

# H3

## Uitwerking vd energietallen vd Eerste Hoofdwet

### Arbeidswisseling

Volume arbeid bij omkeerbare toekomstver.

$$F = P \cdot A$$

$$dW = F \cdot dx$$

$$dW = P \cdot A \underbrace{dx}_{= dV}$$

$$\Rightarrow dW = P dV$$

$$W_{1 \rightarrow 2} = \int_1^2 dW = \int_1^2 P dV$$

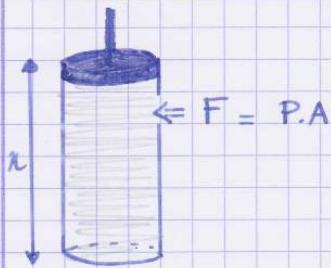


Technische arbeid  $W_t$

$$W_t = W_{in} + W + W_{uit}$$

$\swarrow$  arbeid inlaatdop       $\downarrow$  volume arbeid       $\searrow$  arbeid uitlaatdop

## Inlaatstop



$$W_{in} = F \cdot x = P \cdot A \cdot x = V$$

$$W_{in} = P_1 V_1 > 0$$

(6613) comp  
(0584) exp

## Compressie



$$W = \int_1^2 P dV < 0$$

(4213)

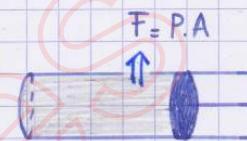
## Expansie



$$W = \int_1^2 P dV > 0$$

(4213)

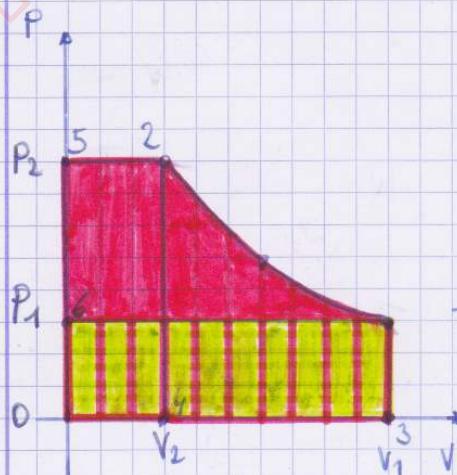
## Uitlaatklep



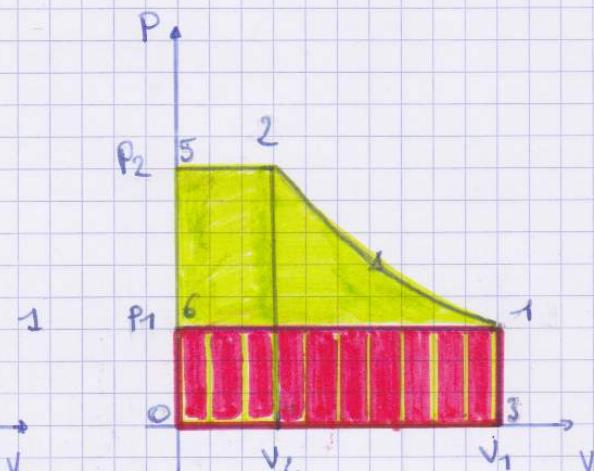
$$W_{out} = -P_2 V_2 < 0$$

(0425) comp  
(0613) exp

## compressie (PV-dia.)



$$W_{t1 \rightarrow 2} = - \int_1^2 V dP$$



$$W_{t2 \rightarrow 1} = - \int_1^2 V dP$$

### Isobaric ( $P = \text{ct.}$ )

$$W_{1 \rightarrow 2} = \int_1^2 P dV$$

$$W_{1 \rightarrow 2} = P \Delta V$$

$$W_{t, 1 \rightarrow 2} = - \int_1^2 V dP$$

$$W_{t, 1 \rightarrow 2} = 0$$

### Isochoric ( $V = \text{ct.}$ )

$$W_{1 \rightarrow 2} = \int_1^2 P dV$$

$$W_{1 \rightarrow 2} = 0$$

$$W_{t, 1 \rightarrow 2} = - \int_1^2 V dP$$

$$W_{t, 1 \rightarrow 2} = V \Delta P$$

### Isotherm ( $T = \text{ct.}$ )

$$W_{1 \rightarrow 2} = \int_1^2 P dV$$

$$P_1 V_1 = m R g T$$

$$= \int_1^2 \frac{P_1 V_1}{V} dV$$

$$PV = m R g T$$

$$= P_1 V_1 \int_1^2 \frac{dV}{V}$$

$$\Rightarrow P = \frac{P_1 V_1}{V}$$

$$= P_1 V_1 \ln\left(\frac{V_2}{V_1}\right)$$

$$\Rightarrow V = \frac{P_1 V_1}{P}$$

$$W_{1 \rightarrow 2} = P_1 V_1 \ln\left(\frac{P_1}{P_2}\right)$$

$$\frac{V_2}{V_1} = \frac{P_2}{P_1}$$

$$W_{t, 1 \rightarrow 2} = - \int_1^2 V dP = - \int_1^2 P_1 V_1 \frac{dP}{P}$$

$$= - P_1 V_1 \ln\left(\frac{P_2}{P_1}\right)$$

$$W_{t, 1 \rightarrow 2} = P_1 V_1 \ln\left(\frac{P_1}{P_2}\right)$$

$$W_{1 \rightarrow 2} = W_{t, 1 \rightarrow 2} \quad \text{want} \quad W_{in} = -W_{out}$$

