

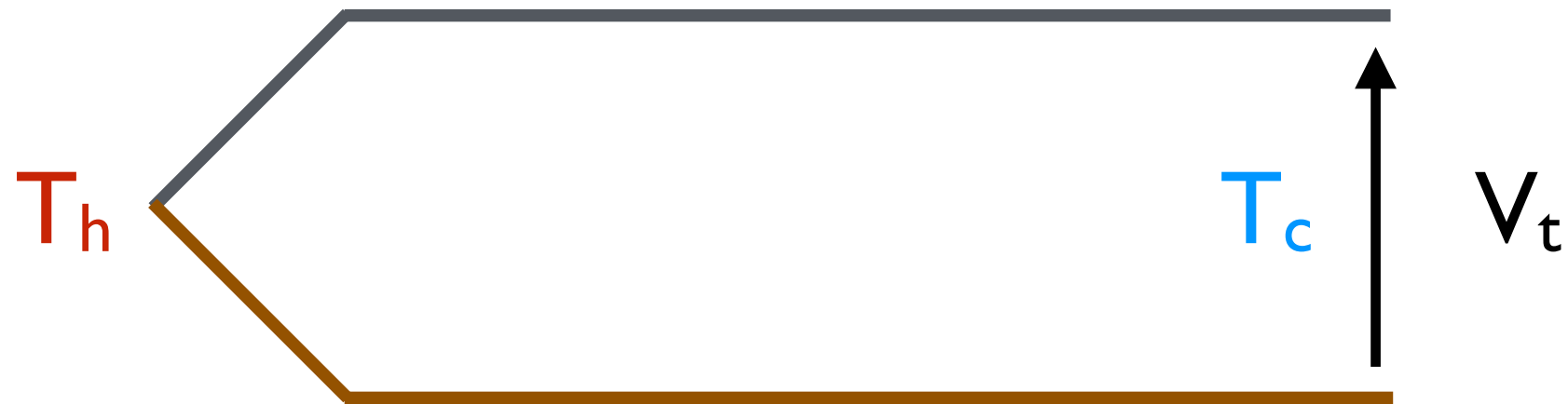
Sensors of temperature (contact)

AE3B38SME - Sensors and Measurement

Thermocouples

hot end

cold end



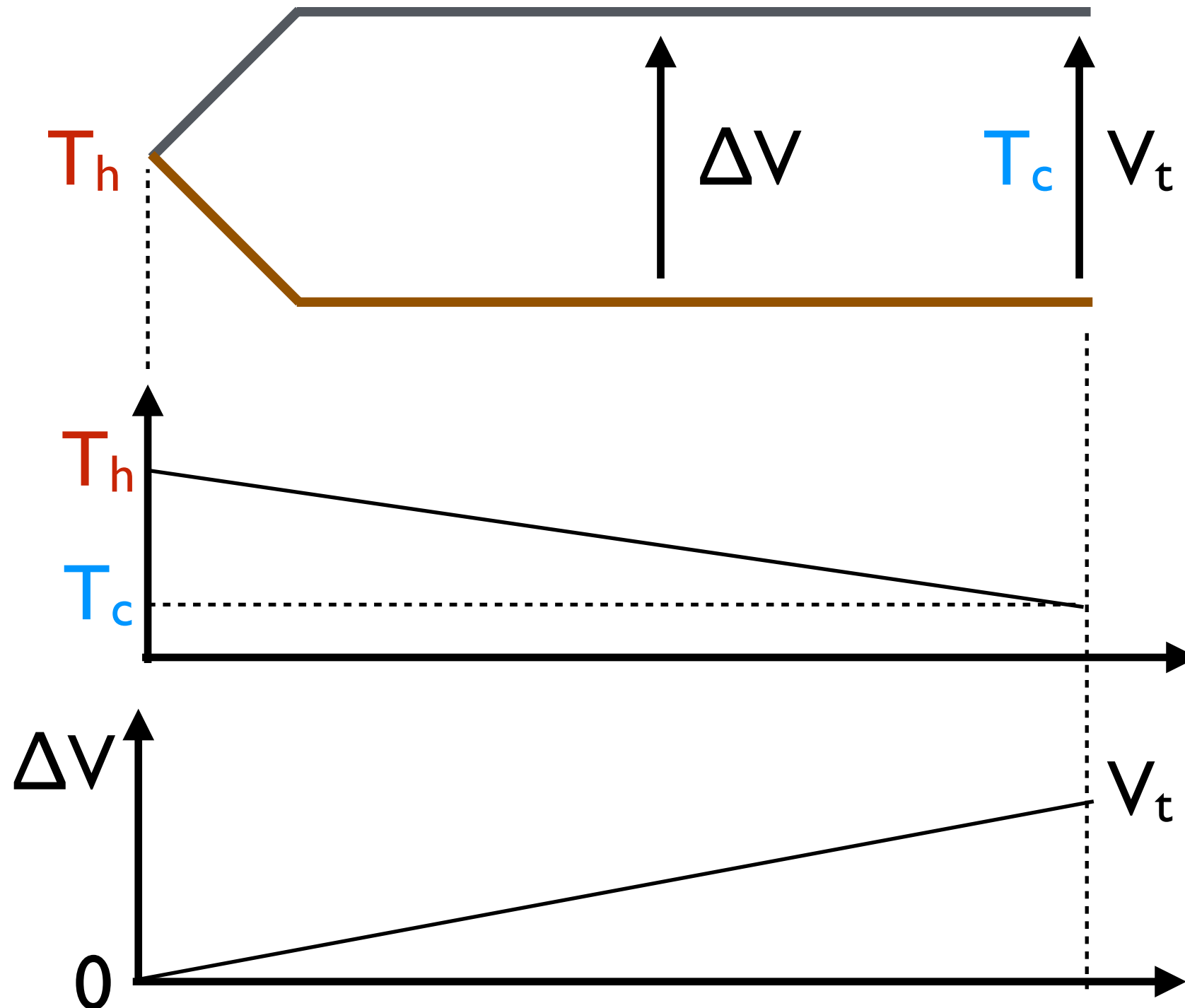
$$V_t = k (T_h - T_c)$$

- it is composed of different materials
- it measure the difference of temperature

The voltage is generated by gradient of temperature

hot end

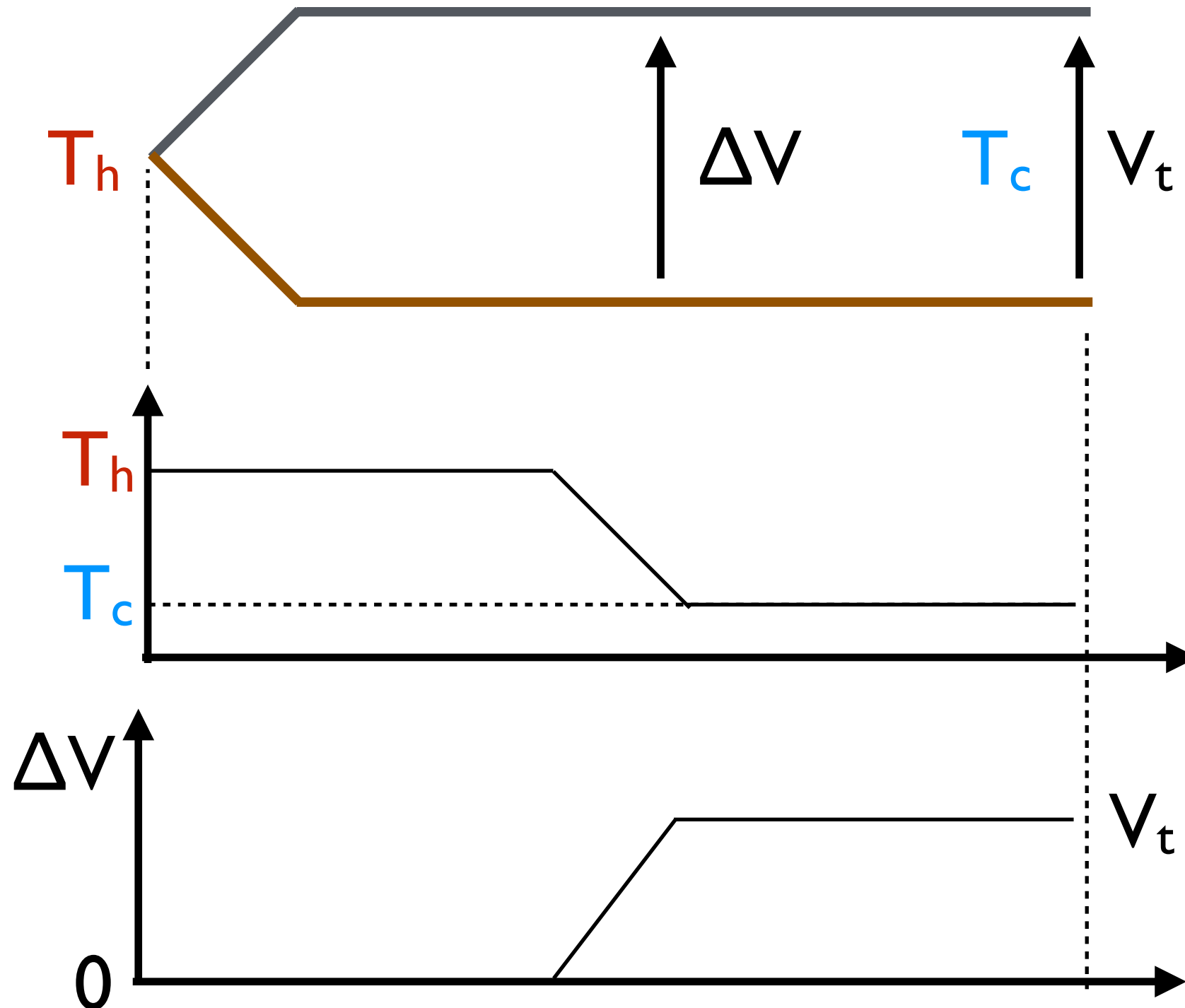
cold end



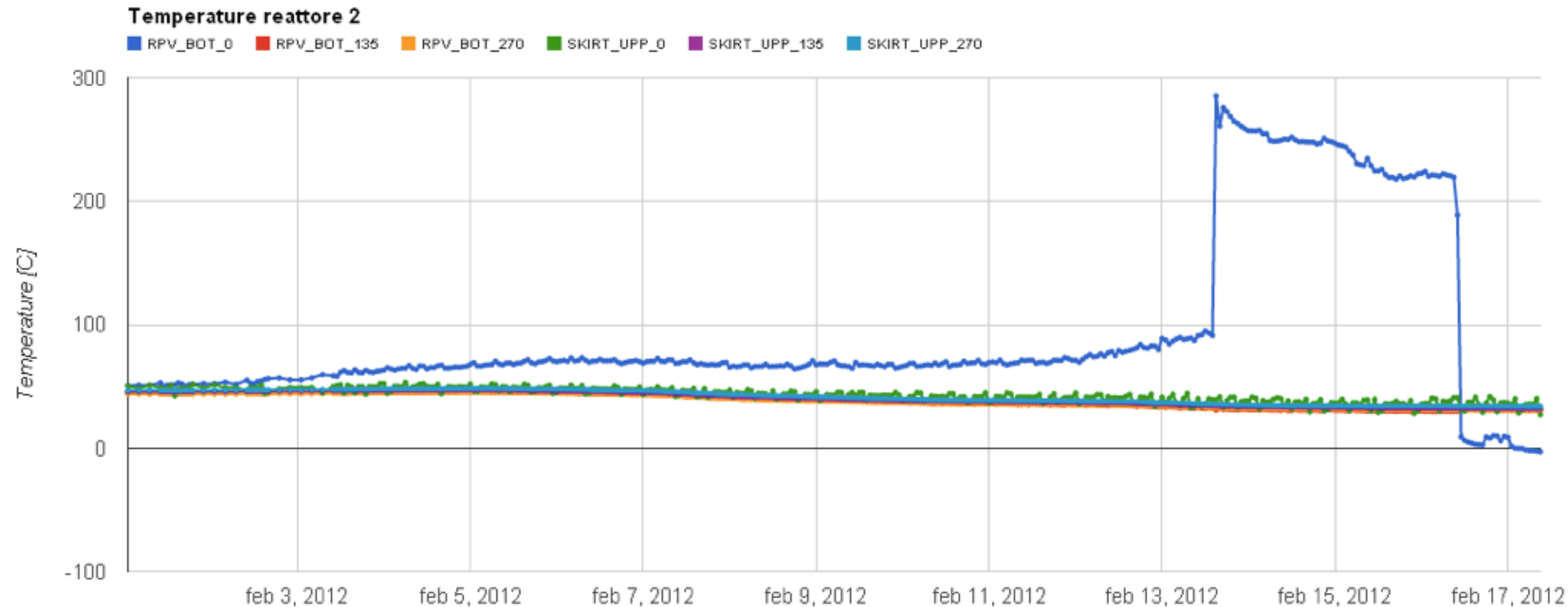
The voltage is generated by gradient of temperature

