

# Sensors of position, speed and vibration

AE3B38SME - Sensors and Measurement

# Sensors of position

## Classification



continuos

They measure the actual  
distance of the object

bistable

They detect if an object  
is closer than threshold

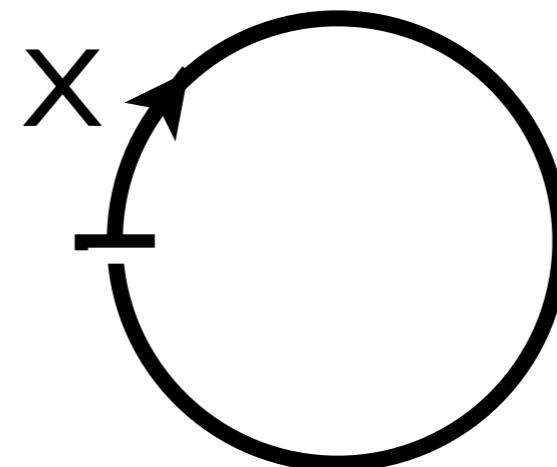
# Sensors of position

## Classification

linear



rotational



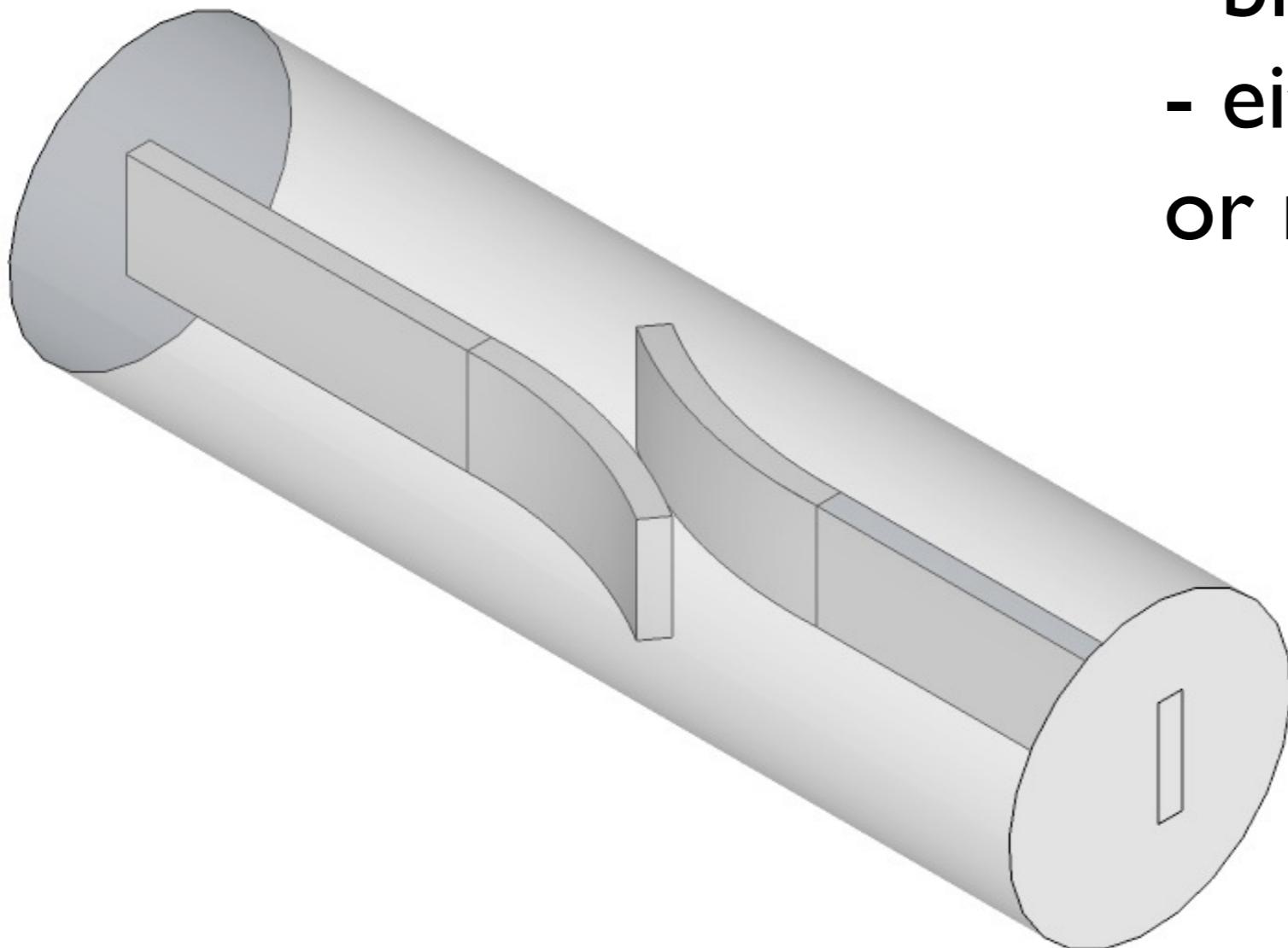
# Sensors of position

## Classification

### Physical principle

- resistance
- capacity
- optic
- ultrasound

# Reed contacts

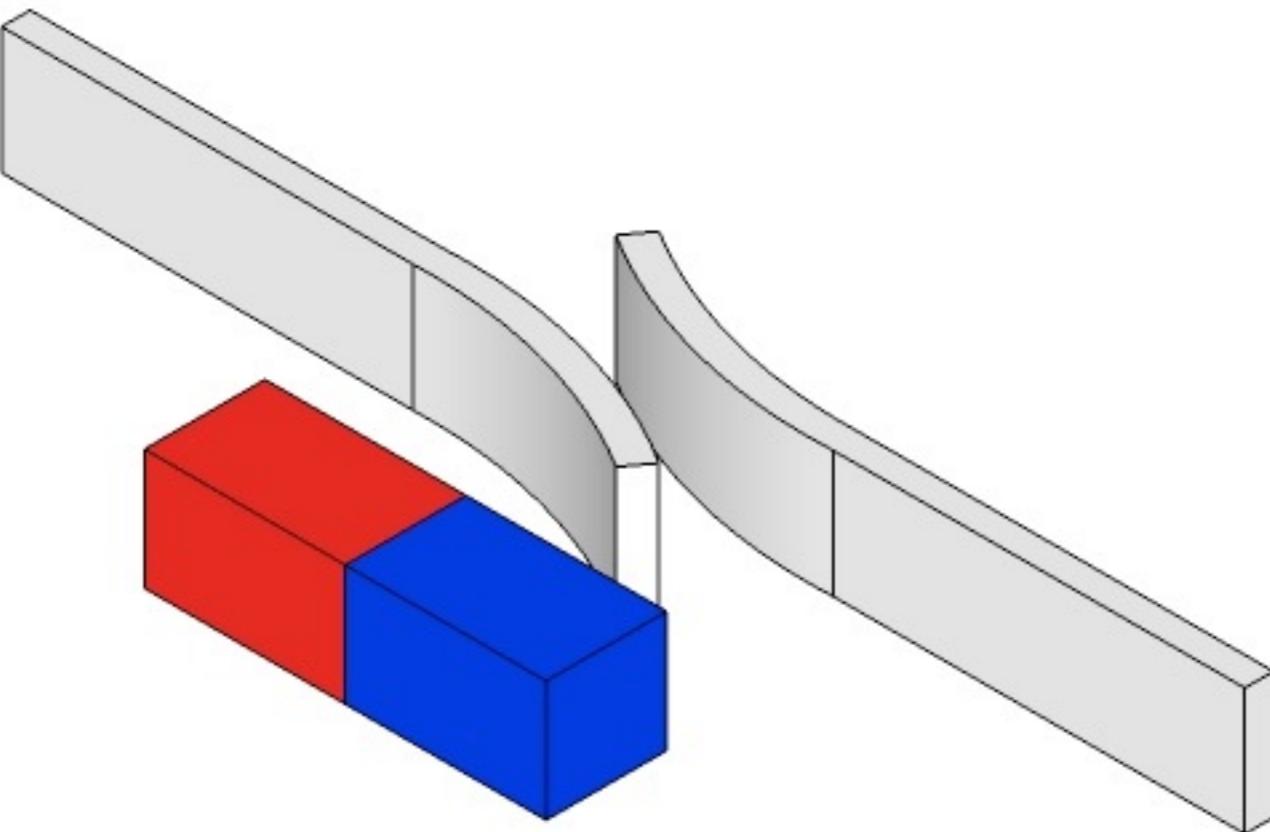


- bistable
- either normally close or normally open

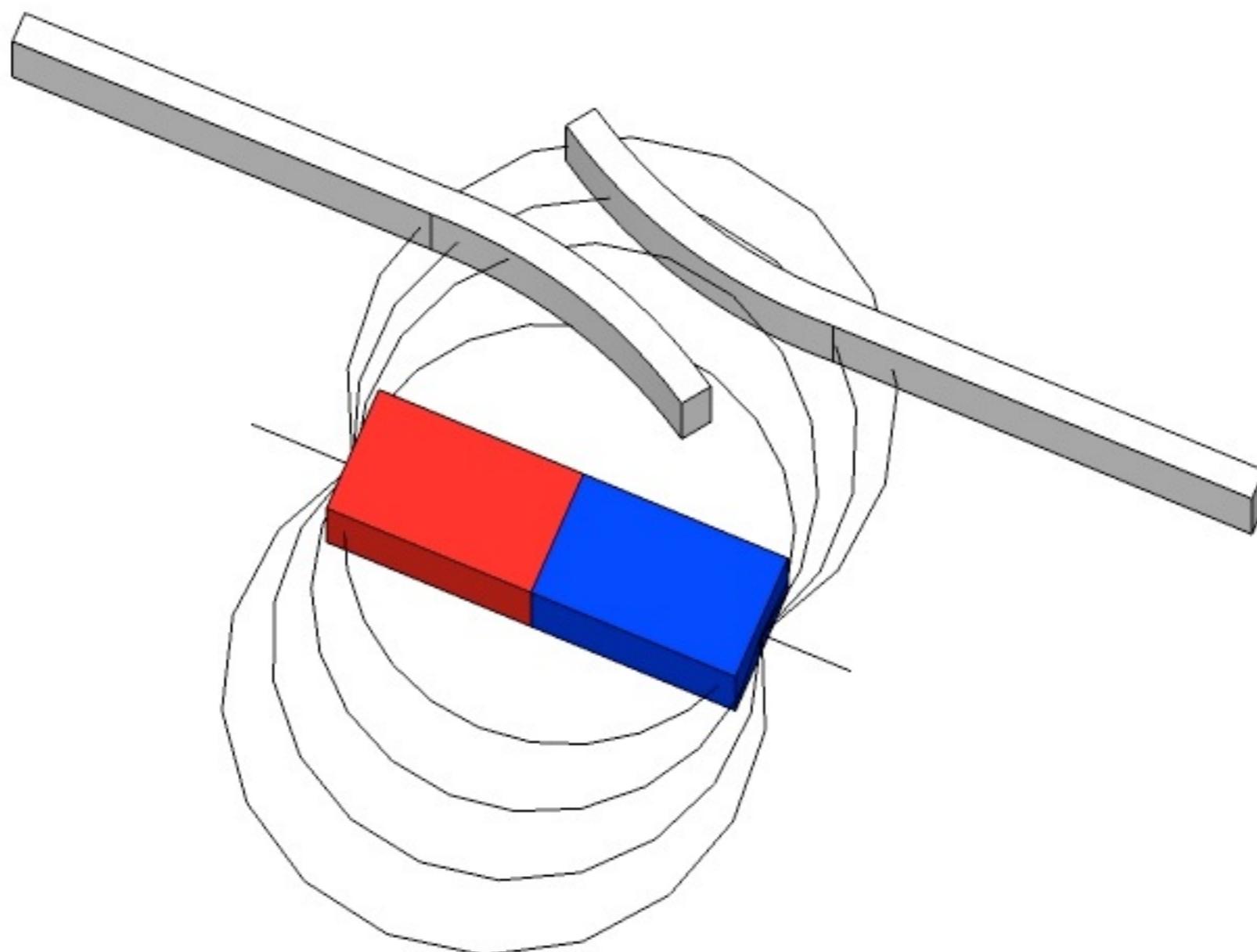


symbol

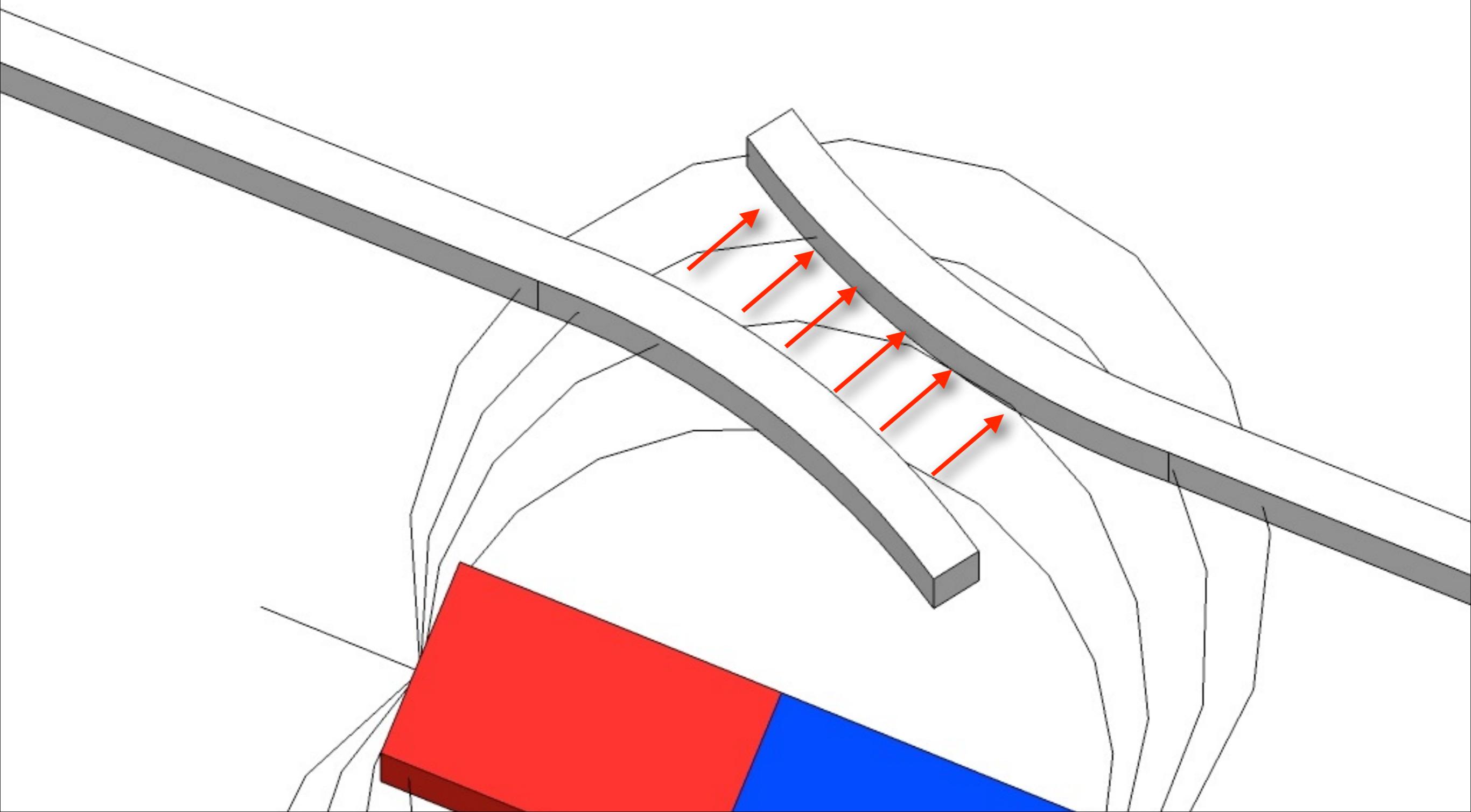
# Reed contacts



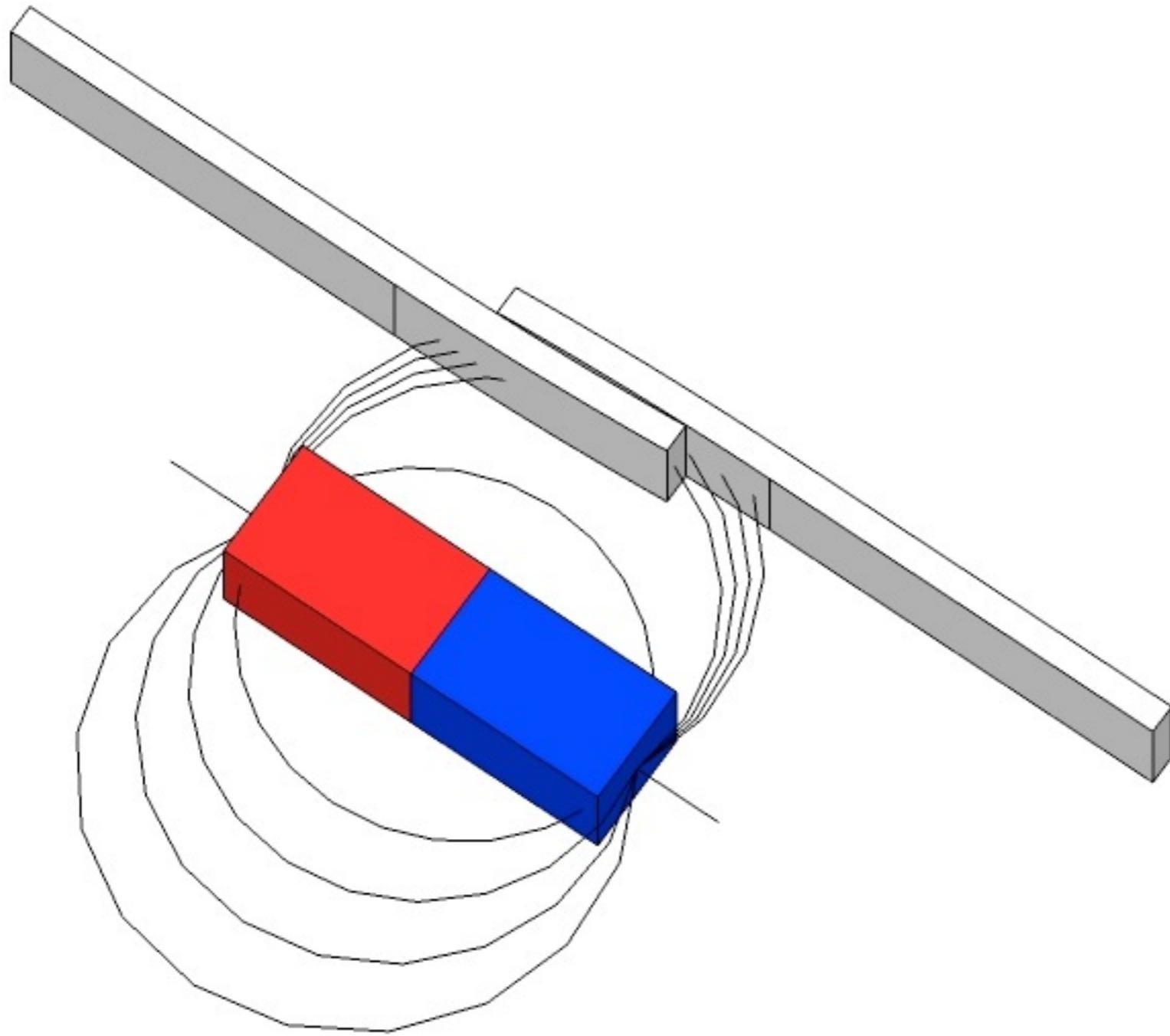
# Reed contacts



# Reed contacts



# Reed contacts



# Reed contacts

## - parameters-



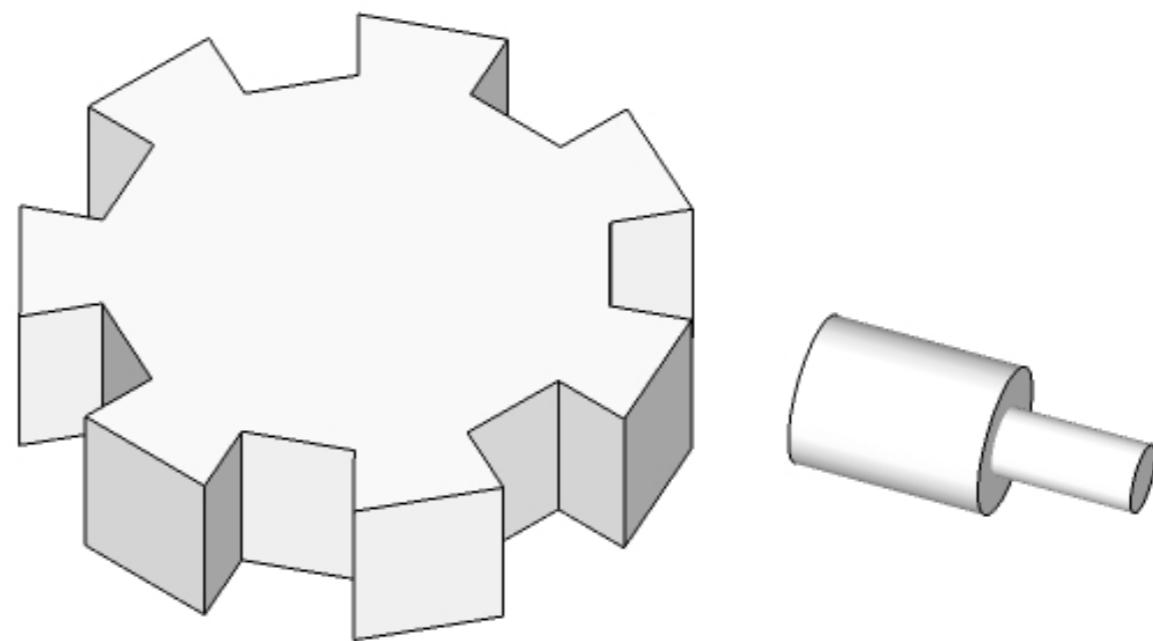
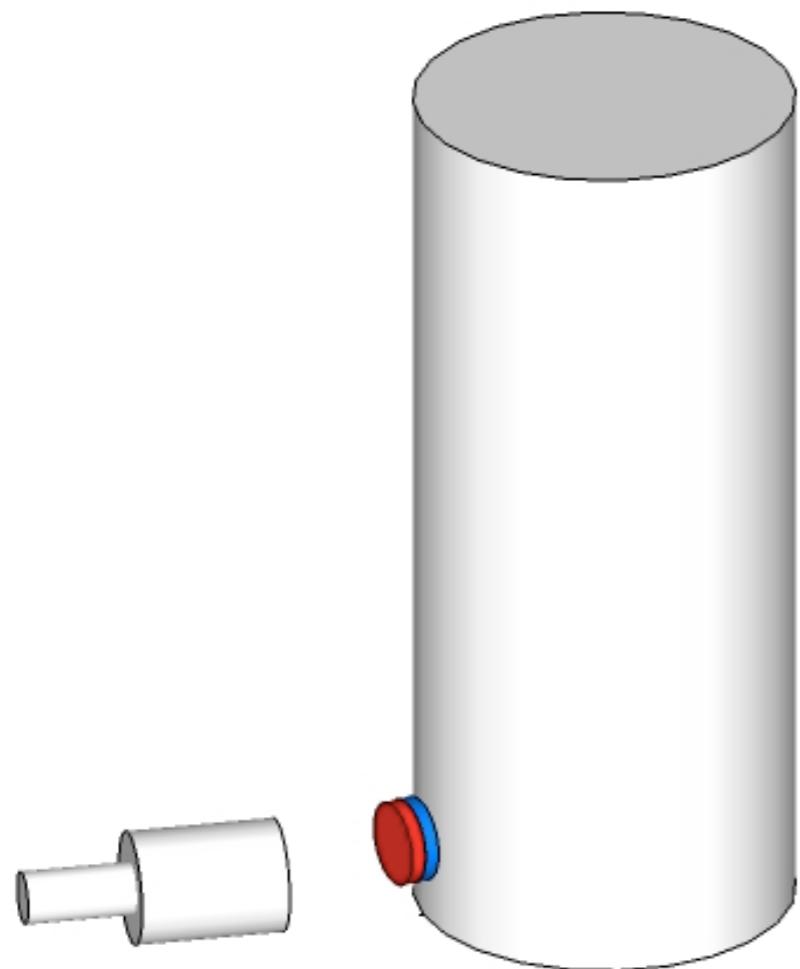
### RI-01B Series Dry Reed Switch

#### Technical Specifications

| Parameters                             | Test Conditions | Units | RI-01BAAA | RI-01BAA | RI-01BA |
|--|-----------------|-------|-----------|----------|---------|
| Operating Characteristics              |                 |       |           |          |         |
| Operate Range                          | AT              | AT    | 6-16      | 14-23    | 18-32   |
| Release Range                          | AT              | AT    | 3-15.5    | 4-21     | 5-27    |
| Operate Time - including Bounce (typ.) |                 | ms    | 0.1       | 0.25     | 0.25    |
| Bounce Time (typ.)                     |                 | ms    | 0.05      | 0.15     | 0.15    |
| Release Time (max)                     |                 | µs    | 70        | 30       | 30      |
| Resonant Frequency (typ.)              |                 | Hz    | 5500      | 5500     | 5500    |
| Electrical Characteristics             |                 |       |           |          |         |
| Switched Power (max)                   |                 | W     | 5         | 10       | 10      |
| Switched Voltage DC (max)              |                 | V     | 160       | 200      | 200     |
| Switched Voltage AC, RMS value (max)   |                 | V     | 110       | 140      | 140     |
| Switched Current DC (max)              |                 | mA    | 250       | 500      | 500     |
|  |                 | mA    | 250       | 500      | 500     |

# Magnetic sensors

They are used to measure the magnetic field generated by a magnet or a ferromagnetic component

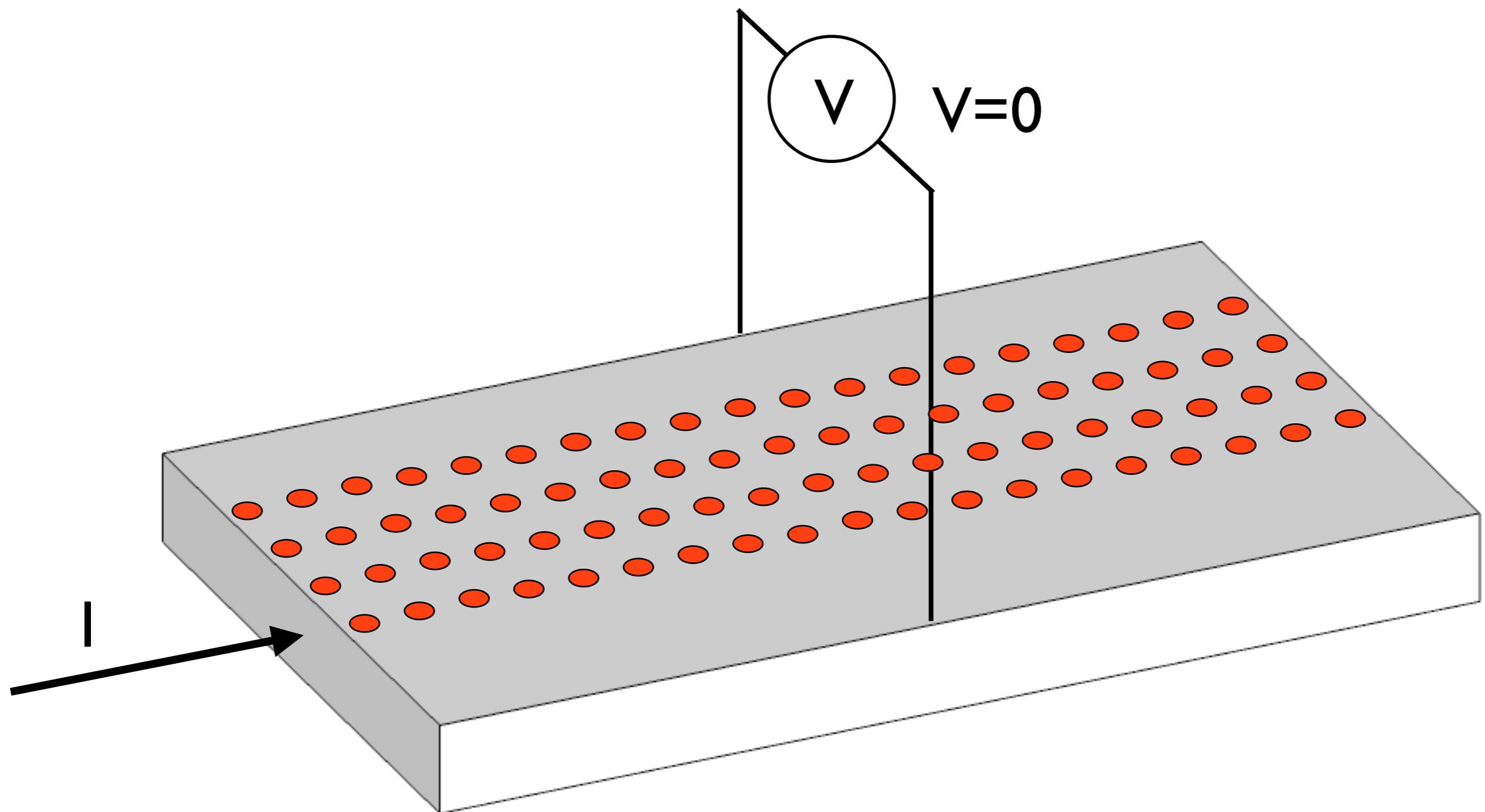


Hall effect

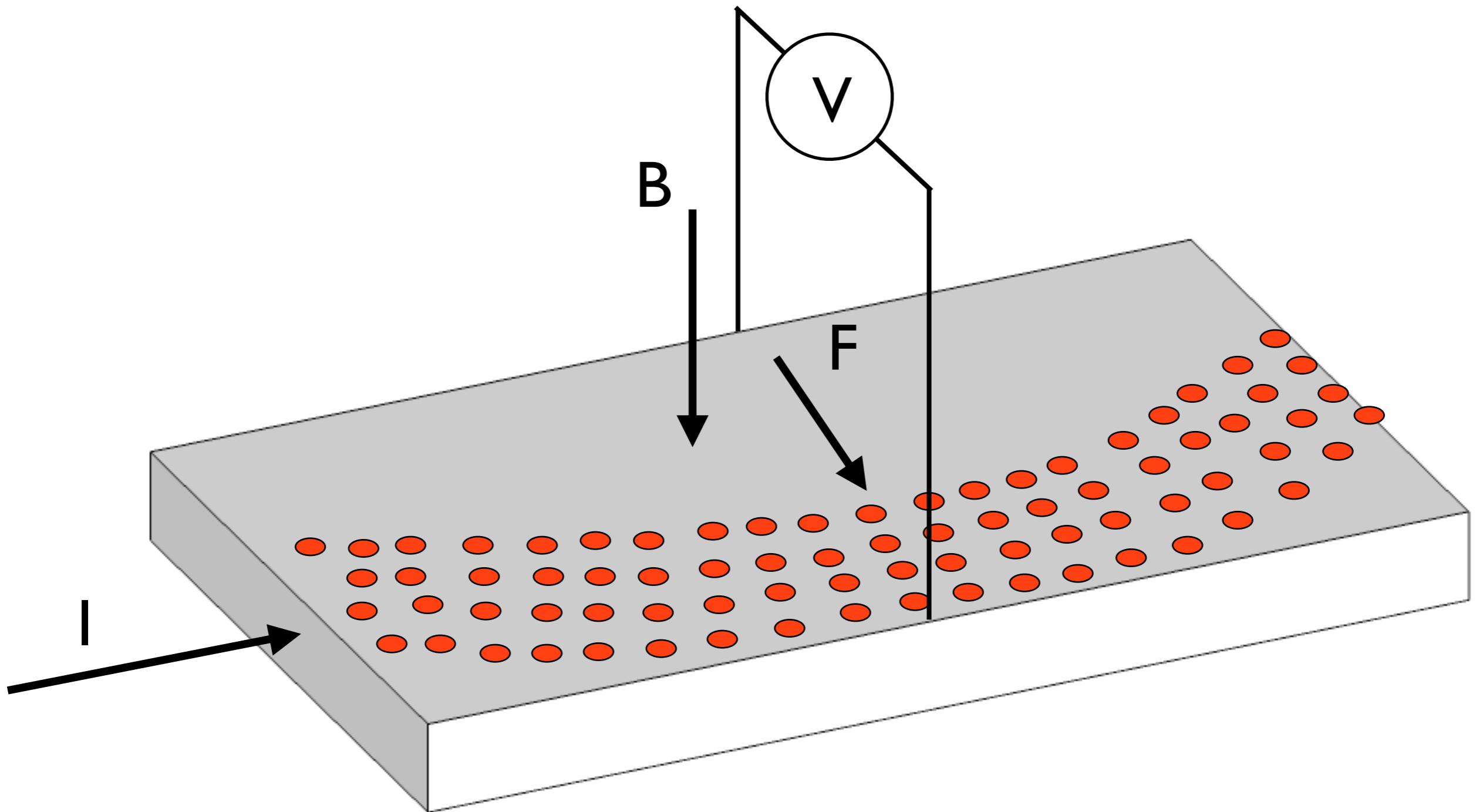
AMR

GMR

# Hall effect sensor

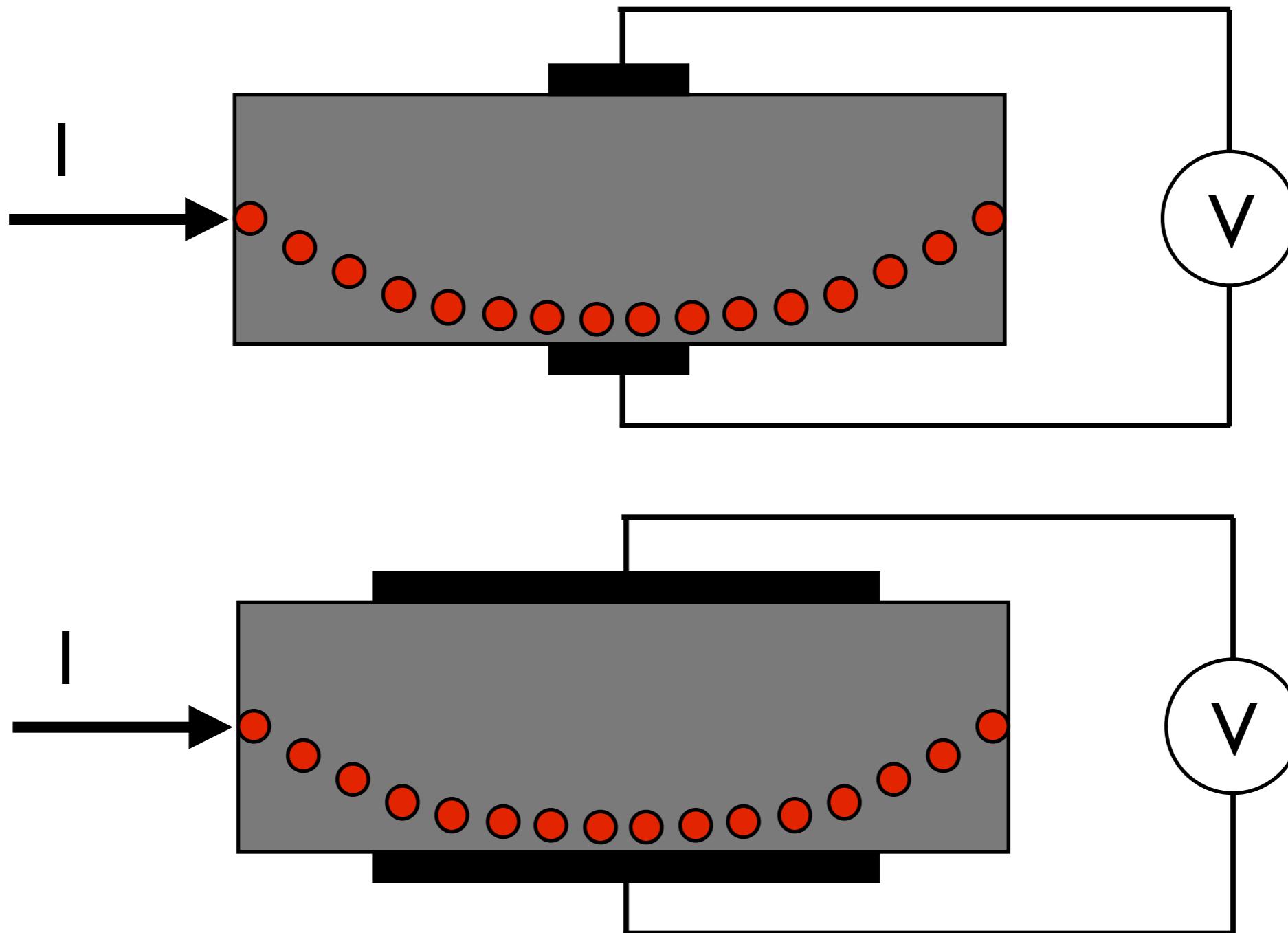


# Hall effect sensor

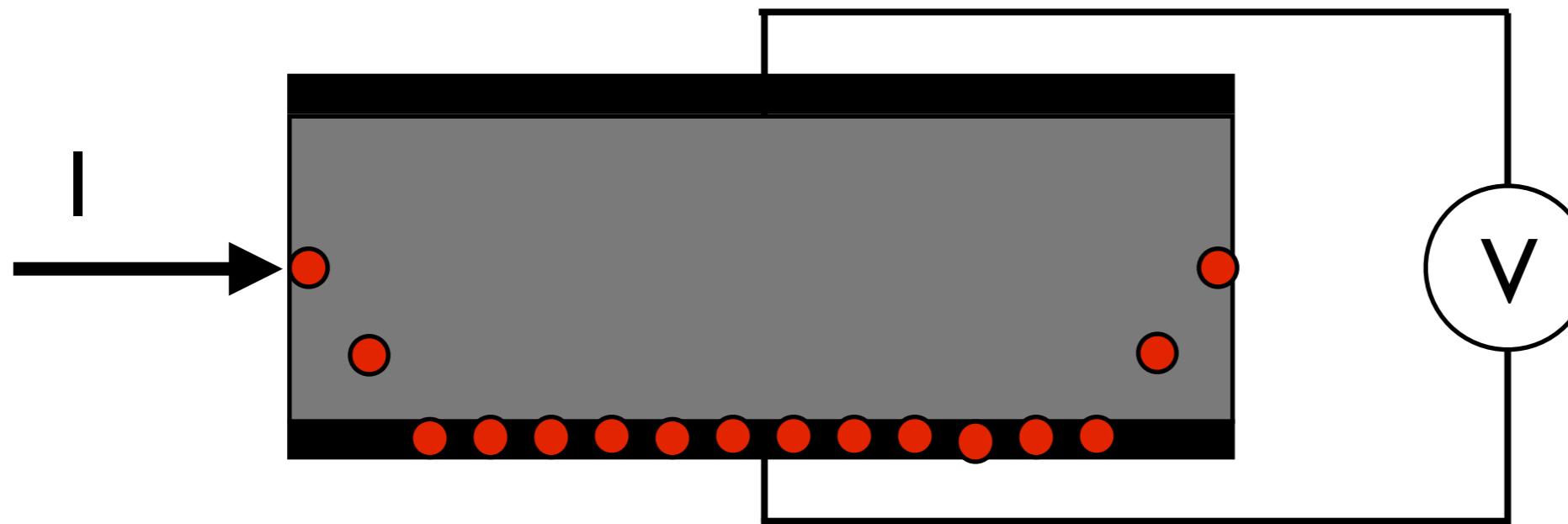


$$V = k \cdot F = k \cdot I \cdot B$$

# Problem 1. How can I pick up the voltage?

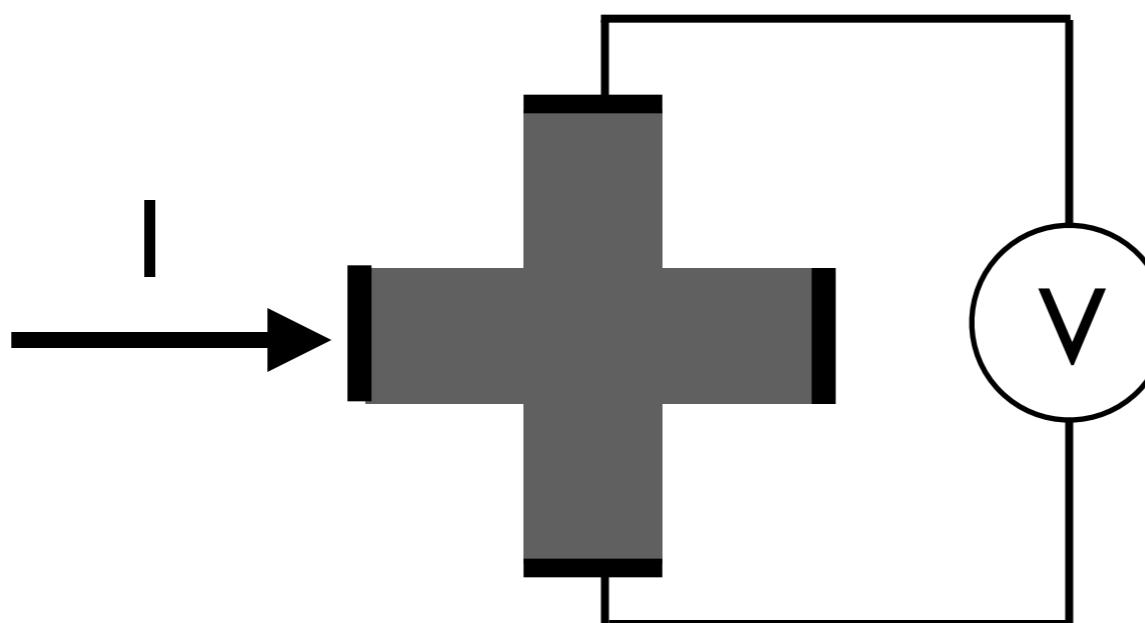
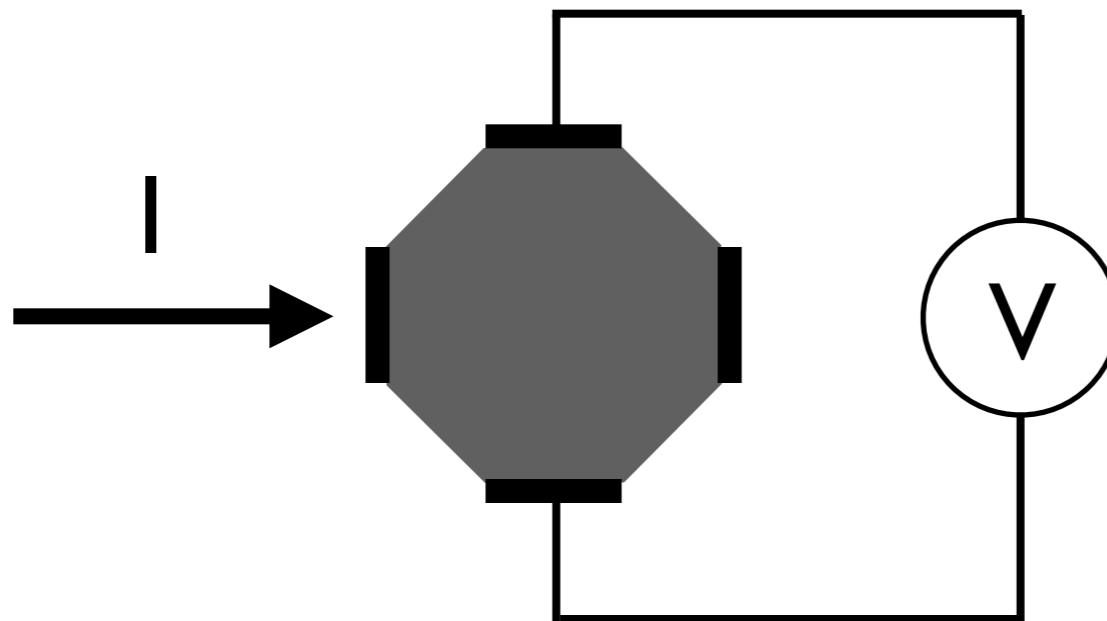


