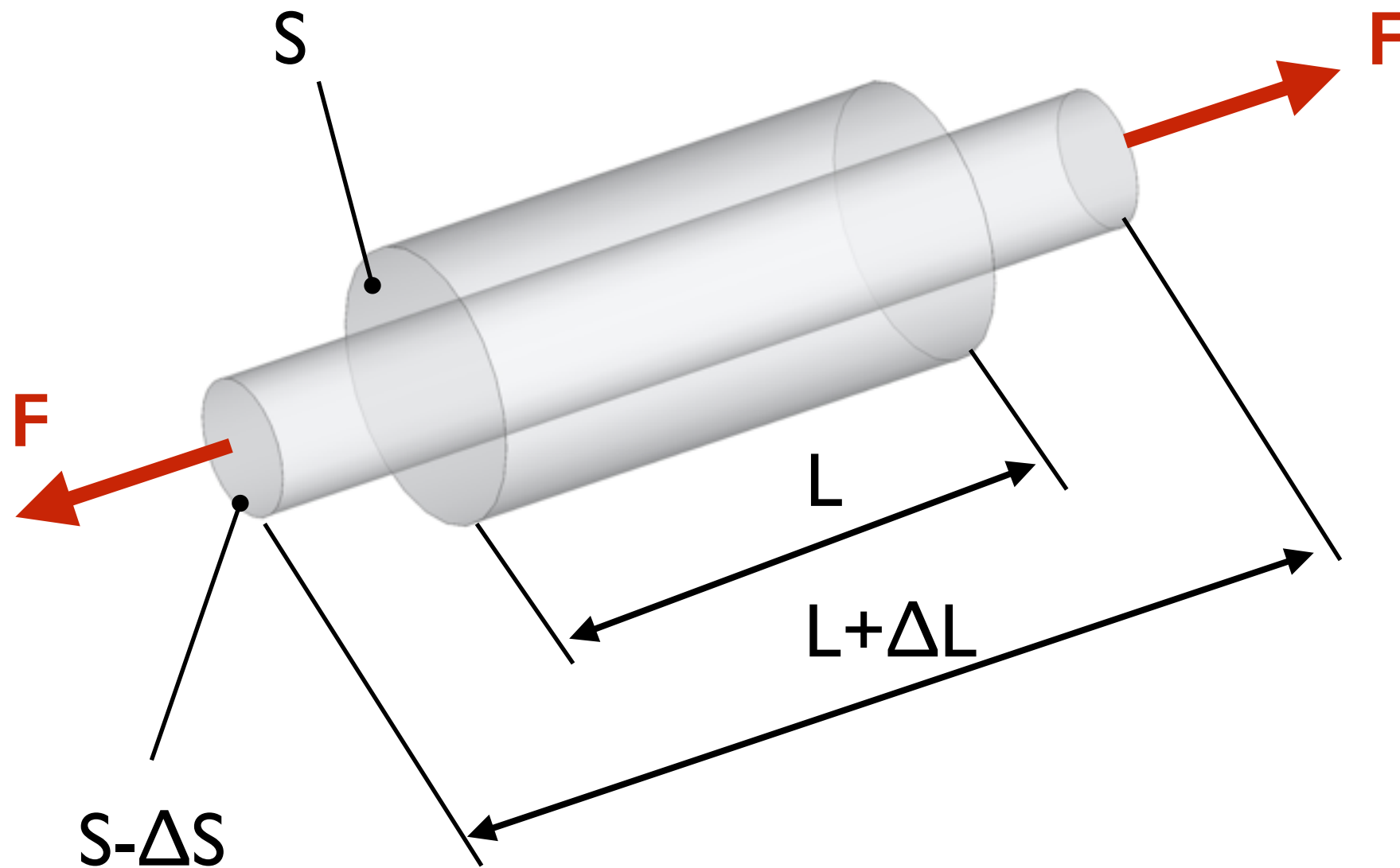


Sensors of force and pressure

AE3B38SME - Sensors and Measurement

Strain gauges



$$R = \rho \frac{L}{S}$$

$$\frac{\Delta R}{R} = \frac{\Delta \rho}{\rho} + \frac{\Delta L}{L} - \frac{\Delta S}{S}$$

$$R \cong R_0 + \frac{dR}{d\rho}(\rho - \rho_0) + \frac{dR}{dL}(L - L_0) + \frac{dR}{dS}(S - S_0)$$

$$\Delta R = R - R_0 \cong \frac{dR}{d\rho}(\rho - \rho_0) + \frac{dR}{dL}(L - L_0) + \frac{dR}{dS}(S - S_0)$$

$$\cong \frac{L}{S}(\rho - \rho_0) + \frac{\rho}{S}(L - L_0) - \frac{\rho L}{S^2}(S - S_0)$$

we want to express the relative change $\Delta R / R$ of resistance to the relative deformation $\varepsilon = \Delta L / L$

$$\frac{\Delta S}{S} = -2\mu \frac{\Delta L}{L}$$

μ Poisson ratio

$$\frac{\Delta R}{R} = \frac{\Delta \rho}{\rho} + \frac{\Delta L}{L} - \frac{\Delta S}{S}$$

$$\frac{\Delta S}{S} = -2\mu \frac{\Delta L}{L}$$

$$\frac{\Delta R/R}{\Delta L/L} = 1 + 2\mu + \frac{\Delta \rho/\rho}{\Delta L/L}$$

$$\frac{\Delta R/R}{\Delta L/L} = \frac{\Delta R/R}{\varepsilon} = 1 + 2\mu + \pi_e E$$

piezoresistive coefficient

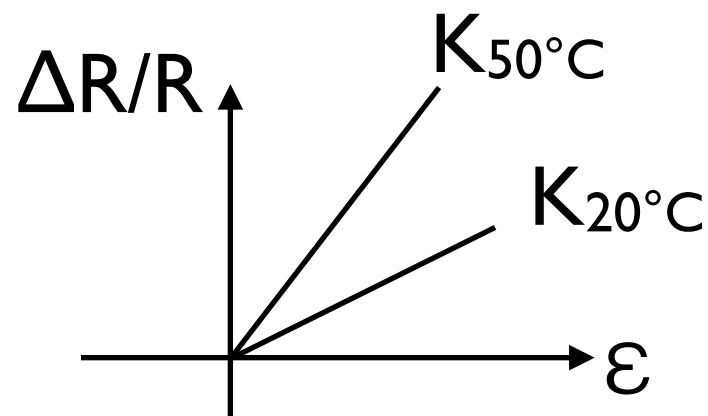
Young module

$$\frac{\Delta R/R}{\Delta L/L} = \frac{\Delta R/R}{\varepsilon} = 1 + 2\mu + \pi_e E$$

$$\Delta R/R = C_1 \varepsilon + C_2 \varepsilon^2 + C_3 \varepsilon^3 + \dots$$

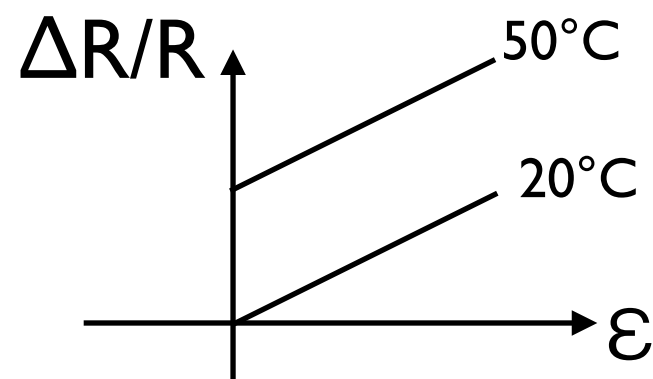
$$K = \frac{d\Delta R/R}{d\varepsilon}$$

strain gauge factor
(how large the response of
the strain gauge is)



$$\alpha_K = \frac{\Delta K/K_{20^\circ\text{C}}}{\Delta \vartheta}$$

temperature coefficient of
sensitivity



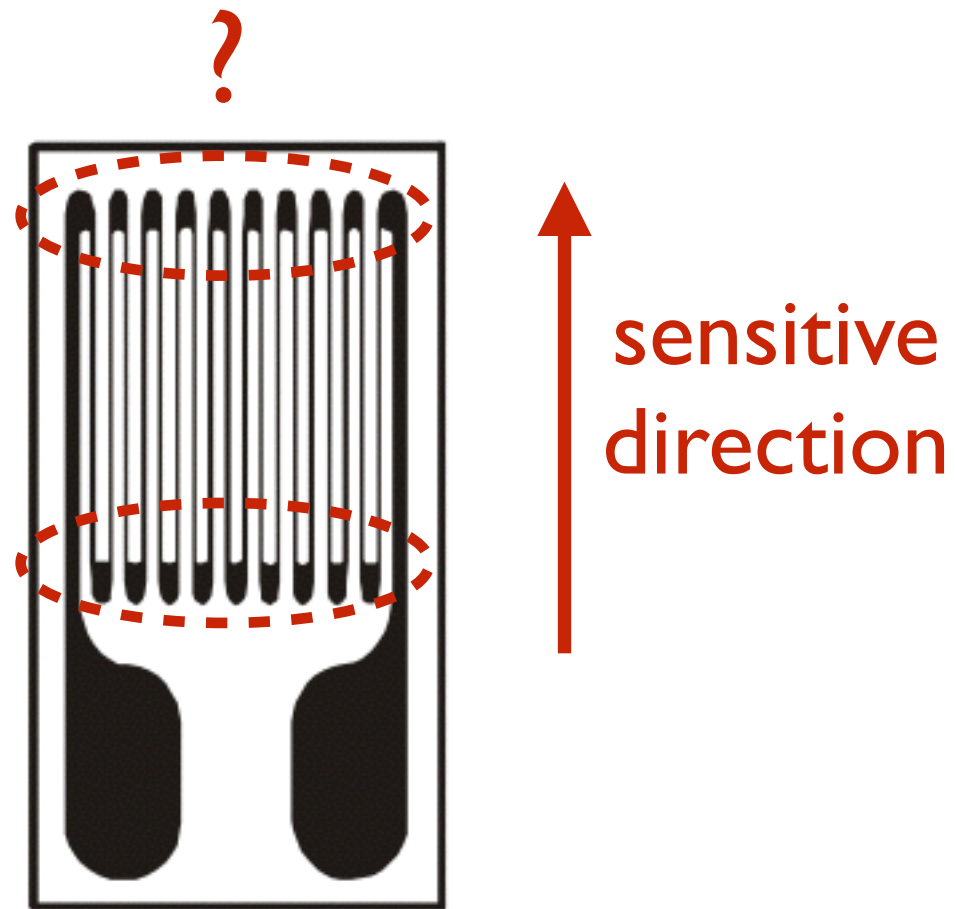
$$\alpha_R = \frac{\Delta R/R_{20^\circ\text{C}}}{\Delta \vartheta}$$

temperature coefficient of
resistance

Metal and semiconductor strain gages

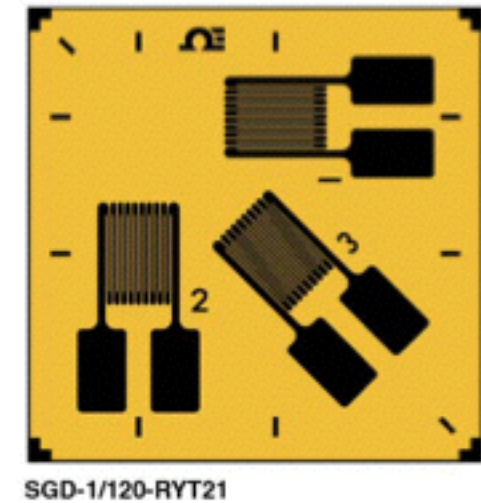
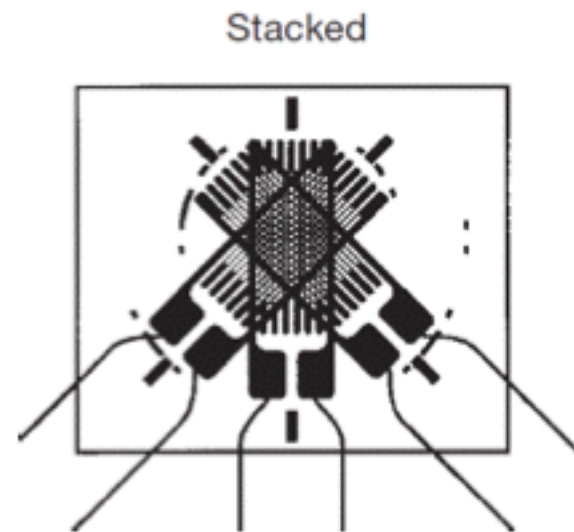
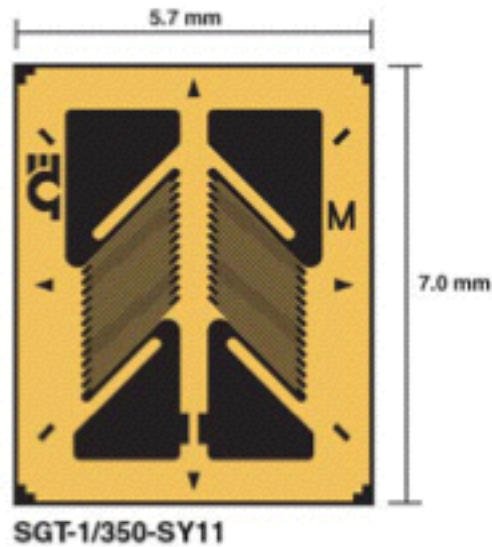
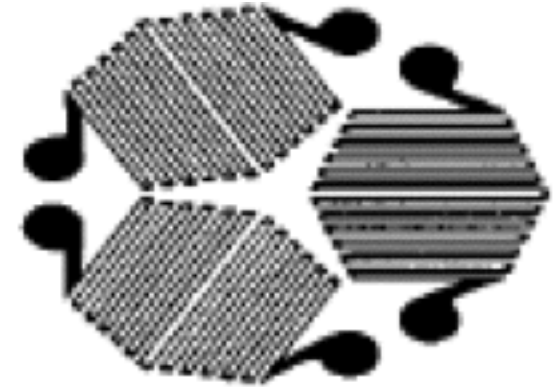
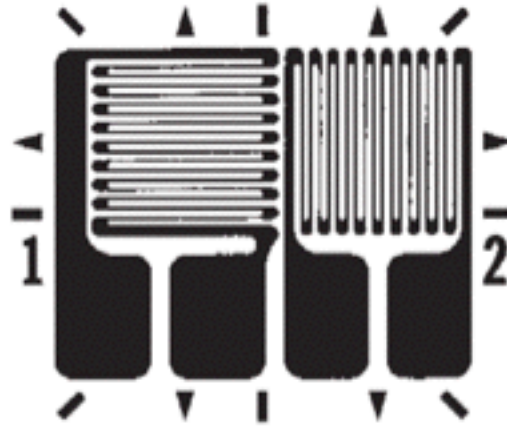
<u>Parameter</u>	Semiconductor	Metal
K	125	2÷4
C ₂	4000	~0
α_R	12 ppm/K	0.2 ppm/K
α_K	16 ppm/K	5 ppm/K

Bonded foil strain gauges



The epoxy resin both transmits the mechanical stress to the metal and provided the necessary electrical insulation

Other shapes of strain gauges to measure in multiple directions

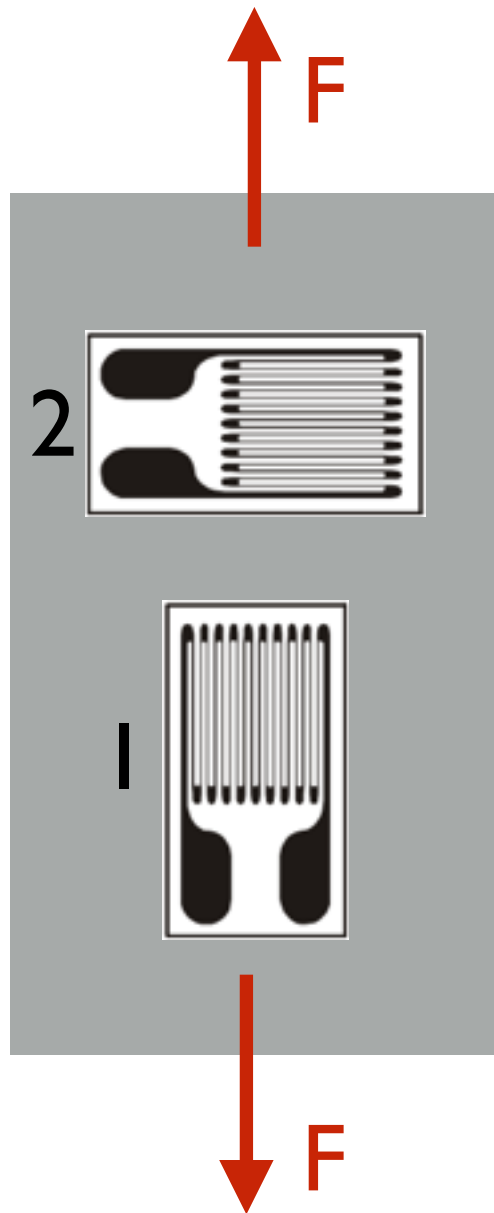


Vishay, Omega Engineering, Hottinger-Baldwin

Problem: what if the temperature changes?

We must compensate ΔR due to temperature.