hot end

cold end

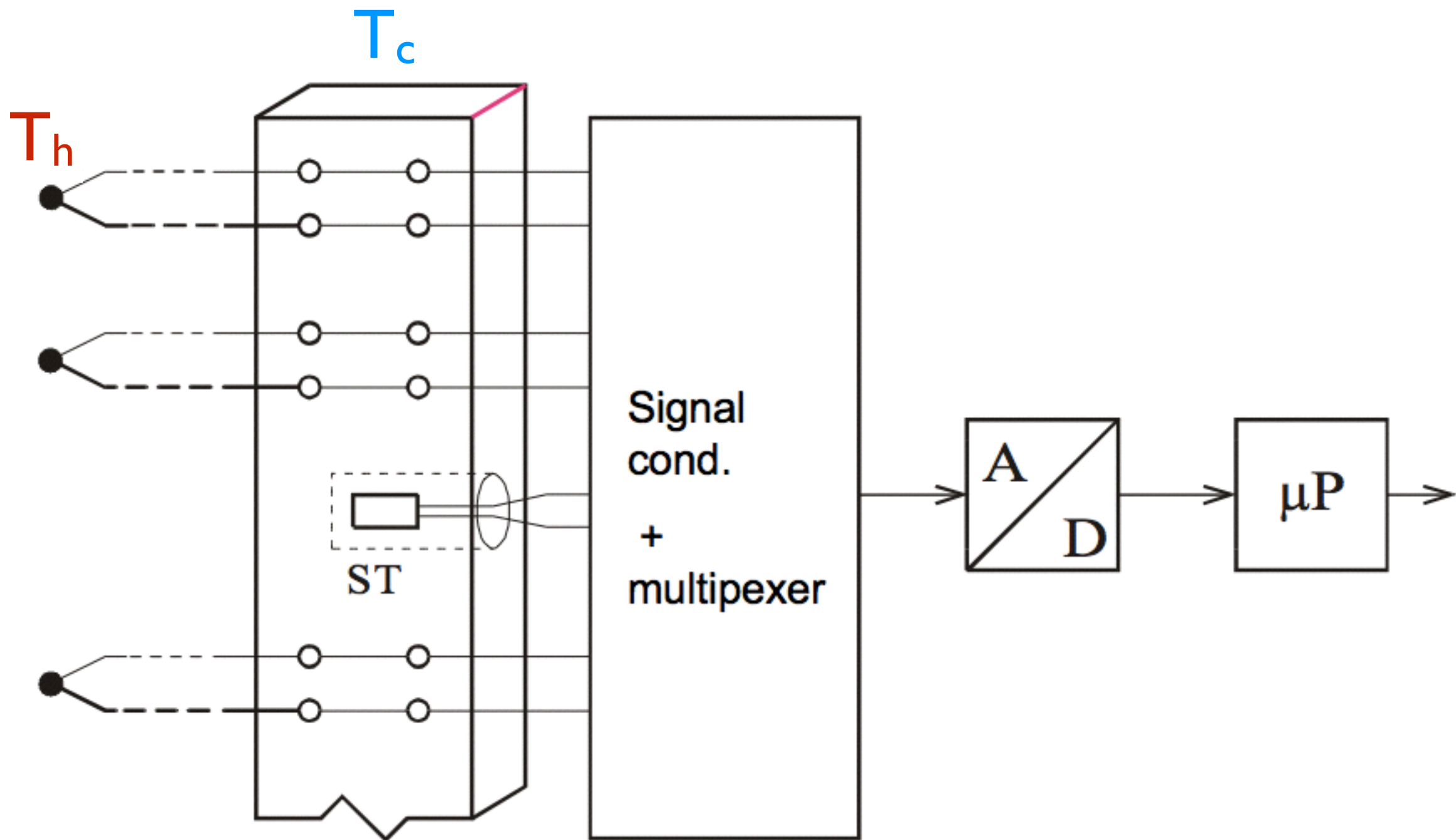


Thermocouples are very robust, but they might fail too



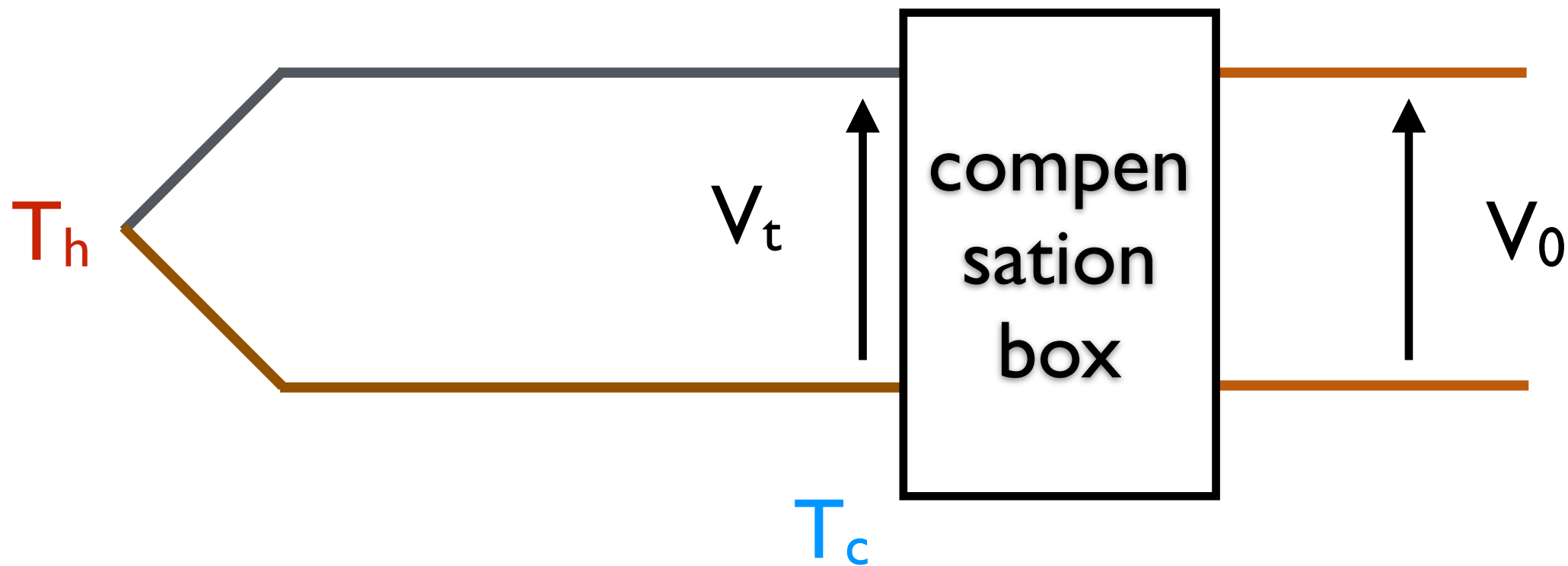
Compensation of cold end temperature

- by measuring the temperature at cold end and numerically adjust the reading



Compensation of cold end temperature

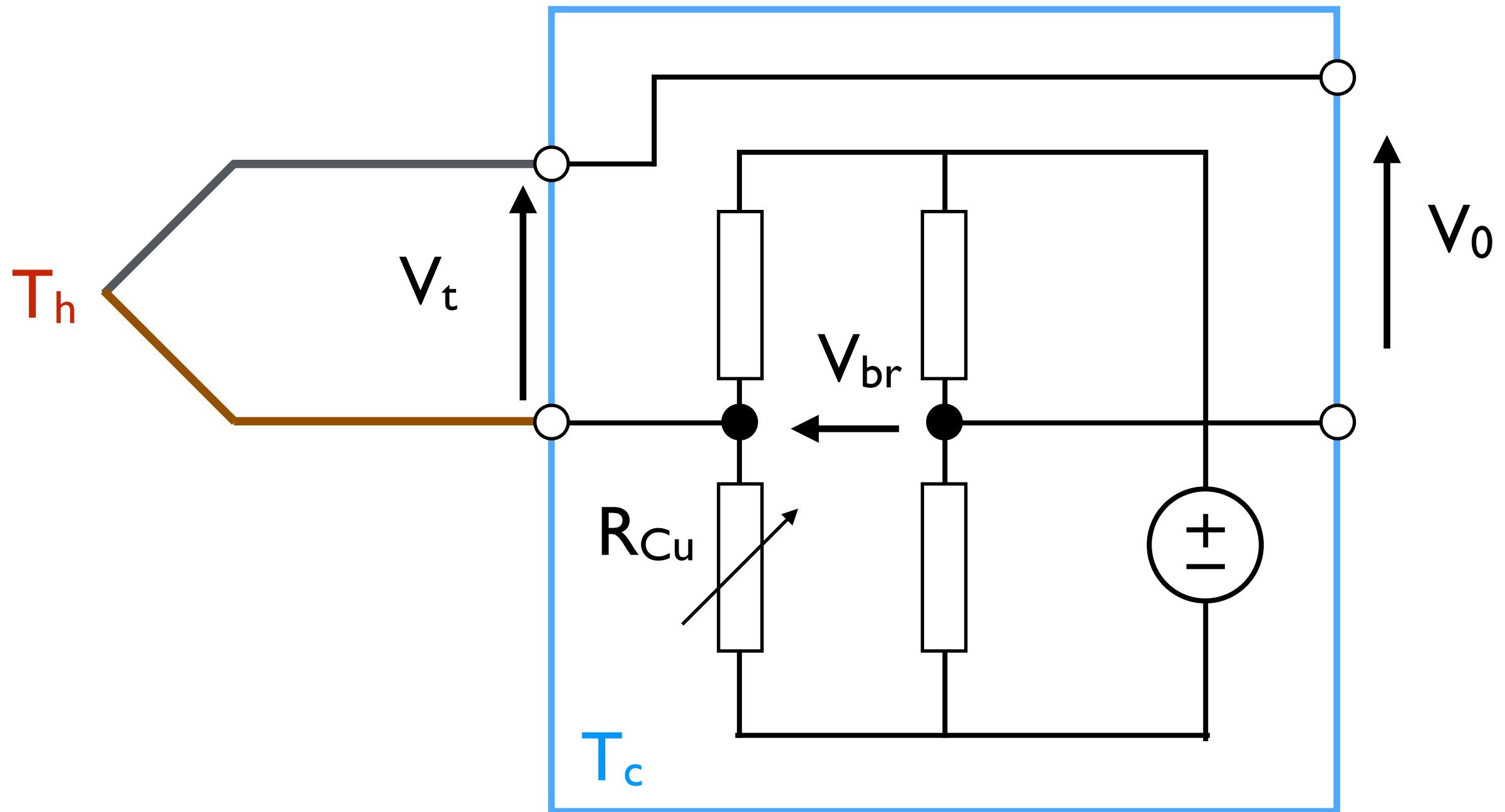
- using compensation box



$$V_t = k (T_h - T_c)$$

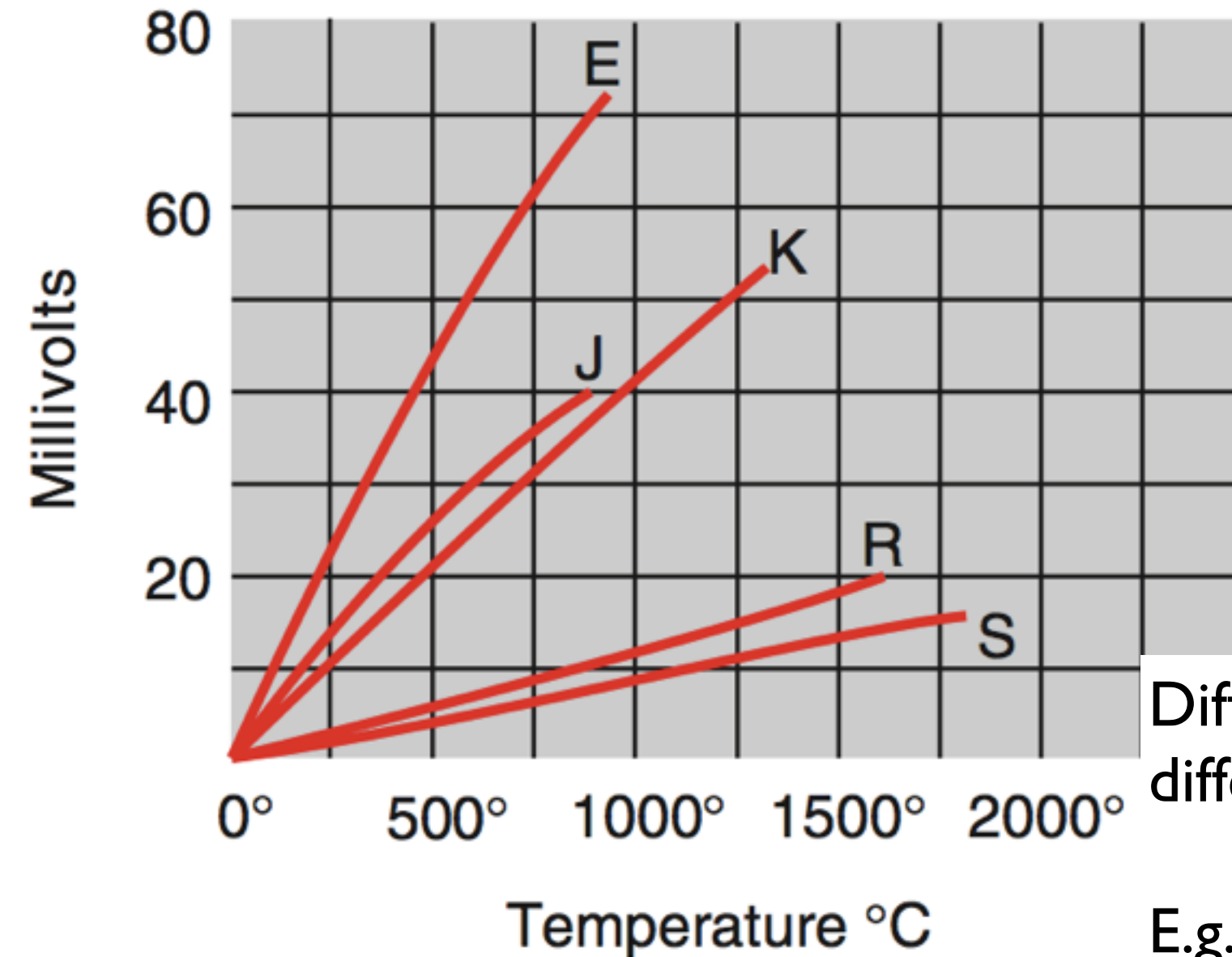
$$V_0 = k T_h$$

Compensation box



$$V_0 = V_t + V_{br} = k (T_h - T_c) + k' T_c$$

Types of thermocouples



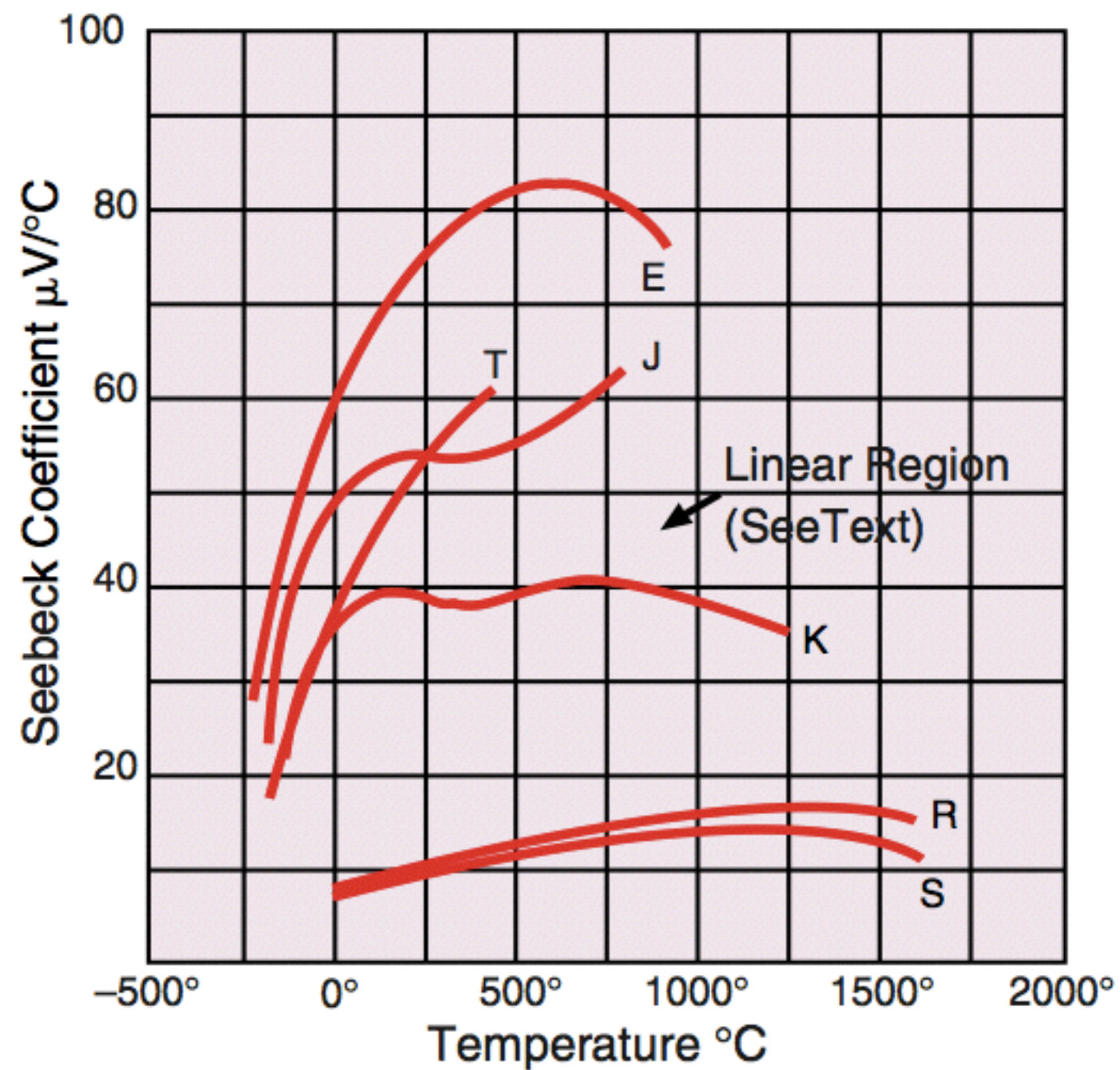
Different couples of metals give different response