## Warme wisseling

$$dQ = m \cdot C \cdot dT$$

$$dQ = dU + dW$$

afh. van onafh. afh. v.  
transformatie v. proces proces

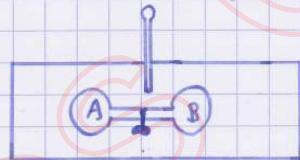
$$m \cdot C \cdot dT = dU + p \cdot dV$$

⇒ De warmewisseling  
is dus afh. v.  
gevolgd wcp.

$C_p$        $C_V$

## Inwendige Energie

### Wet van Joule



⇒ geen temp. ver.  $\Rightarrow du = dq - dw = 0$

$$\Rightarrow u = f(T) \quad (\text{toestandsgrootheid})$$

### De inwendige energie bij ideale gassen

Geen arbeid: isochoor:  $dq = du + dw$

$$\rightarrow C_V \cdot dT = du$$

verandering v. d. toestandsgrootheid  $u$

## De wet van Mayer voor ideale gassen

$$\text{Isobarisch: } dq = du + dw$$

$$cp \, dT = cv \, dT + pdv$$

$$\text{met } Pv = RgT$$

↓

$$dp + dvP = Rg \, dT$$

$$cp \, dT = cv \, dT + Rg \, dT$$

$$cp = cv + Rg$$

## Enthalpie

$$h = u + pv \rightsquigarrow dh = du + dpv$$

$$\left. \begin{array}{l} du = cv dT \\ dpv = Rg dT \end{array} \right\} \rightsquigarrow$$

$$\begin{aligned} dh &= cv dT + Rg dT \\ dh &= cv dT + (cp - cv) dT \end{aligned}$$

voor  $T$  mogelijke processen  $\Rightarrow$

$$dh = cp dT$$

$$dh = du + pdv + vdp$$

$$\begin{array}{c} dw \\ \hline dq \end{array}$$

$$dh = dq + vdp$$

$$dh = dq - dw$$

$$\Rightarrow dq = dw + dh$$

Besluit:

$$dq = cv dT + pdv$$

$$dq = cp dT - vdp$$

# H4

## Polytrope toestandsveranderingen bij ideale gassen

### Definitie

soortgelijke warmte v.h. fluidum ch.

isobarer  $C_p$   
isochoor  $C_v$

### Afleiding vol. algemene formule

$$dq = du + dw$$

$$C_v dT = C_v dT + P dv$$

$$(C_i - C_v) dT = P dv$$

$$(C_i - C_v) \left( \frac{P dv + v dP}{Rg} \right) = P dv$$

$$(C_i - C_v)(P dv + v dP) = Rg P dv$$

$$(C_i - C_v - Rg) P dv = -v dP(C_i - C_v)$$

$$(C_i - C_{ip}) P dv = -v dP(C_i - C_v)$$

$$\left( \frac{C_i - C_{ip}}{C_i - C_v} \right) \frac{dv}{v} + \frac{dP}{P} = 0$$

