Due Date: 30.06.22

Computer Homework 3

Submission guidelines

students.

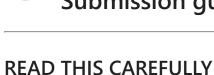
via mail, and not via Moodle.

imports for the HW

1.a - Spatial Sampling:

rectangle in the following figure:

course also use the Internet's help.



topic before learning about it in class, or you may wait until the topic is taught, and solve only the questions on the topics you already learned. • Avoid unethical behavior. This includes plagiarism, not giving credit to source code you decide to use, and false reporting of results. Consulting with friends is allowed and even recommended, but you must write the code on your own, independently of others. The staff will treat unethical behavior with

• Please notice: Some of the exercises contain questions on topics that are yet to be taught in the

lecture or the frontal exercises. You may consider them as background or preparation questions to the

the utmost severity. !אנא המנעו מהתנהגות שאינה אתית והעתקות

- Code submission in **Python only**. You can choose your working environment: ■ You can work in a Jupyter Notebook , locally with Anaconda (the course's computer HW will not require a GPU).
- You can work in a Python IDE such as PyCharm or Visual Studio Code. Both also allow opening/editing Jupyter Notebooks. • The exercise must be submitted IN PAIRS (unless the computer homework grader approved
- differently) until Thursday 30.06.2022 at 23:55.

No other file-types (.docx , .html , ...) will be accepted

- The exercise will be submitted via Moodle in the following form: You should submit two **separated**
 - A report file (visualizations, discussing the results and answering the questions) in a .pdf format, with the name hw3_id1_id2.pdf where id1, id2 are the ID numbers of the submitting

• Be precise, we expect on point answers. But don't be afraid to explain you statements

- (actually, we expect you to). Even if the instructions says "Show/Display...", you still need to explain what are you showing and what can be seen.
 - A compressed .zip file, with the name: hw3_id1_id2.zip which contains: A folder named code with all the code files inside (.py or .ipynb ONLY!) • The code should be reasonably documented, especially in places where non-trivial
 - actions are performed. • Make sure to give a suitable title (informative and accurate) to each image or graph, and also to the axes. Ensure that graphs and images are displayed in a sufficient size to
 - understand their content (and maintain the relationship between the axes do not
 - distort them). A folder named my_data , with all the files required for the code to run (your own images/videos) and all the files you created. make sure to refer to your input files in the code

directory): img = cv2.imread('../my_data/my_img.jpg')

locally. i.e. (if the code is in 'code' directory, and the input file is in a parallel 'my_data'

as it is located in a folder named given_data . i.e.: img = cv2.imread('../given_data/given_img.jpg') • If you submit your solution after the deadline, 4 points will be reduced automatically for each of the days that have passed since the submission date (unless you have approved it with the course staff

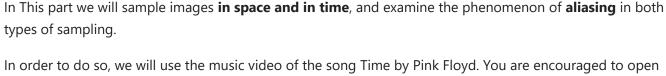
before the submission date). Late submission will be done directly to the computer homework grader

Several Python, numpy, openCV reference files are attached in the Moodle website, and you can of

Questions about the computer exercise can be directed to the computer homework grader through

• DO NOT include the given input data in the zip. The code should refer to the given input data

- the relevant Moodle forum or by email. **General Notes:**
- import numpy as np import matplotlib.pyplot as plt import cv2 import glob
- Part 1 Sampling and Aliasing in Images



1. Sample the first frame from the 33rd second of the Time - Pink Floyd.mp4 video and display it. You may use the video_to_frames function from your first python HW. For the spatial sampling in this section we will use the region in the frame which contains a row of 7 clocks, as seen in the red

the file Time - Pink Floyd.mp4, to watch the video and enjoy the music.:)

2. Let us examine the 292 nd row of the image. Create a copy of the original image in which this row is marked in red and display it. In addition, create and display a graph containing the gray levels of the

292 nd row of one of the color channels (your choice) as a function of the column index.

3. Now, for the spatial sampling: sample the image with sampling interval of $\Delta x = 64$ (meaning sample only the columns of the image, with no sampling on the y-axis). The sampling will start at the middle of the image (the green line in the above figure) and continue towards both directions (i.e., the central column of the image is sampled, and then all the columns in the image that are of $n\cdot \Delta x$ distance from it, for $n \in \mathbb{Z}$ (within image borders, of course). Display the sampled image and a copy of the original image in which the sampled columns are marked in red. 4. In order to evaluate the result of sampling we would like to return the image to its original dimensions. 292 nd row in one of the color channel you previously chose as a function of the column index for the new image. What are the differences between this graph and the graph from section 1.a.2? Explain.

1.b - Temporal Sampling:

your first python HW.

Order Hold interpolation: every frame in your sampled video will be translated in the new video into $\Delta p=16$ consecutive frames. Create the video and save it in <code>mp4</code> format. **Attach the video to your** submission in the my_data folder. (Note that the video does not need to contain sound).