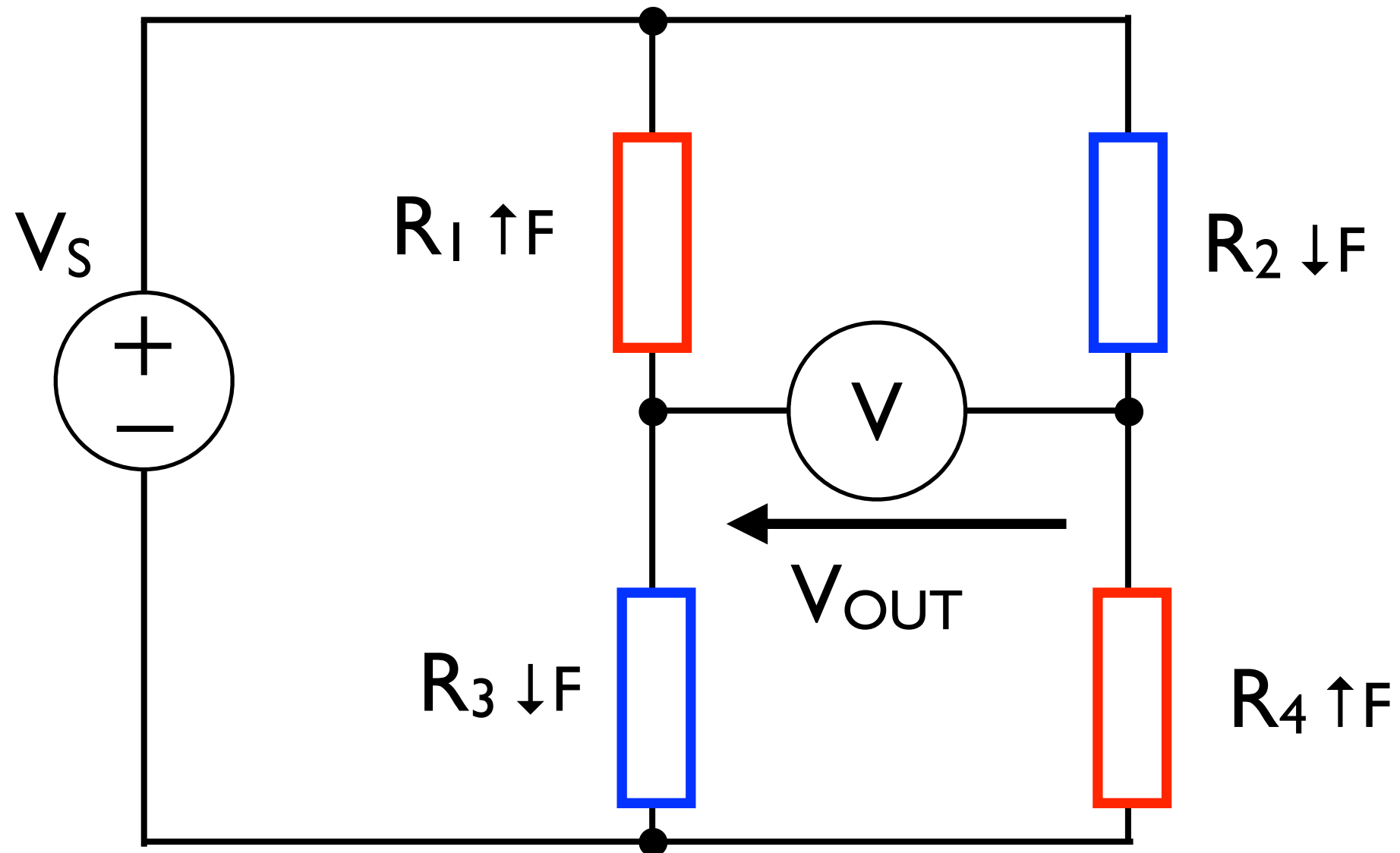
Basic principle: use two “identical” sensors, only one of which measures the force.



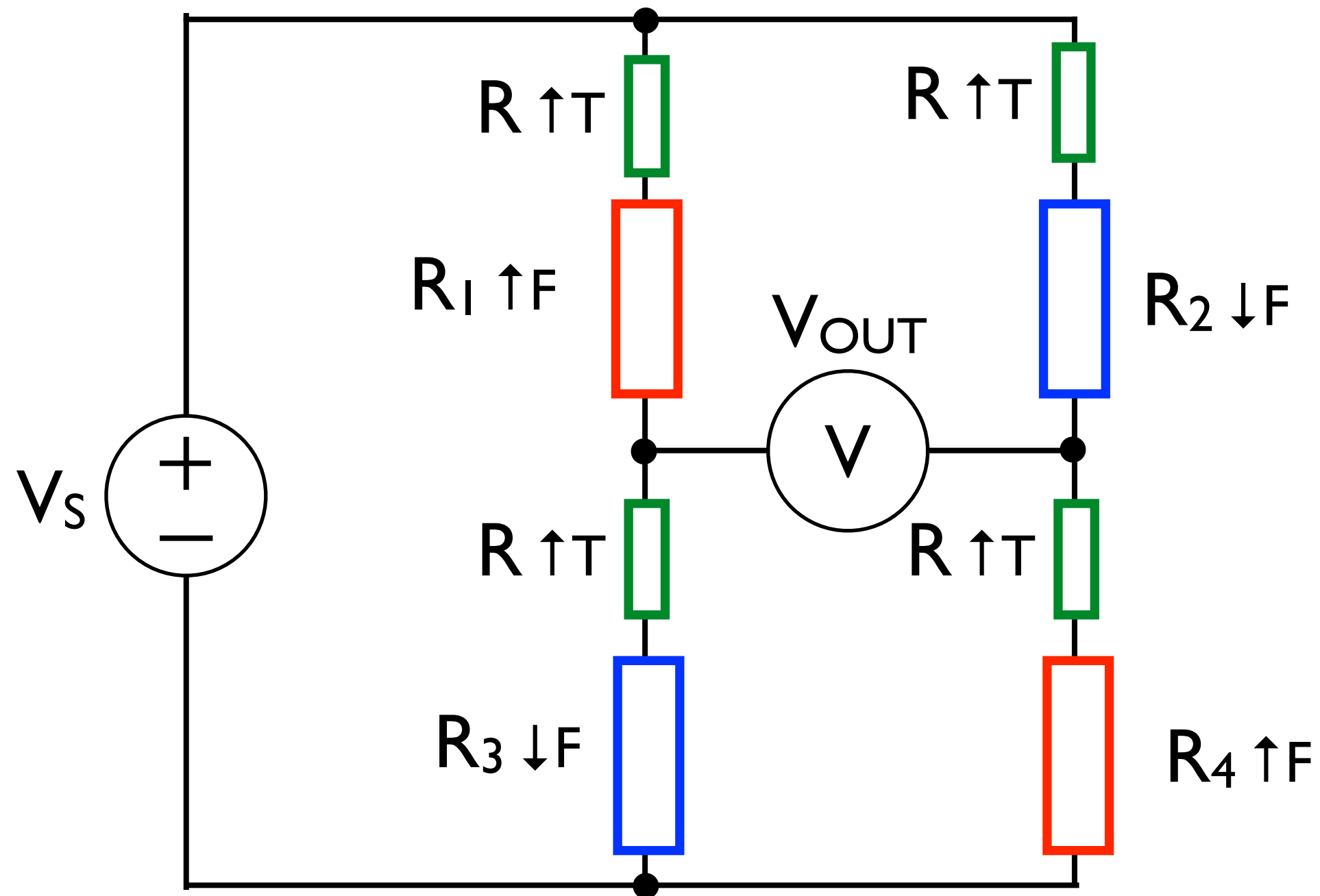
R_2 depends only on temperature

R_1 depends on F and temperature

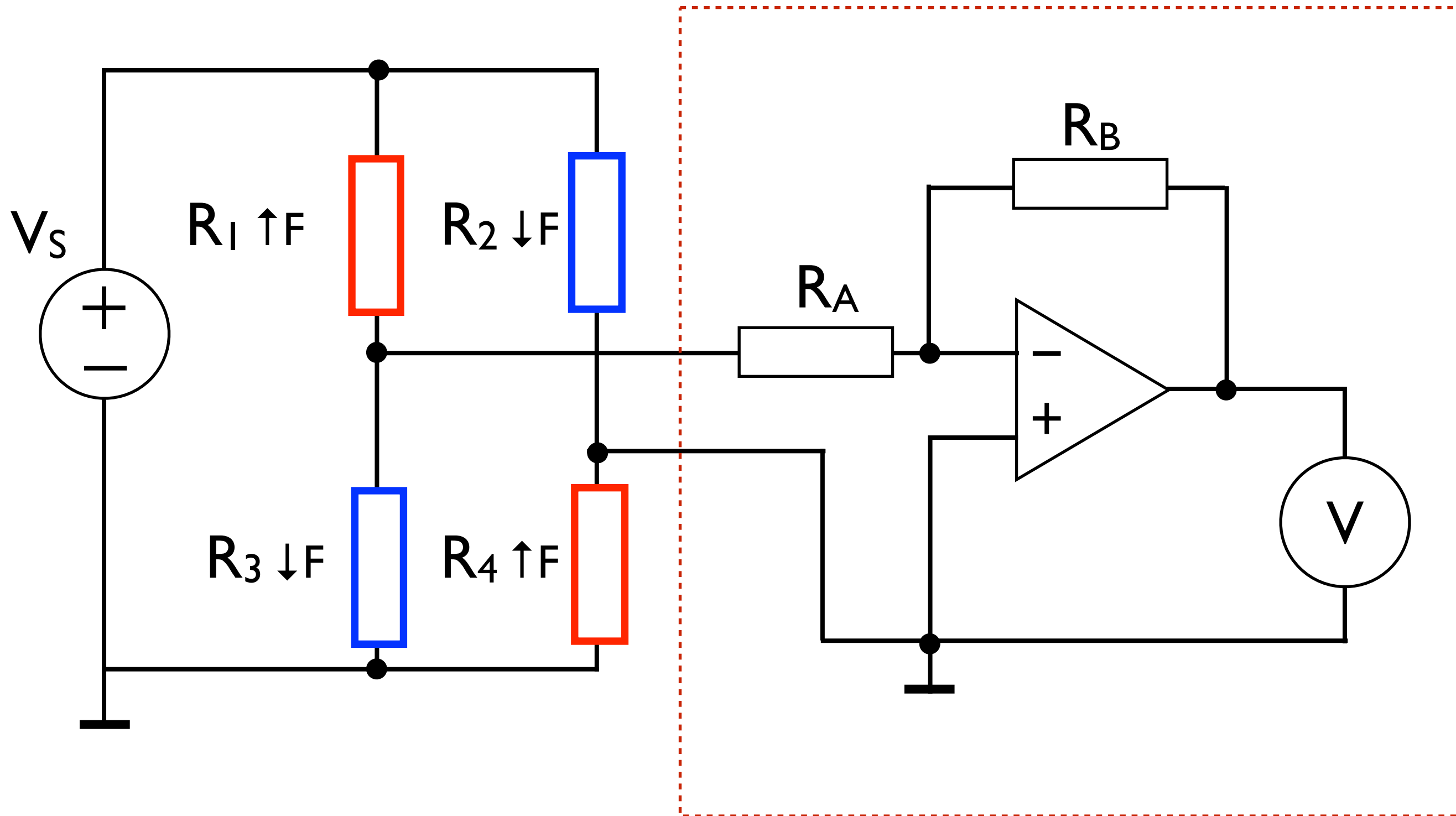
Other solution: use a full bridge and identical sensors



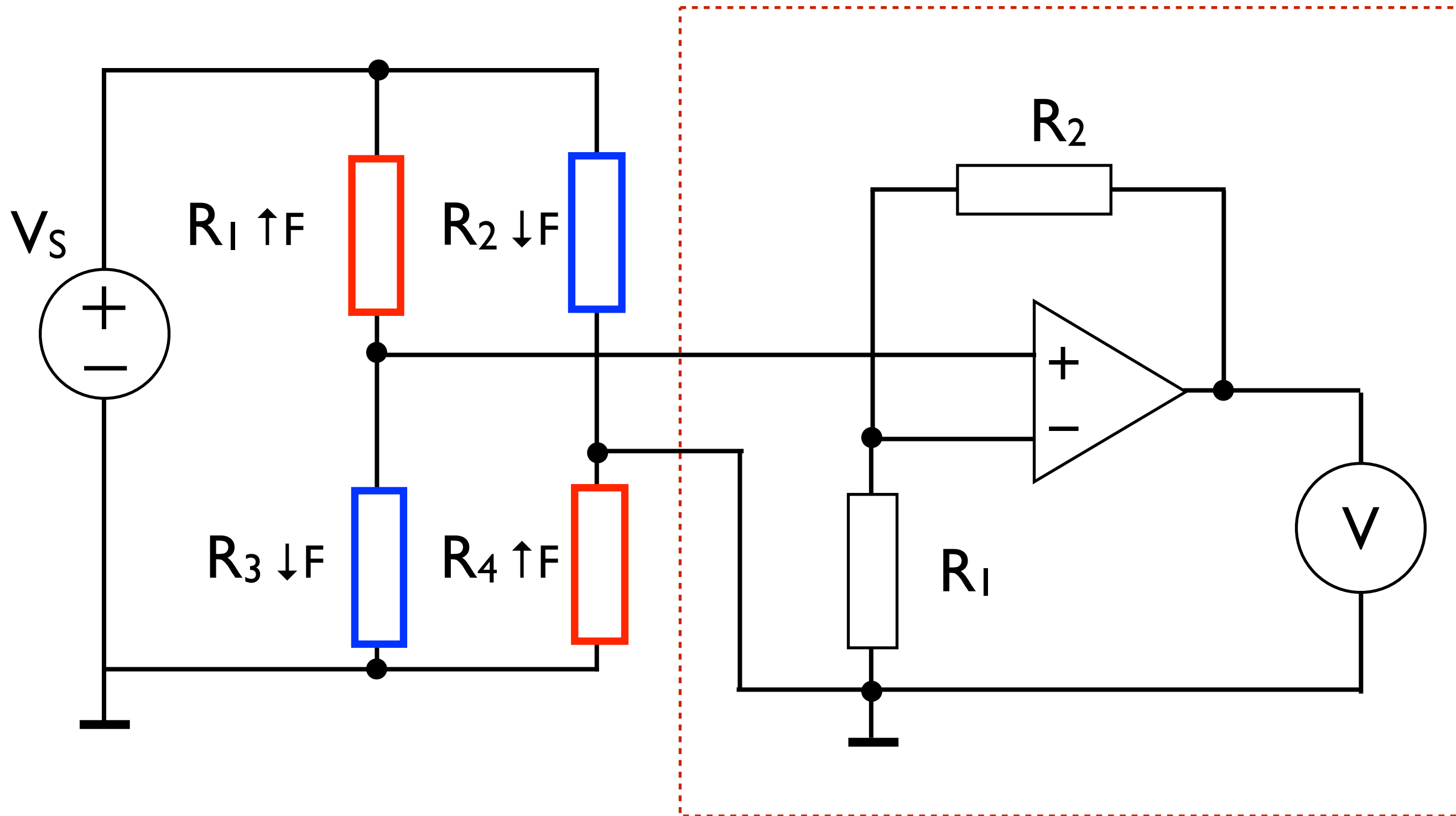
Other solution: use a full bridge and identical sensors



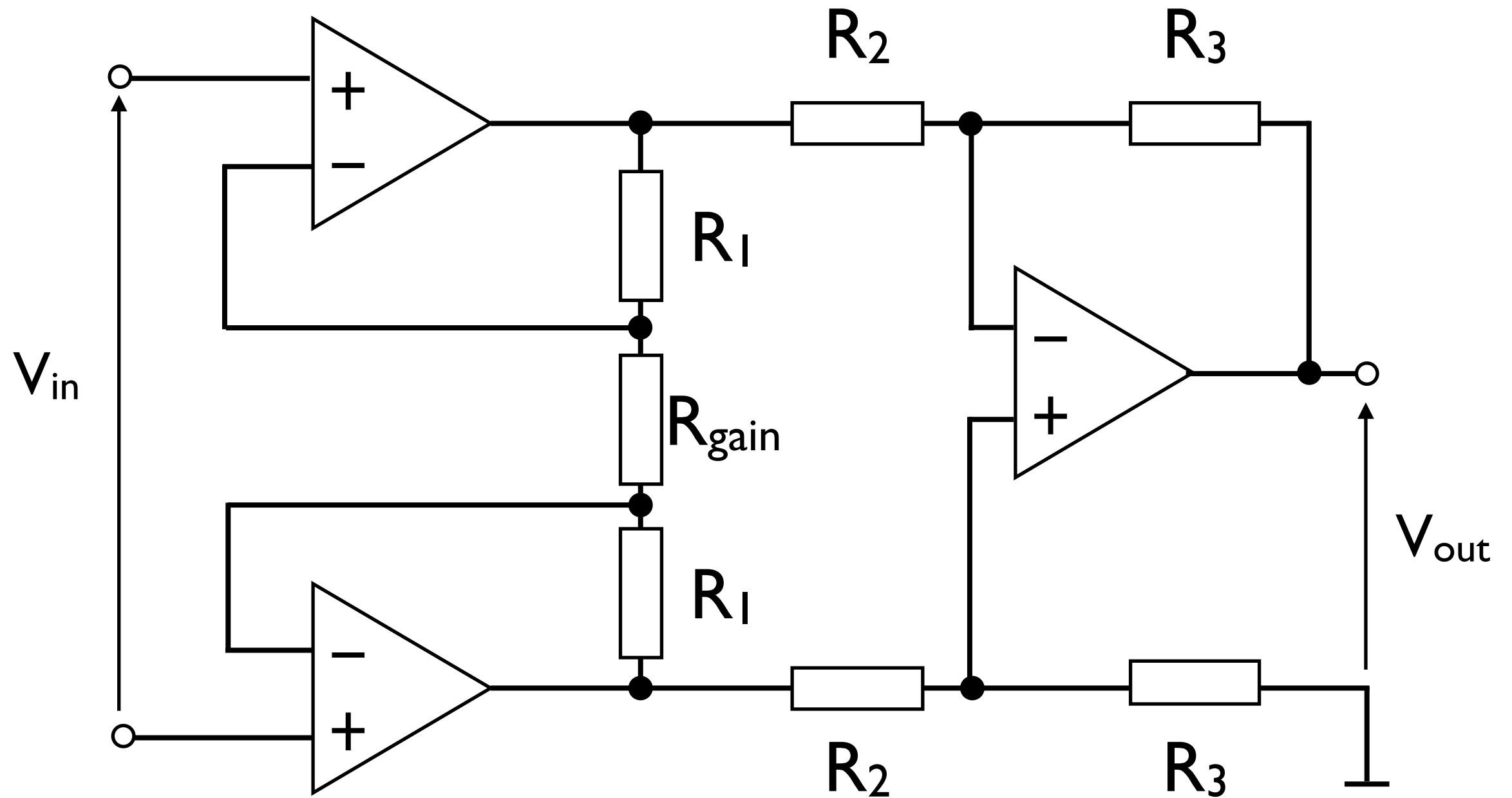
How to amplify the voltage output?



How to amplify the voltage output?