$P \neq 0$   
 $v \neq 0$   
 $C_i \neq C_v$

} integrieren met  $n = \frac{C_i - C_{ip}}{C_i - C_v}$

$$n dv + \ln P = ct.$$

$$\ln(Pv^n) = ct. \Rightarrow Pv^n = ct.$$

$$PV^n = ct.$$

$$n = \frac{C_p - C}{C_V - C} \Rightarrow C_i = \frac{n C_V - C_p}{n-1}$$

Isobaric :  $n = 0$

$$C_i = C_p$$

Isochoric :  $n \rightarrow \infty$

$$C_i = C_V$$

Isothermal :  $n = 1$

$$C_i = \infty$$

$$\lim_{n \rightarrow 1^-} \frac{n C_V - C_p}{n-1} < 0$$

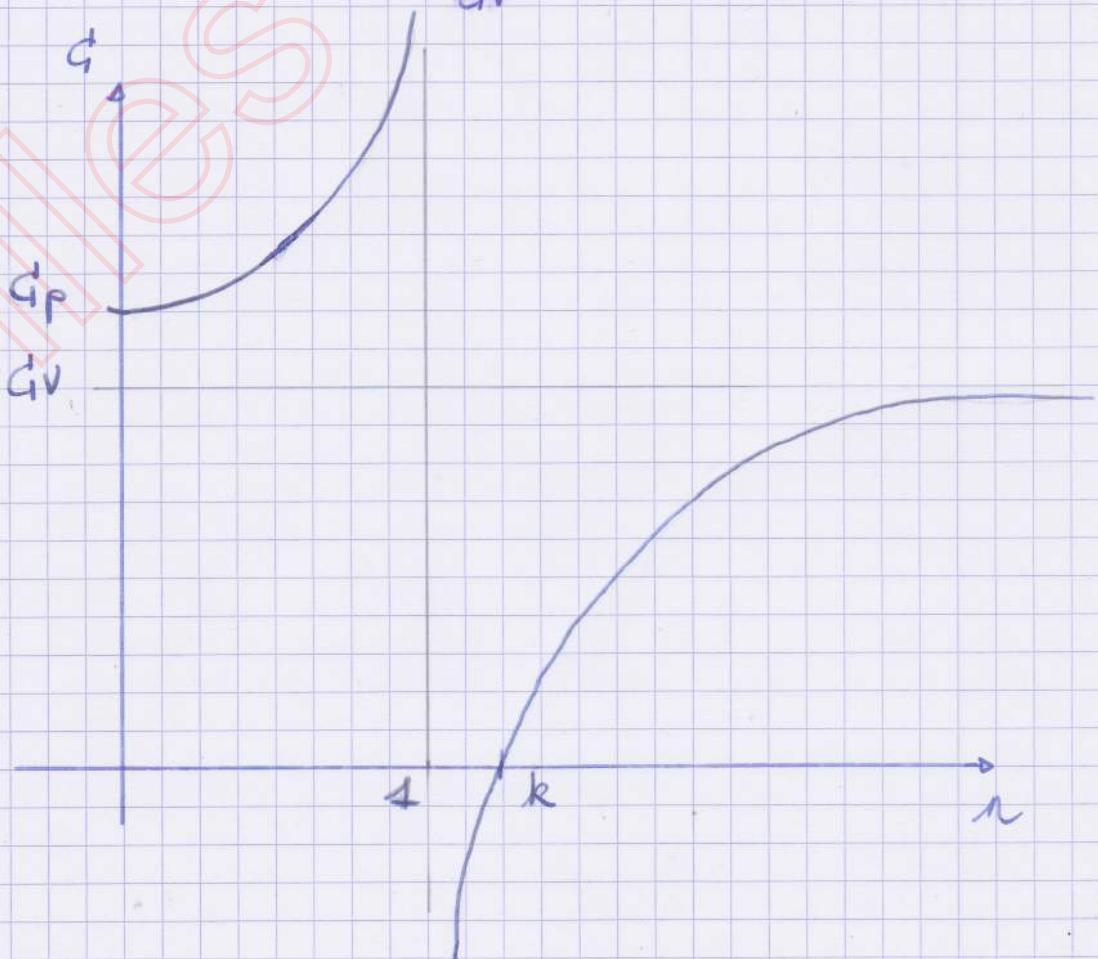
$$C_i = +\infty$$

$$\lim_{n \rightarrow 1^+} \frac{n C_V - C_p}{n-1} > 0$$

$$C_i = -\infty$$

Isentropic :  $n = k = \frac{C_p}{C_V}$

$$C_i = 0$$



# formules van Poisson

$$PV^n = \text{ct.}$$

$$\text{met } PV = m R g T$$

$$\frac{m R g T}{V} \cdot V^n = \text{ct} \Rightarrow T \cdot V^{(n-1)} = \text{ct.}$$

$$P \left( \frac{m R g T}{P} \right)^n = \text{ct.}$$

$$\Rightarrow P \cdot T^{(1-n)} = \text{ct.}$$

## Berekening vd volumearbeit

$$W_{1 \rightarrow 2} = \int_1^2 P dV = \int_1^2 P_1 V_1^n \cdot V^{-n} dV$$

~~$$PV^n = P_1 V_1^n \Rightarrow P = \frac{P_1 V_1^n}{V^n}$$~~

$$= P_1 V_1^n \int_1^2 V^{-n} dV = \frac{P_1 V_1^n}{1-n} \left[ V^{1-n} \right]_{V_1}^{V_2}$$

$$= \frac{P_1 V_1^n}{1-n} \left( V_2^{1-n} - V_1^{1-n} \right) = \frac{P_1 V_1^n}{n-1} \left( V_1^{1-n} - V_2^{1-n} \right)$$

$$= \frac{P_1 V_1}{n-1} \left( 1 - \left( \frac{V_2}{V_1} \right)^{1-n} \right)$$

$$T_1 V_1^{n-1} = T_2 V_2^{n-1} \rightarrow \left( \frac{V_2}{V_1} \right)^{n-1} = \frac{T_1}{T_2}$$

