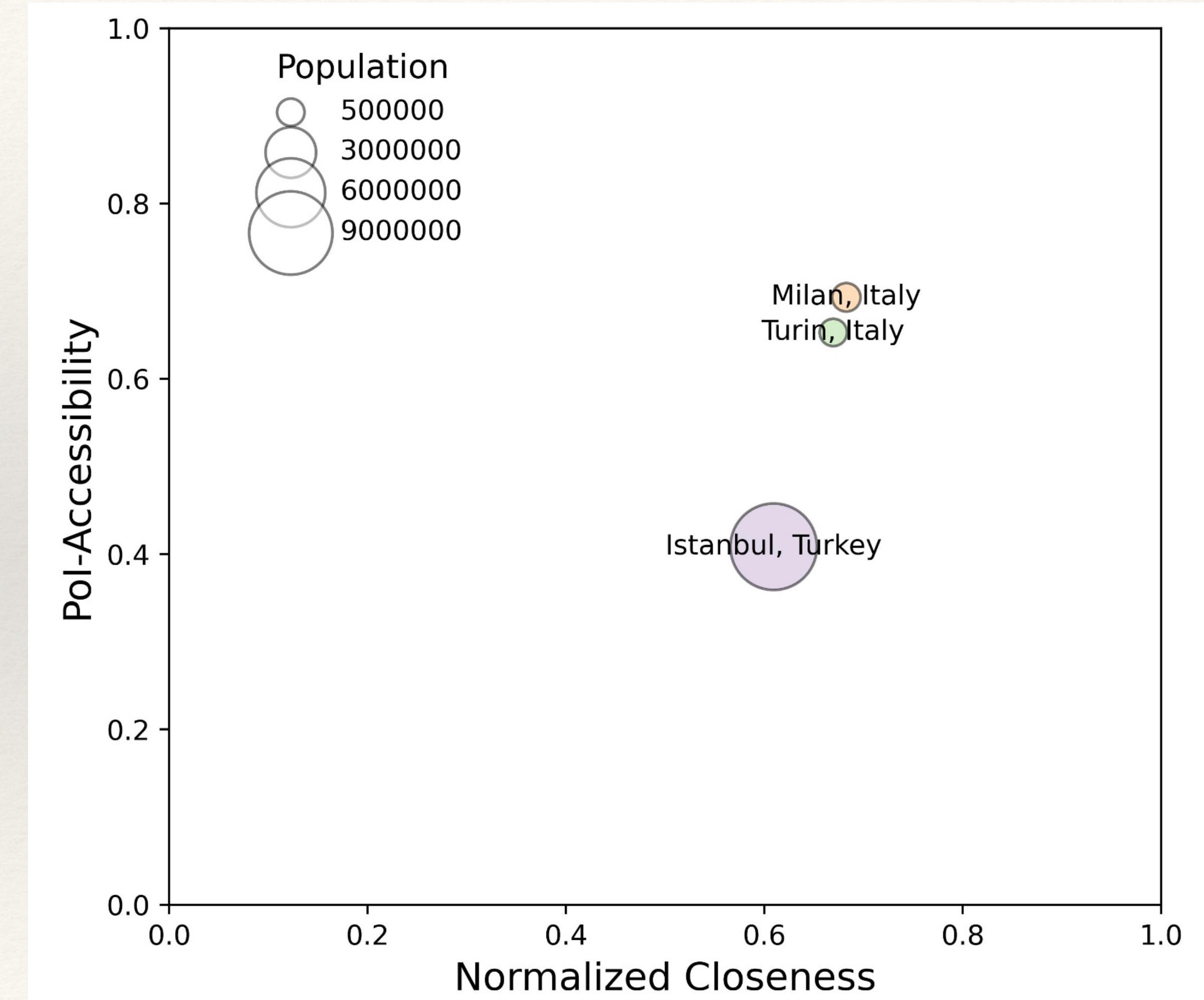
Closeness vs PoI-Accessibility

- ❖ Low closeness relates to high isolation / segregation
- ❖ Low PoI-Accessibility relates to lack of services at walkable distance
- ❖ **Bubble charts** helps to understand how accessibility relates to urban connectivity and segregation



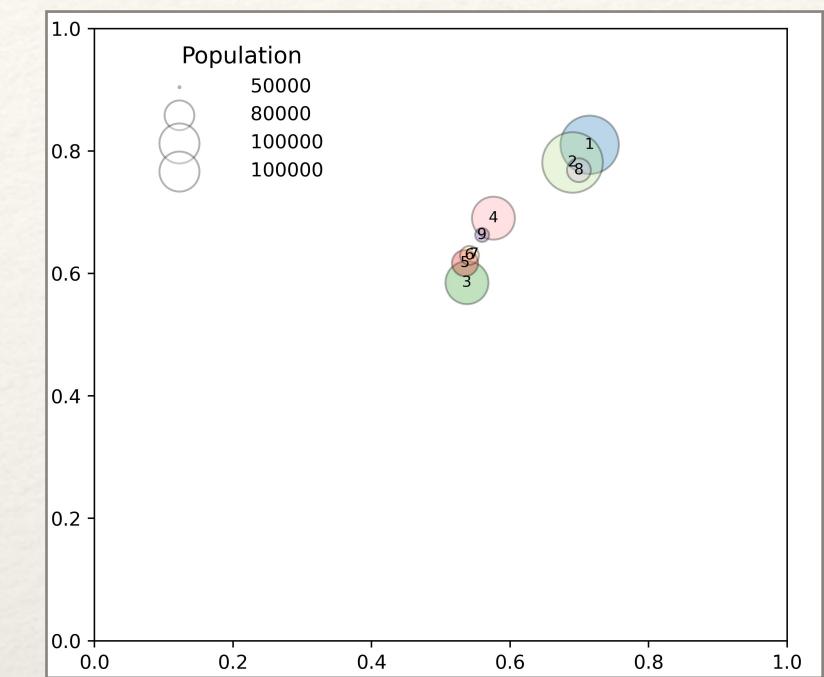
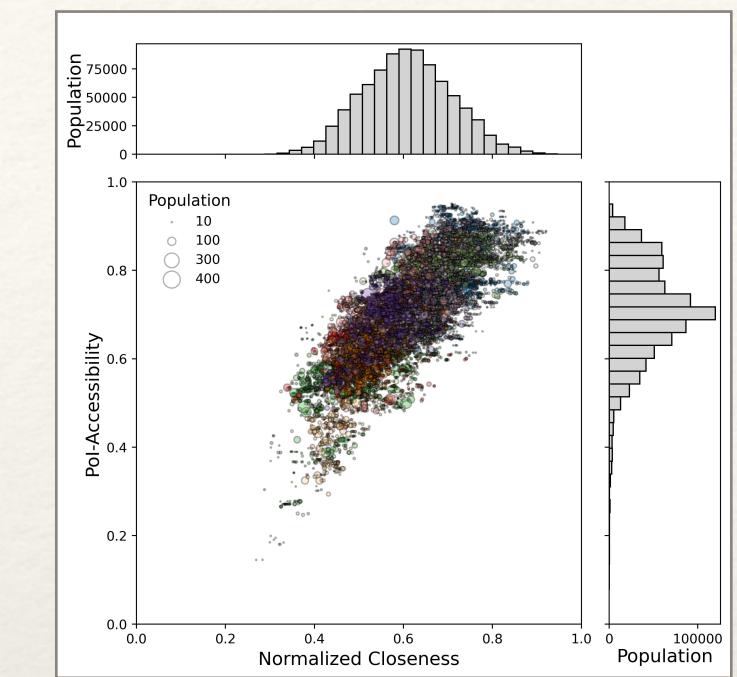
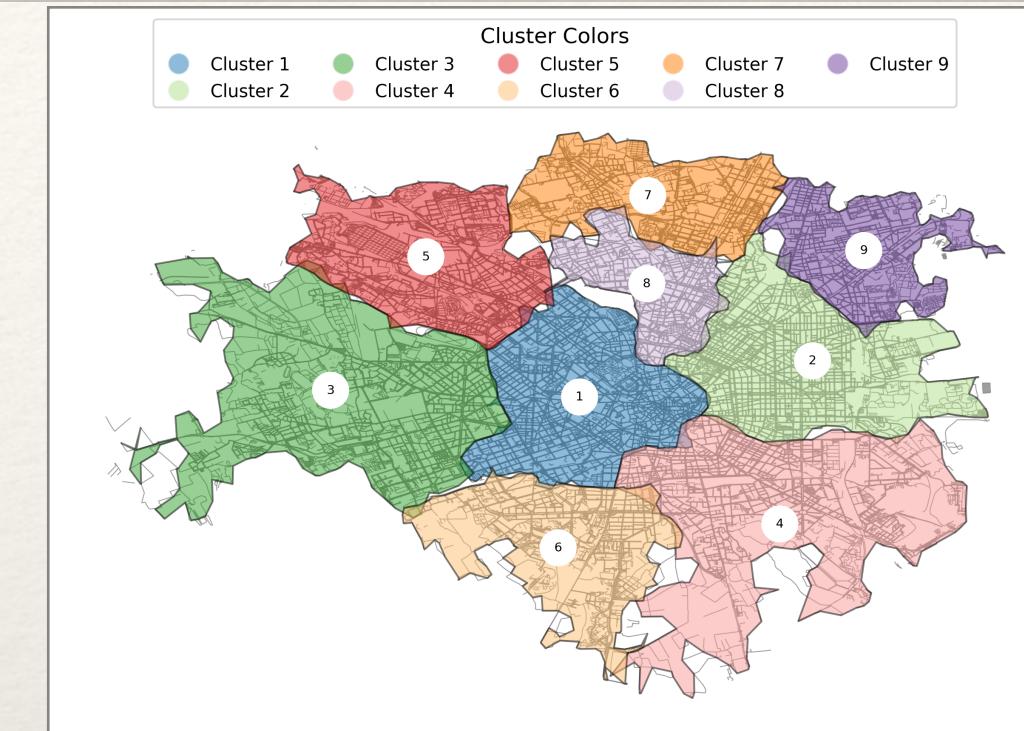
PoI-Accessibility vs Closeness($t=15'$)

- ❖ RQ2: There are signals that accessibility relates to urban connectivity and segregation
- ❖ RQ3: For stronger signals, nodes in N_c can be aggregated in census areas, network clusters (e.g., by infomap), administrative districts, ...

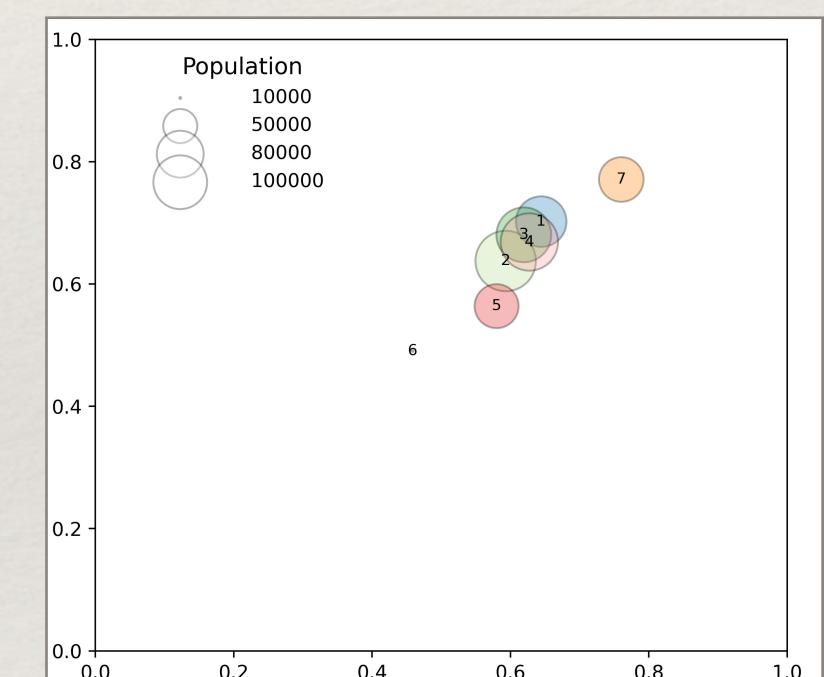
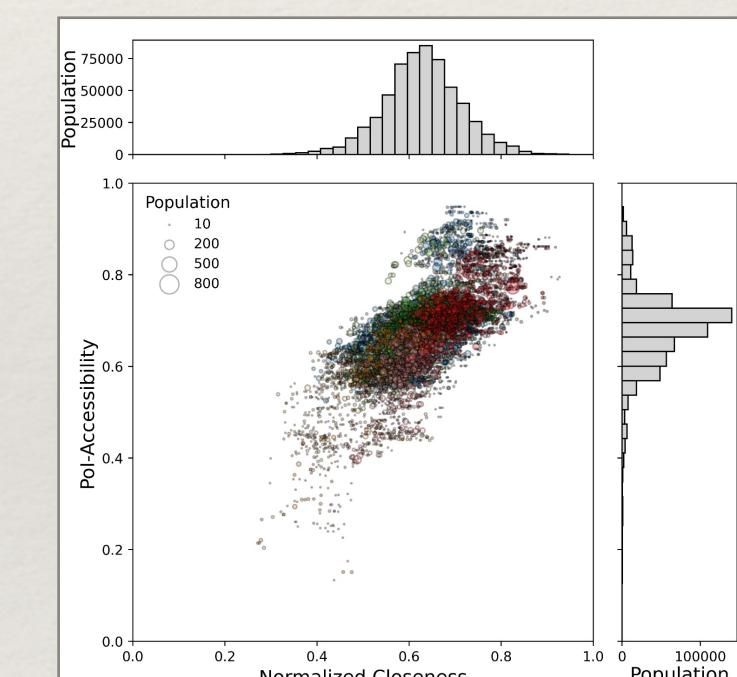
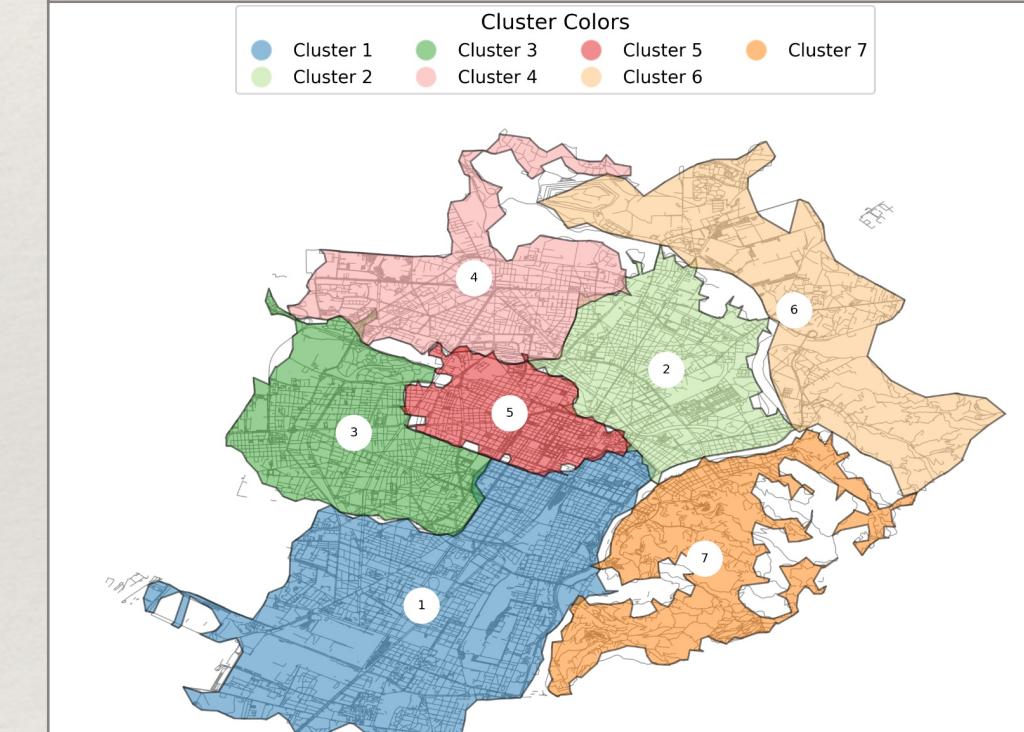


Accessibility, closeness, and population

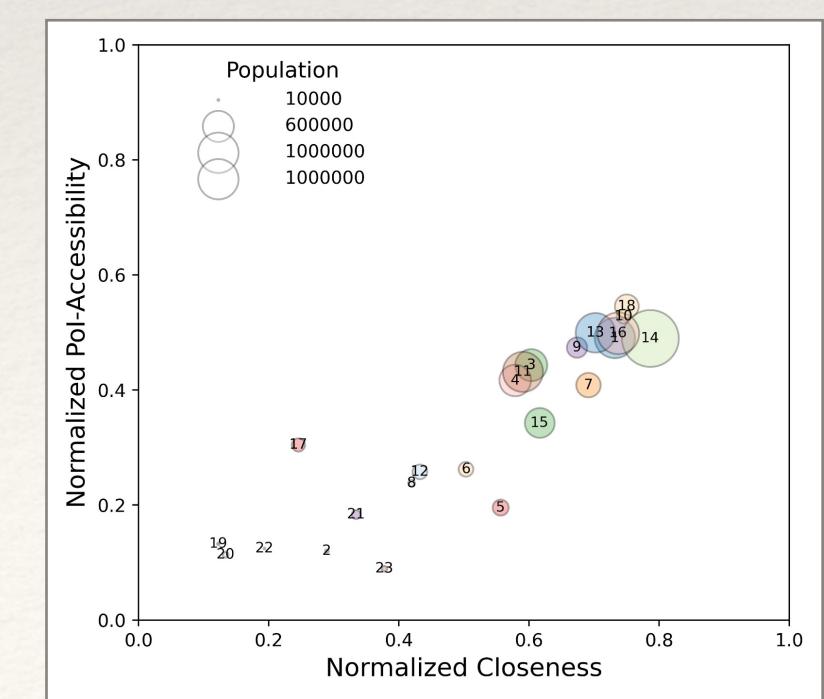
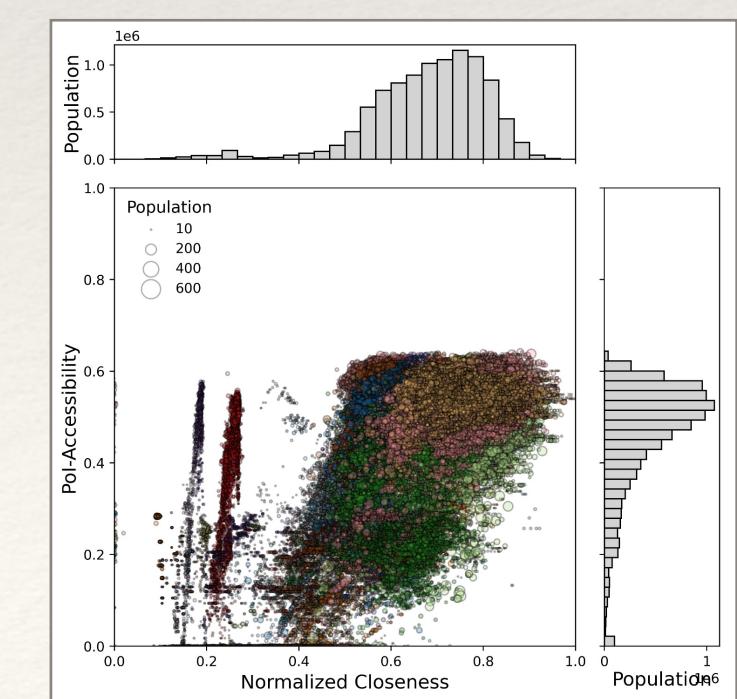
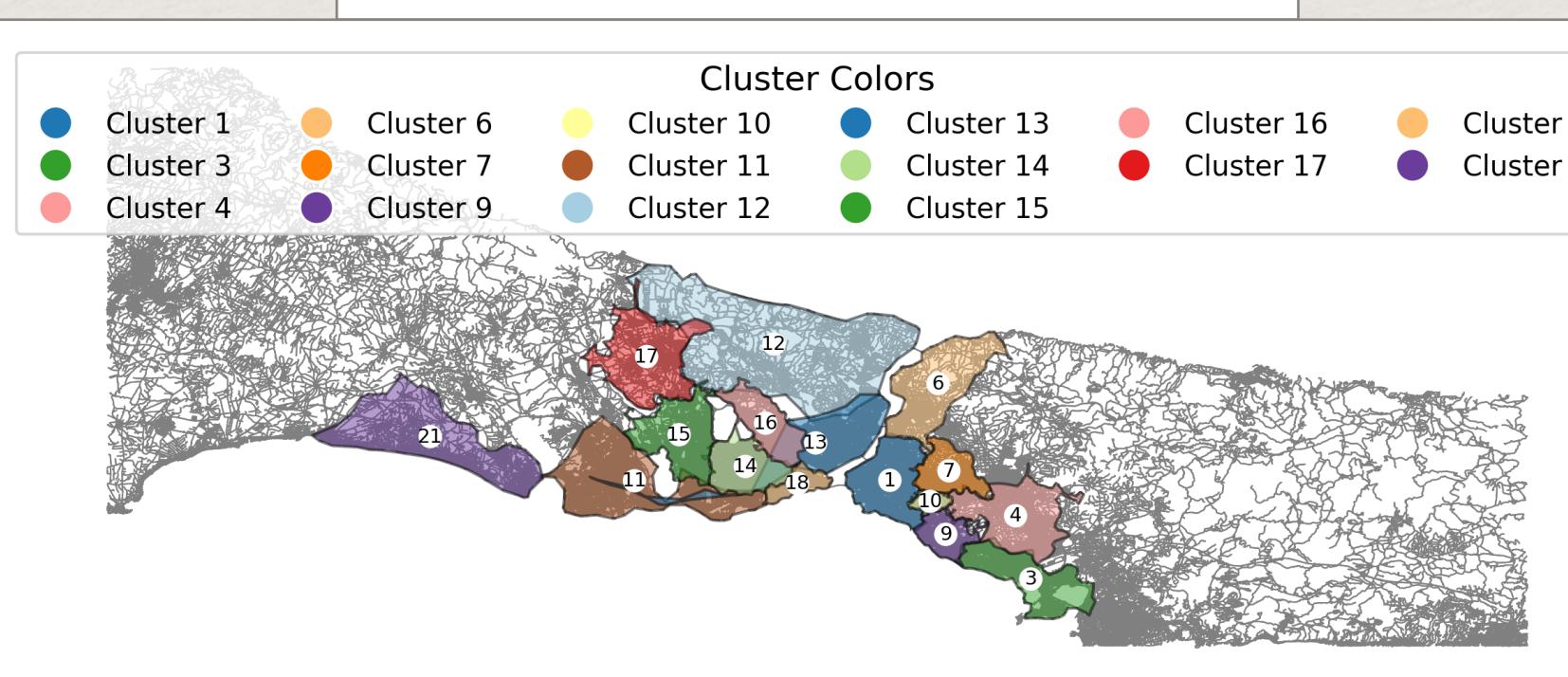
Milan