E.g. K type : Chromel-Alumel

Chromel: 90% nickel + 10% chromium

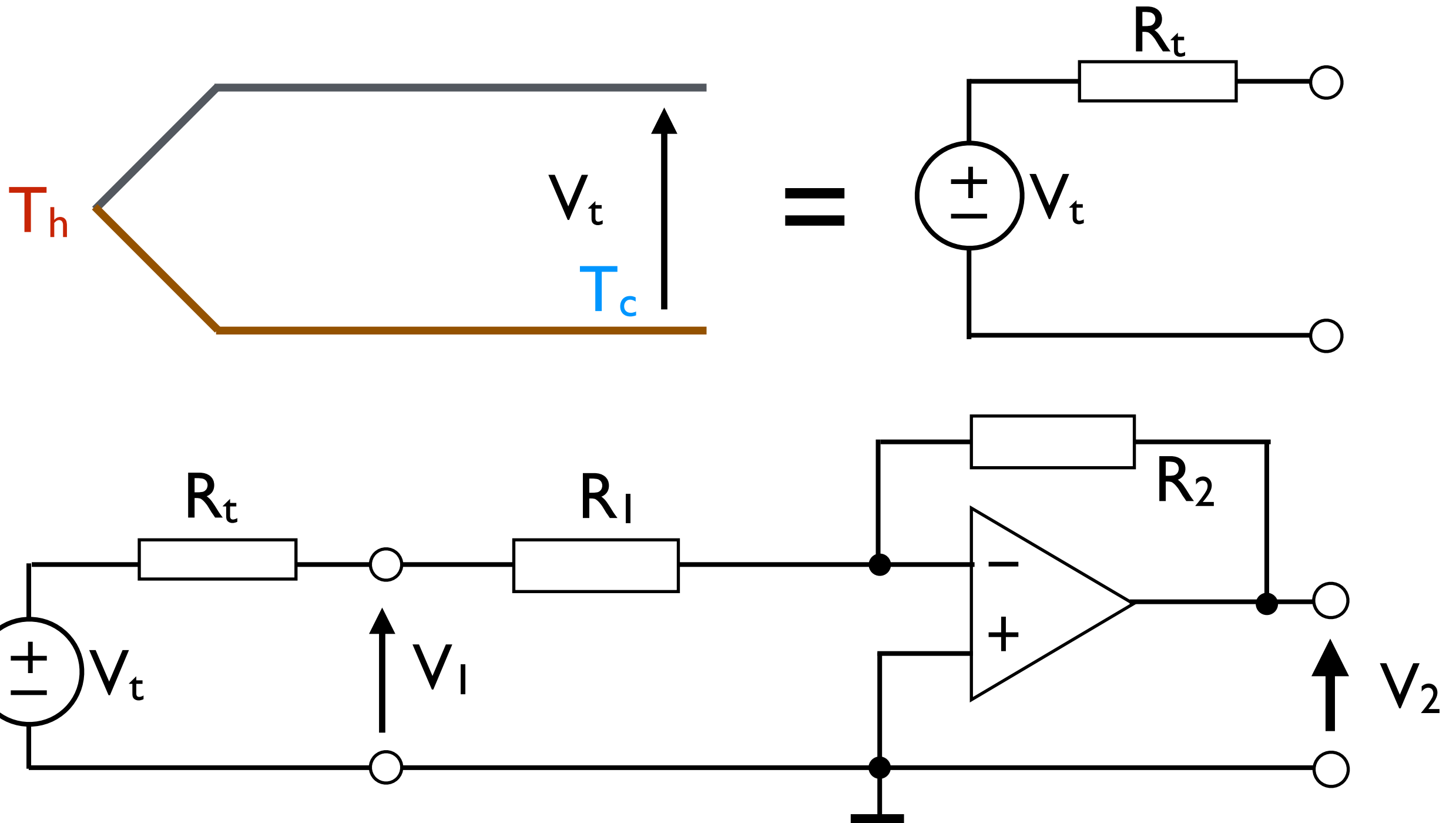
Alumel: 95% nickel, 2% manganese, 2% aluminium

Sensitivity is not always constant



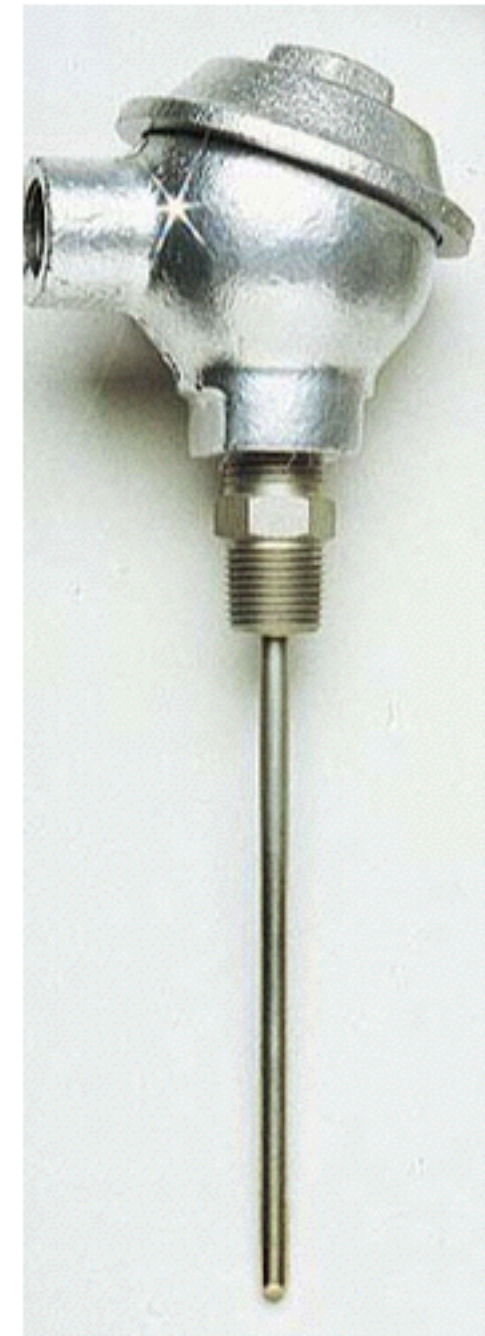
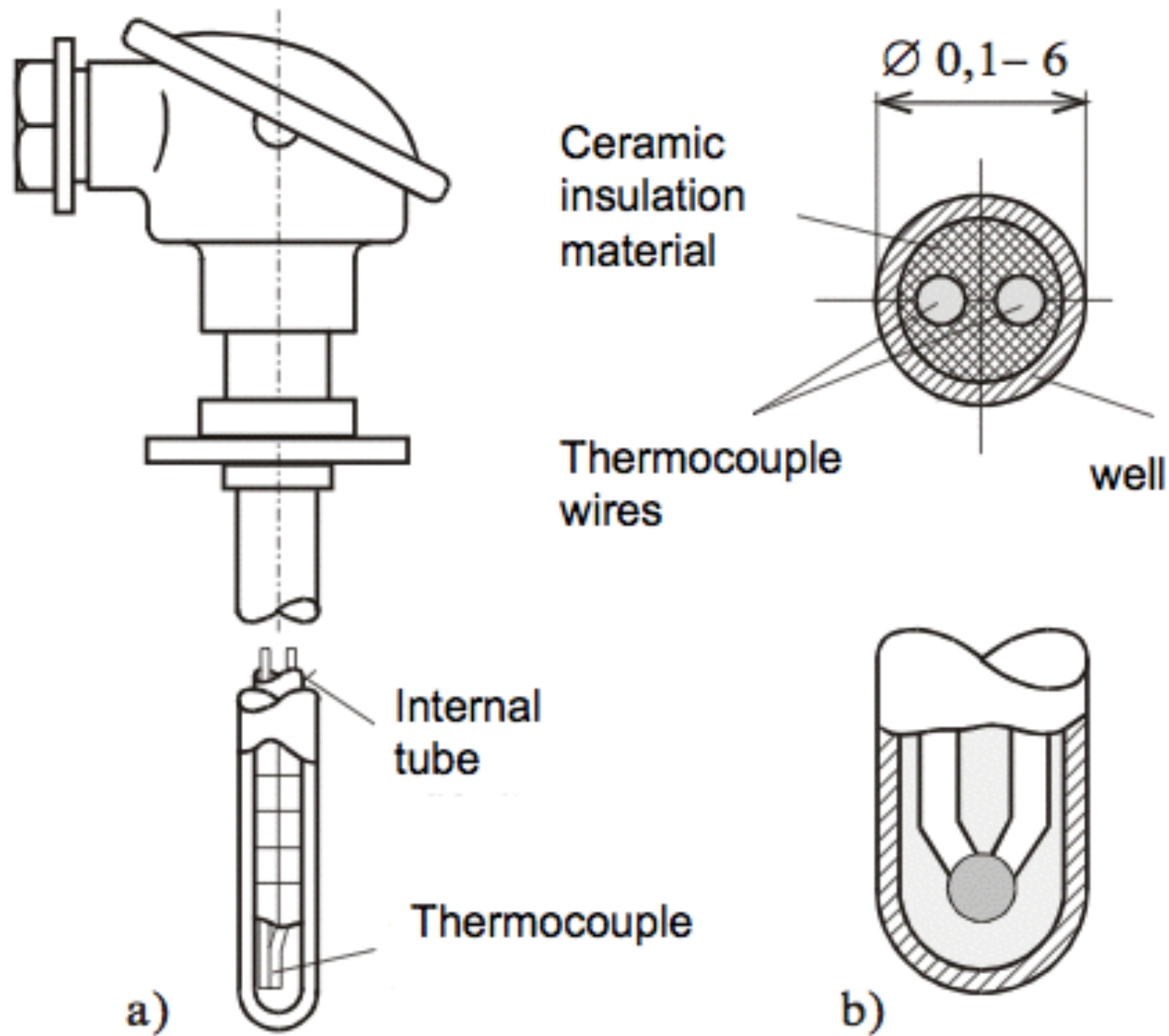
Omega

The sensitivity is always about tens of $\mu\text{V}/\text{K}$.
Amplification is often required.



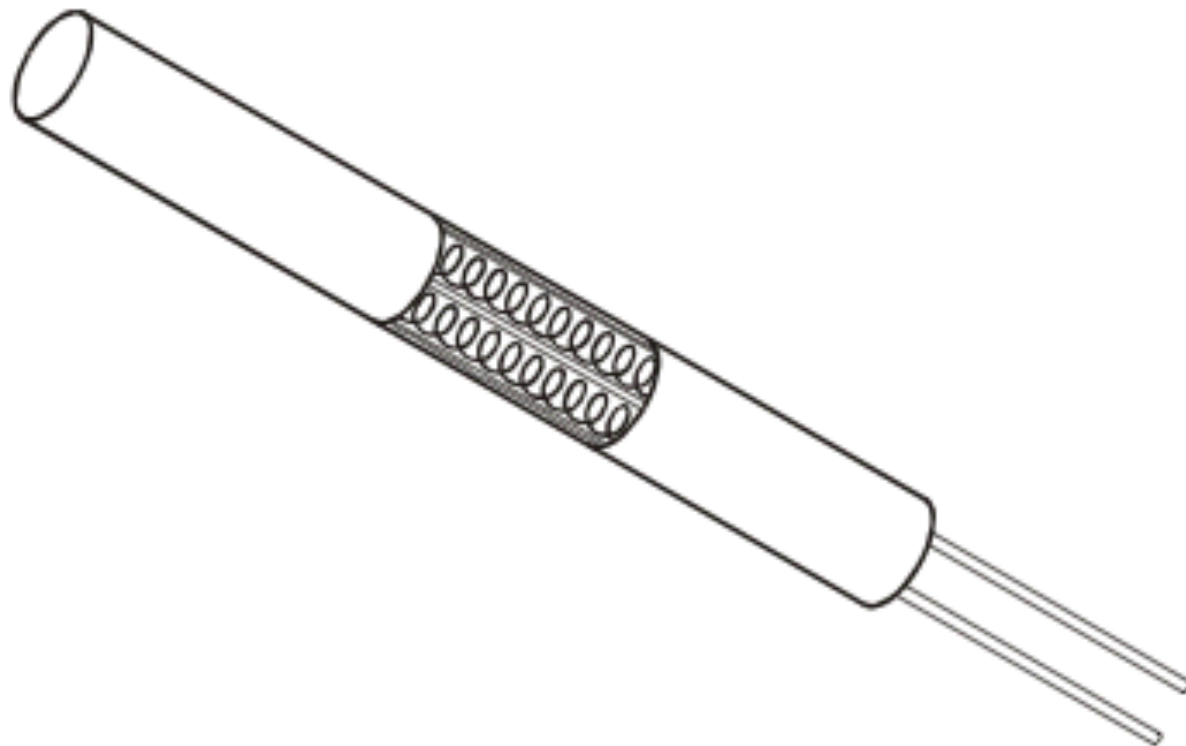
!!! $V_I \neq V_t$

Industrial thermocouple



Metal Resistive Thermometers

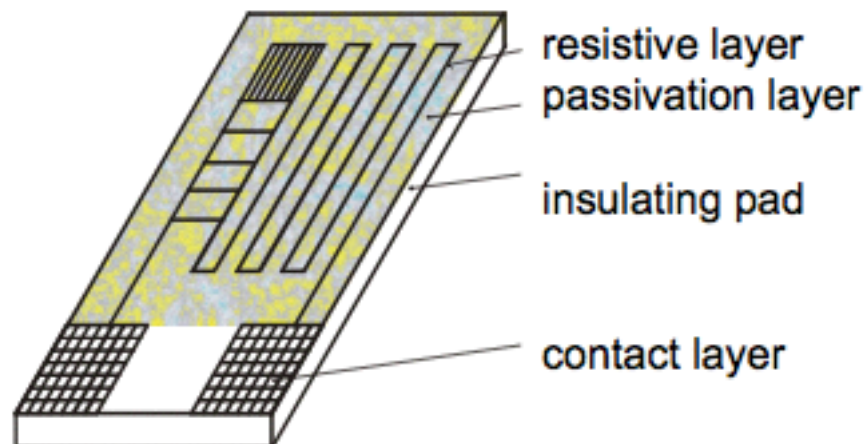
wire wound thermometer



$$R = R_0 \cdot (1 + \alpha \cdot \Delta T)$$

Common materials

thin layer resistive thermometer

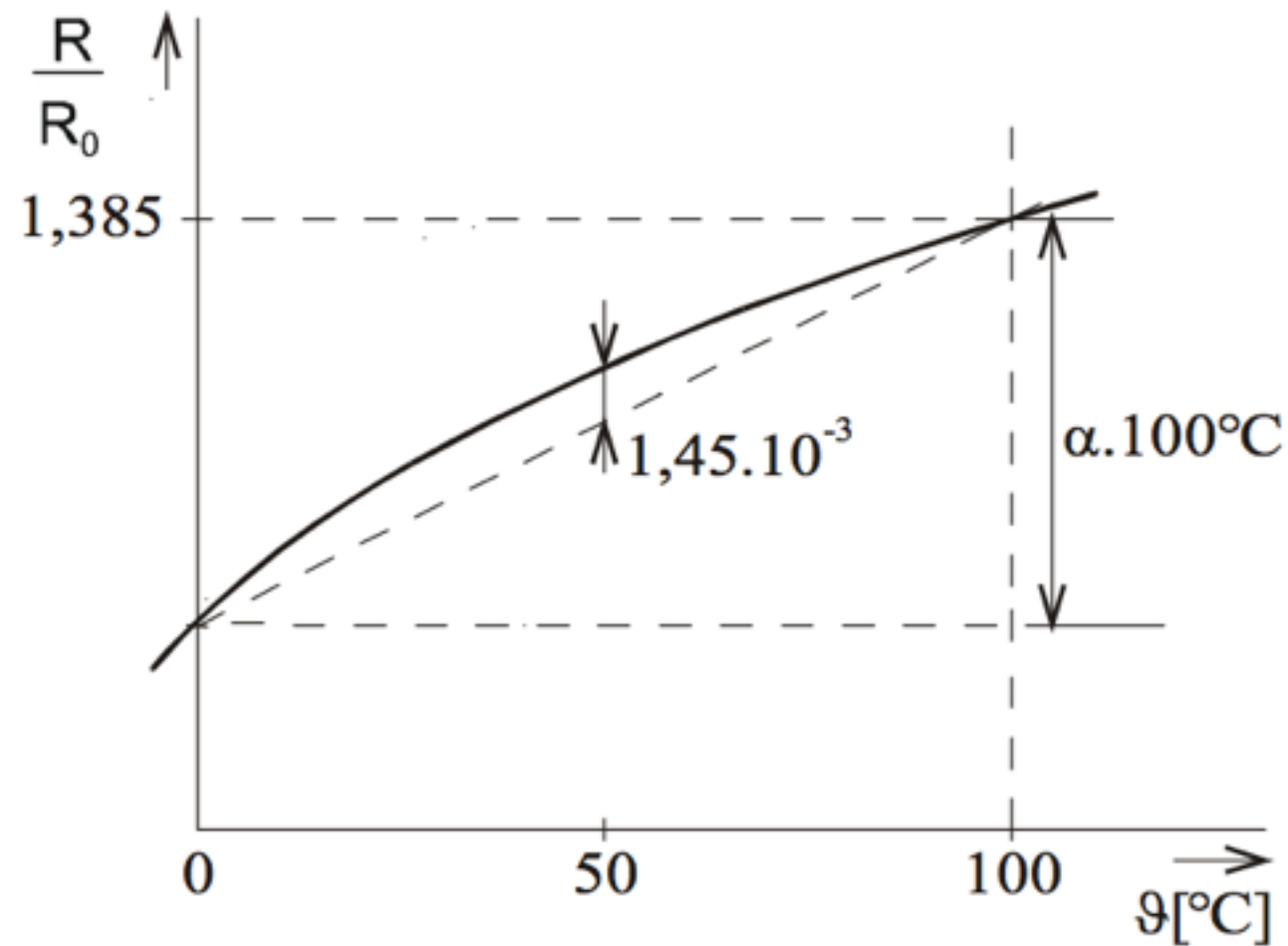


	α [%/K]	range [°C]
Platinum	0.39	- 200 / 850
Nickel	0.69	- 80 / 320
Copper	0.43	- 200 / 260