$$P_1 V_1 = R g T_1$$

$$= \frac{R g T_1}{n-1} \left( 1 - \frac{T_2}{T_1} \right)$$

$$W_{1 \rightarrow 2} = \frac{R g}{n-1} \left( T_1 - T_2 \right)$$

$$q_{1 \rightarrow 2} = C_i dT$$

$$W_{1 \rightarrow 2} = \frac{Rq}{n-1} [T_1 - T_2]$$

$$C_i = \frac{nC_{iV} - C_p}{n-1}$$

$$Rq = C_p - C_{iV}$$

$$k = \frac{C_p}{C_v}$$

$$W_{1 \rightarrow 2} = \frac{Rq}{n-1} (T_1 - T_2) \quad q_{1 \rightarrow 2} = C_i (T_2 - T_1)$$

$$\Rightarrow W = \frac{Rq}{n-1} \frac{q}{-C_i} \quad C_i = \frac{nC_{iV} - C_p}{n-1}$$

$$\Rightarrow W = \frac{Rq}{(n-1)} \cdot \frac{q(n-1)}{C_p - nC_v} \quad Rq = C_p - C_{iV}$$

$$W = \frac{C_p - C_v}{C_p - nC_v} q \quad k = \frac{C_p}{C_v}$$

$$W = \frac{k-1}{k-n} q$$

$$\Rightarrow q = \frac{k-n}{k-1} W$$

$$W_{t,1 \rightarrow 2} = - \int_1^2 v dp$$

$$PV^n = ct.$$

$$= +n \int_1^2 P dV$$

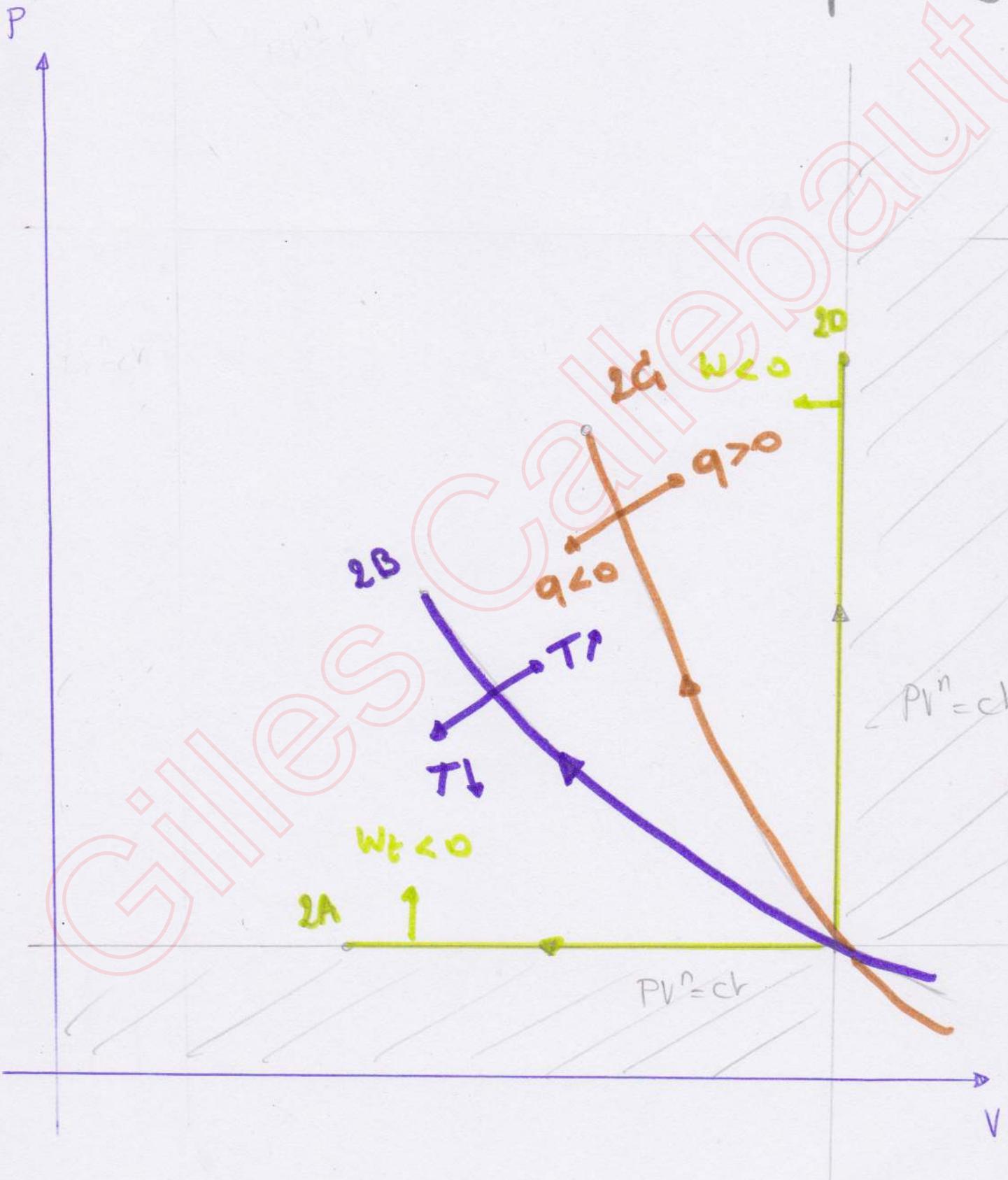
$$v^n dp + np v^{n-1} dv = 0$$

$$= n W_{1 \rightarrow 2}$$