Turin

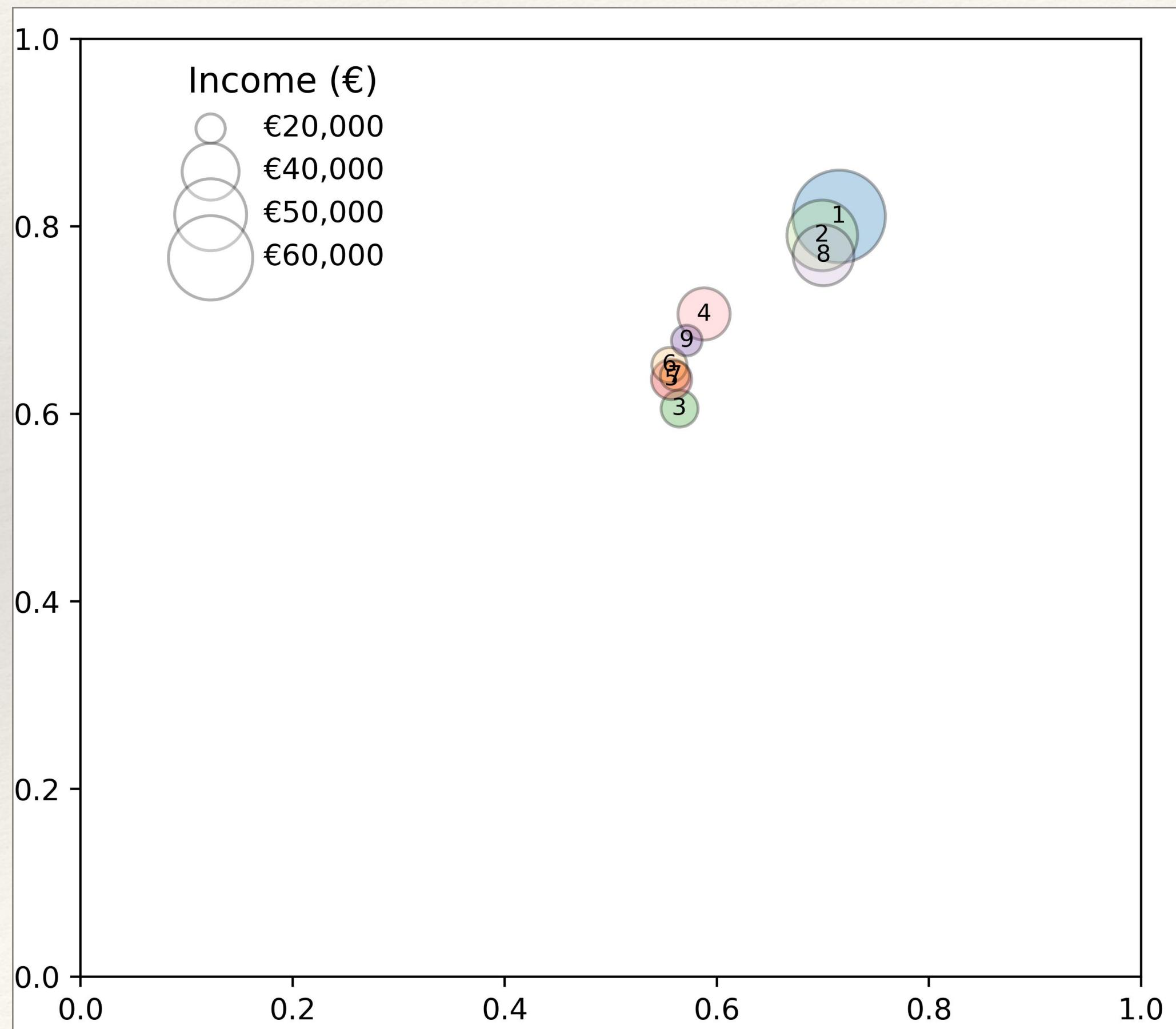


Istanbul

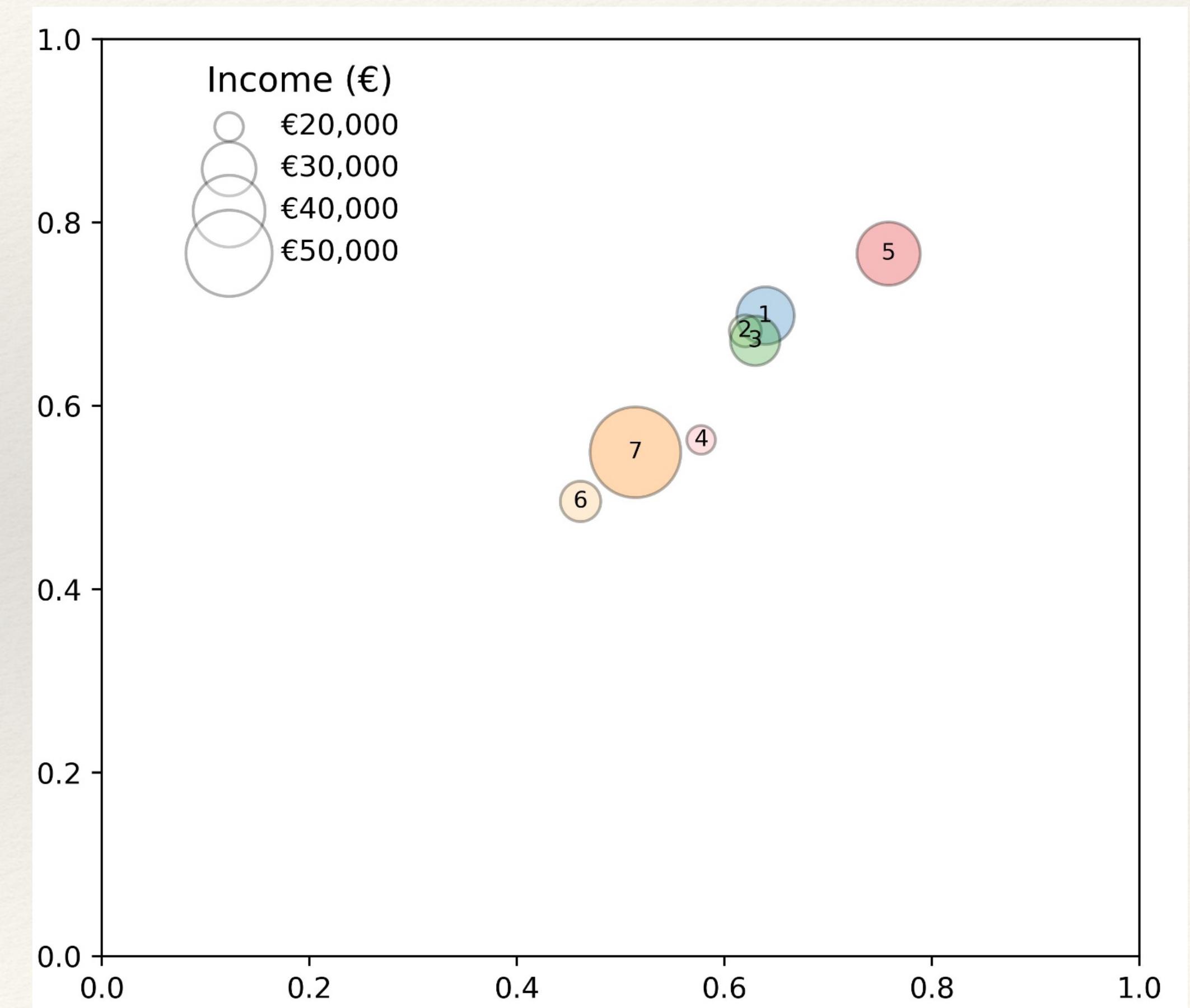


Accessibility, closeness and income

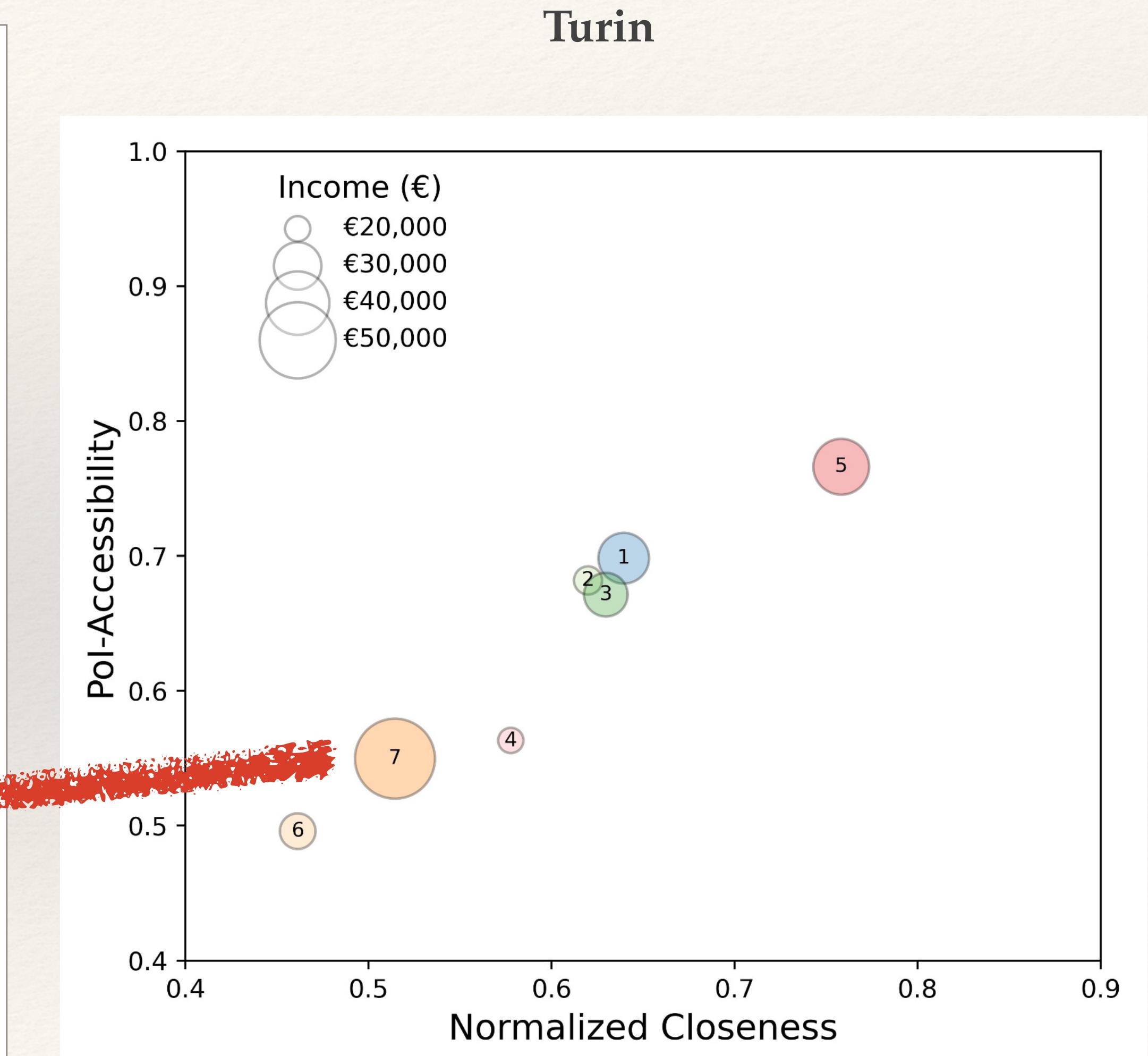
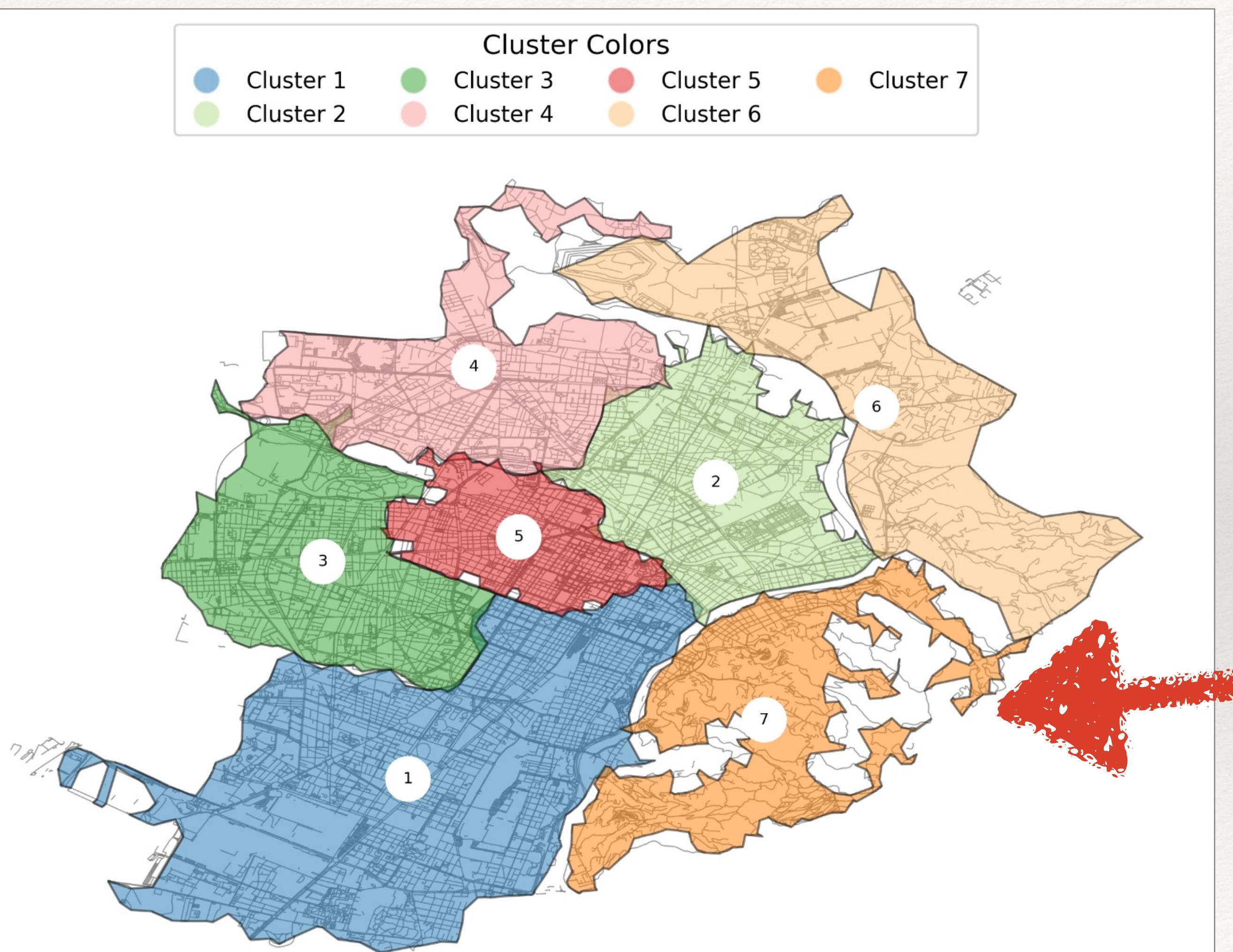
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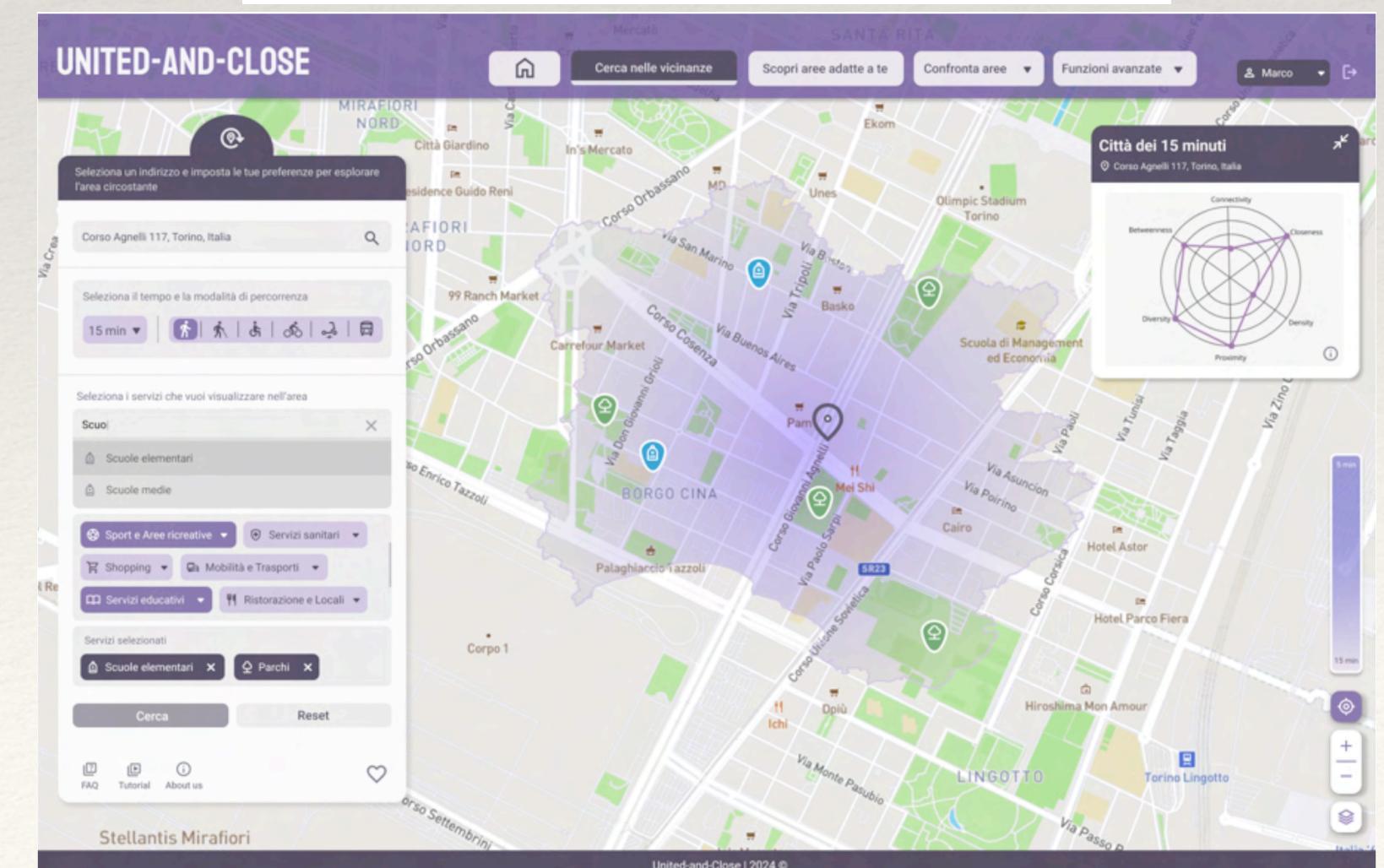
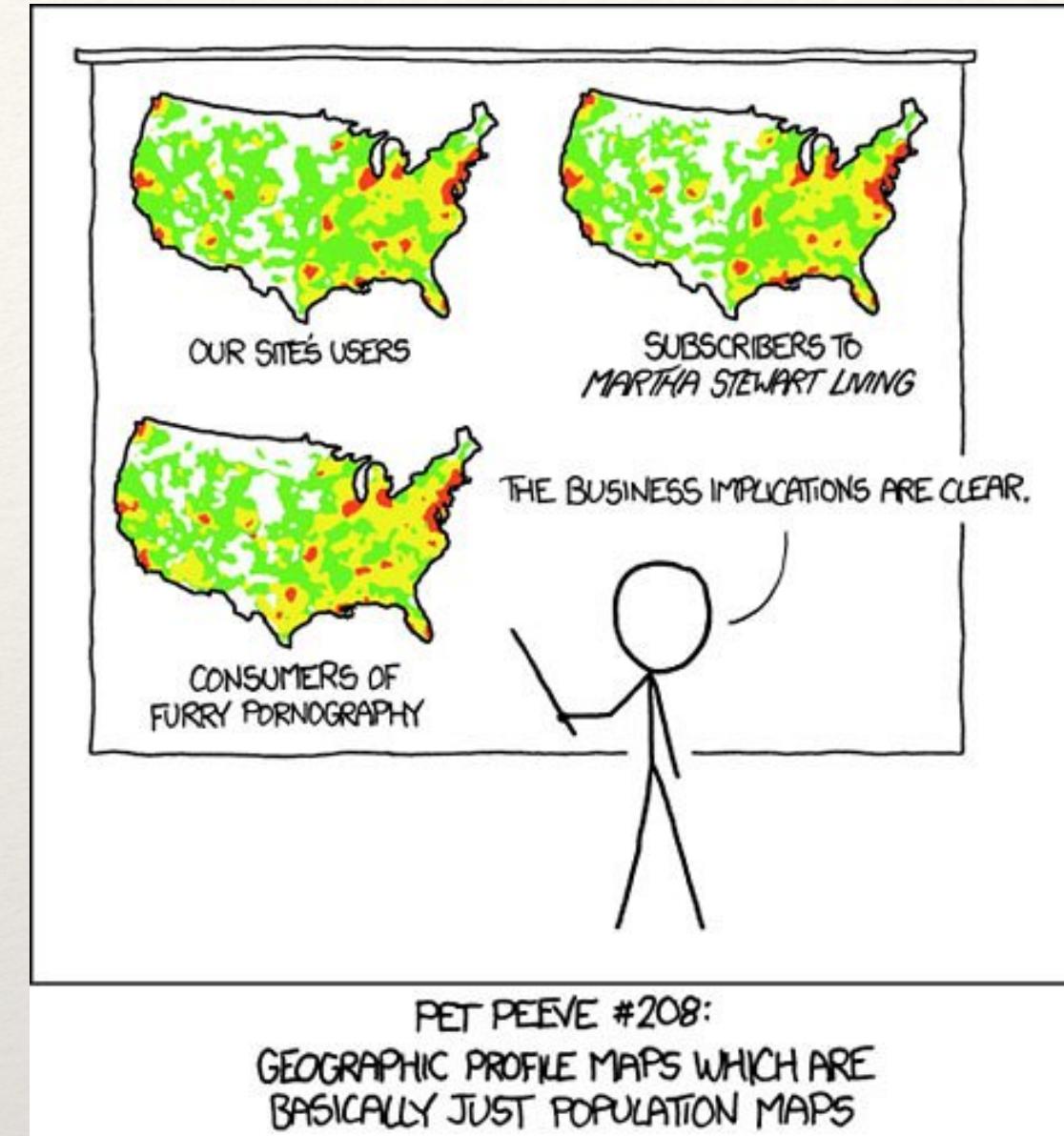


Accessibility, closeness and income



Conclusions: focus on citizens!