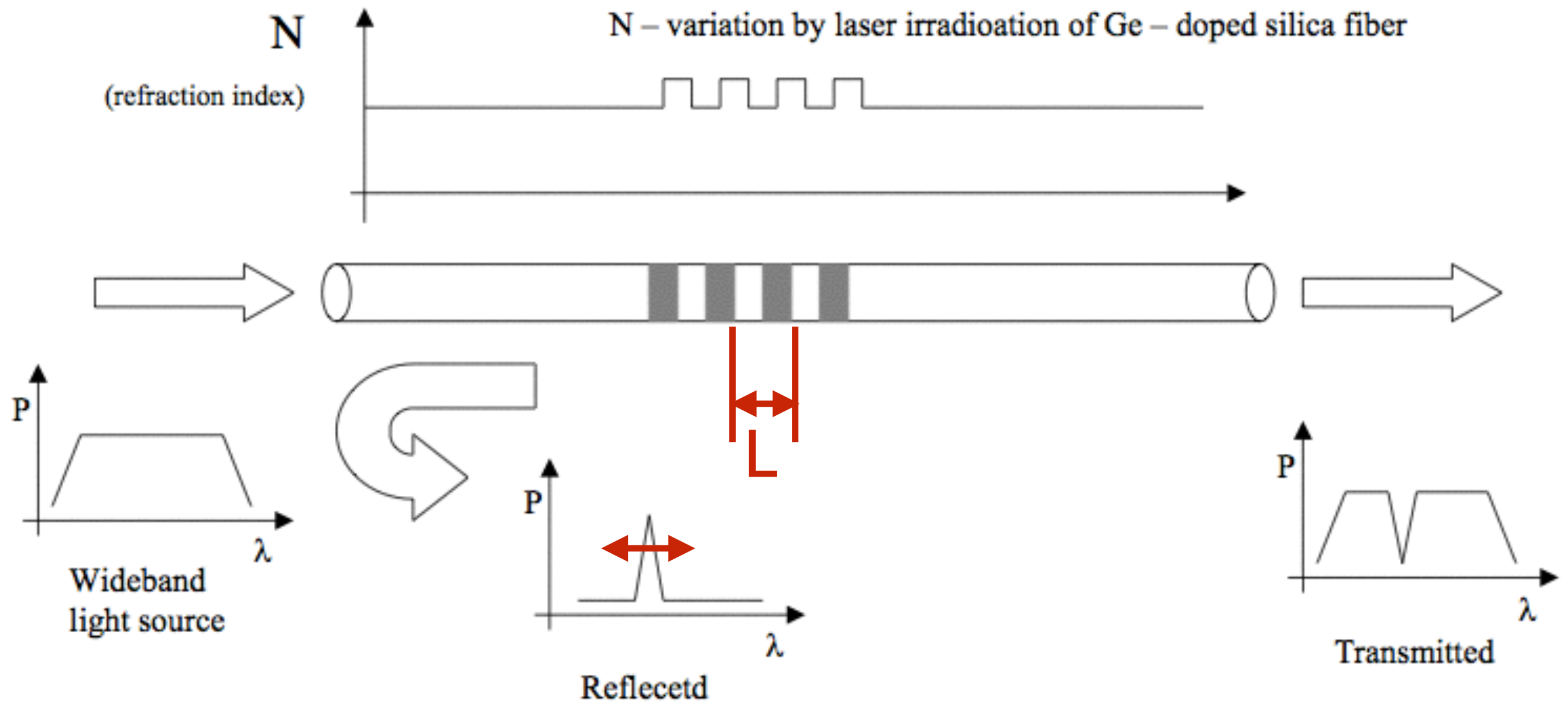


Solution: instrumentation amplifier

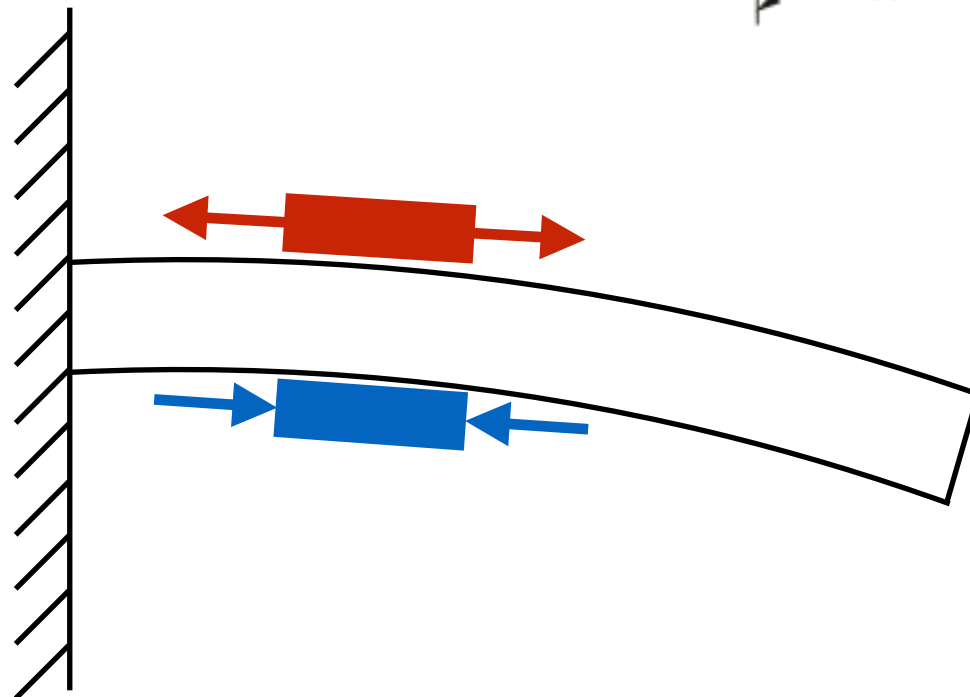
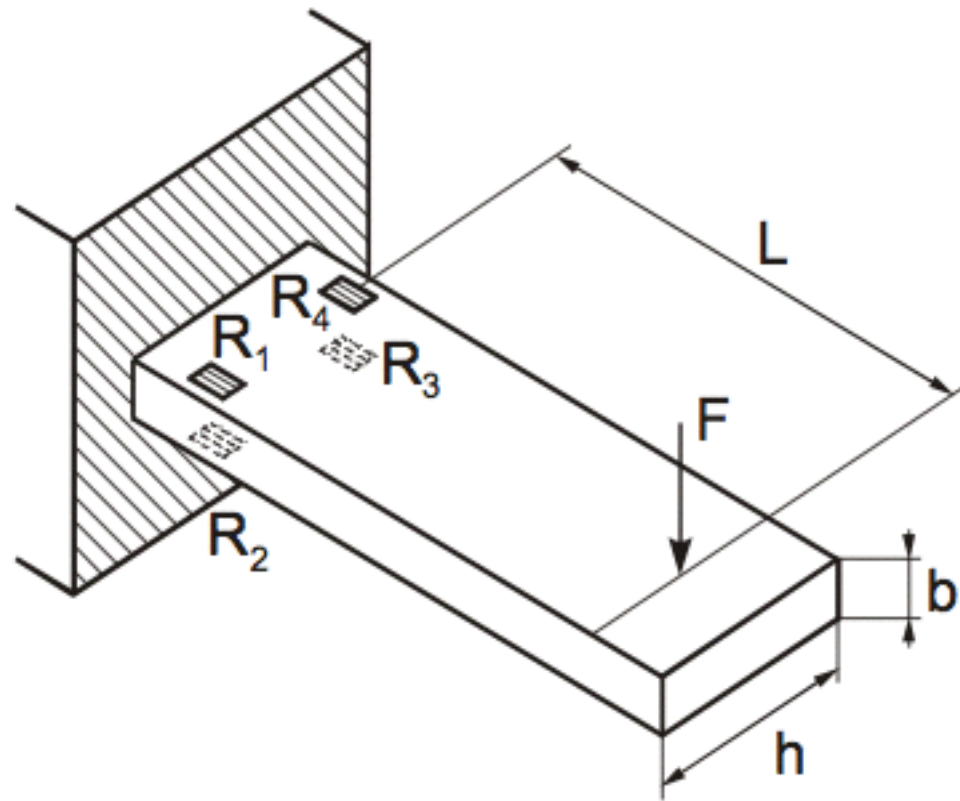


$$V_{out} = \left(\frac{2R_1}{R_g} + 1 \right) \frac{R_3}{R_2} (-V_{in})$$

Fiber Bragg Grating sensors



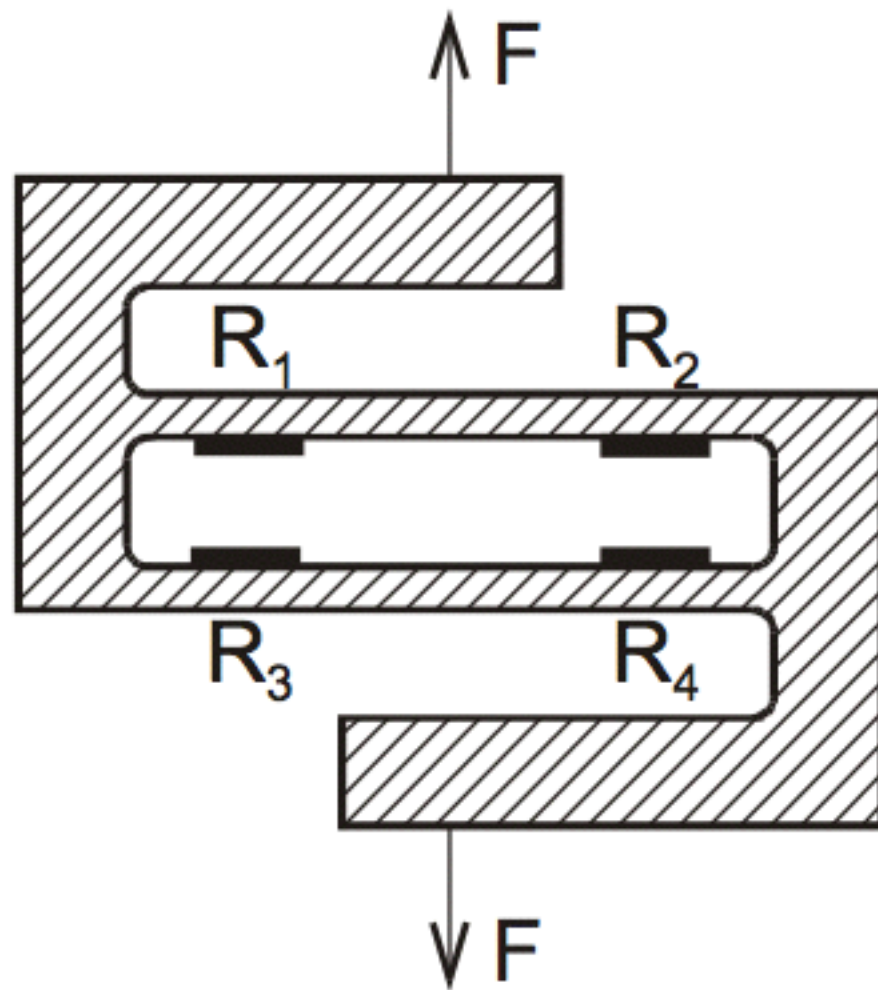
How to measure force



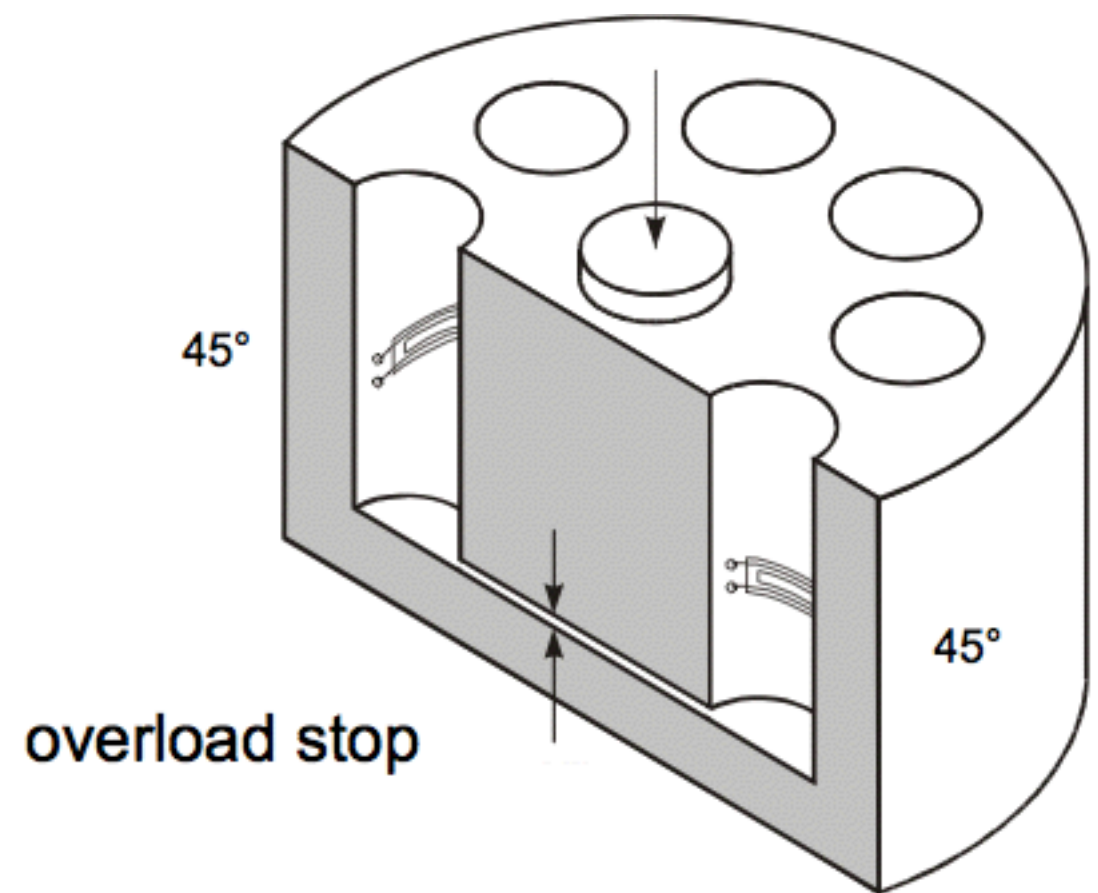
for small forces (up to some kN)