Platinum resistive thermometers

Normalized resistance



$$R_{100} / R_0 = 1.385$$

Standards define the ratio
between the resistance at 100°C
and the resistance at 0°C

(1.3910 in GB, USA, Japan, Russia)

The resistance is not linear

$$R_t = R_0 [1 + A \cdot t + B \cdot t^2 + C \cdot t^3 (t - 100)]$$

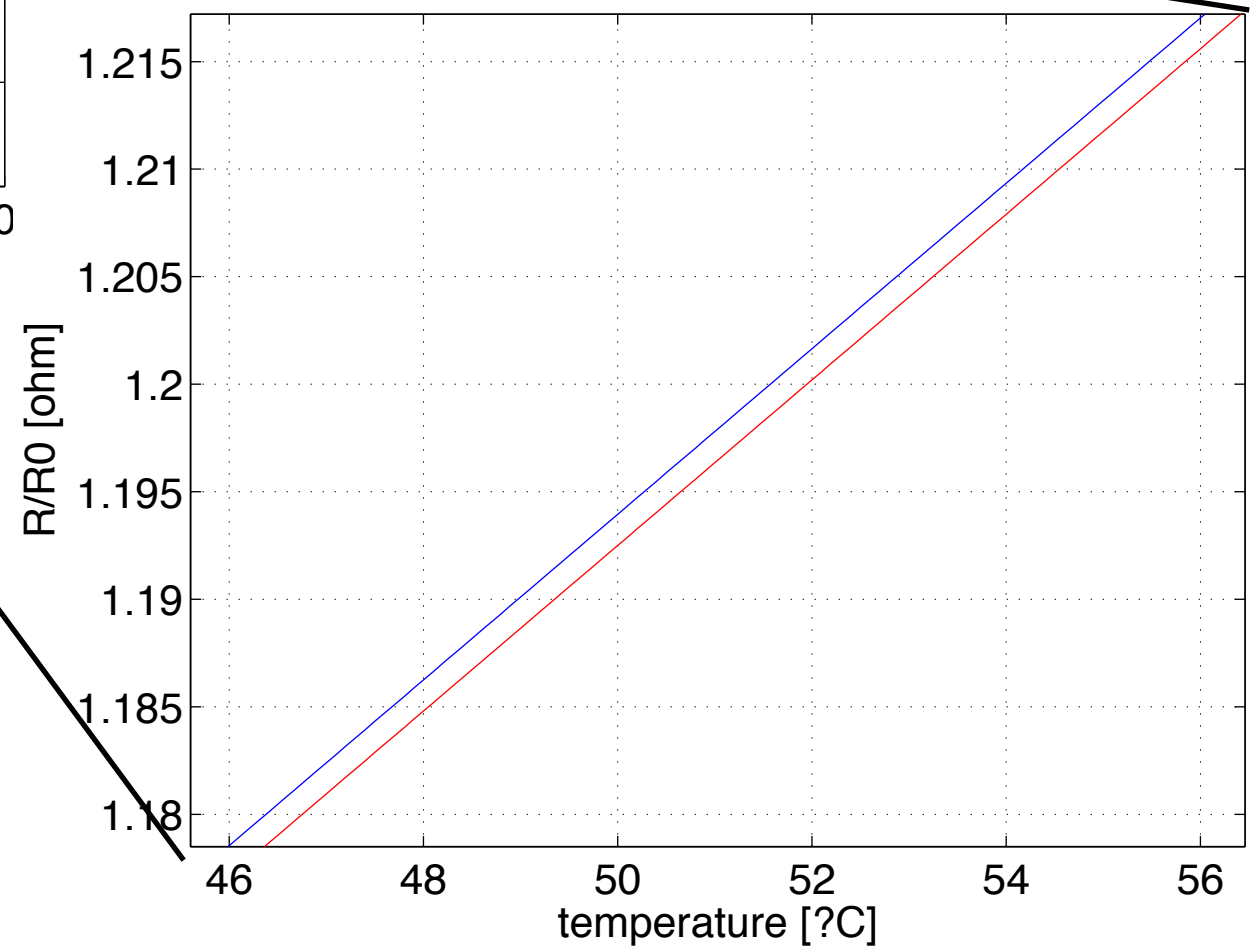
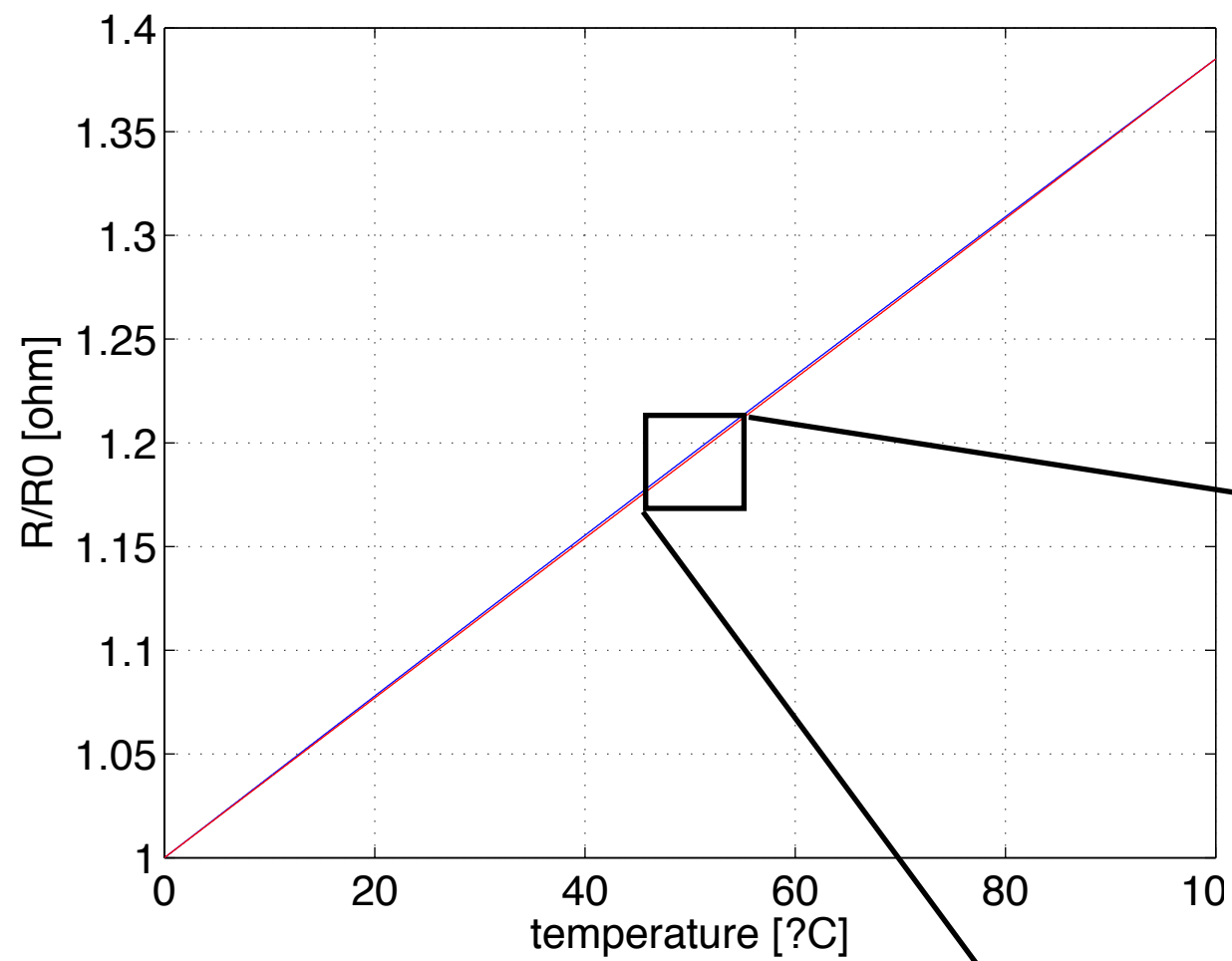
$$A = 3.90802 \cdot 10^{-3} \text{ K}^{-1}$$

$$B = -5,802 \cdot 10^{-7} \text{ K}^{-2}$$

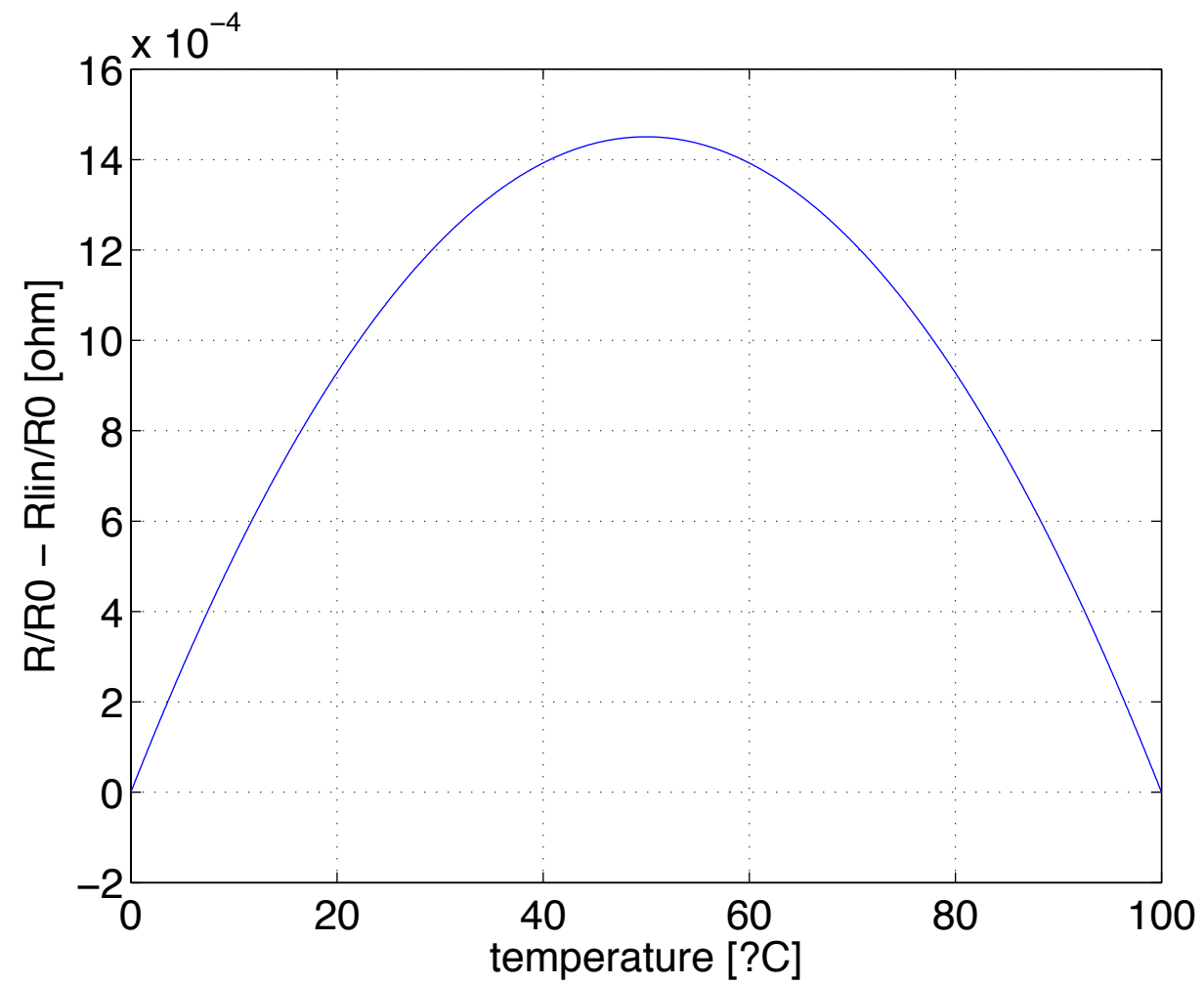
$$t < 0^{\circ}\text{C} \quad C = -4,27350 \cdot 10^{-12} \text{ K}^{-4}$$

$$t > 0^{\circ}\text{C} \quad C = 0$$

Actual non-linearity



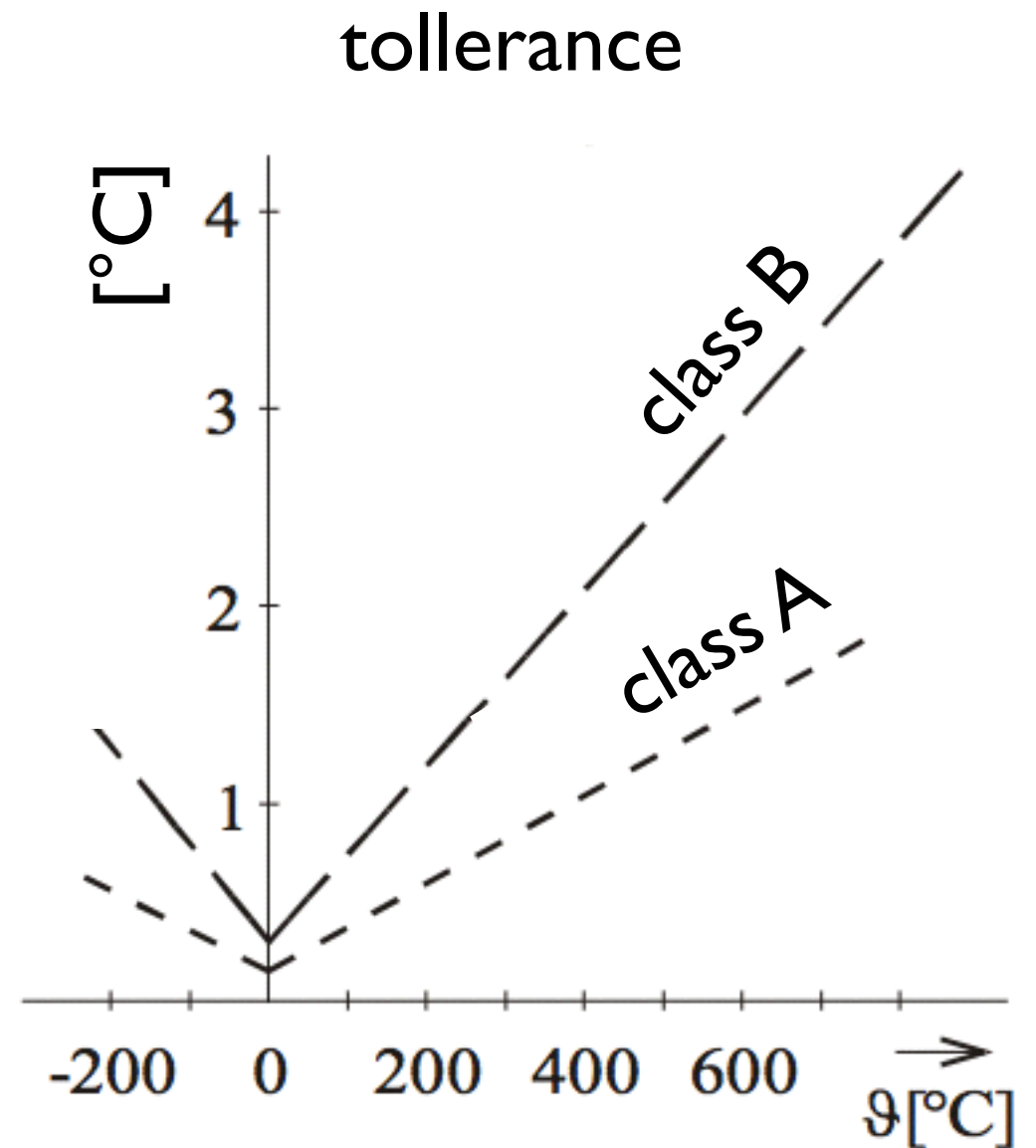
Actual non-linearity



Standard value of Pt resistance:

$Pt100 \rightarrow 0^{\circ}C \ R = 100 \ \Omega$

200, 500, 1000, 2000 Ω



Nickel resistance thermometer:

- high sensitivity, quick response, small dimensions
- limited temperature range

$$R_t = R_0 [1 + A \cdot t + B \cdot t^2 + C \cdot t^3 (t - 100)]$$

$$A = 5.49 \cdot 10^{-3} \text{ K}^{-1}$$

$$B = 6.80 \cdot 10^{-6} \text{ K}^{-2}$$

$$C = 9.24 \cdot 10^{-9} \text{ K}^{-3} \text{ for } t > 0 \text{ (else } C = 0)$$

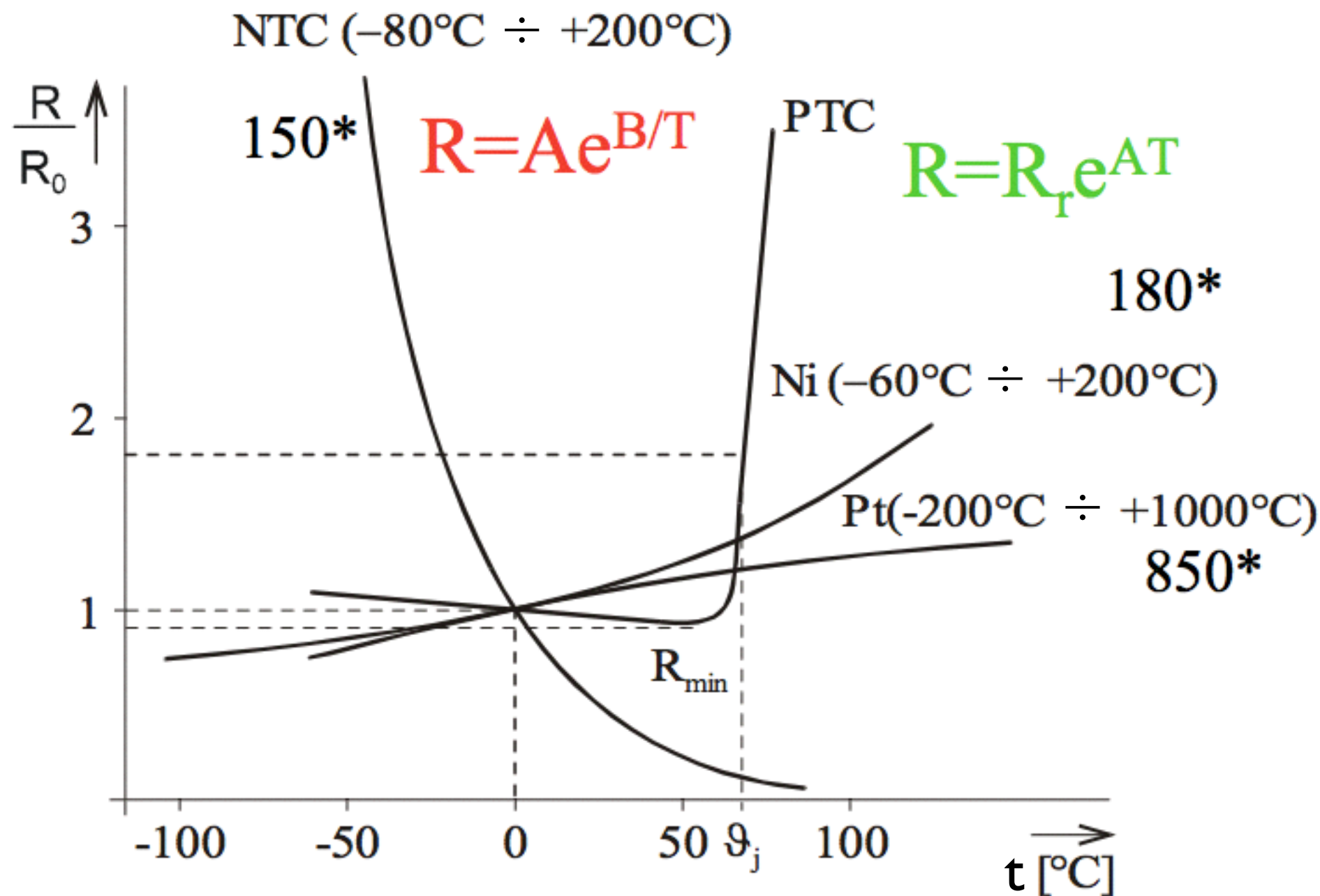
Copper resistance thermometer:

- limited range (from -200°C to $+200^\circ\text{C}$)
- small resistance
- direct measurement of windings temperature

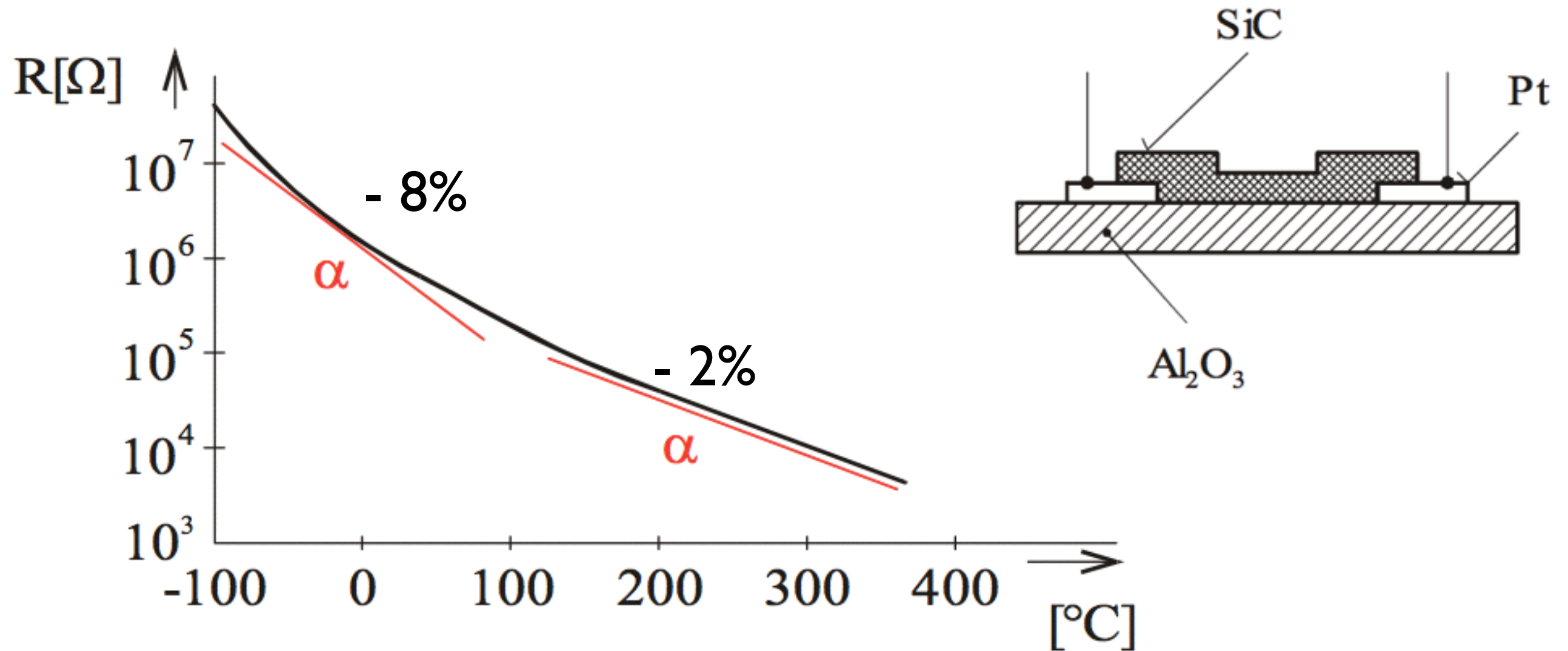
$$R_t = R_0 [1 + \alpha \cdot t] \quad \alpha = 4.26 \cdot 10^{-3} \text{ K}^{-1}$$

Semiconductor resistive sensors of temperature

Thermistor PTC - Positive Temperature Coefficient
 NTC - Negative Temperature Coefficient



NTC - Negative Temperature Coefficient



- produced e.g. by sintering technology from the powder of metal oxides
- usable range - from 4.2K to 1000 °C

$$R = A \cdot e^{\frac{B}{T}}$$

$$\begin{aligned} R_1 &= A \cdot e^{\frac{B}{T_1}} \\ R_2 &= A \cdot e^{\frac{B}{T_2}} \end{aligned} \rightarrow \frac{R_1}{R_2} = e^{\left(\frac{B}{T_1} - \frac{B}{T_2}\right)} \rightarrow B$$

PTC, posistors

$\alpha > 0$

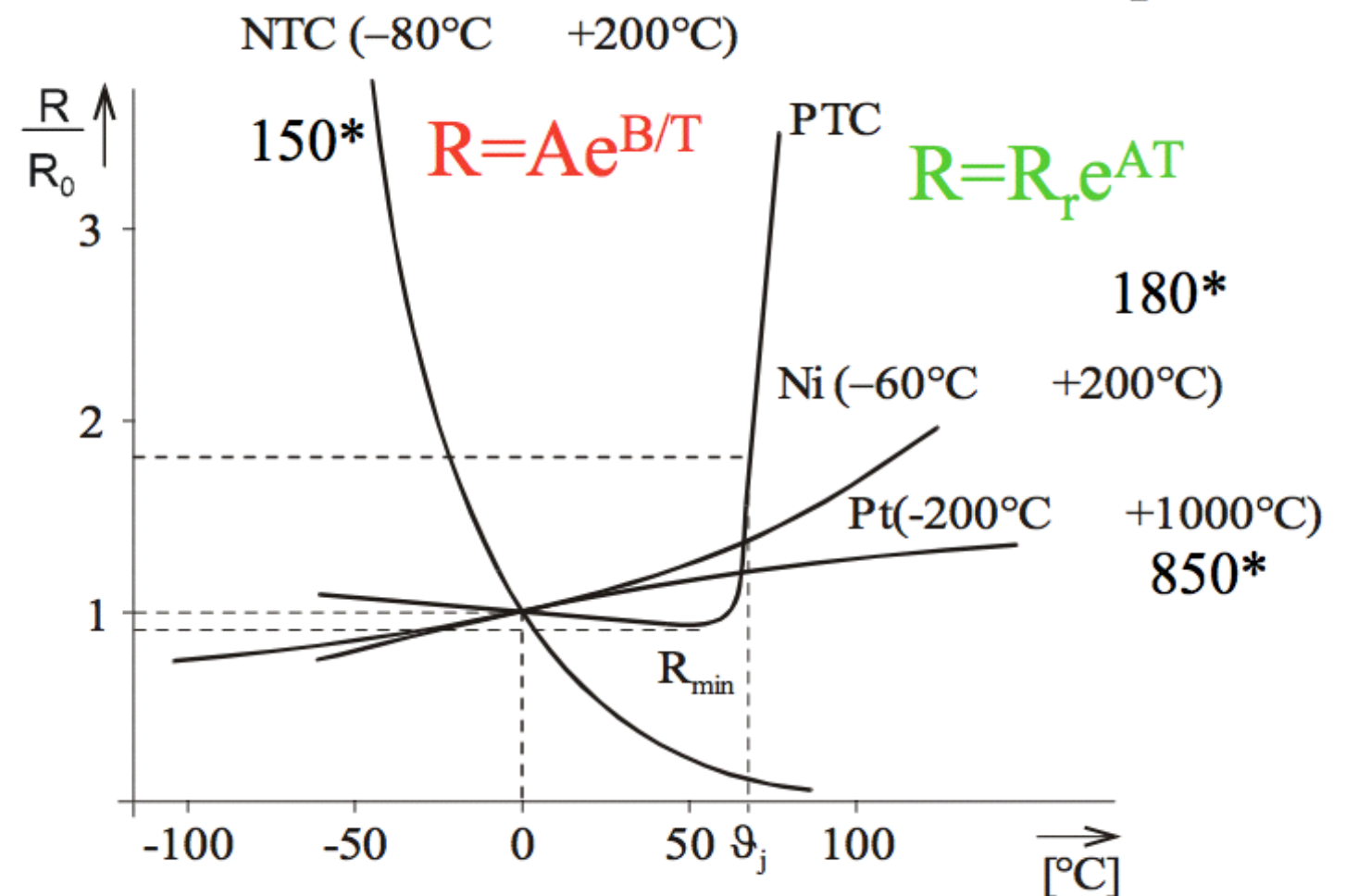
- made from polycrystalline ferroelectric ceramics e.g. (BaTiO_3)

- application: two state sensors

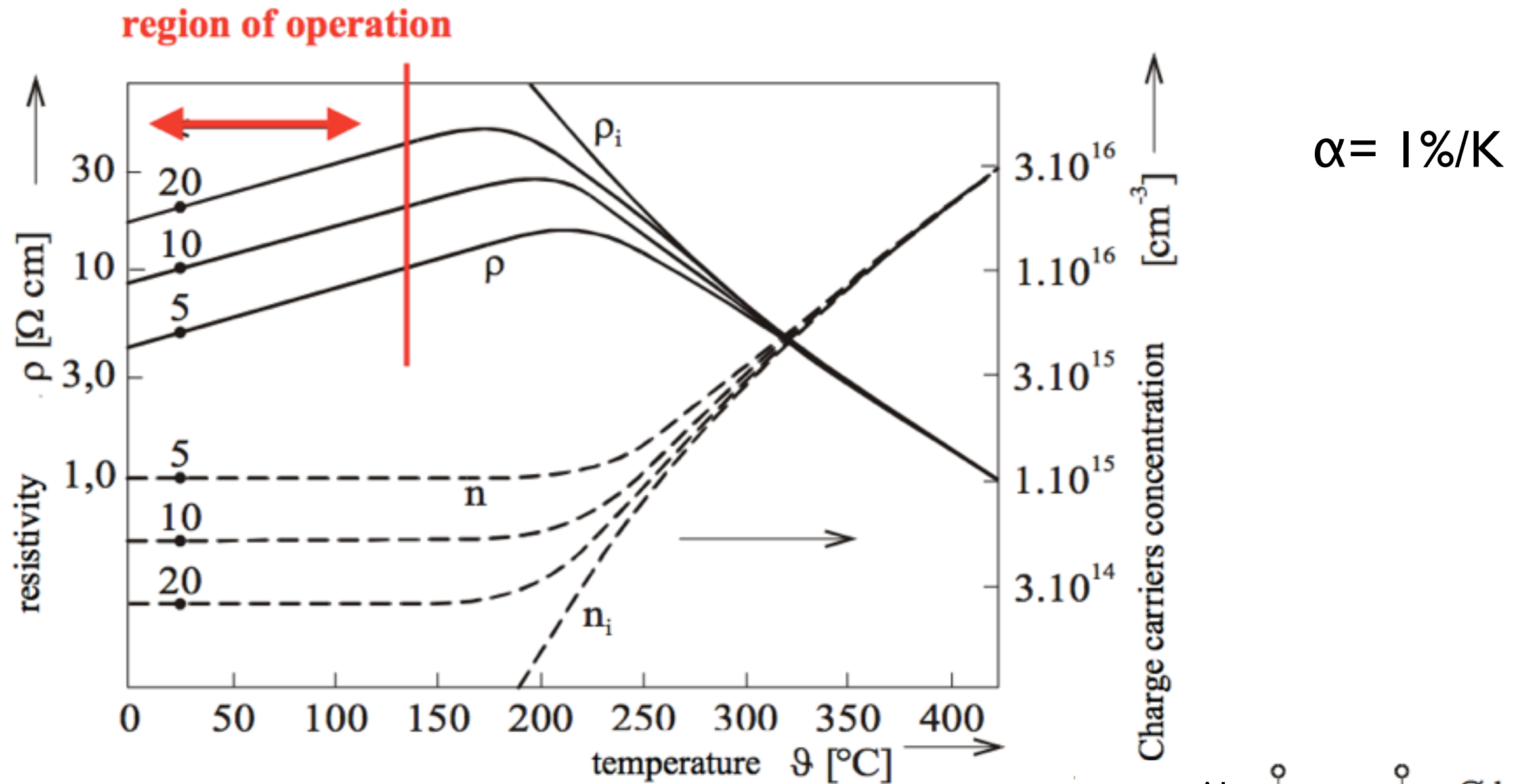
(thermal switches – indication of excessing max. temp.)