$$- v dp = np dV$$

$$\Rightarrow W_{t,1 \rightarrow 2} = n W_{1 \rightarrow 2}$$

Compressive



2A

$$T_{2A} < T_1$$

$$q_{1 \rightarrow 2A} < 0$$

$$W_{1 \rightarrow 2A} < 0$$

isobaric  $n=0$

$$W_{t,1 \rightarrow 2A} = 0$$

2B

$$T_{2B} = T$$

isothermal  $n=1$

$$q_{1 \rightarrow 2B} = W_{1 \rightarrow 2B}$$

$$= W_{t,1 \rightarrow 2B}$$

$$< 0$$

2C

$$q_{1 \rightarrow 2C} = 0$$

$$W_{1 \rightarrow 2C} < 0$$

$$W_{t,1 \rightarrow 2C} < 0$$

Isentropic  $n=k \rightarrow \dot{c}=0$

$$T_{2C} > T_1$$

$$U_1 < U_{2C}$$

2D

$$T_{2D} > T_1$$

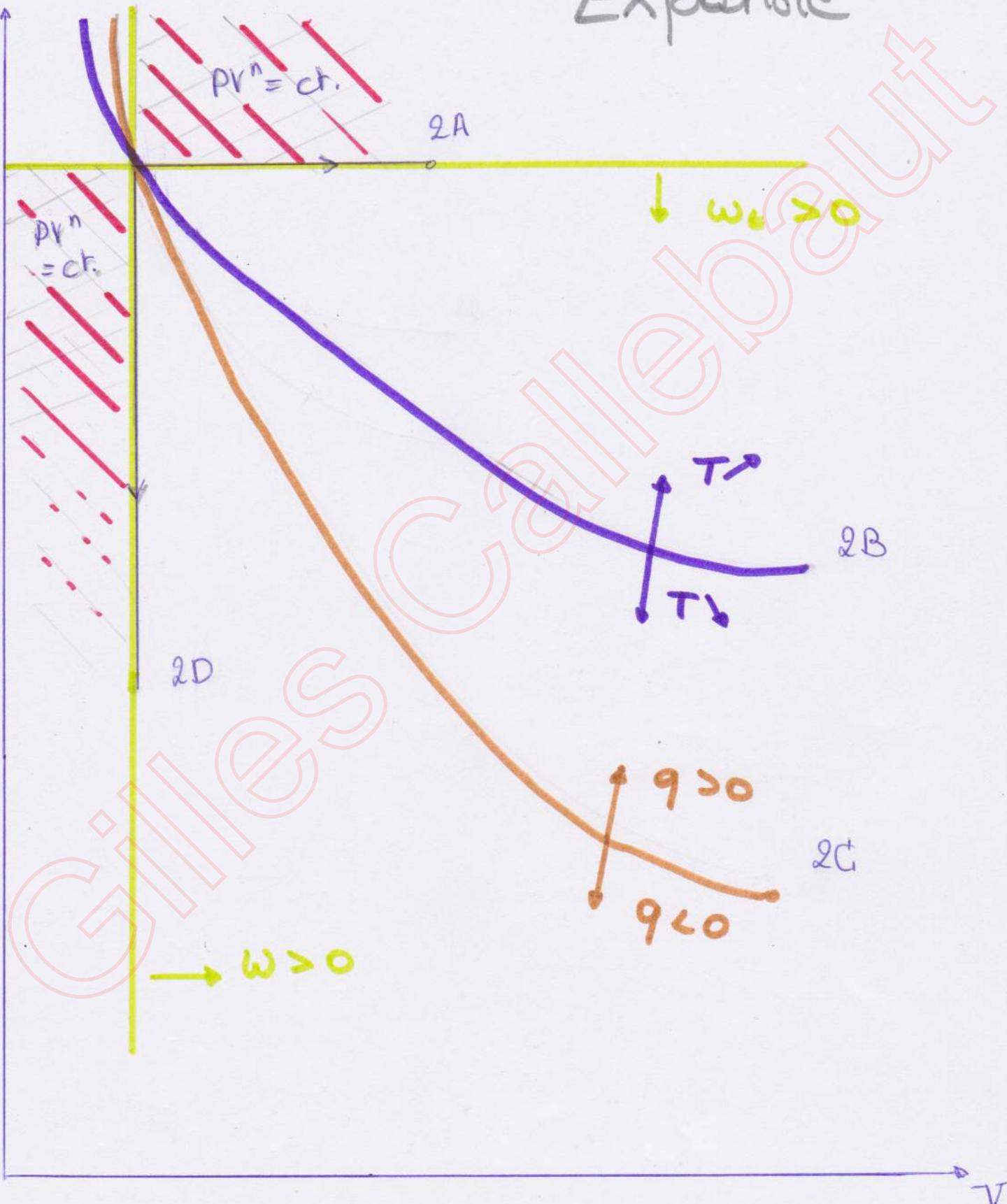
$$q_{1 \rightarrow 2D} > 0$$

$$W_{1 \rightarrow 2D} = 0$$

$$W_{t,1 \rightarrow 2D} < 0$$

Isochoric  $n=\infty$

Compressive



Expansion

$\omega_e > 0$

$T \nearrow$   
 $T \searrow$

2B

$q > 0$   
 $q < 0$

2C

2D

$\omega > 0$

$PV^n = c.t.$

2A

①

Helling:  $PV^n = c$

$$v^n dp + nv^{n-1} p dv = 0$$