I would like to have the contacts as large as possible

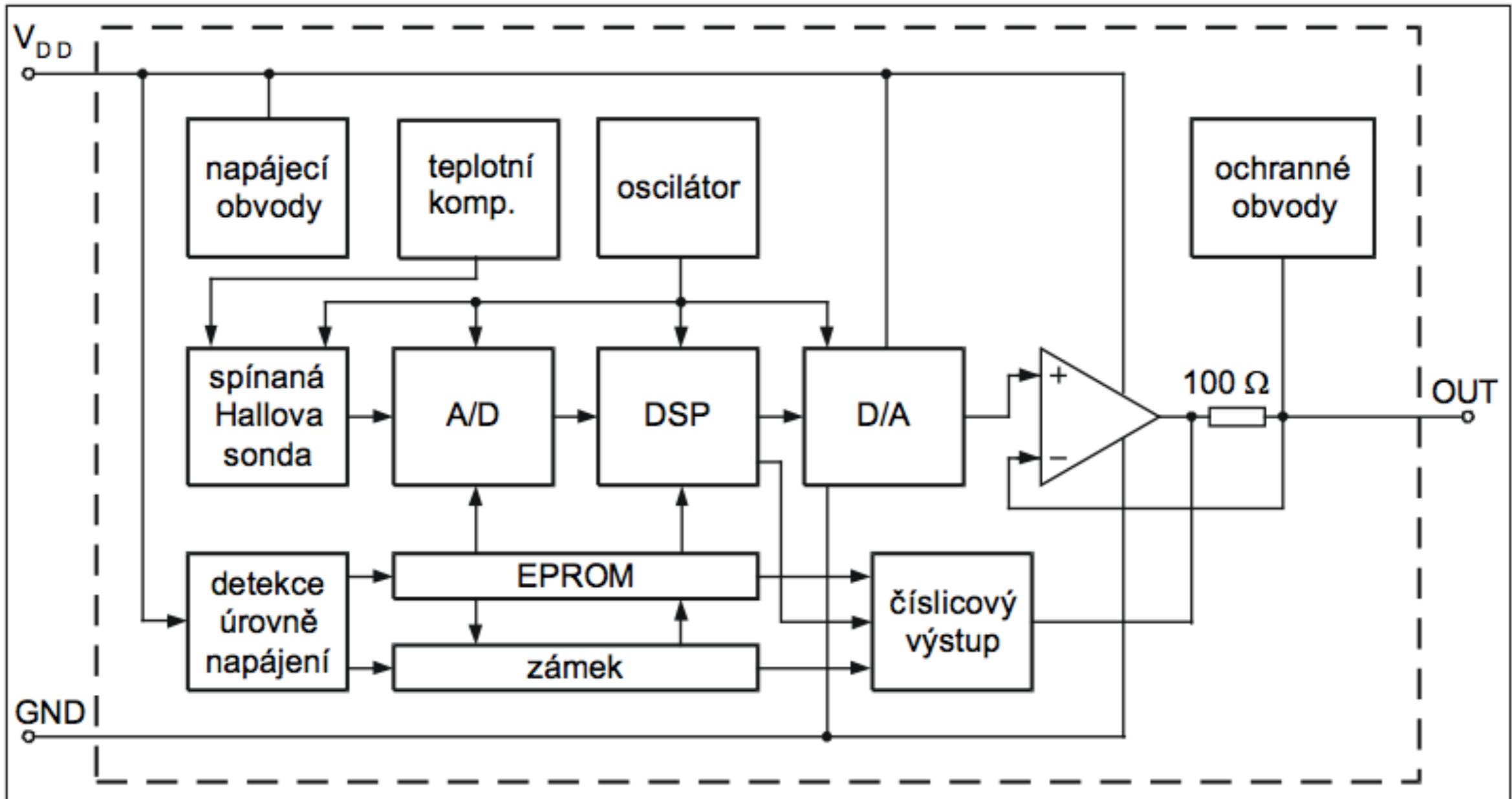


but if the contacts are too large  
they short circuit the current

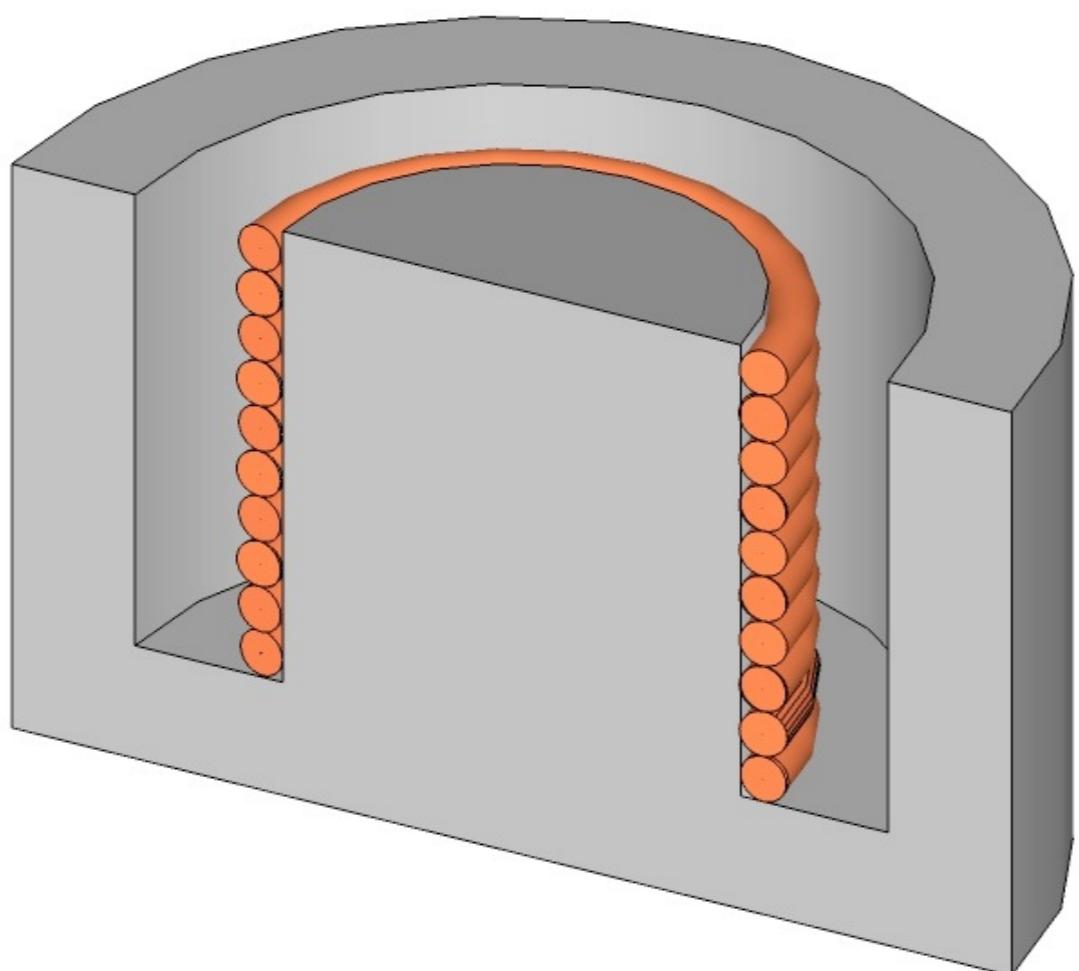
# Several shapes provide a compromise



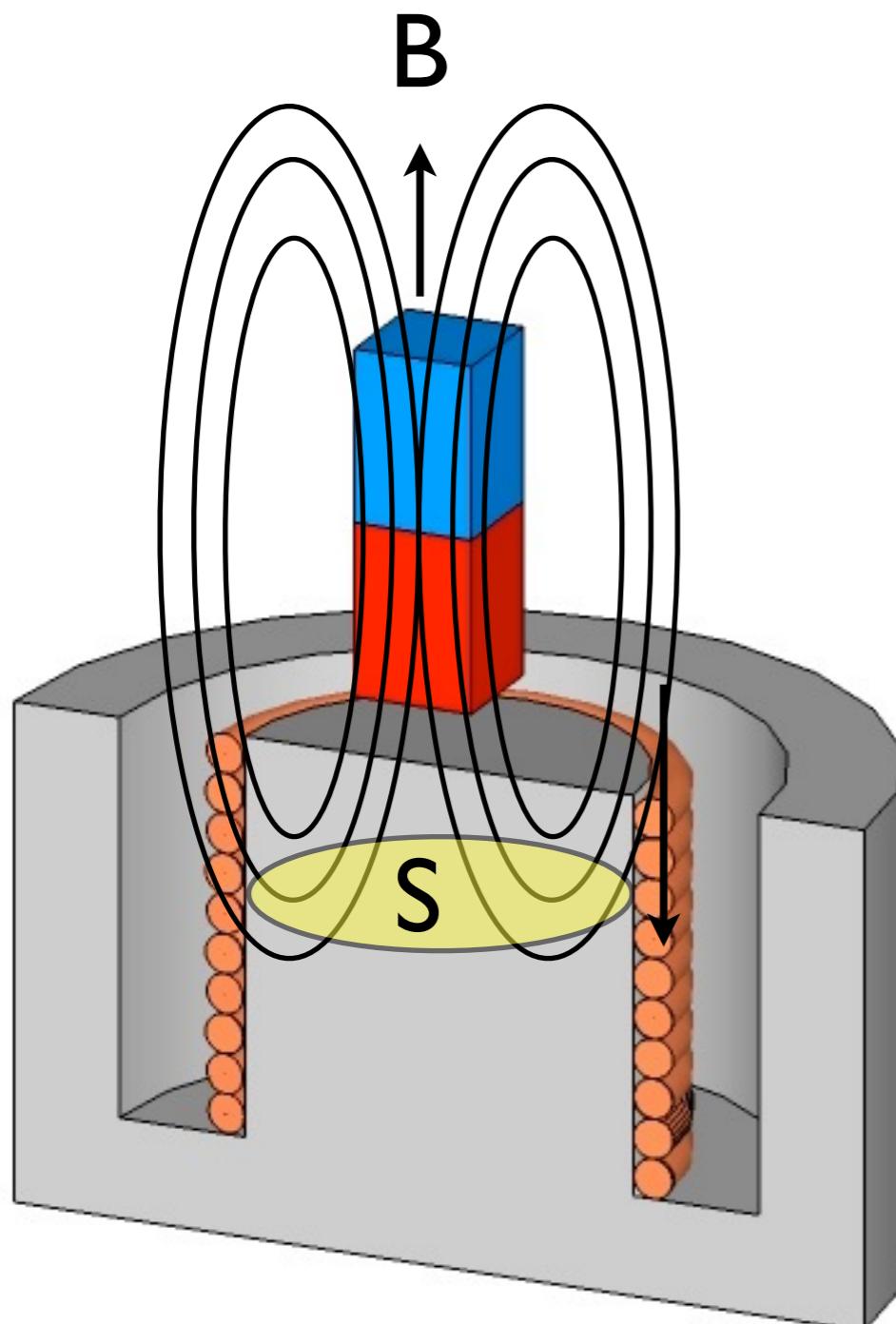
# Intelligent Hall effect sensor



# Induction coil



## Induction coil



$$v = - \frac{d\phi}{dt}$$

Based on Faraday's induction law

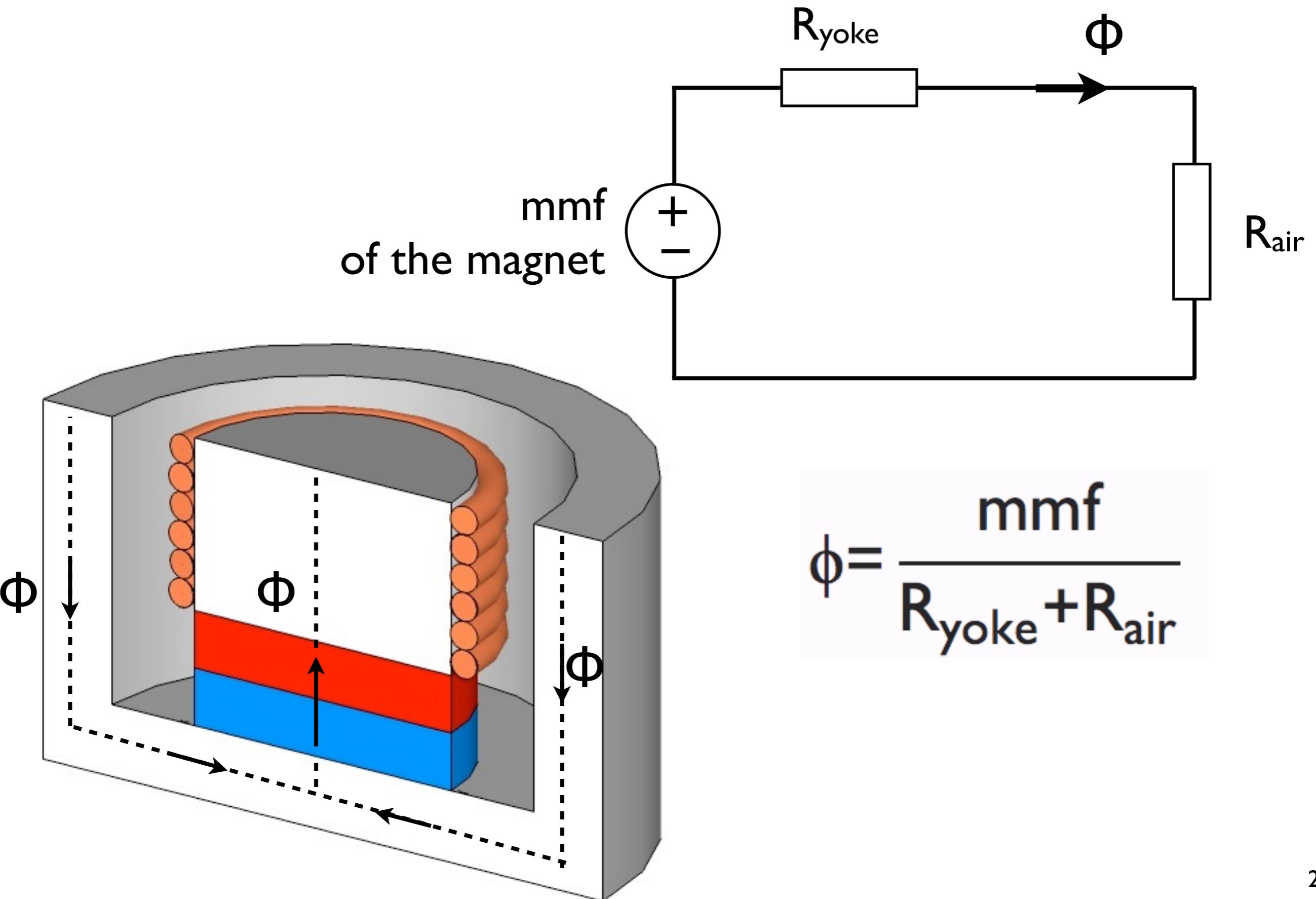
The amplitude of the pulse depends on the speed of the magnet

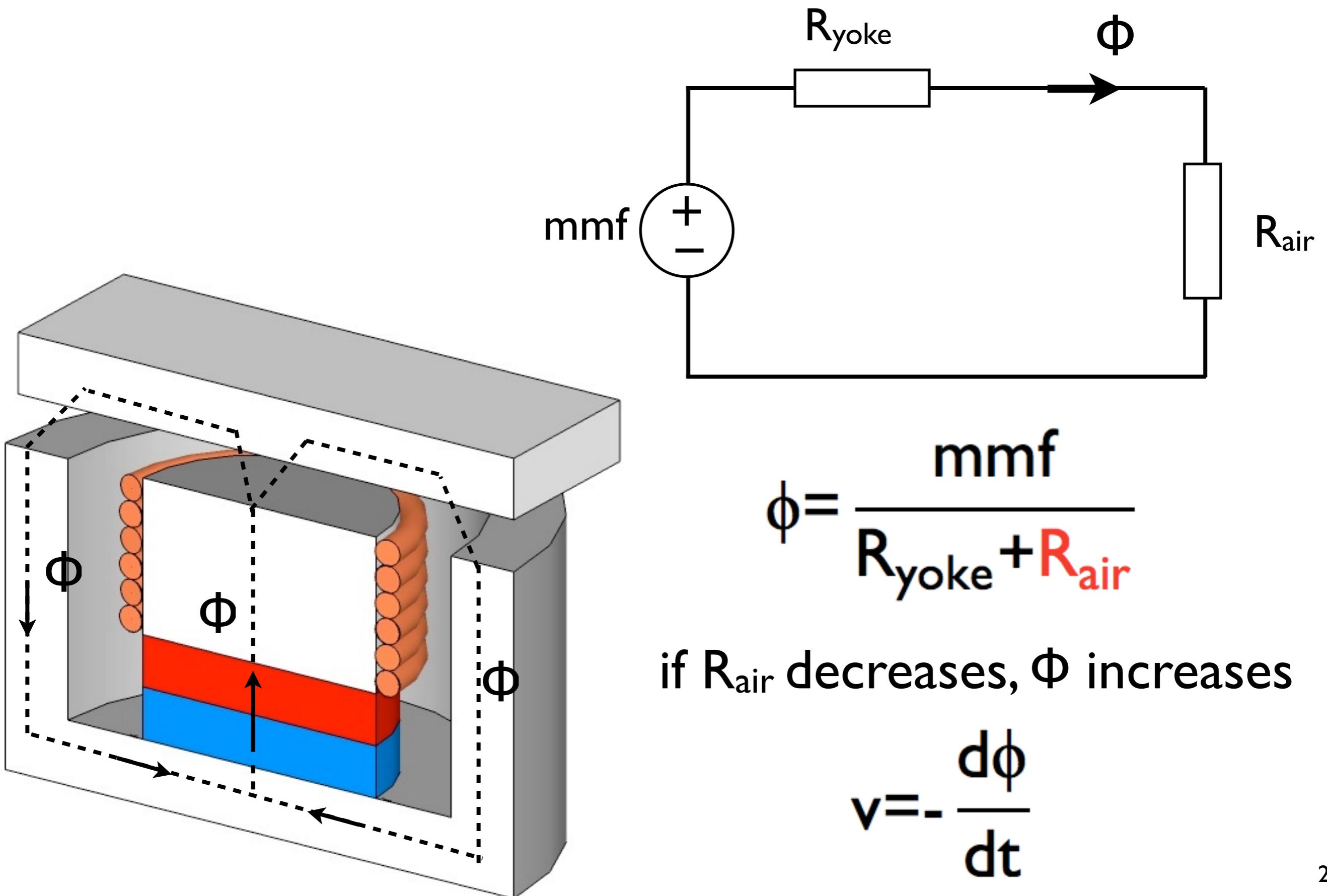
At low speed the signal is too low

$\Phi$  = magnetic flux

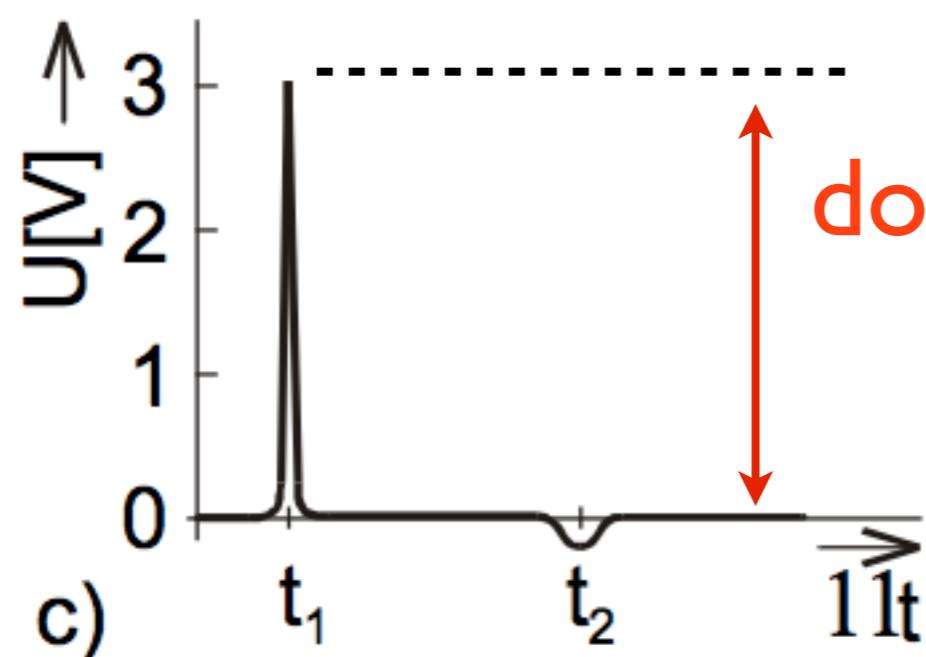
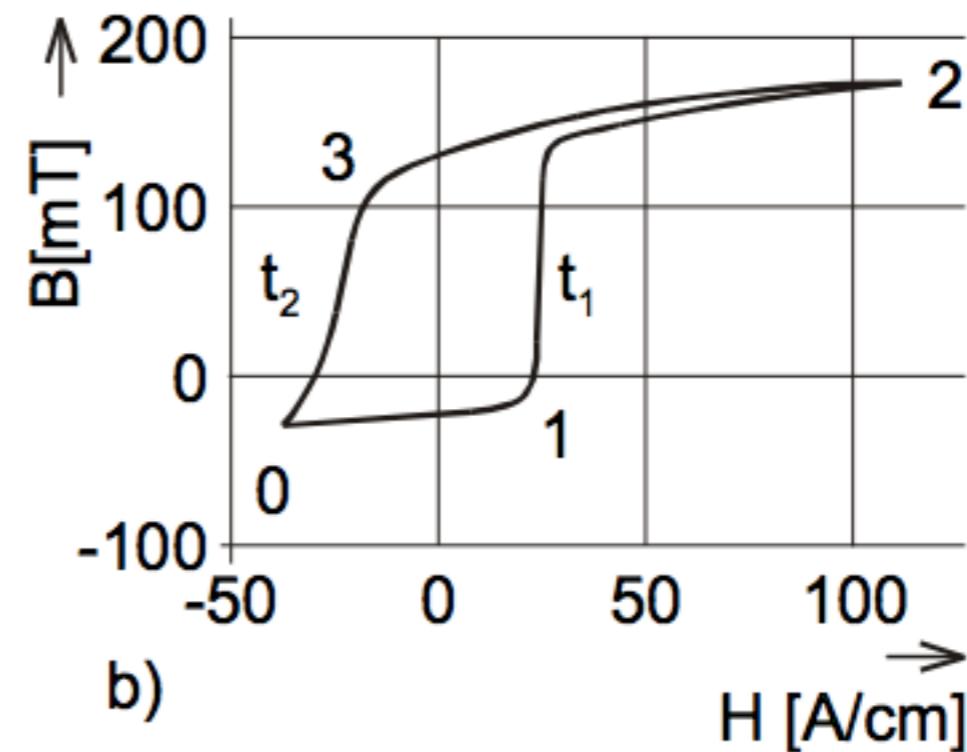
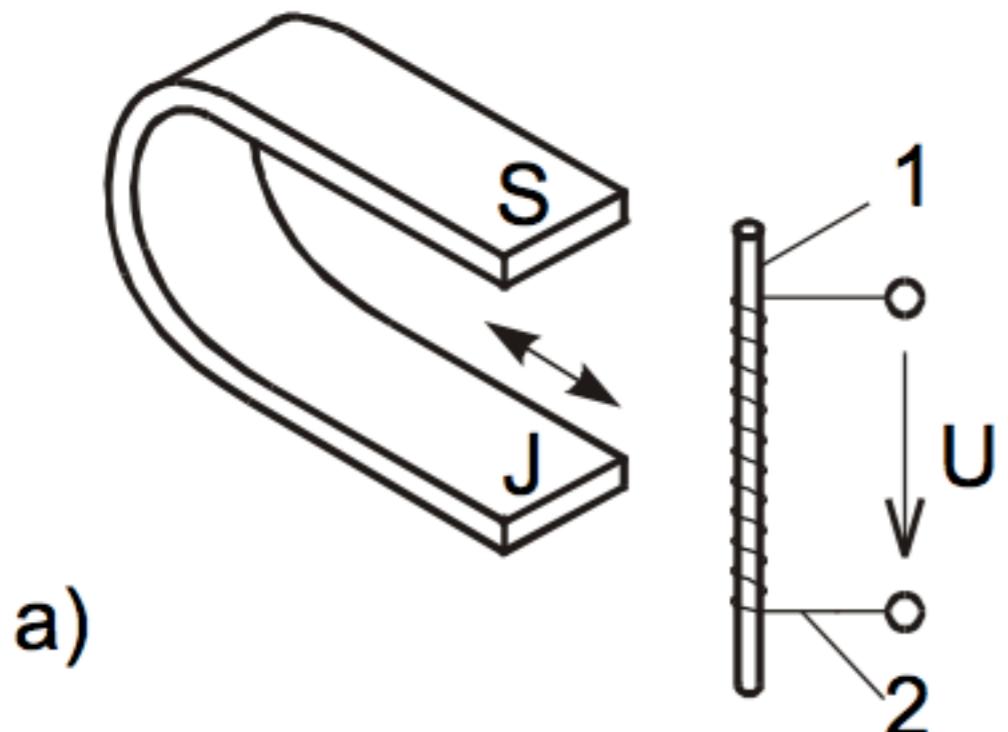
$$\Phi = \int_S \bar{B} \cdot \bar{n} \, ds$$

An alternative: the magnet is placed inside.





# Wiegand's wire

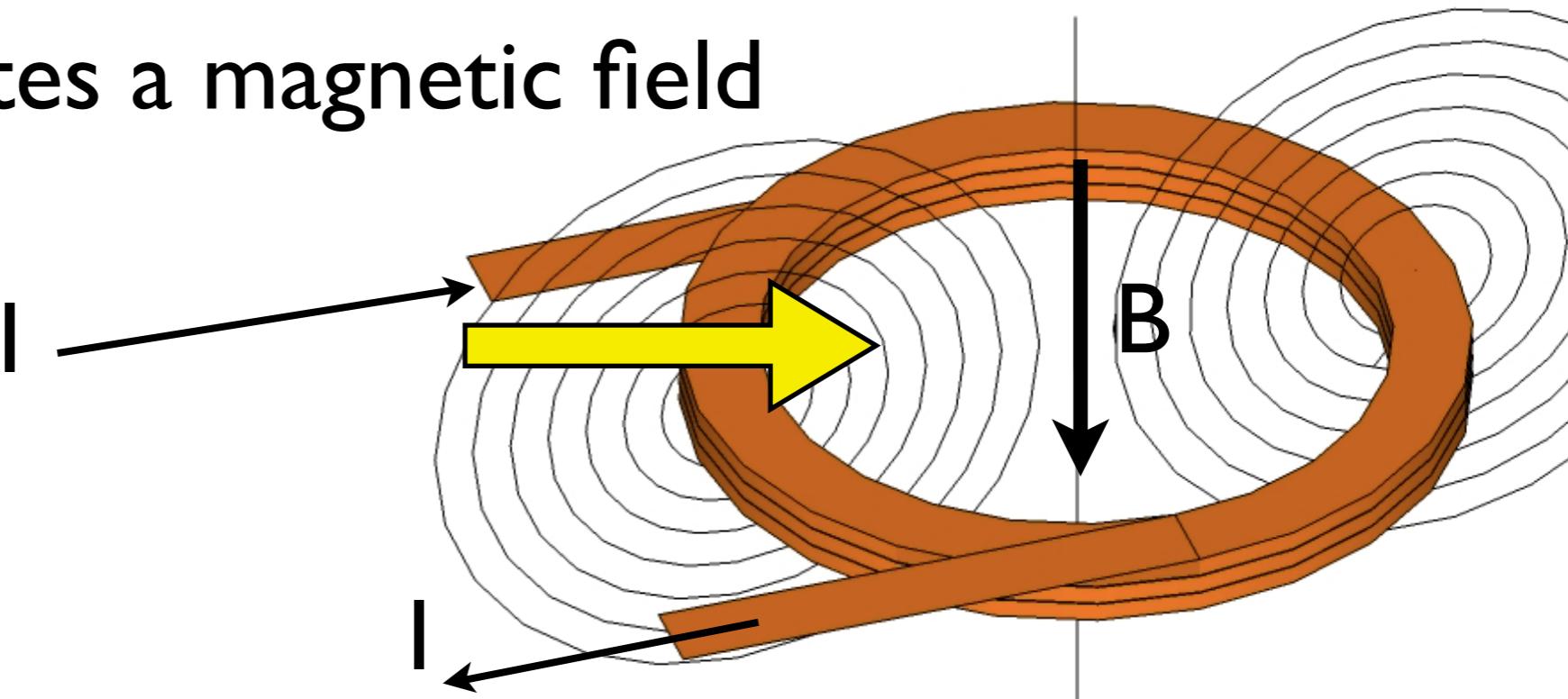


does not depend on the  
velocity  $H$  changes

# Eddy current sensors

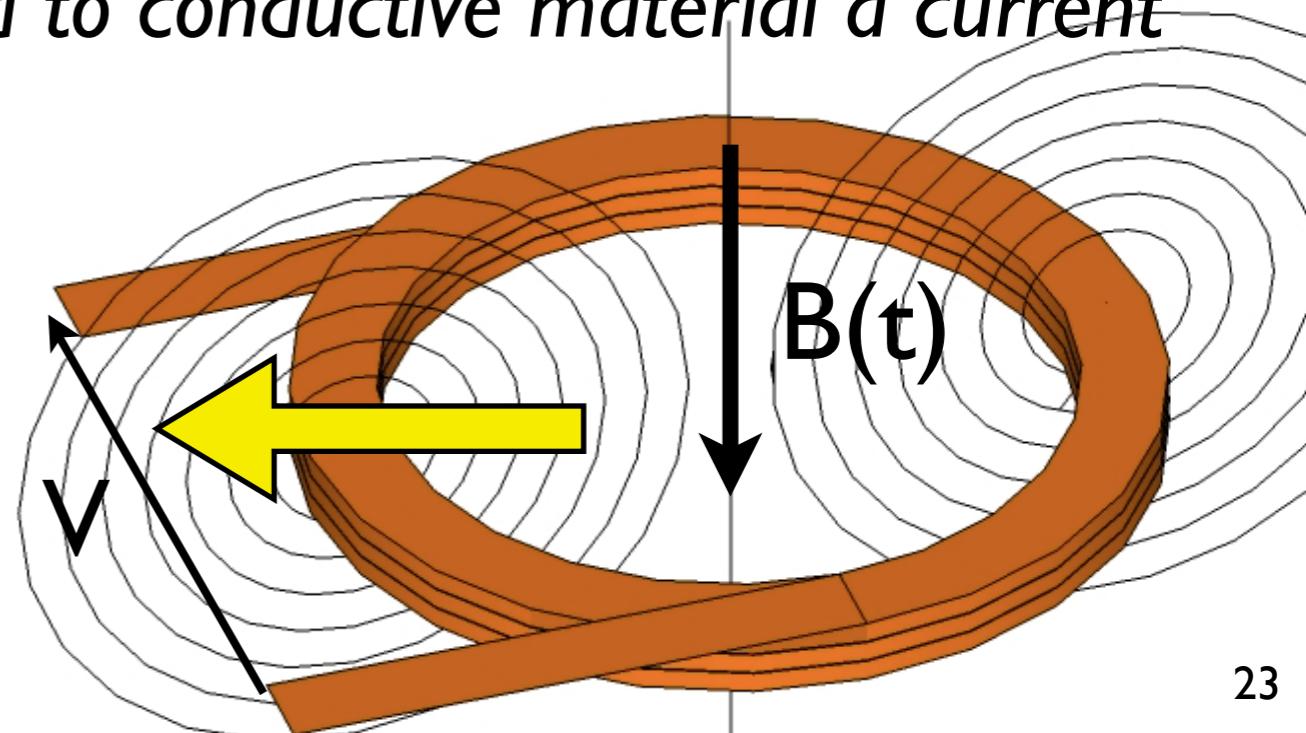
Two principles:

I) A current generates a magnetic field

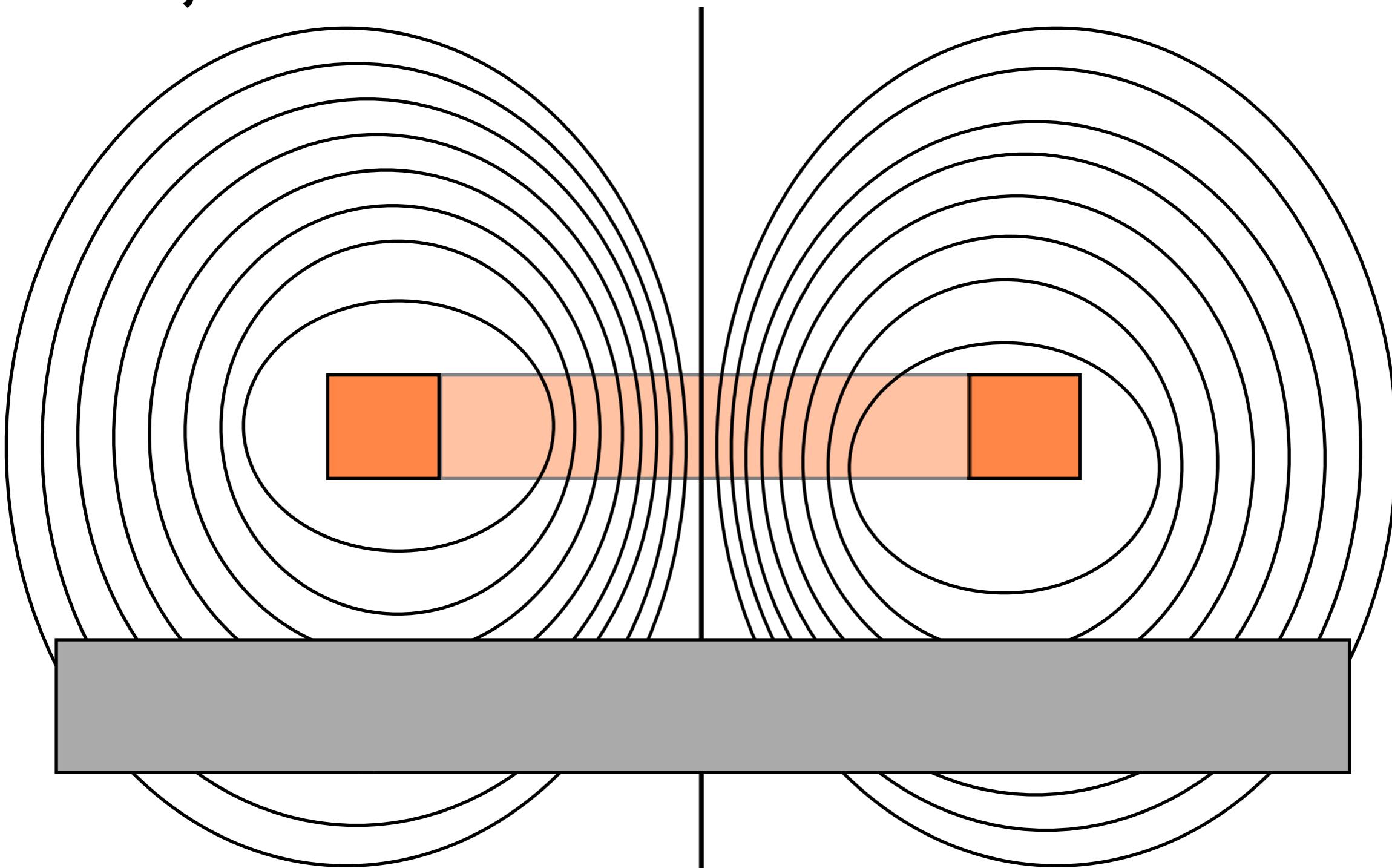


2) A time-varying magnetic field induces a voltage.

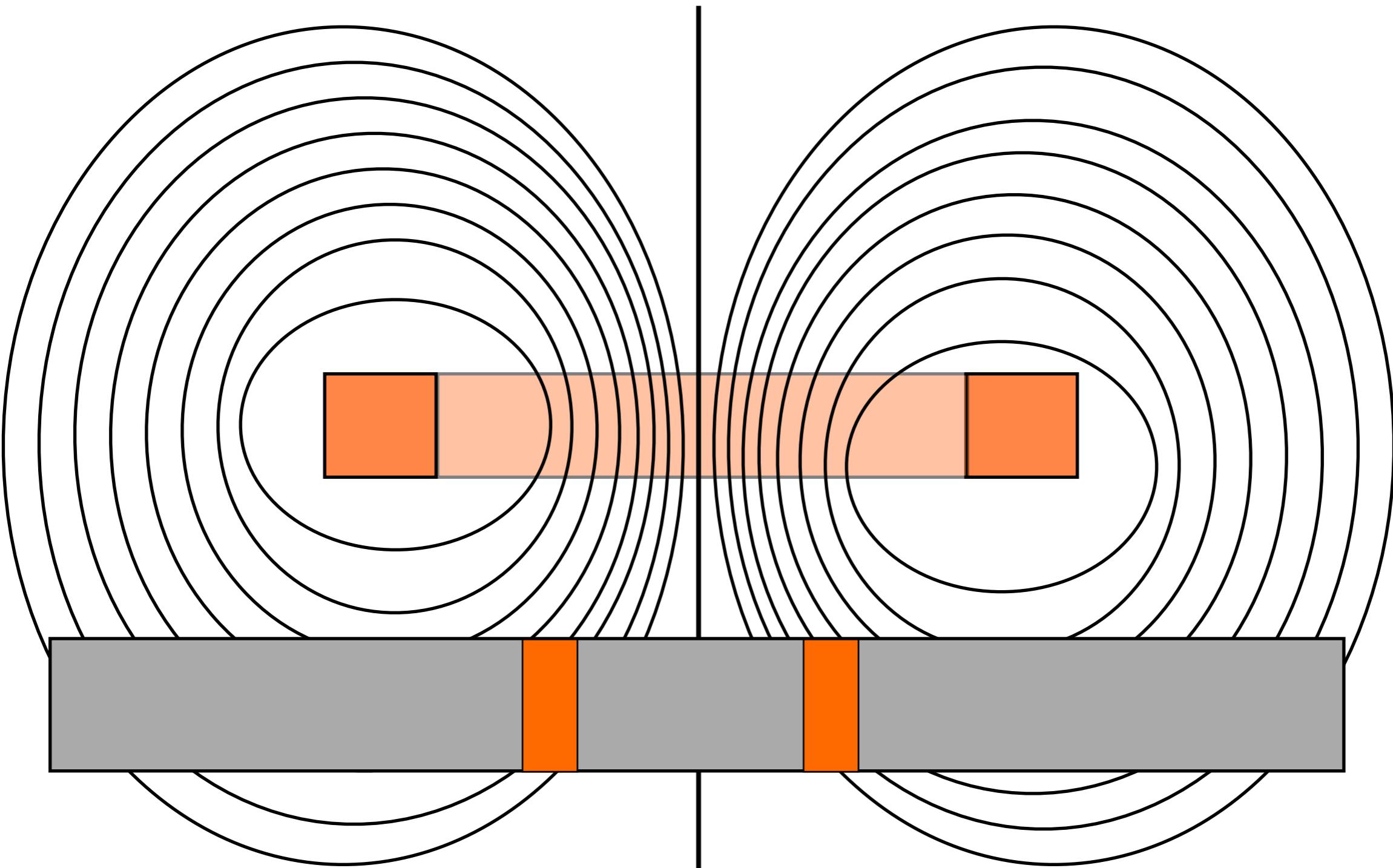
[and, of course, if the voltage is applied to conductive material a current is generated]



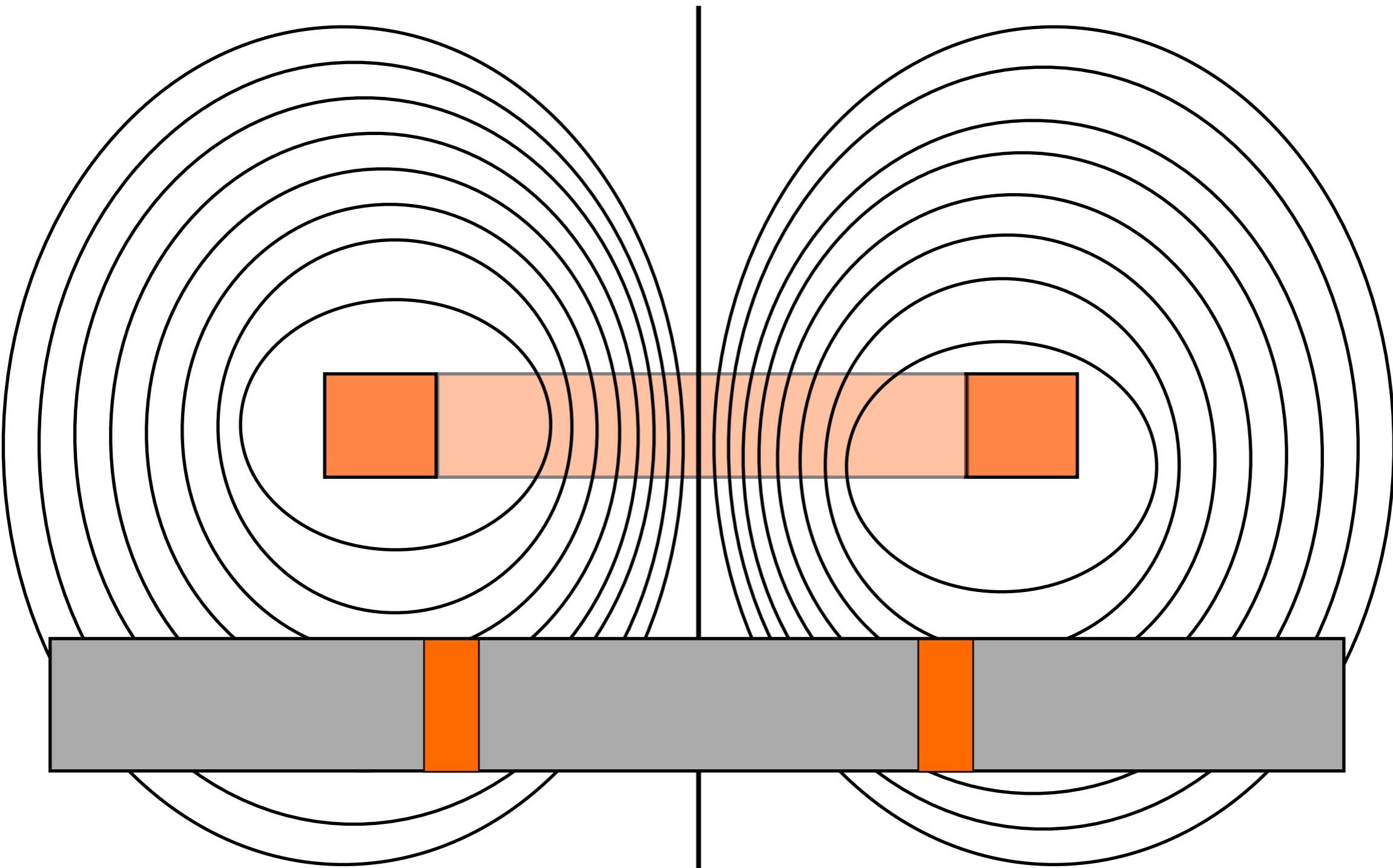
First of all I use a coil to generate a magnetic field above a metal object



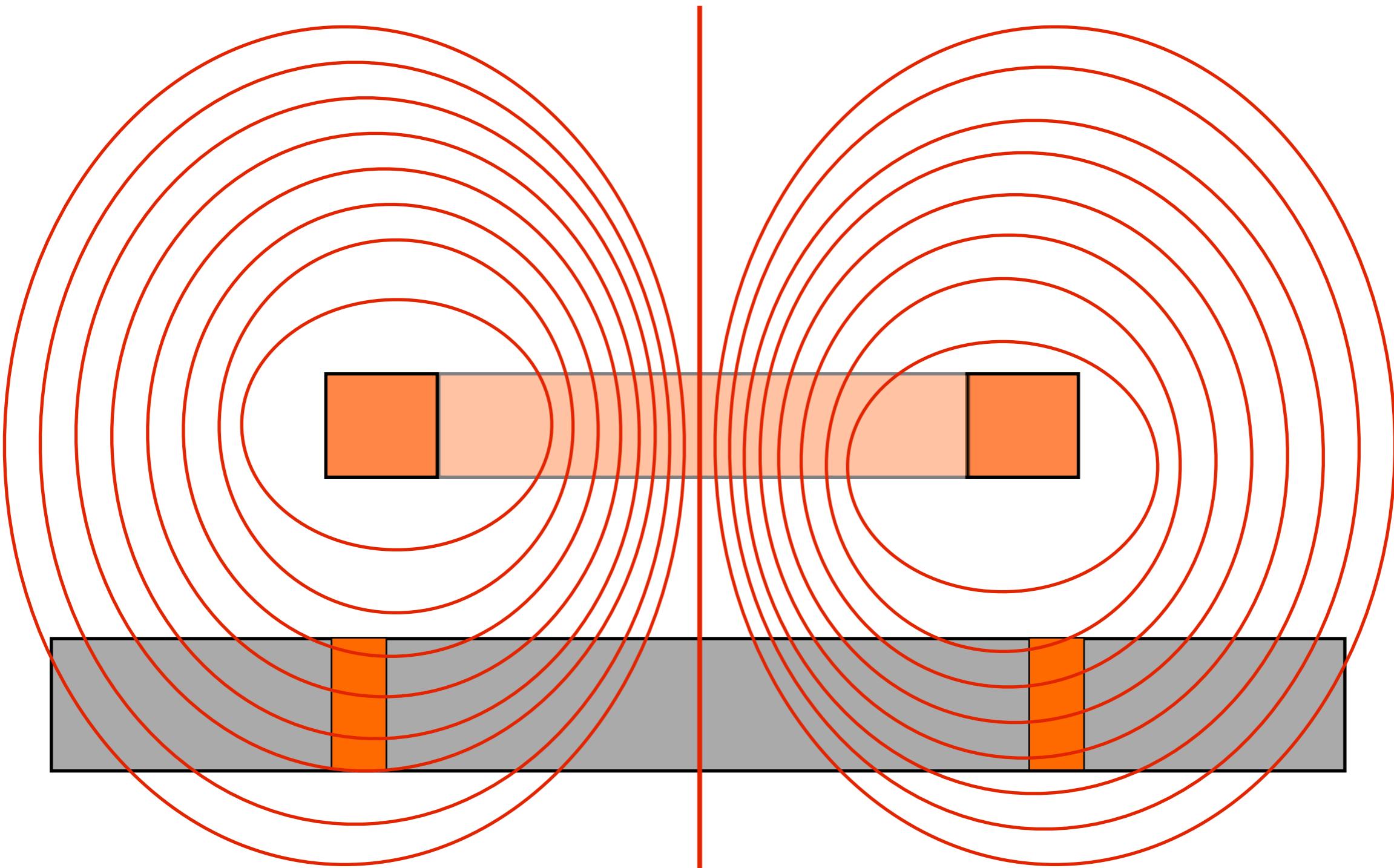
The metal can be seen as a union of several coils



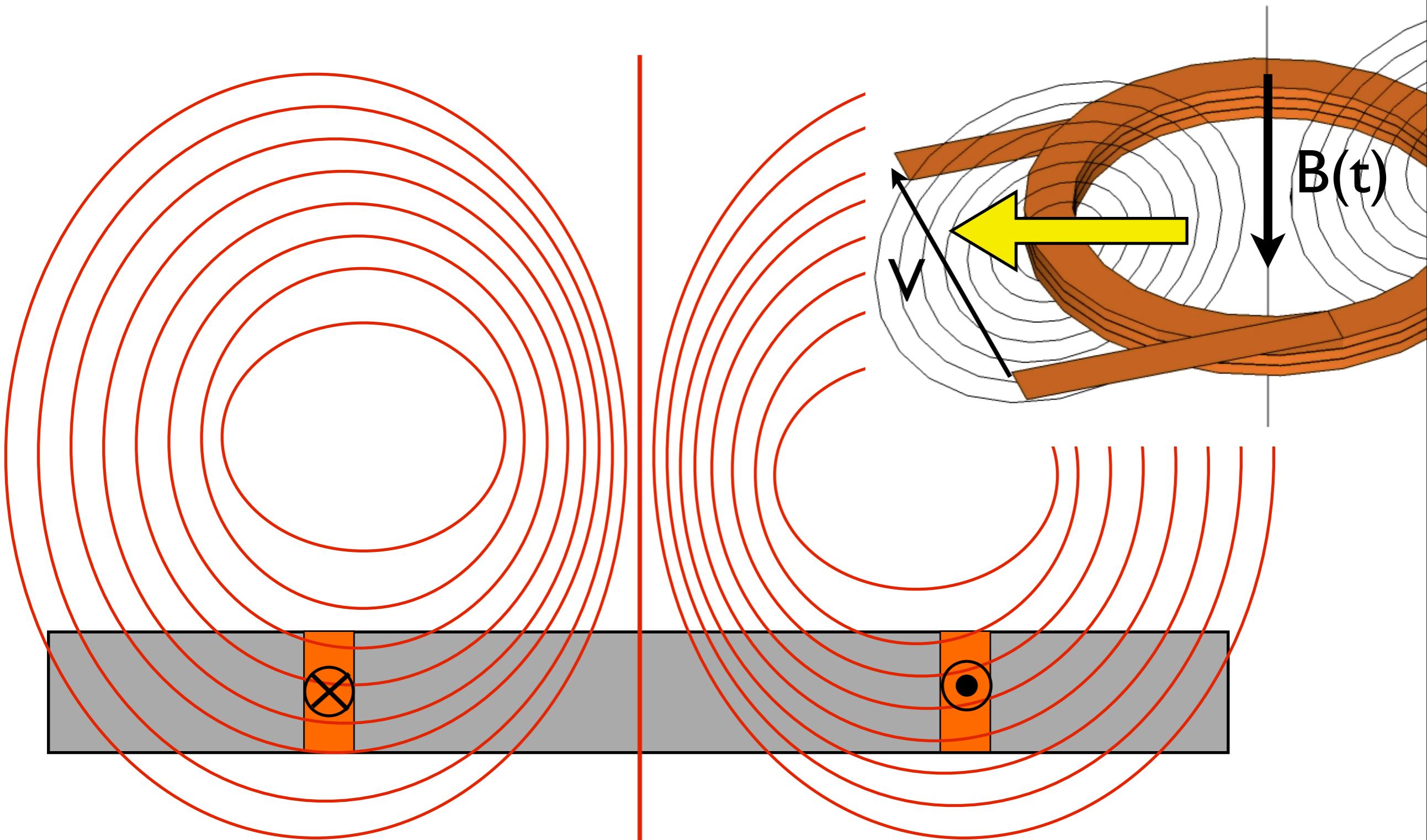
The metal can be seen as a union of several coils



In any these coils there is a time-varying magnetic field



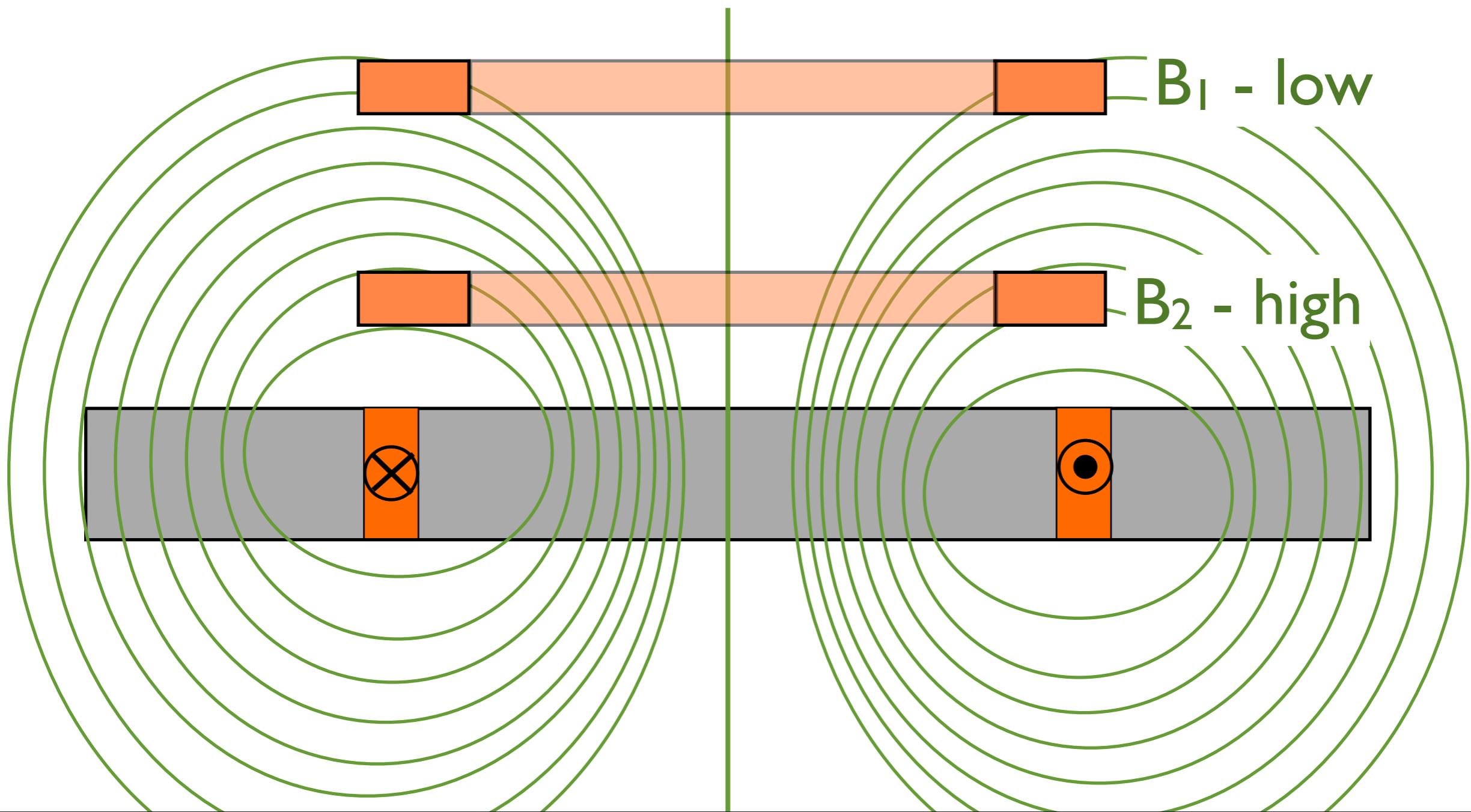
In any these coils there is a time-varying magnetic field



Therefore a voltage is generated, and since the material is conductive a current flows (eddy current)

The eddy currents generate also a magnetic field which is as low as the distance from the metallic object decreases.