1. In this part we would like to perform a temporal sample on a time section from the video. Watch the time section between the seconds 30-45. In this part we will use only this time section. In what direction do the clocks in the time section progress in space? In what direction do the clocks hands turn? Load all the frames from this time section. You may use the video_to_frames function from

2. Sample the time section with sampling interval of $\Delta p=16$ (meaning - the frames indexed 0, 16, 32, etc...). In order to examine the influence of the temporal sampling, create a new video having the duration of the original time section (15 seconds) and the same FPS rate. In order to do so, use Zero-

- Part 2 PCA Compression One of the ways to compress images is by using dimensionality reduction and saving the image representaion in the lower dimension. One of the classic methods for dimensionality reduction is Principal Component Analysis (PCA).
 - 3. Calculate the mean of every pixel in the X array (results in a 4096 vector) and display it as a 64x64 image (don't forget the 'F' argument in np.reshape). Now, transform the mean vector into a 4096x1 array and call it mu . Subtract mu from X to get an array of data centered around 0 - call it

4. Calculate the covariance matrix of Y using np.cov. Note that the size of the covariance matrix is depended on the size of each sample, and in our case we should get a matrix of size 4096x4096.

2. Define numpy array X of size 4096x13233 in which every column represents one of the images in

2.b - Principal Components

2.d - Restoration

More extensively, you will:

Gaussian Pyramid

different frequency ranges.

:return:

Guidance:

assert $m \ge 0$ and $m \le n$

===== YOUR CODE: =====

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return gauss pyr, laplace pyr

3.a - Pyramids creation

components.

exercise).

Υ.

2.c - Compression by projection Find the projection of every image in the space spanned by the k=10 principal components by calculating:

 $P = V^T Y$

smaller than the original image. Part 3 - Multiple Resolutions

how to calculate these pyramids and you will implement a useful app using them.

construct a Gaussian pyramid and a Laplacian pyramid out of an image

 $L_i = G_i - \operatorname{expand}(G_{i+1})$

in each axis (reduce operation). The 0th level is the original image.

:param n: number of pyramid levels

:param img: The input gray-scale image.

gauss pyr: The Gaussian pyramid.

laplace_pyr: The Laplacian pyramid.

np array of of type uint8. :param gauss pyr: The Gaussian pyramid so far.

:param laplace_pyr: The Laplacian pyramid so far.

:param m: current pyramid level

reconstruct the image from the Laplacian pyramid implement image blending using multiple resolutions

have enlarged the dimension of the images in the low dimesional space, it is still less than 7 times (!)

columns and then convolving the result with the same Gaussian filter as in the Gaussian pyramid, multiplied by 4). For Gaussian and Laplacian pyramids with n levels, the nth level of the Laplacian pyramid will be equal to the nth level of the Gaussian pyramid. In fact, the Laplacian pyramid divides the image into

created by calculating the difference between the corresponding Gaussian level and the next Gaussian level after expansion is applyed on it (expansion - upsampling the source image by injecting even zero rows and

Gaussian pyramid: each level of the Gaussian pyramid (the left column in the above illustration) is created by filtering of the previous level using a Gaussian filter, and then sampling one pixel from every two pixels

Laplacian pyramid: each level of the Laplacian pyramid (the right column in the above illustration) is

- the bottom of the pyramid. Note that the cv2.pyrUp function doesn't accept int inputs, therefore you should change the type of its input to uint8. def laplace_recon(laplace_pyr): Image reconstruction from Laplacian pyramid. :param laplace_pyr: The Laplacian pyramid.

as np arrays of type int.

We will do so by interpolating on the column dimension, using cv2.resize that uses bilinear interpolation by default. Return the sampled image to its original dimensions and display the result. 5. Examine our region of interest (the red rectangle in section 1.a.1) in your new image. How many "smeared" clocks can you identify now? Create and display a graph containing the gray levels of the

- 3. Watch the video you created in what direction do the clocks progress now? In what direction do the clocks hands turn? Explain.
- Note: You ar not allowed to use PCA functions already implemented in Python packages in this part. 2.a - Pre-processing & covariance matrix 1. Uncompress the dataset in a sub-folder named LFW in the given_data folder. Load all of the images into a 3D numpy array of size 64x64x13233 (after converting them to grayscale). Display 4 images from the data set (remember their indices - these are the images you will restore later in the

In This part we will examine this method and its performance on a set of images containing faces of people:

Labelled Face In the Wild (LFW). The set consists of 13233 gray-scale images of size 64x64.

• Note: DO NOT upload the data set as part of your submission!

column-major representation (don't forget the 'F' argument in np.reshape).

The eigenvectors of the covariance matrix are called the **Principal Components**. If one would calculate all of the principal components of our covariance matrix, they will get a spanning set of the \mathbb{R}^{4096} space. In practice, in order to perform dimensionality reduction, we want to project our data into a lower dimension.