$$\frac{dp}{dv} = -\frac{np}{v}$$

Vorm: hyperbool, buik naar beneden (2x aftrekken)  
 ↳ thuis



②A

$$T_{2A} > T_1$$

$$\text{grootte } \leftarrow (q_{1 \rightarrow 2A}) > 0$$

$$w_{1 \rightarrow 2A} > 0$$

$$w_{t,1 \rightarrow 2A} = 0$$

isobar

$$n=0$$

②B

$$T_{2B} = T_1$$

$$q_{1 \rightarrow 2B} = w_{1 \rightarrow 2B} = w_{t,1 \rightarrow 2B} > 0$$

isotherm

$$n=1$$

②C

$$q_{1 \rightarrow 2C} = 0$$

$$w_{1 \rightarrow 2C} > 0$$

$$w_{t,1 \rightarrow 2C} > 0$$

$$v_{2C} < v_1$$

$$T_{2C} < T_1$$

Isentroop

$$c_i = 0$$

$$n = k$$

②D

$$T_{2D} < T_1$$

$$q_{1 \rightarrow 2D} < 0$$

$$w_{1 \rightarrow 2D} = 0$$

$$w_{t,1 \rightarrow 2D} > 0$$

Isochor

$$n = \infty$$

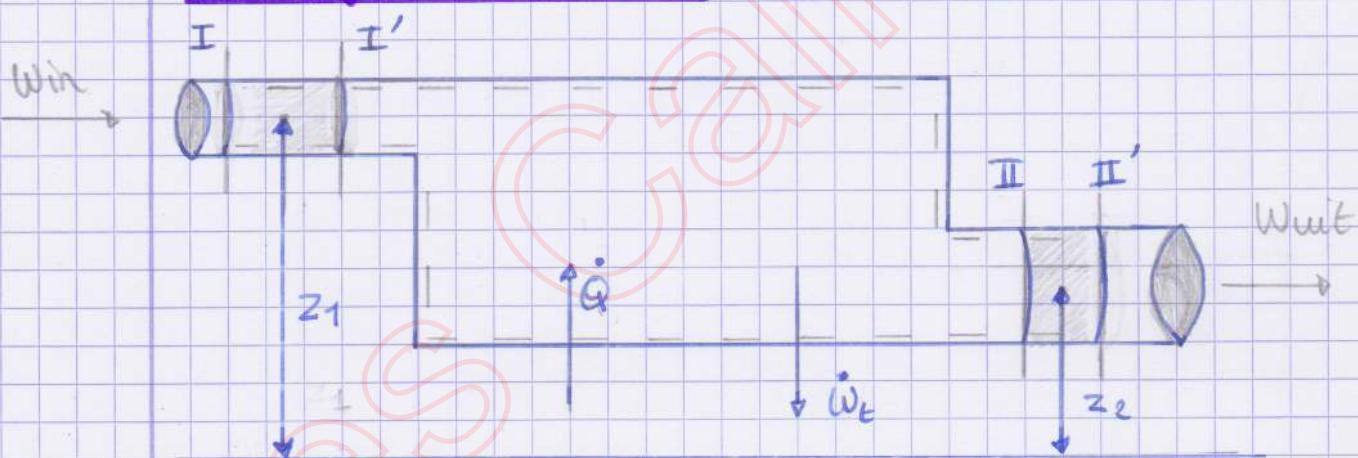
Expansie

# H5

## De eerste hoofdwet voor open systemen

Bij open systemen stroomt het fluidum door een energiewisselaar zodat ook de kinetische en potentiële energie ervan kunnen veranderen.