- ❖ Network based measures:
 - ❖ not only accessibility but also general connectivity
- ❖ A signal that (good / poor) walkable accessibility correlates to (good / poor) urban transport connectivity
 - ❖ Poorly served citizens are not equally distributed world wide
 - ❖ Turin's interesting exception: not always "poorer" accessibility / connectivity is at interplay with "lower income"
- ❖ Need for open data and open platforms
- ❖ Ongoing:
 - ❖ Personalized filters for close by services
 - ❖ **Unite-and-Close:** a magnifying glass for the 15-minute city



Extra slides

Ideal vs real cities



Kudos to Vittorio Loreto!

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PoI's categories:

Mobility



Active Living



Entertainment



Food Choices



Community



Education



Health and Well-being



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n

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- ❖ PoI-Accessibility $\mathcal{A}(n, t)$



PoI's categories:

Mobility



Active Living



Entertainment



Food Choices



Community



Education



Health and Well-being



Accessibility Metrics

- ❖ Given $n \in N_c$
 - ❖ **PoI-Proximity** $\mathcal{P}(n) = t$
 - ❖ PoI-Density $\mathcal{D}(n, t)$
 - ❖ PoI-Entropy $\mathcal{E}(n, t)$
 - ❖ PoI-Accessibility $\mathcal{A}(n, t)$



PoI's categories:

Mobility



Active Living



Entertainment



Food Choices



Community



Education

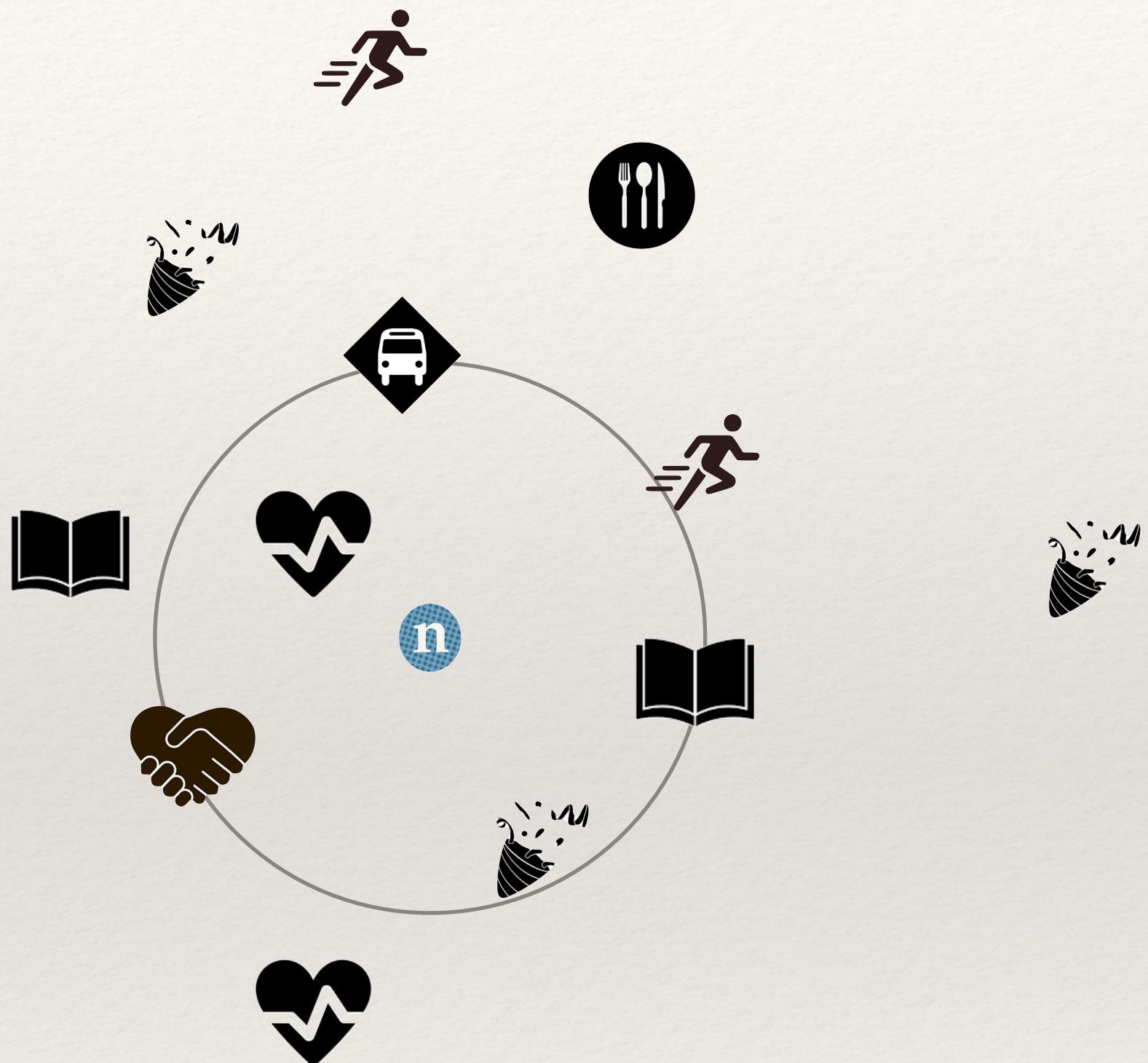


Health and Well-being



Accessibility Metrics

- ❖ Given $n \in N_c$
 - ❖ **PoI-Proximity** $\mathcal{P}(n) = t$
 - ❖ PoI-Density $\mathcal{D}(n, t)$
 - ❖ PoI-Entropy $\mathcal{E}(n, t)$
 - ❖ PoI-Accessibility $\mathcal{A}(n, t)$



PoI's categories:

Mobility



Active Living



Entertainment



Food Choices



Community



Education

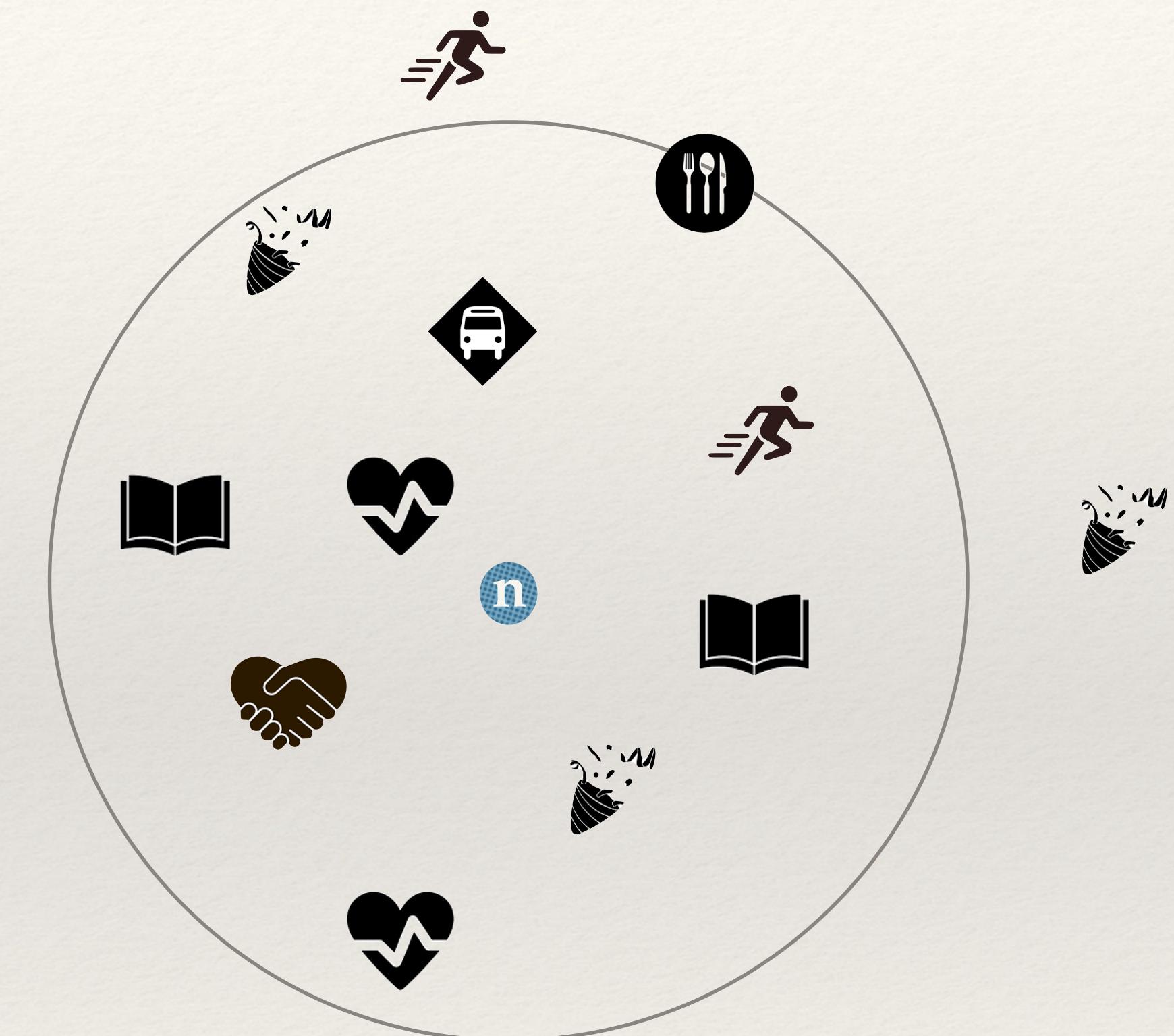


Health and Well-being



Accessibility Metrics

- ❖ Given $n \in N_c$
 - ❖ **PoI-Proximity** $\mathcal{P}(n) = t$
 - ❖ PoI-Density $\mathcal{D}(n, t)$
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PoI's categories:

Mobility



Active Living



Entertainment



Food Choices



Community



Education

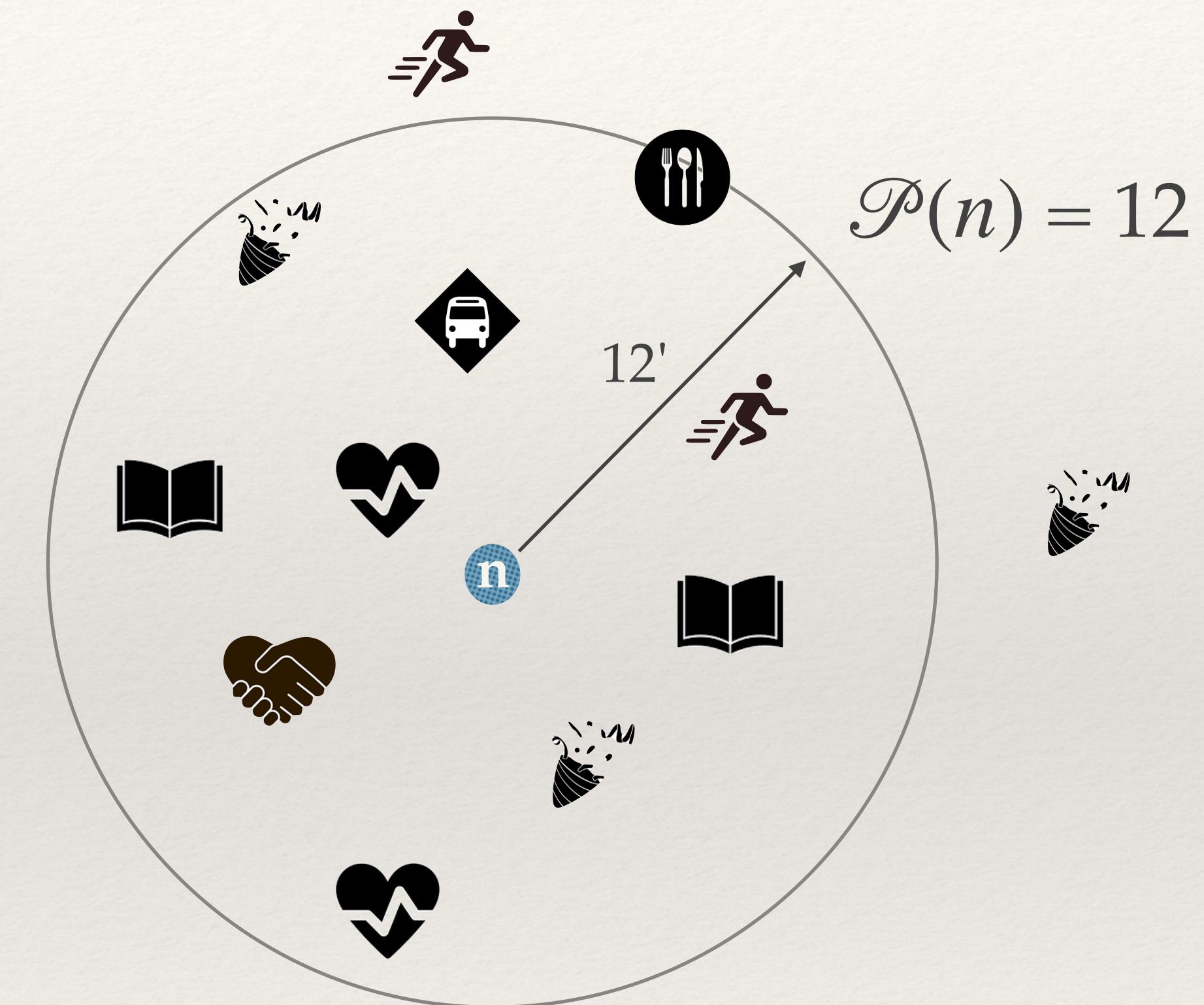


Health and Well-being



Accessibility Metrics

- ❖ Given $n \in N_c$
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 - ❖ PoI-Density $\mathcal{D}(n, t)$
 - ❖ PoI-Entropy $\mathcal{E}(n, t)$
 - ❖ PoI-Accessibility $\mathcal{A}(n, t)$



PoI's categories:

Mobility



Active Living



Entertainment



Food Choices



Community



Education



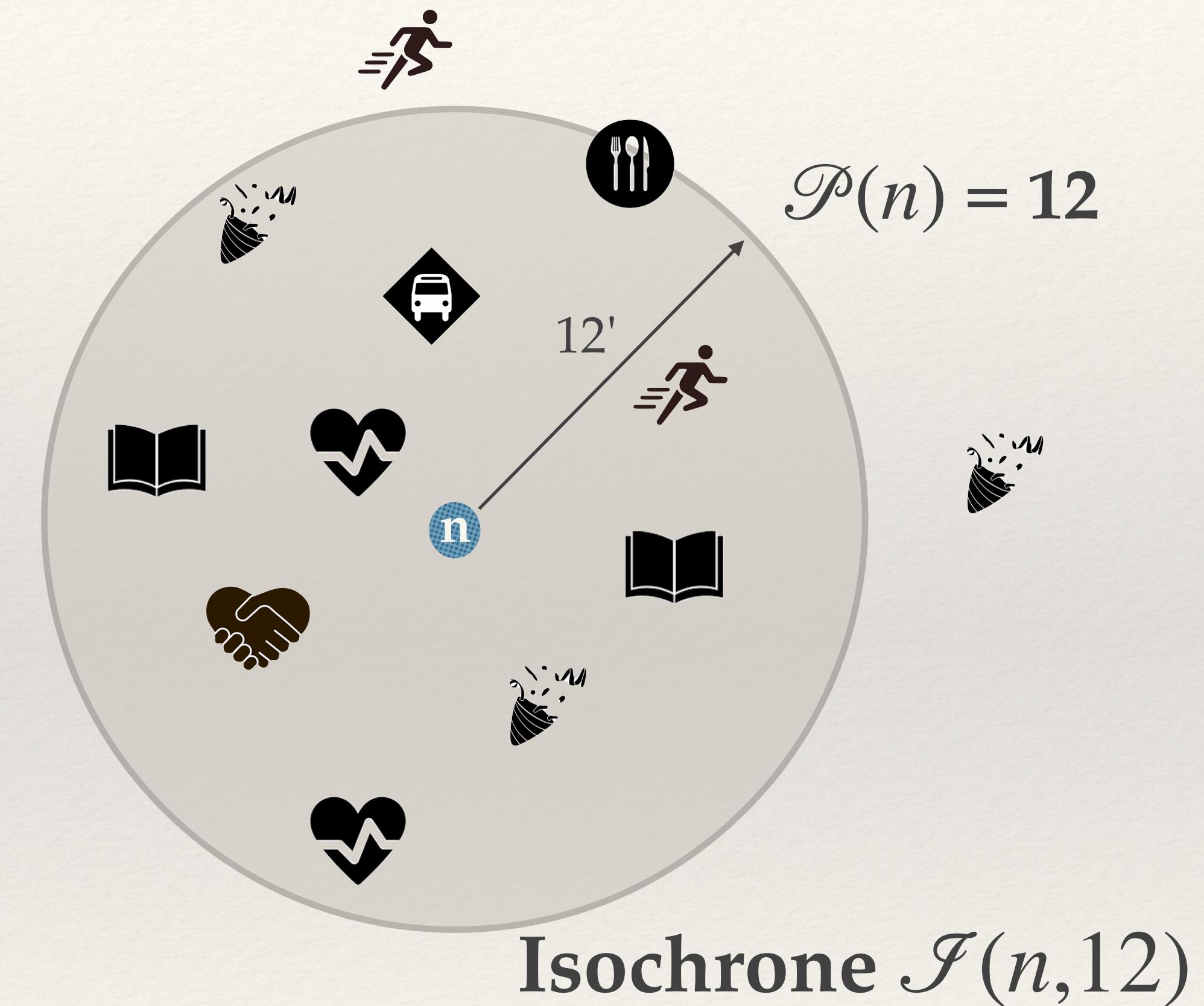
Health and Well-being



$\mathcal{P}(n) = 12$

Accessibility Metrics

- ❖ Given $n \in N_c$
 - ❖ **PoI-Proximity** $\mathcal{P}(n) = t$
 - ❖ PoI-Density $\mathcal{D}(n, t)$
 - ❖ PoI-Entropy $\mathcal{E}(n, t)$
 - ❖ PoI-Accessibility $\mathcal{A}(n, t)$



PoI's categories:

Mobility



Active Living



Entertainment



Food Choices



Community



Education

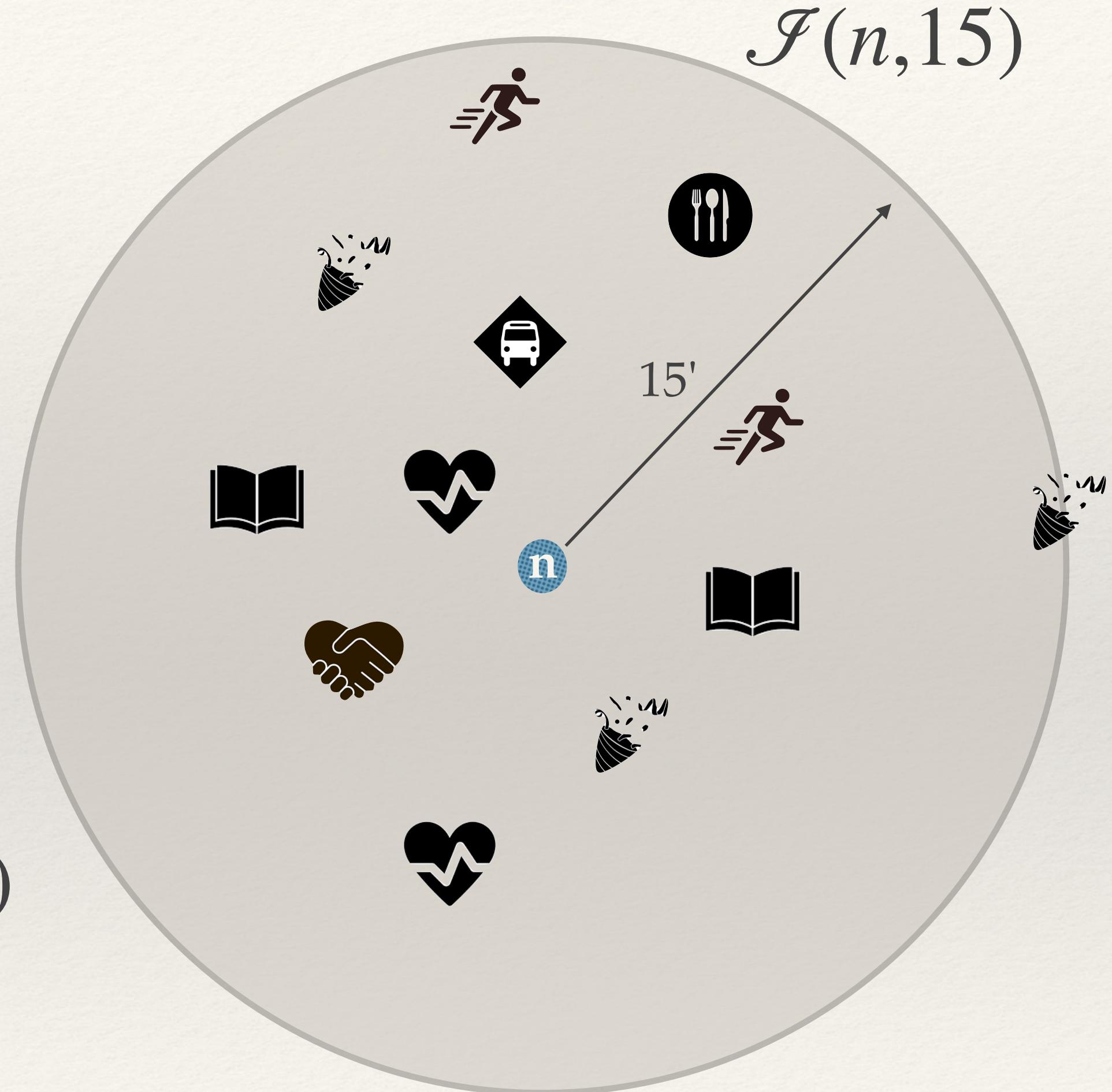


Health and Well-being



Accessibility Metrics

- ❖ Given $n \in N_c$
 - ❖ PoI-Proximity $\mathcal{P}(n) = t$
 - ❖ PoI-Density $\mathcal{D}(n, t)$
 - ❖ PoI-Entropy $\mathcal{E}(n, t)$
 - ❖ PoI-Accessibility $\mathcal{A}(n, t)$



PoI's categories:

Mobility



Active Living



Entertainment



Food Choices



Community



Education



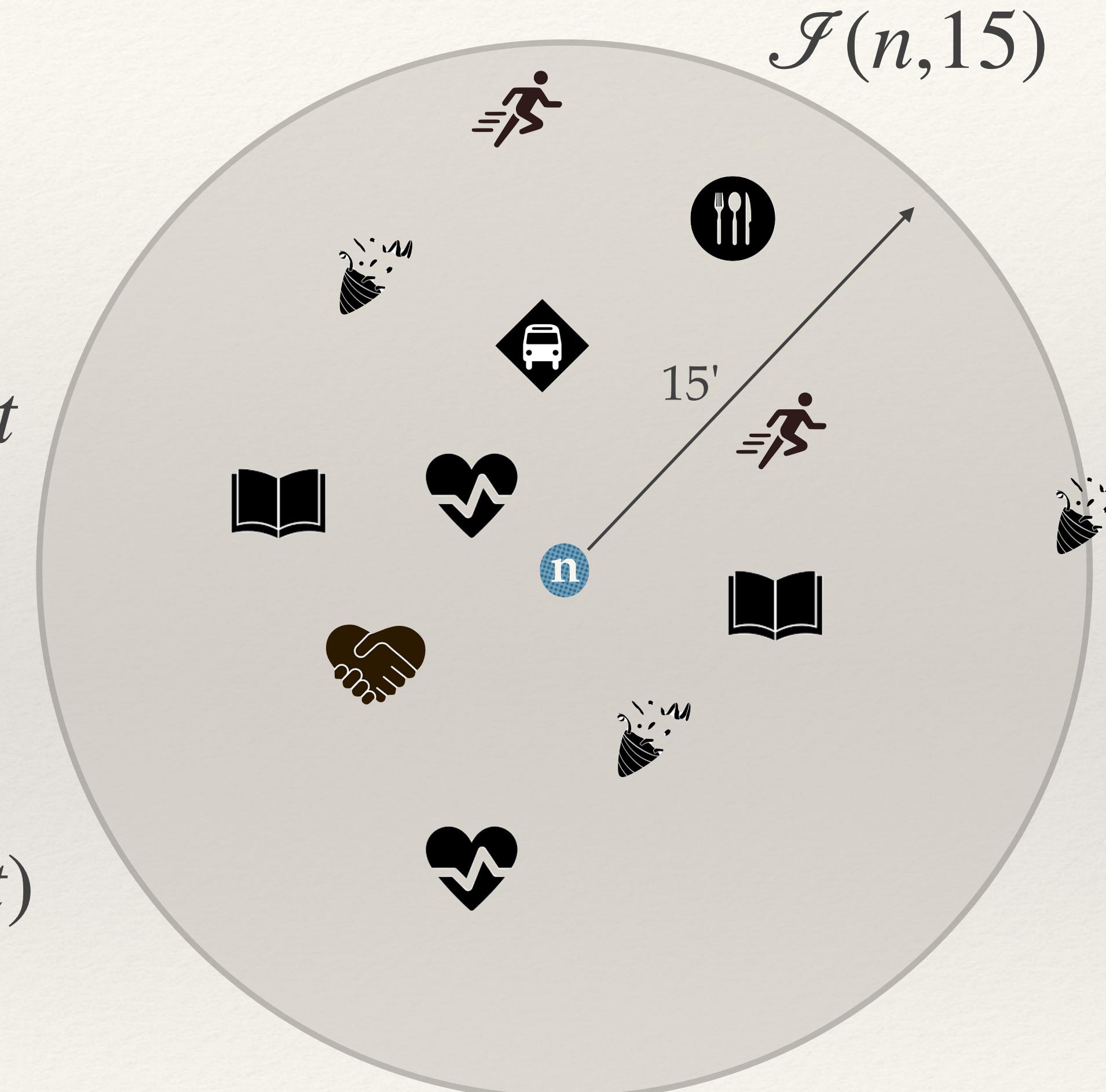
Health and Well-being



$$\mathcal{P}(n) = 12$$

Accessibility Metrics

- ❖ Given $n \in N_c$
- ❖ PoI-Proximity $\mathcal{P}(n) = t$
- ❖ PoI-Density $\mathcal{D}(n, t)$
- ❖ PoI-Entropy $\mathcal{E}(n, t)$
- ❖ PoI-Accessibility $\mathcal{A}(n, t)$



PoI's categories:

Mobility



Active Living



Entertainment



Food Choices



Community



Education



Health and Well-being

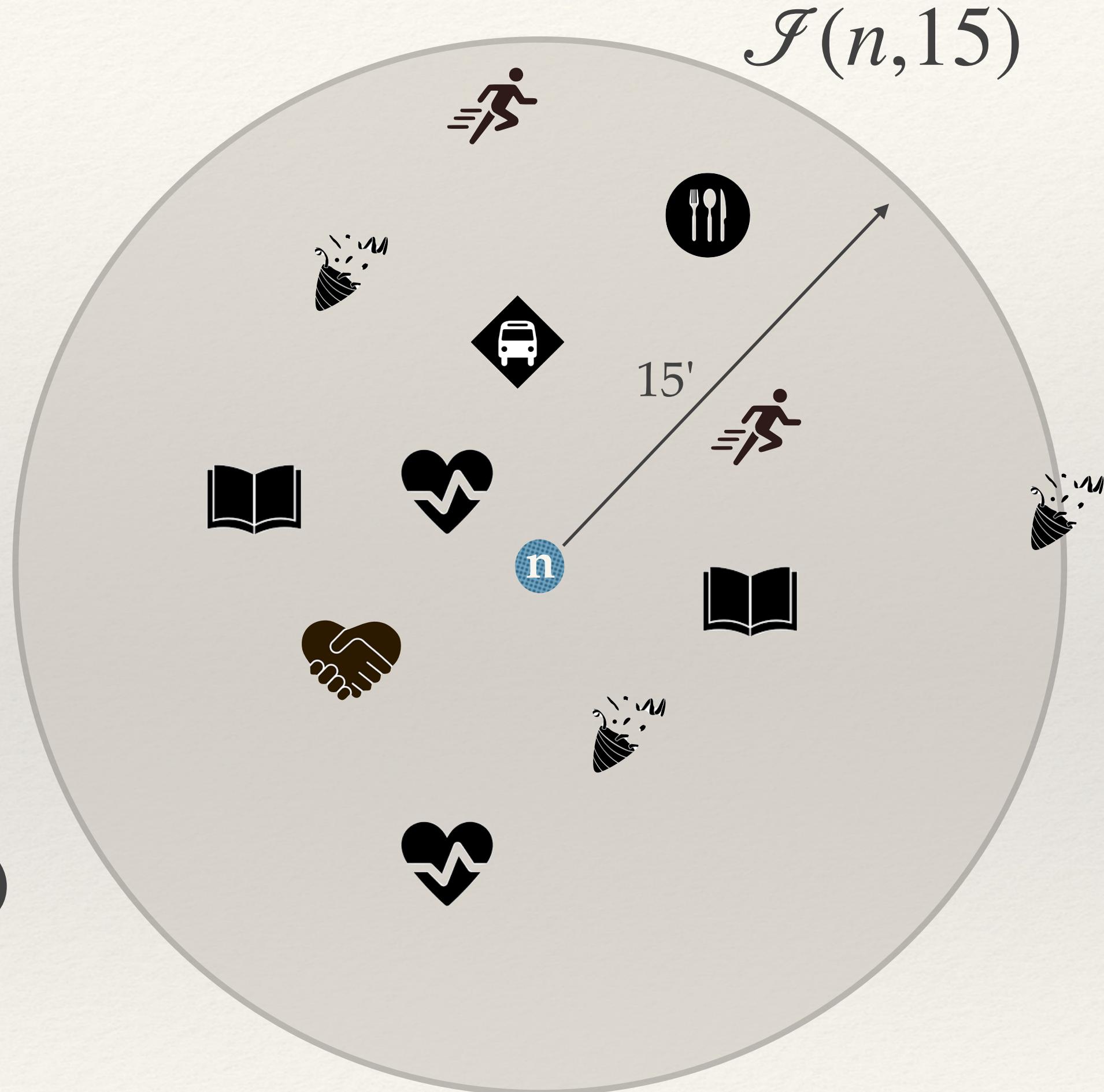


$$\mathcal{P}(n) = 12$$

$$\mathcal{D}(n, 15) = \frac{|\text{PoIs} \in \mathcal{J}(15)|}{\text{Area of } \mathcal{J}(n, 15)} = \frac{12}{7\text{km}^2} = 1.71$$

Accessibility Metrics

- ❖ Given $n \in N_c$
 - ❖ PoI-Proximity $\mathcal{P}(n) = t$
 - ❖ PoI-Density $\mathcal{D}(n, t)$
 - ❖ PoI-Entropy $\mathcal{E}(n, t)$
 - ❖ PoI-Accessibility $\mathcal{A}(n, t)$



PoI's categories:

Mobility



Active Living



Entertainment



Food Choices



Community



Education



Health and Well-being

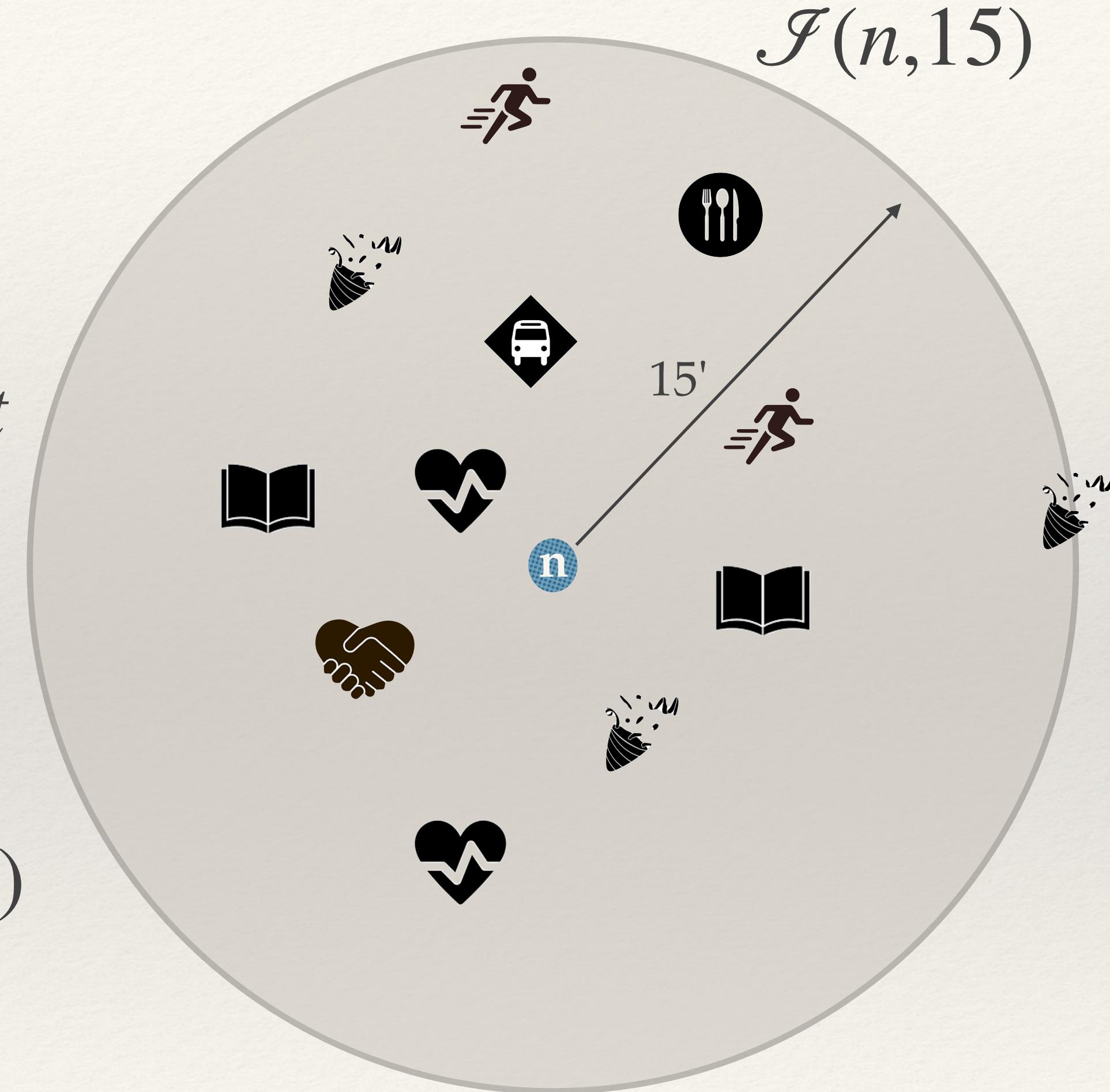


$$\mathcal{P}(n) = 12$$

$$\mathcal{D}(n, 15) = 1.71$$

Accessibility Metrics

- ❖ Given $n \in N_c$
 - ❖ PoI-Proximity $\mathcal{P}(n) = t$
 - ❖ PoI-Density $\mathcal{D}(n, t)$
 - ❖ PoI-Entropy $\mathcal{E}(n, t)$
 - ❖ PoI-Accessibility $\mathcal{A}(n, t)$



PoI's categories:

Mobility



Active Living



Entertainment



Food Choices



Community



Education



Health and Well-being



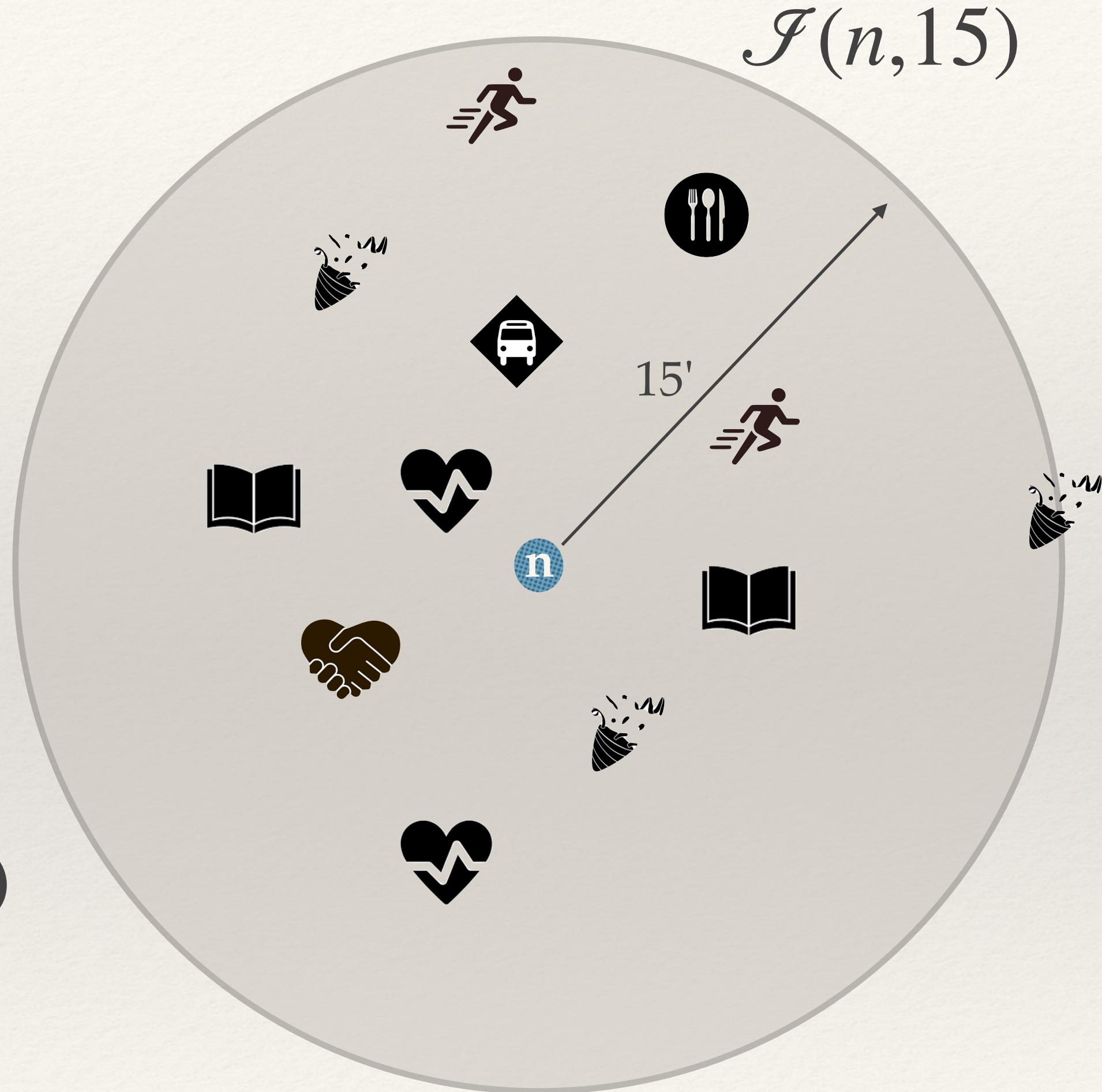
$$\mathcal{P}(n) = 12$$

$$\mathcal{D}(n, 15) = 1.71$$

$\mathcal{E}(n, 15)$ = the entropy of the distribution of PoIs' categories within $\mathcal{J}(n, 15) = 2.69$

Accessibility Metrics

- ❖ Given $n \in N_c$
 - ❖ PoI-Proximity $\mathcal{P}(n) = t$
 - ❖ PoI-Density $\mathcal{D}(n, t)$
 - ❖ PoI-Entropy $\mathcal{E}(n, t)$
 - ❖ PoI-Accessibility $\mathcal{A}(n, t)$