In PCA we do so by projecting every image into a space with a spanning set of k eigenvectors (principal

• The parameter eig_vals will contain the k=10 eigenvalues in descending order (largest eigenvalue

• The parameter eig_vecs will contain a matrix in which the columns are the corresponding principal

Display a plot of the eig_vals vector. In addition, display the first 4 principal components in eig_vecs

Calculate the k=10 largest eigenvalues of the covariance matrix and their corresponding principal

• The covariance matrix is symmetric, so you can use np.linalg.eigh in order to find them.

components) corresponding to the k largest eigenvalues of the covariance matrix.

as images of size 64x64 (don't forget the 'F' argument in np.reshape).

where V is the eig_vecs matrix and Y is the data matrix Y. Note that now each column of the matrix P is actually a representation of one image from the data set (after subtracting the mean), in the lower dimension.

components in order respective to eig_vals.

Where x_i is the original image corresponding to column p_i in X. 2.e - Changing k value Now, compress Y using k=570 principal components, and restore and display again the 4 images you

chose. What do you think of the restored results now? Compare to the k=10 case. Note that although we

Multi-resolution pyramids are a very useful tool in the field of image processing. In this part you will learn

The construction of a Gaussian pyramid and a Laplacian pyramid is depicted in the following illustration:

Laplacian Pyramid

 $L_n = G_n$

• You may use the cv2.pyrUp and cv2.pyrDown functions in your implementation. You should implement the function recursively. • The Laplacian pyramid levels should contain negative values (because of the subtraction). So, each Laplacian level contains a nparray of type int. Therefore during the calculation of each Laplacian level, you should convert the gaussian level and the expansion to be of int type. different sizes (your choice). 3.b - Reconstruction using Laplacian pyramid

----return recon img

recon img: The reconstructed image.

:return:

Credits

the original images and the reconstructions. 3.c - Image blending Create a mask of the same size as the original images. The mask will contain 1 s in its left half and 0 s in its right half. Create a Gaussian pyramid out of this mask. Create a new Laplacian pyramid. let us define $L_{Ironman}^{(i)}$ as the ith level of the Laplacian pyramid of the Ironman image, $L_{Downey}^{(i)}$ as the ith level of the Laplacian pyramid of the Downey image, and $G_{mask}^{(i)}$ as

Icons from Icon8.com - https://icons8.com

===== YOUR CODE: =====

 $L_{blend}^{(i)} = G_{mask}^{(i)} L_{Ironman}^{(i)} + (1 - G_{mask}^{(i)}) L_{Downey}^{(i)}$

Now use laplace_recon on the new pyramid and display the reconstructed image. Explain the result.

Now, reconstruct both of the images using laplace_recon and display the reconstructed images and the subtraction images between the original and reconstructed images. Calculate and display the MSE between

the ith level of the Gaussian pyramid of the mask. The ith level of the new pyramid, $L_{blend'}^{(i)}$ will be defined

as follows:

 $\hat{x}_i = V p_i + \mu$ Where μ is the calculated mean mu . Display the 4 restored images (sized 64x64). In the title of each image display the MSE between the original image and the restoration. Reminder: $MSE_i = rac{1}{MN} \sum_{m=0}^{M-1} \sum_{n=0}^{N-1} (x_i[m,n] - \hat{x}_i[m,n])^2$

For the 4 images you presented in section 2.a.1, extract the appropriate columns in the P matrix. We will denote each column as p_i where $i \in \{1,2,3,4\}$. Find \hat{x}_i , the restoration of each column by applying:

Implement the function pyr_gen that constructs Gaussian and Laplacian pyramids out of an image. def pyr gen(n, m, img, gauss pyr, laplace pyr): Constructs Gaussian and Laplacian pyramids out of an image.

The m-1 level of the Gaussian pyramid.

as np arrays of type uint8.

as np arrays of type int.

as np arrays of type uint8.

as np arrays of type int.

(excluding the 0th level - total number of levels - n+1).

Python list of length [m-1] containing the pyramid levels

Python list of length [n-m+1] containing the pyramid levels

Python list of length [n-m+1] containing the pyramid levels

Python list of length [m-1] containing the pyramid levels

Now, load the images Ironman.jpg and Downey.jpg and convert them to grayscale. Build for both of them Gaussian and Laplacian pyramids with n=4 levels using pyr_gen. Display the results: two figures, one for every image. The top row of each figure will contain the Gaussian pyramid, and the bottom row will contain the Laplacian pyramid (5 images in each row). The images can be displayed in the same size, or in Implement the function laplace_recon which reconstructs an image by summing all of its Laplacian pyramid levels. The summation will start from the top of the pyramid (level n - smallest image) and will continue iteratively: Perform expansion on the ith level and sum it with the (i-1)th level, until reaching

Python list containing the pyramid levels

2D np array of the same shape as laplace_pyr[0].