### Energiewisselaar



Stel�ntumming stationair:  $(\text{Energie})_{\text{in}} = (\text{Energie})_{\text{uit}}$

$$q_{1 \rightarrow 2} + e_{II'} = w_{1 \rightarrow 2} + e_{II''}$$

$$\left\{ \begin{array}{l} e_{II'} = u_1 + \frac{c_1^2}{2} + g z_1 \\ e_{II''} = u_2 + \frac{c_2^2}{2} + g z_2 \end{array} \right. \quad \begin{matrix} \text{inh.} \\ \text{kin.} \\ \text{pot.} \end{matrix} \quad \begin{matrix} \text{energie} \end{matrix}$$

$$w_{1 \rightarrow 2} = w_{t,1 \rightarrow 2} + w_{in} + w_{out}$$

$$= w_{t,1 \rightarrow 2} - p_1 v_1 + p_2 v_2$$

$$(u_2 + p_2 v_2) - (u_1 + p_1 v_1) + \frac{(c_2^2 - c_1^2)}{2} + g(z_2 - z_1) = q - w_t$$

$\underbrace{\quad}_{= (h_2 - h_1)}$

$$dh + d\left(\frac{c^2}{2}\right) + g dz = dq - dw_t$$

# Toepassingen

## Warmtewisselingen

→ afkoelen of opwarmen

→  $\bar{q}$  m arbeid, kin. en pot. te verwaarlozen

$$\Rightarrow \Delta h = q_{1 \rightarrow 2}$$

$$\Rightarrow q_{1 \rightarrow 2} = \Delta h = C_p(T_2 - T_1) \quad \text{Enkel ideaal gas}$$

## ISENTROPE arbeidswisseling

↳ zonder noemijswaardig warmteverlies

→ kin. en pot. te verwaarlozen

$$\Rightarrow \Delta h = -W_{t,1 \rightarrow 2} \quad \text{of} \quad \Delta h = W_{t,1 \rightarrow 2}$$

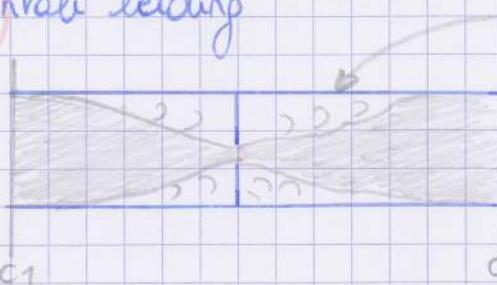
↑  
compressie

↑  
expansie

## Stroomprocessen

→  $\bar{q}$  m arbeid, warmteoverdracht te verwaarlozen

→ horizontale leiding



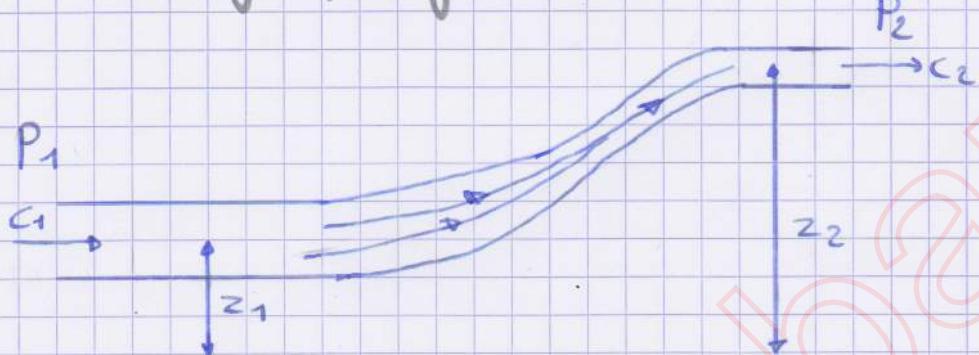
$$\partial h + d\left(\frac{C^2}{2}\right) = 0$$

→ kin. te verw.  $\rightarrow dh = 0$

→ ideaal gas:  $\Delta h = C_p(T_2 - T_1)$

plus zonder temp. verandering

# De vergelijking van Bernoulli



→ grn waarde of arbeid wisseling, grn temp. verandering

$$\Rightarrow \Delta h + \frac{\Delta c^2}{2} + g \Delta z = 0$$

$$\left| \begin{array}{l} \Delta h = \Delta U + \Delta W \\ \end{array} \right.$$

$$\Delta W + \frac{\Delta c^2}{2} + g \Delta z = 0$$

$$\left| \begin{array}{l} v = ct. \\ \rightarrow v = \frac{1}{\rho} = ct. \end{array} \right.$$

