Authors CS 109

## Take-Home Quiz

Handout #1 March 13–20, 2021

Exam # 00000

Here are directions for how to use this LaTeX-generated document:

## 1 Video Views: Binomial Approximation [10 points]

We are studying a video streaming platform. We define a viewer for a particular video as a user who watches the video in entirety. Let the number of viewers for each video be distributed as a Binomial random variable Bin(n, p), where n is the initial number of viewers and p is the probability that each initial viewer watches the entire video.

Suppose that the number of viewers for a popular video A is distributed as Bin(200, 0.4). Furthermore, suppose that the number of viewers for a not-so-popular video B is distributed as Bin(100, 0.15). What is the **approximate** probability that the number of viewers for video A is **more than twice** the number of viewers for video B?

In addition to providing justification above,	
please compute a numeric answer:	

## 2 Jointly Continuous Random Variables [10 points]

*X* and *Y* are jointly continuous random variables with the following joint PDF:

$$f_{X,Y}(x,y) = c(2x^2 + 2y)$$
  $0 \le x \le 1 \text{ and } 0 \le y \le 1$  (1)

Note that  $f_{X,Y}(x, y)$  is a valid PDF if the constant c = 3/5. What is E[Y]? Provide a numeric answer (fractions are fine).

In addition to providing justification above, please compute a numeric answer:

## 3 Mystery Code [10 points]

```
unsigned char mystery(unsigned char n) {
    n |= n >> 1;
    n |= n >> 1;
    n |= n >> 2;
    n++;
    return (n >> 1);
}
What does the following code print out?
printf("%u", mystery(88));
```