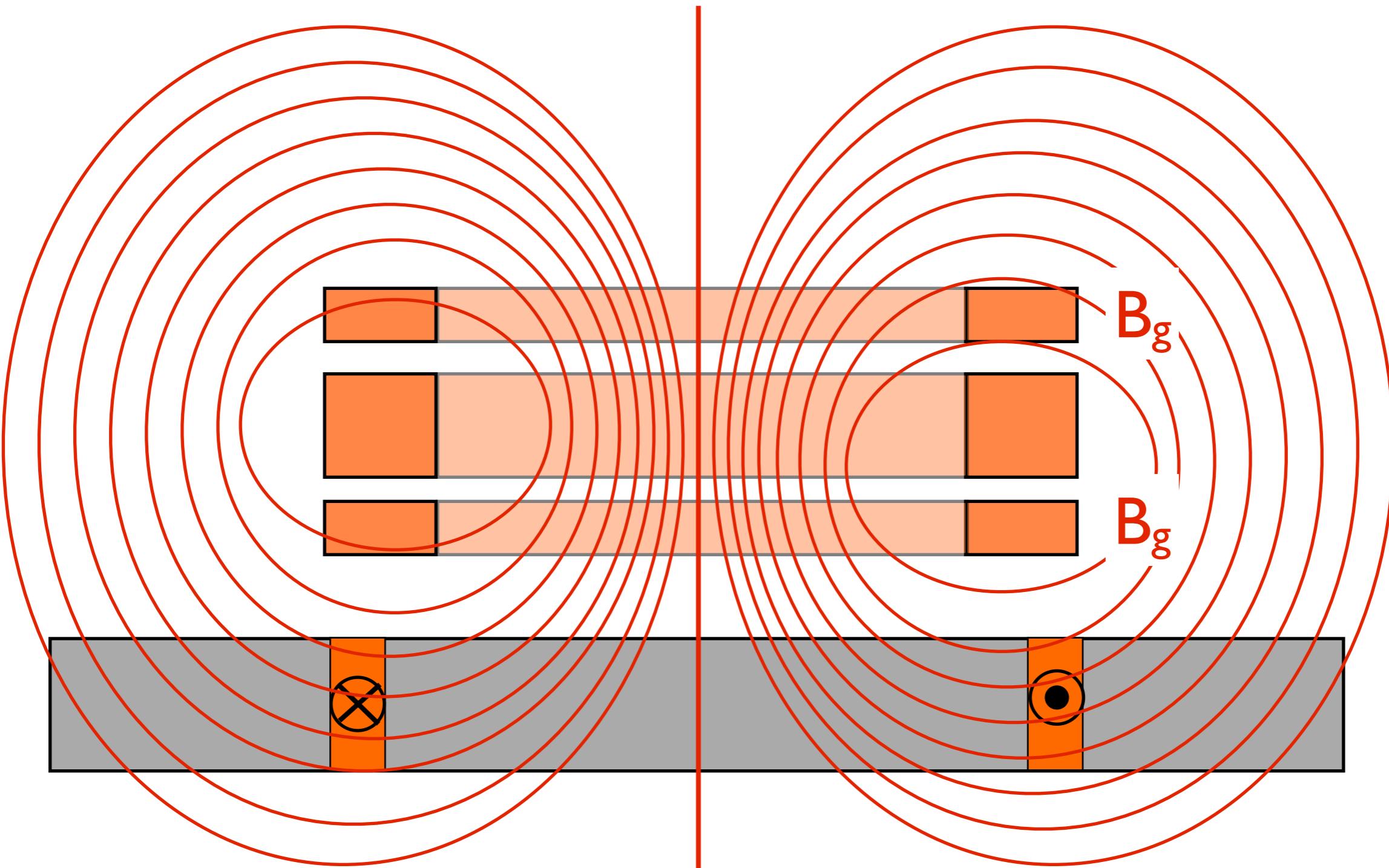
I use two coils to detect it, place at different distance



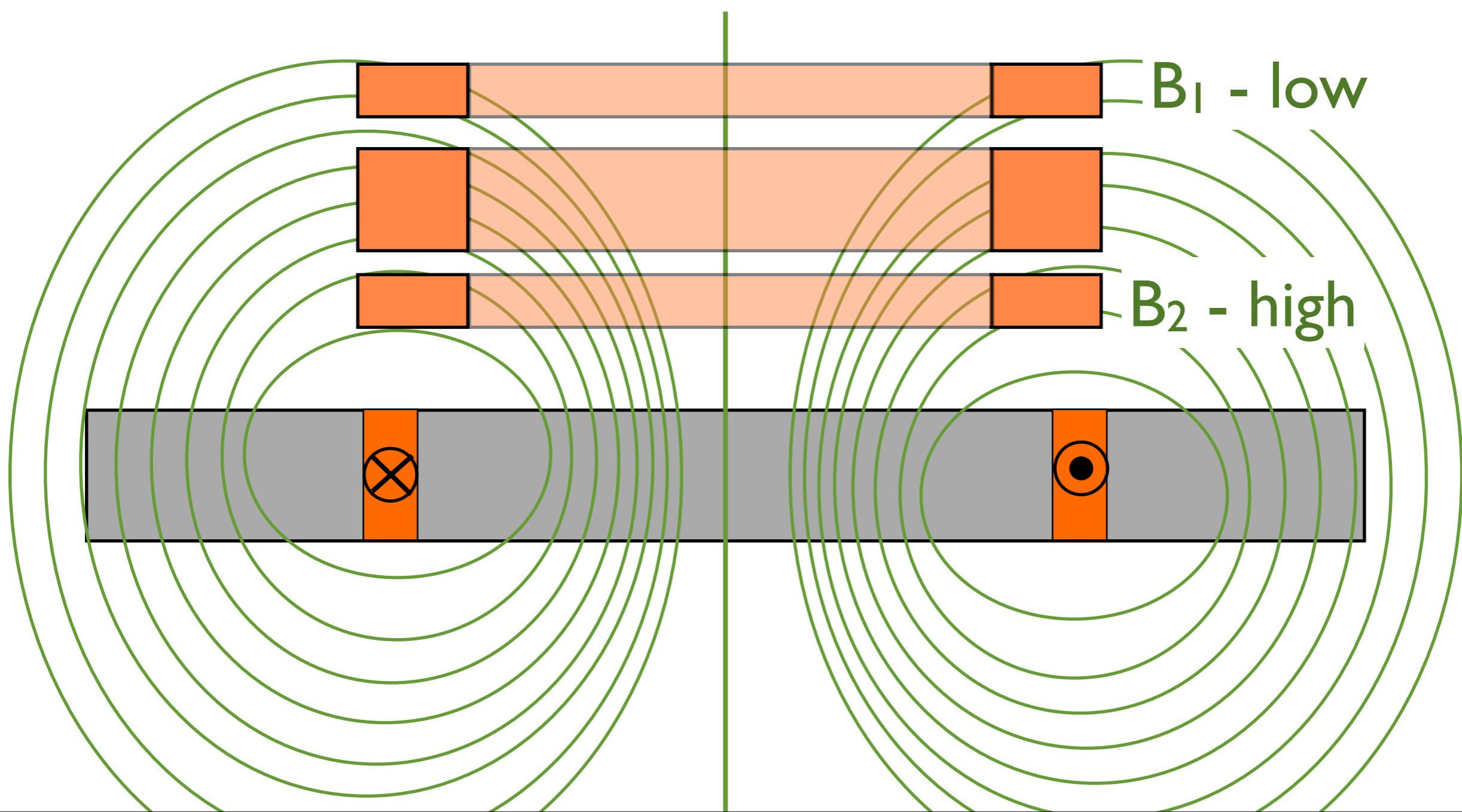
The two detection coils are place symmetrically to the generating coil. They receive both the field by the generating coil and the field generated by the eddy current



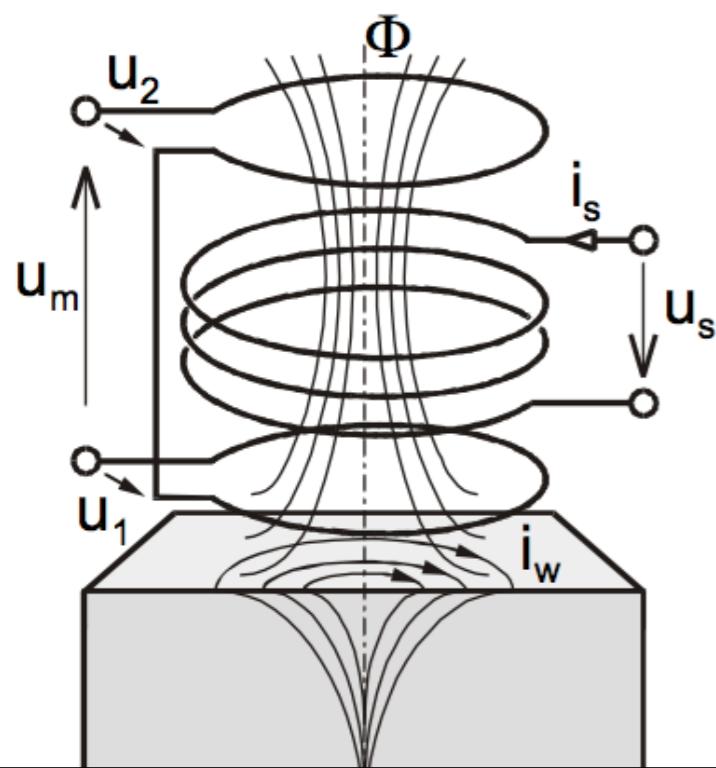
The field created by the generating coil is equal for both coil 1 and coil 2 (they are at the same distance)



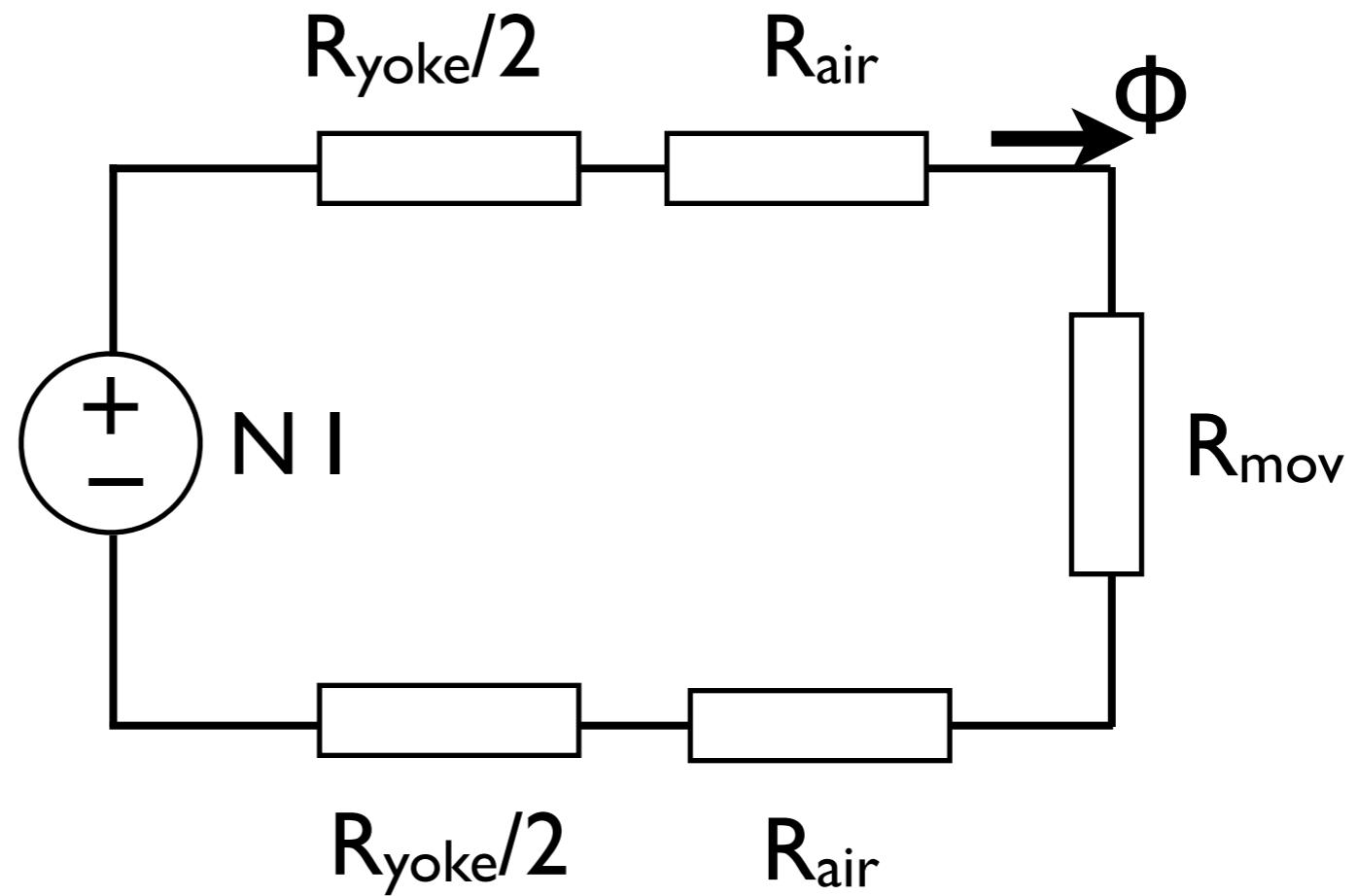
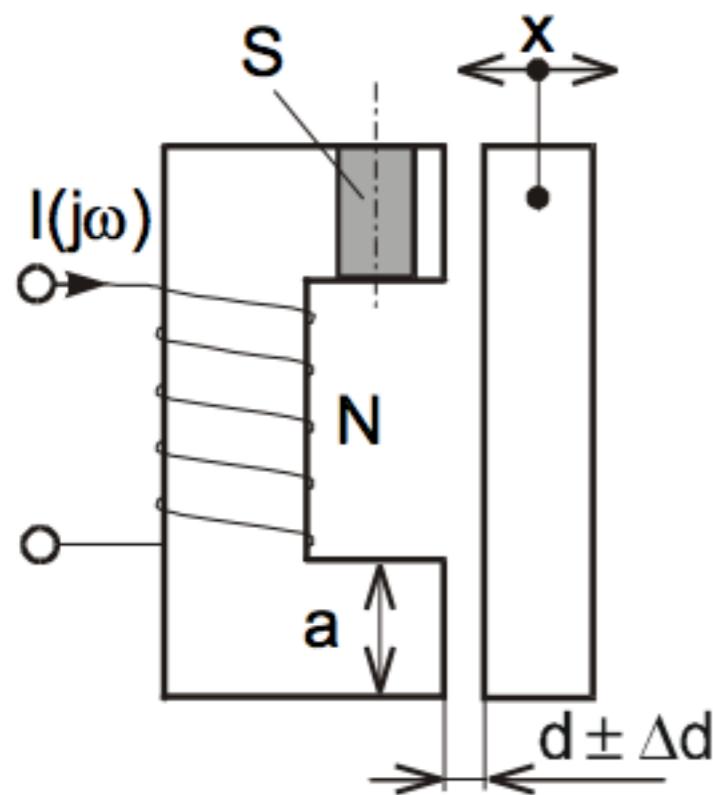
While the field generated by eddy current is larger in coil 2  
than in coil 1



We take the difference between the voltage induced the two coils



# Inductive sensors with variable air gap



$N I$  = magnetomotive force

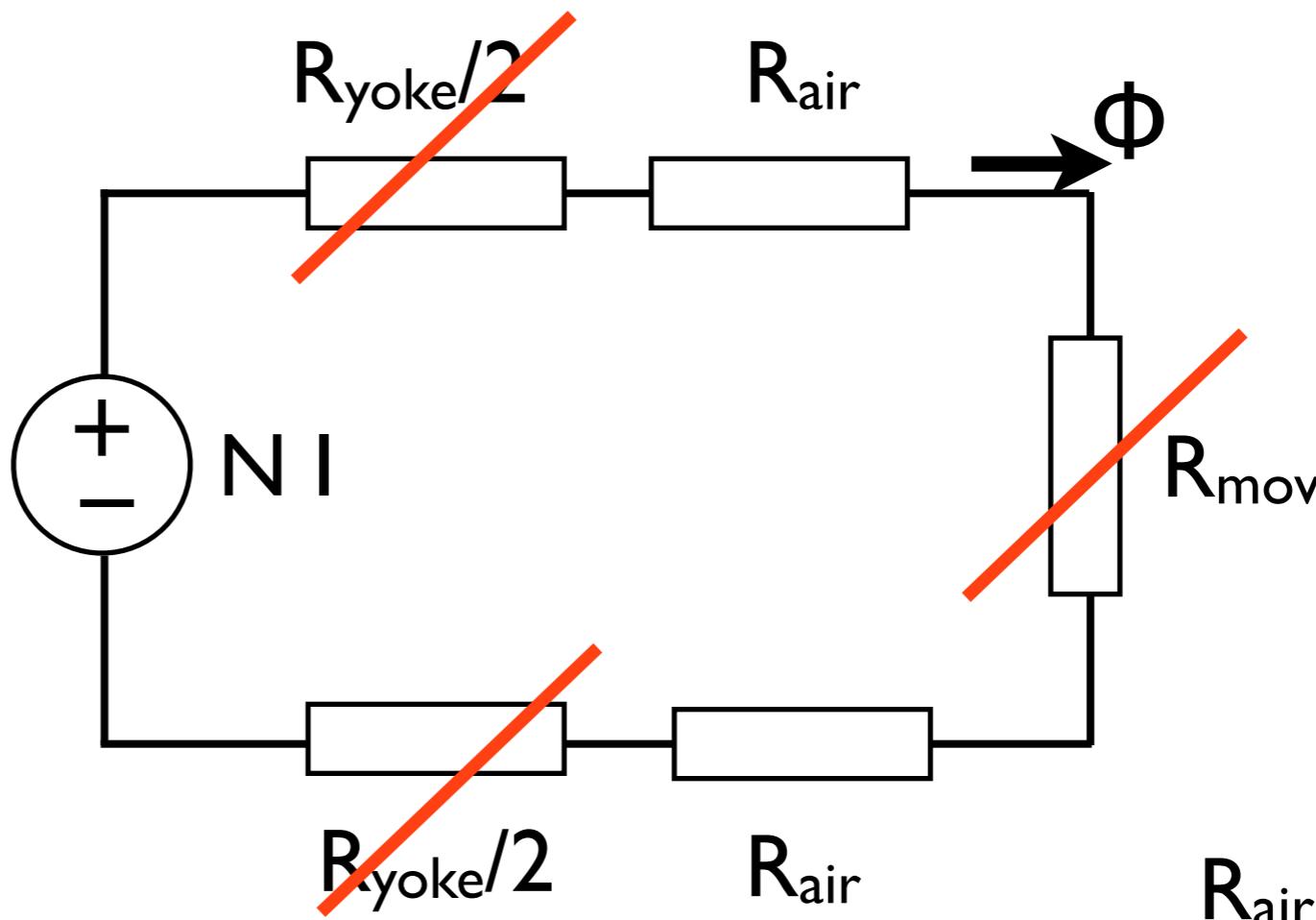
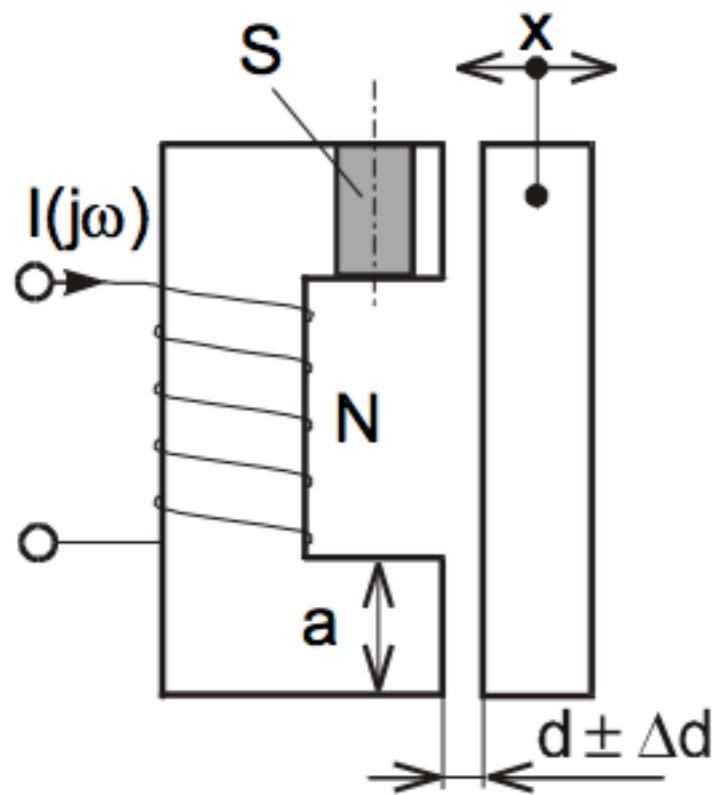
$\Phi$  = magnetic flux

$R_{yoke}$  = reluctance of the yoke

$R_{air}$  = reluctance of air gap

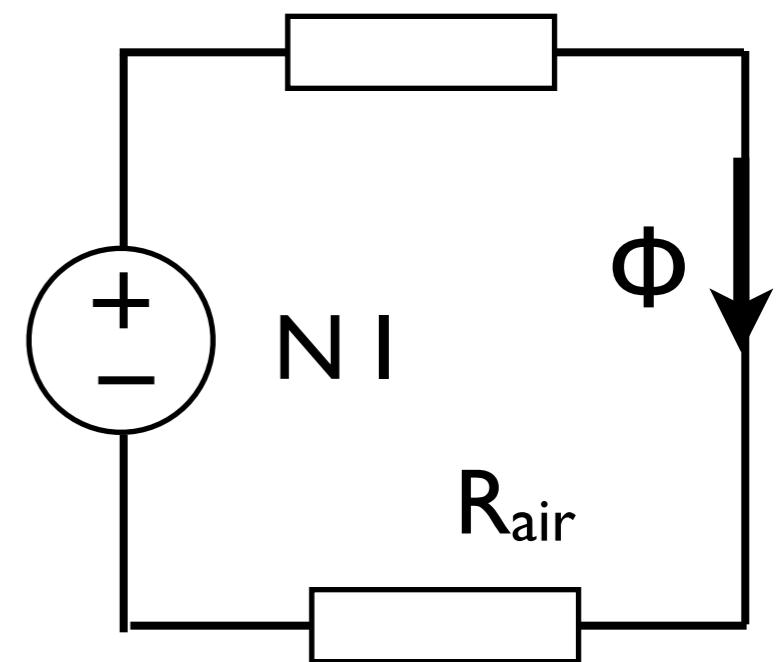
$R_{mov}$  = reluctance of movable part

# Inductive sensors with variable air gap

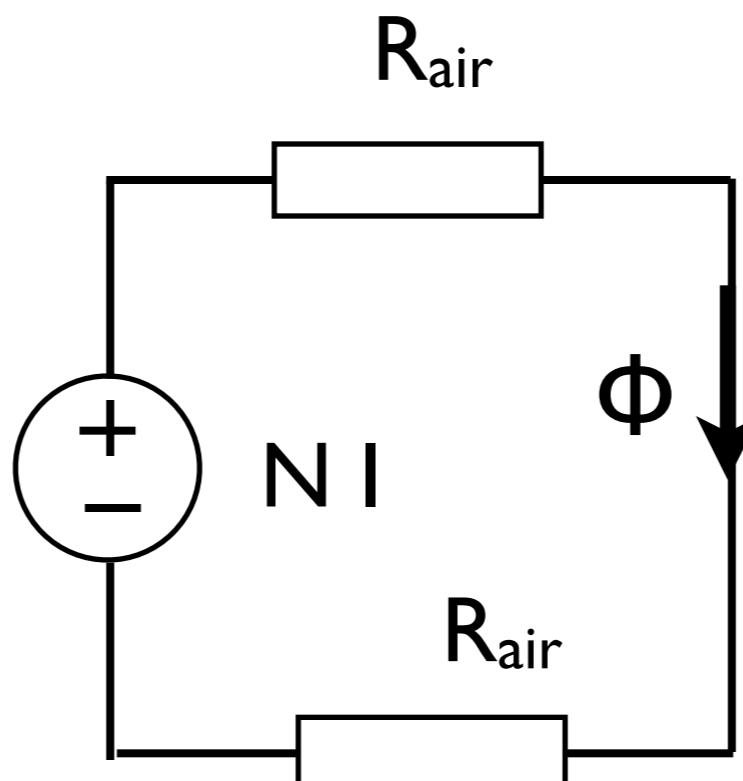
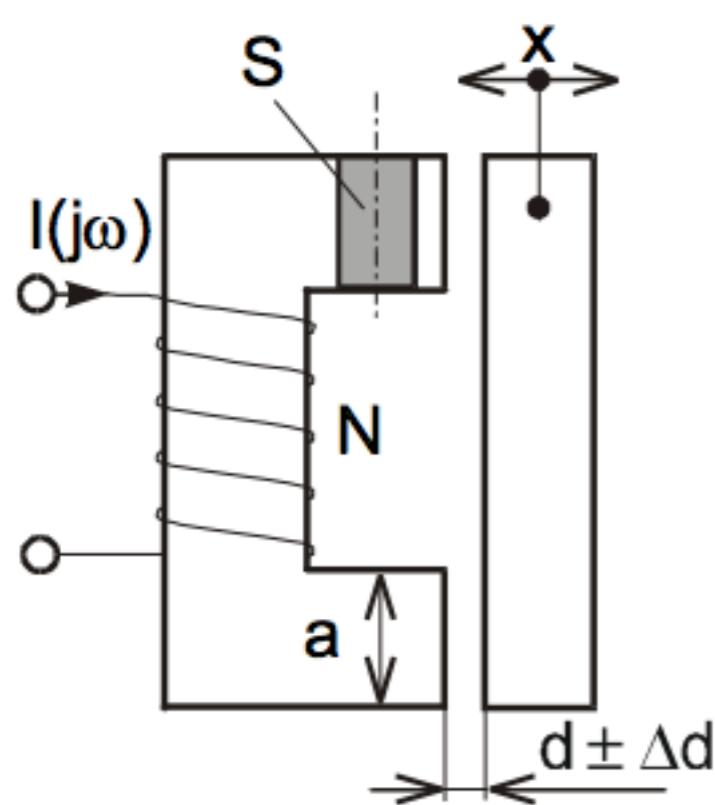


$$R = \text{length} / (\mu \cdot \text{Surface})$$

We neglect  $R_{yoke}$  and  $R_{mov}$  because  $\mu_{Fe} \gg \mu_0$



# Inductive sensors with variable air gap

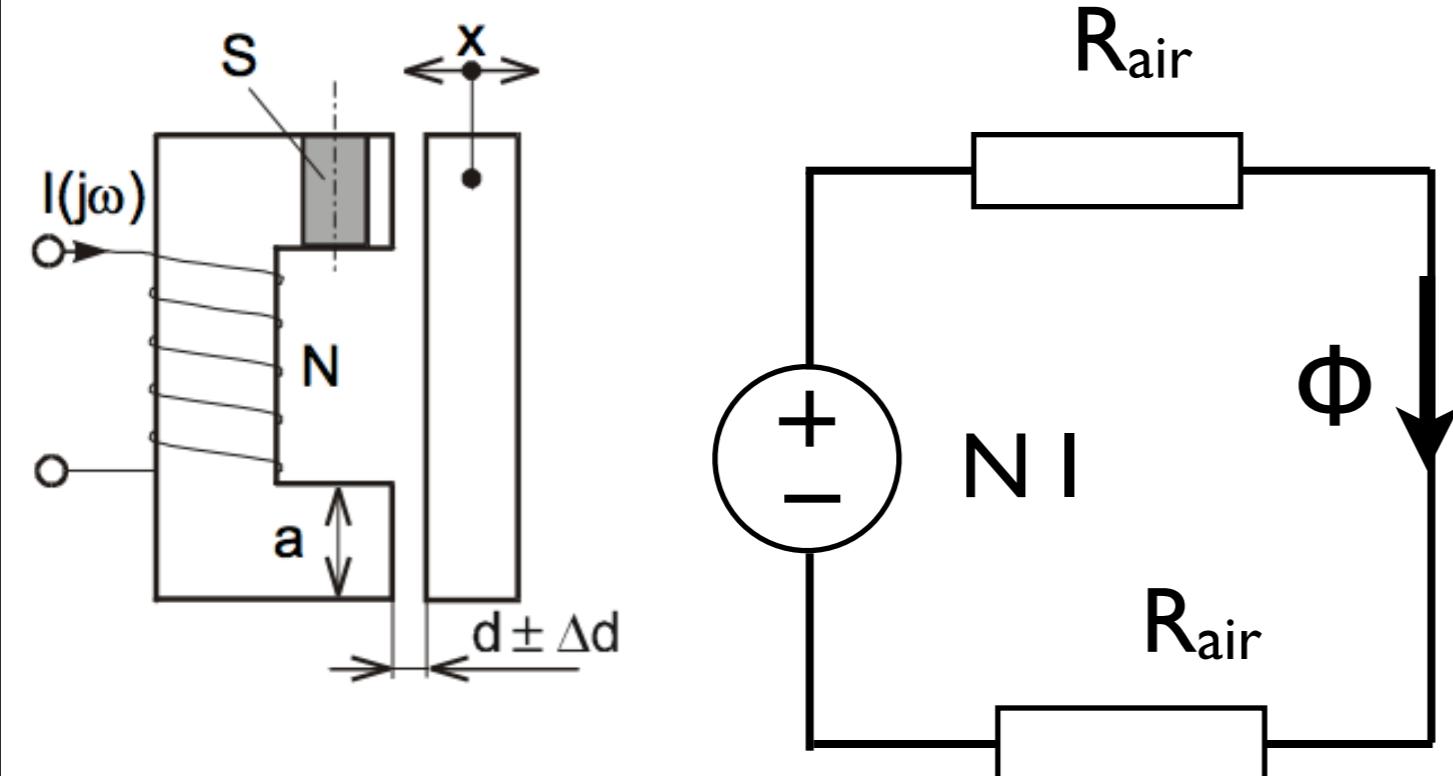


$$R_{air} = d / (\mu_0 \cdot S)$$

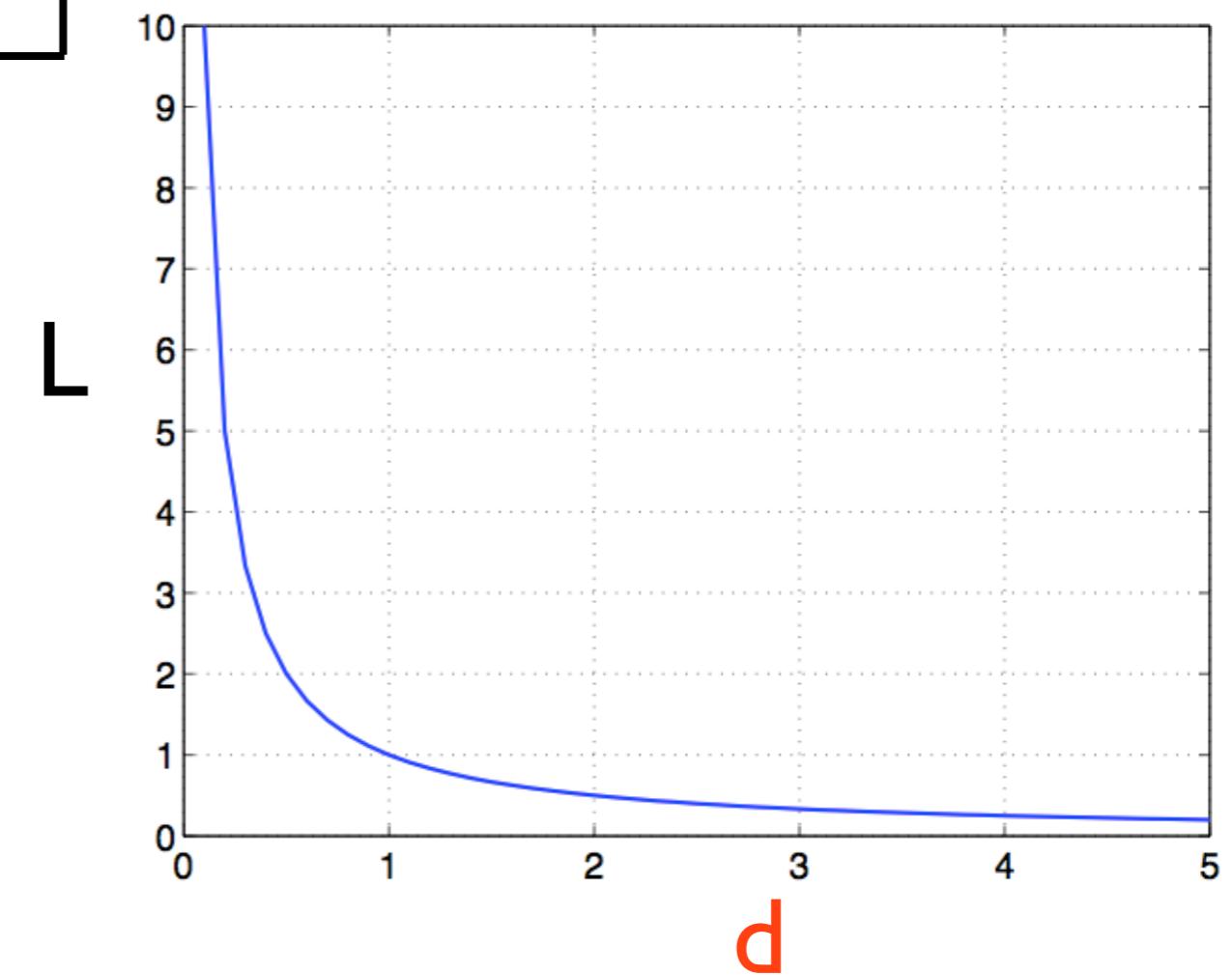
$$\phi = \frac{NI}{2R_{air}} = \frac{NI}{2d} \mu_0 S$$

$$L = N \frac{\phi}{I} = \frac{N^2}{2d} \mu_0 S$$

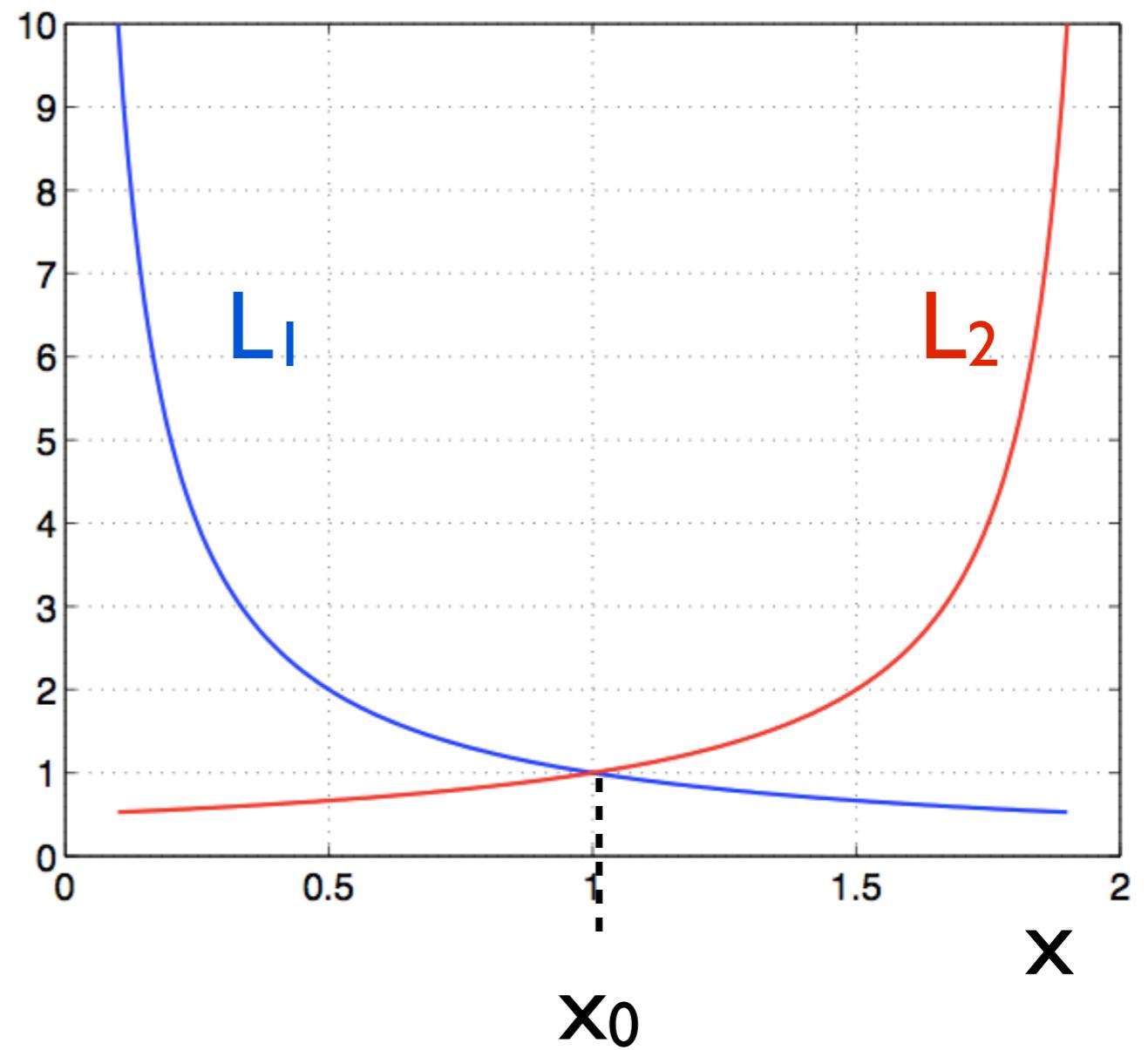
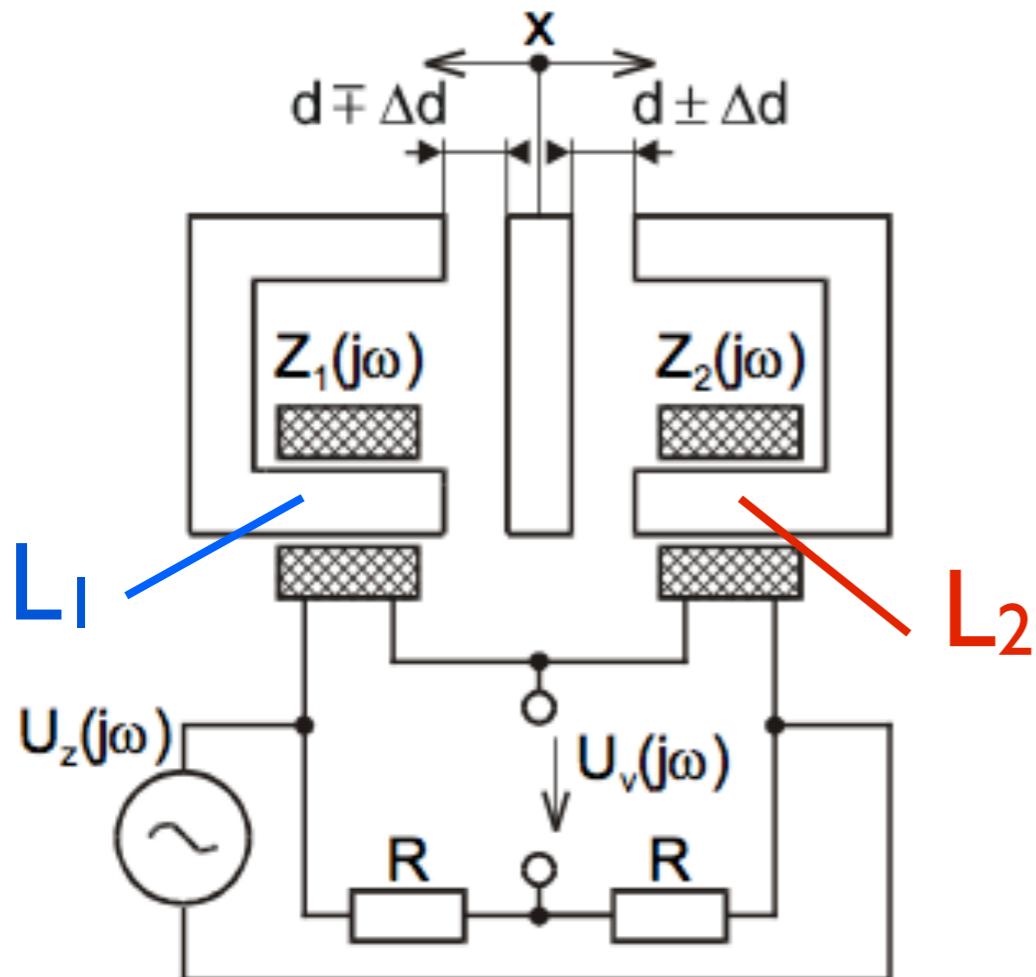
# Inductive sensors with variable air gap