PoI's categories:

Mobility



Active Living



Entertainment



Food Choices



Community



Education



Health and Well-being



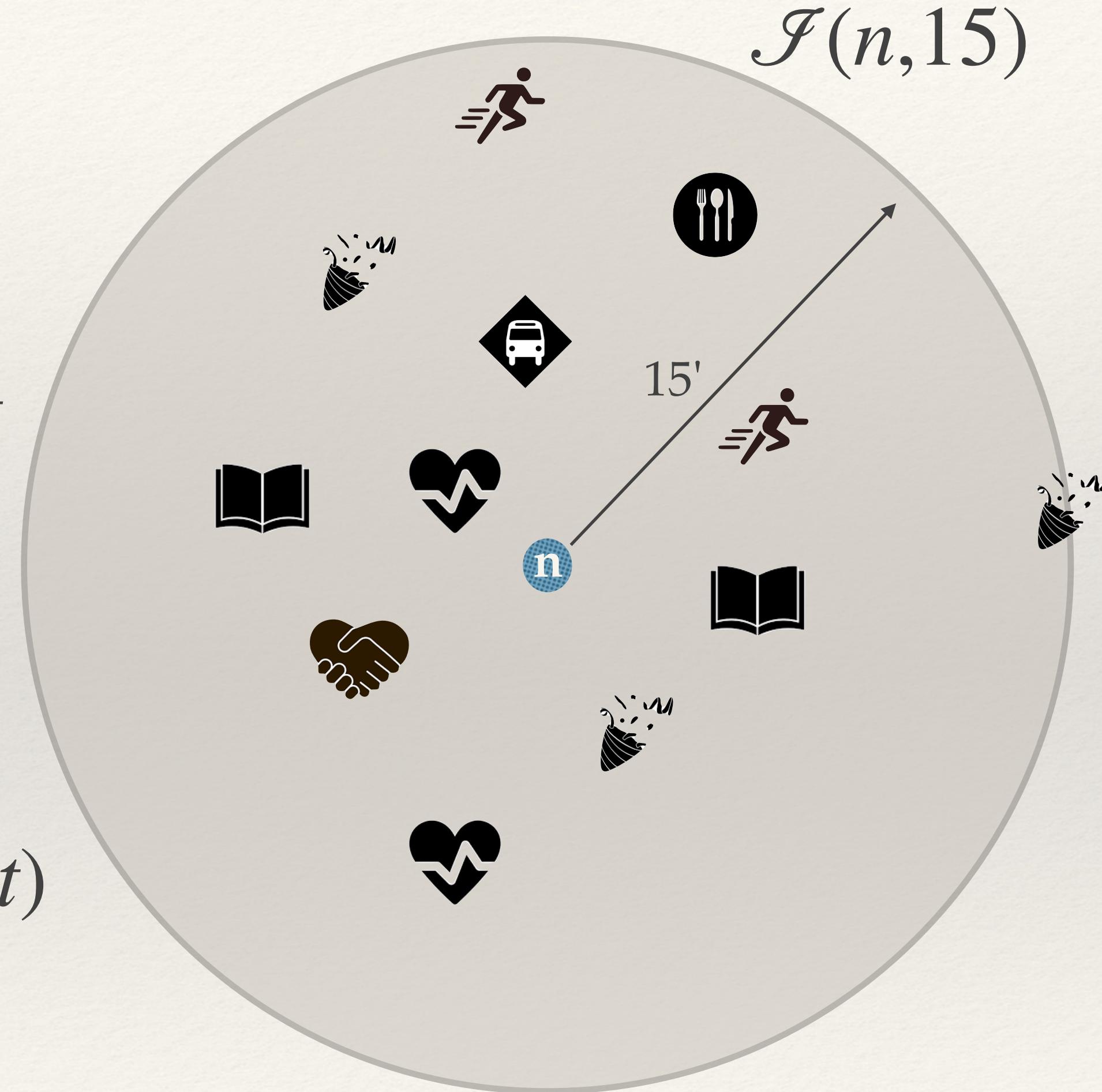
$$\mathcal{P}(n) = 12$$

$$\mathcal{D}(n, 15) = 1.71$$

$$\mathcal{E}(n, 15) = 2.69$$

Accessibility Metrics

- ❖ Given $n \in N_c$
- ❖ PoI-Proximity $\mathcal{P}(n) = t$
- ❖ PoI-Density $\mathcal{D}(n, t)$
- ❖ PoI-Entropy $\mathcal{E}(n, t)$
- ❖ **PoI-Accessibility** $\mathcal{A}(n, t)$



PoI's categories:

Mobility



Active Living



Entertainment



Food Choices



Community



Education



Health and Well-being



$$\mathcal{P}(n) = 12$$

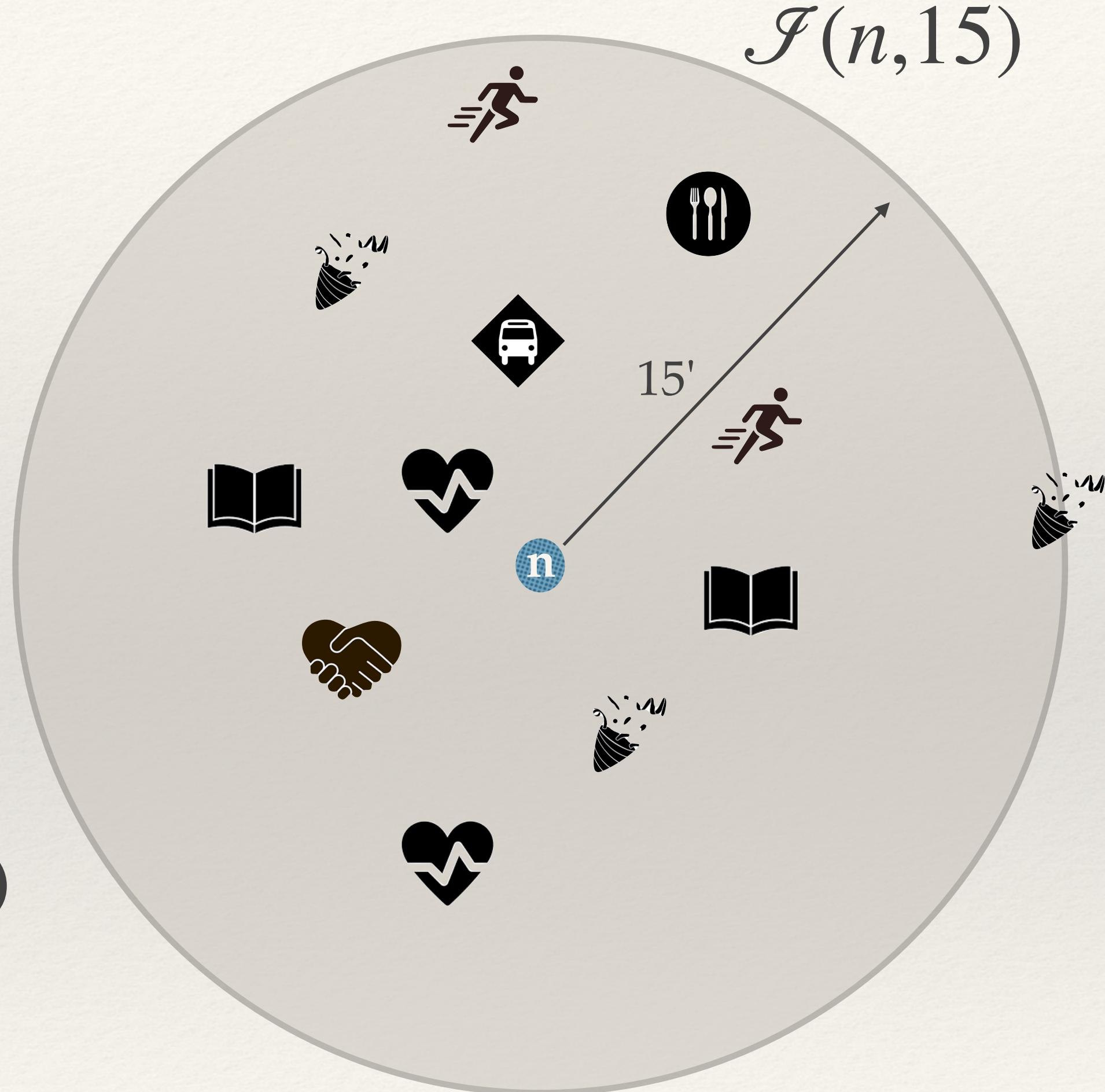
$$\mathcal{D}(n, 15) = 1.71$$

$$\mathcal{E}(n, 15) = 2.69$$

$$\mathcal{A}(n, t) = w_1 \mathcal{P}'(n) + w_2 \mathcal{D}'(n, t) + w_3 \mathcal{E}'(n, t) \quad \text{e.g., } w_1 = w_2 = w_3 = 1/3, \text{ and } t = 15$$

Accessibility Metrics

- ❖ Given $n \in N_c$
 - ❖ PoI-Proximity $\mathcal{P}(n) = t$
 - ❖ PoI-Density $\mathcal{D}(n, t)$
 - ❖ PoI-Entropy $\mathcal{E}(n, t)$
 - ❖ PoI-Accessibility $\mathcal{A}(n, t)$



PoI's categories:

Mobility



Active Living



Entertainment



Food Choices



Community



Education



Health and Well-being



$$\mathcal{P}(n) = 12$$

$$\mathcal{D}(n, 15) = 1.71$$

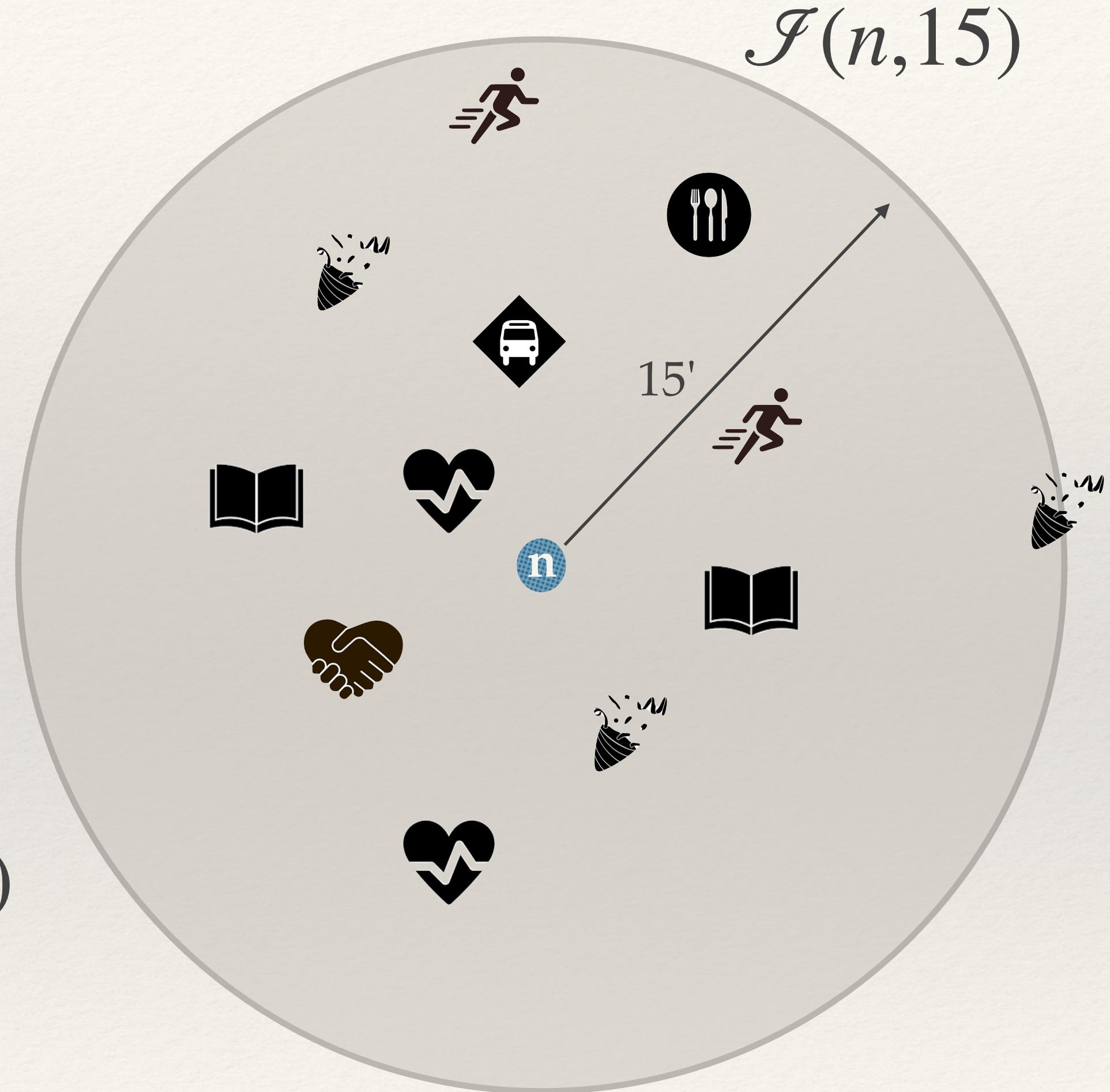
$$\mathcal{E}(n, 15) = 2.69$$

$$\mathcal{A}(n, 15) \in [0, 1]$$

Alternatives for density and entropy

Accessibility Metrics

- ❖ Given $n \in N_c$
 - ❖ PoI-Proximity $\mathcal{P}(n) = t$
 - ❖ PoI-Density $\mathcal{D}(n, t)$
 - ❖ PoI-Entropy $\mathcal{E}(n, t)$
 - ❖ PoI-Accessibility $\mathcal{A}(n, t)$



PoI's categories:

Mobility



Active Living



Entertainment



Food Choices



Community



Education



Health and Well-being



$$\mathcal{P}(n) = 12$$

Accessibility Metrics

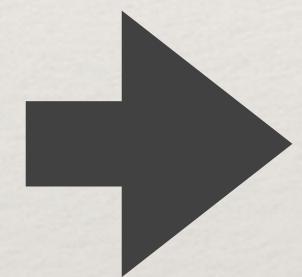
❖ Given $n \in N_c$

❖ PoI-Proximity $\mathcal{P}(n) = t$

❖ PoI-Density $\mathcal{D}(n, t)$

❖ PoI-Entropy $\mathcal{E}(n, t)$

❖ PoI-Accessibility $\mathcal{A}(n, t)$



We aim to give a higher value to isochrones containing more PoIs

PoI's categories:

Mobility



Active Living



Entertainment



Food Choices



Community



Education



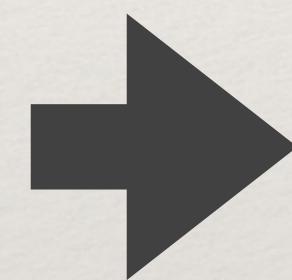
Health and Well-being



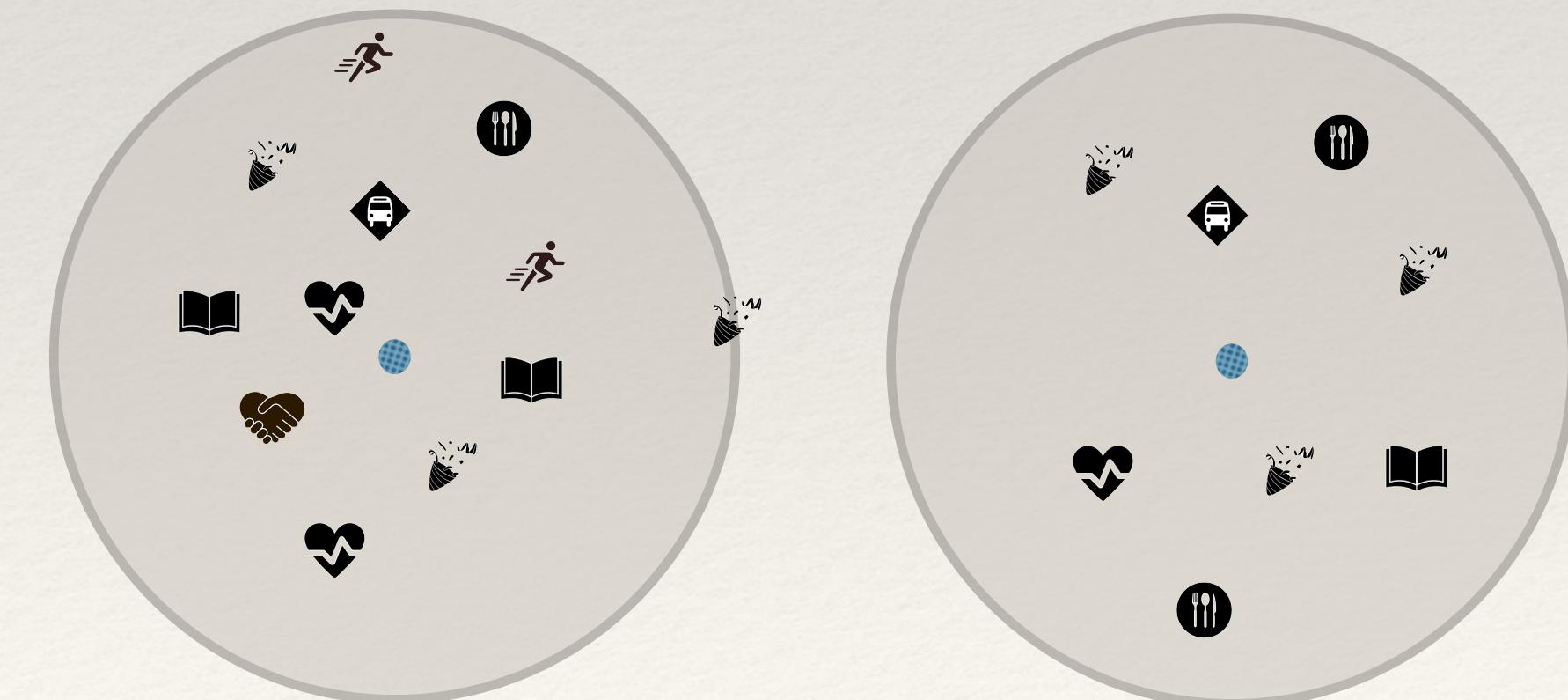
$\mathcal{P}(n) = 12$

Accessibility Metrics

- ❖ Given $n \in N_c$
- ❖ PoI-Proximity $\mathcal{P}(n) = t$
- ❖ PoI-Density $\mathcal{D}(n, t)$
- ❖ PoI-Entropy $\mathcal{E}(n, t)$
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We aim to give a higher value to isochrones containing more PoIs



$$\mathcal{D}(n, t) = \frac{|\text{PoIs} \in \mathcal{J}(t)|}{\text{Area of } \mathcal{J}(n, t)}$$

PoI's categories:

Mobility



Active Living



Entertainment



Food Choices



Community



Education



Health and Well-being



$$\mathcal{P}(n) = 12$$

Accessibility Metrics

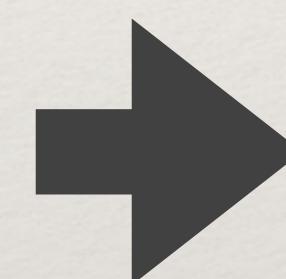
❖ Given $n \in N_c$

❖ PoI-Proximity $\mathcal{P}(n) = t$

❖ PoI-Density $\mathcal{D}(n, t)$

❖ PoI-Entropy $\mathcal{E}(n, t)$

❖ PoI-Accessibility $\mathcal{A}(n, t)$



We aim to give a higher value to isochrones containing more PoIs



$$\mathcal{D}(n, 15) = \frac{12}{7 \text{ km}^2} = 1.71$$



$$\mathcal{D}(m, 15) = \frac{8}{7 \text{ km}^2} = 1.14$$

PoI's categories:

Mobility



Active Living



Entertainment



Food Choices



Community



Education



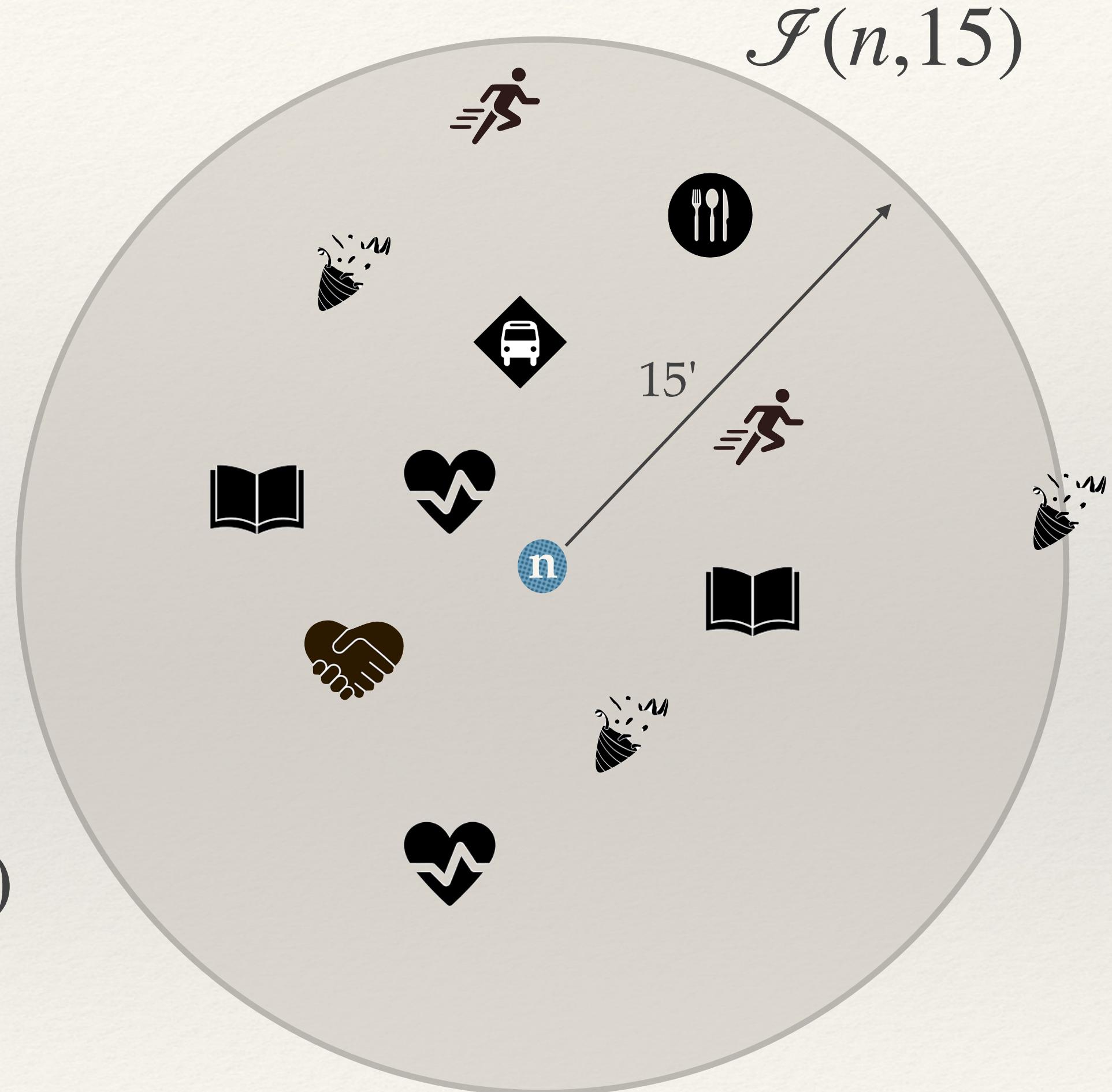
Health and Well-being



$$\mathcal{P}(n) = 12$$

Accessibility Metrics

- ❖ Given $n \in N_c$
 - ❖ PoI-Proximity $\mathcal{P}(n) = t$
 - ❖ PoI-Density $\mathcal{D}(n, t)$
 - ❖ PoI-Entropy $\mathcal{E}(n, t)$
 - ❖ PoI-Accessibility $\mathcal{A}(n, t)$



PoI's categories:

Mobility



Active Living



Entertainment



Food Choices



Community



Education



Health and Well-being

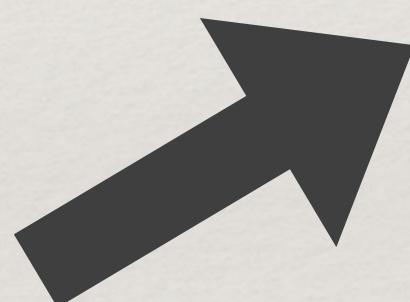


$$\mathcal{P}(n) = 12$$

$$\mathcal{D}(n, 15) = 1.71$$

Accessibility Metrics

- ❖ Given $n \in N_c$
 - ❖ PoI-Proximity $\mathcal{P}(n) = t$
 - ❖ PoI-Density $\mathcal{D}(n, t)$
 - ❖ PoI-Entropy $\mathcal{E}(n, t)$
 - ❖ PoI-Accessibility $\mathcal{A}(n, t)$



We aim to give a higher value to isochrones containing a greater diversity of PoIs' categories

PoI's categories:

Mobility



Active Living



Entertainment



Food Choices



Community



Education



Health and Well-being



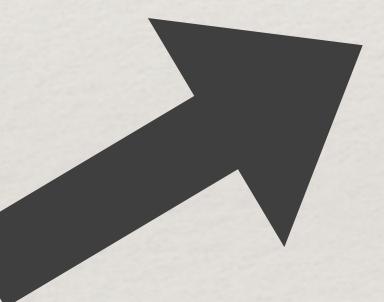
$$\mathcal{P}(n) = 12$$

$$\mathcal{D}(n, 15) = 1.71$$

$\mathcal{E}(n, 15)$ = the entropy of the distribution of PoIs' categories within $\mathcal{I}(n, 15) = 2.69$

Accessibility Metrics

- ❖ Given $n \in N_c$
 - ❖ PoI-Proximity $\mathcal{P}(n) = t$
 - ❖ PoI-Density $\mathcal{D}(n, t)$
 - ❖ PoI-Entropy $\mathcal{E}(n, t)$
 - ❖ PoI-Accessibility $\mathcal{A}(n, t)$



$\mathcal{E}(n, t) = \text{the entropy of the distribution of PoIs' categories within } \mathcal{J}(n, t)$

We aim to give a higher value to isochrones containing a greater diversity of PoIs' categories

PoI's categories:

Mobility



Active Living



Entertainment



Food Choices



Community



Education



Health and Well-being



$$\mathcal{P}(n) = 12$$

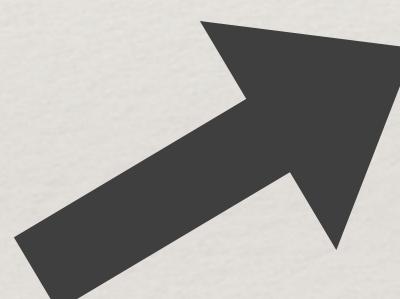
$$\mathcal{D}(n, 15) = 1.71$$

Accessibility Metrics

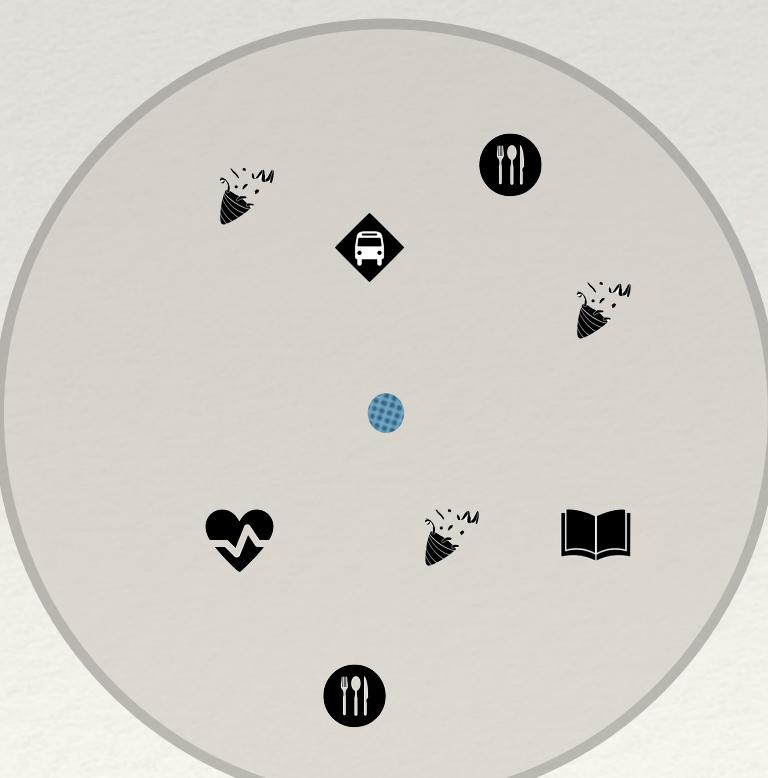
- ❖ Given $n \in N_c$
 - ❖ PoI-Proximity $\mathcal{P}(n) = t$
 - ❖ PoI-Density $\mathcal{D}(n, t)$
 - ❖ PoI-Entropy $\mathcal{E}(n, t)$
 - ❖ PoI-Accessibility $\mathcal{A}(n, t)$

$\mathcal{E}(n, t) =$ the entropy of the distribution of PoIs' categories within $\mathcal{J}(n, t)$

We aim to give a higher value to isochrones containing a greater diversity of PoIs' categories



$$\mathcal{E}(n, 15) = 2.69$$



$$\mathcal{E}(m, 15) = 0.76$$

PoI's categories:

Mobility



Active Living



Entertainment



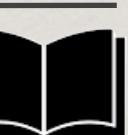
Food Choices



Community



Education



Health and Well-being

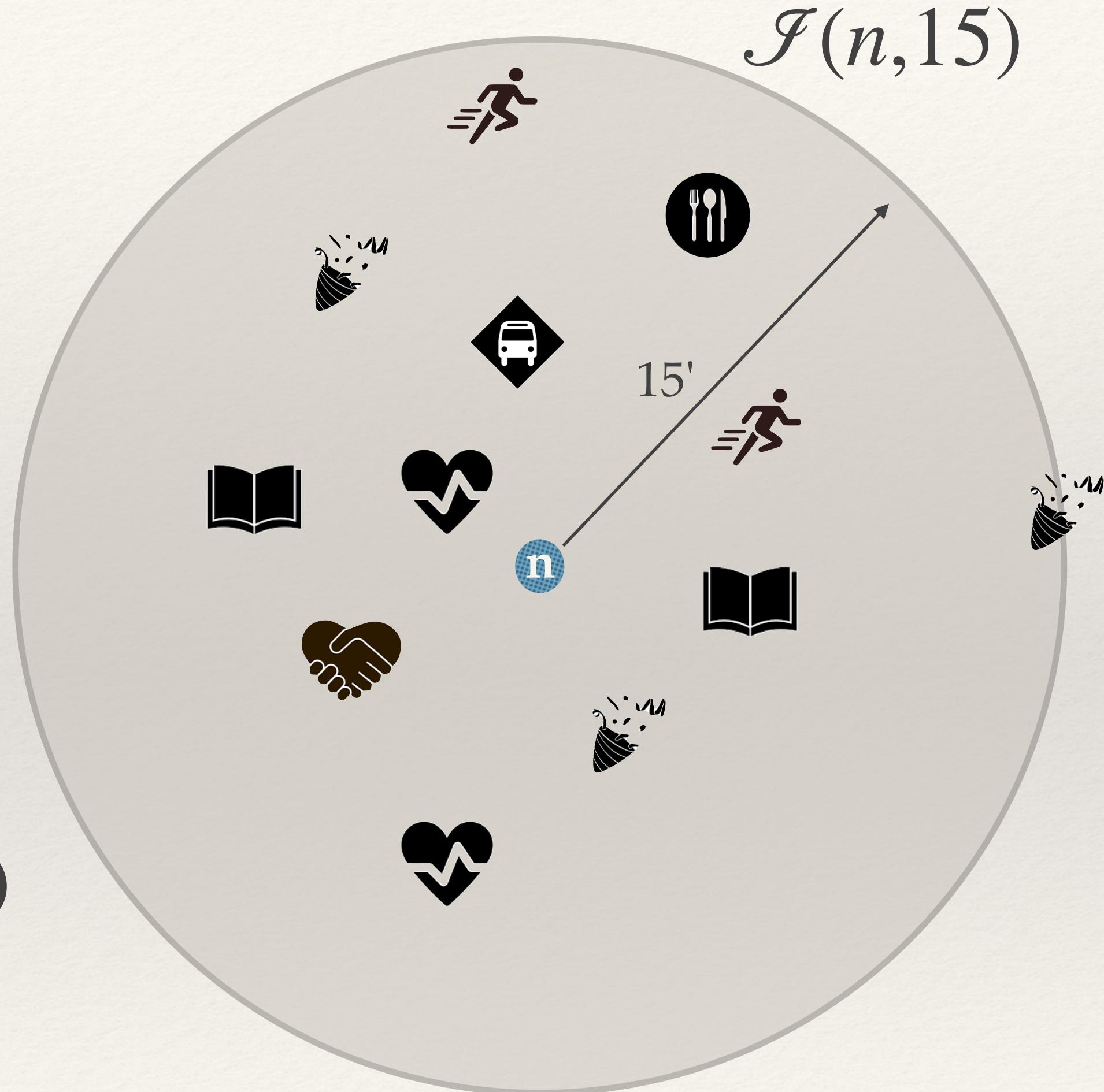


$$\mathcal{P}(n) = 12$$

$$\mathcal{D}(n, 15) = 1.71$$

Accessibility Metrics

- ❖ Given $n \in N_c$
 - ❖ PoI-Proximity $\mathcal{P}(n) = t$
 - ❖ PoI-Density $\mathcal{D}(n, t)$
 - ❖ PoI-Entropy $\mathcal{E}(n, t)$
 - ❖ PoI-Accessibility $\mathcal{A}(n, t)$



PoI's categories:

Mobility



Active Living



Entertainment



Food Choices



Community



Education



Health and Well-being



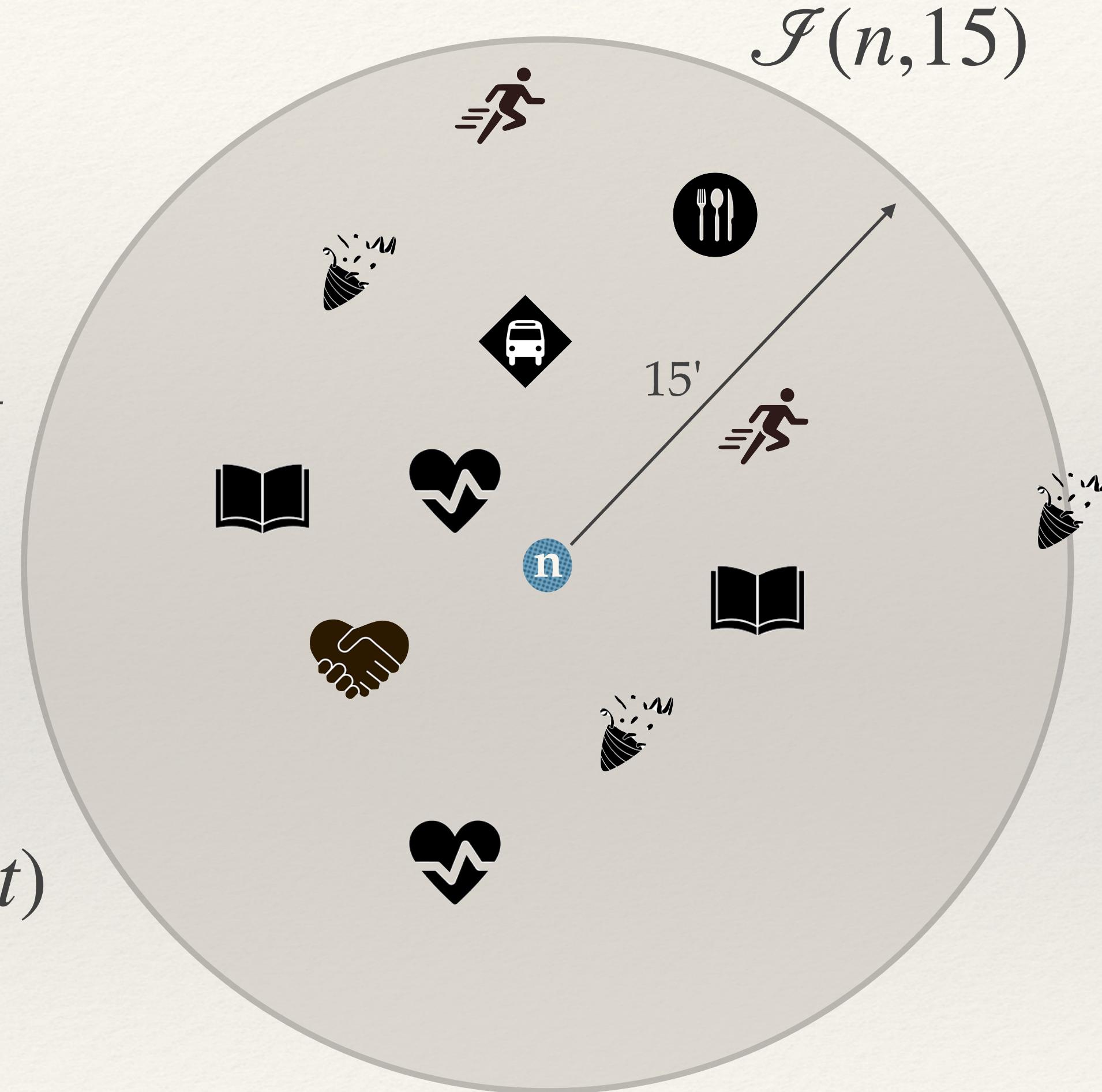
$$\mathcal{P}(n) = 12$$

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Accessibility Metrics

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- ❖ PoI-Density $\mathcal{D}(n, t)$
- ❖ PoI-Entropy $\mathcal{E}(n, t)$
- ❖ **PoI-Accessibility** $\mathcal{A}(n, t)$



PoI's categories:

Mobility



Active Living



Entertainment



Food Choices



Community



Education



Health and Well-being



$$\mathcal{P}(n) = 12$$

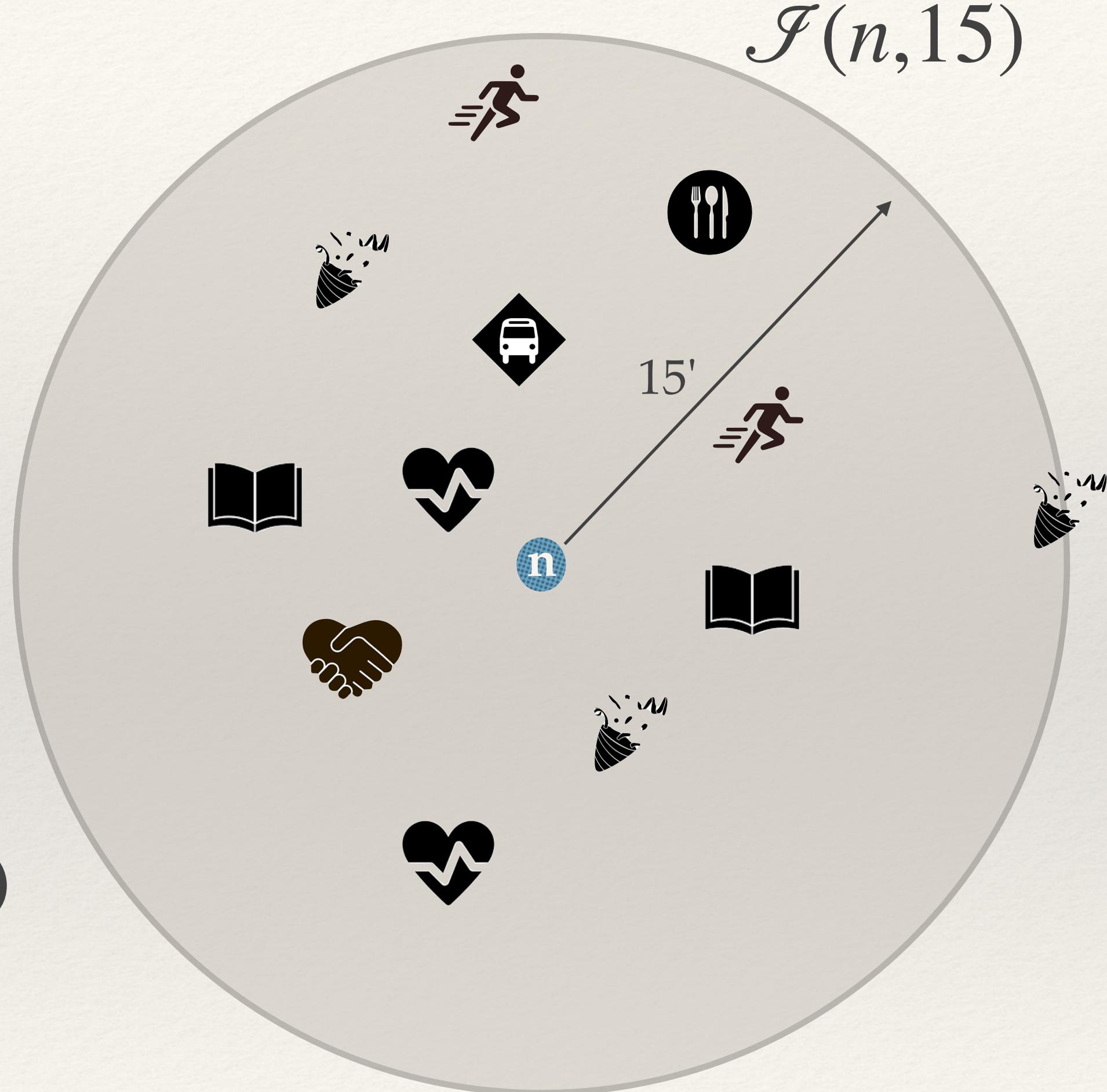
$$\mathcal{D}(n, 15) = 1.71$$

$$\mathcal{E}(n, 15) = 2.69$$

$$\mathcal{A}(n, t) = w_1 \mathcal{P}'(n) + w_2 \mathcal{D}'(n, t) + w_3 \mathcal{E}'(n, t) \quad \text{e.g., } w_1 = w_2 = w_3 = 1/3, \text{ and } t = 15$$

Accessibility Metrics

- ❖ Given $n \in N_c$
 - ❖ PoI-Proximity $\mathcal{P}(n) = t$
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 - ❖ PoI-Entropy $\mathcal{E}(n, t)$
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PoI's categories:

Mobility



Active Living



Entertainment



Food Choices



Community



Education



Health and Well-being



$$\mathcal{P}(n) = 12$$

$$\mathcal{D}(n, 15) = 1.71$$

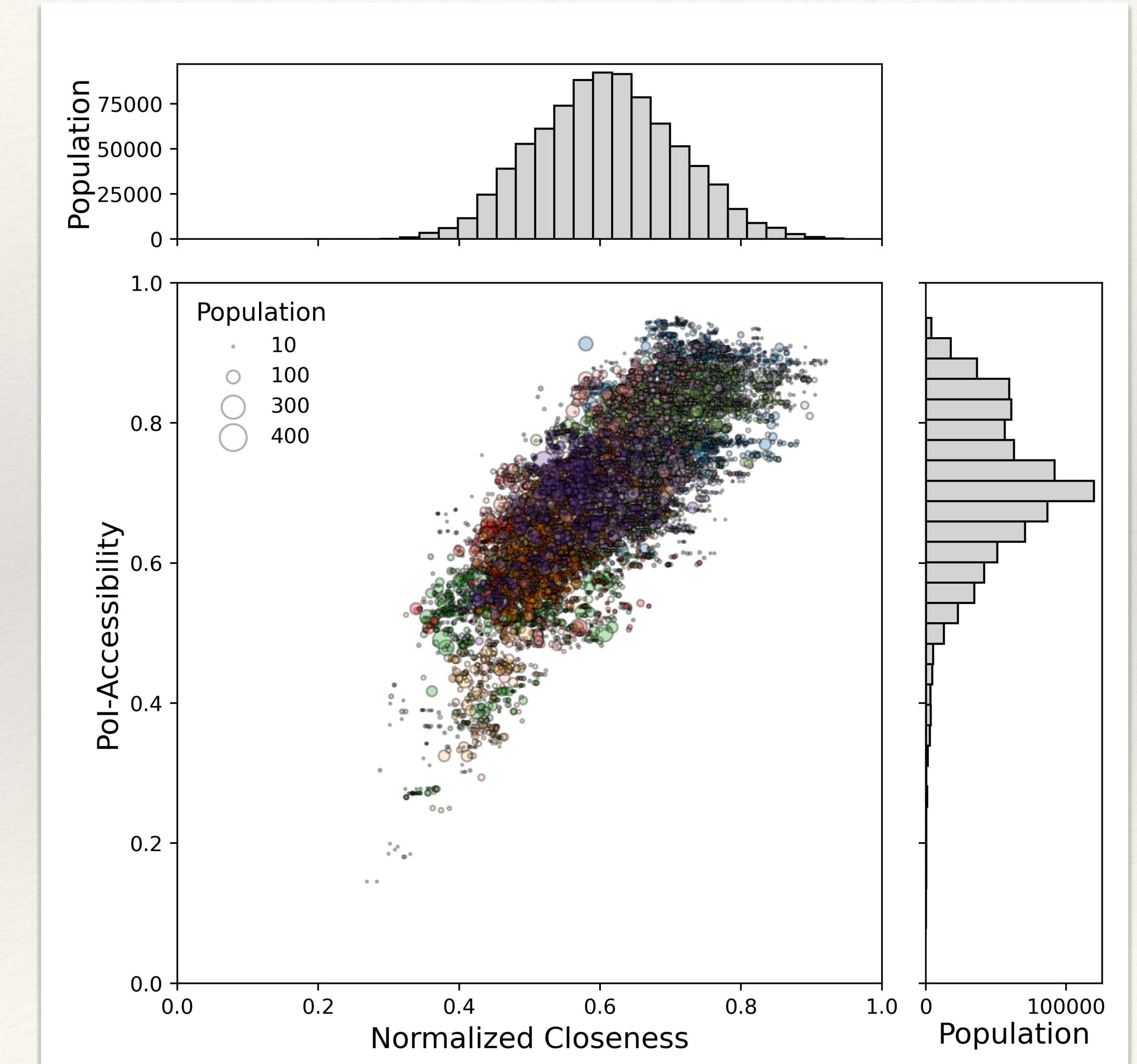
$$\mathcal{E}(n, 15) = 2.69$$

$$\mathcal{A}(n, 15) \in [0, 1]$$

closeness vs poi-accessibility

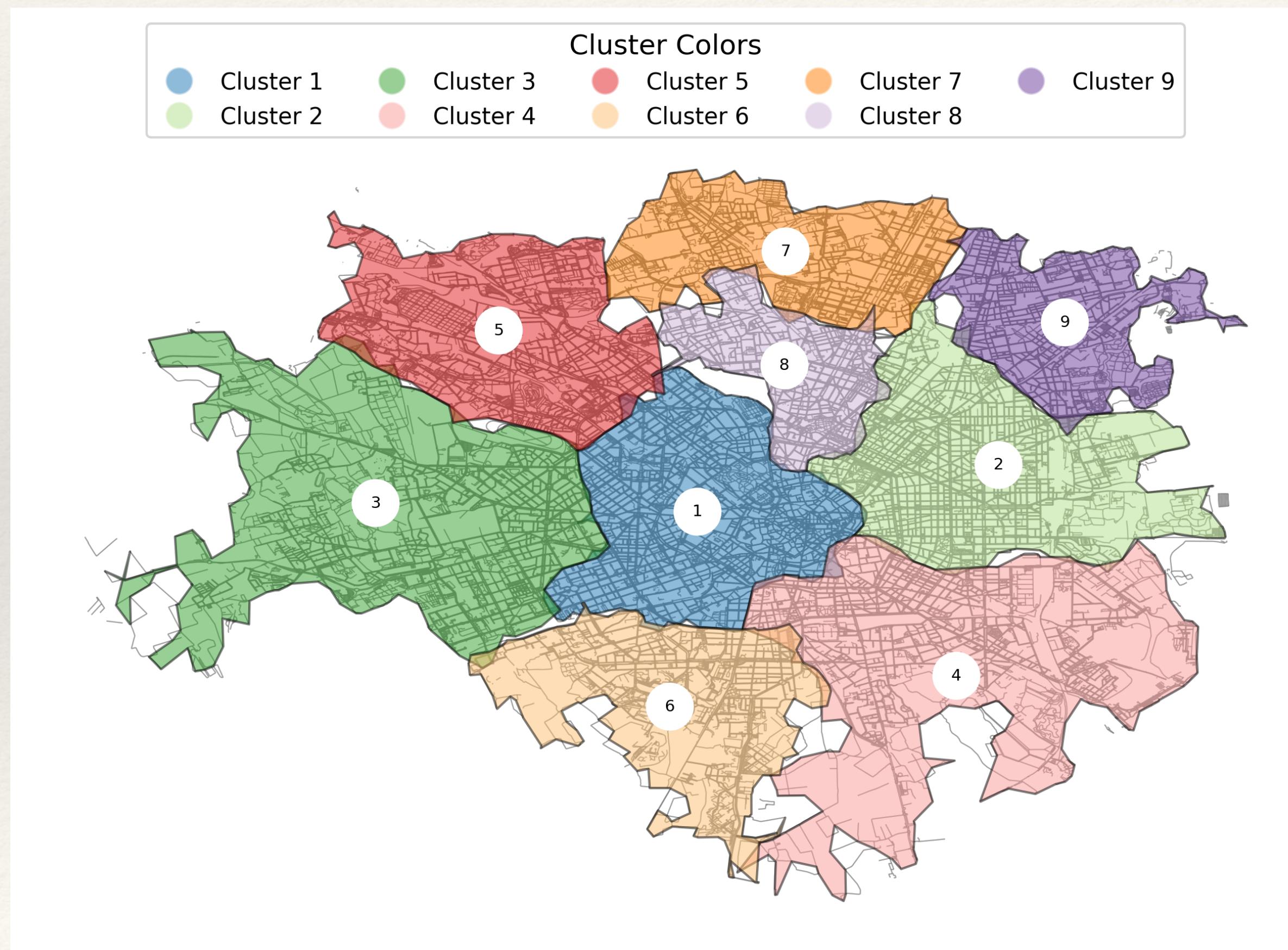
Closeness vs PoI-Accessibility ($t=15'$)

Milan, census areas

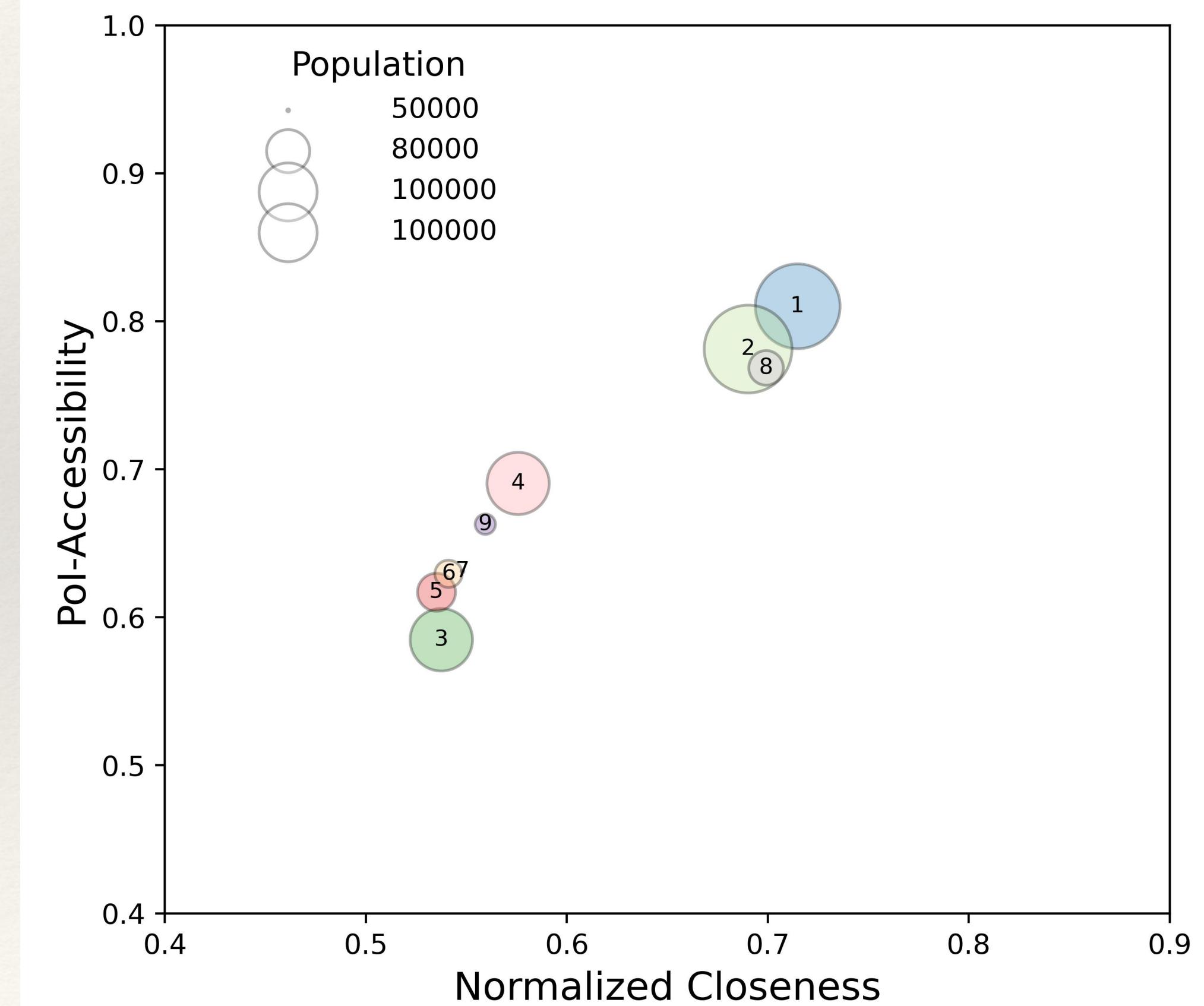


Closeness vs PoI-Accessibility ($t=15'$)

Milan, infomap clusters

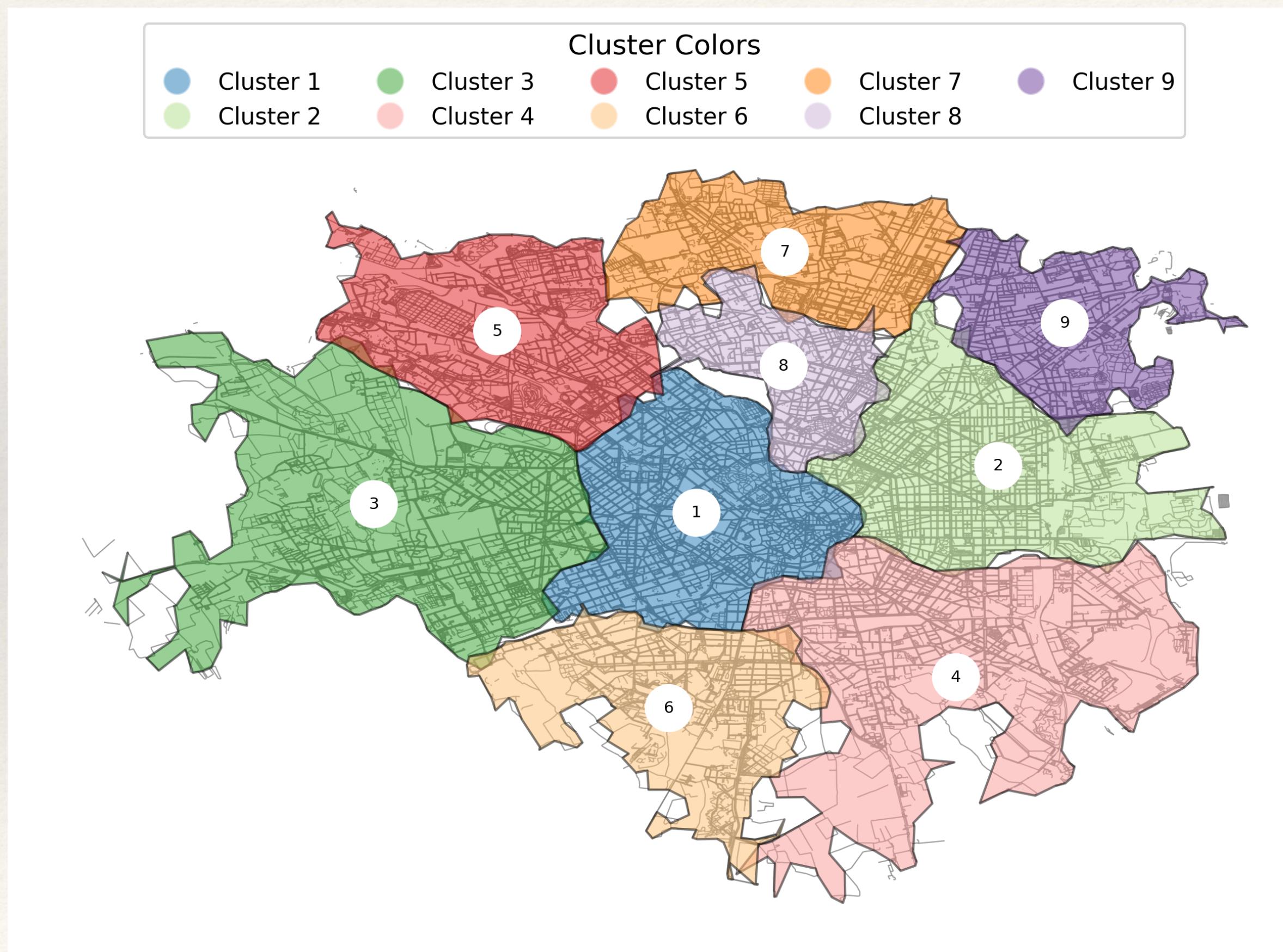


Pol-Accessibility vs Closeness - Milan, Italy

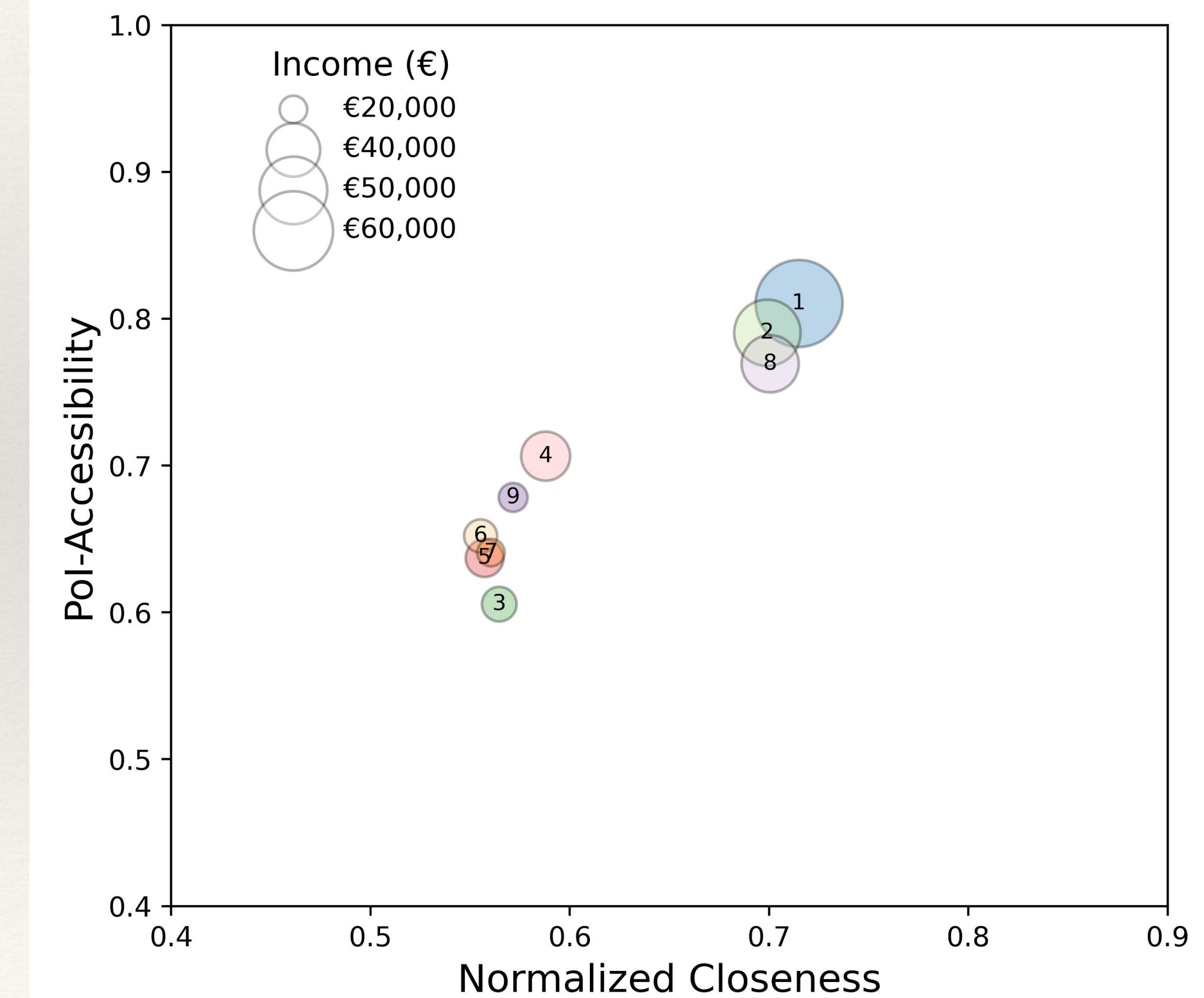


Closeness vs PoI-Accessibility ($t=15'$)