How to measure a large force

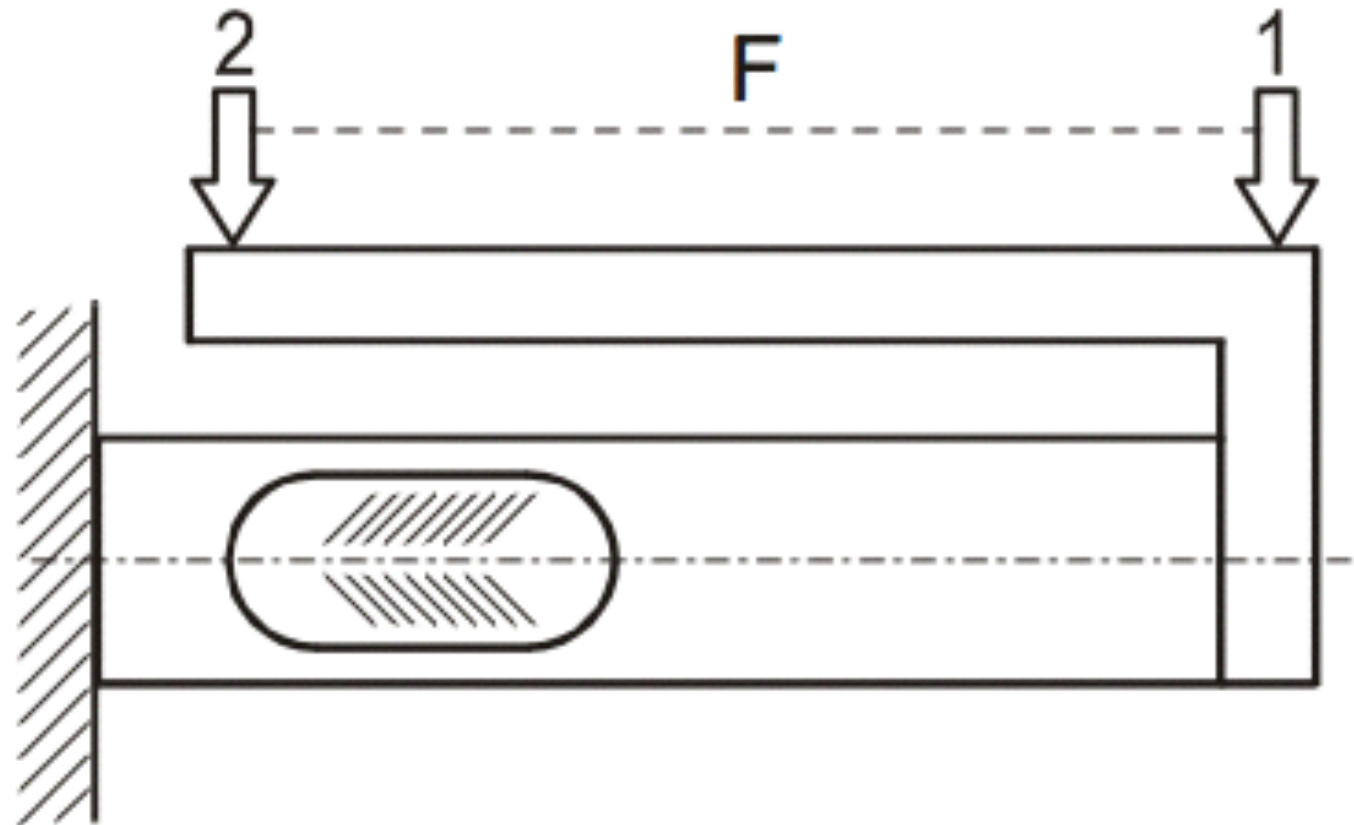
S-type load cell



Shear-web force transducer

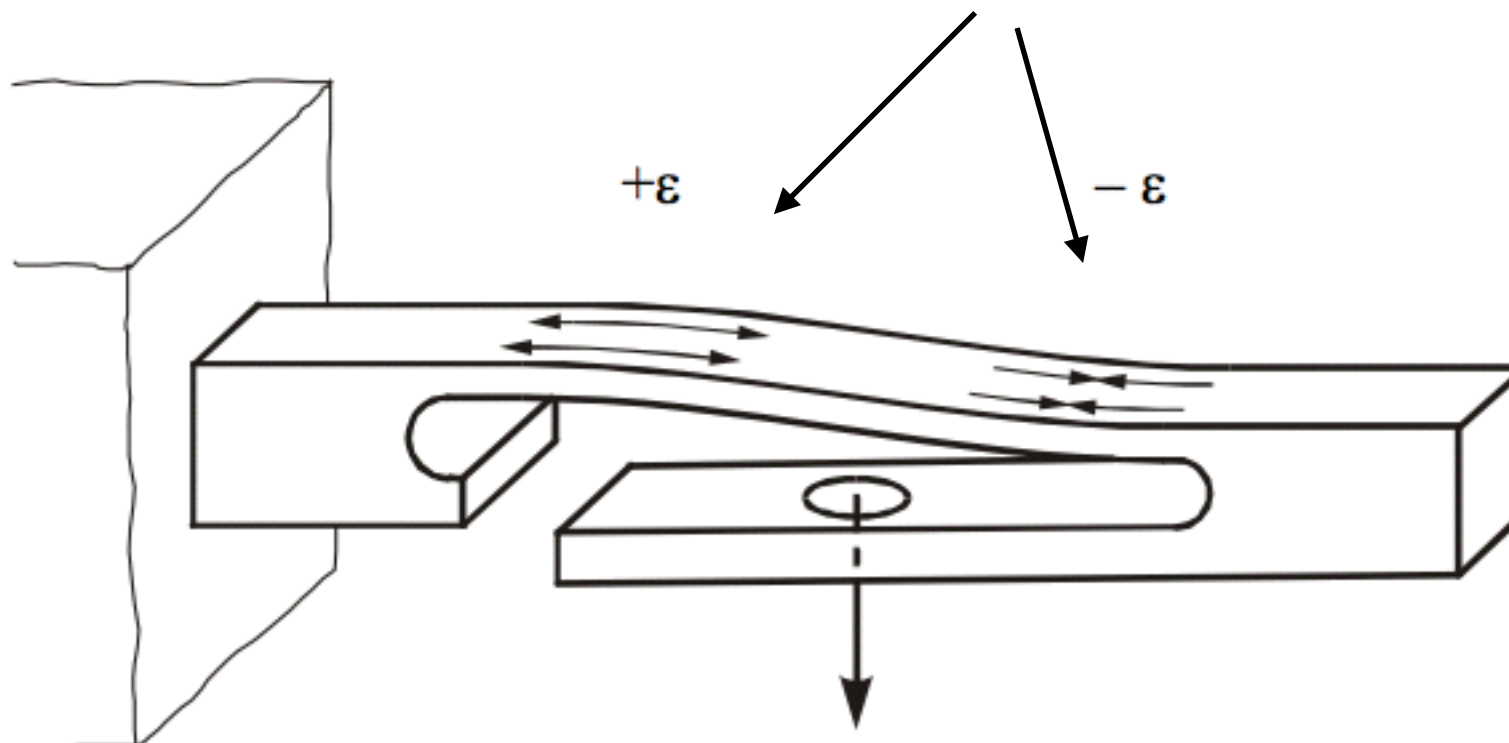


How to measure shear

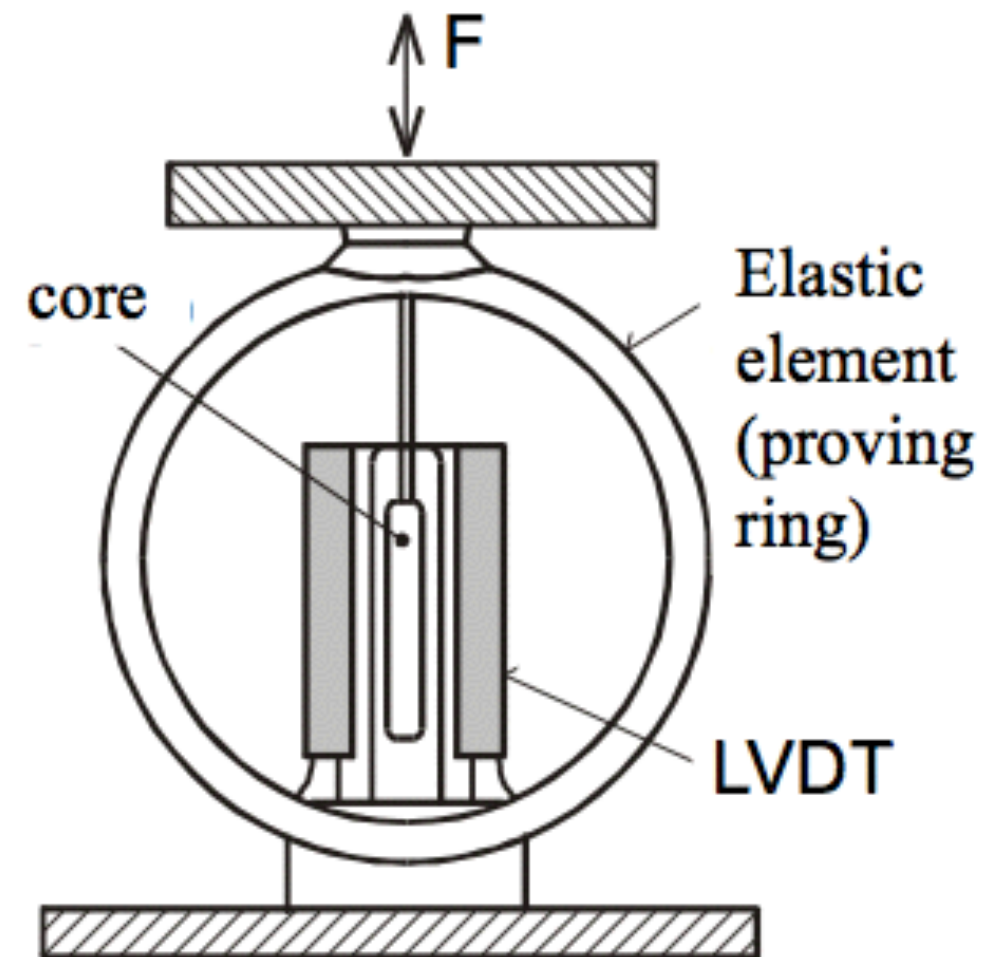
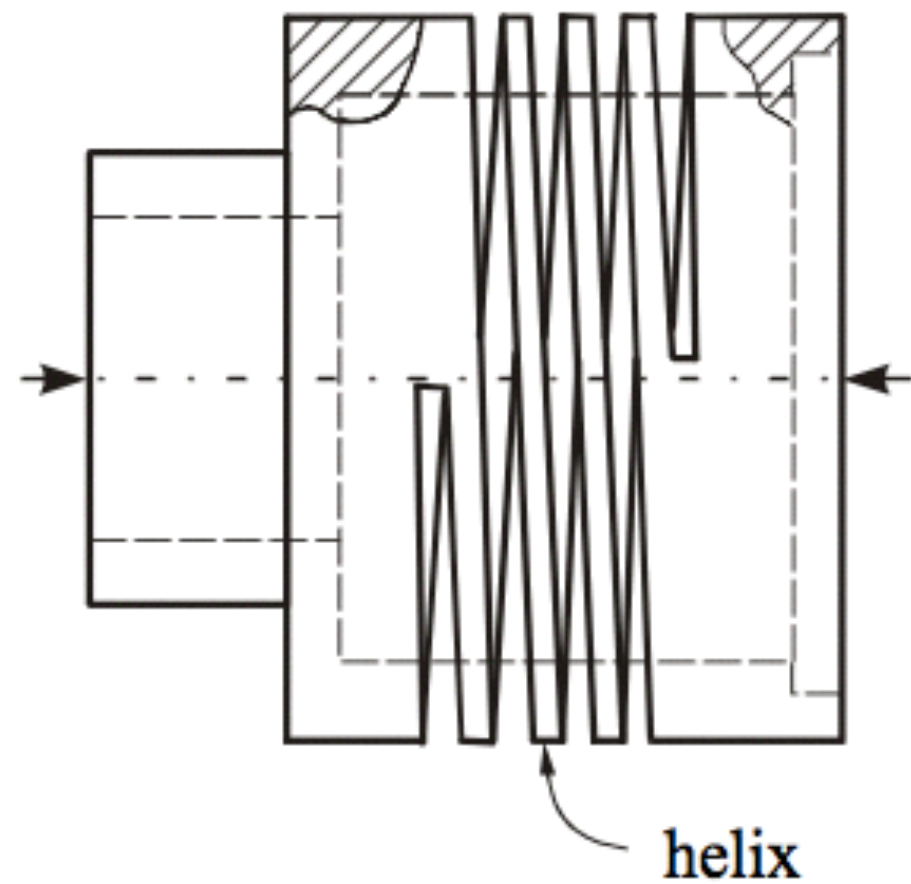


Folded cantilever

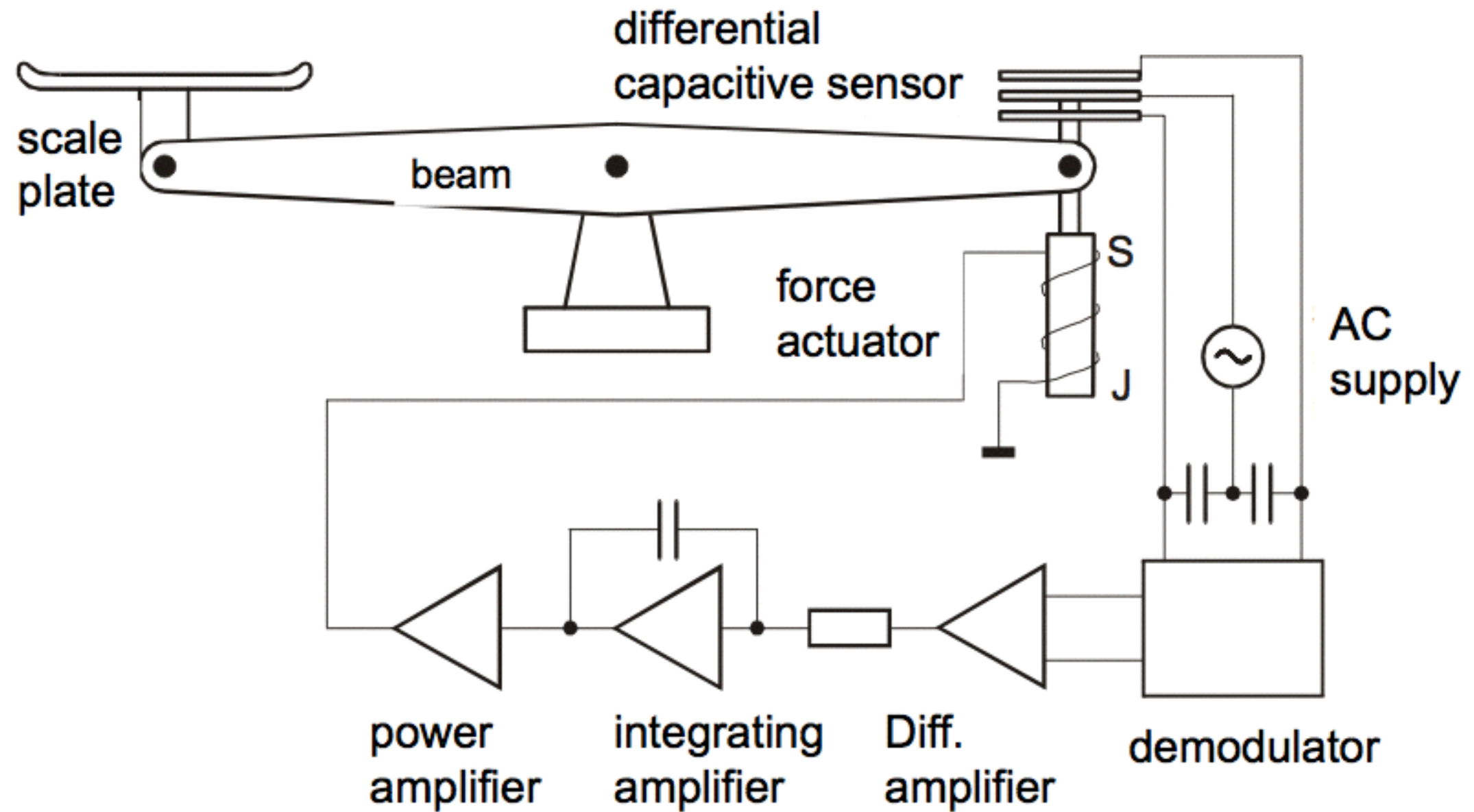
extension and compression are the same



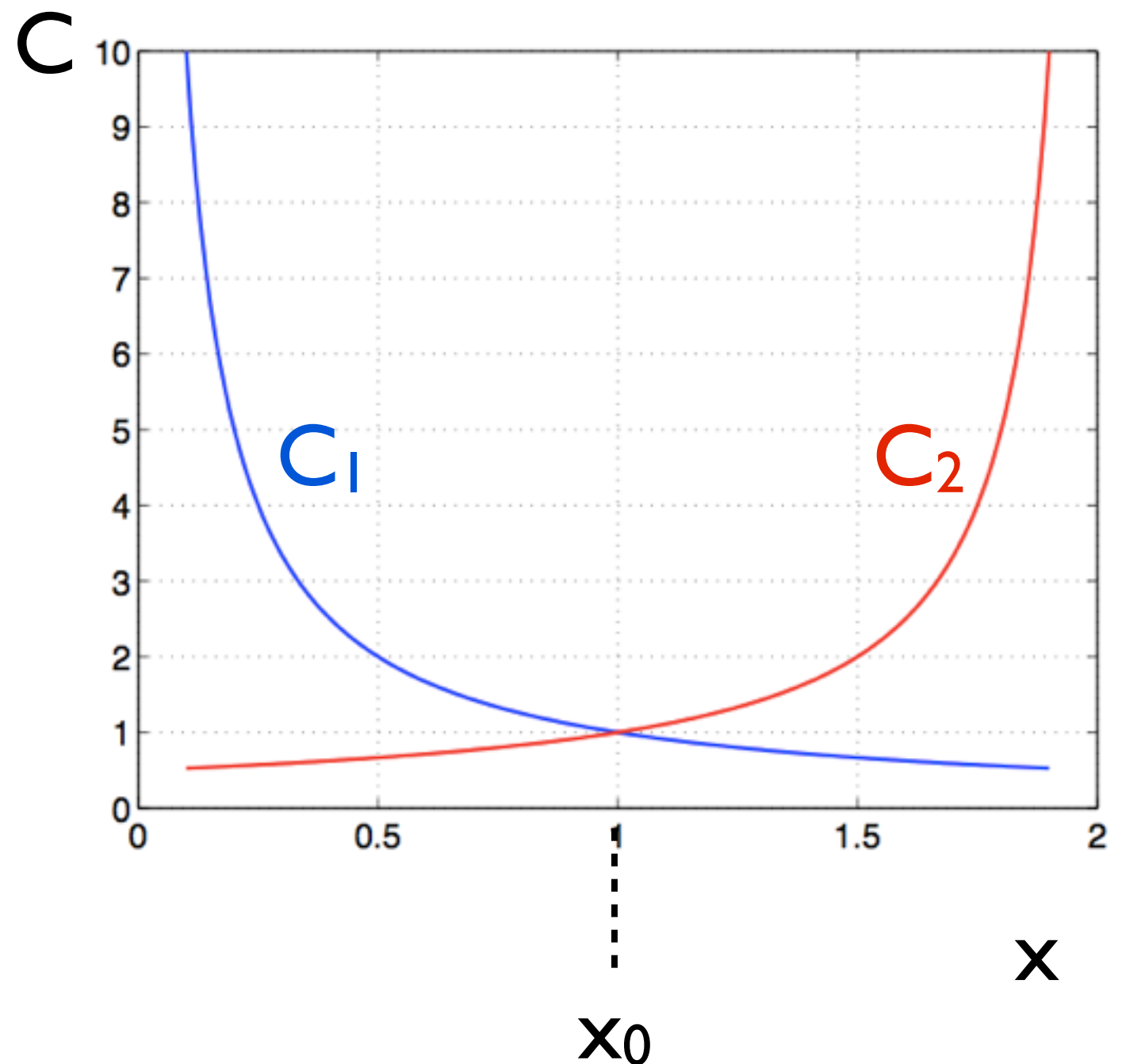
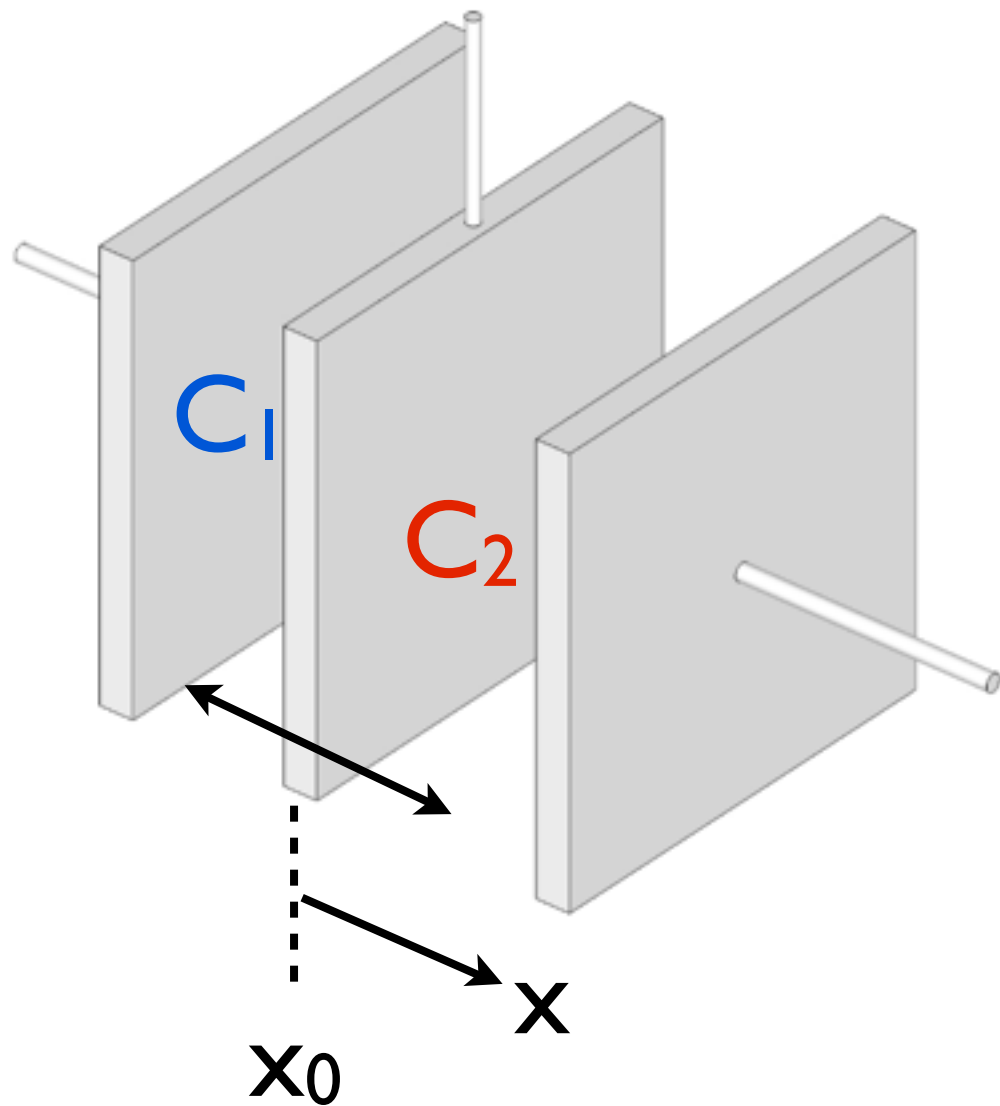
Sensors of force based on displacement