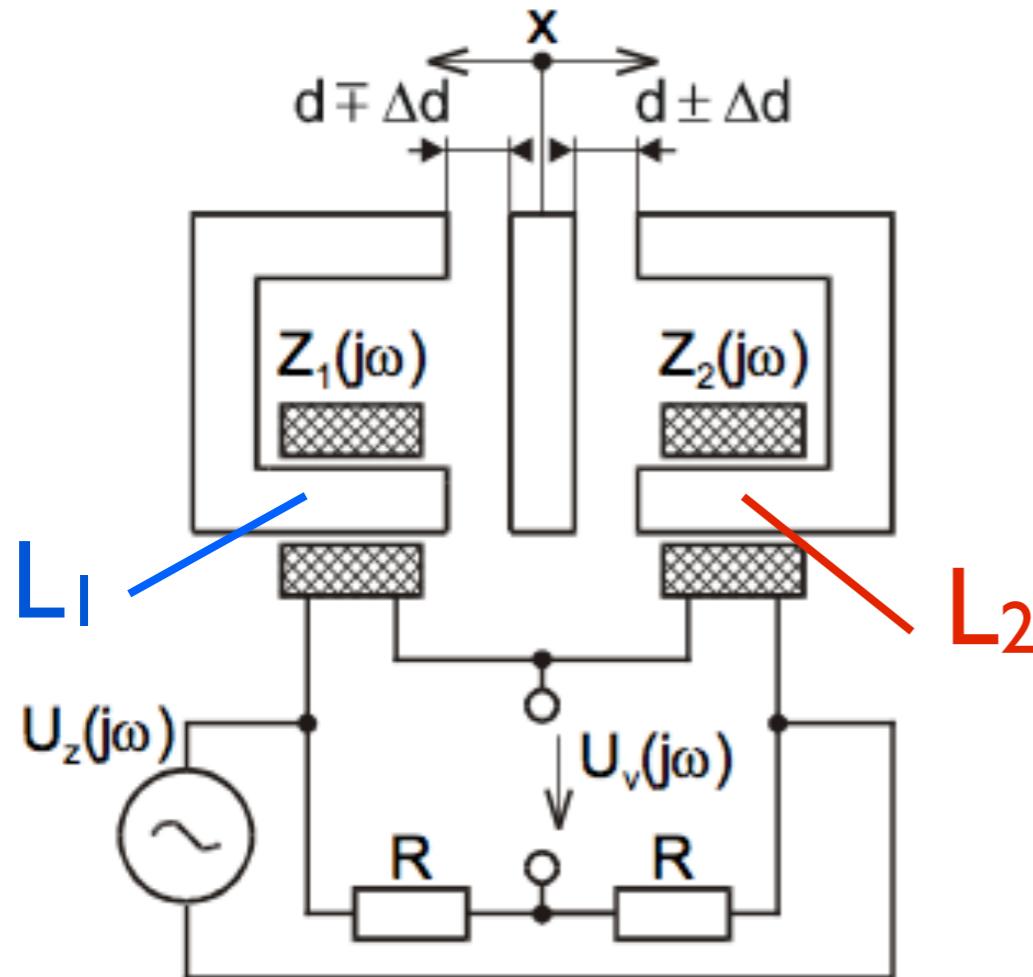
$$L = \frac{N^2}{2d} \mu_0 S$$



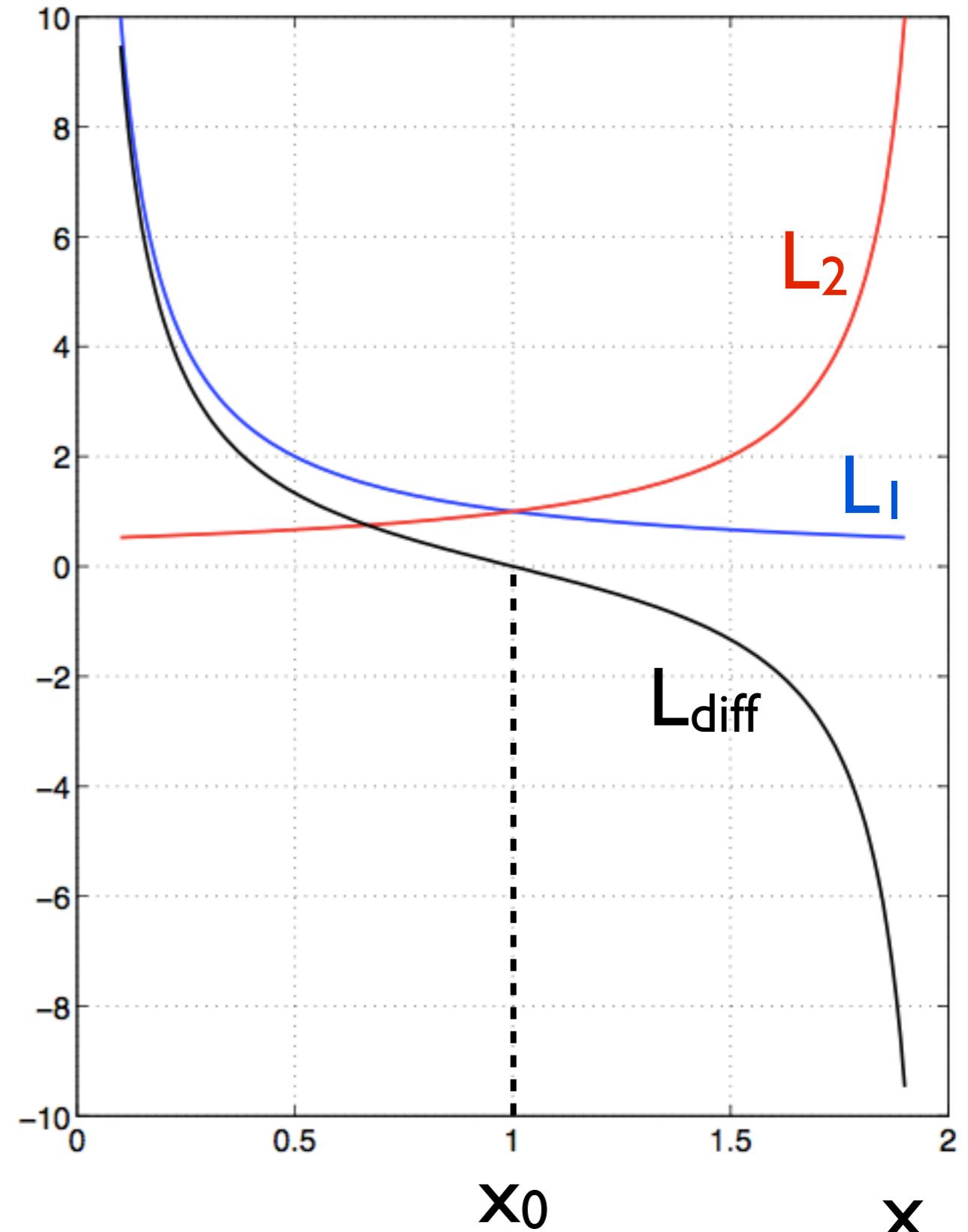
# Differential inductive sensor



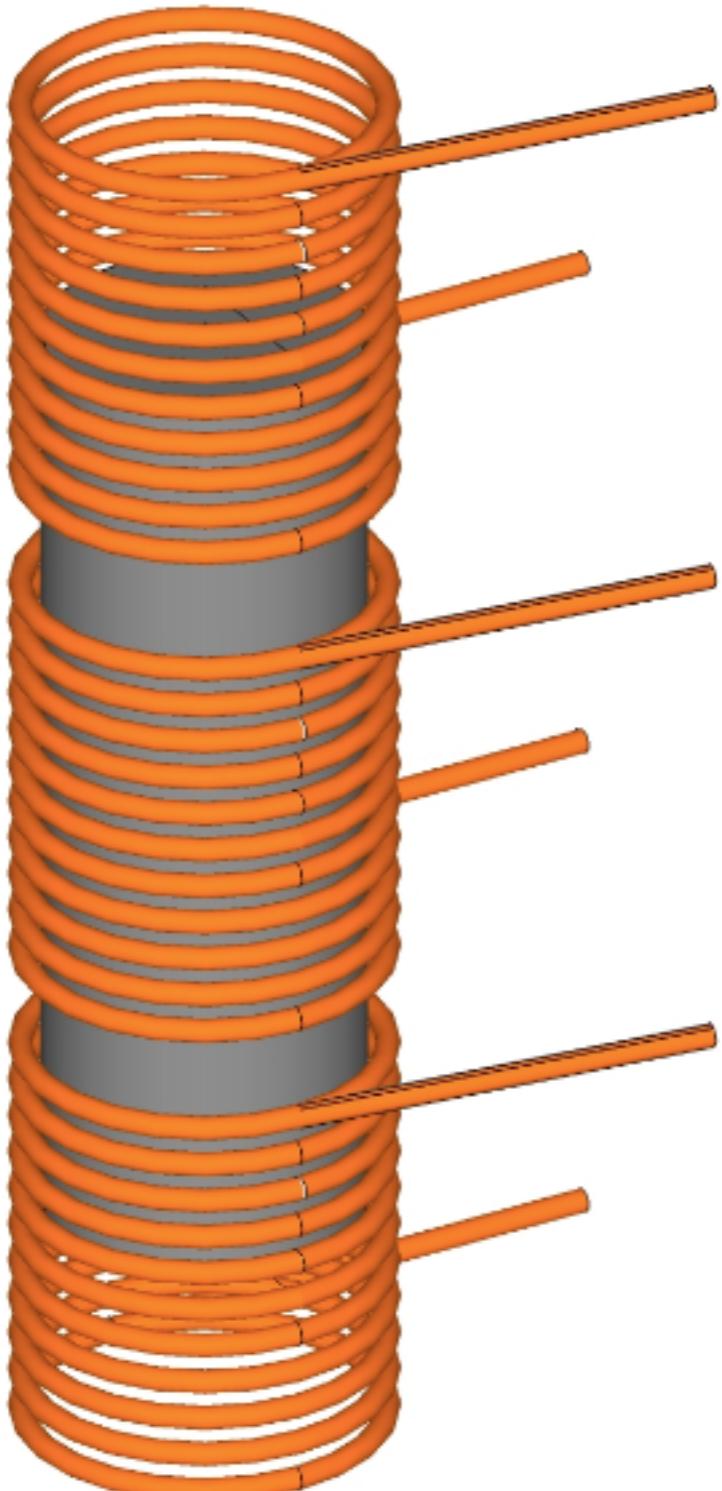
# Differential inductive sensor



$$L_{\text{diff}} = L_1 - L_2$$

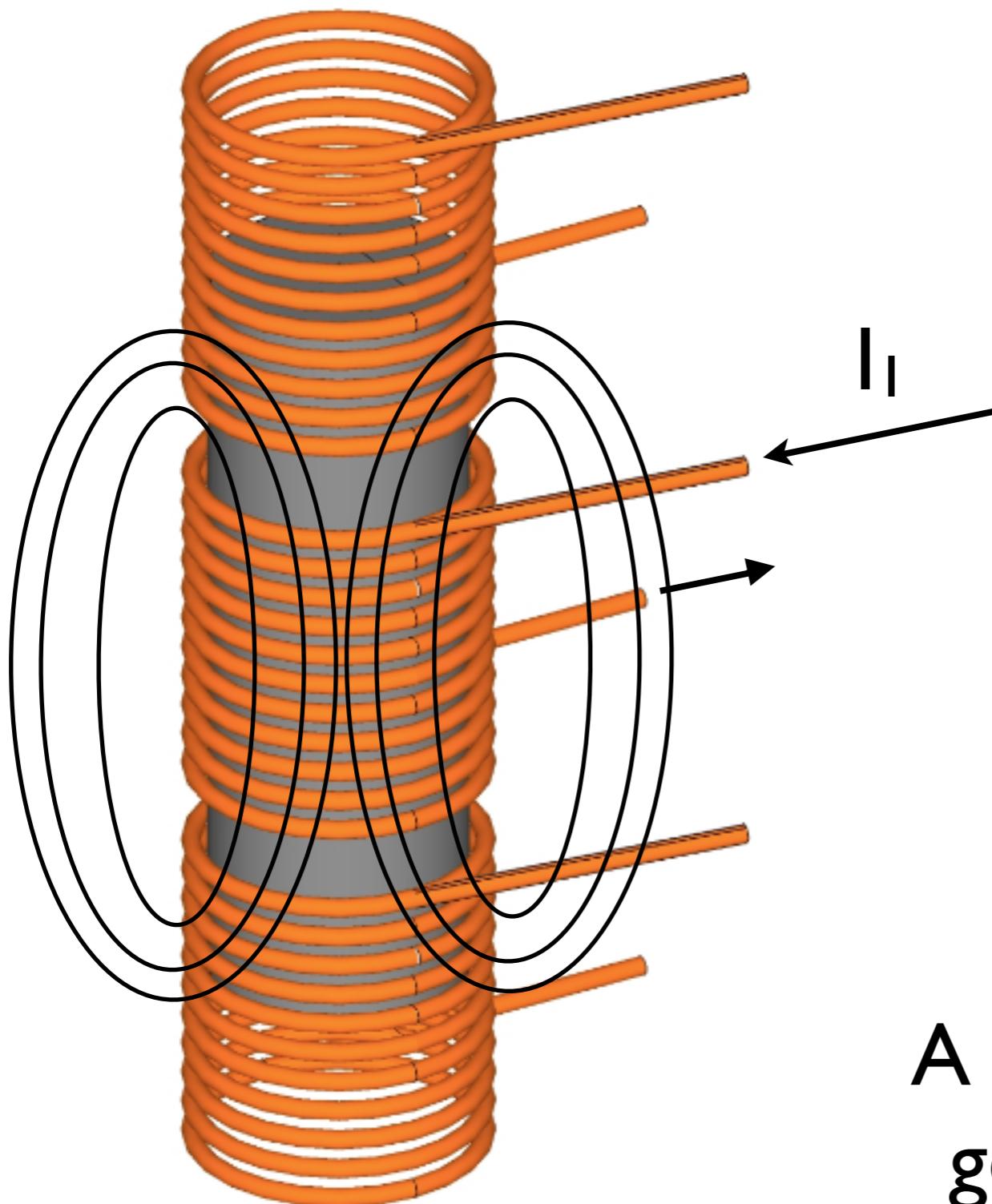


# LVDT - Linear Variable Differential Transformer



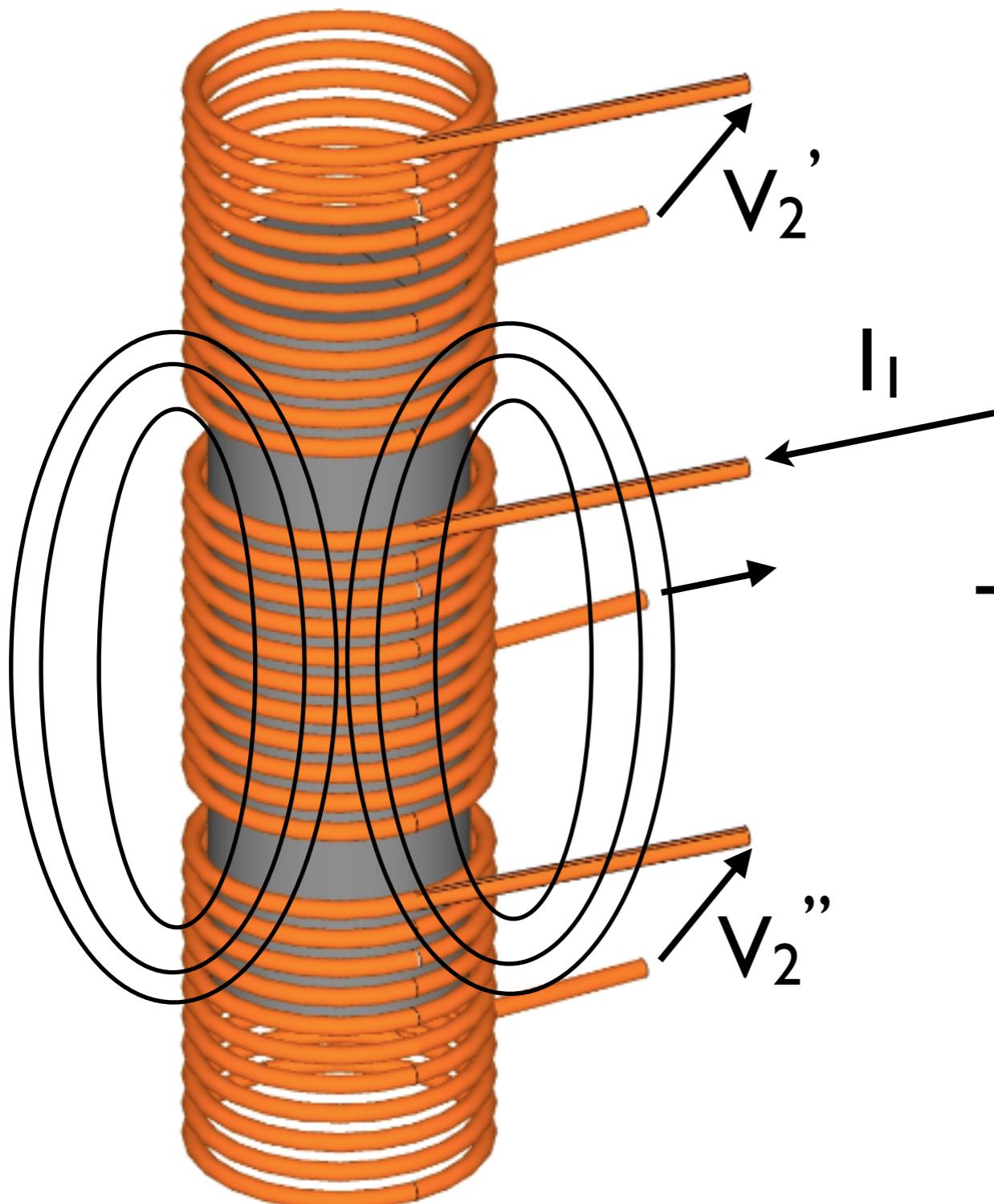
- It's a Transformer  
(it works only in AC);
- it has one primary coil and  
two secondary coils;
- it has a movable core.

# LVDT - Linear Variable Differential Transformer



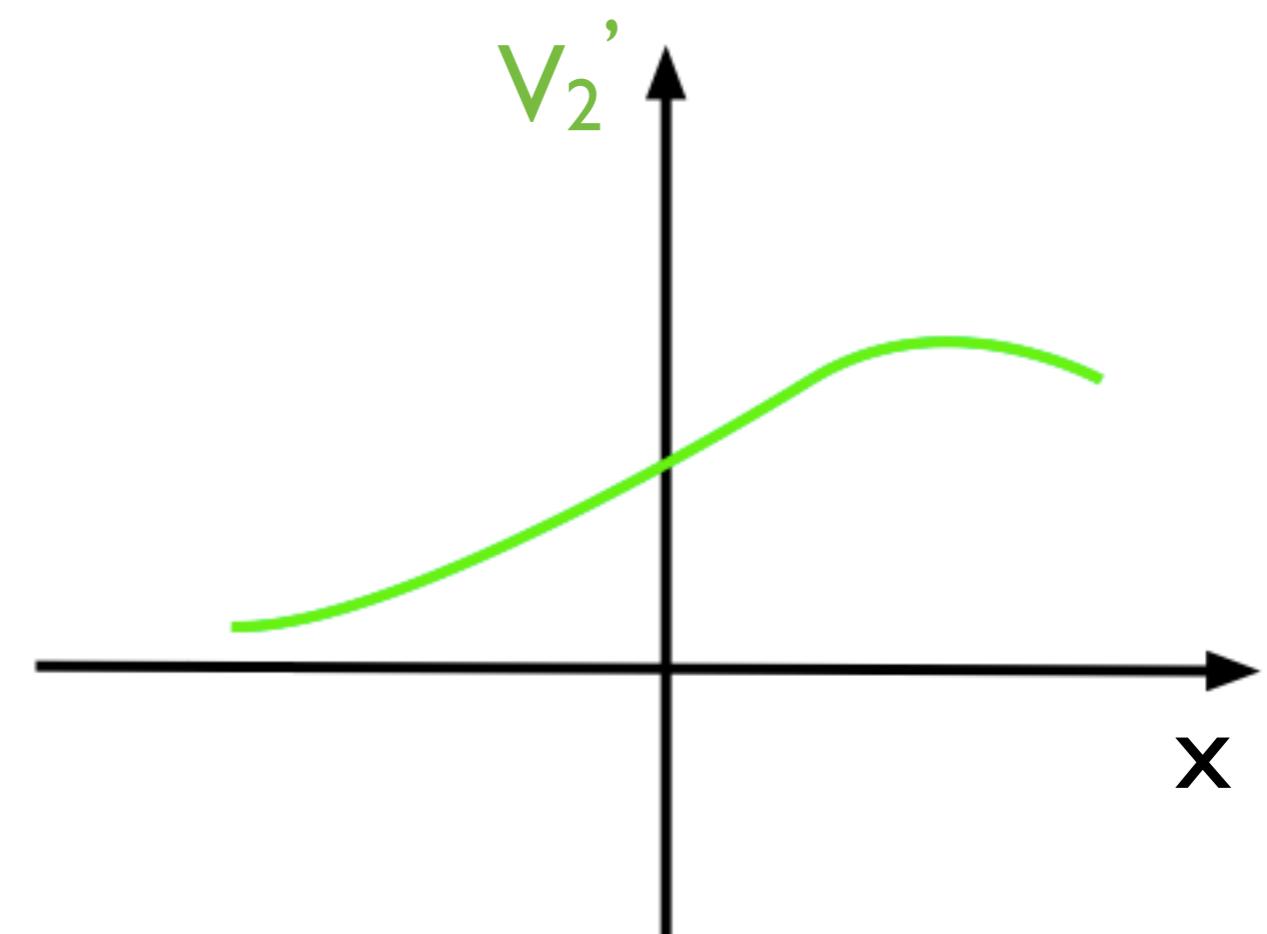
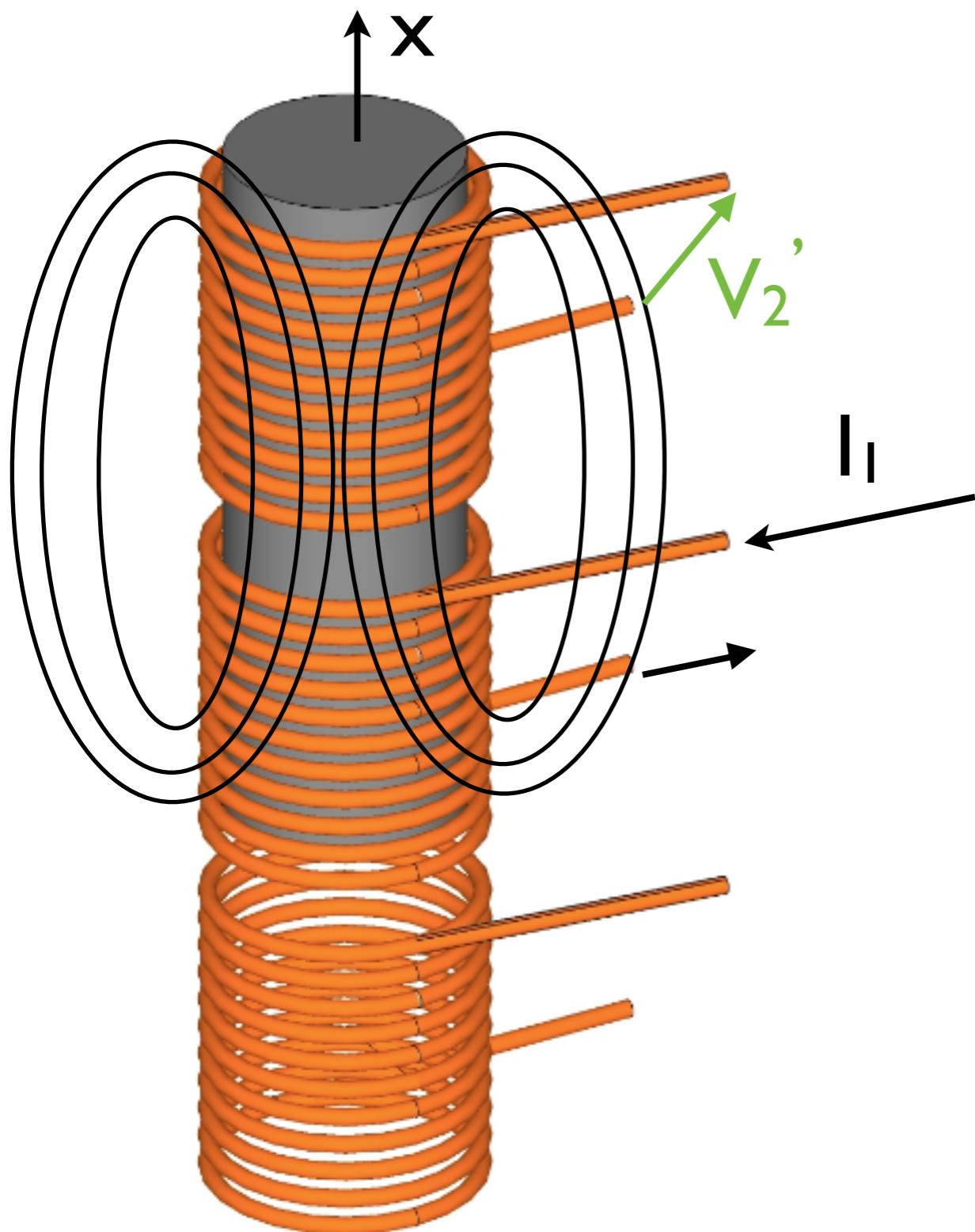
A current in the central coil generates a magnetic field

# LVDT - Linear Variable Differential Transformer

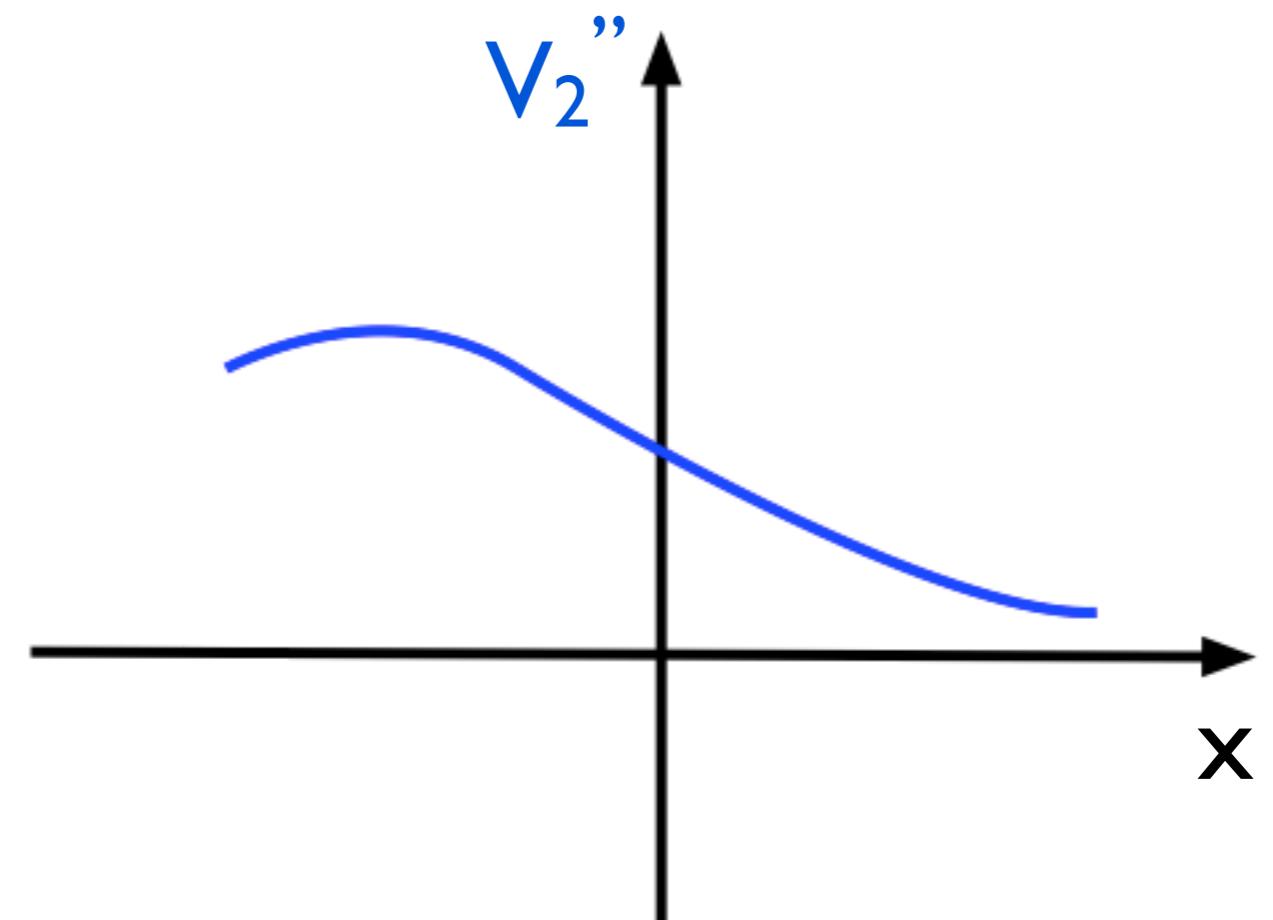
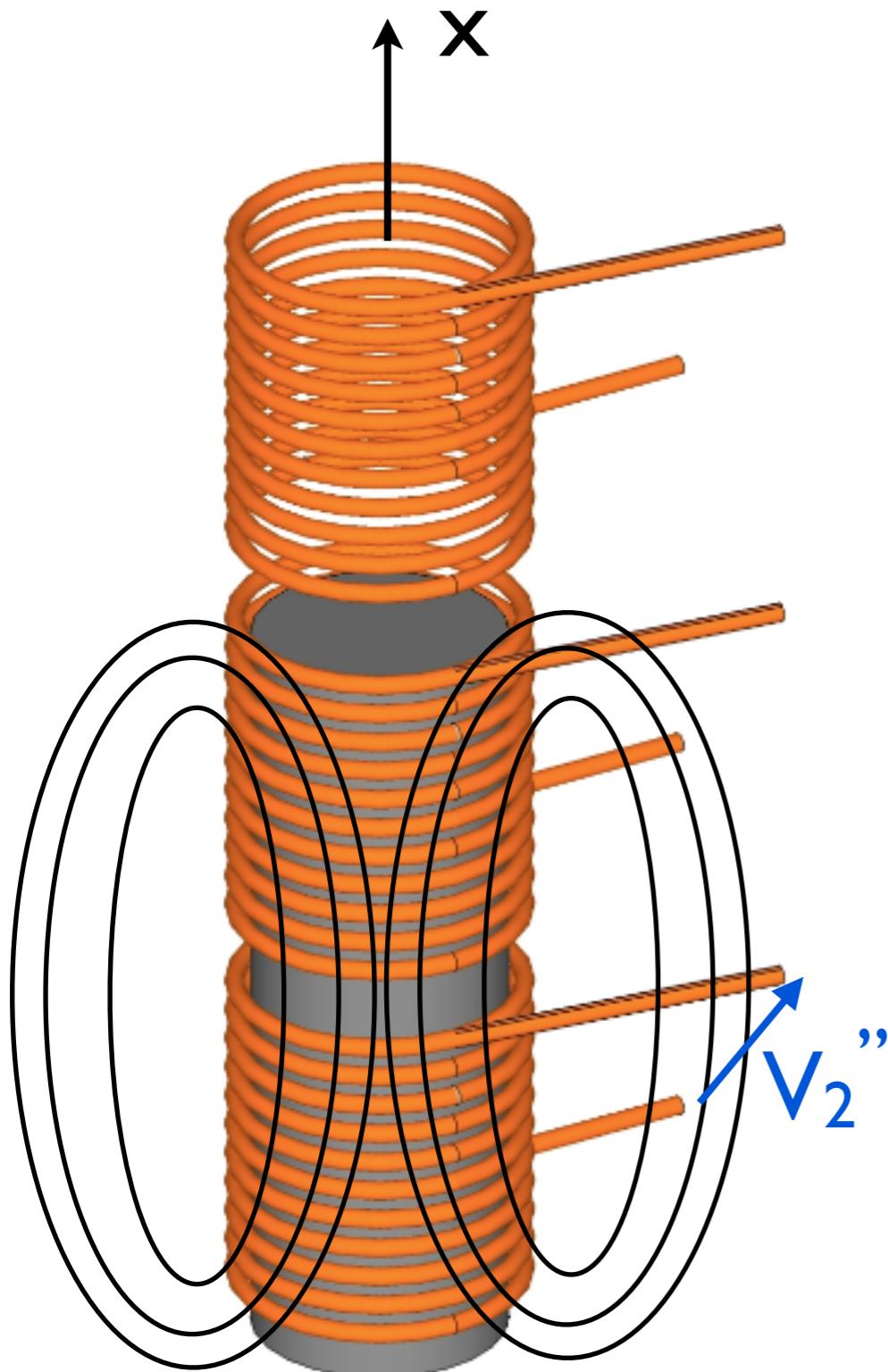


The time-varying magnetic field induces a voltage in the external coils

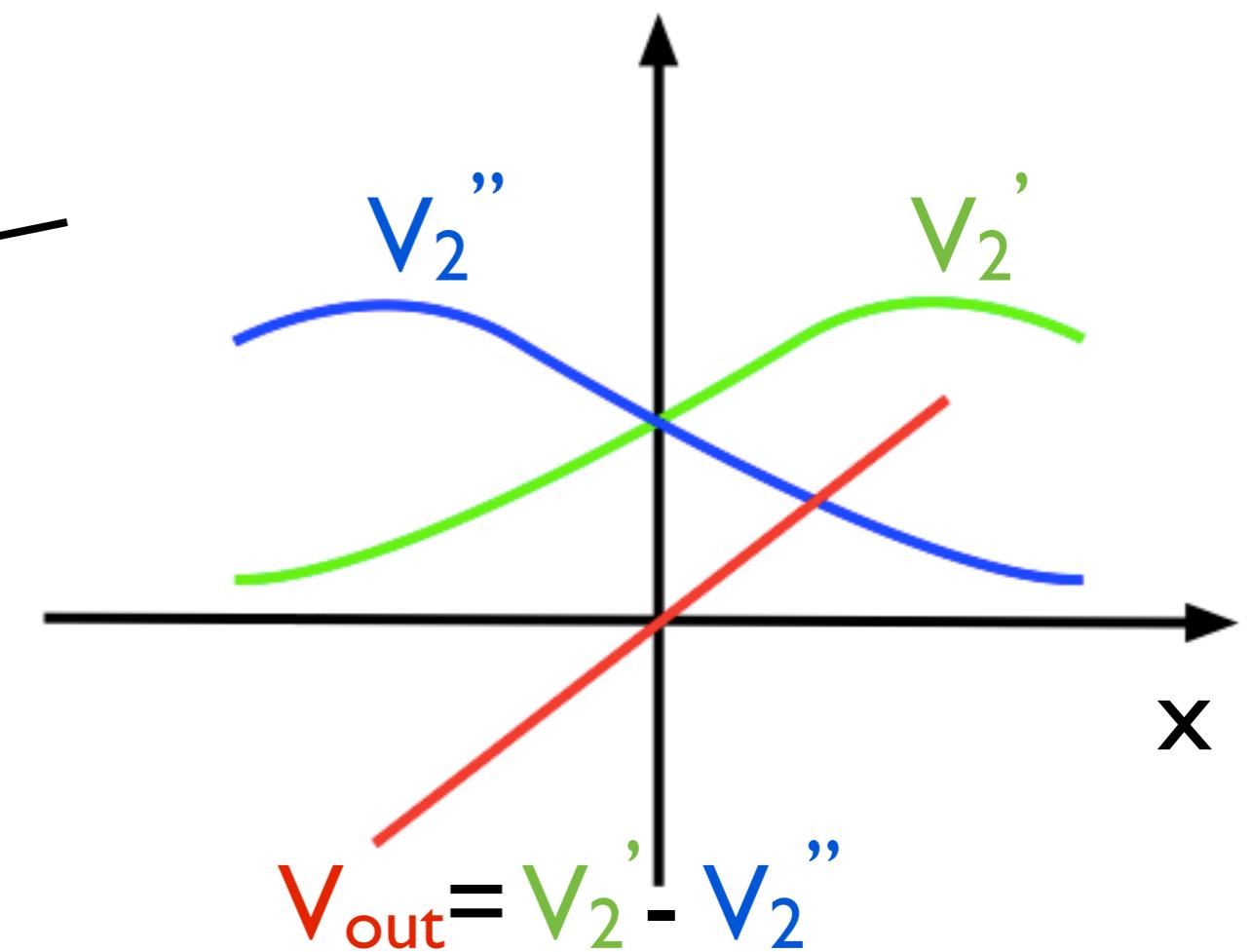
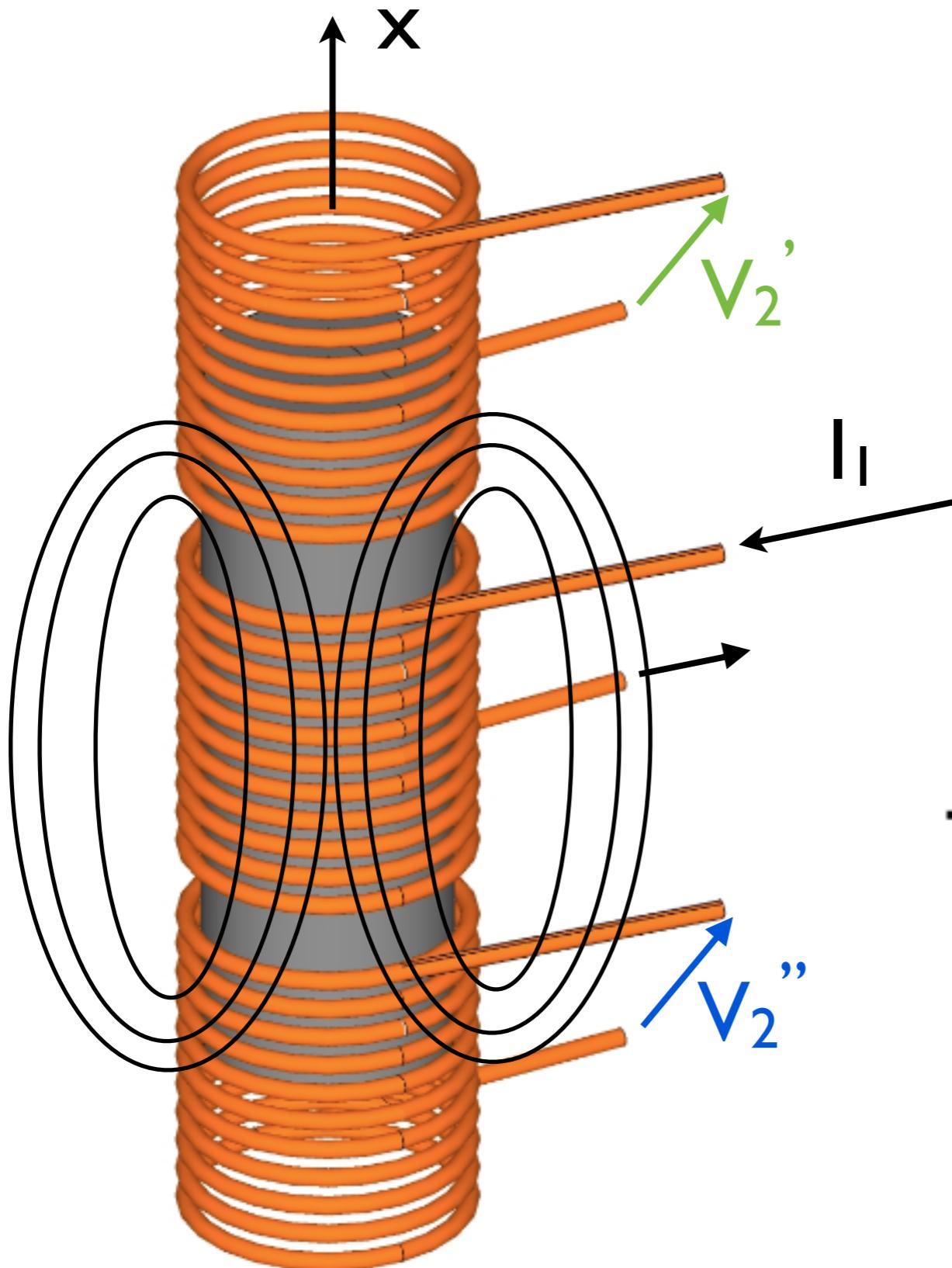
# LVDT - Linear Variable Differential Transformer



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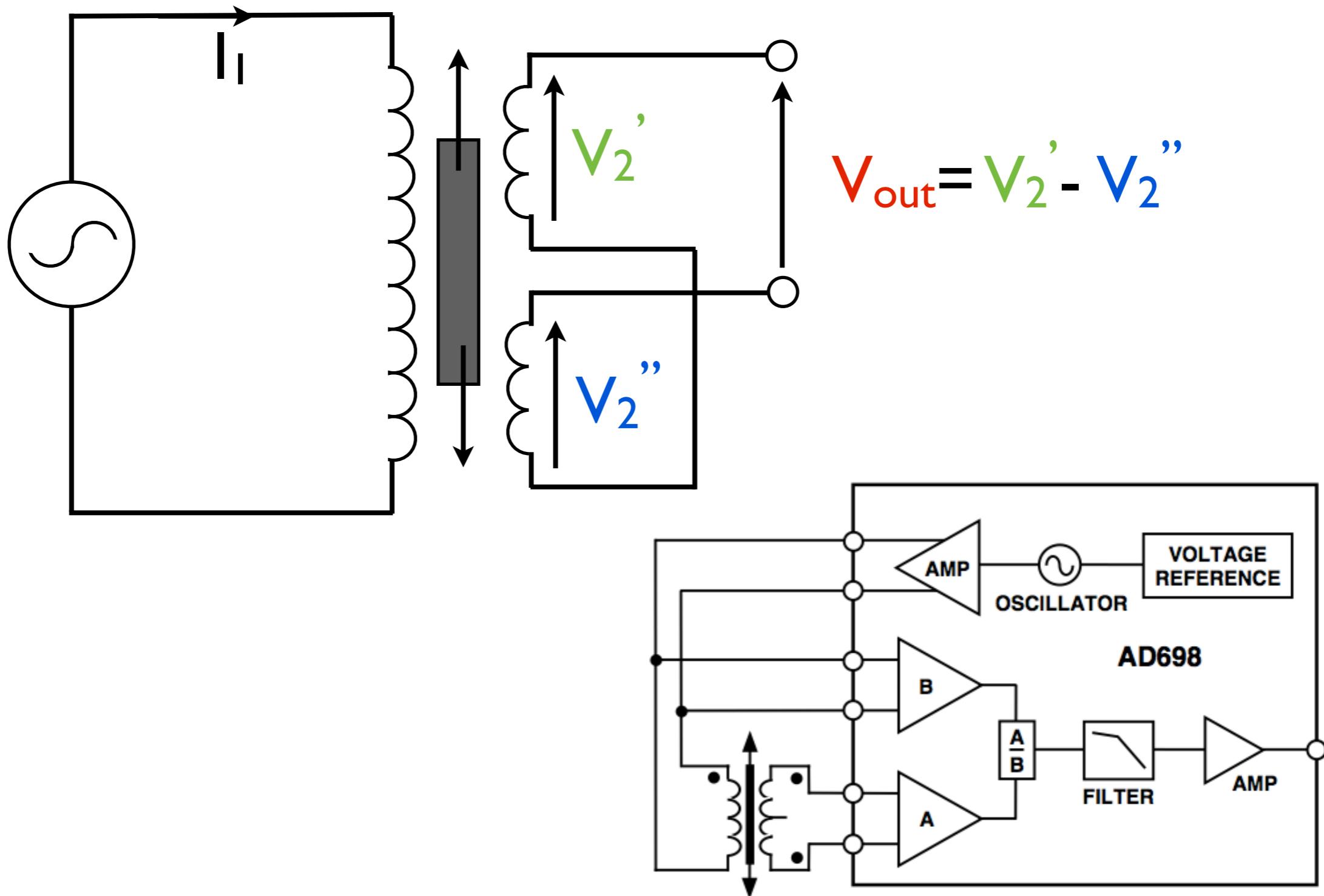


