

## Problem #9

1 - Activity Selection : Dp vs Greedy

a. Optimal Substructure?

Yes. if  $a_k$  is in an optimal solution for  $S-ap$ , then the subproblems  $(S-a_k)$  and  $(a_k, p)$  must also be optimal (removing an activity from an optimal solution leaves an optimal sub-solution).

b. Recu Select ( $s, f, k, n$ )

RecuSelect ( $s, f, a, p$ ):

if  $S-ap = \emptyset$ : return []  
best = [ ]

for each  $a_k$  in  $S-ap$ :

left = RecuSelect ( $s, f, a, k$ )

right = RecuSelect ( $s, f, a, p$ )

candidate = left +  $[a_k]$  + right

if len (candidate) > len (best) = candidate

return best.

Subject \_\_\_\_\_

Month \_\_\_\_\_

Year \_\_\_\_\_

Date \_\_\_\_\_

### C. Bottom-Up Tabulation

for length  $l = 2$  to  $n+1$ :

for all pairs  $(i, j)$  with  $j \geq i$ :

$c[i][j] = \max_{0 \leq k < j} \{c[i][k] + c[k][j]\}$

$\in \{i-j\}$  of  $\{c[i][k] + c[k][j]\} + 1$

If no such  $k$ :  $c[i][j] = 0$

Answer =  $c[0][n]$

### Greedy approach

→ always pick the activity with

the earlier finish time that is

compatible with the last selected activity

GreedySchedule( $s, f, n$ )

→ sort activities by finish time  $f$

$A = \{a\}$

$last = 1$

for  $i = 2$  to  $n$ :

if  $s[i] > f[last]$ :

$A = A \cup \{a\}$

$last = i$

return  $A$

AN