resistance slowly decrease
with increasing
temperature

after Curie point rapid increase
of resistance - relation for
increase of resistance



Semiconductor monocrystalline sensors of temperature



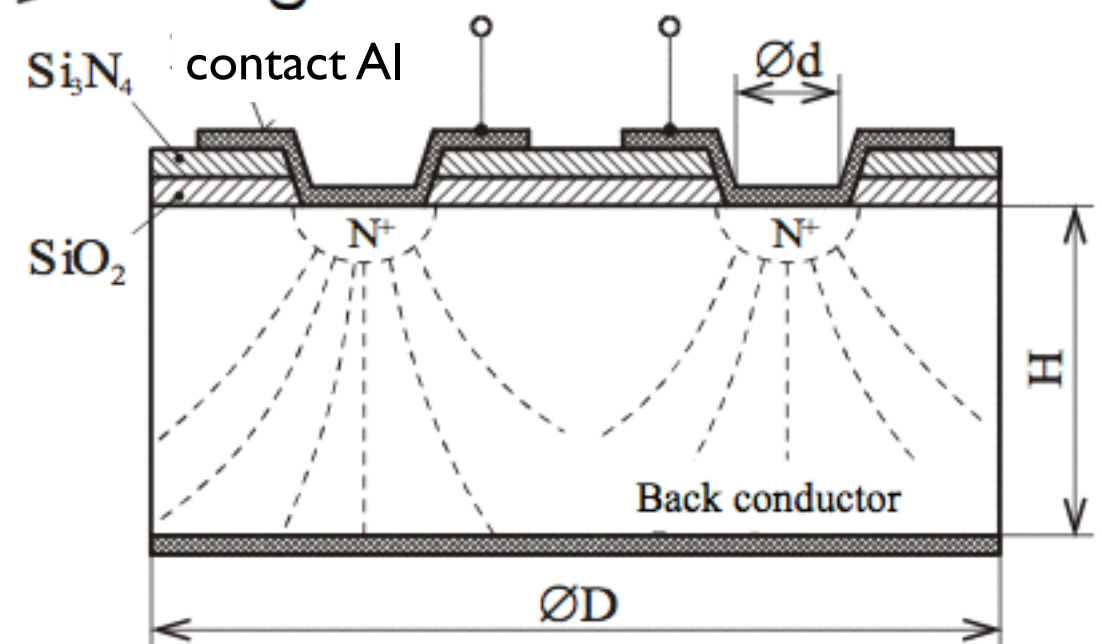
Resistance of the sensor

$$R = \frac{\rho}{\beta d}$$

β – geometrical factor

d – diameter of contact

ρ – resistivity



Problem: in order to measure a resistance we need to inject a current which generates heat!

SELF HEATING

difference of temperature given by self heating:

$$\Delta T = \frac{RI^2}{D}$$

power loss

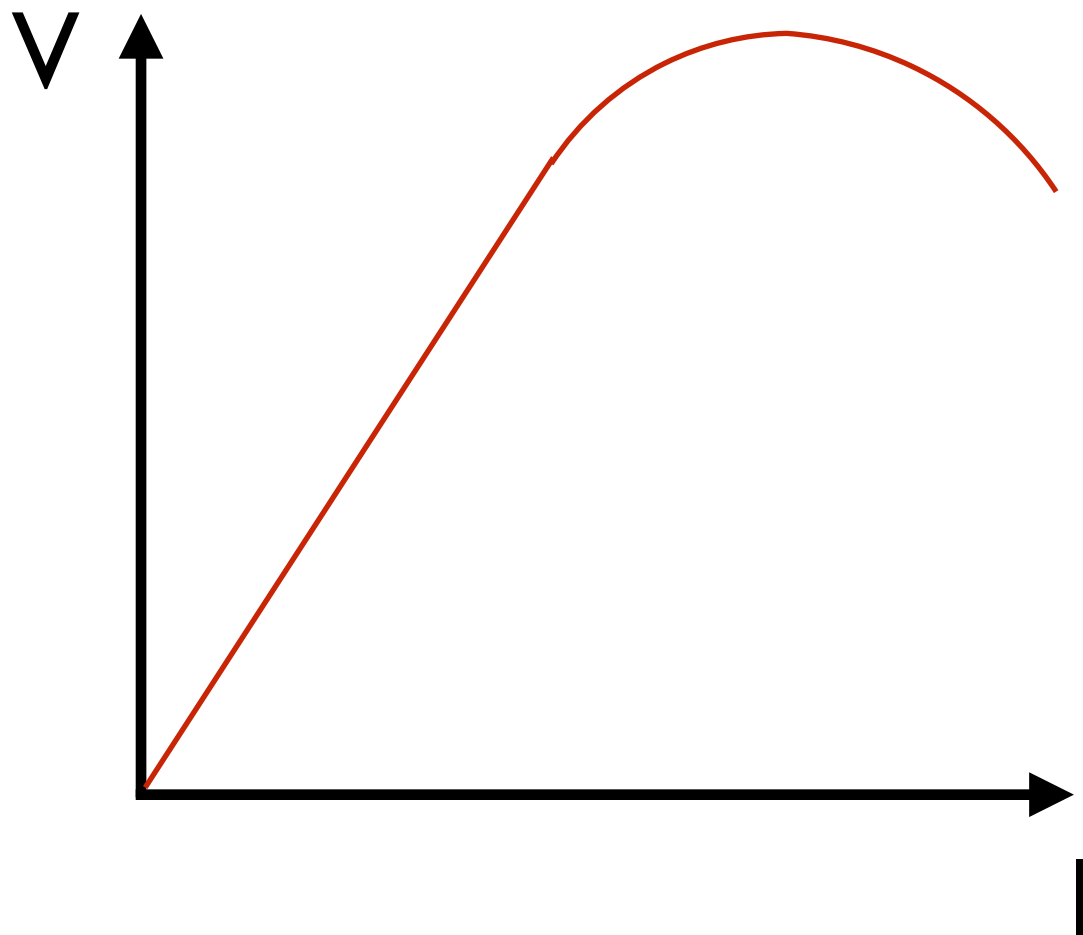
thermal resistance

Pt100 : max 1 mA to have max $\Delta T = 0.1^\circ\text{C}$

Effect of self heating on

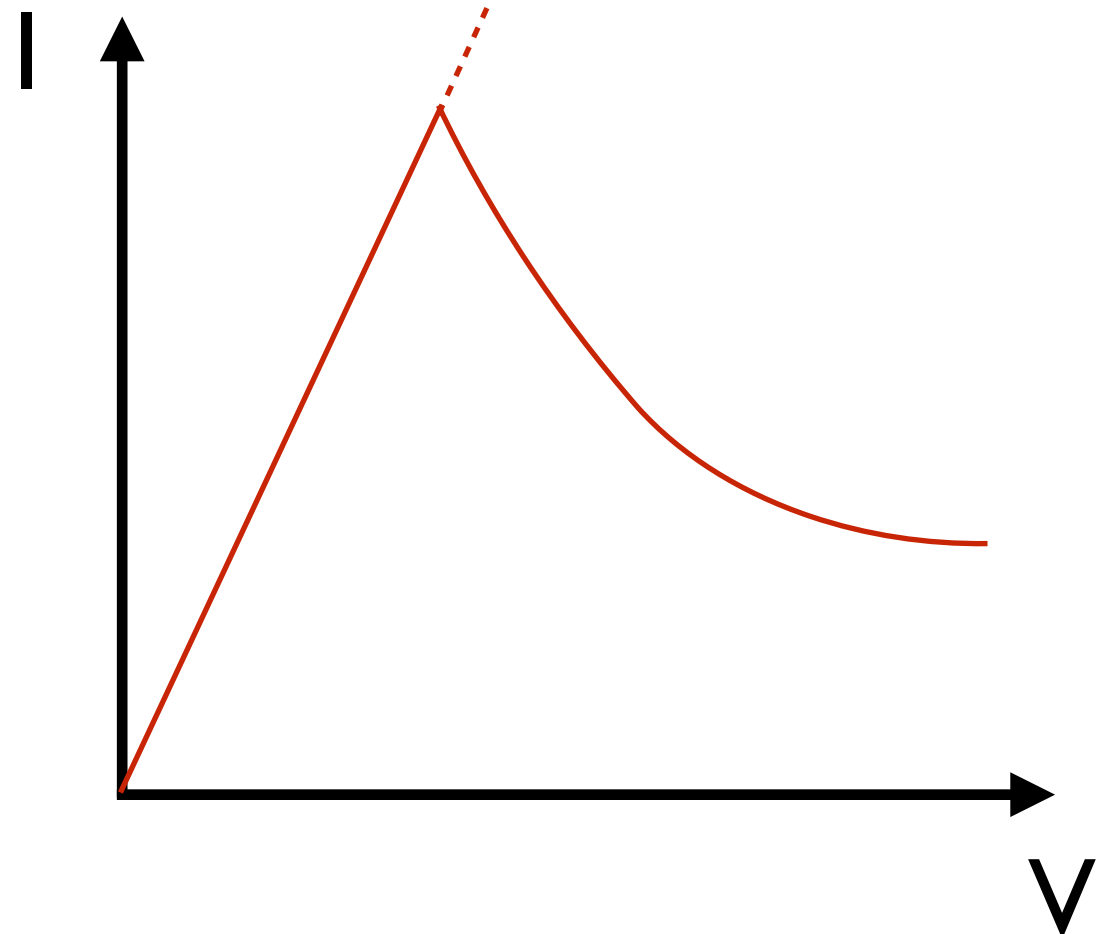
negastor (NTC thermistor)

at high I the temp increases so the R drops and therefore $V=RI$ drops.

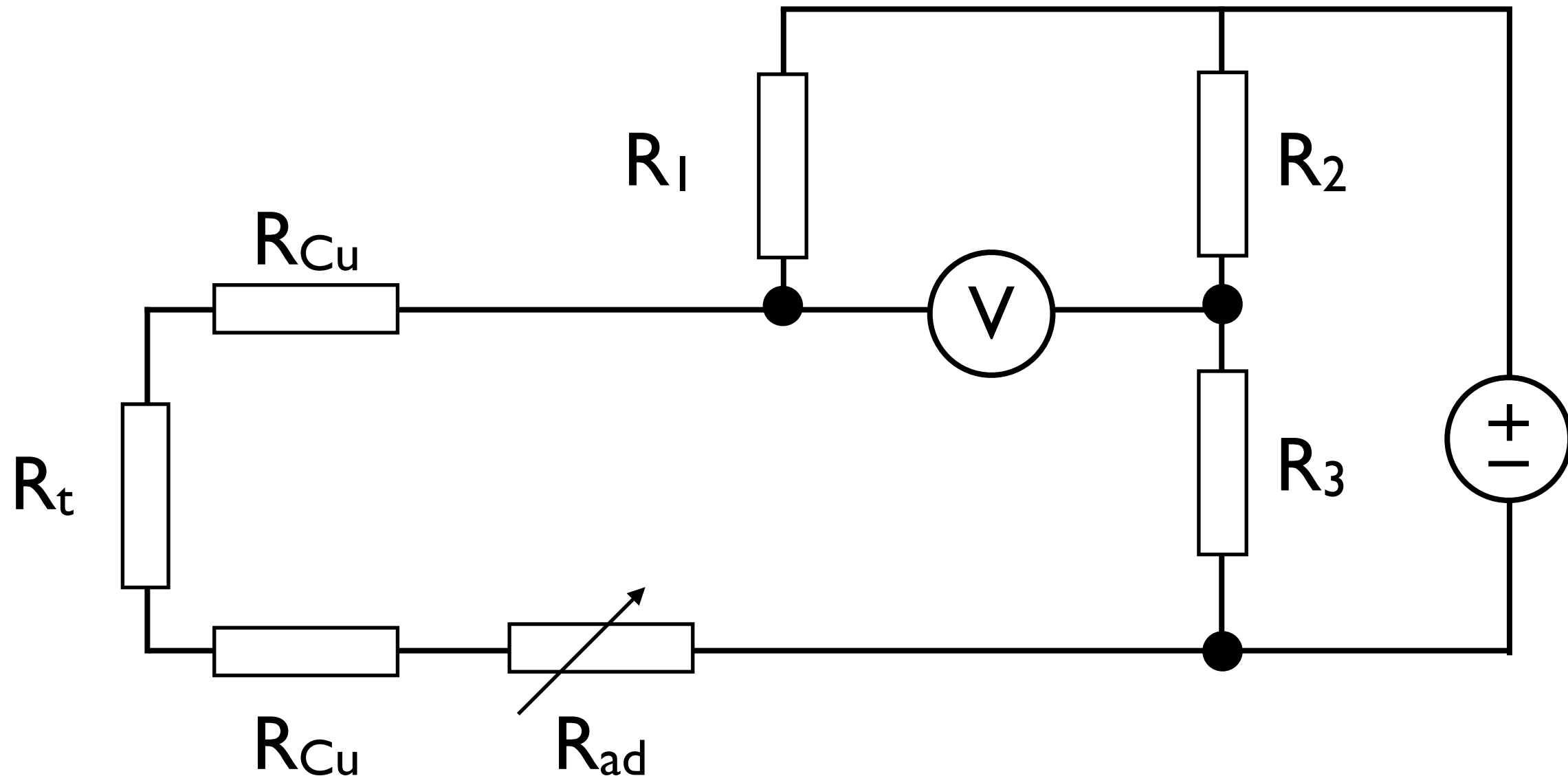


posistor (PTC thermistor)

we can't increase I because increment of I would increase R and then decrease I back.