# LVDT - Linear Variable Differential Transformer

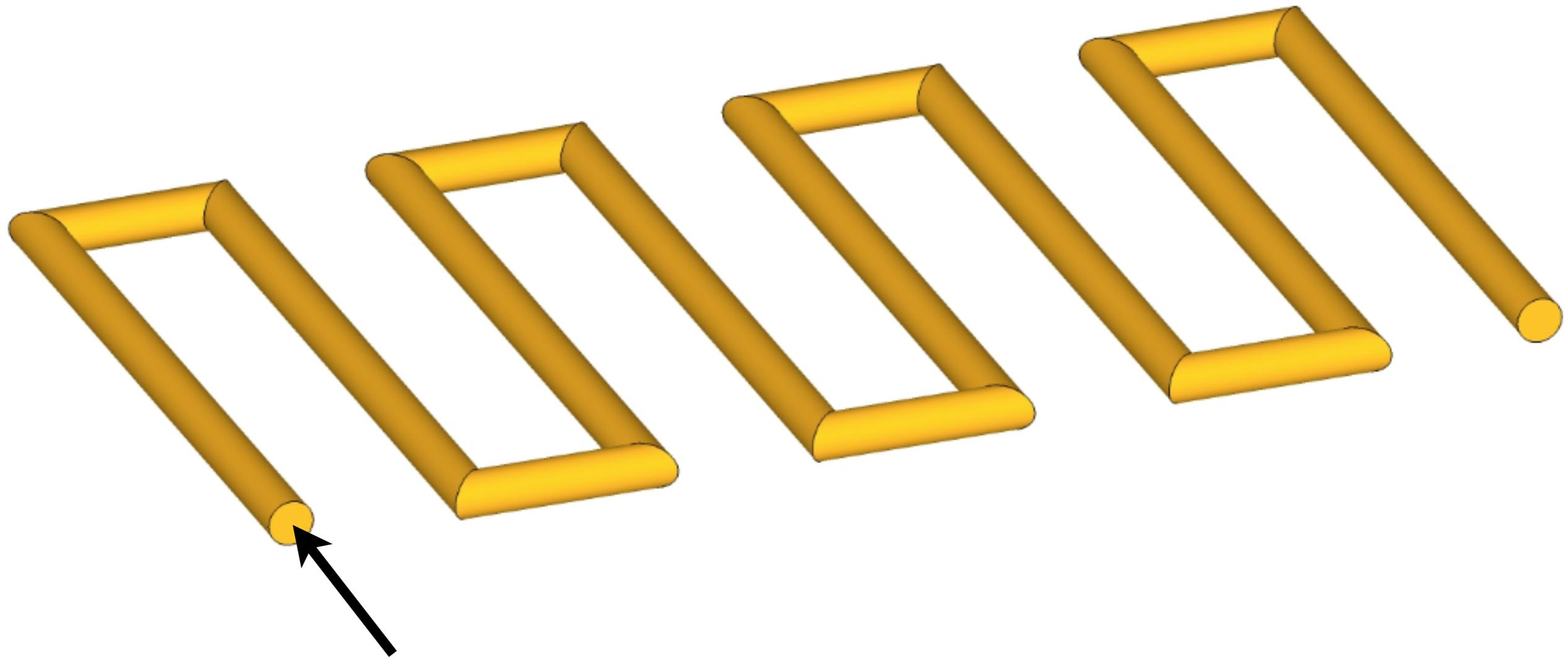


# LVDT - Linear Variable Differential Transformer

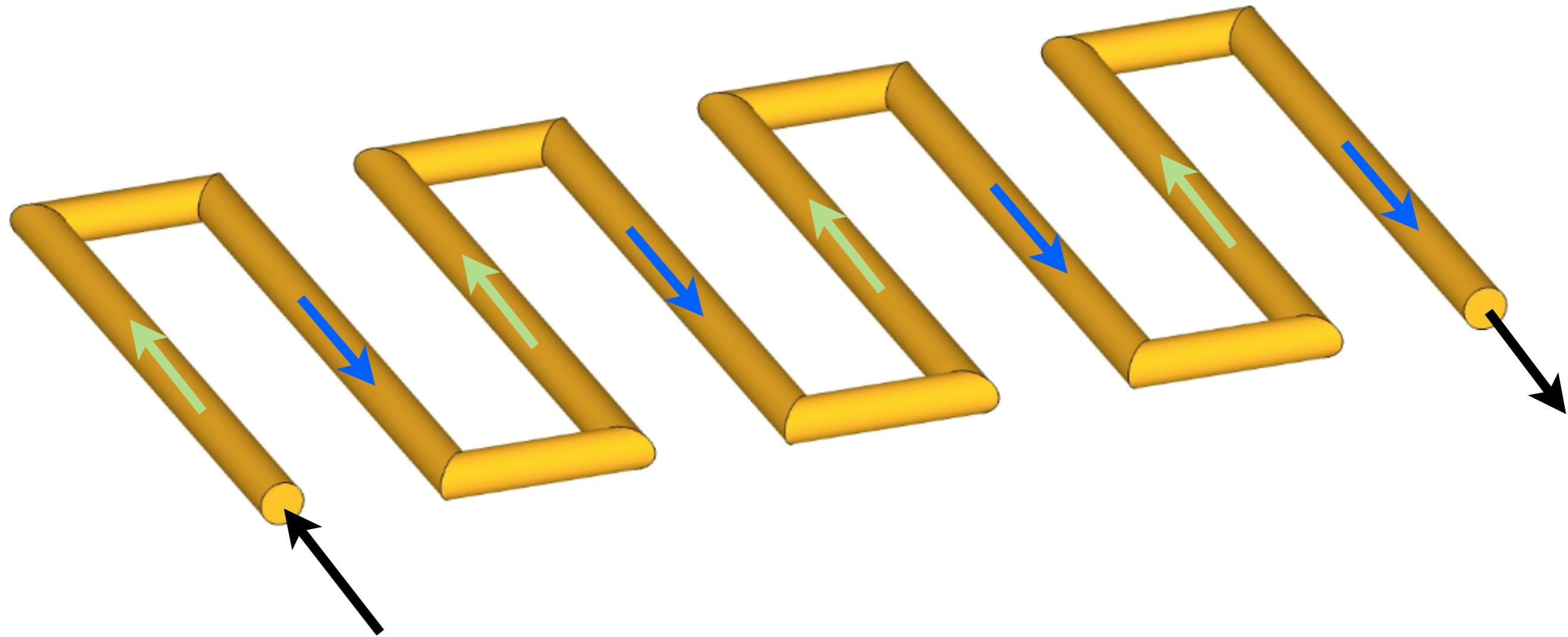
## Scheme



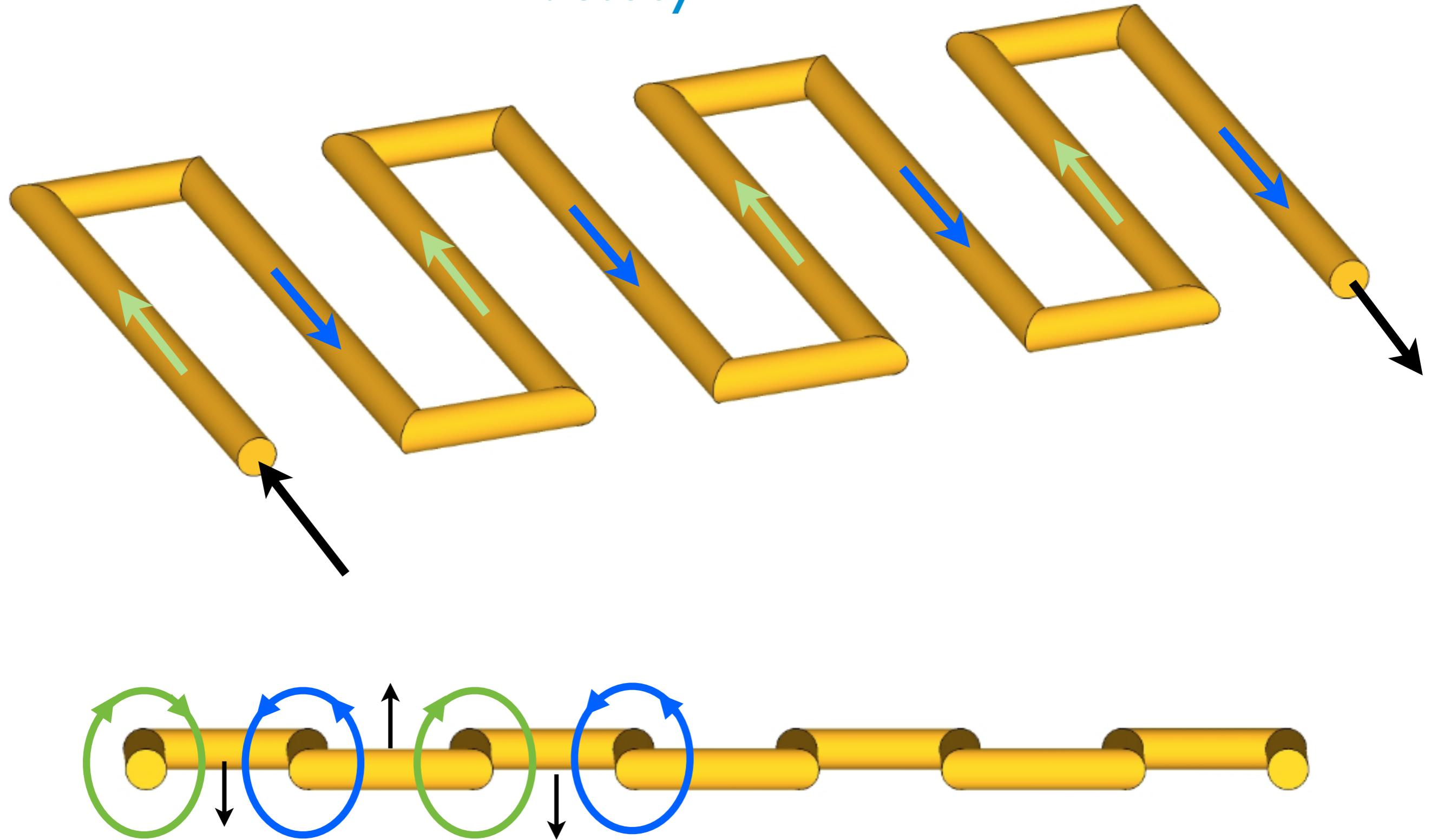
# Inductosyn

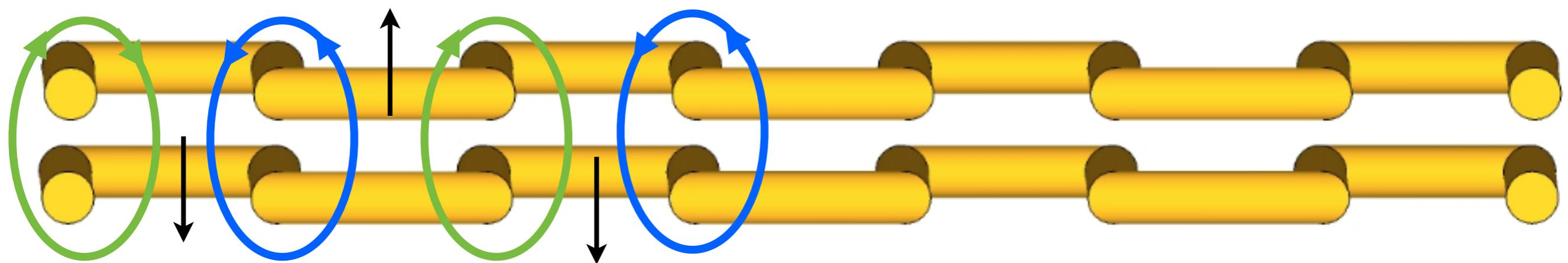


# Inductosyn

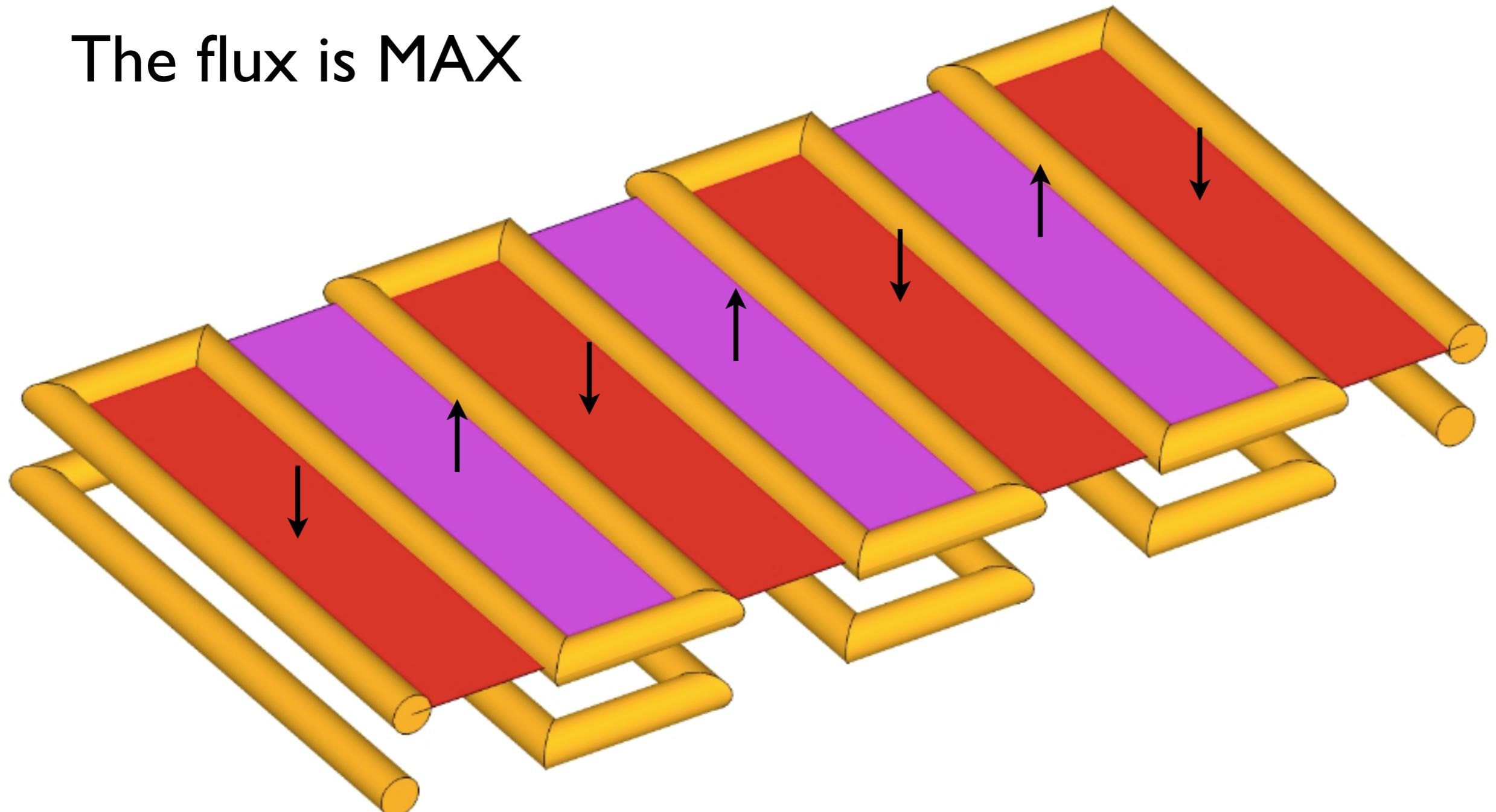


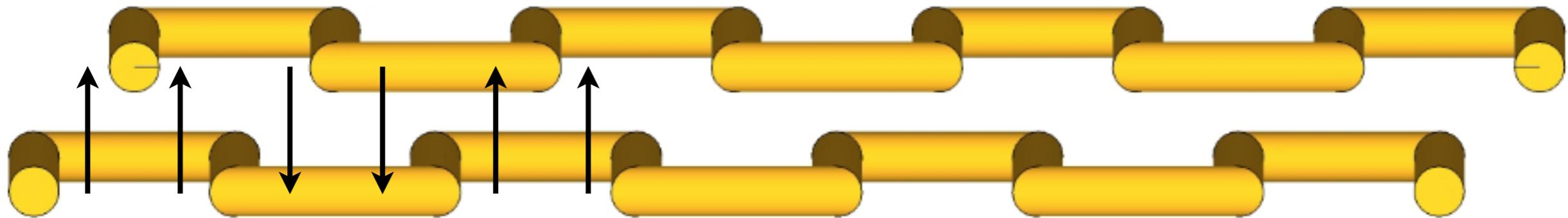
# Inductosyn



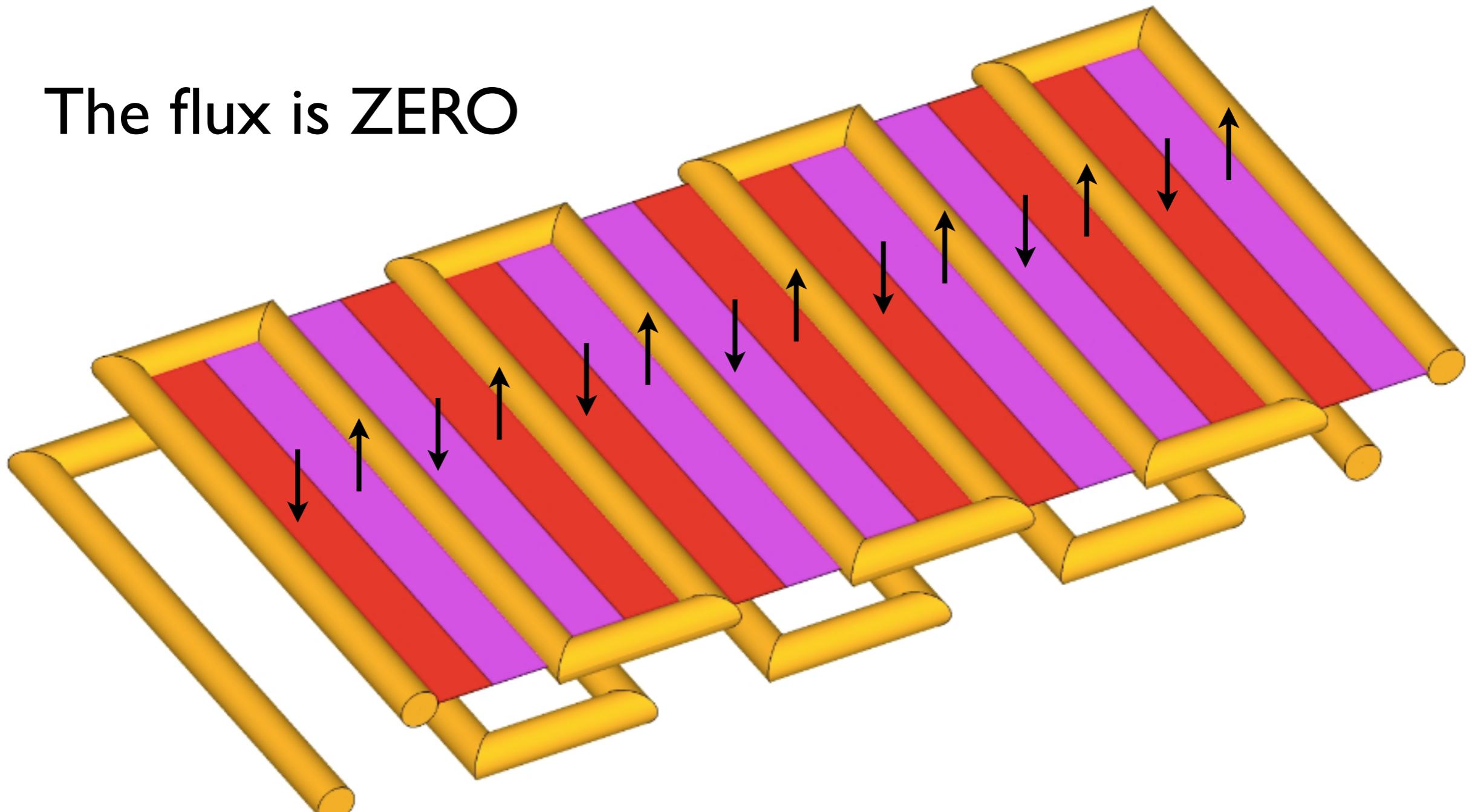


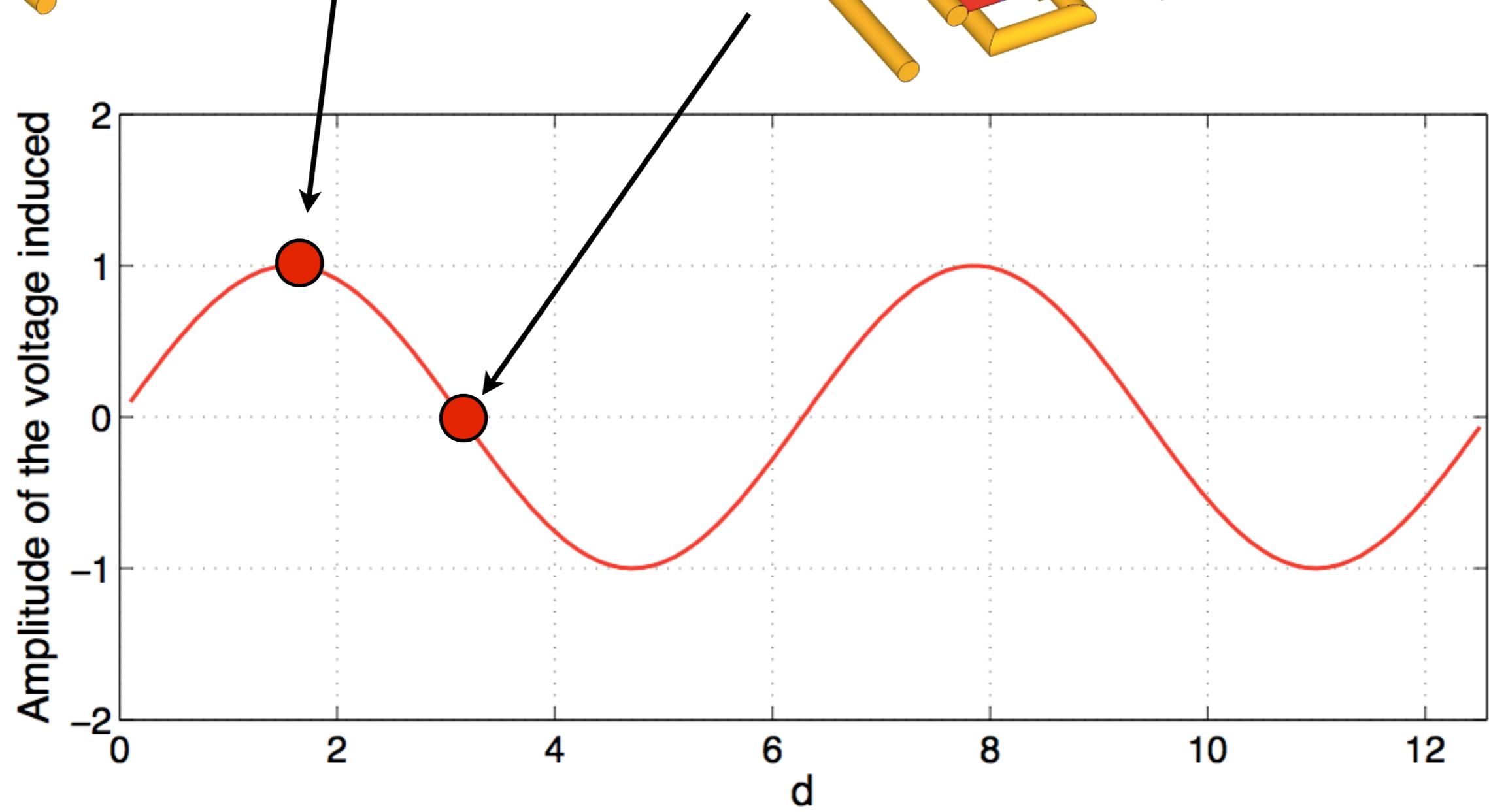
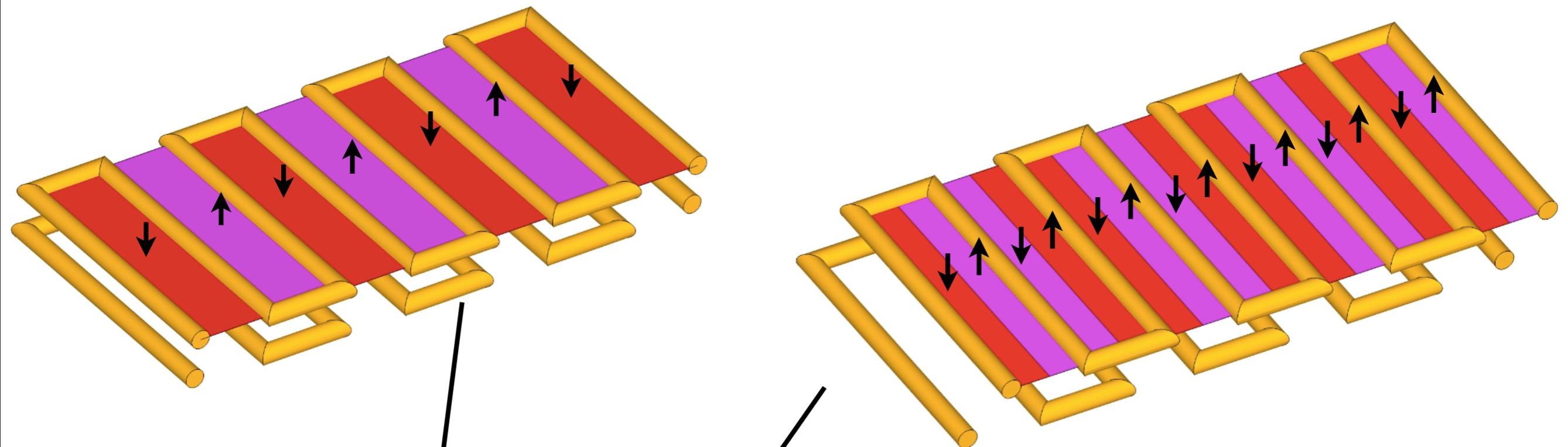
The flux is MAX