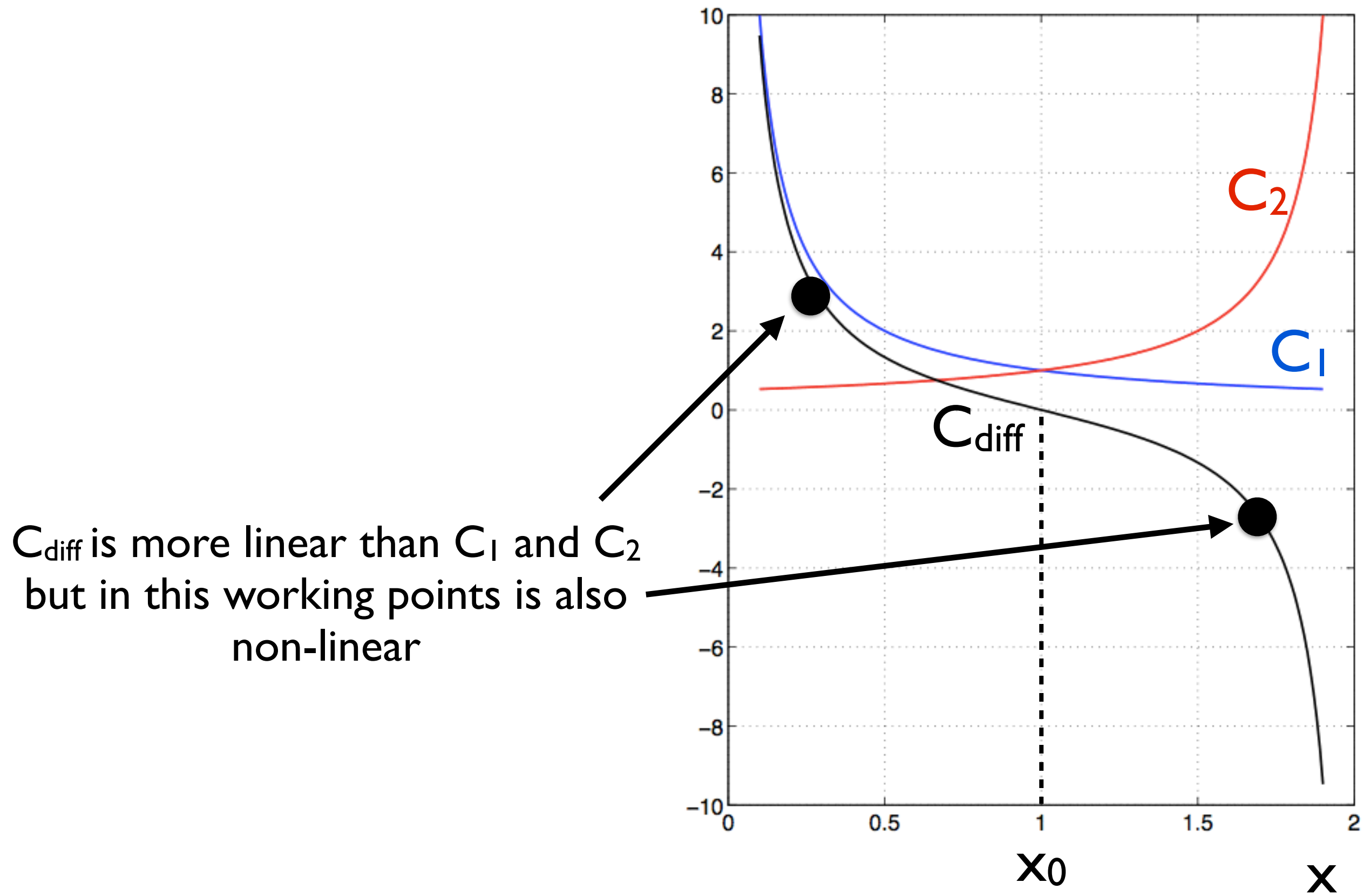
Sensors with electromechanical feedback



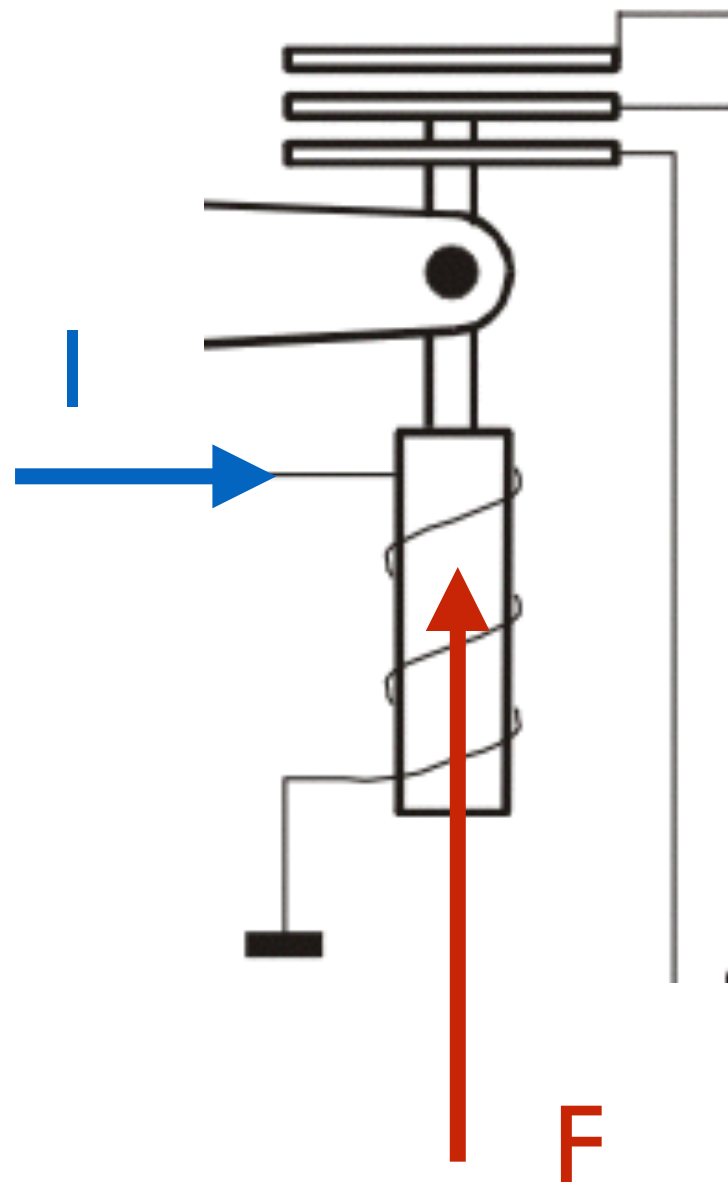
Why should we use feedback?
Can't we simply read the difference of capacity?



Why should we use feedback?
Can't we simply read the difference of capacity?



