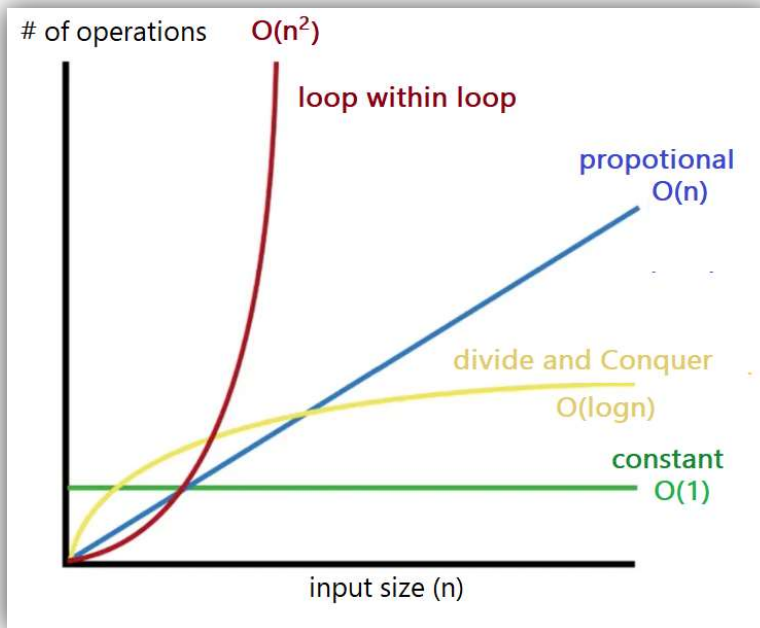


## Big O

- A Measure to the worst-case scenario for a
- A way of comparing two sets of code mathematically about how efficient they run.
- We measure time complexity. But it is not measured in time, but in number of operations it takes to complete something.



## Rules for simplifications for Big O

### 1. Drop constants:

If Big O =  $O(n+n) = O(2n)$   
It can be simplified to  $O(n)$

### 2. Drop non-dominant:

If Big O =  $O(n^2)+O(n) = O(n^2+n)$   
It can be simplified to  $O(n^2)$

### 3. Different terms for inputs

If Big O =  $O(a) + O(b)$  it cannot be simplified further as  $a \neq b$

## Examples on how to calculate Big O:

- 1- If we have one loop, Big O =  $O(n)$ ,  $n$  is the max number of operations this loop takes.

```
public static void printItems(int n) {  
    for (int i = 0; i < n; i++) {  
        System.out.println(i);  
    }  
}
```

the Big O for one  
for loop is  $O(n)$

- 2- If we have 2 loops, Big O =  $O(n) + O(n) = O(2n) = O(n)$

```
public static void printItems(int n) {  
    for (int i = 0; i < n; i++) {  
        System.out.println(i);  
    }  
  
    for (int j = 0; j < n; j++) {  
        System.out.println(j);  
    }  
}
```

Big O for 2  
for loops =  
 $O(n) + O(n)$

- 3- If we have 2 nested loops, Big O =  $O(n * n) = O(n^2)$

```
public static void printItems(int n) {  
    for (int i = 0; i < n; i++) {  
        for (int j = 0; j < n; j++) {  
            System.out.println(i + " " + j);  
        }  
    }  
}
```

Big O of two  
nested loops  
=  $O(n * n)$   
=  $O(n^2)$

4- If we have 2 loops of different lengths (inputs), Big O=  $O(a)+O(b)$

```
public static void printItems(int a, int b) {  
    for (int i = 0; i < (a); i++) {  
        System.out.println(i);  
    }  
  
    for (int j = 0; j < (b); j++) {  
        System.out.println(j);  
    }  
}
```

we have to use  
different terms for  
inputs

$O(a)+O(b)=O(a+b)$

#### 4. Big O= $O(1)$

$O(1)$  does not mean that there will be only one operation; but it means that as  $n$  grows, the number of operations stays constant.

```
public int addElement(int n) {  
    return n+n+n;  
}
```

$O(1)$  is the most efficient Big O

## Big O for array Lists:

- If we want to add/remove an element to the end of the list, then no re-indexing needed so Big O =  $O(1)$
- If we want to add/remove element from the beginning of the list, so we need to re-index the whole list, Big O =  $O(n)$ ,  $n$  is the arraylist length
- If we want to add a new element to in the middle of the arraylist, Big O =  $O(n-i) = O(n)$ ,  $i$  is the index at which we will insert the new element and start re-indexing the remaining list.
- If we search for an element by index, Big O =  $O(1)$
- If we search for an element by value, Big O =  $O(n)$

```
int array[] = {1,2,3,4,5};
List<Integer> numbers = Arrays.stream(array).boxed().toList();

//Big O to add/remove element to the end of the list will always be O(1)
numbers.add(5); //O(1)
numbers.remove(index: 5); //O(1)

//Big O to add/remove element at the first index is O(n), n number of array elements
numbers.add(index: 0, element: 7); //O(n)
numbers.remove(index: 0); //O(n)

//Big O to find an element by value O(n), because the worst case here is we are
//searching on the element of value 5, so will iterate all over the array till we find it
numbers.contains(5); //O(n), find the element of value 5

//Big O to find an element by index is much better, as it is always O(1)
//we access the element directly
numbers.get(3); //O(1), find element of index 3
```