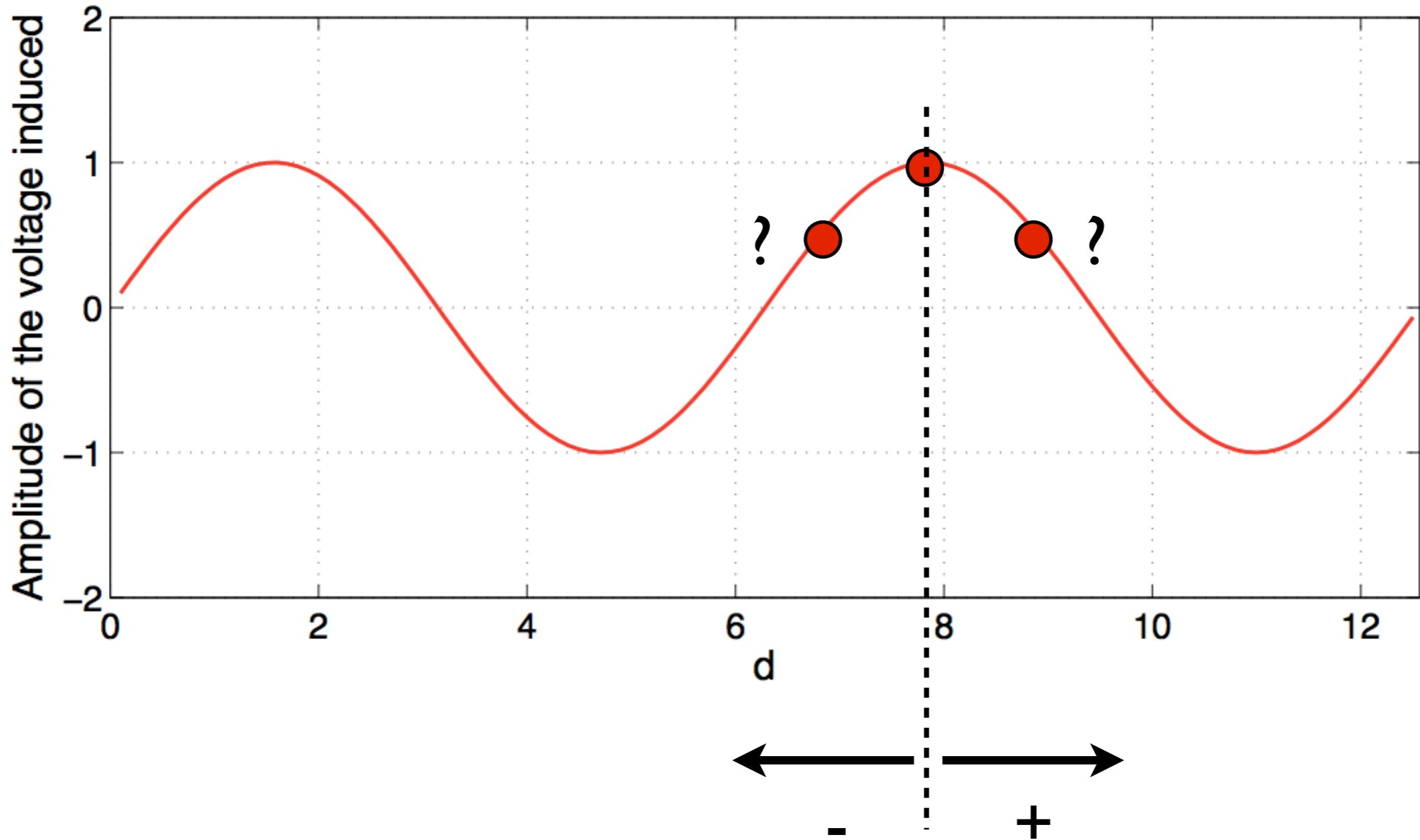
The flux is **ZERO**





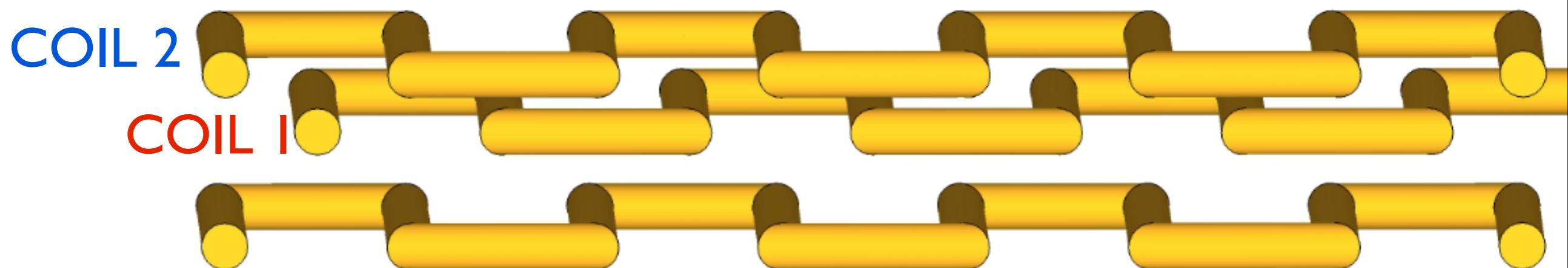
# Inductosyn

## - problem -



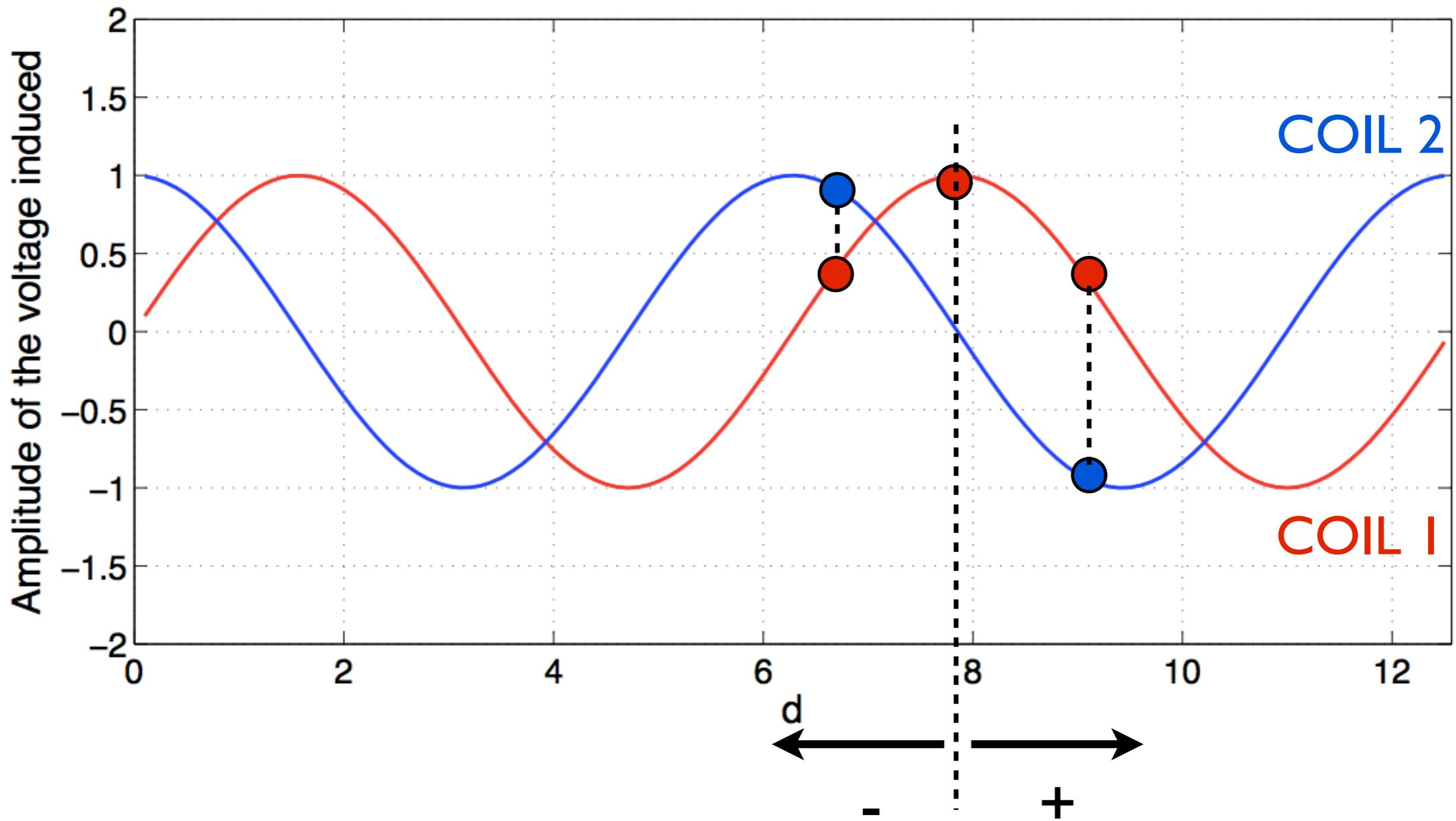
# Inductosyn

- solution -

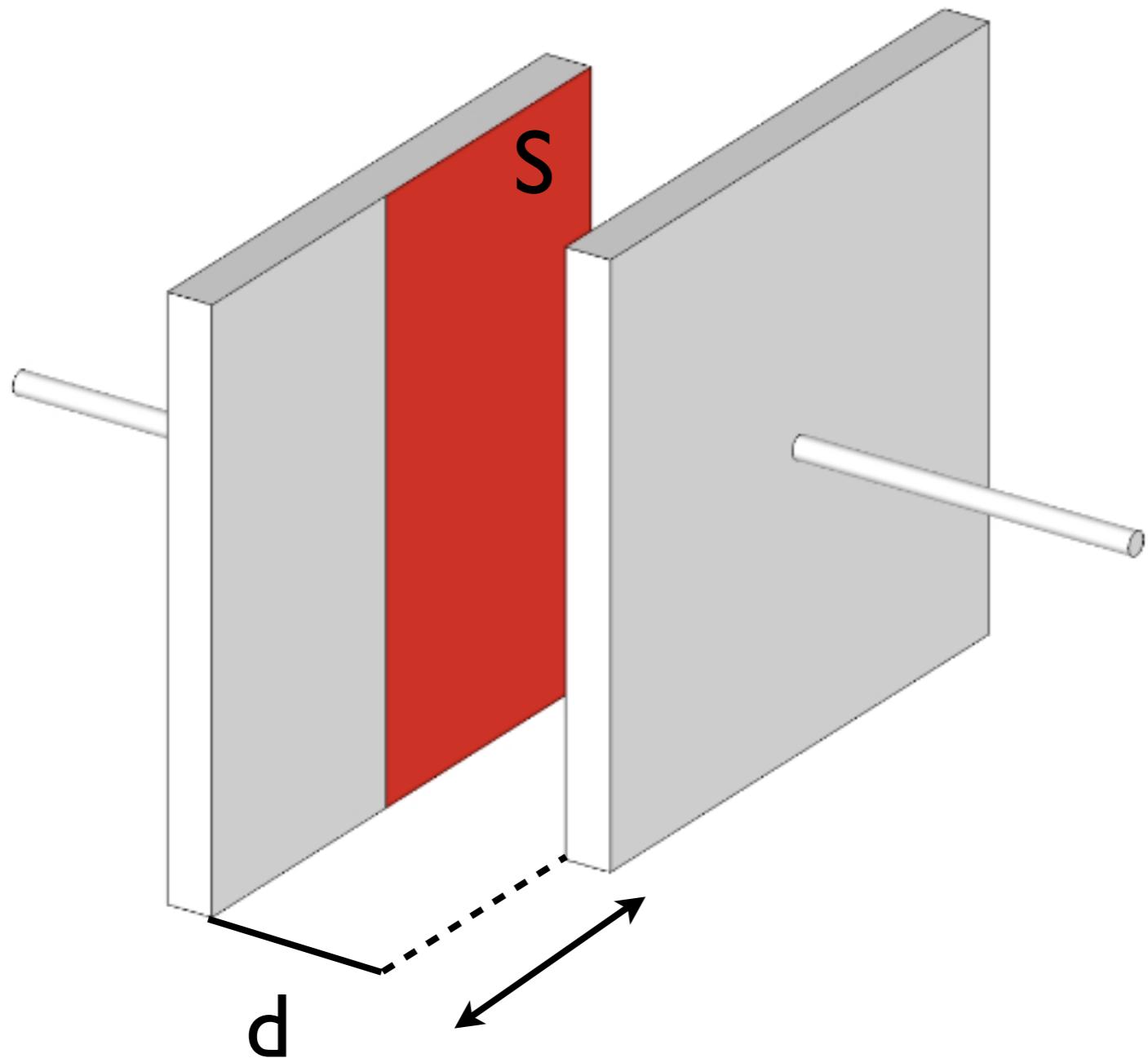


# Inductosyn

- solution -

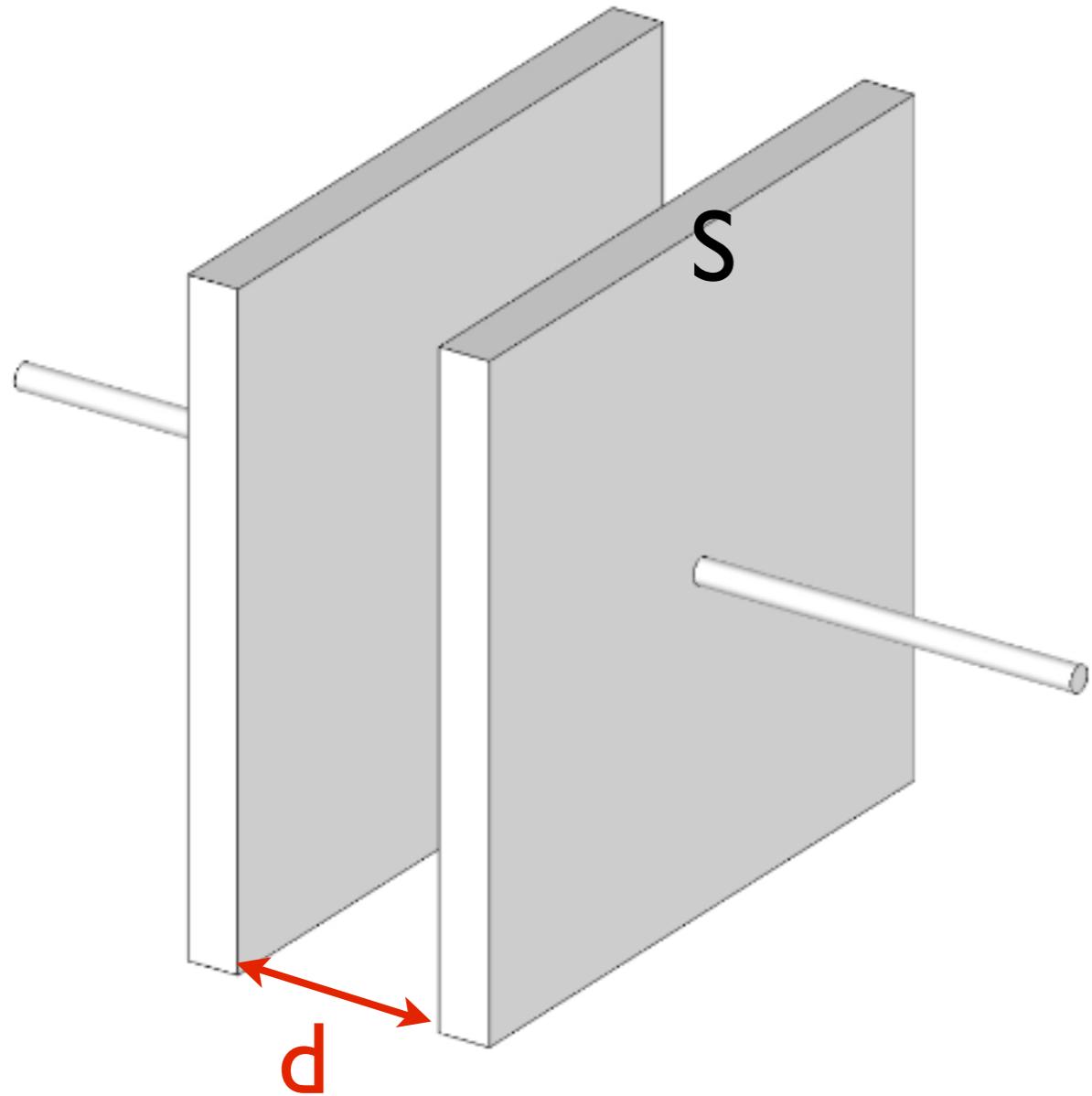


# Capacitive sensor

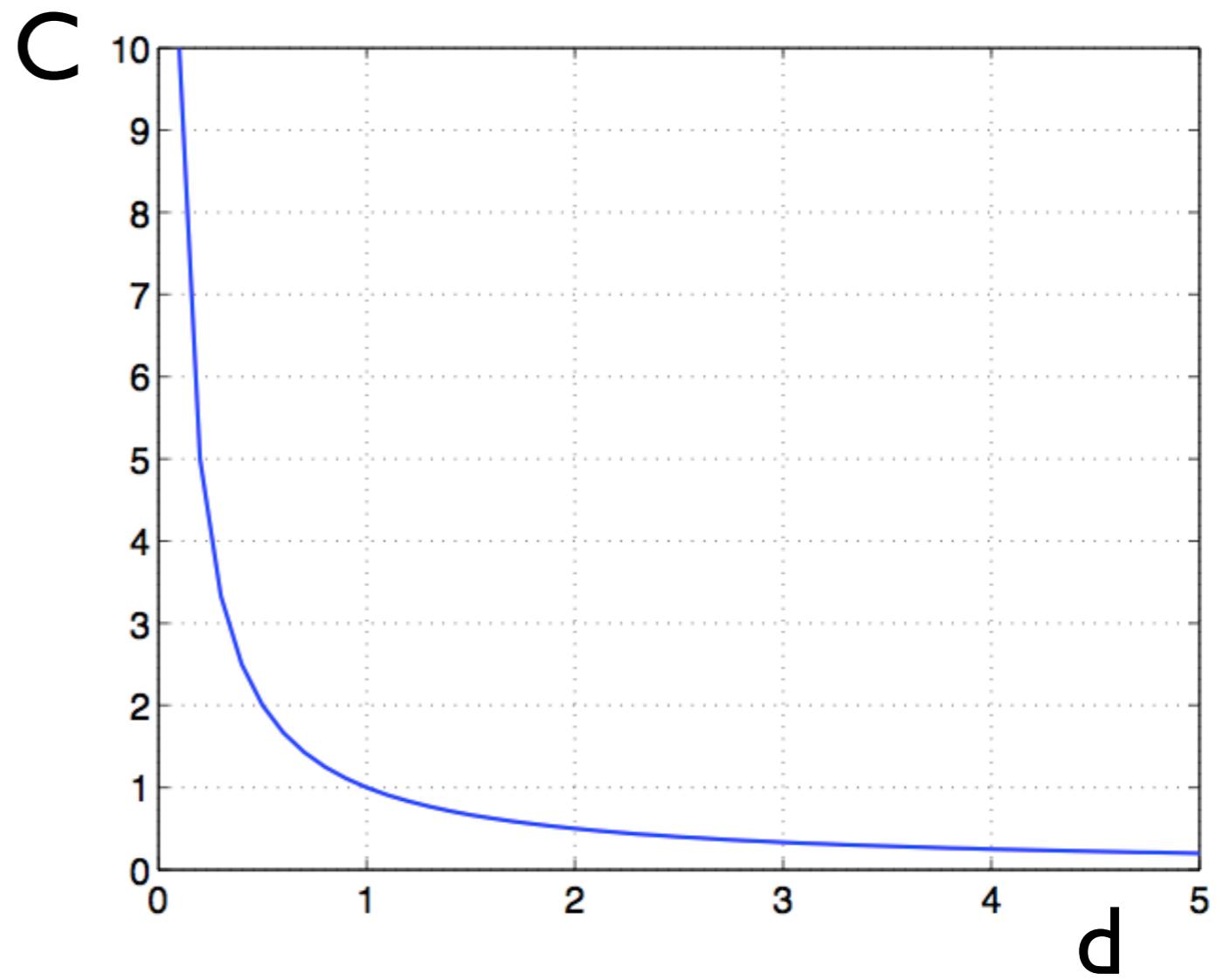


$$C = \epsilon \frac{S}{d}$$

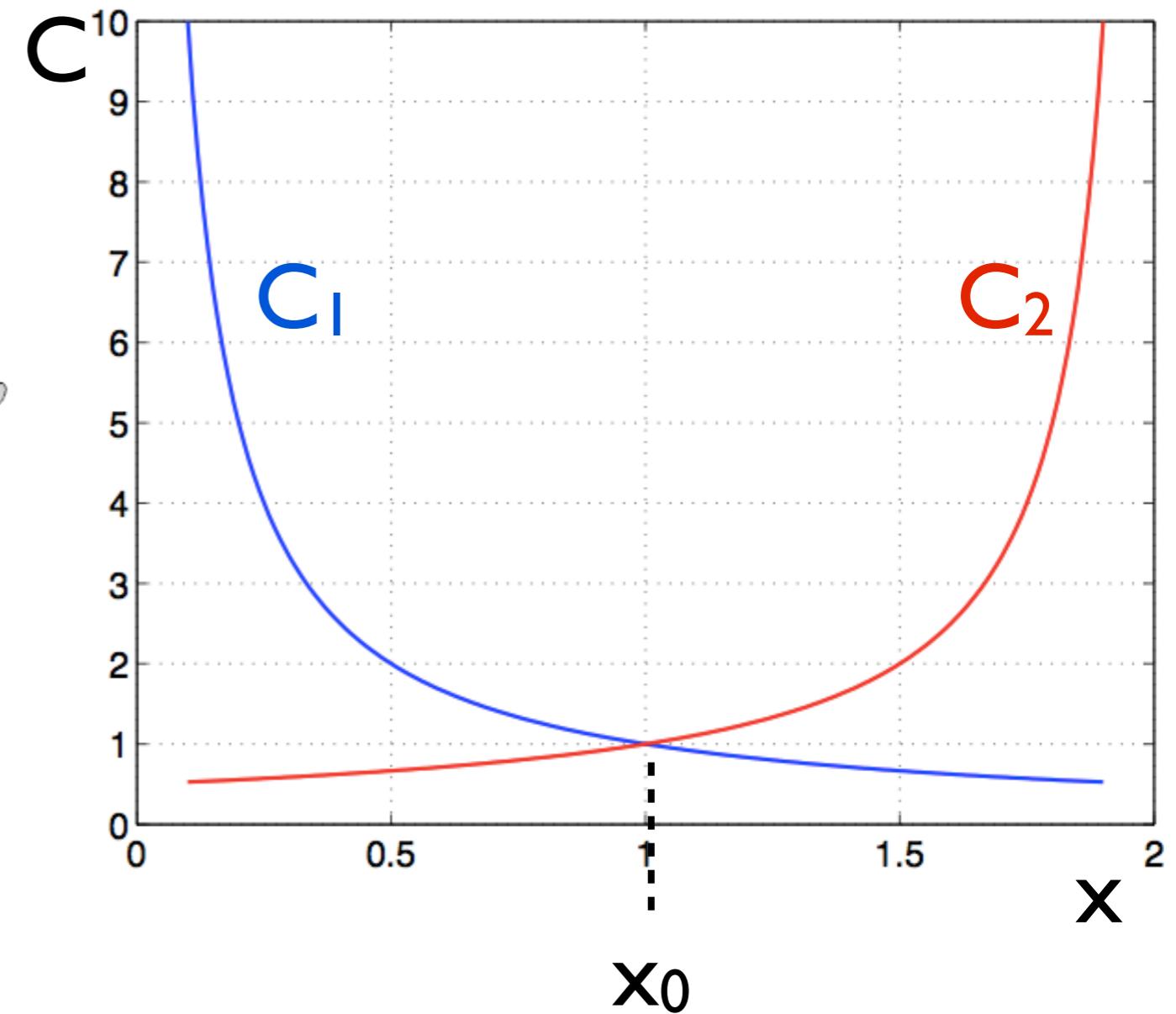
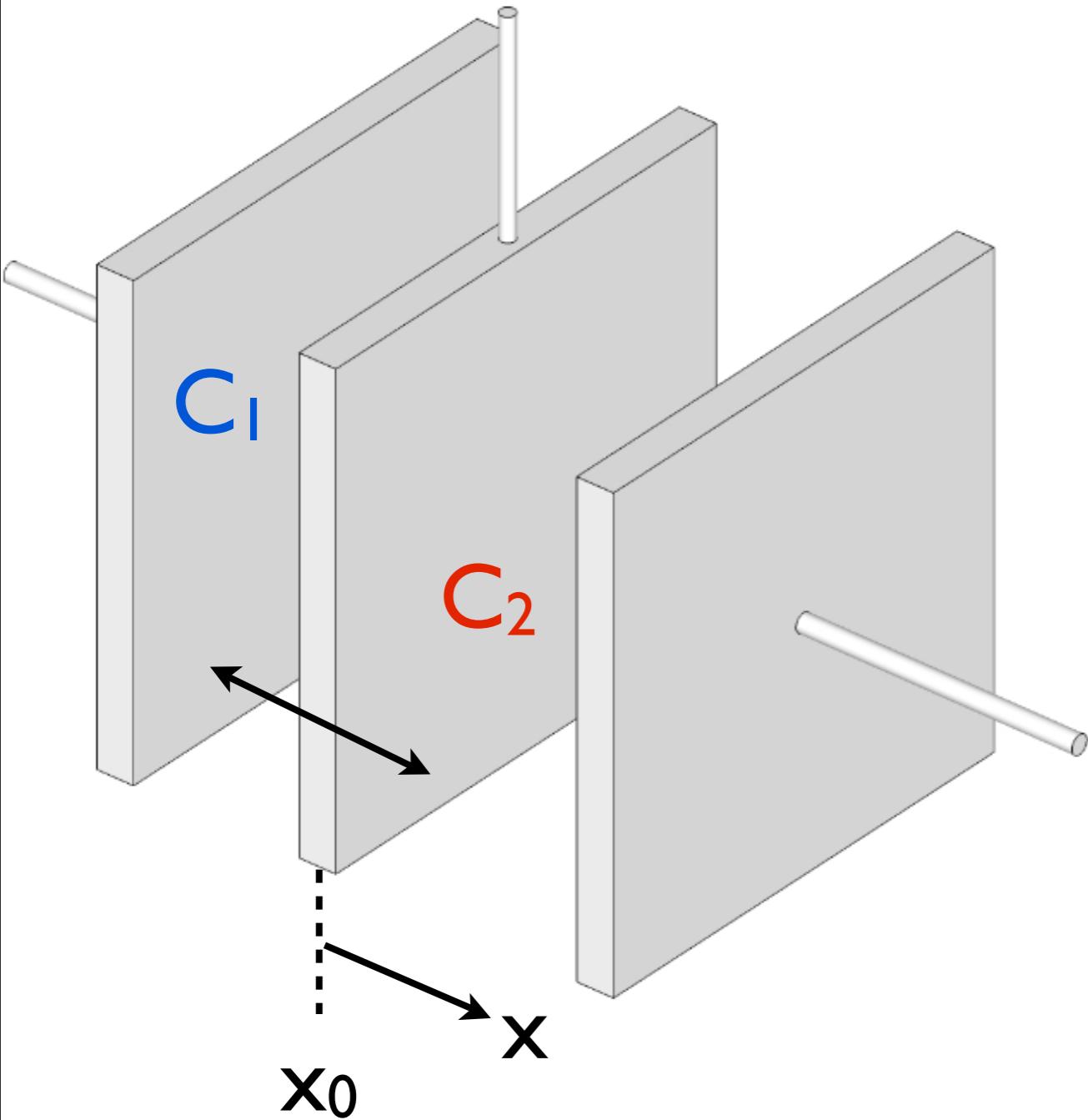
# Capacitive sensor



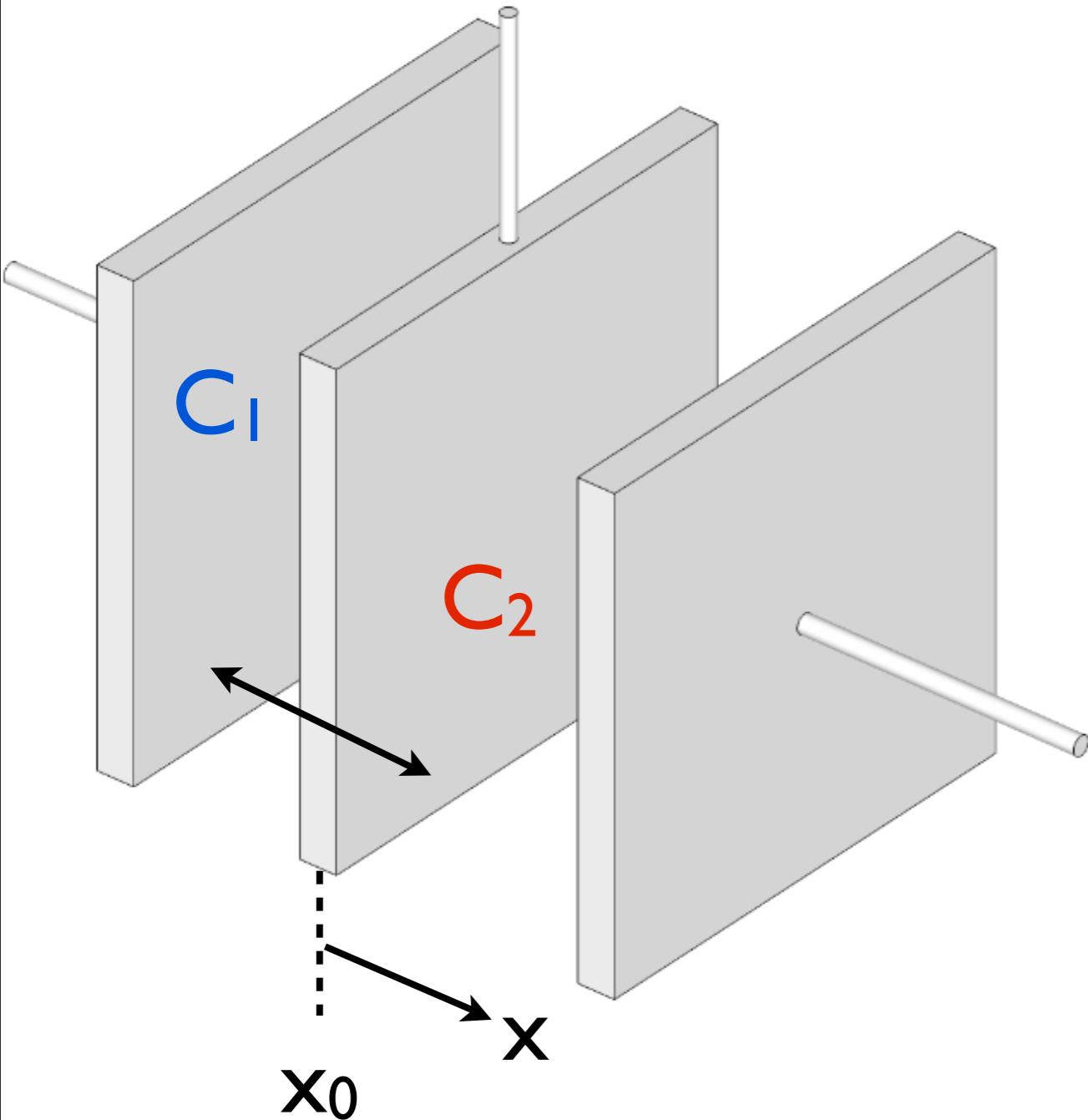
$$C = \epsilon \frac{S}{d}$$



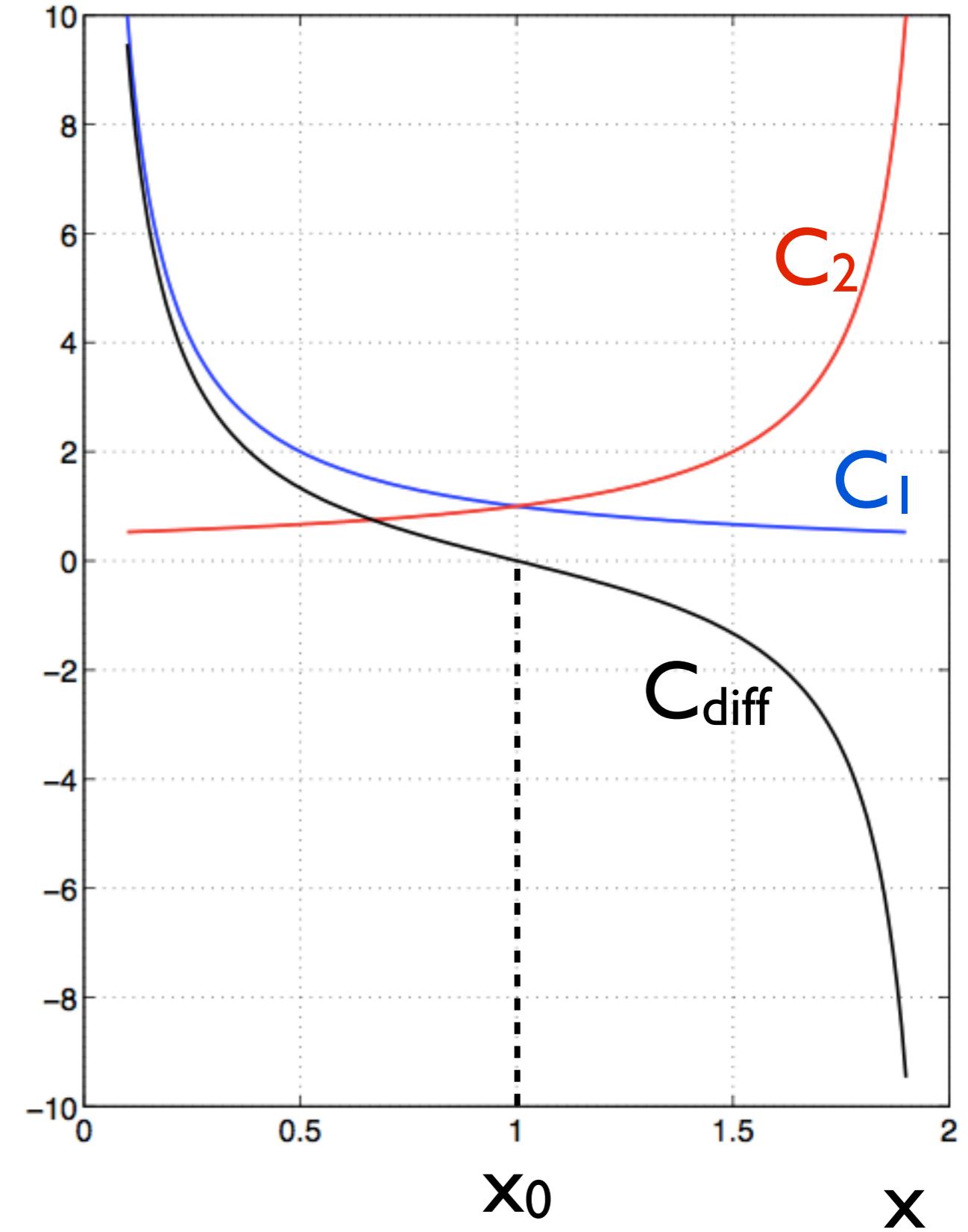
# Capacitive sensor



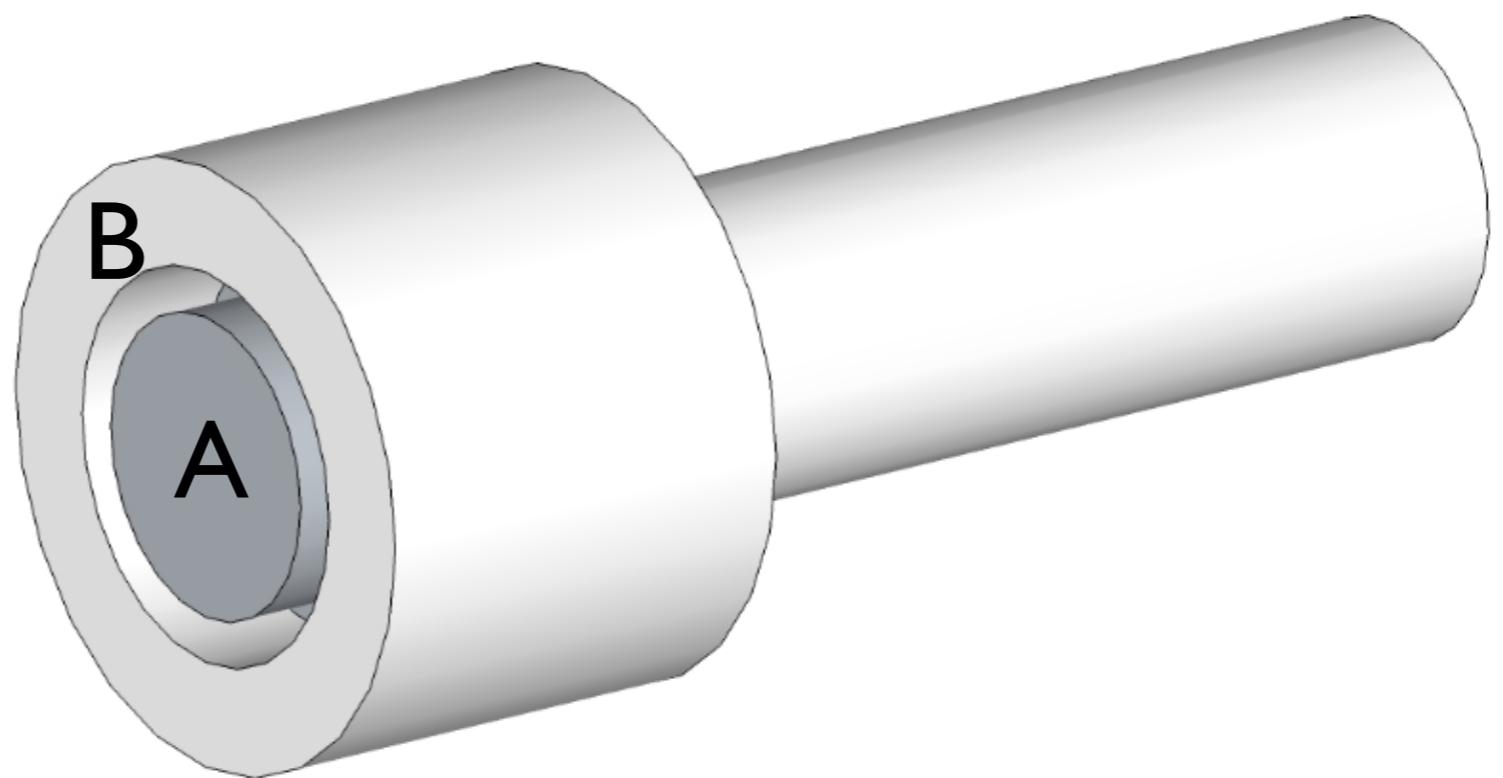
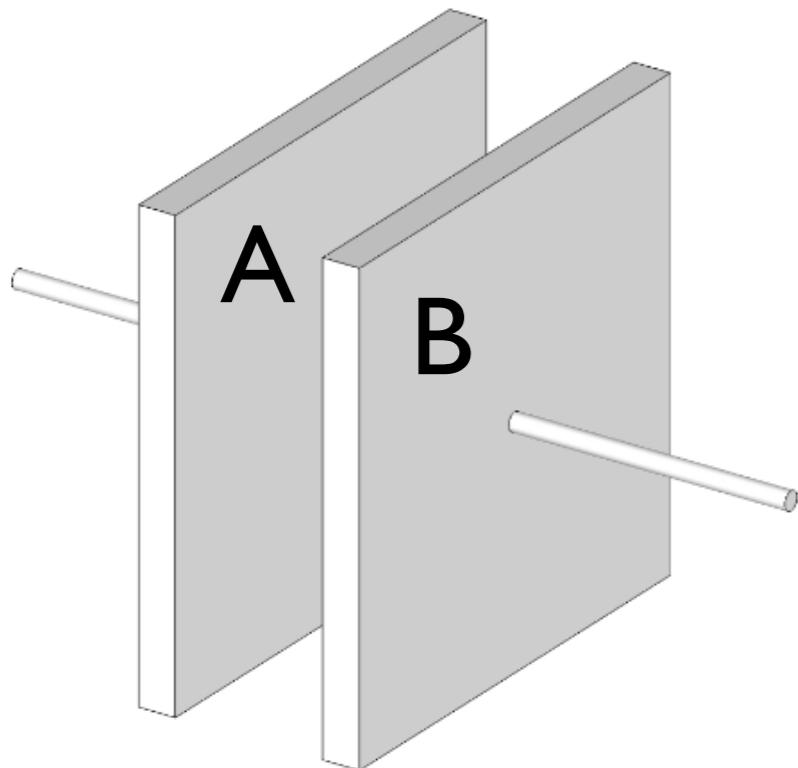
# Capacitive sensor



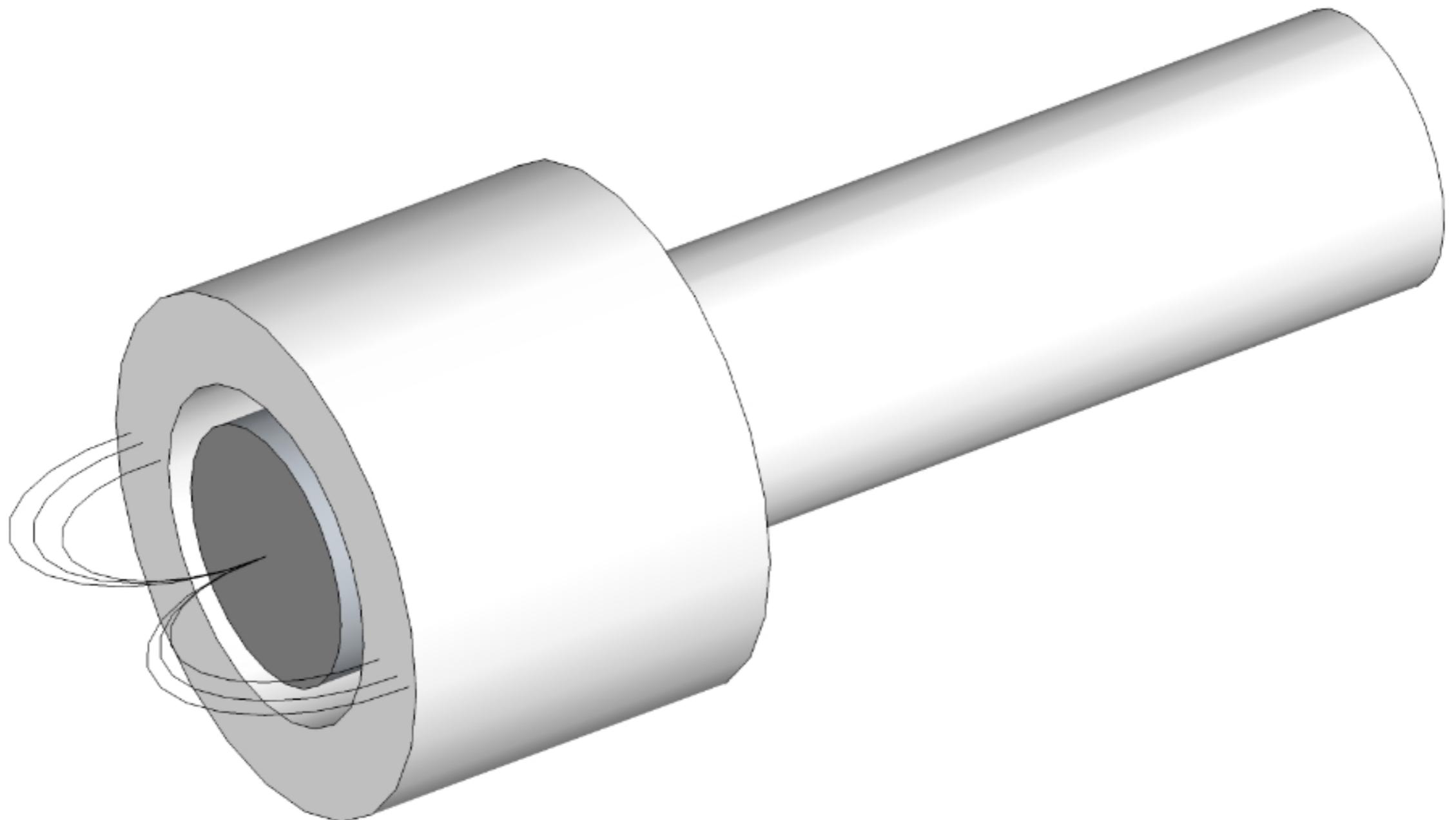
$$C_{\text{diff}} = C_1 - C_2$$



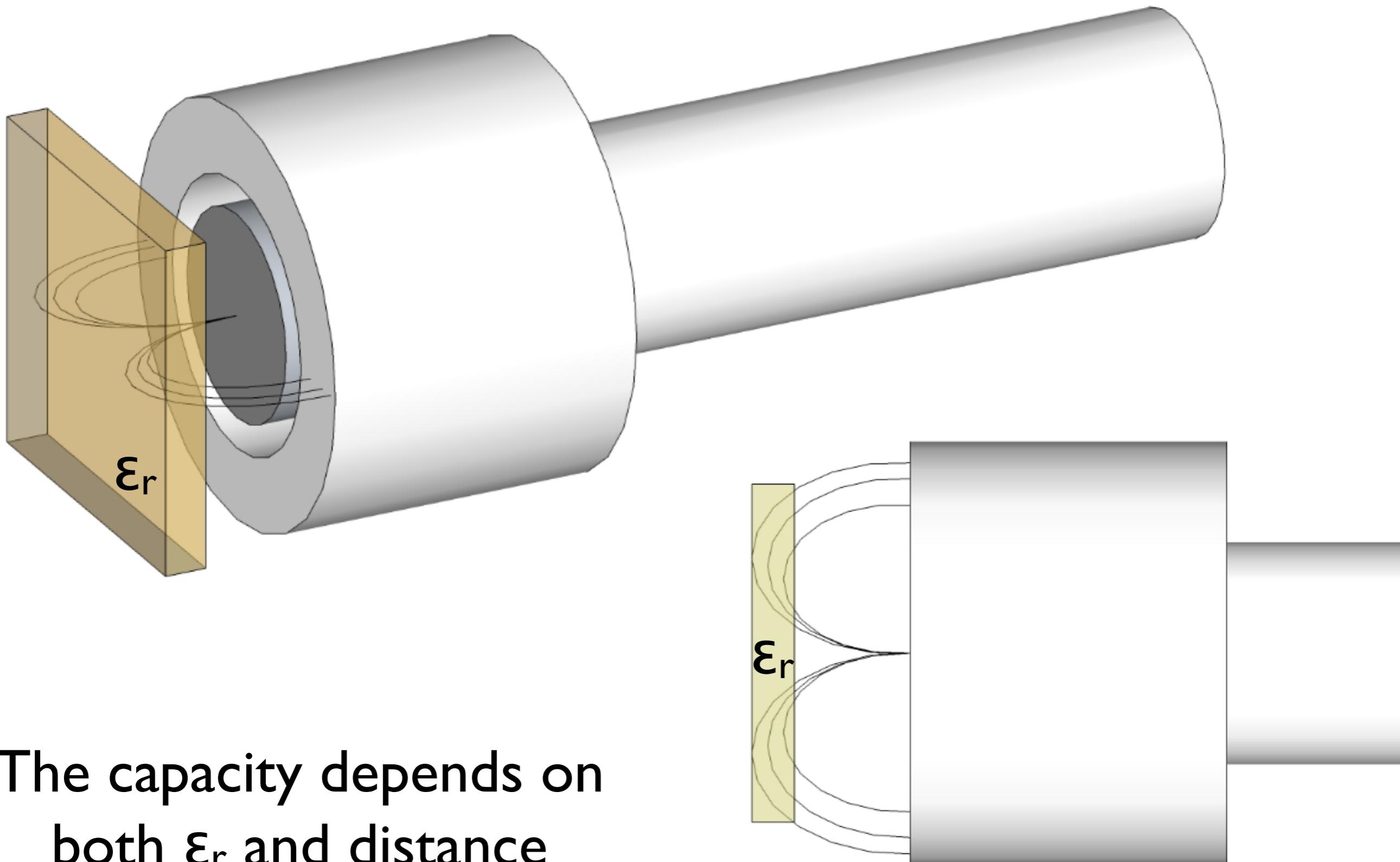
# Capacitive Proximity sensor



# Capacitive Proximity sensor

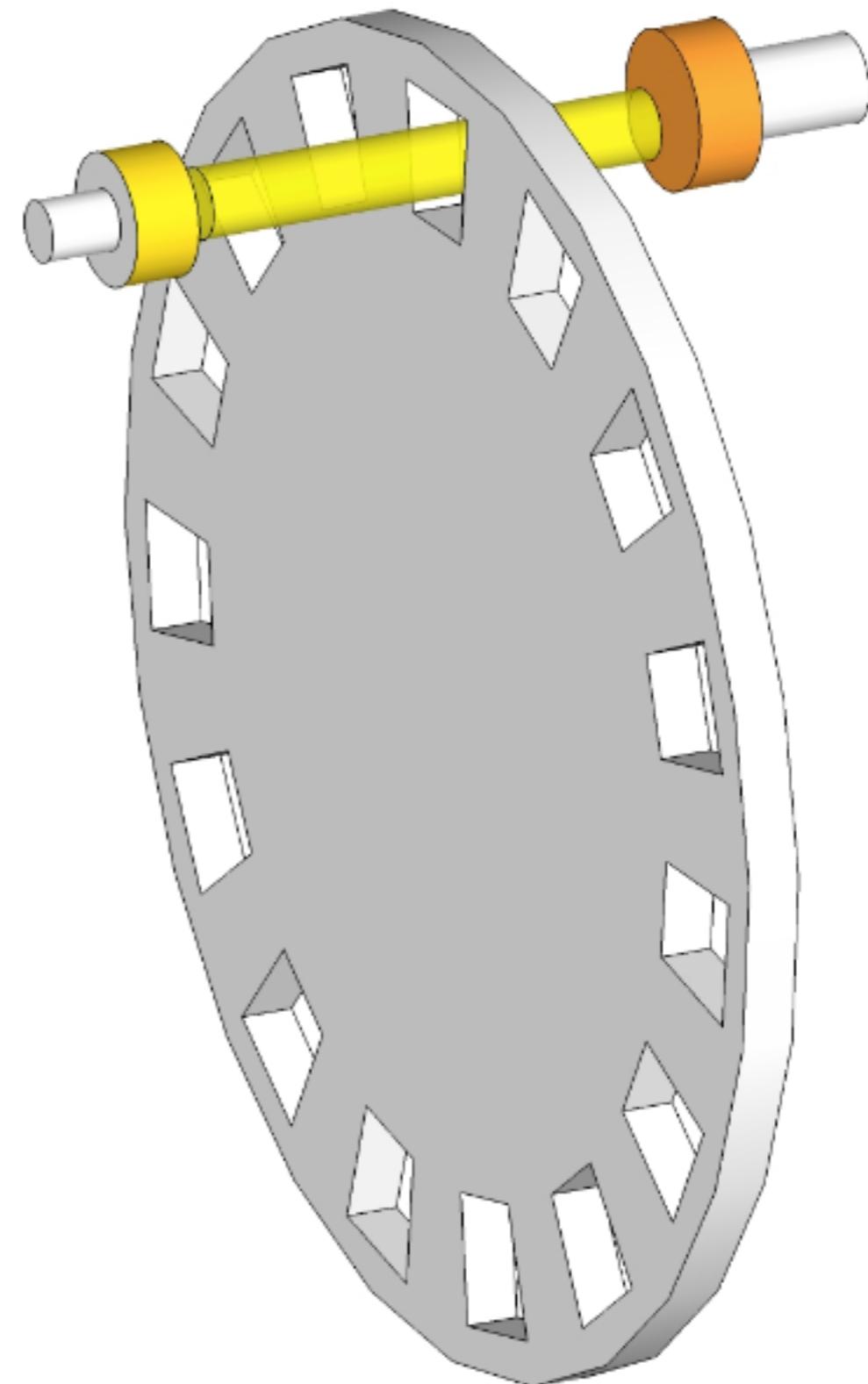
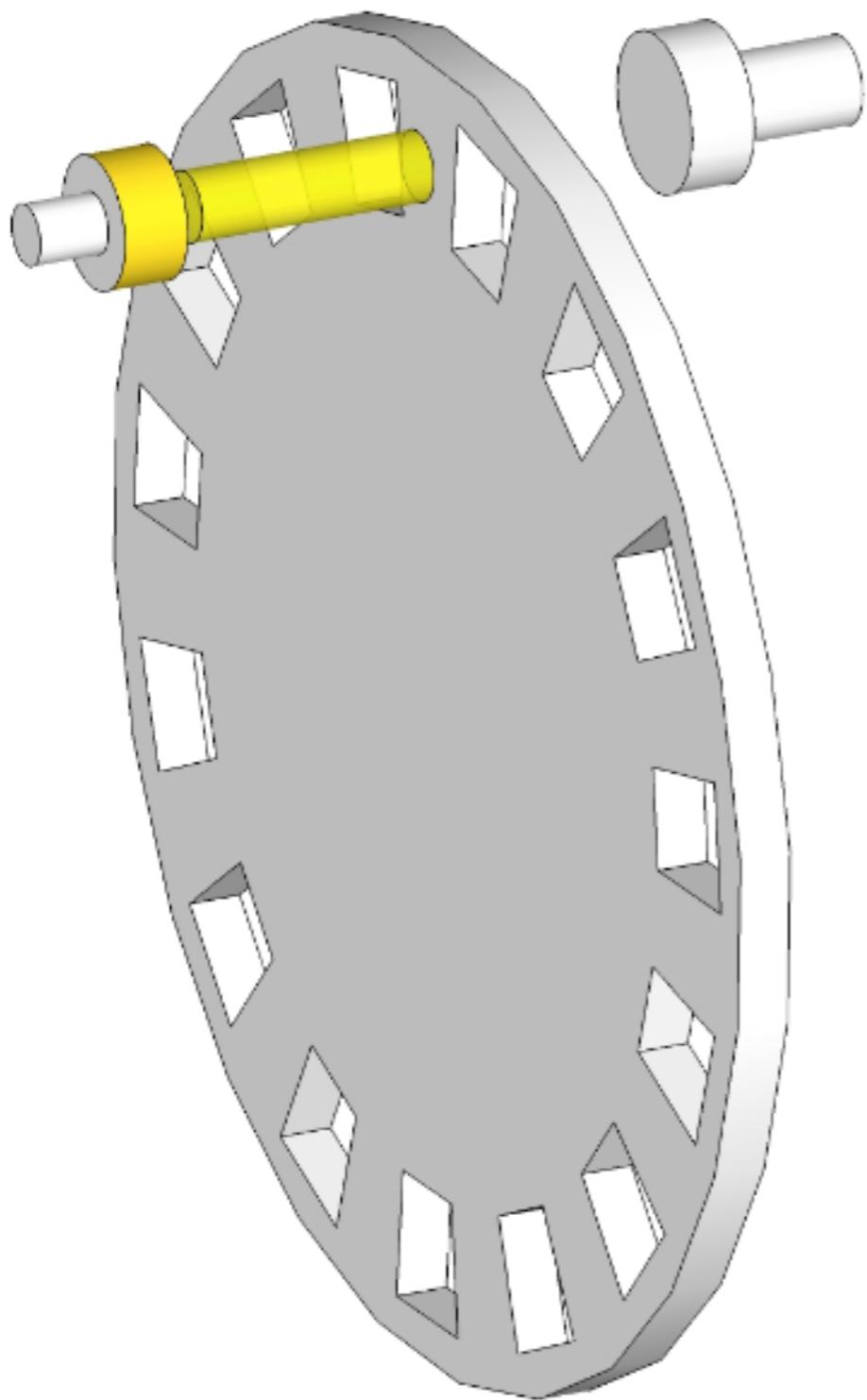


# Capacitive Proximity sensor

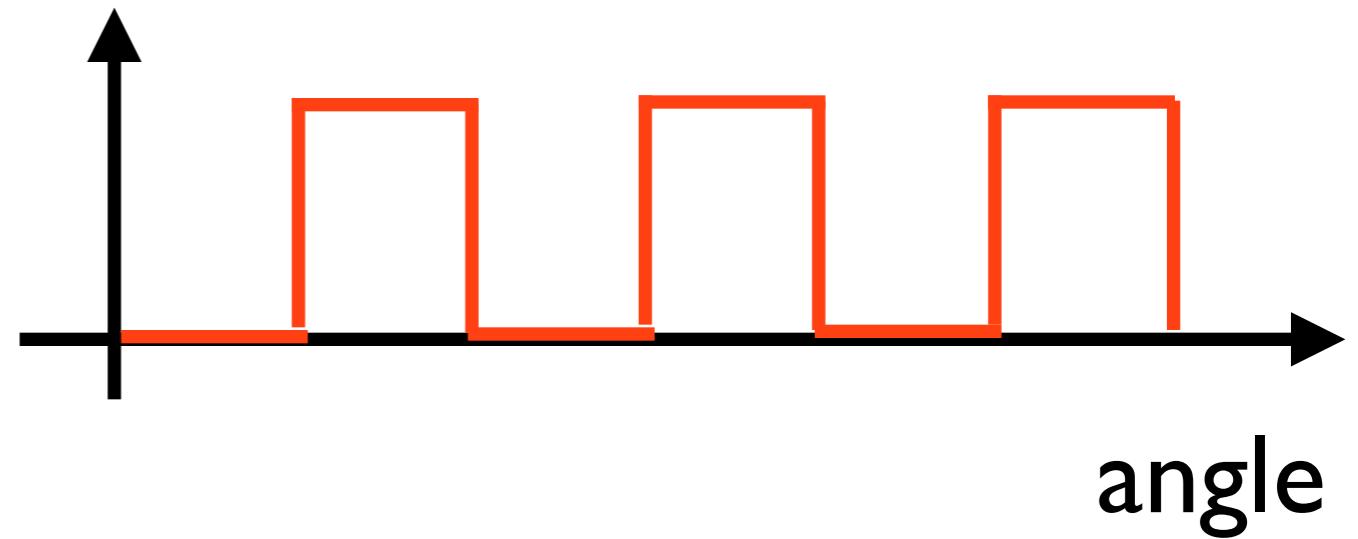
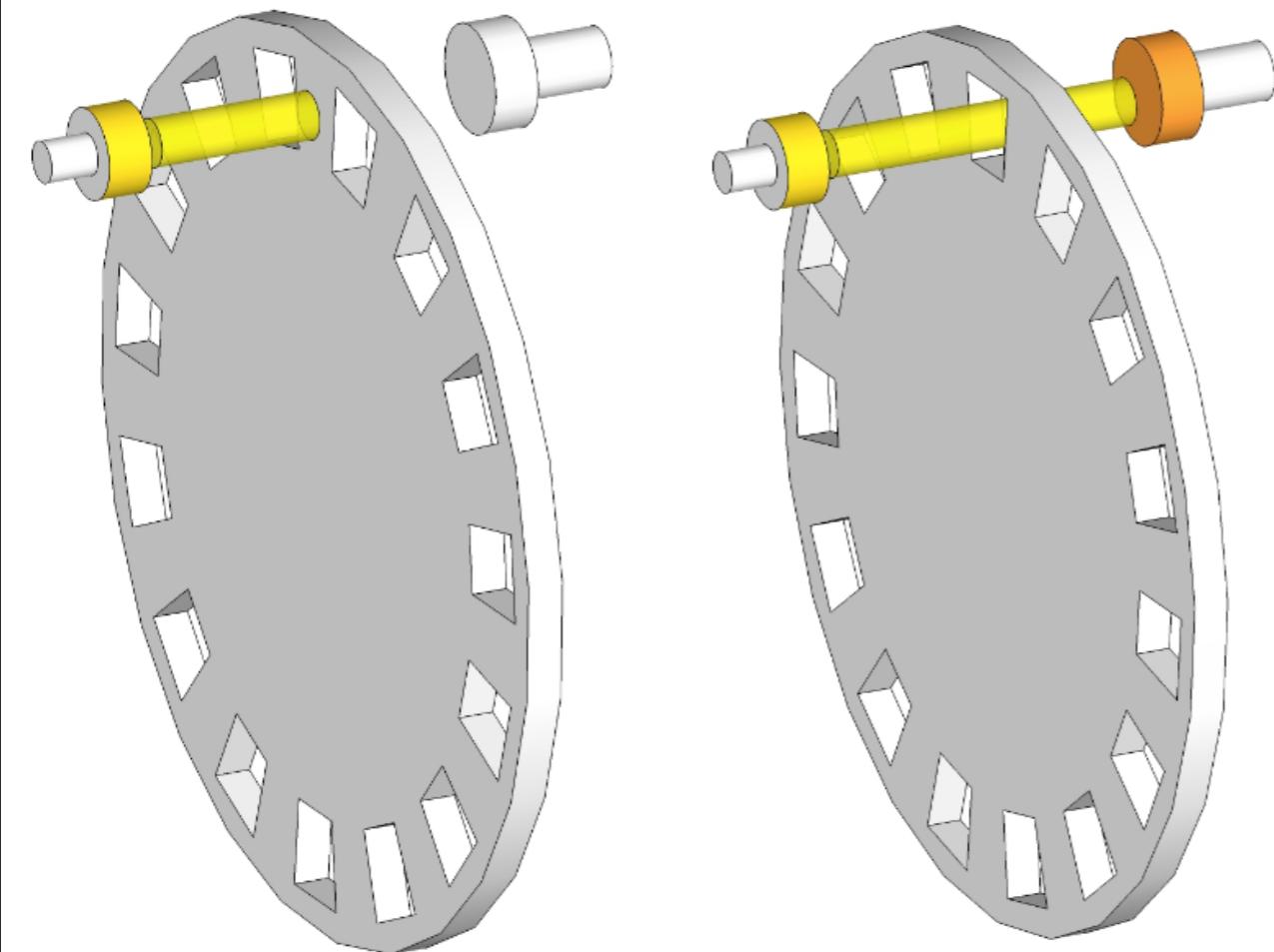