How feedback works

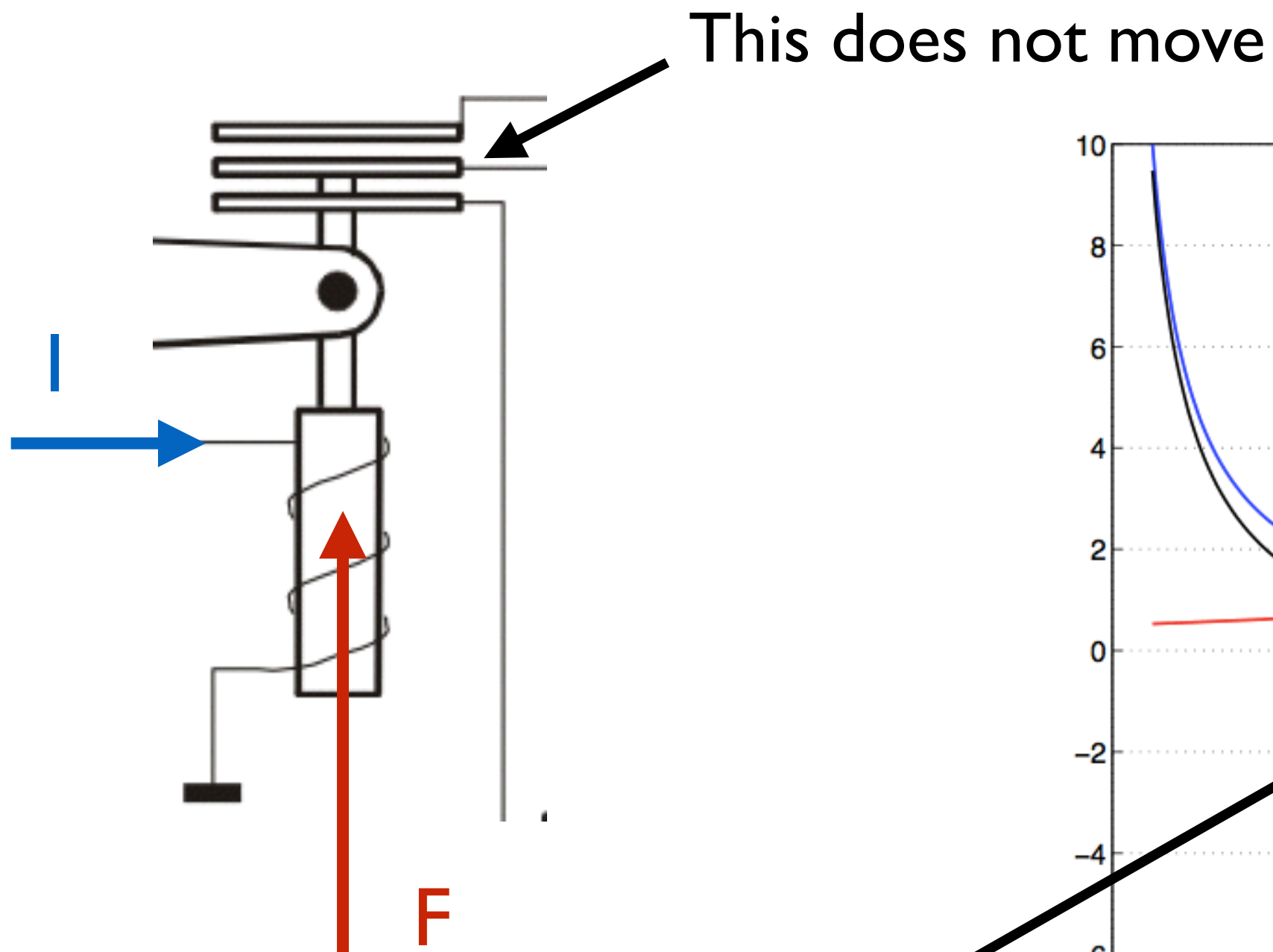


The current I in the solenoid
creates a force F

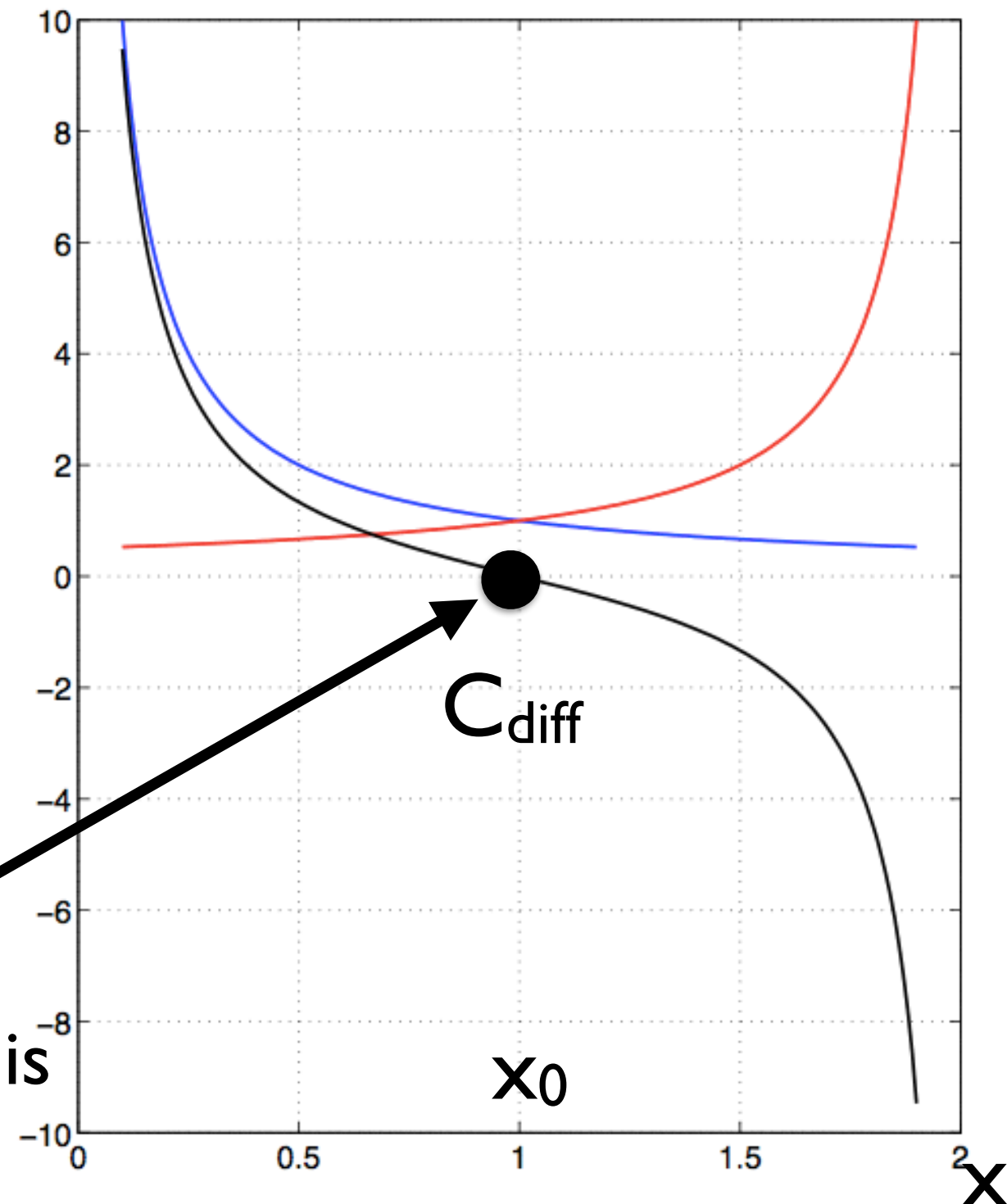
$$F = kI$$

so that the differential capacitor is
always in the central position

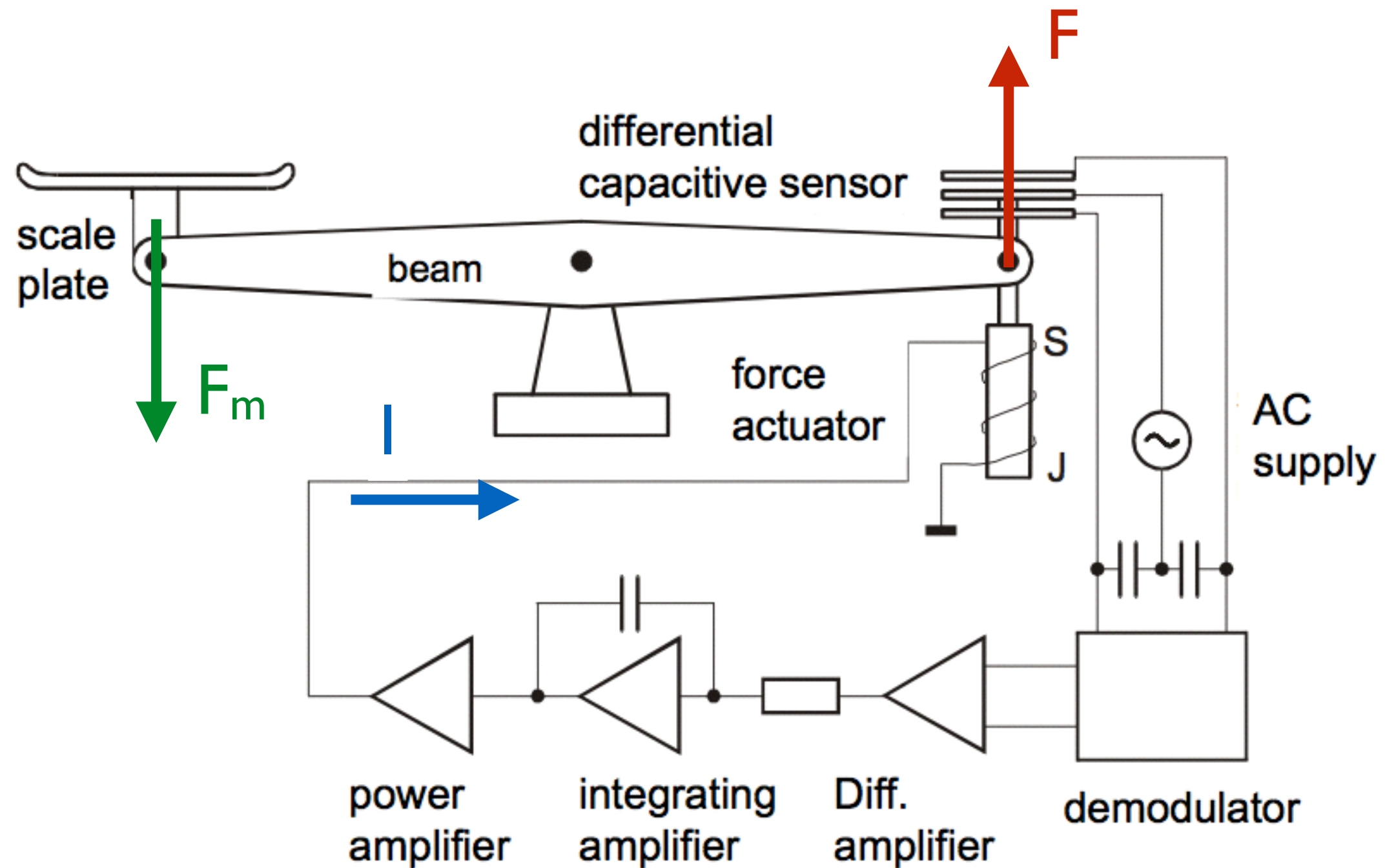
How feedback works



The working point of the capacitor is
always in zero



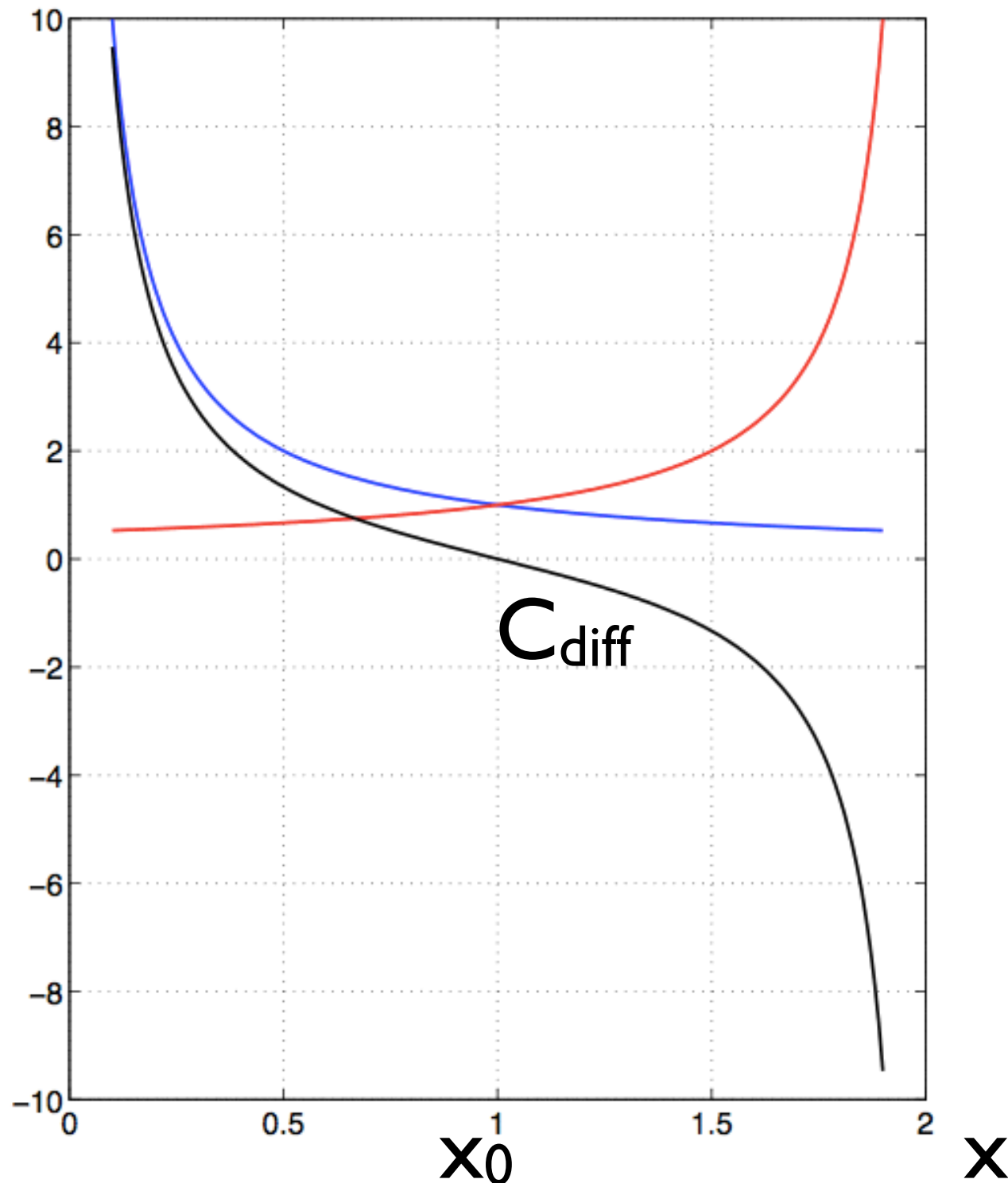
The output signal is not capacity anymore.
The output signal is the current used to produce the balancing force.



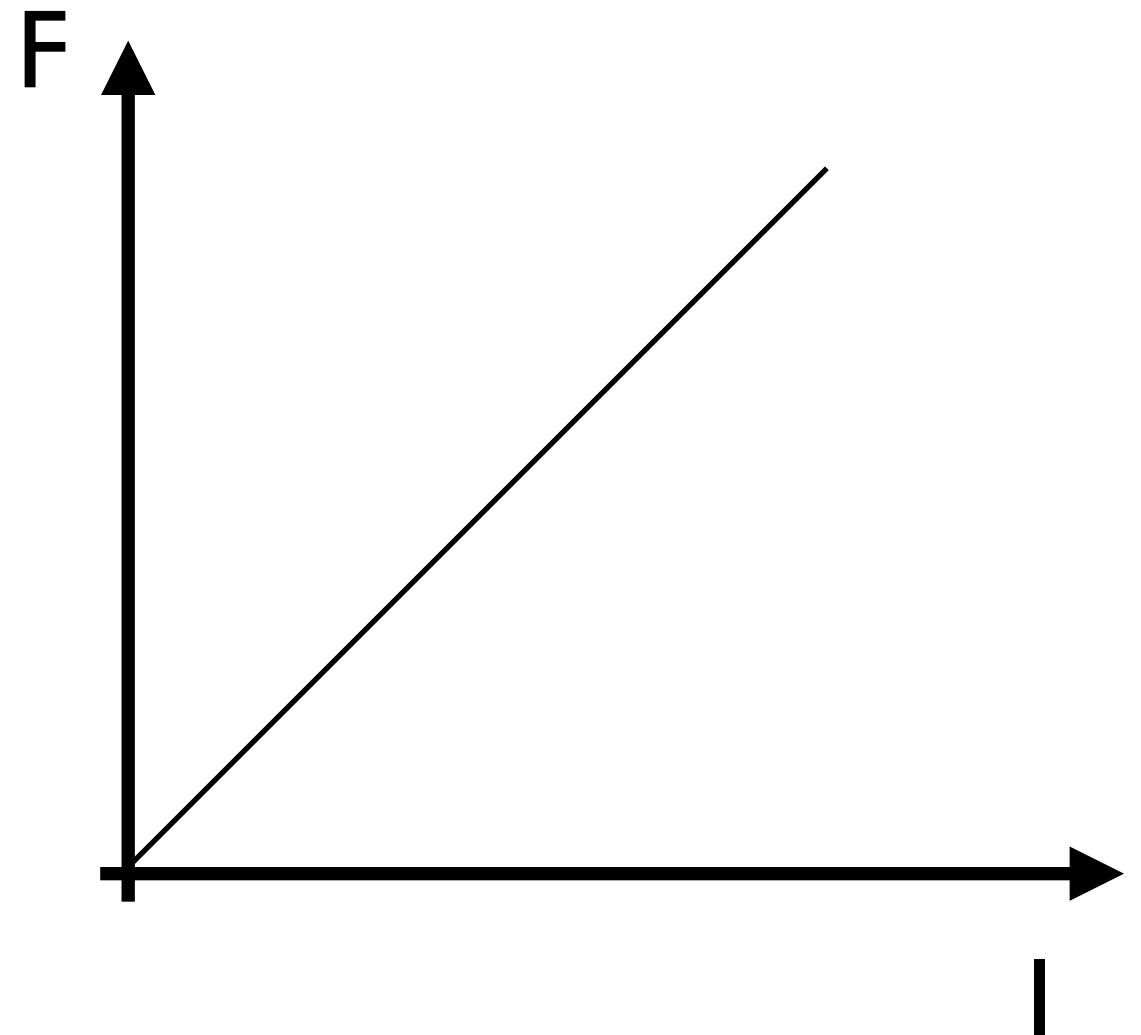
If $C_{diff} = 0$ then
 $F_m = F = kl$

So, finally
 $F_m = kl$

If I measure the capacity I get a non-linear dependence of the output quantity C_{diff} on displacement (and then force F_m)



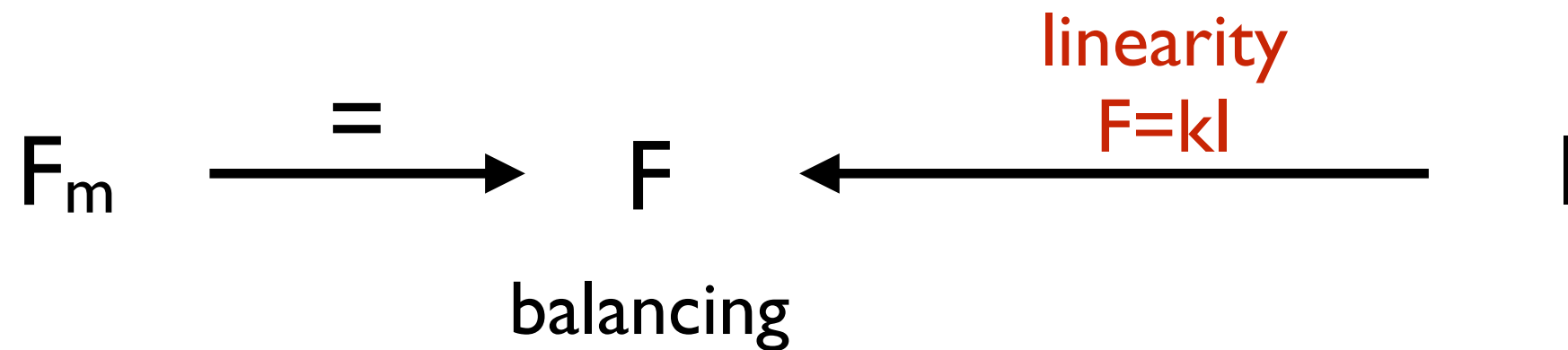
If I measure the current I , I obtain a linear dependence of the output current on the measured force F_m)



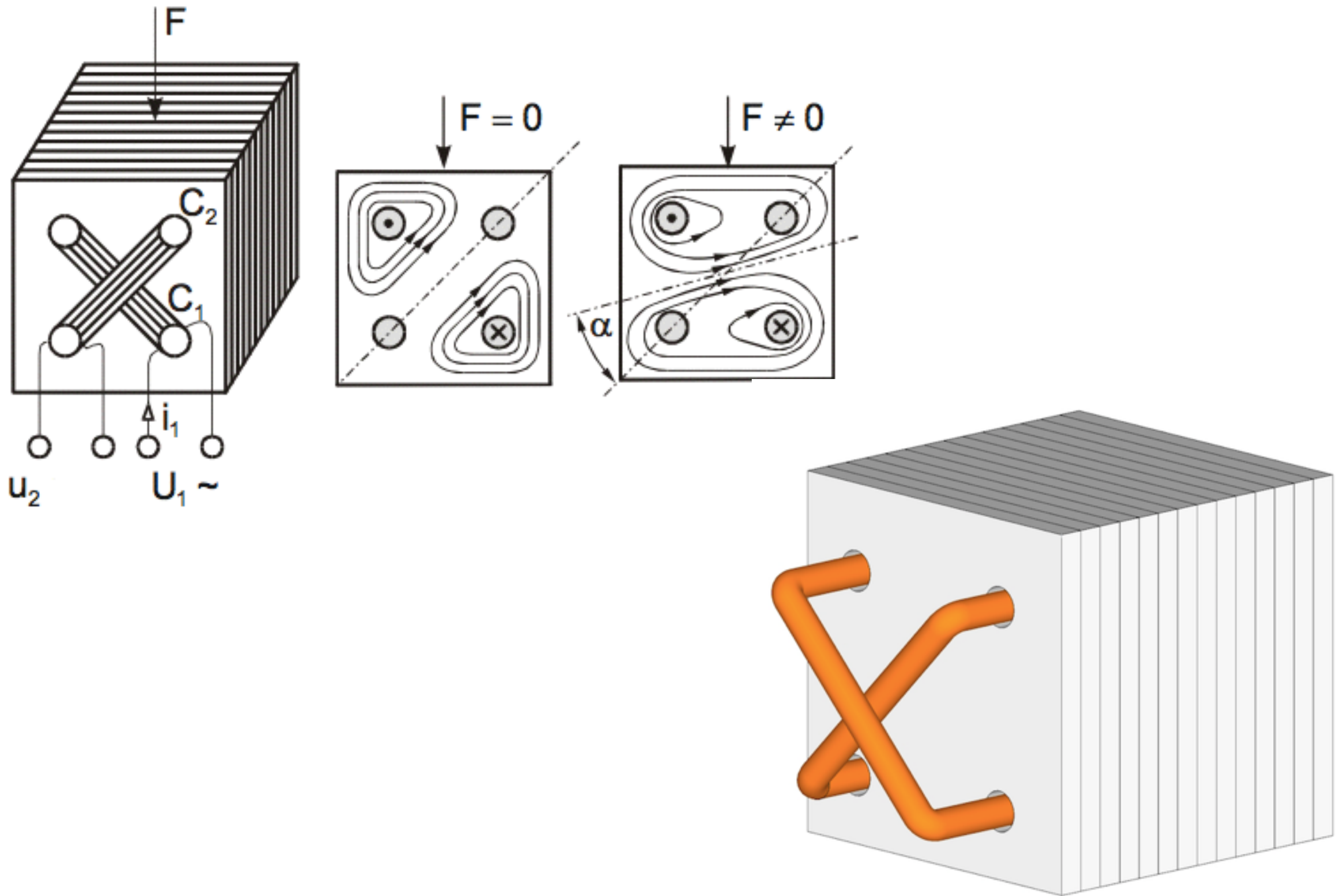
No feedback:



With feedback:

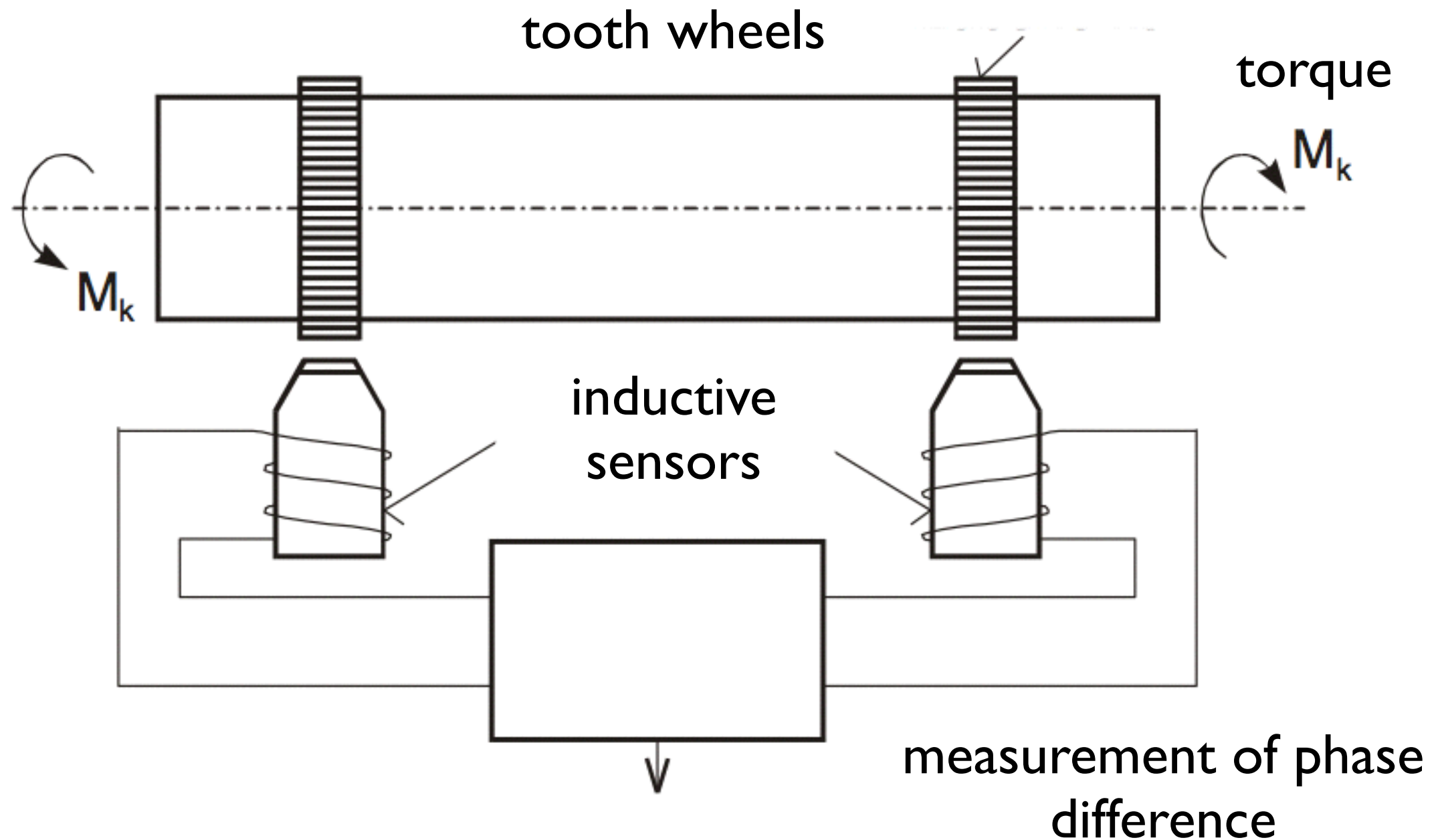


Magnetoanisotropic sensor of force



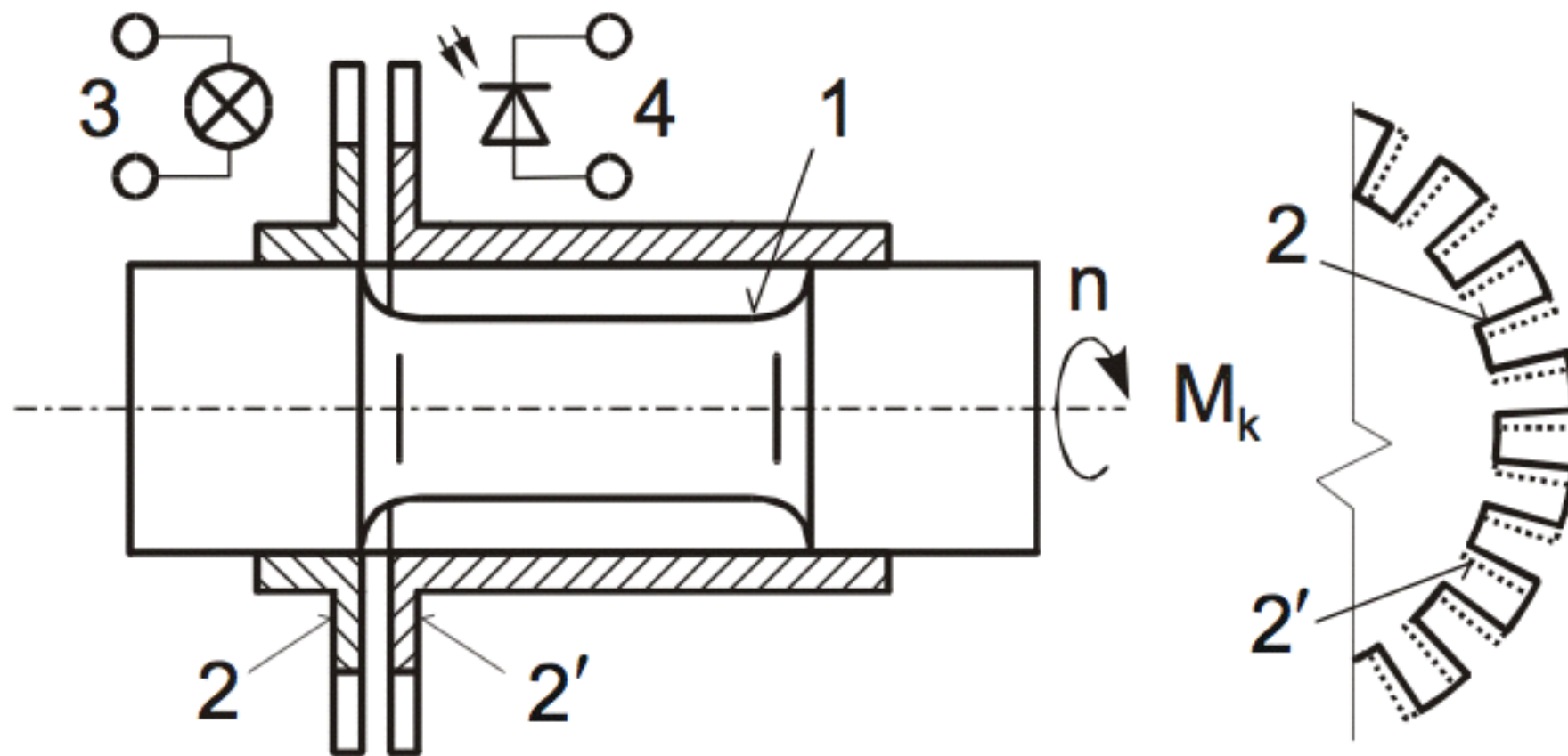
Measurement of torque

sensor of torque based on angular displacement:

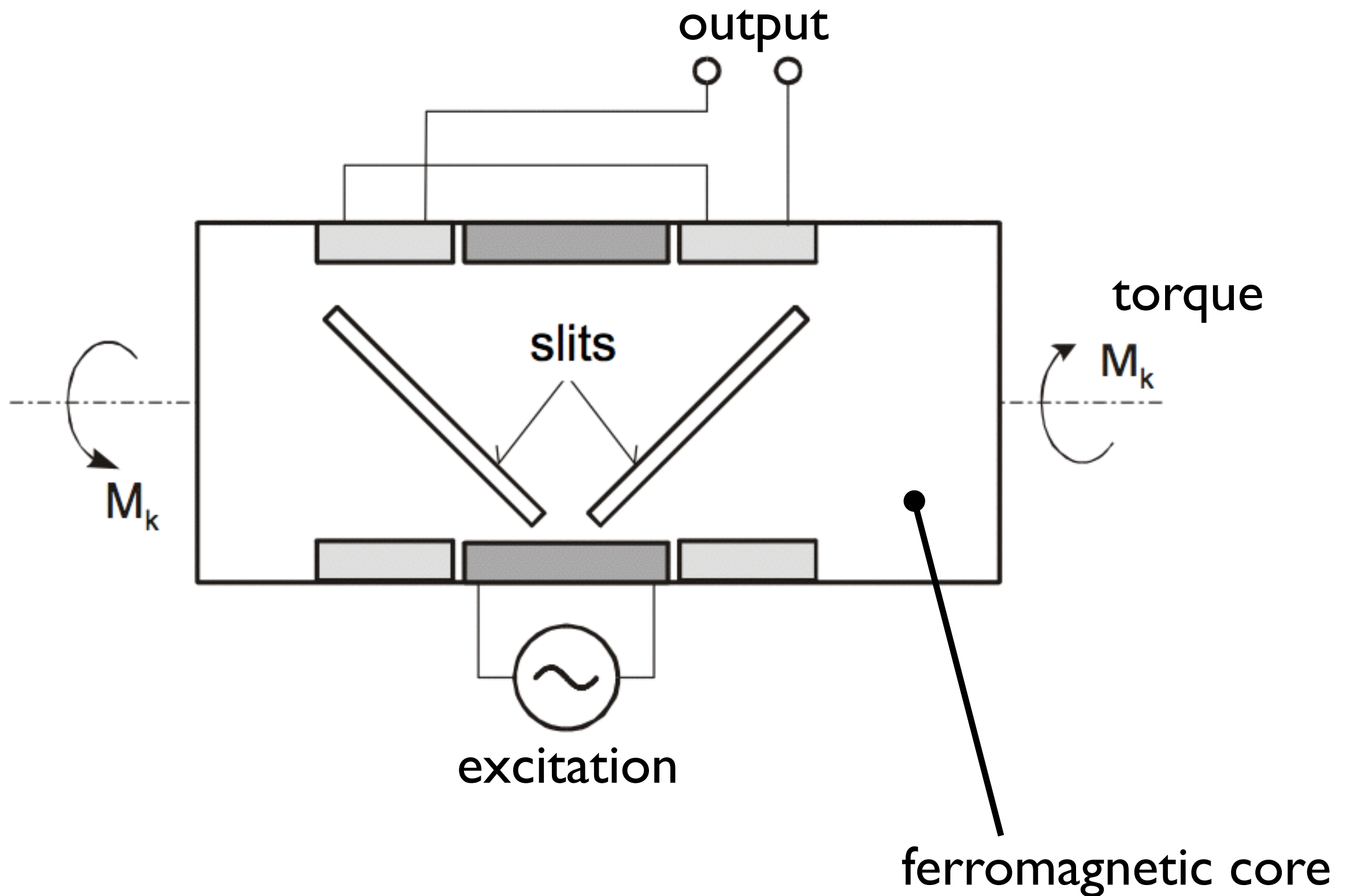


Measurement of torque

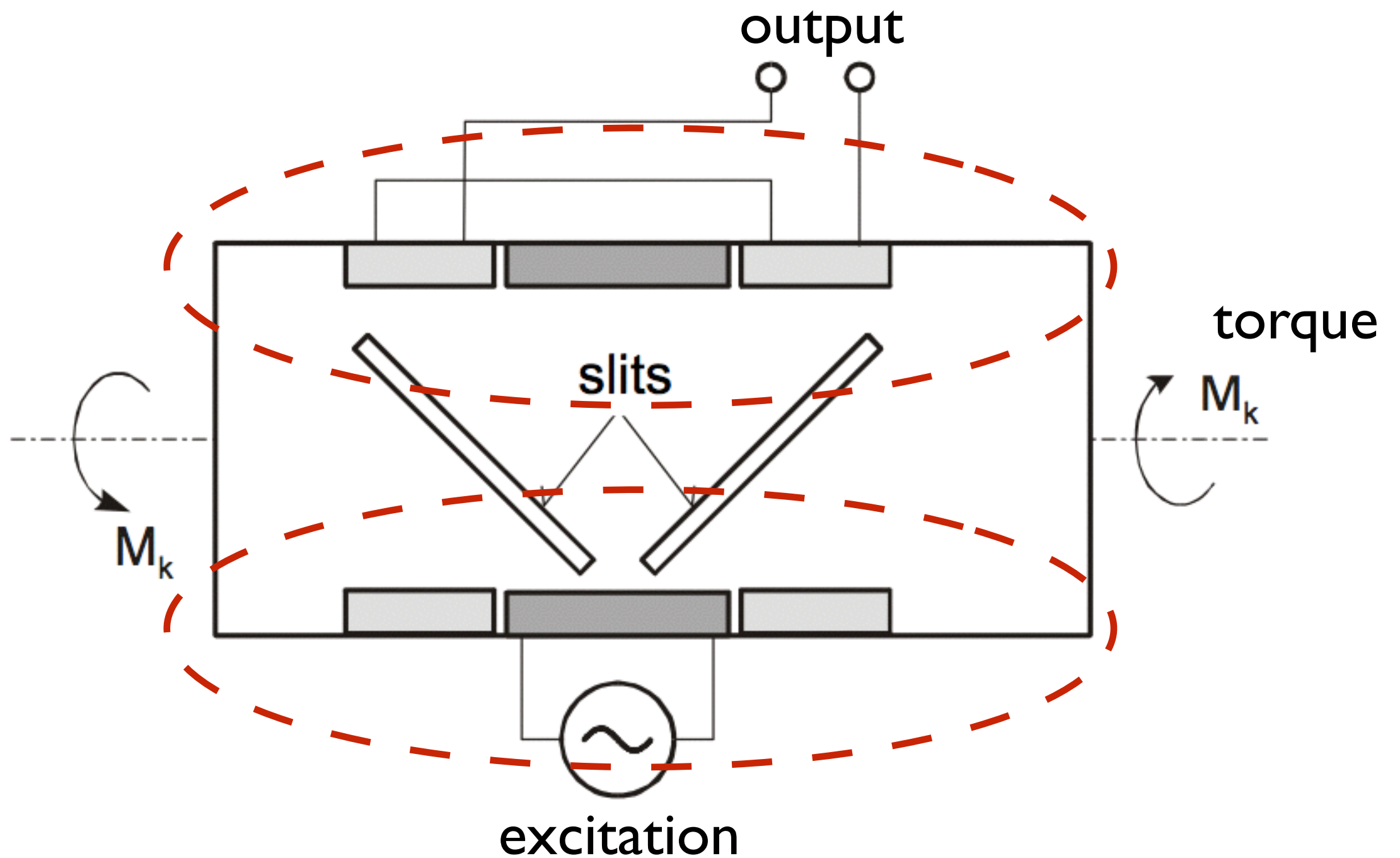
optoelectronic sensor based on overlapping of shades 2-2'



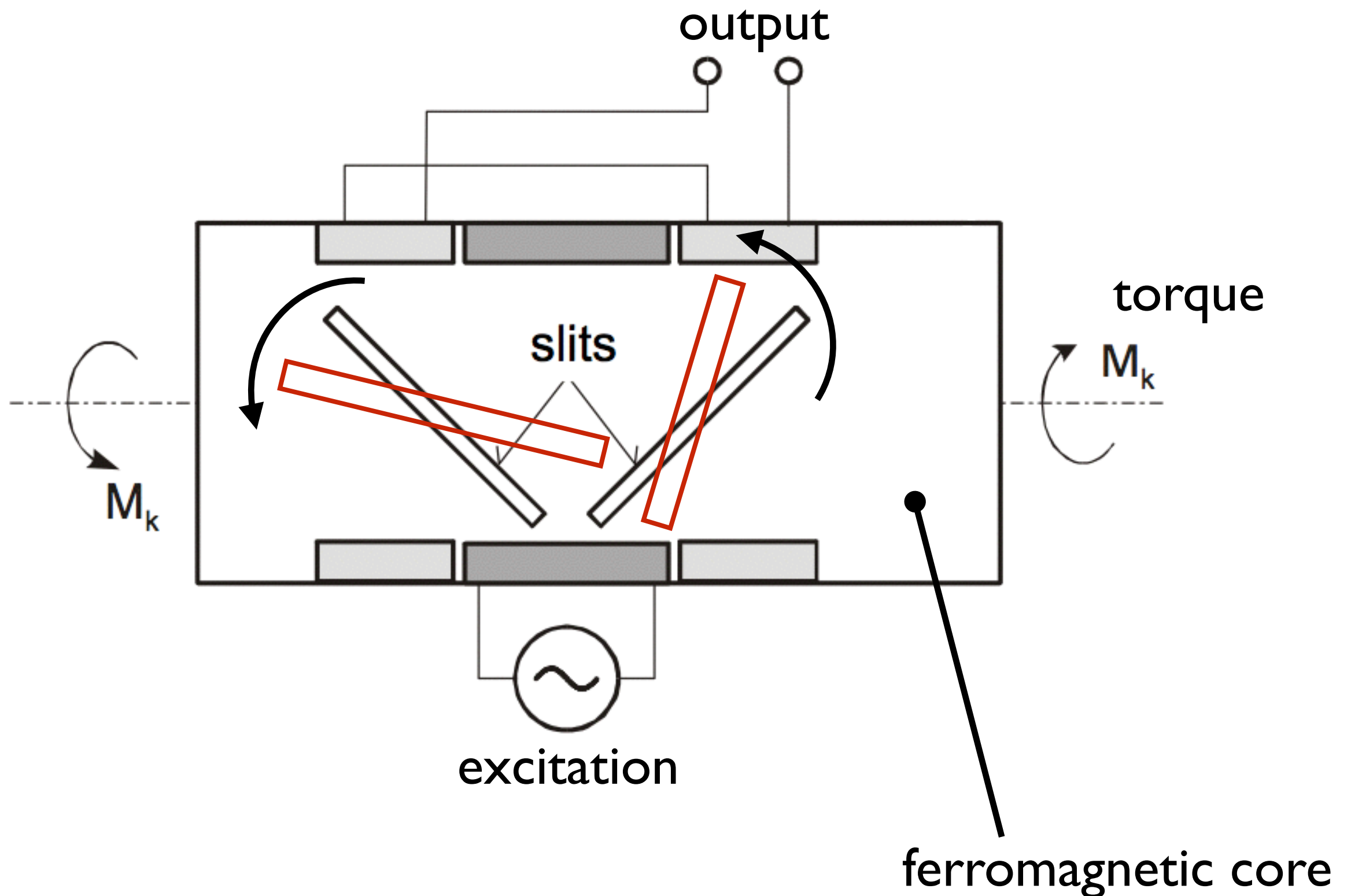
Magnetic (variable reluctance) sensors of torque



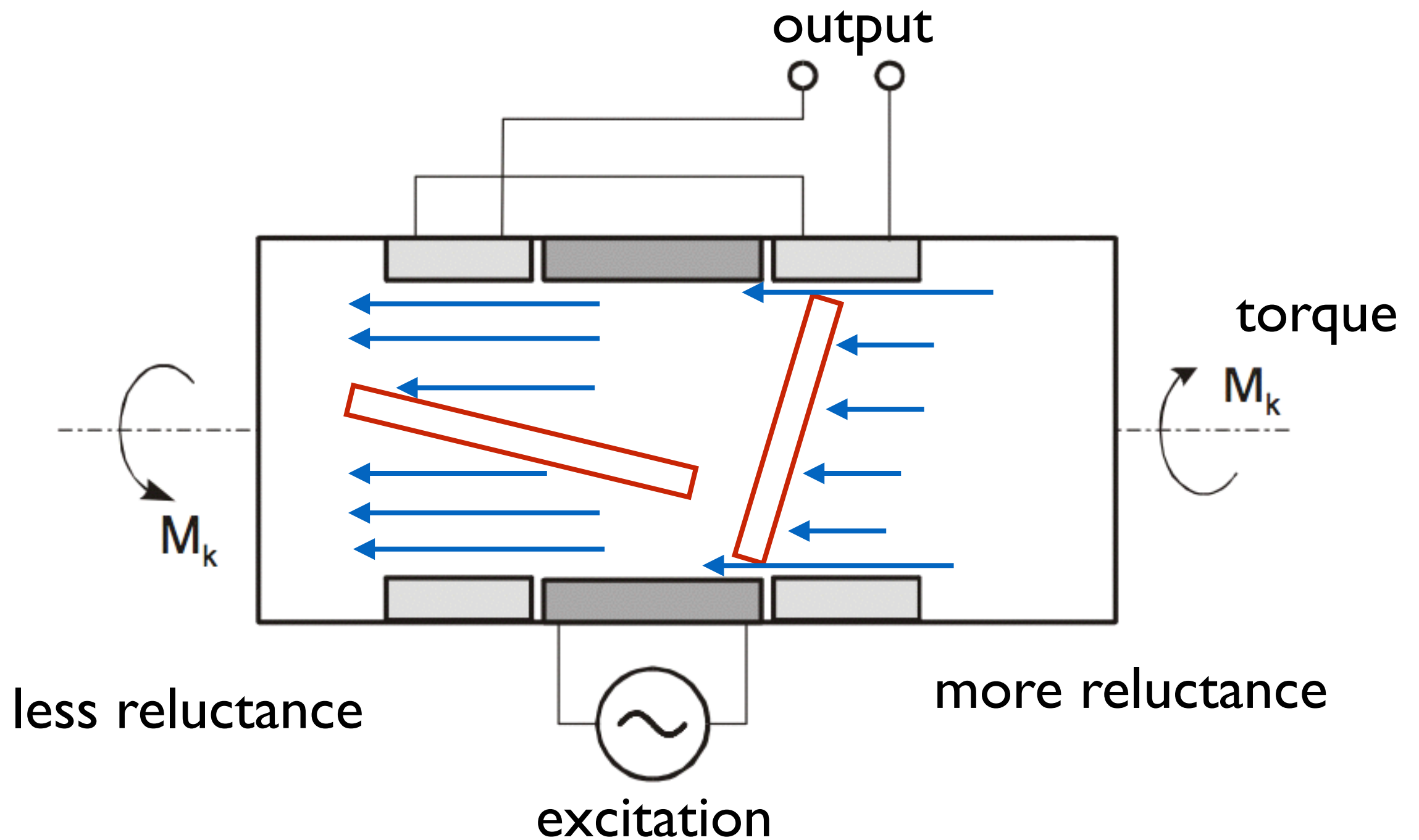
Magnetic (variable reluctance) sensors of torque