Milan, infomap clusters



Pol-Accessibility vs Closeness - Milan, Italy

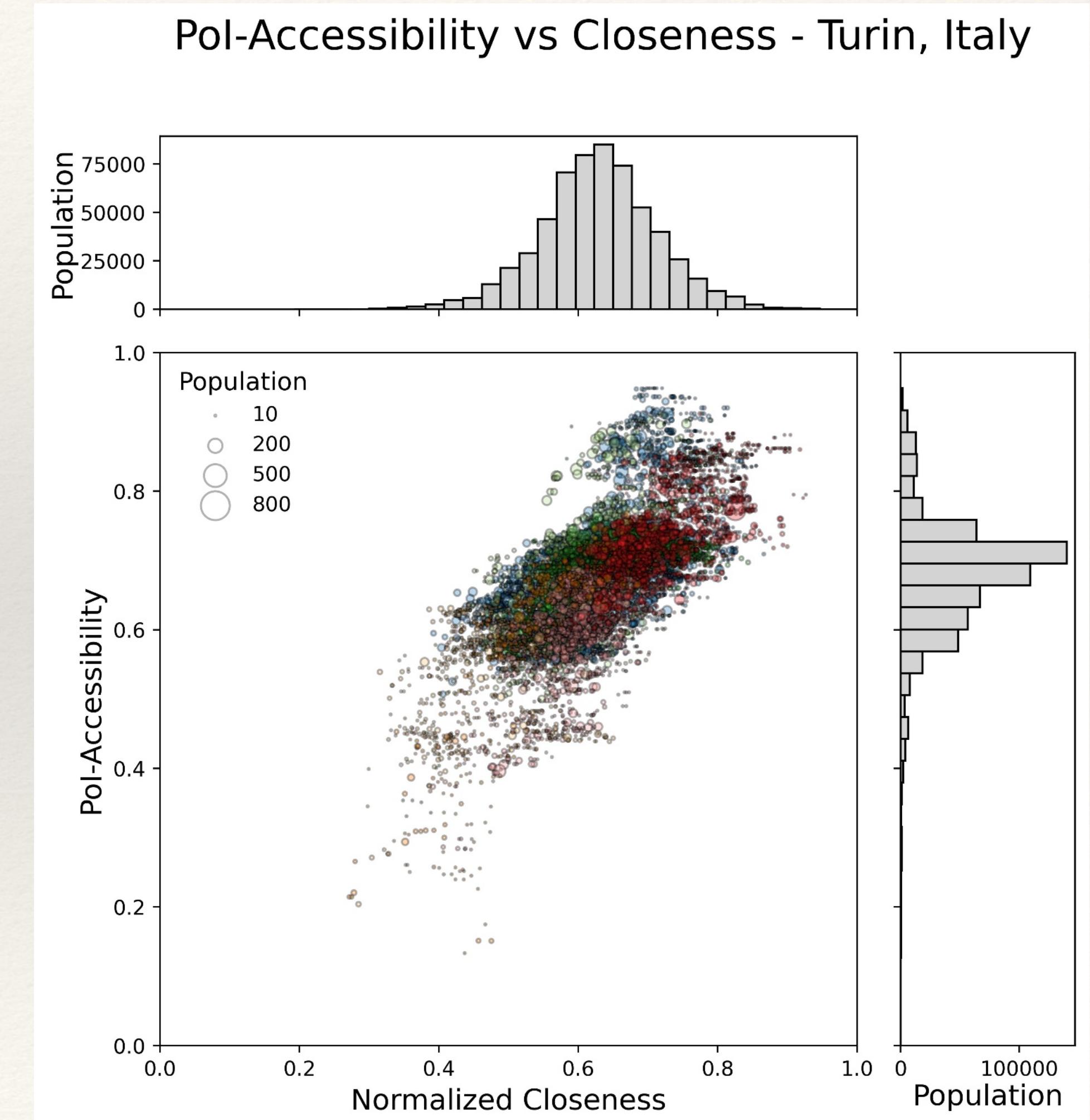


Closeness vs PoI-Accessibility ($t=15'$)

Turin, census areas

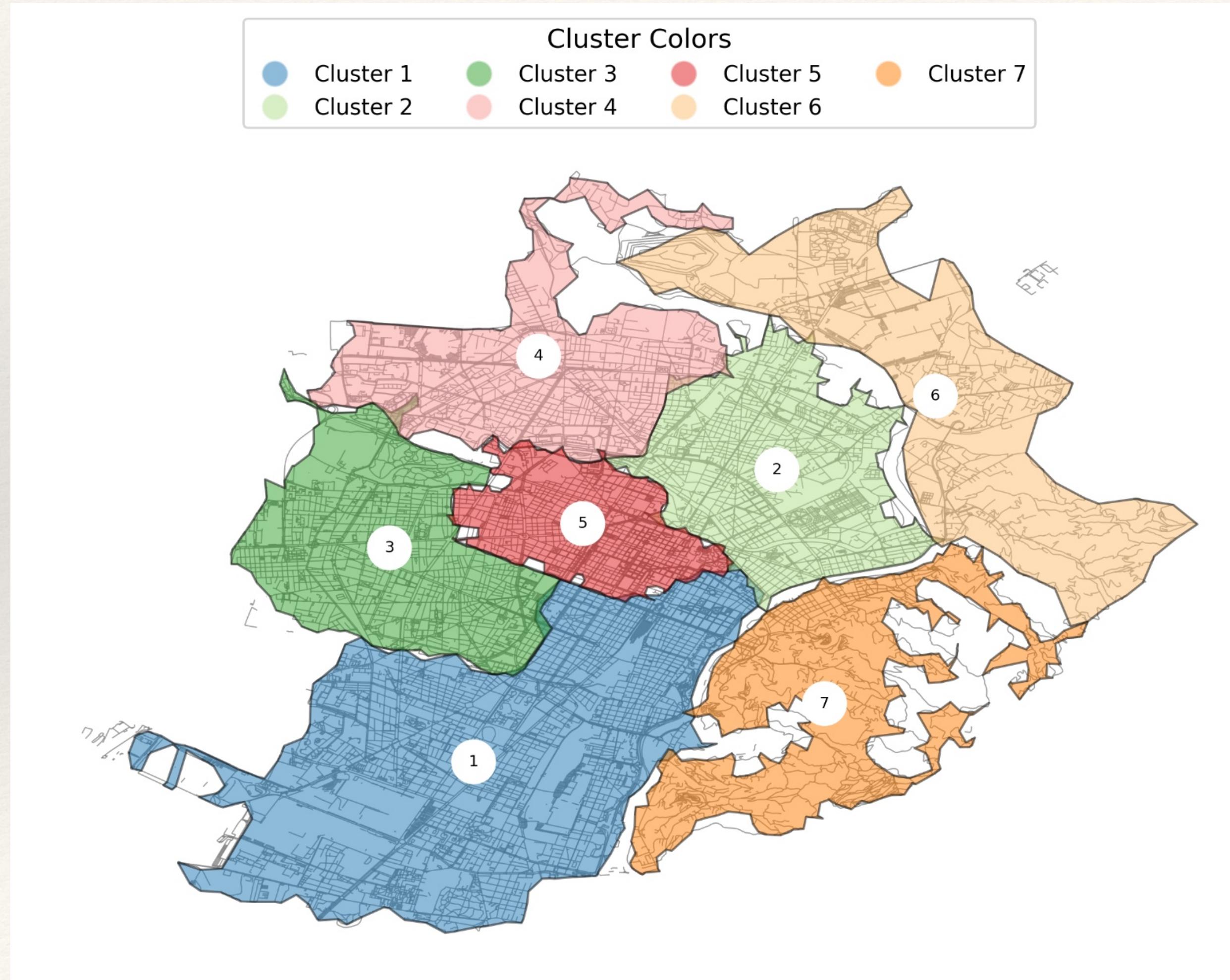


Pol-Accessibility vs Closeness - Turin, Italy

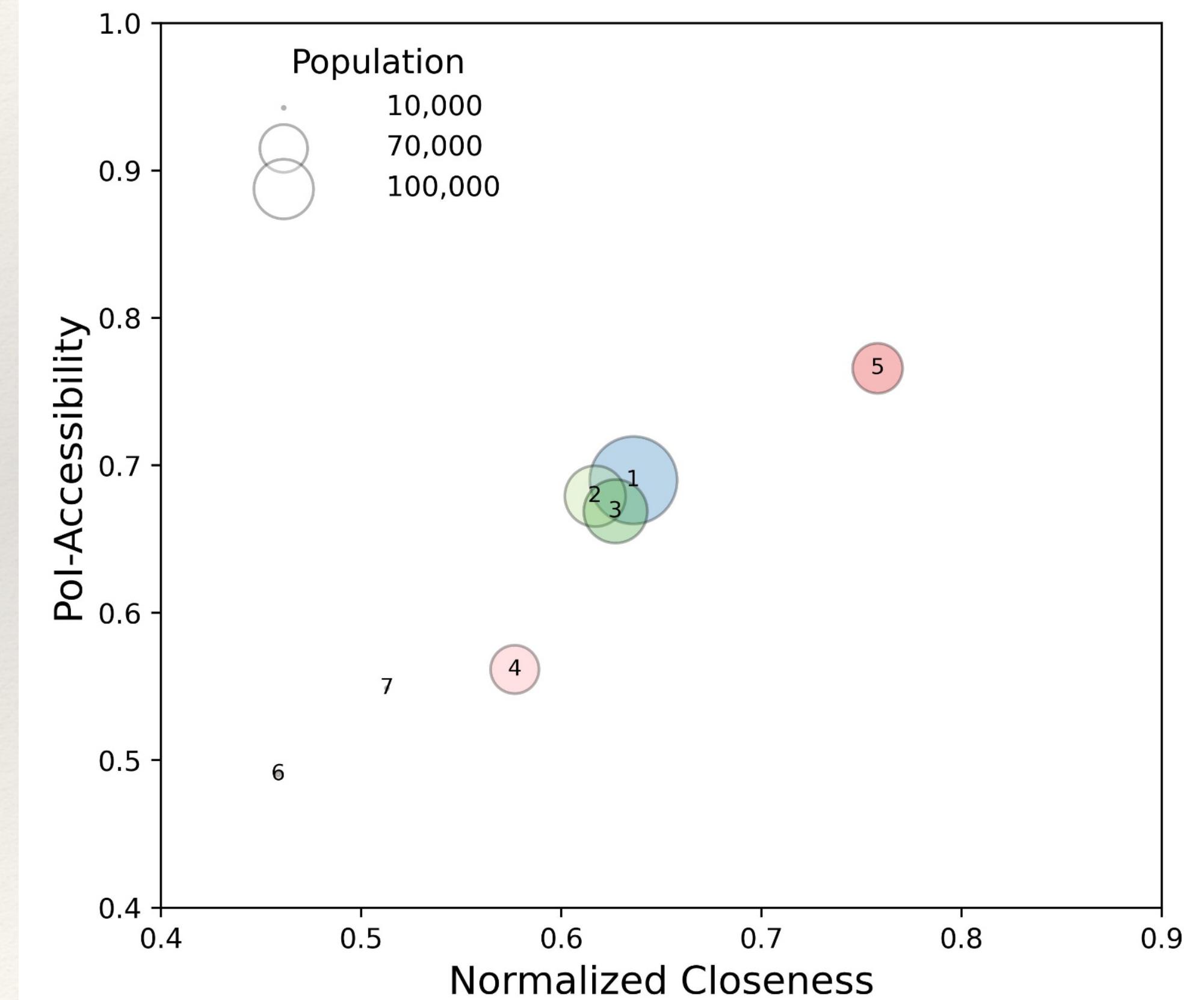


Closeness vs PoI-Accessibility ($t=15'$)

Turin, infomap clusters

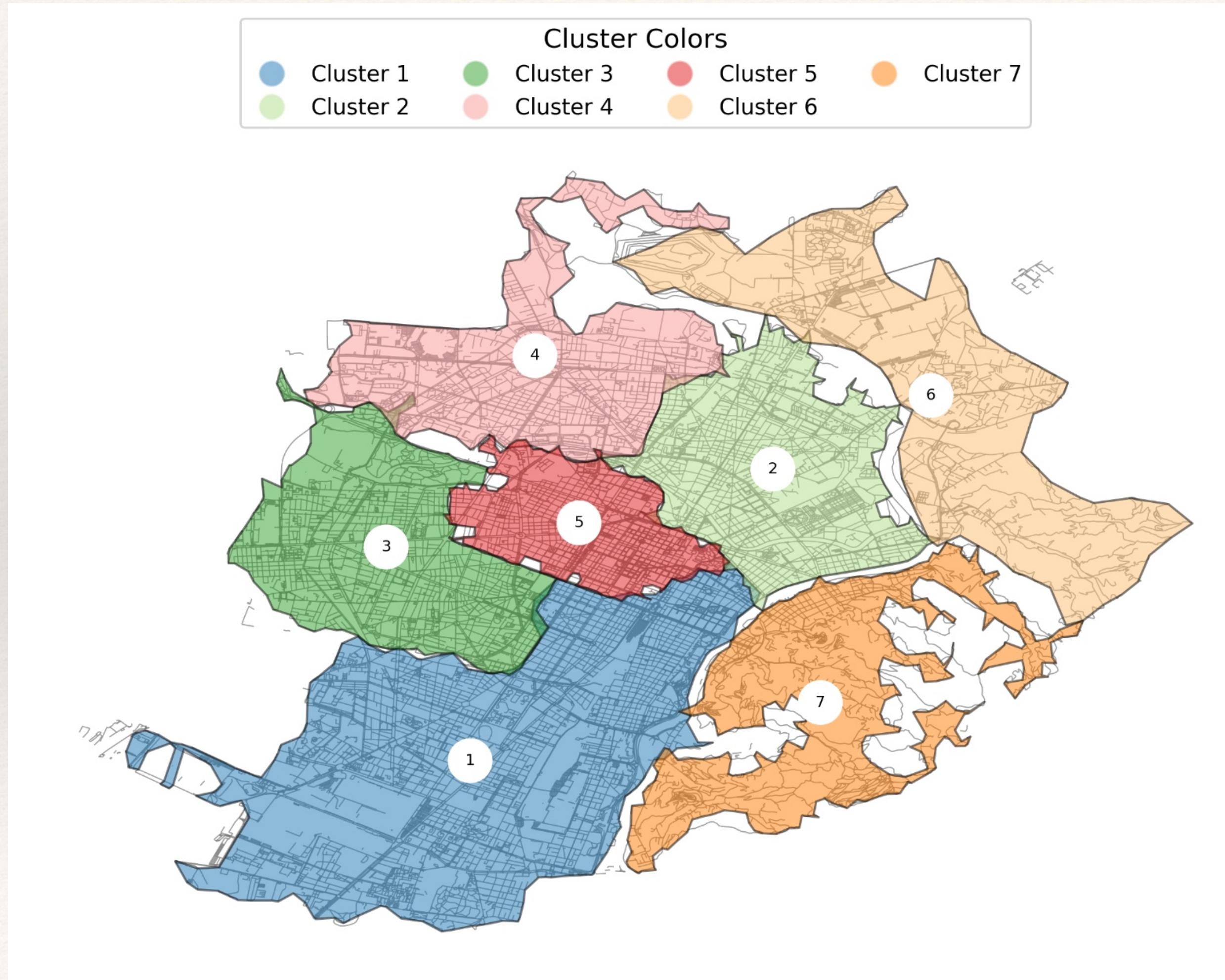


Pol-Accessibility vs Closeness - Turin, Italy

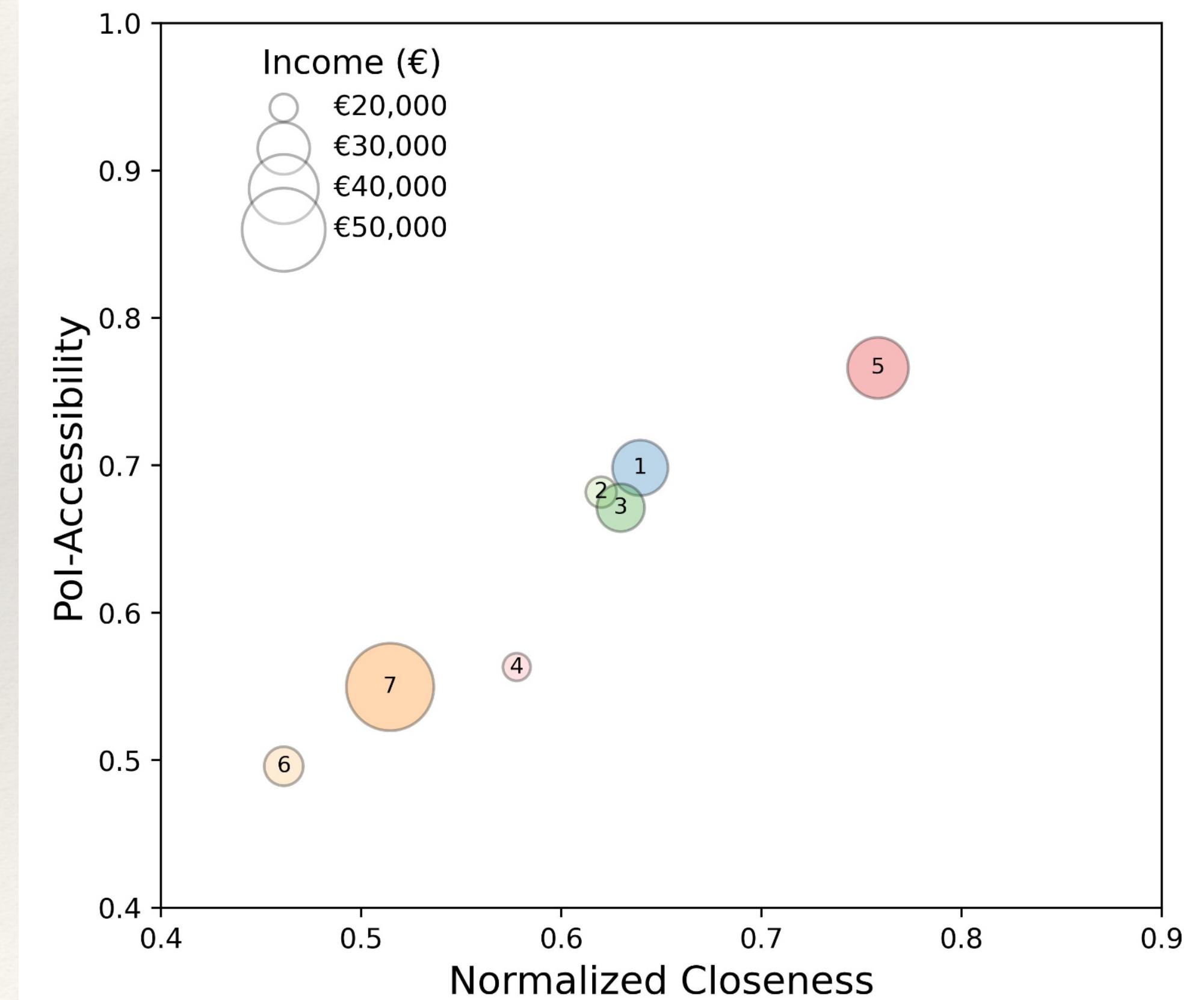


Closeness vs PoI-Accessibility (t=15')

Turin, infomap clusters

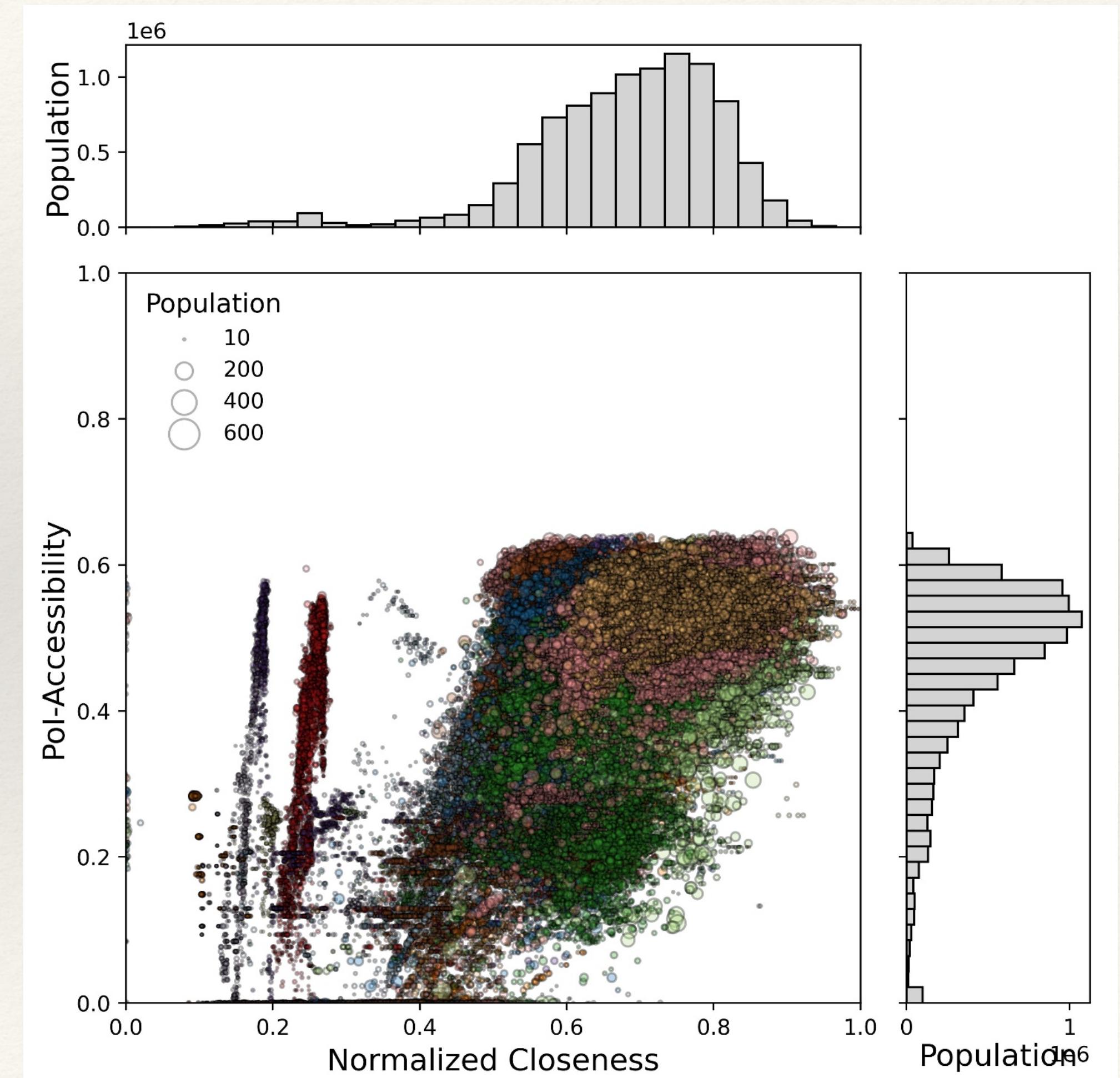


Pol-Accessibility vs Closeness - Turin, Italy



Closeness vs PoI-Accessibility ($t=15'$)

Istanbul, census areas



Closeness vs PoI-Accessibility ($t=15'$)

Istanbul, infomap clusters