# Incremental optical sensor

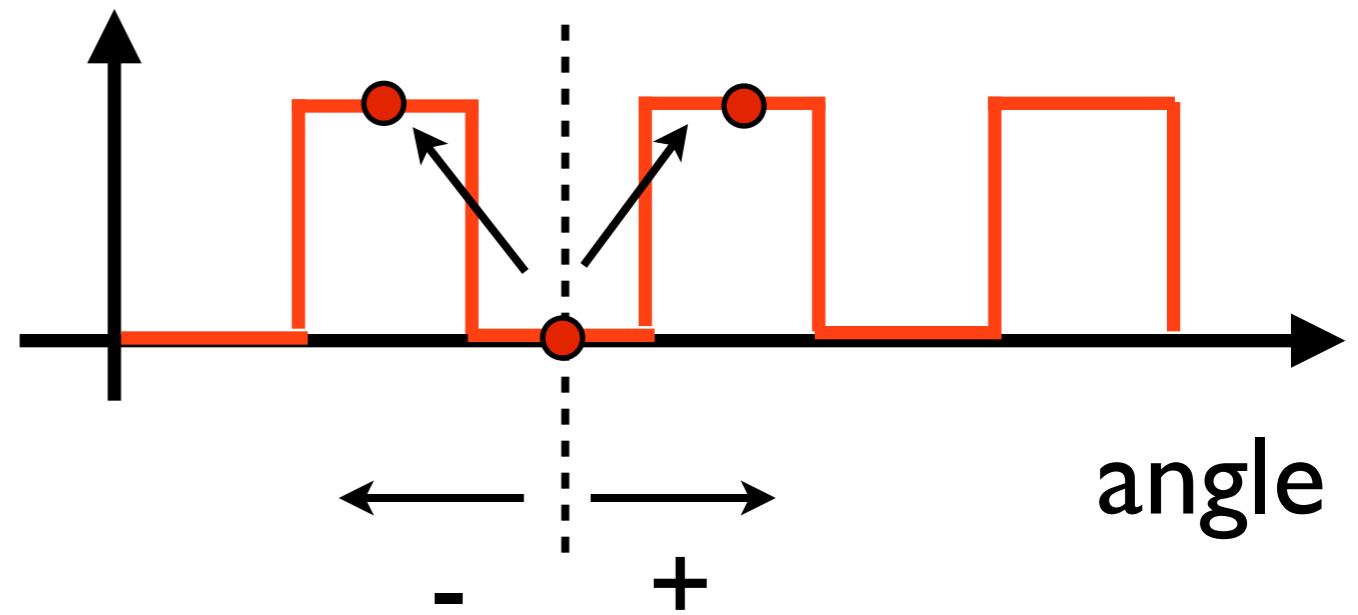
- rotative -



# Incremental optical sensor

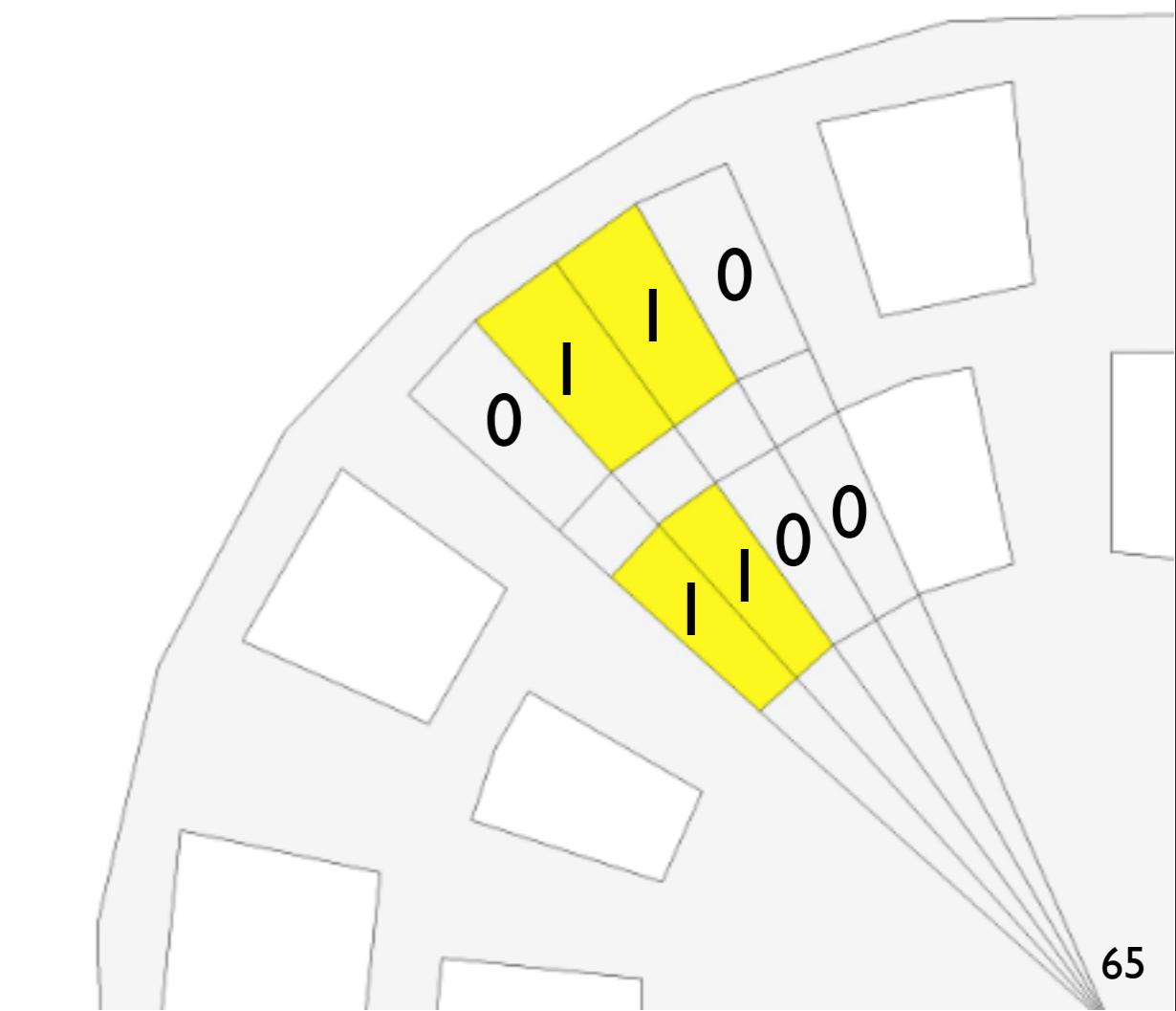
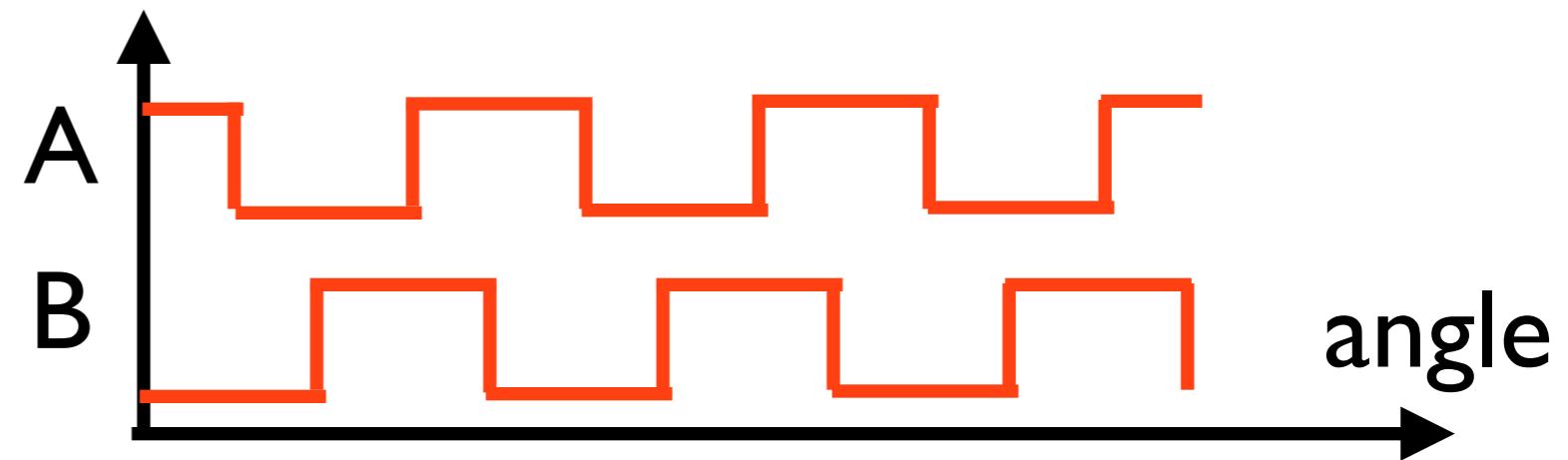
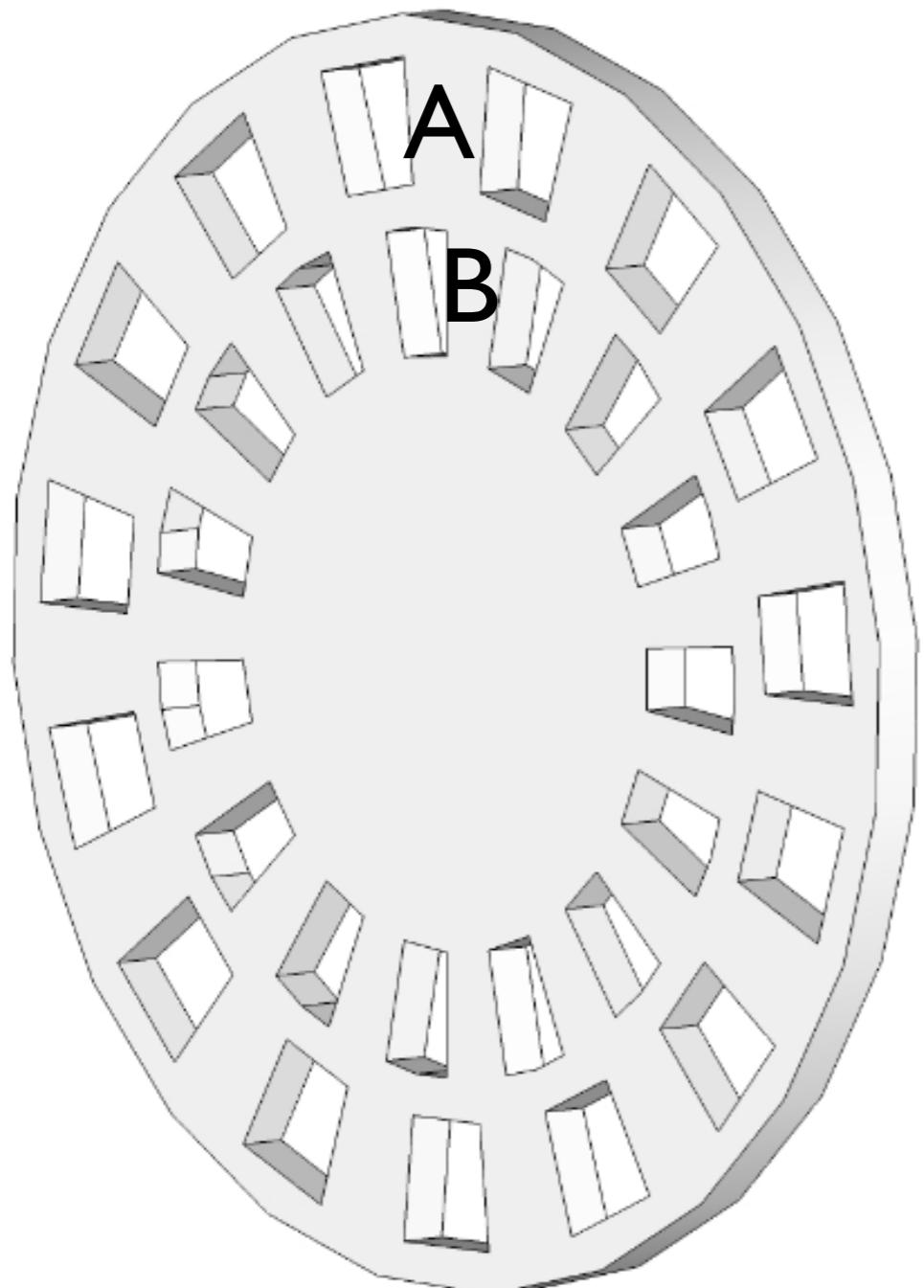


Problem



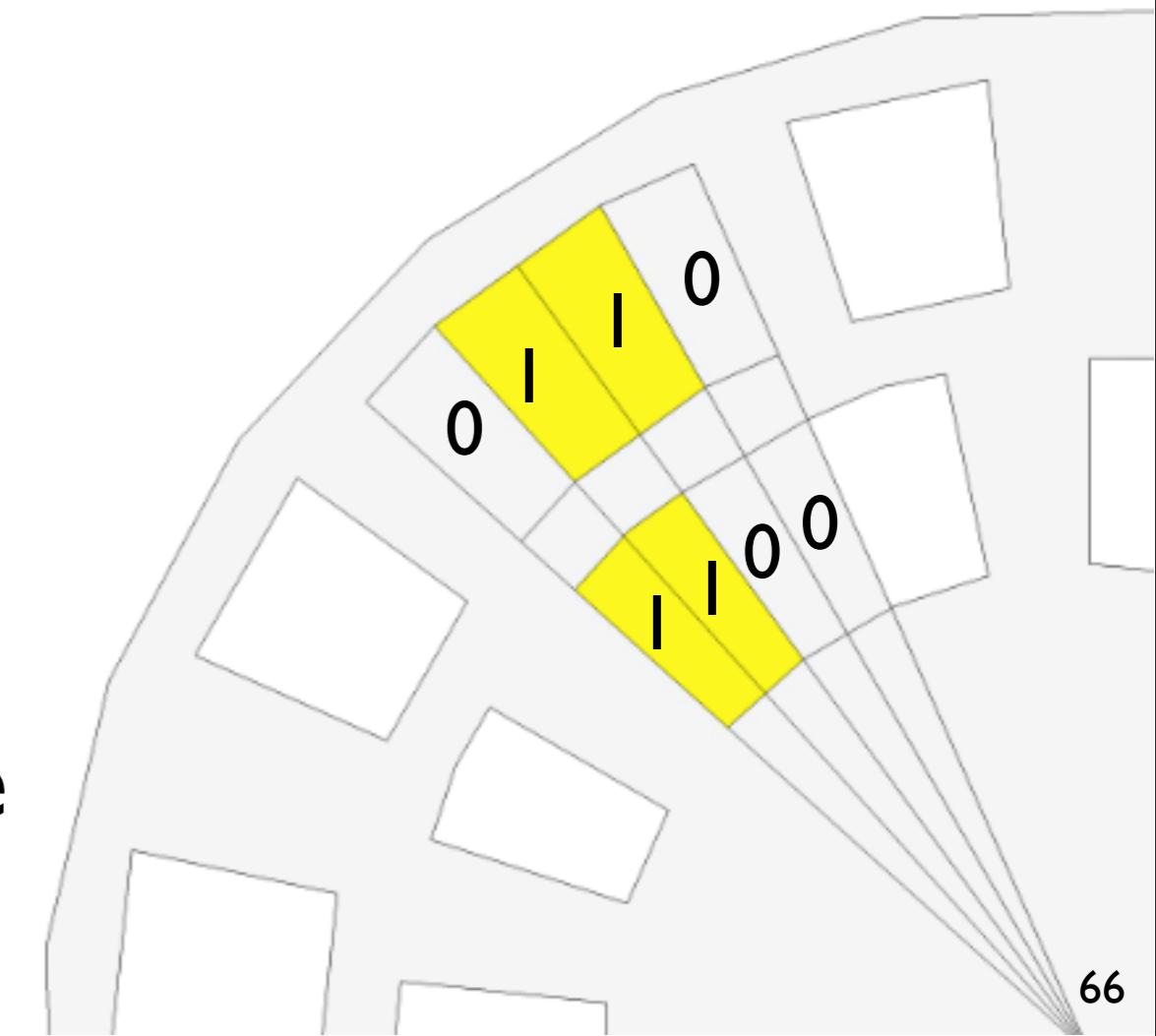
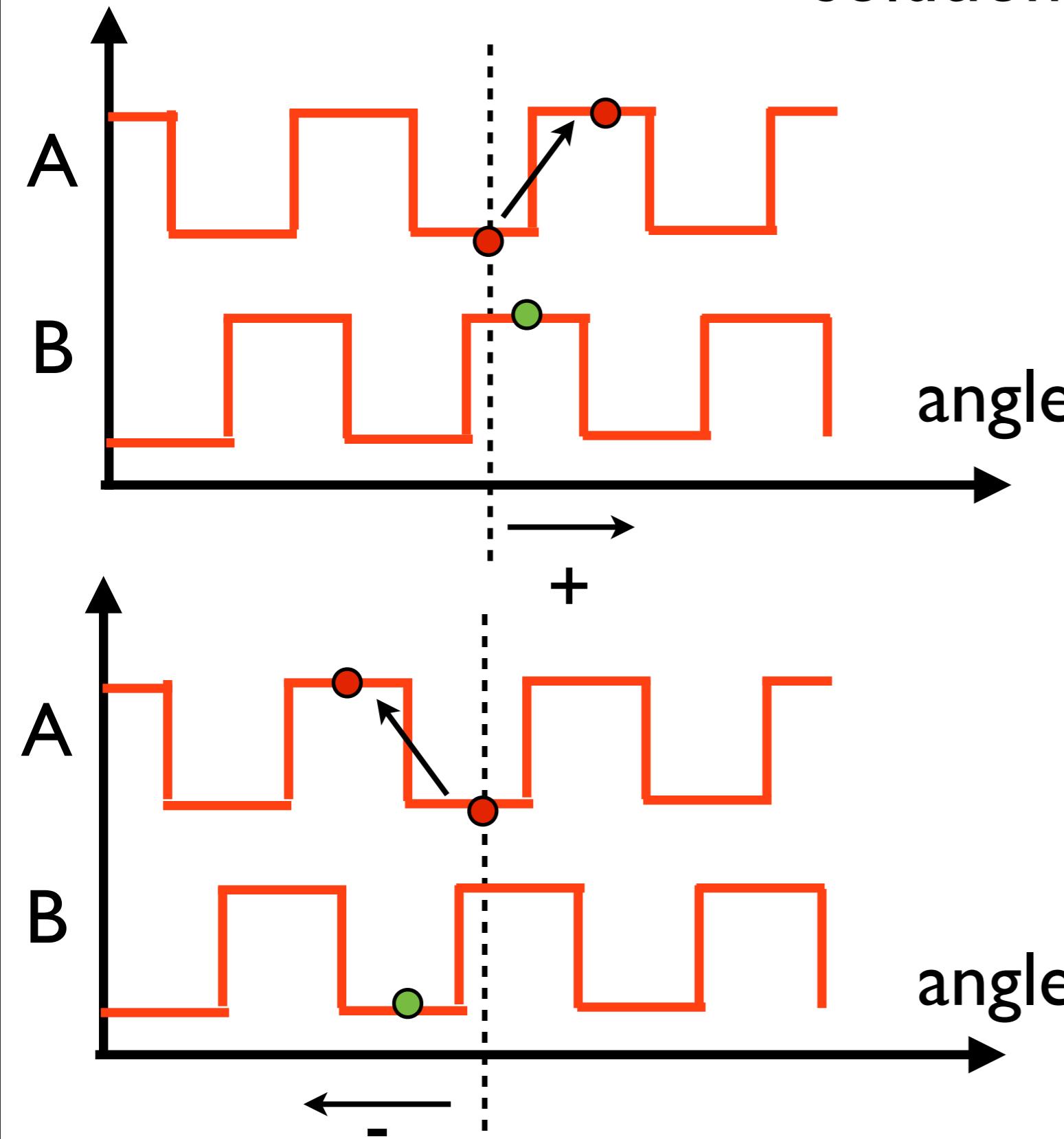
# Incremental optical sensor

- solution -



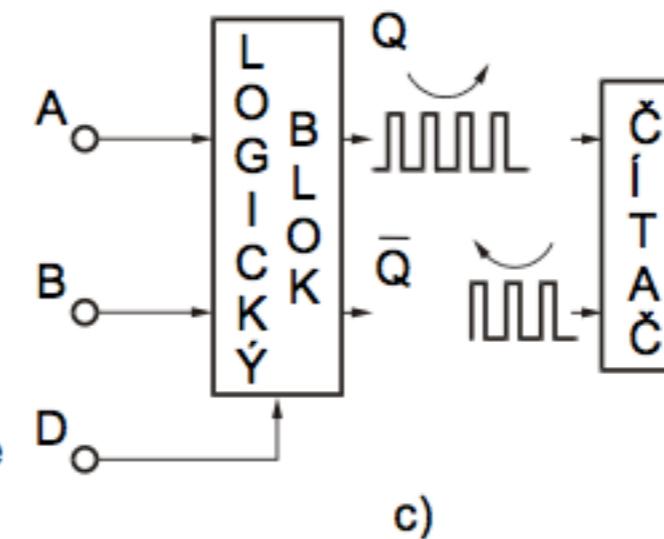
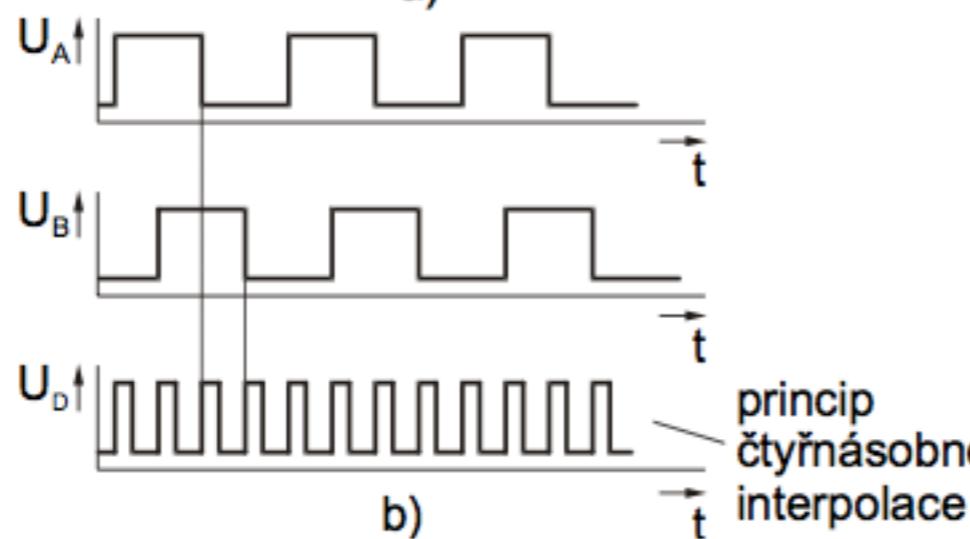
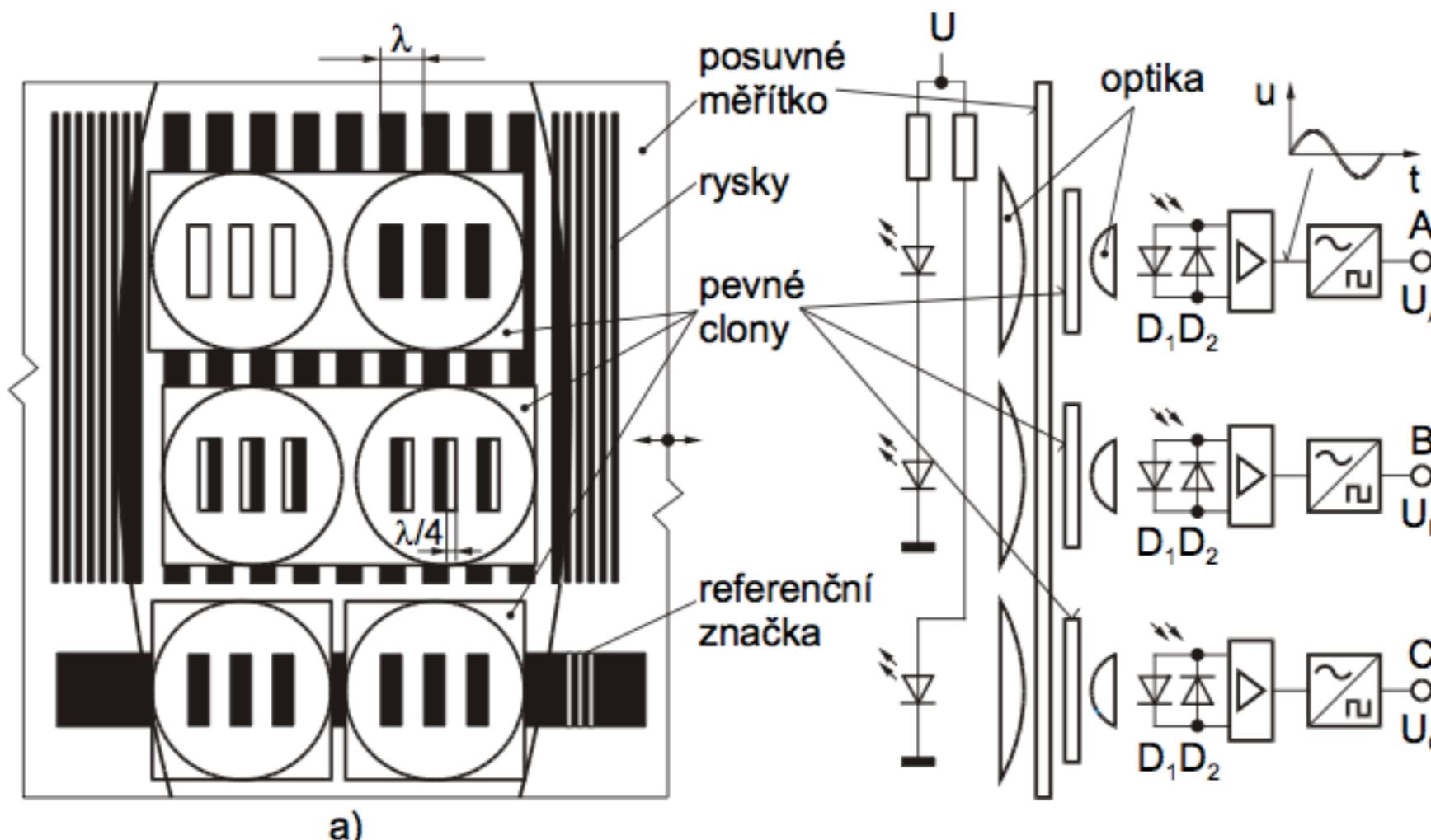
# Incremental optical sensor

- solution -

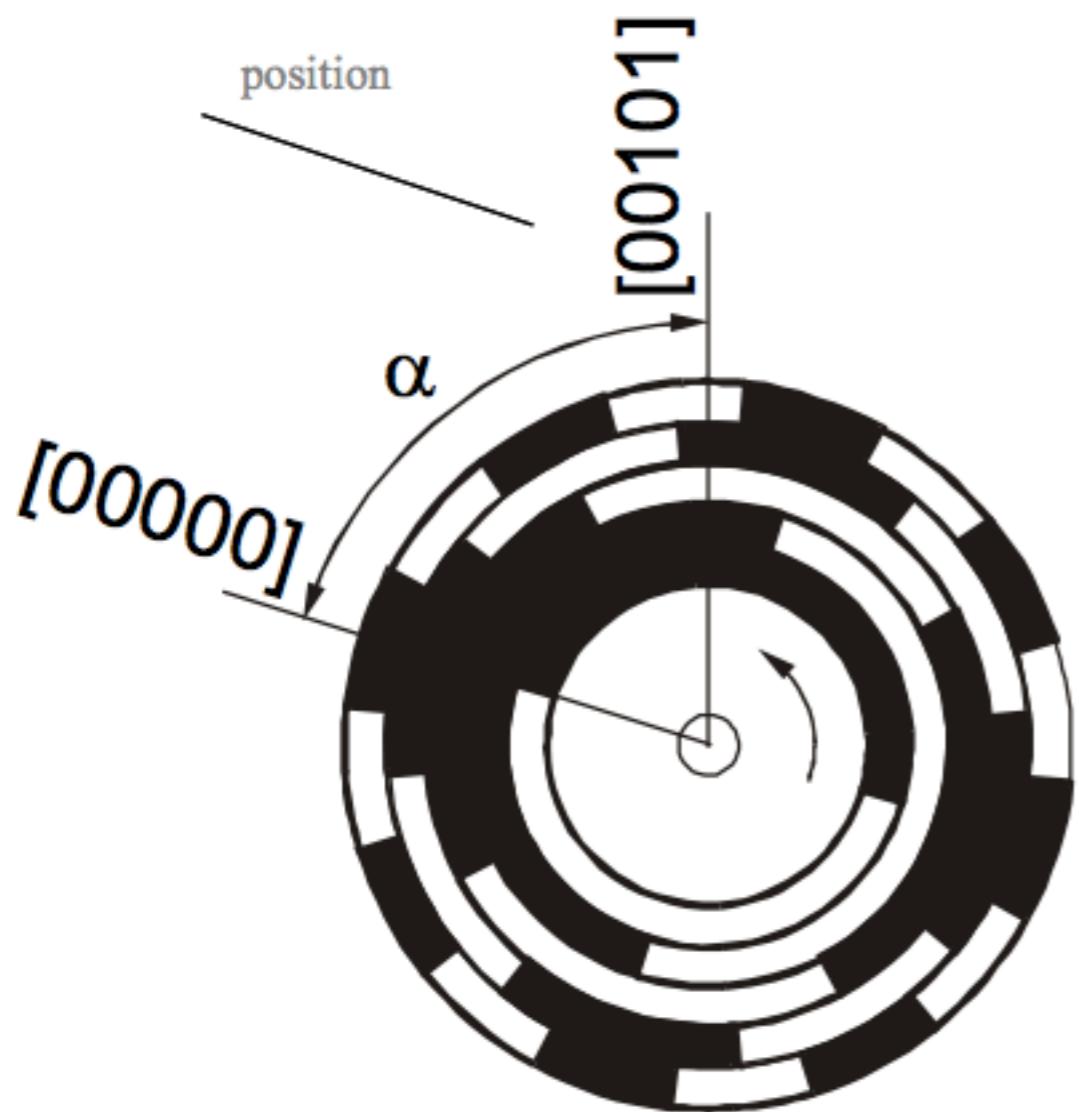


# Incremental optical sensor

- linear -

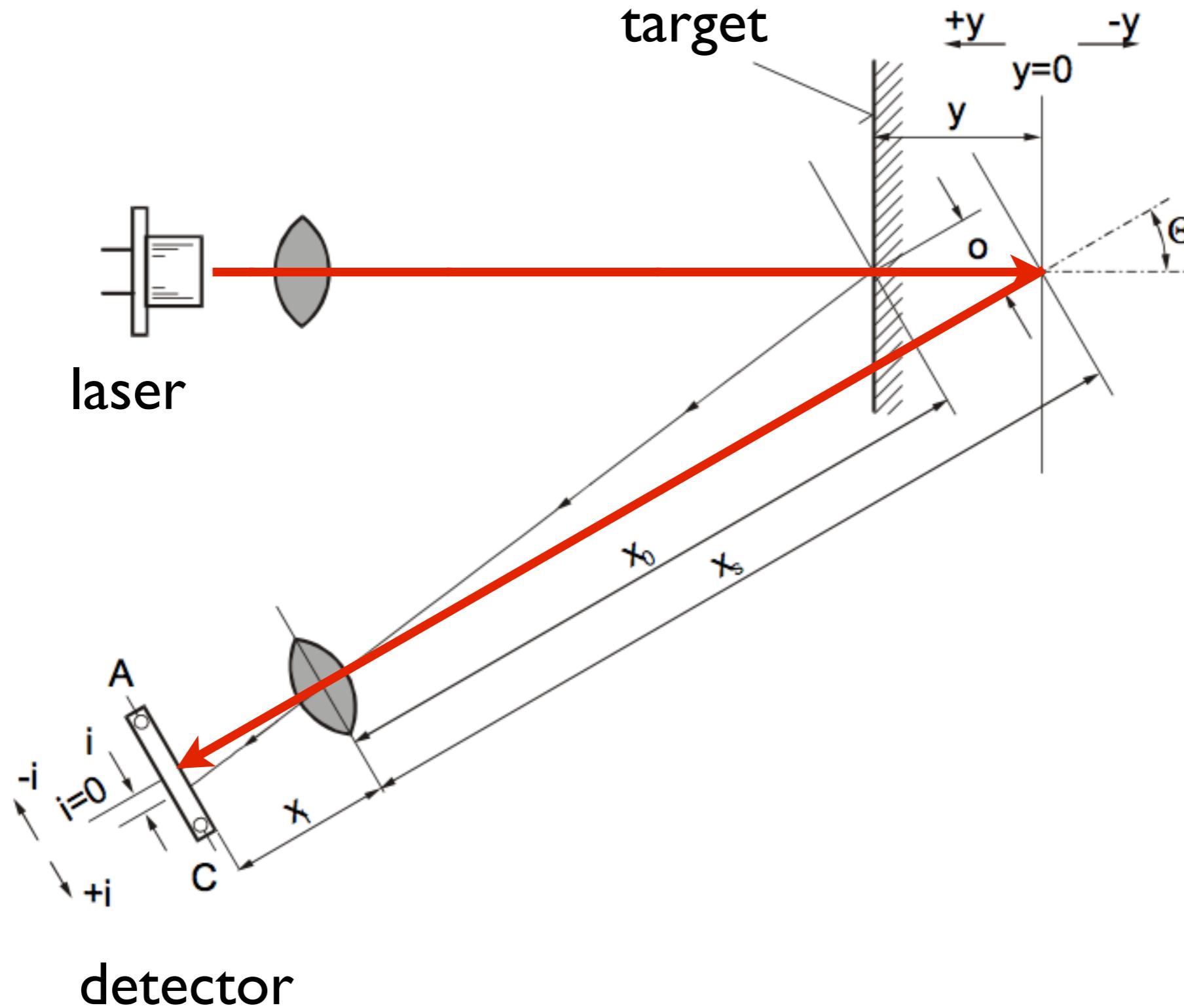


# Absolute optical sensor

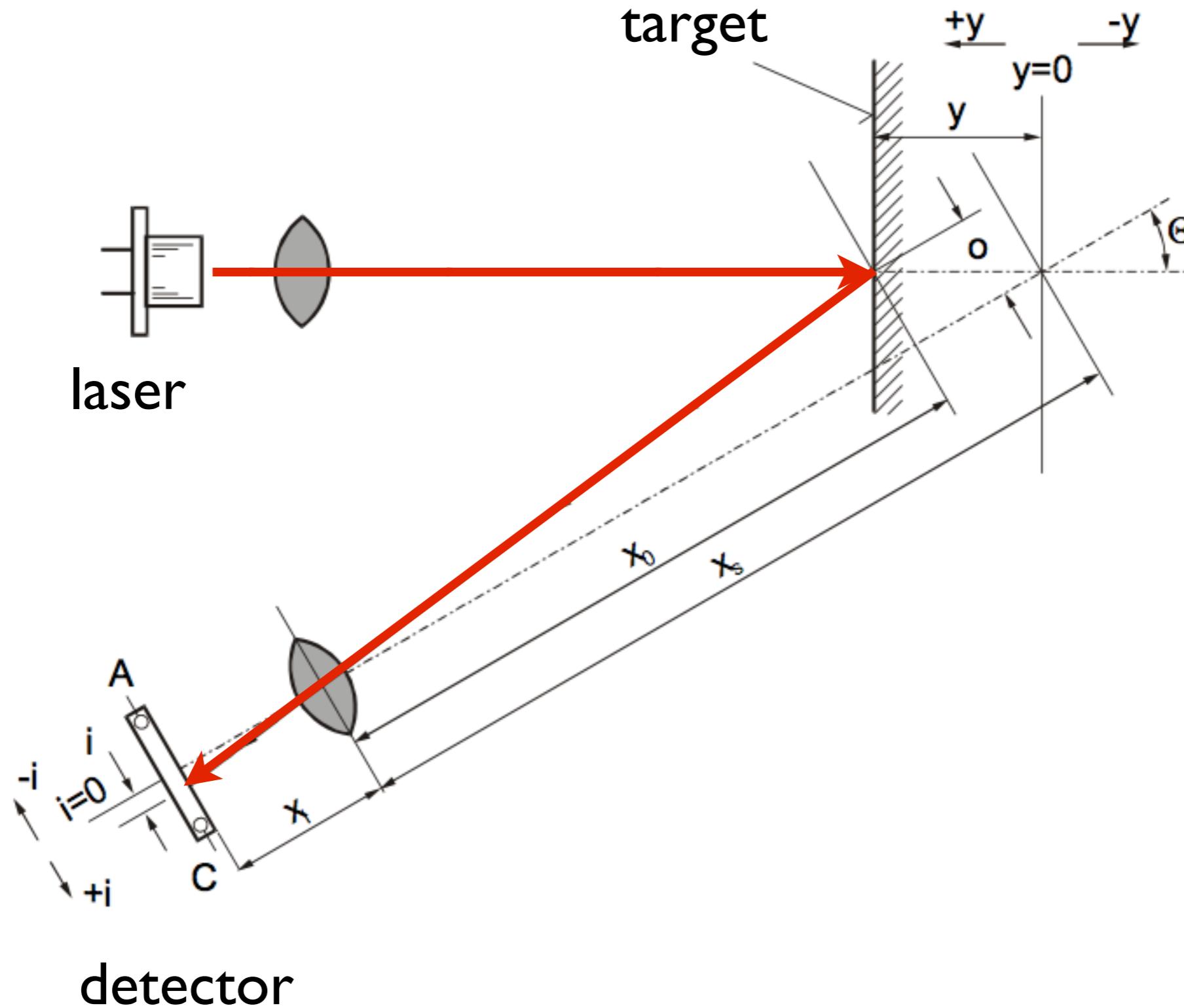


Omron

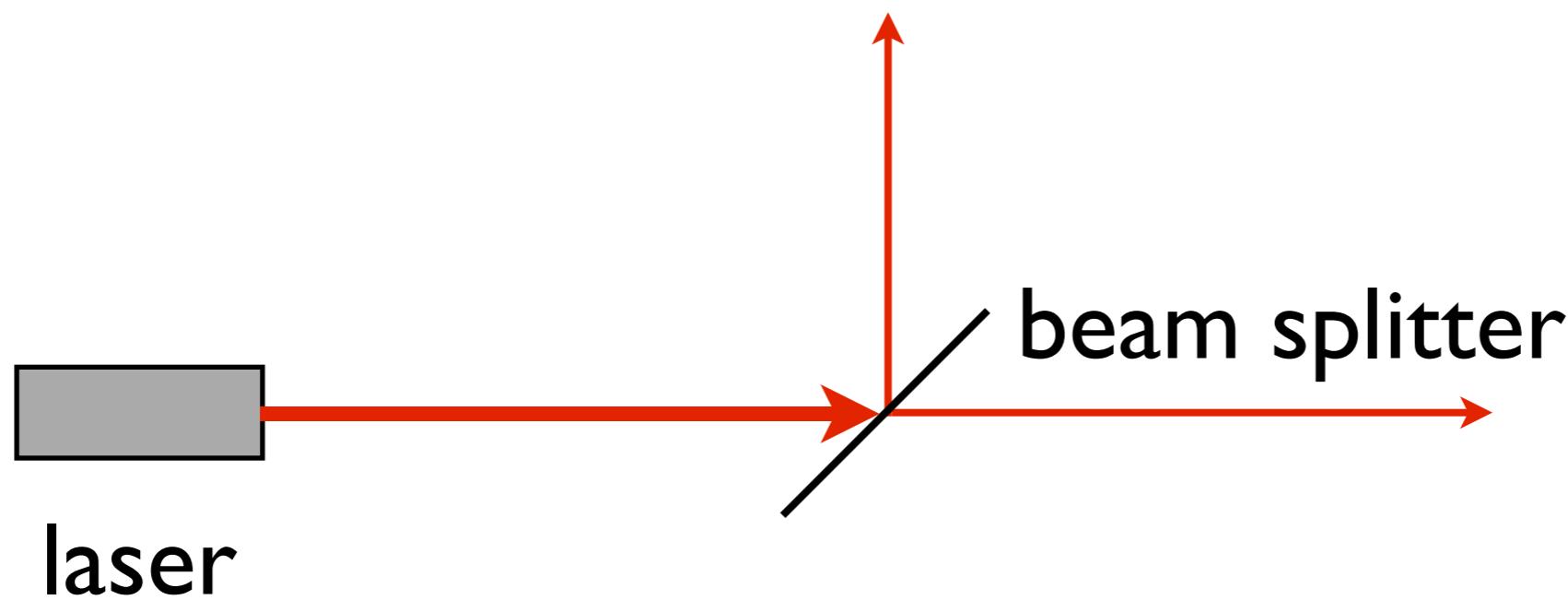
# Triangulation optical sensor



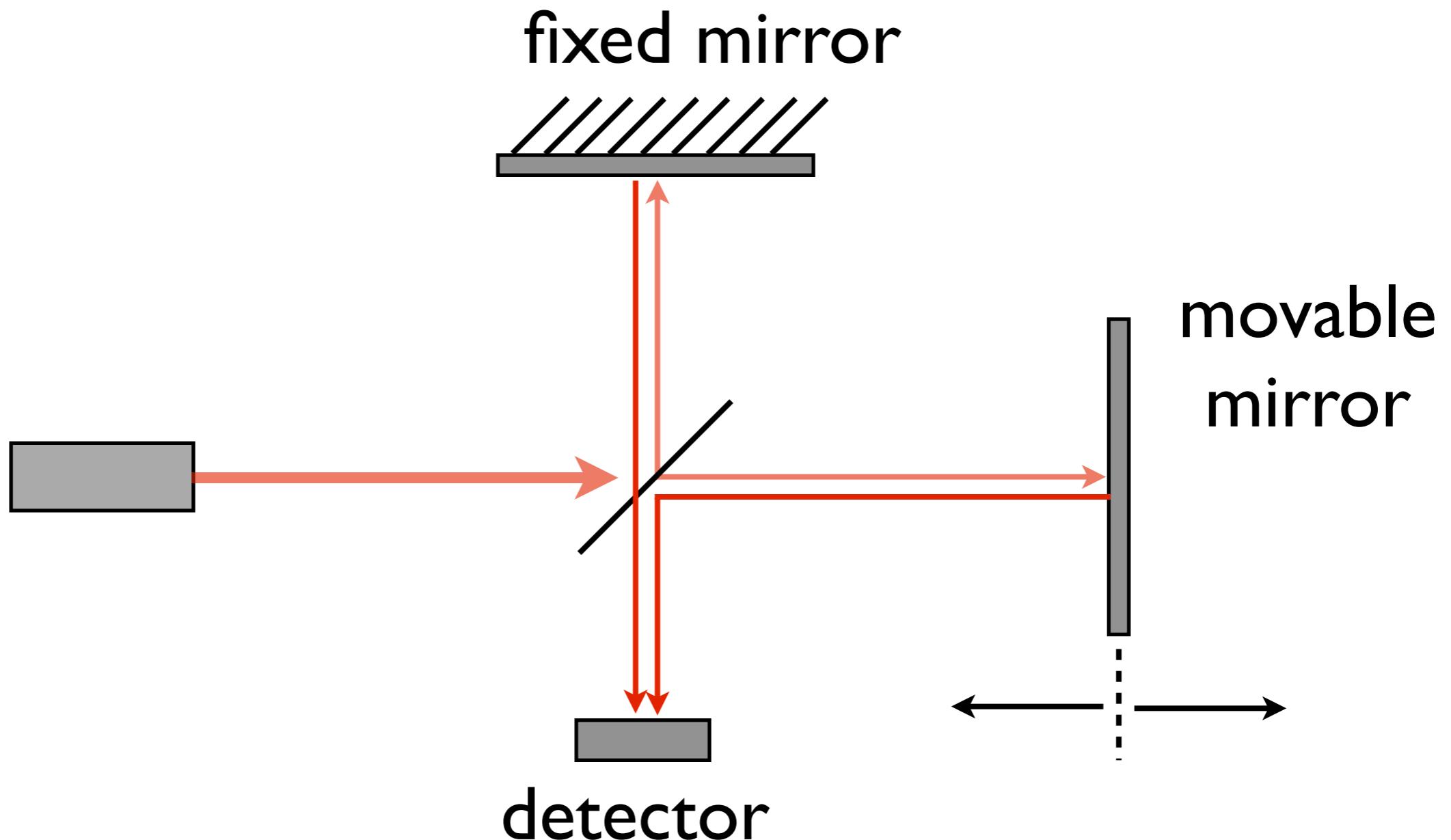
# Triangulation optical sensor



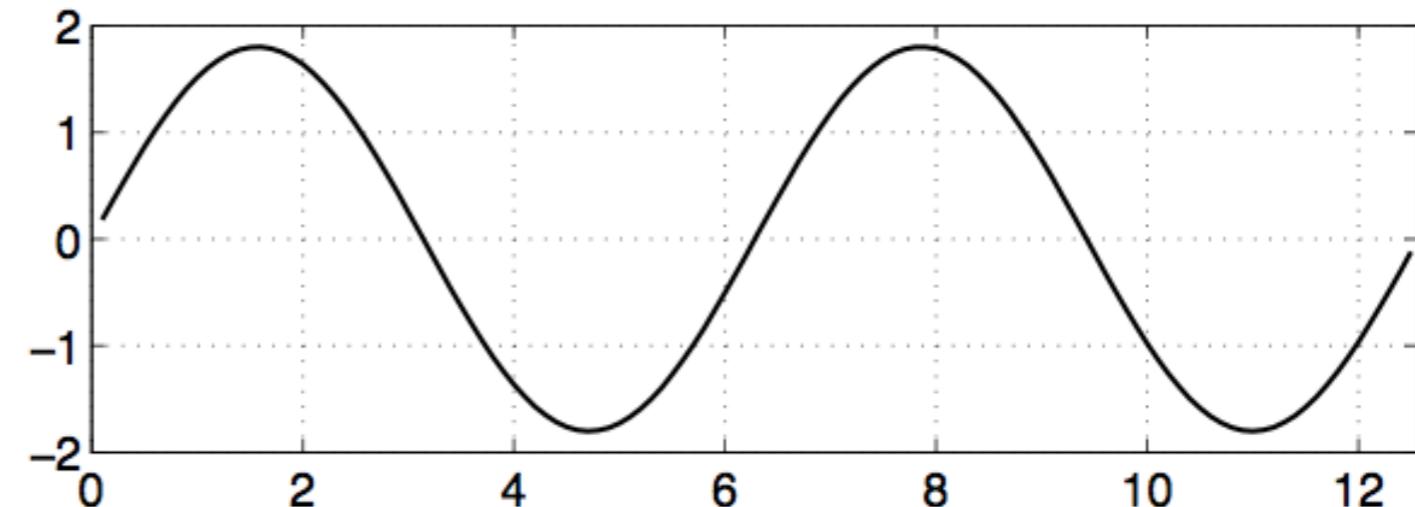
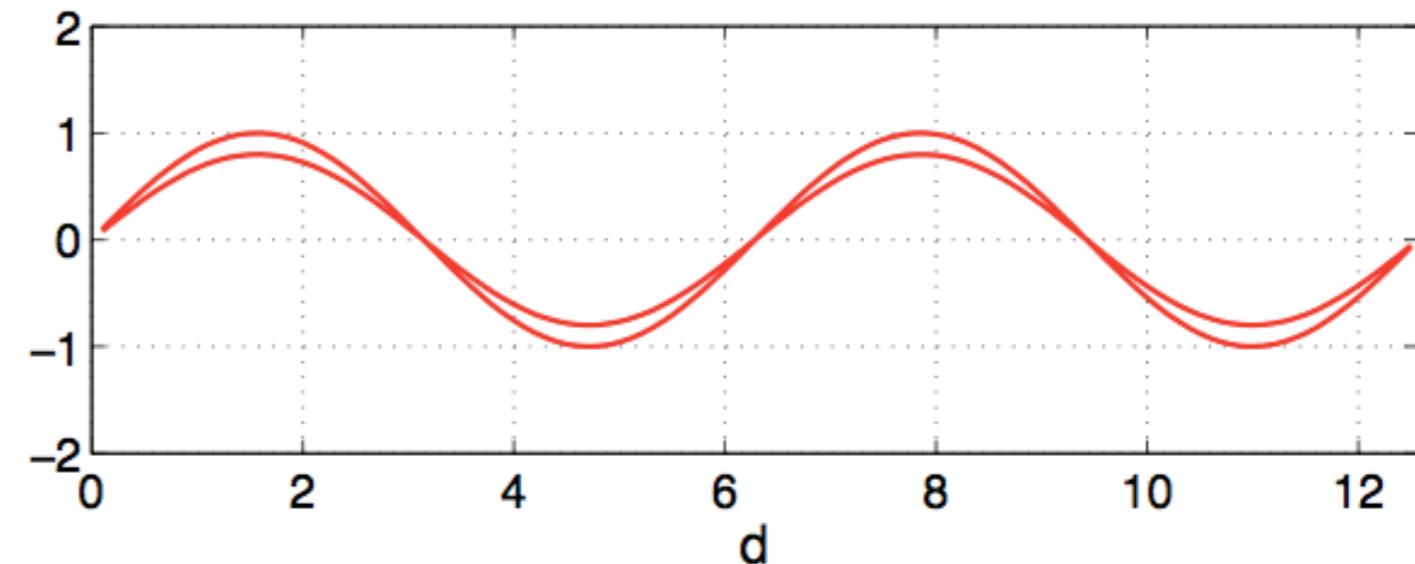
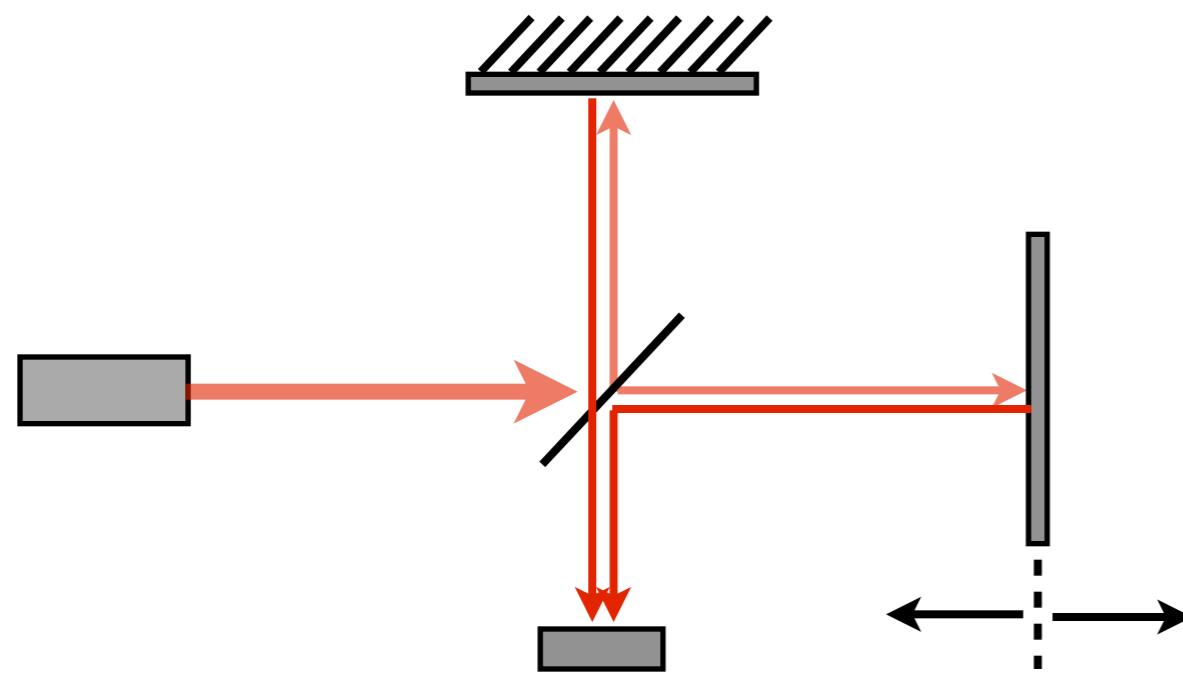
# Michelson Interferometer