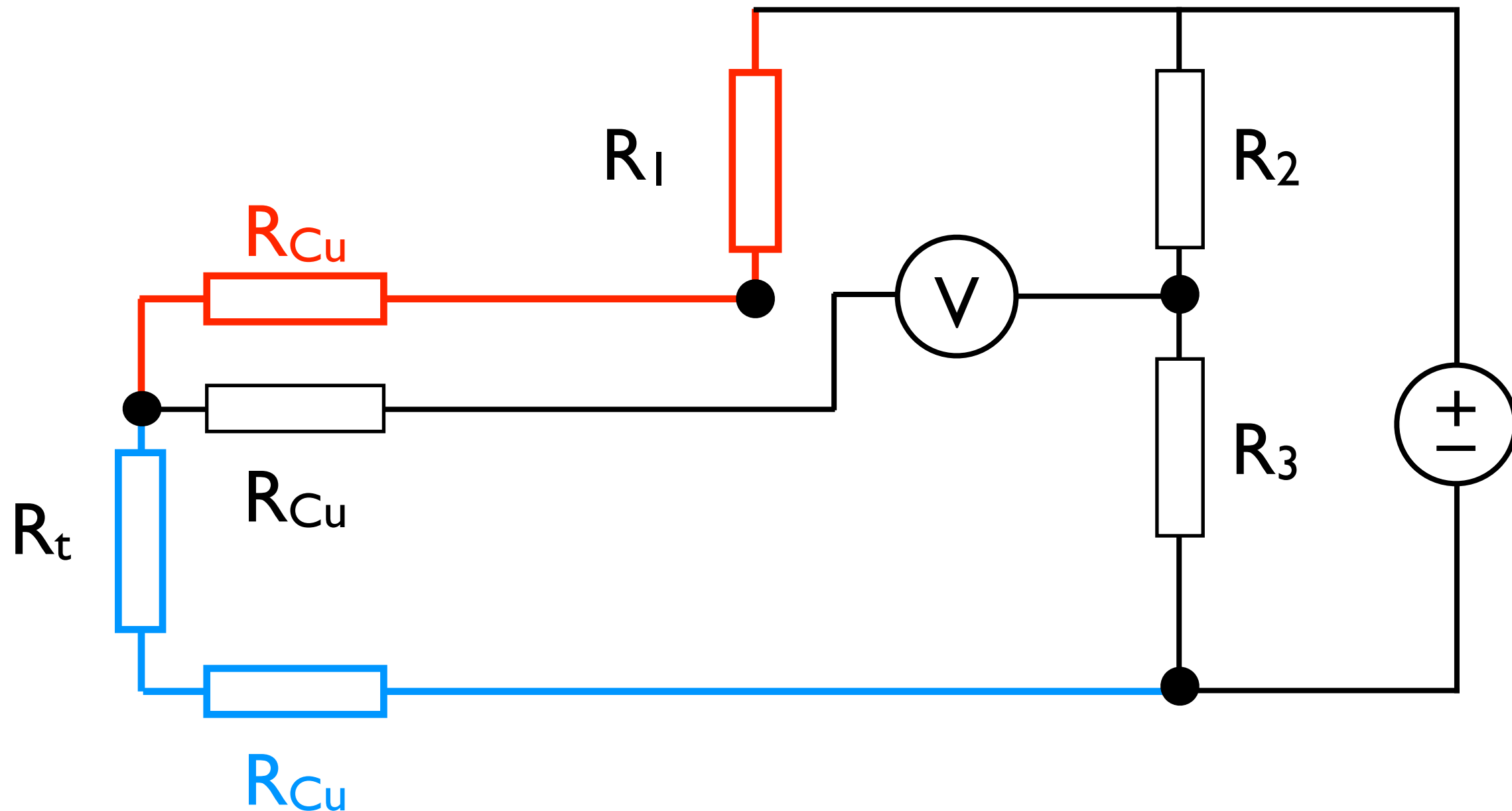


Two wire connection in a bridge



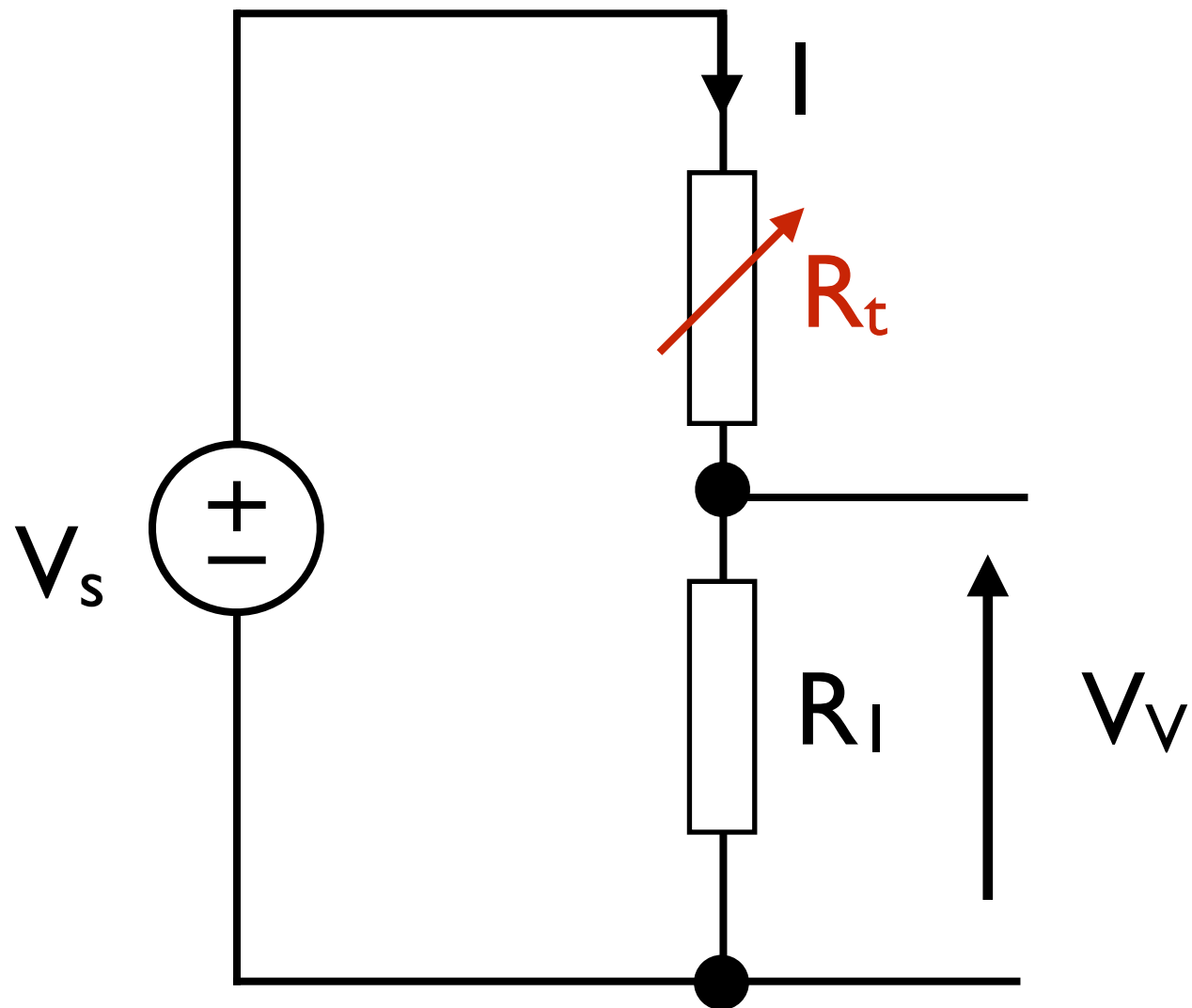
R_{ad} can be adjusted to balance the bridge and null the contribution of R_{Cu} .
Problem: the resistance of the cables might change too with temperature

Three wire connection in a bridge



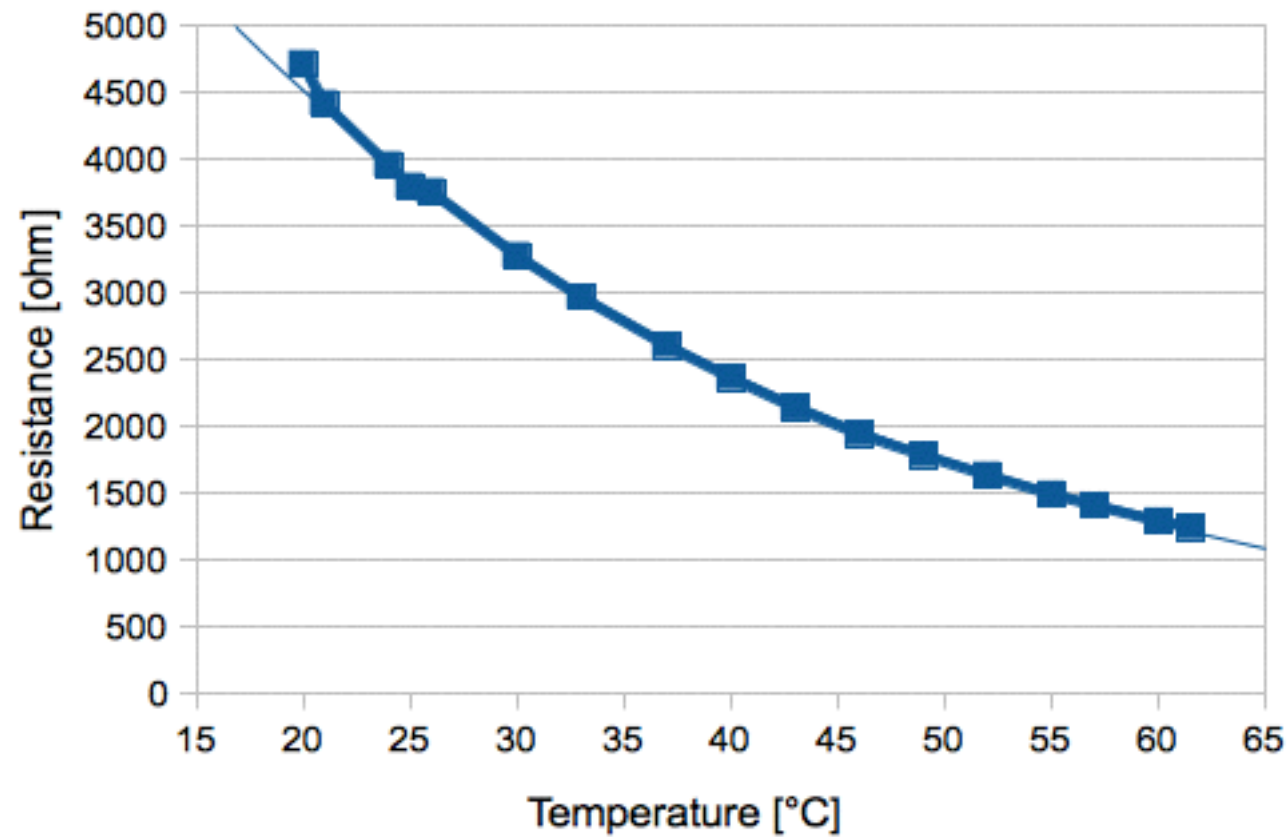
Two resistances of the cables fall in opposite sides of the bridge's leg, the compensate each other. The 3rd cable resistance has no effect ($I_v=0$)

Linearization of thermistor with a series resistor



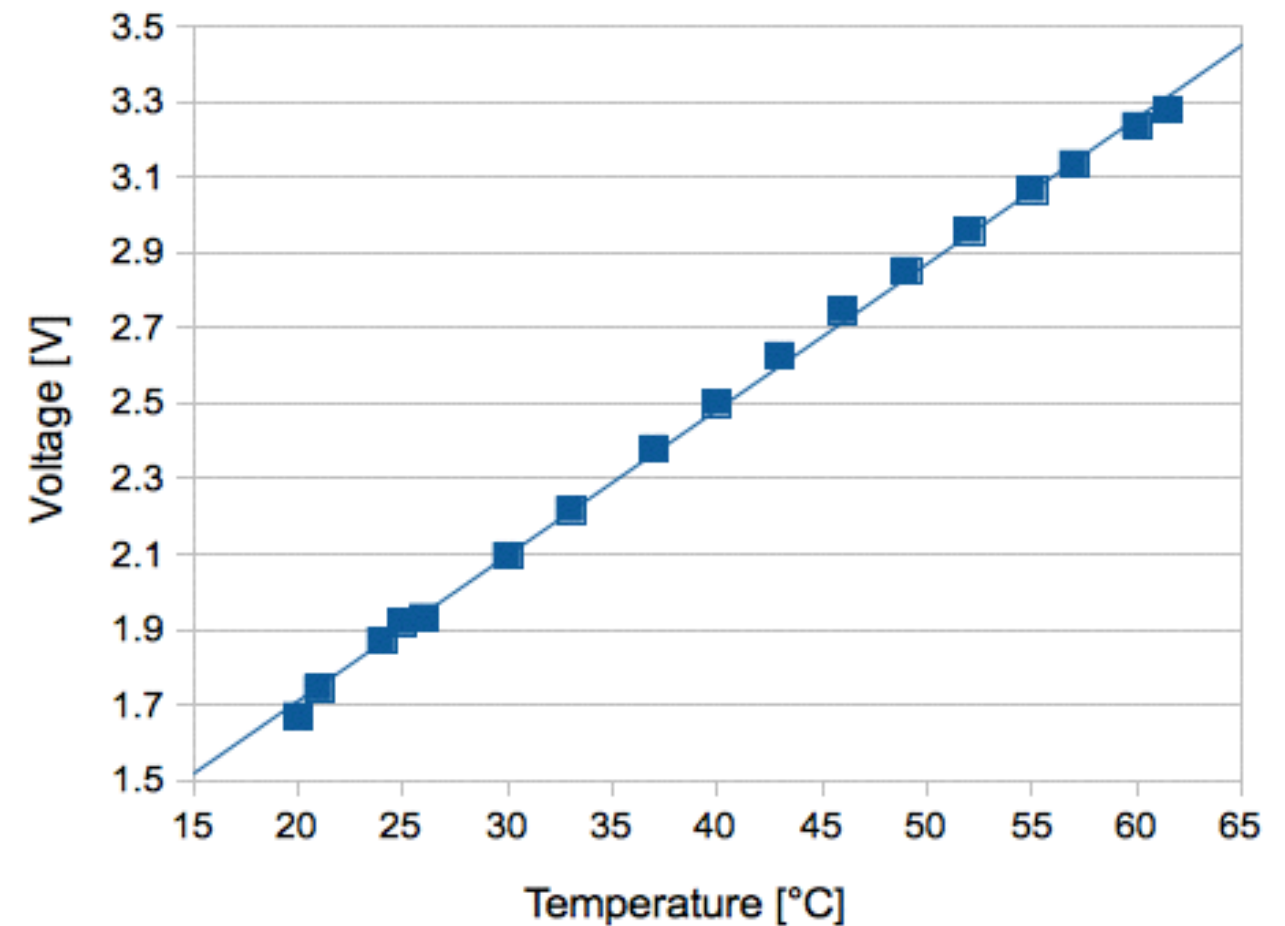
$$V_{\text{lin}} = V_s \frac{R_I}{R_I + R_t}$$