Magnetic (variable reluctance) sensors of torque

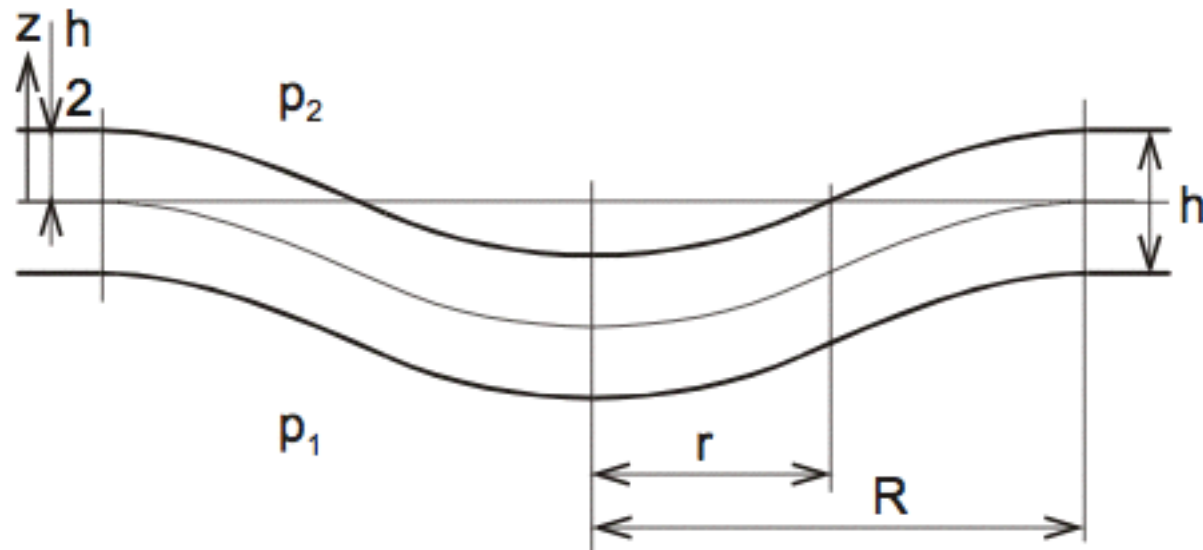


Magnetic (variable reluctance) sensors of torque

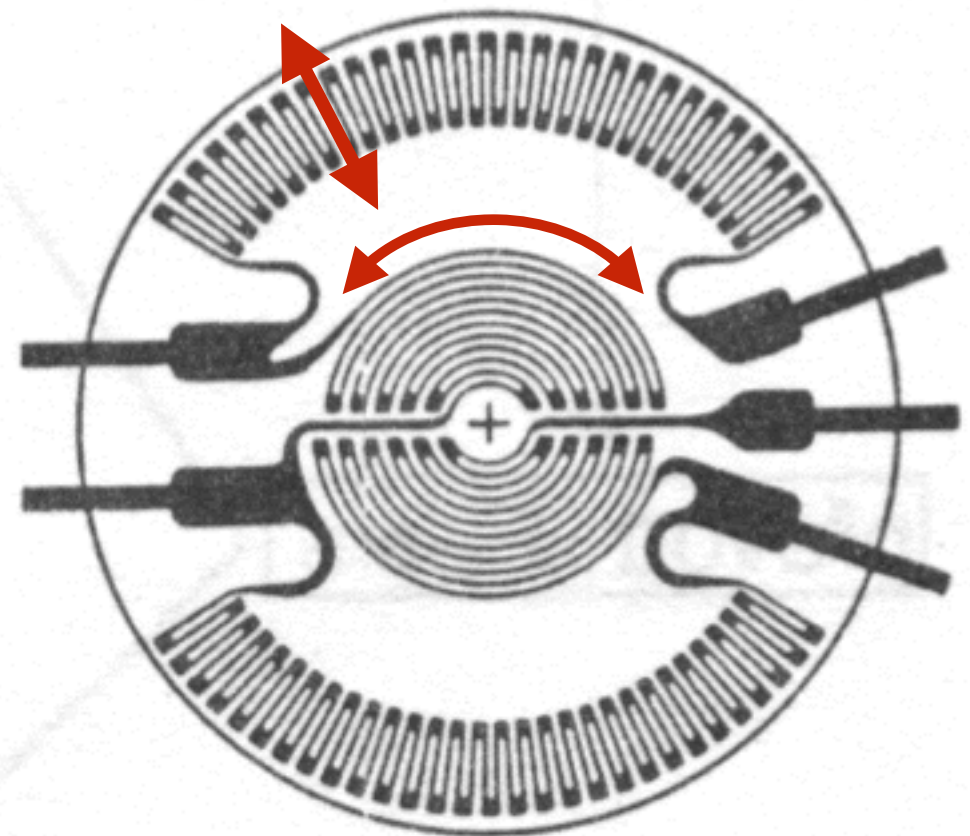
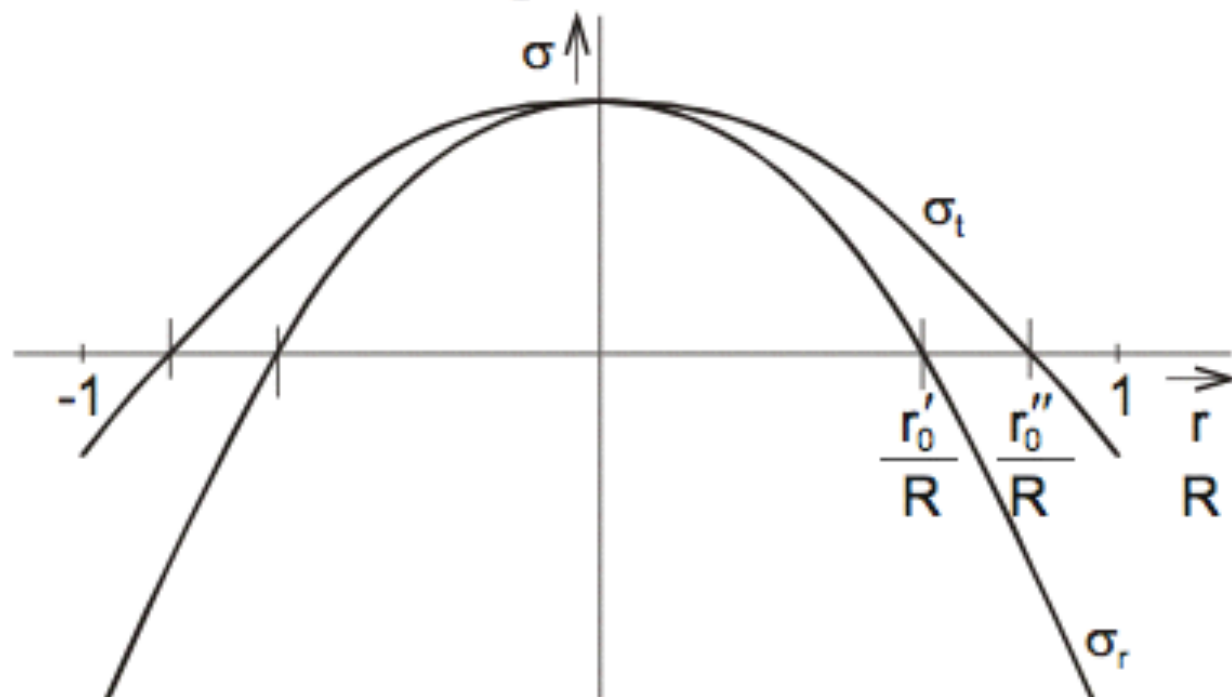


Measurement of pressure

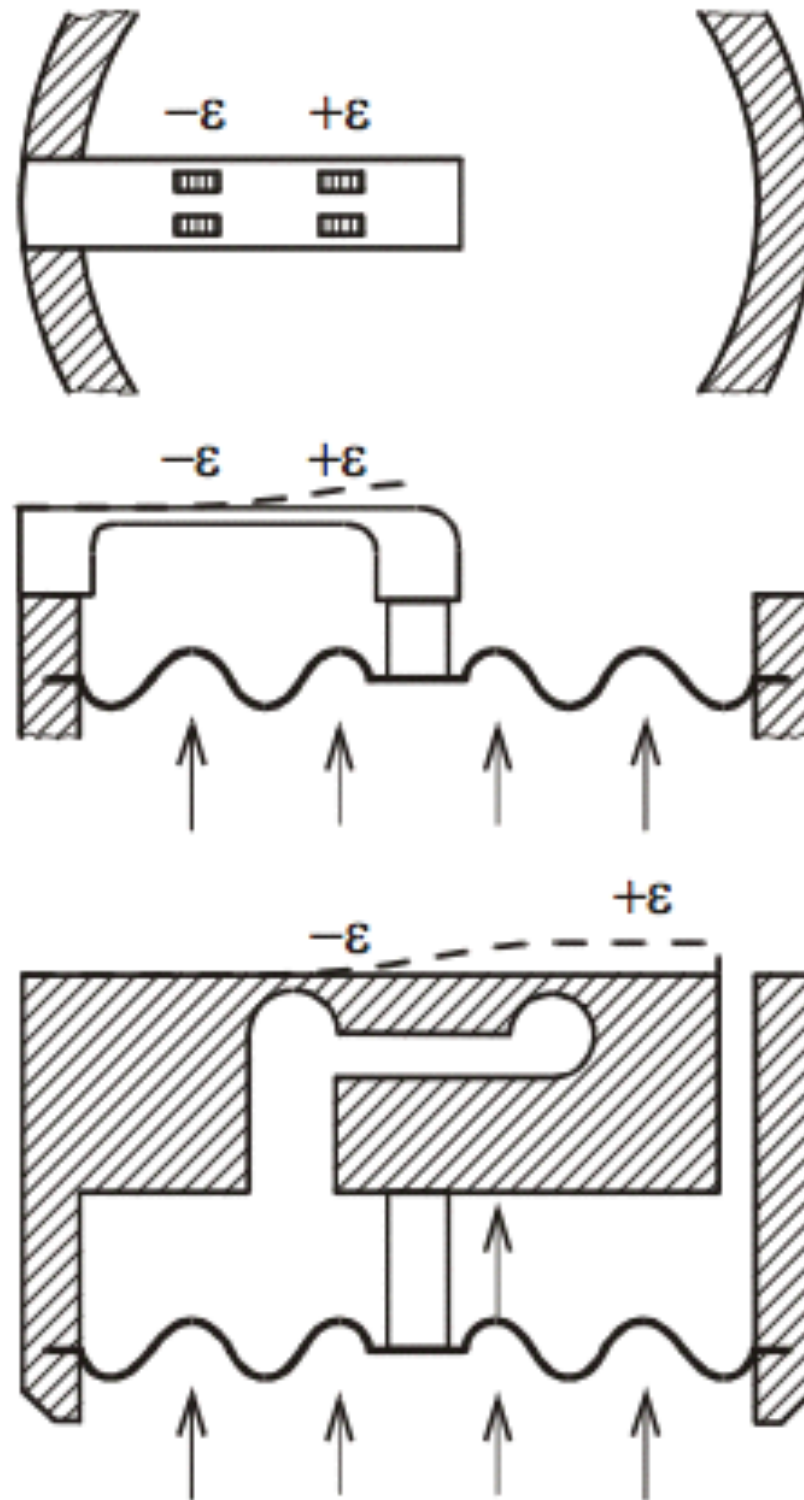
Membrane with rosette strain gauges



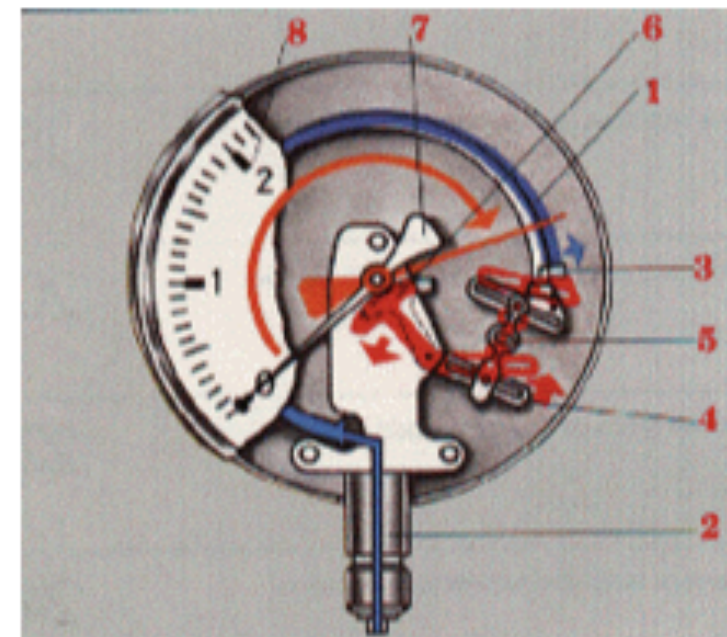
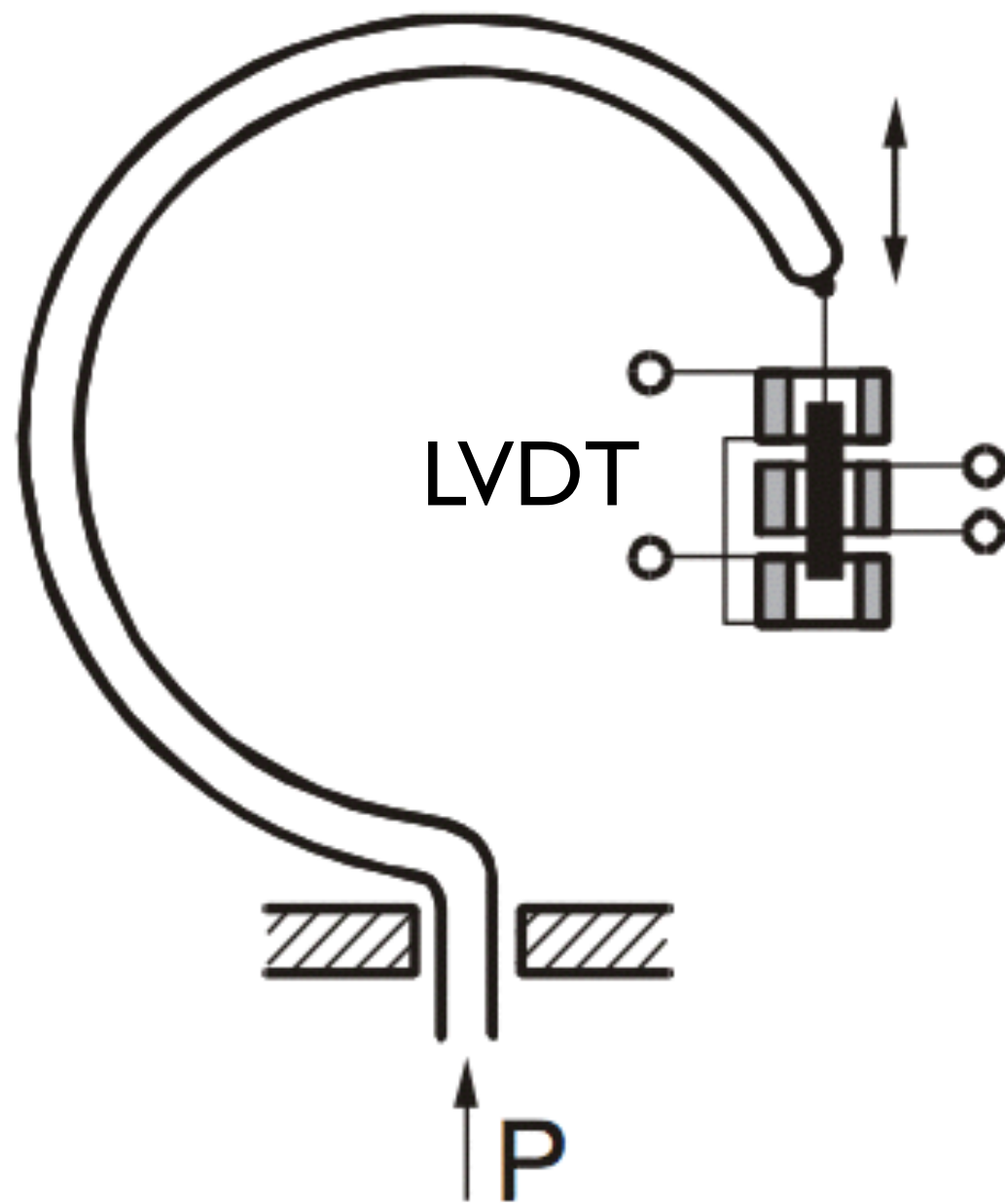
Distribution of radial and tangential strain under pressure-deformation



Deformation elements with cantilever and bellows



Bourdon tube



Differential capacitor with separating liquid