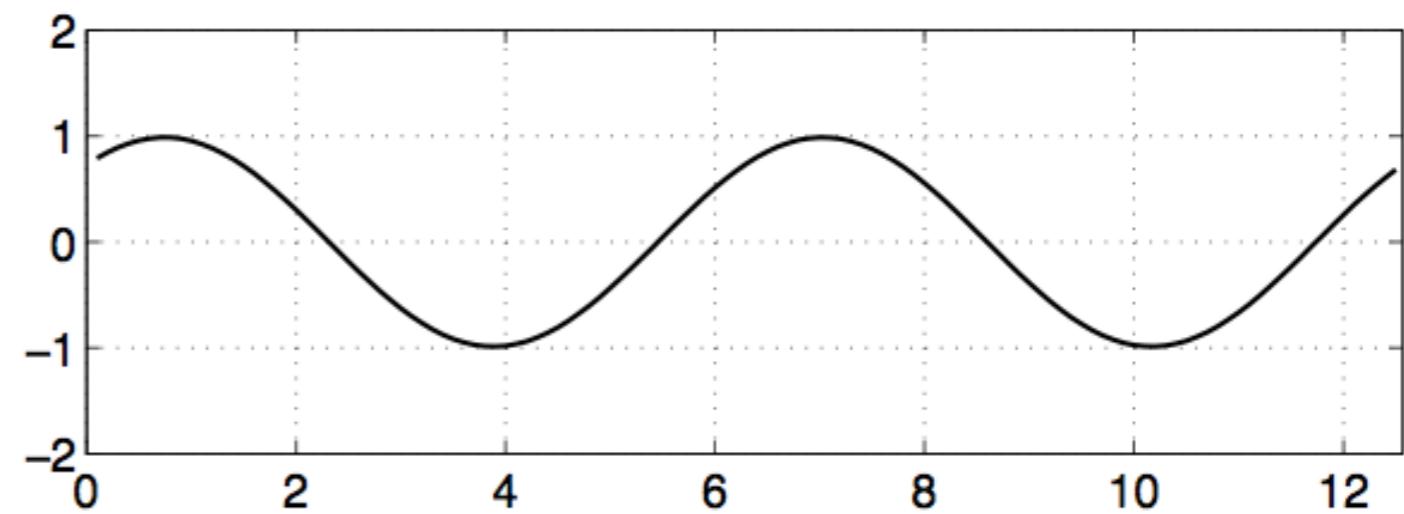
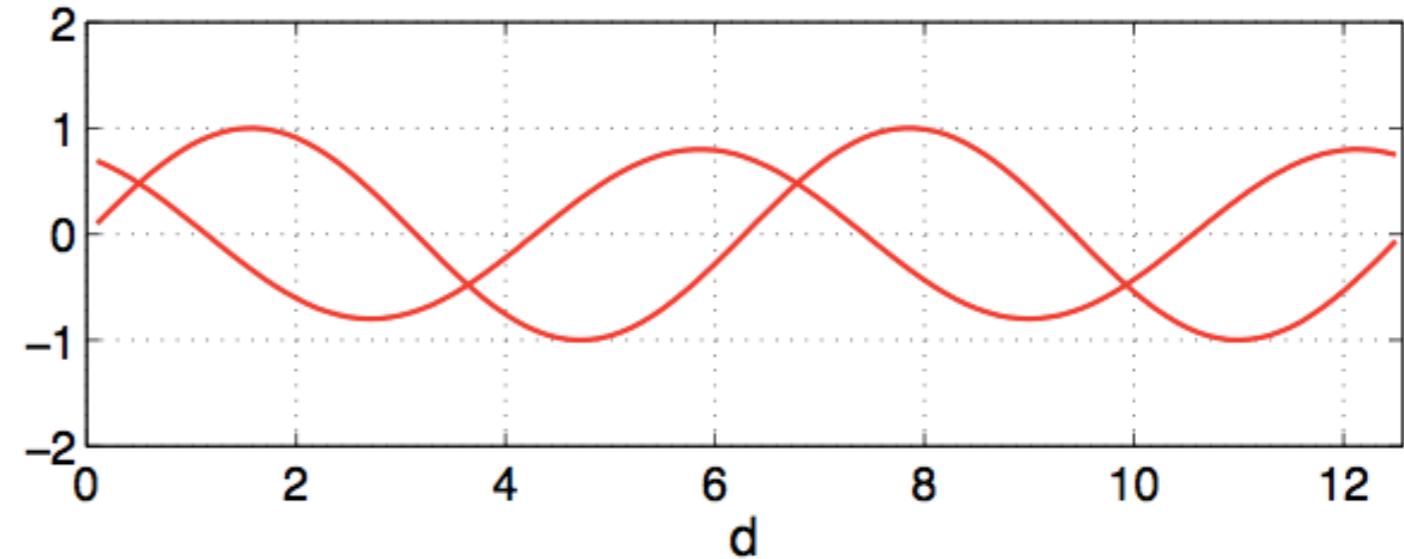
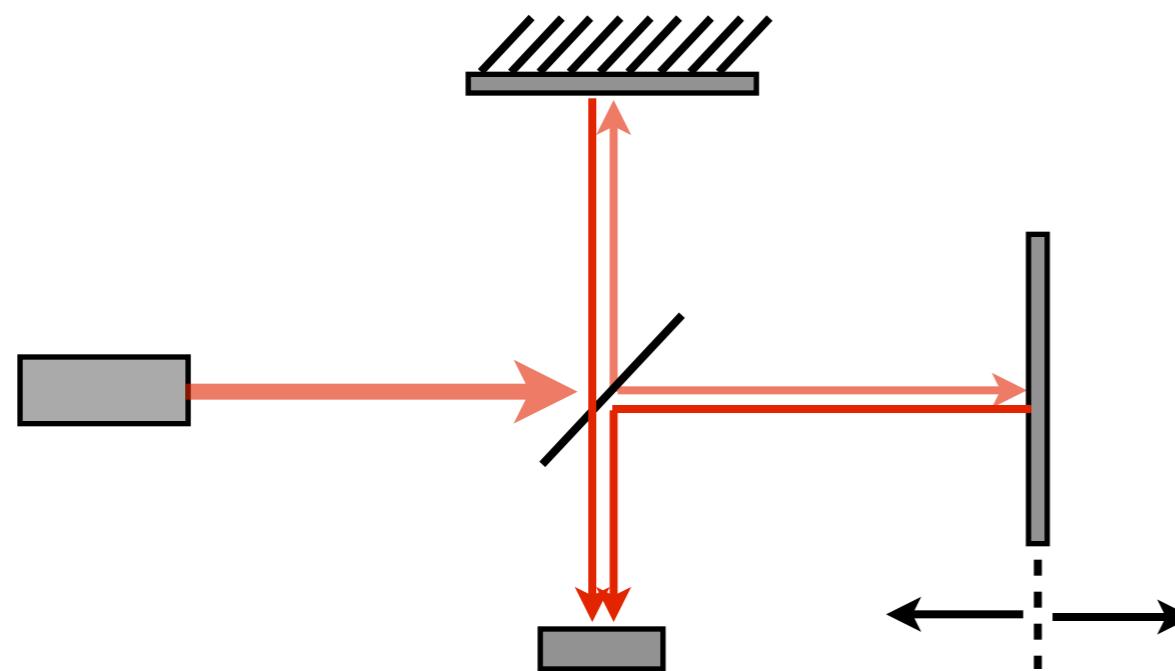
# Michelson Interferometer



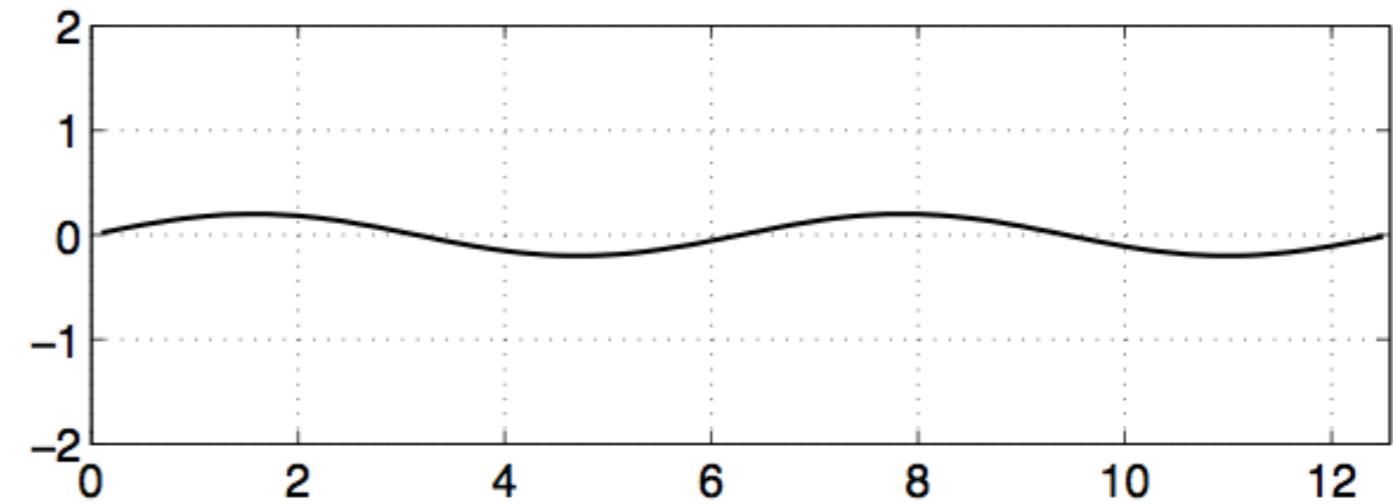
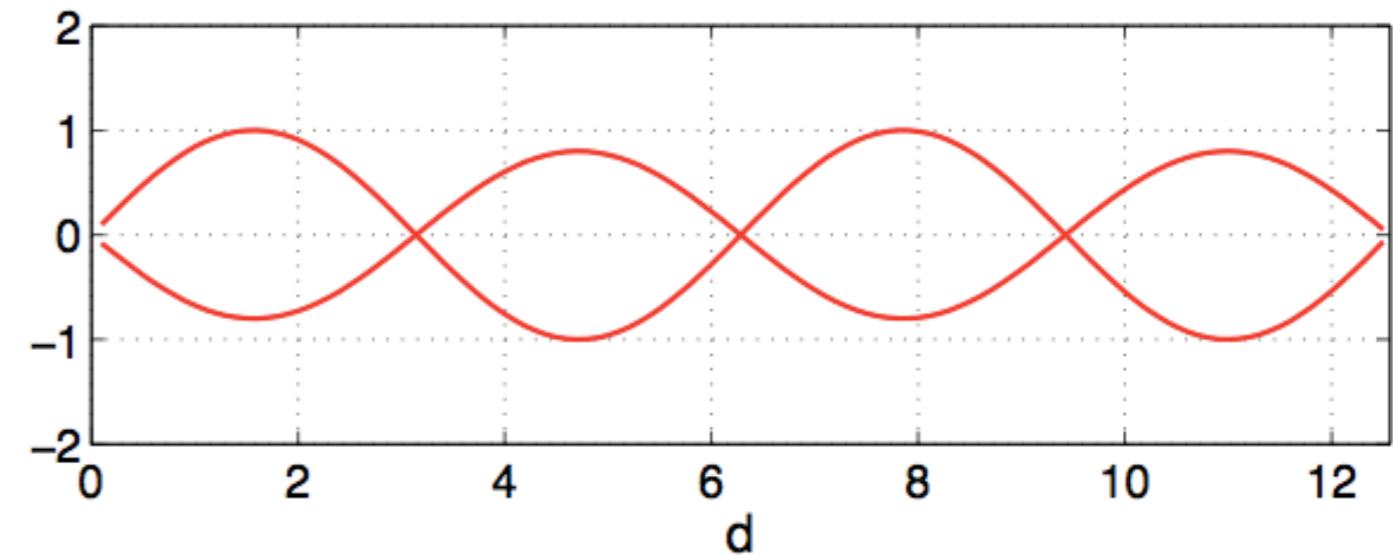
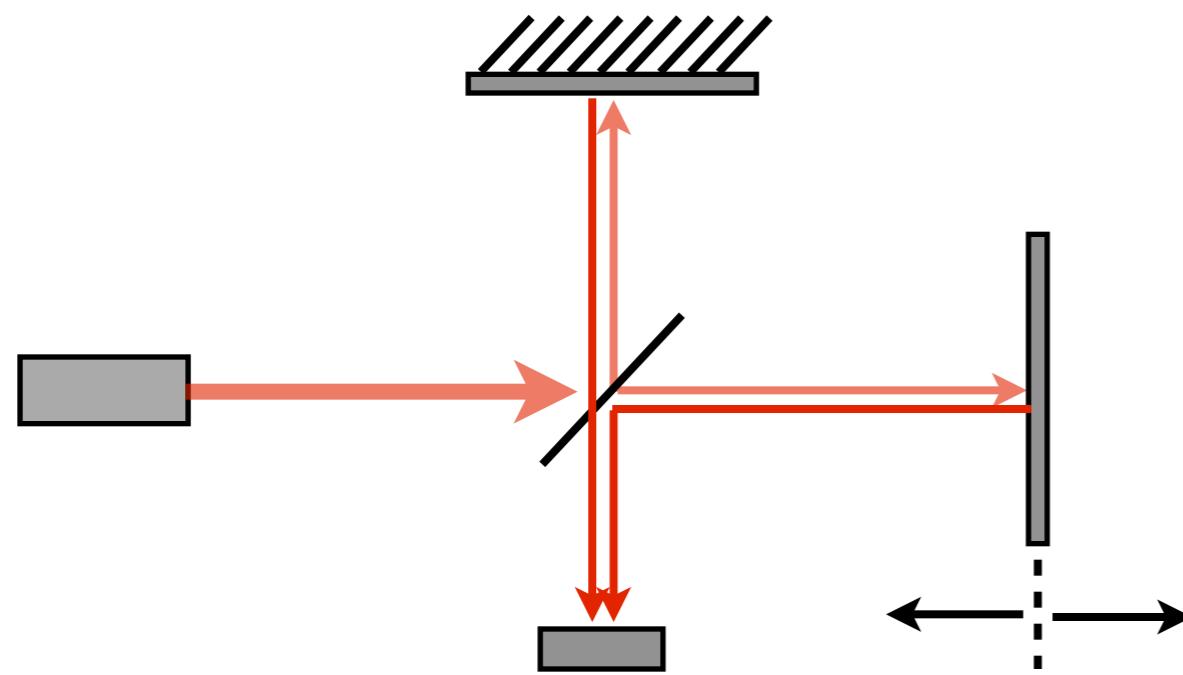
# Michelson Interferometer



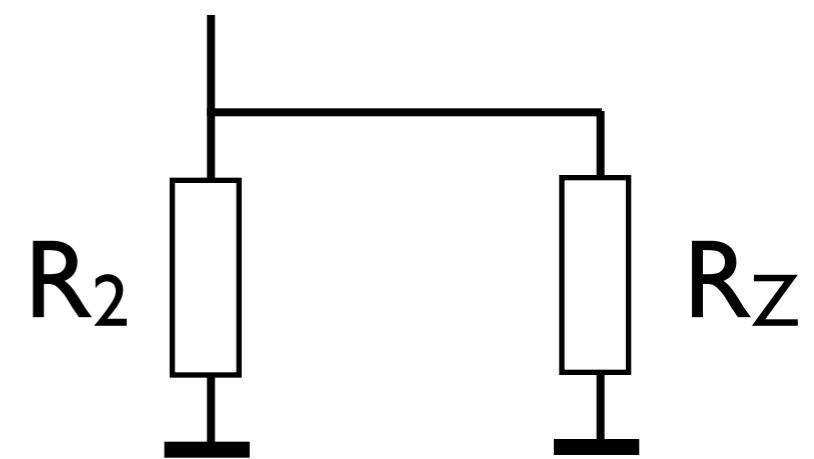
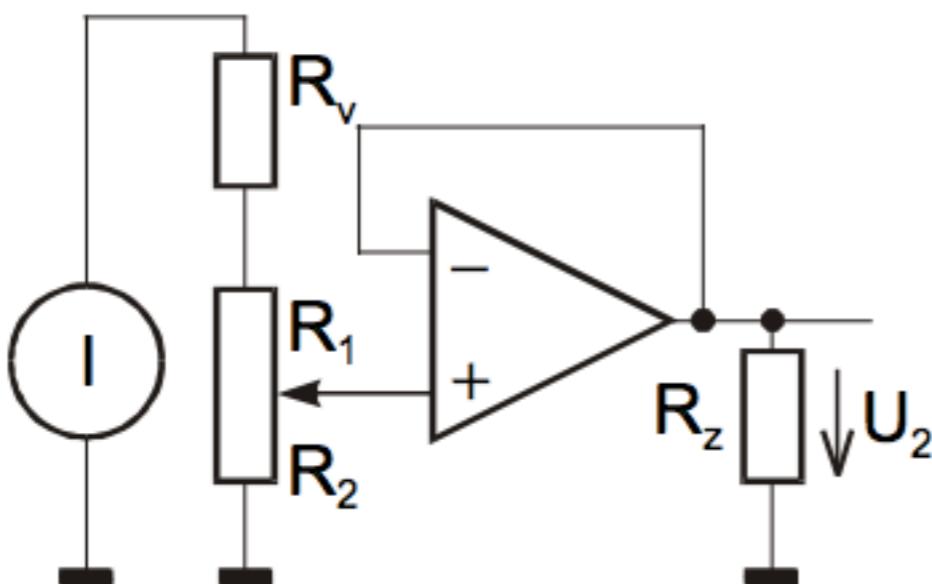
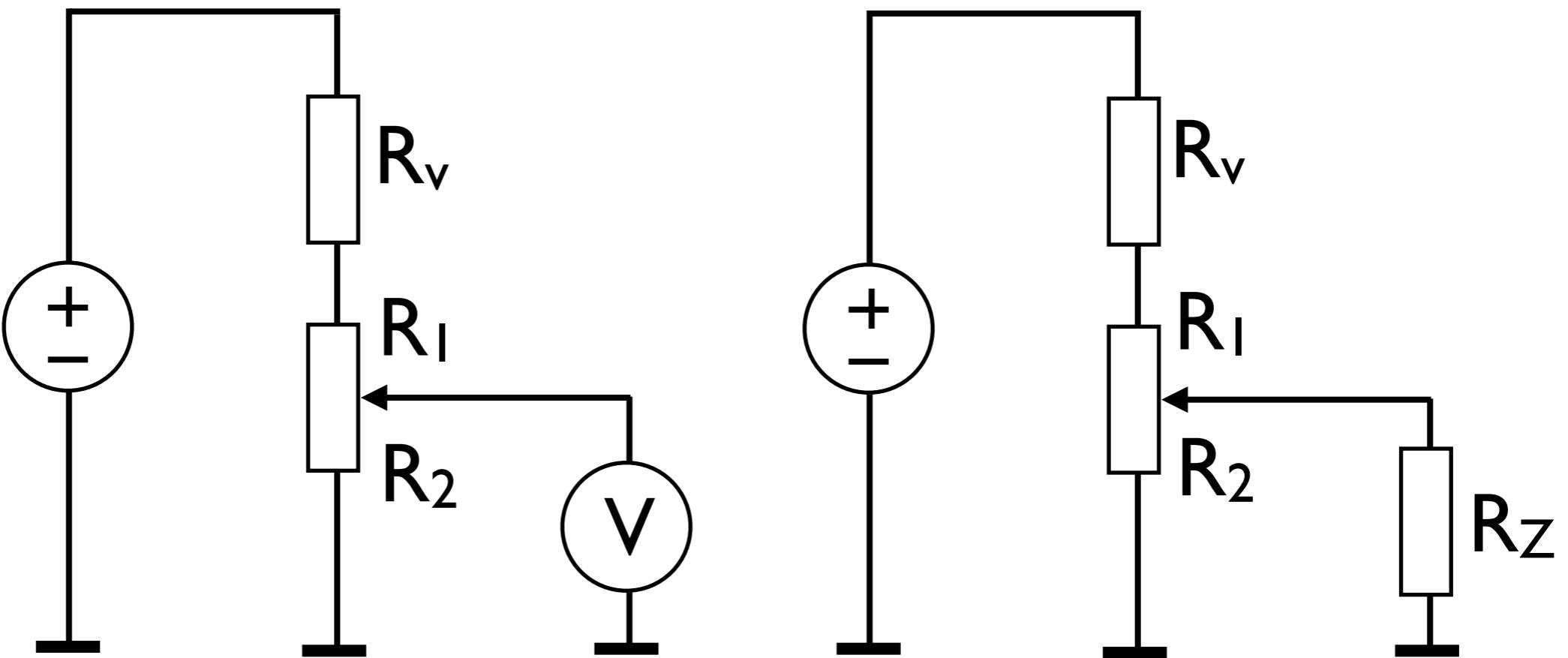
# Michelson Interferometer



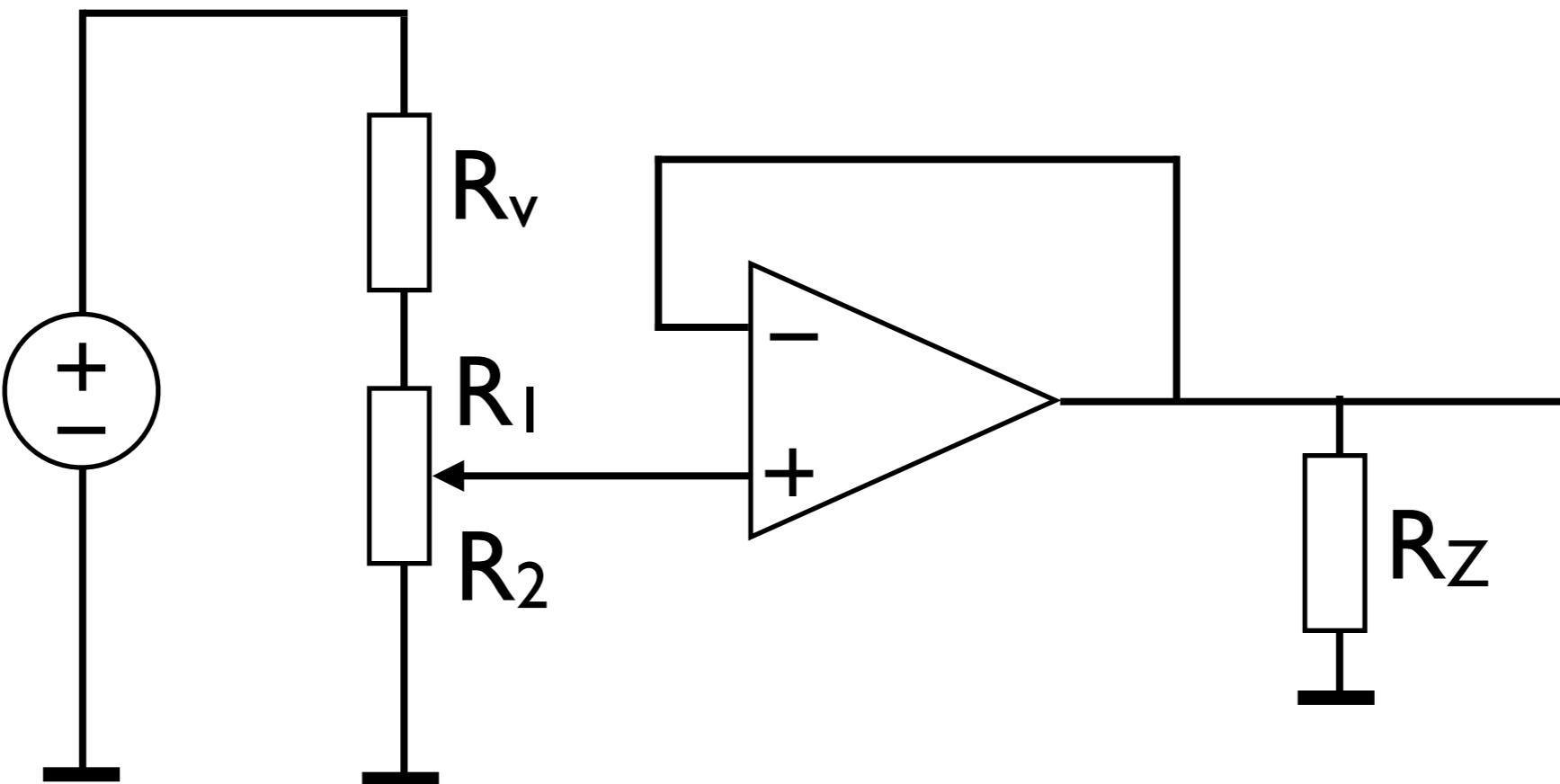
# Michelson Interferometer



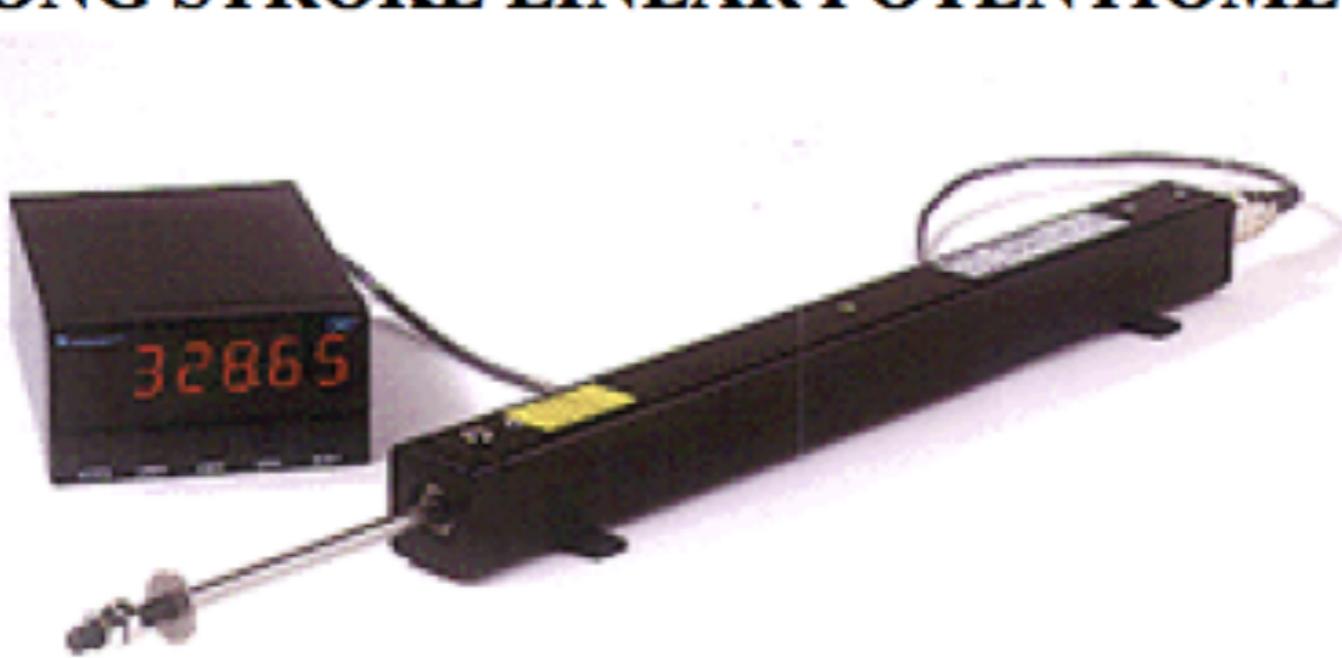
# Resistive sensors



# Resistive sensors



## LONG STROKE LINEAR POTENTIOMETERS



### SPECIFICATIONS

**Total Resistance:** 5000 Ohms  $\pm$  20%

**Linearity:**  $\pm$ 1% S

**Hysteresis:**  $\pm$ 0.001" (0.025 mm)

**Repeatability:**  $\pm$ 0.0005" (0.012 mm)

**Incremental Sensitivity:** 0.00005"

**Power Rating:** 0.75 watts/stroke inch

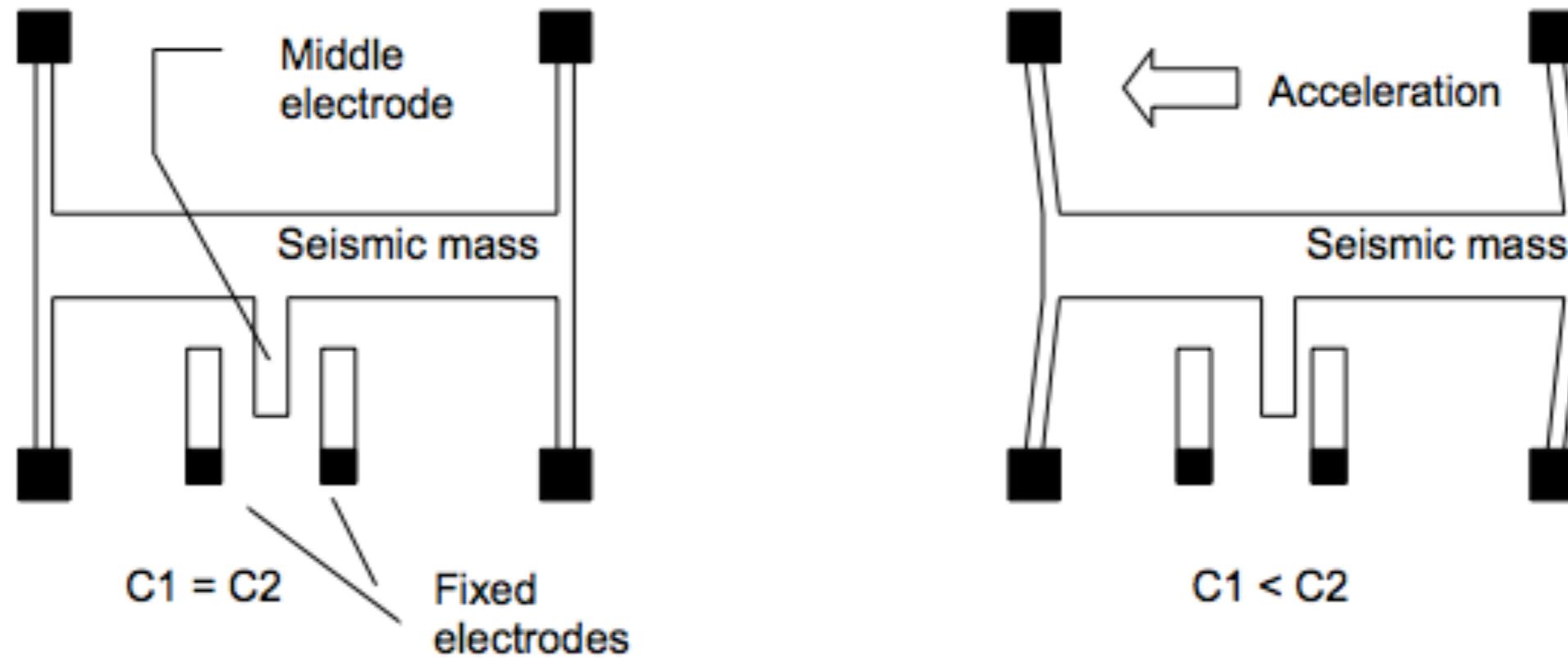
**Temp. Range:** -65 to 105°C (-85 to 221°F)

**Operating Force:** 450 grams (1 Lb) maximum

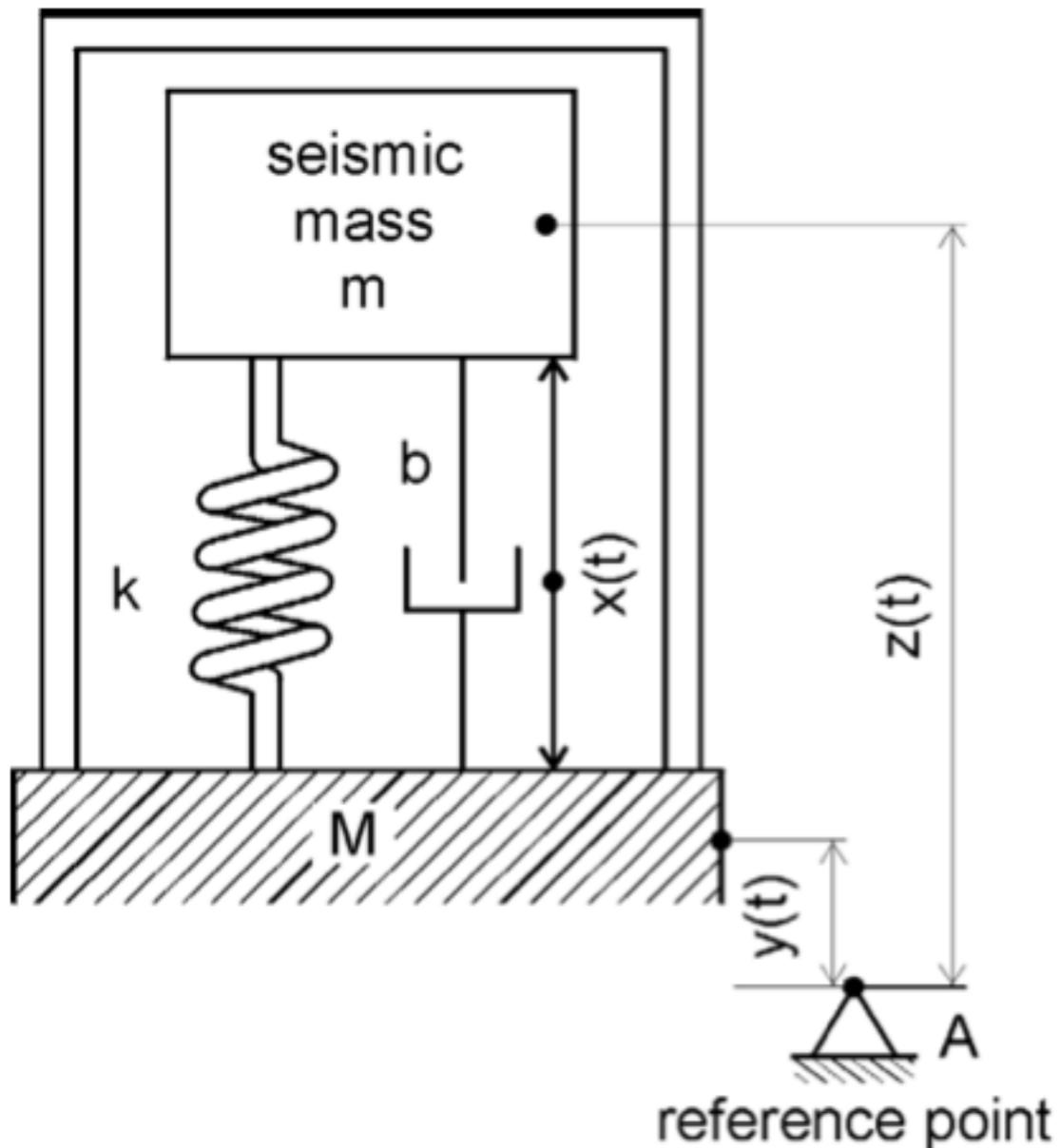
**Shaft:** 0.236" (6 mm) diameter with 1 $\frac{1}{4}$ -28 threaded end adapter

**Life:** 100 million operations up to 12" stroke-rated proportionally for longer units (standard rate of travel 2"/sec)

# MEMS accelerometers



# Absolute sensors of vibrations



$m$  - mass

$k$  - stiffness (spring constant)

$b$  – viscous friction coefficient

Equation of motion of mass-spring system

$$m \frac{d^2 z}{dt^2} + b \frac{dx}{dt} + kx = 0$$

$$z(t) = x(t) + y(t)$$

$$m \frac{d^2 x}{dt^2} + b \frac{dx}{dt} + kx = -m \frac{d^2 y}{dt^2}$$

inertial force

spring force

damping

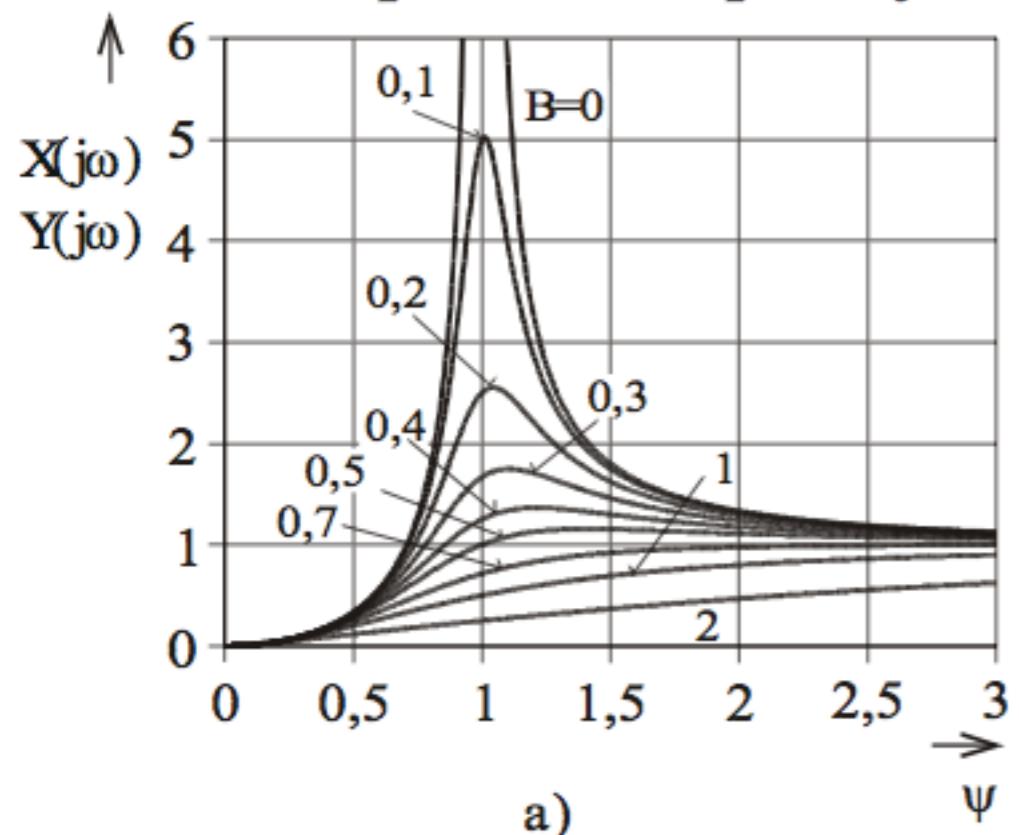
presumption:

$$y(t) = Y(j\omega)e^{j\omega t}$$

Solution:

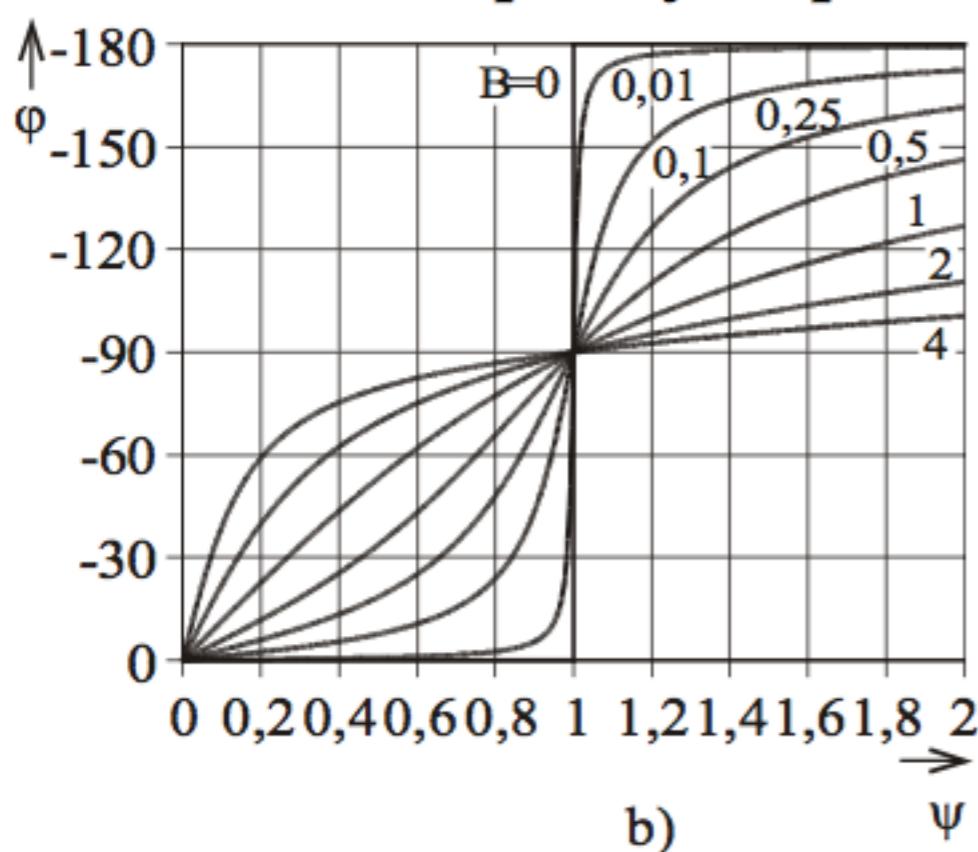
$$x(t) = X(j\omega)e^{j(\omega t - \varphi)}$$

## Amplitude frequency response:



$$\left| \frac{X(j\omega)}{Y(j\omega)} \right| = \frac{\Psi^2}{\sqrt{(1 - \Psi^2)^2 + (2B\Psi)^2}}$$

## Phase frequency response

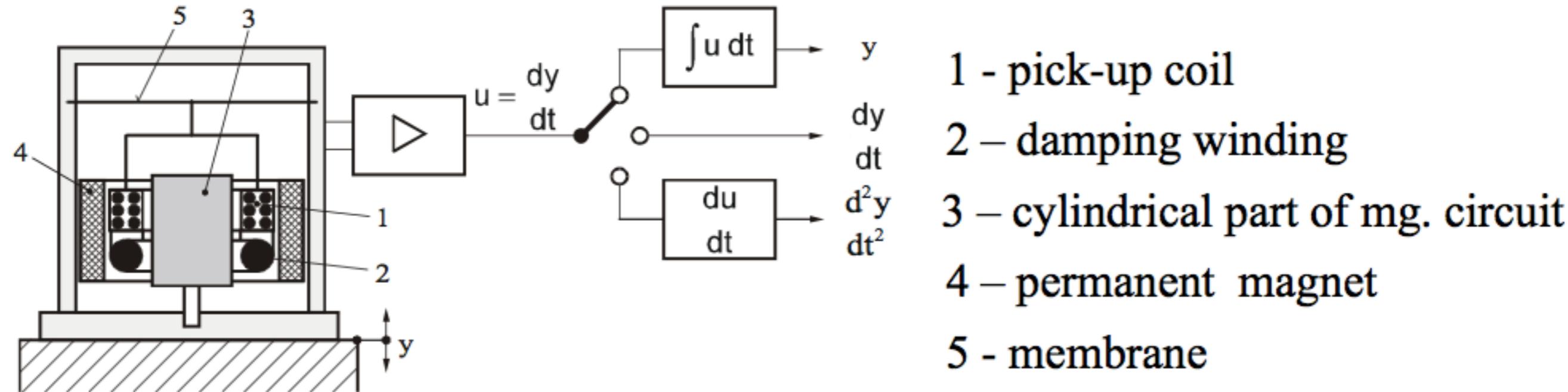


$$\varphi = \text{arctg} \frac{-2B\Psi}{1 - \Psi^2}$$

where:

|                                  |   |
|----------------------------------|---|
| $\Psi = \frac{\omega}{\omega_0}$ | - normalised frequency<br>(referenced to resonance freq.) |
| $B = \frac{b}{b_{kr}}$           | - damping ratio   |
| $b_{kr} = 2m\omega_0$            | - critical damping ratio                                  |
| $\omega_0 = \sqrt{\frac{k}{m}}$  | - resonant frequency                                      |

# Electrodynamic sensor of vibration



- seismic mass = mass of coil 1 + mass of winding 2
- viscous damping – due to currents induced in winding 2

- induced voltage  $u = \frac{d\Phi}{dt}$  proportional to the *velocity* of coil

☺ - universality

## GEOPHONE

- application: vibrations of machines, buildings, occupancy detection

☺ - cheap  $f_r = 1 \dots 100 \text{ Hz}$ ,  $m = 20\text{g} \dots 5 \text{ kg}$