Linearization of thermistor with a series resistor

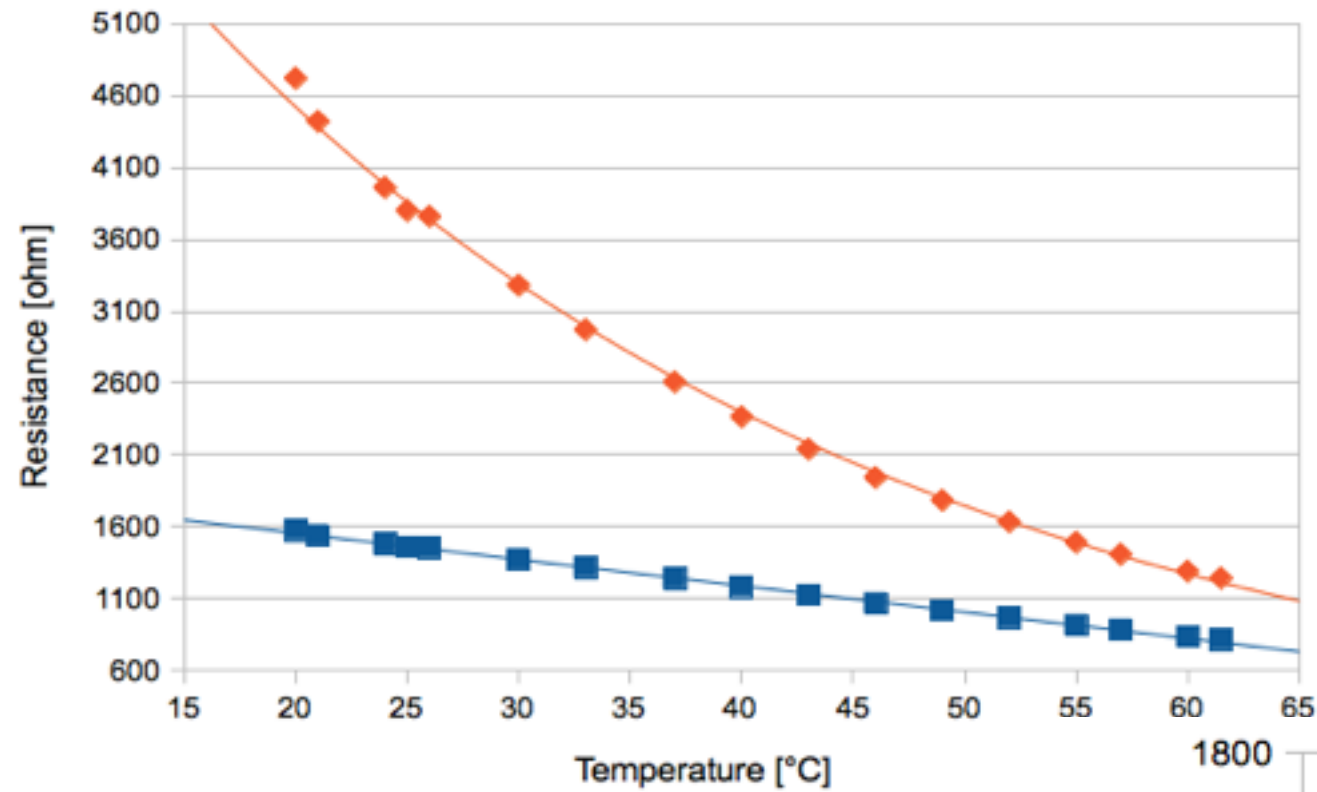


$$V_s = 5 \text{ V}$$

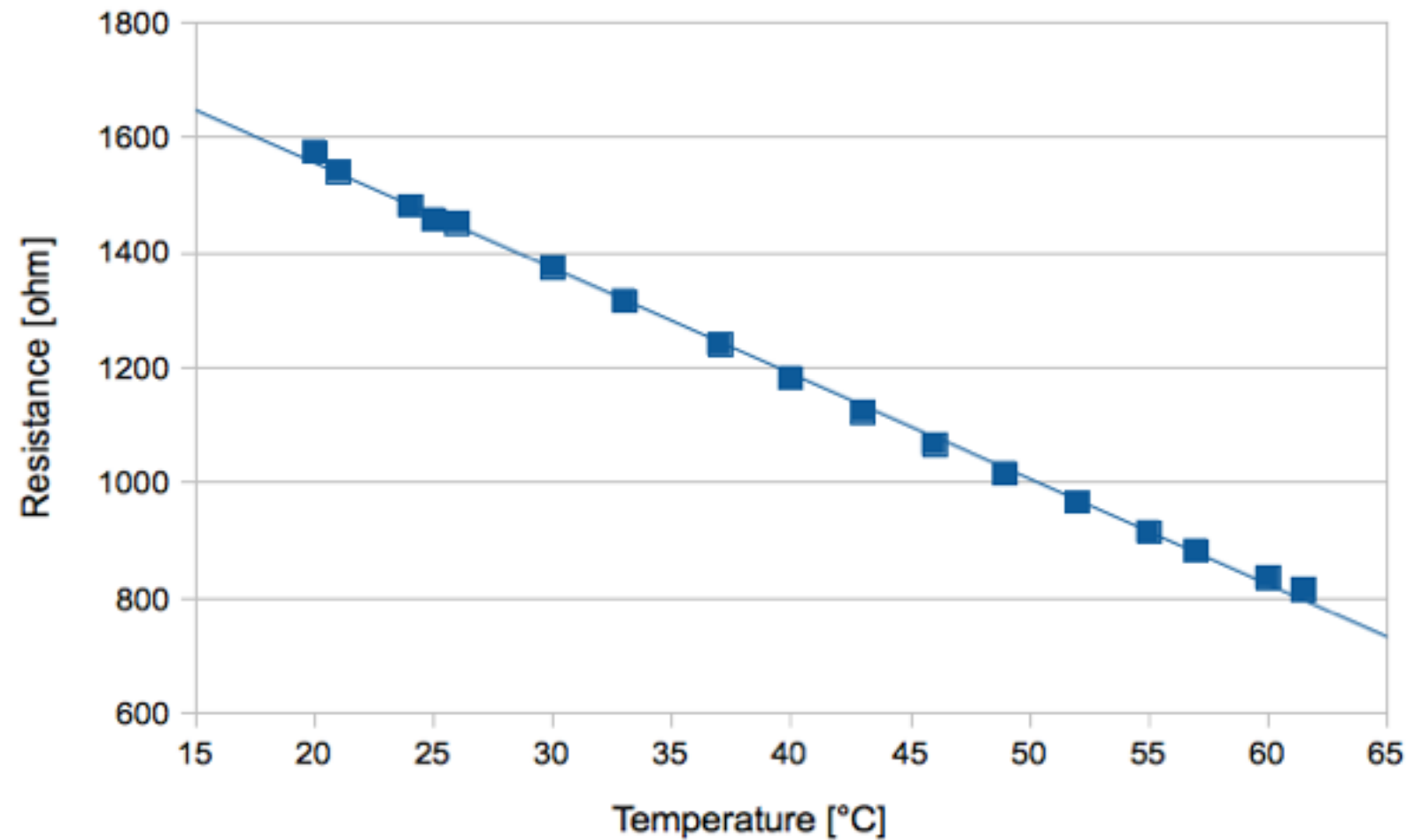
$$R_I = 2,365 \text{ } \Omega$$



Linearization of thermistor with parallel resistor

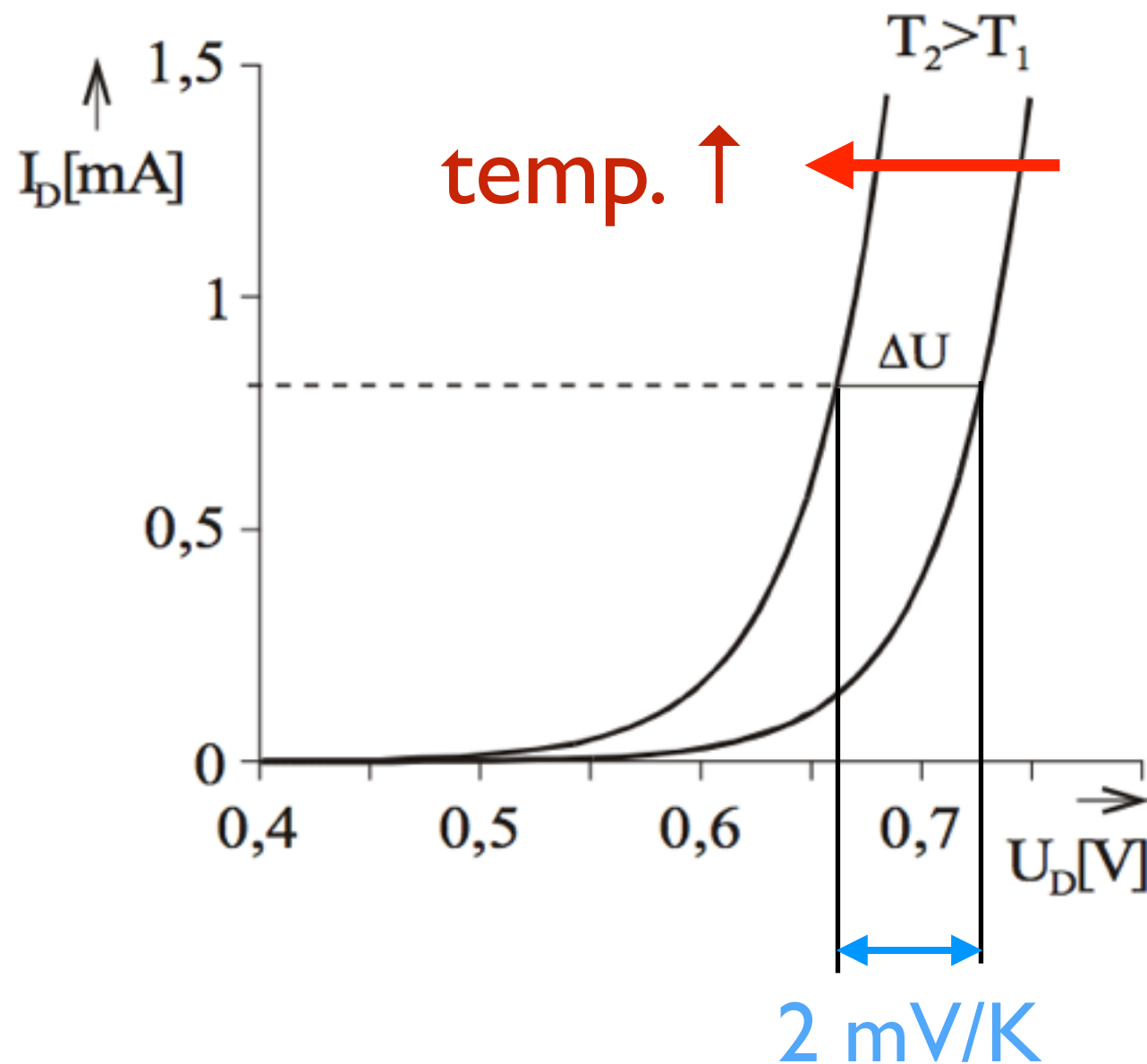


$$R_p = 2,365 \, \Omega$$



PN junction based sensors of temperature

The V-I curve of PN junction depends on temperature



Shockley equation

$$I_D = I_S \left(e^{\frac{V_D}{mV_T}} - 1 \right)$$

$$V_D = m \cdot V_T \cdot \ln \left(\frac{I_D}{I_S} + 1 \right)$$

I_S – reverse saturation current

I_D - forward current in PN junction

m – coefficient of recombination

V_D – forward voltage on PN junction

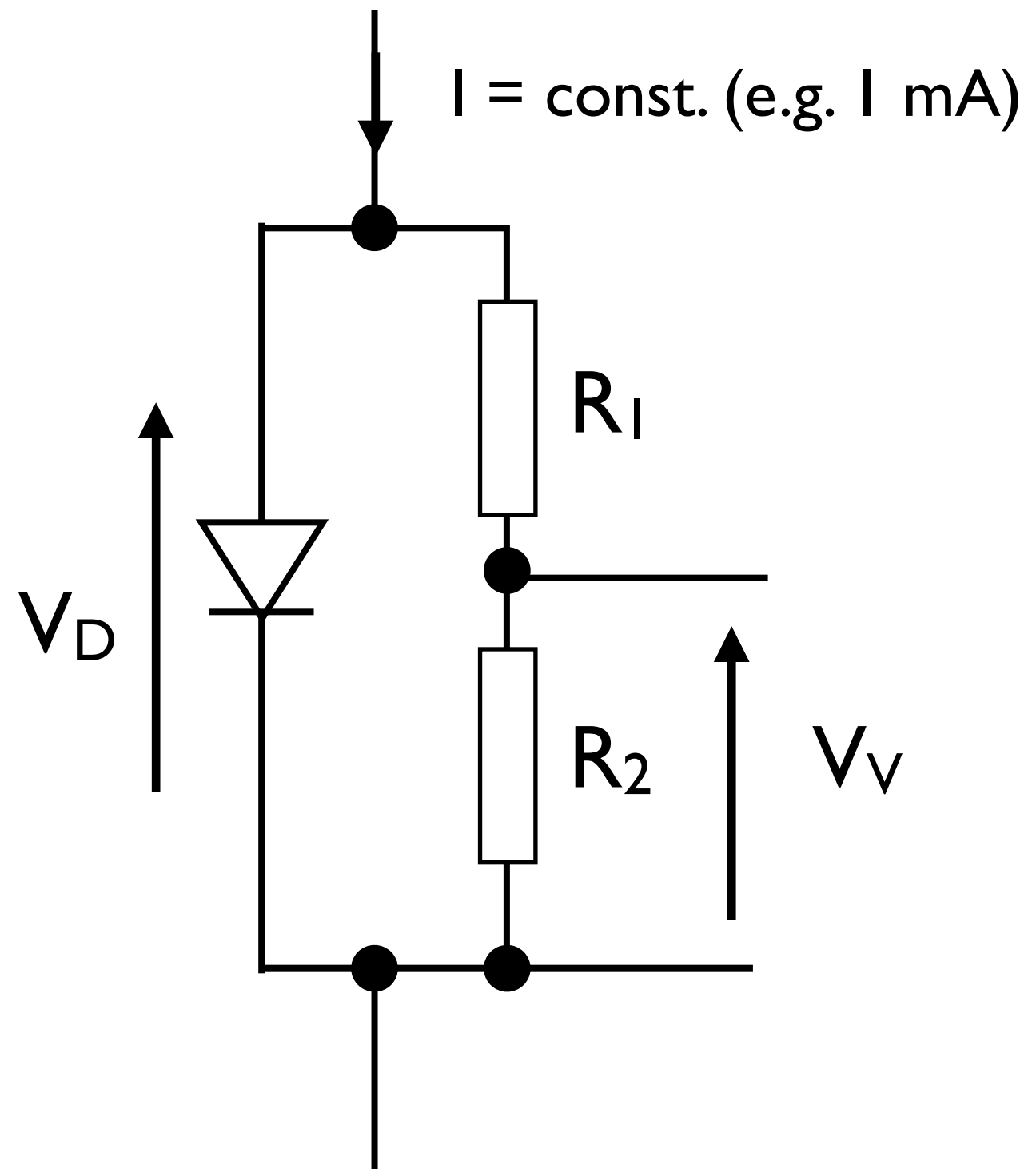
V_T – thermal voltage

e – elementary charge

k – Boltzmann constant

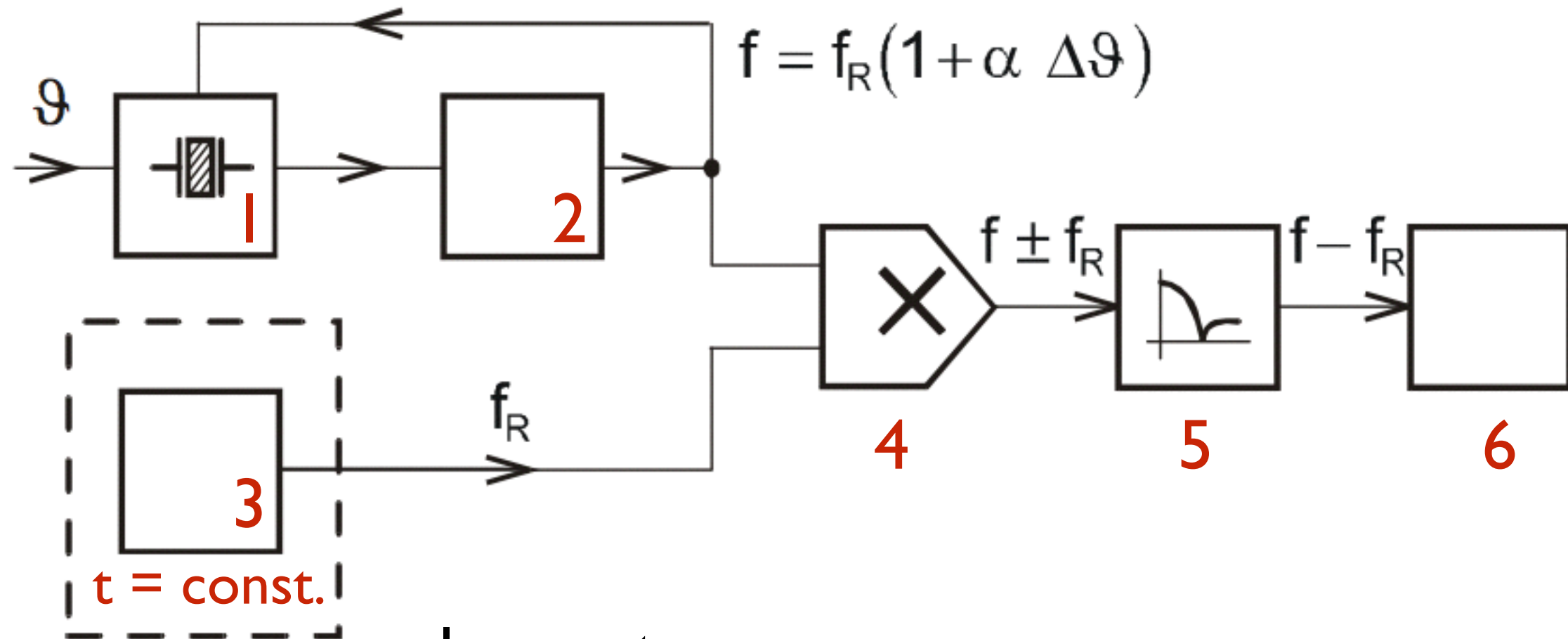
$$V_T = \frac{kT}{e}$$

This principle can be used to create a compensation circuit for thermocouples cold end



V_D changes with about 2 mV/K.
A voltage divider is used to
achieved the desired sensitivity.

Quartz thermometer



- 1 – quartz
- 2 – quartz controlled oscillator
- 3 – ref. quartz controlled oscillator (thermostated)
- 4 – mixer (analogue multiplier)
- 5 – low frequency filter (4+5=synchronous detector)
- 6 – counter with display

very precise!

Reversible temperatur labels



Omega



Non-reversible temperatur labels