$$W + \frac{c^2}{2} + gz = \text{cte.}$$

$$\Rightarrow \frac{P}{\rho} + \frac{c^2}{2} + gz = \text{cte.}$$

$$\Rightarrow \frac{P}{\rho g} + \frac{c^2}{2g} + z = \text{cte.}$$

## De eerste hoofdwet voor gesloten systemen

→ grn kin., grn pot. energie

$$dh = dq - dw_t$$

$$du + dw = dq - dw_t$$

$$du + dw_{1 \rightarrow 2} = dq$$

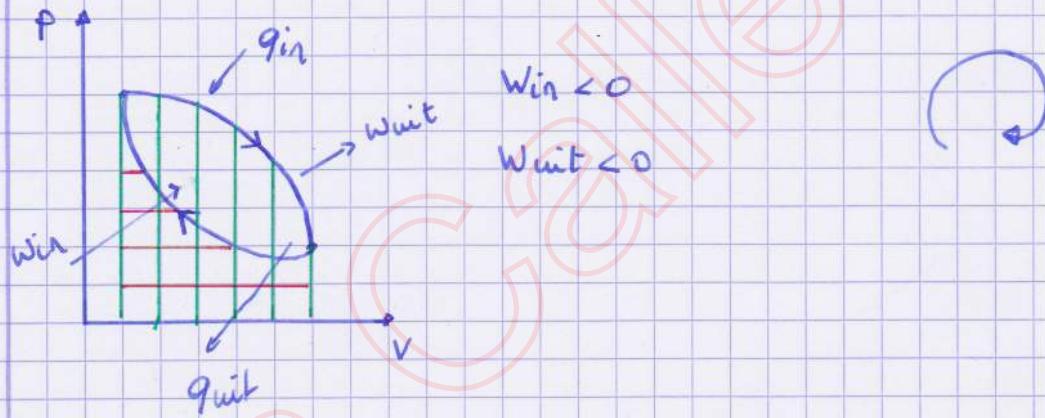
# H6

## Sociale kringprocessen en hun fundamentelementen

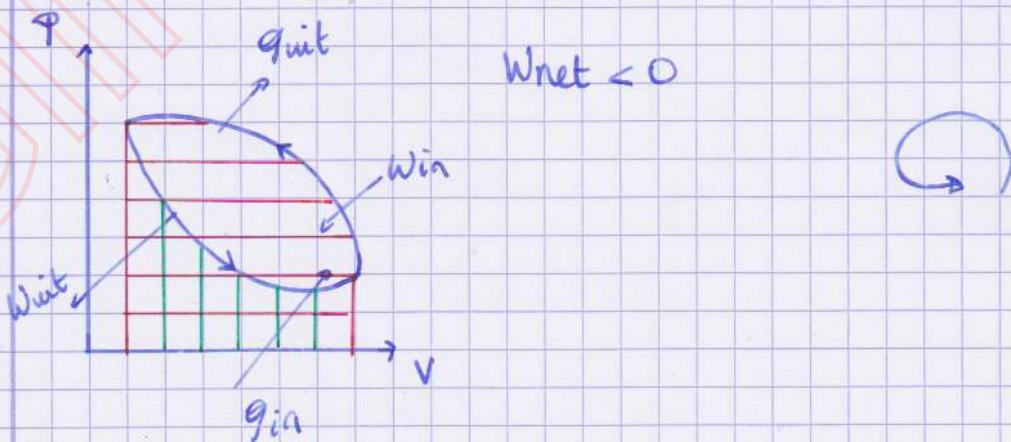
### Arbeidsleverende of positieve kringprocessen

(motoren)

→ De expansielijn ligt hoger dan de compressielijn.



### Arbeidsverbruikende of negatieve kringprocessen



# Rendement van een kringproces

De eerste hoofdwet:

Open systeem

gesloten systeem

$$dq = du + dw$$

$$dq = dh + dw_{\text{ext}} + d(\frac{c^2}{2}) + pdz$$

$$\text{met } \oint du = \oint dh = \oint d(c^{3/2}) = \oint q dz = 0$$

$$\Rightarrow \oint dq = \oint dw$$

$$\oint dq = \oint dw_{\text{ext}}$$

## Thermisch rendement ve pos. kringproces

$$q_{\text{in}} - |q_{\text{uit}}| = W_{\text{nut}} - |W_{\text{int}}|$$

$$\eta_{\text{th}} = \frac{W_{\text{nut}}}{q_{\text{in}}} = \frac{q_{\text{in}} - |q_{\text{uit}}|}{q_{\text{in}}} = 1 - \frac{|q_{\text{uit}}|}{q_{\text{in}}}$$

## Kooleffect (of koudifactor) en warmteproductiegetal v. neg. kringproces

Koelmachine

Warmtepomp

$$\epsilon = \frac{q_{\text{in}}}{|W_{\text{nut}}|} = \frac{q_{\text{in}}}{|q_{\text{uit}}| - q_{\text{in}}}$$

$$\epsilon_w = \frac{|q_{\text{uit}}|}{|W_{\text{nut}}|}$$

$$\epsilon = \frac{1}{\frac{|q_{\text{uit}}|}{q_{\text{in}}} - 1}$$

$$|W_{\text{nut}}| = |q_{\text{uit}}| - q_{\text{in}}$$

$$1 = \frac{|q_{\text{uit}}|}{W_{\text{nut}}} - \frac{q_{\text{in}}}{W_{\text{nut}}}$$

$$1 = \epsilon_w - \epsilon$$

# H7 De tweede hoofdwet en Entropie

## Principe van Kelvin

$$\eta_{th} = \frac{W_{net}}{q_{in}} = \frac{q_{in} - q_{out}}{q_{in}}$$

$\Rightarrow q_{out} \neq 0 \Rightarrow$  het is onmogelijk een kringproces uit te voeren die warmte uit één bron volledig omzet in arbeid.

## Principe van Clausius

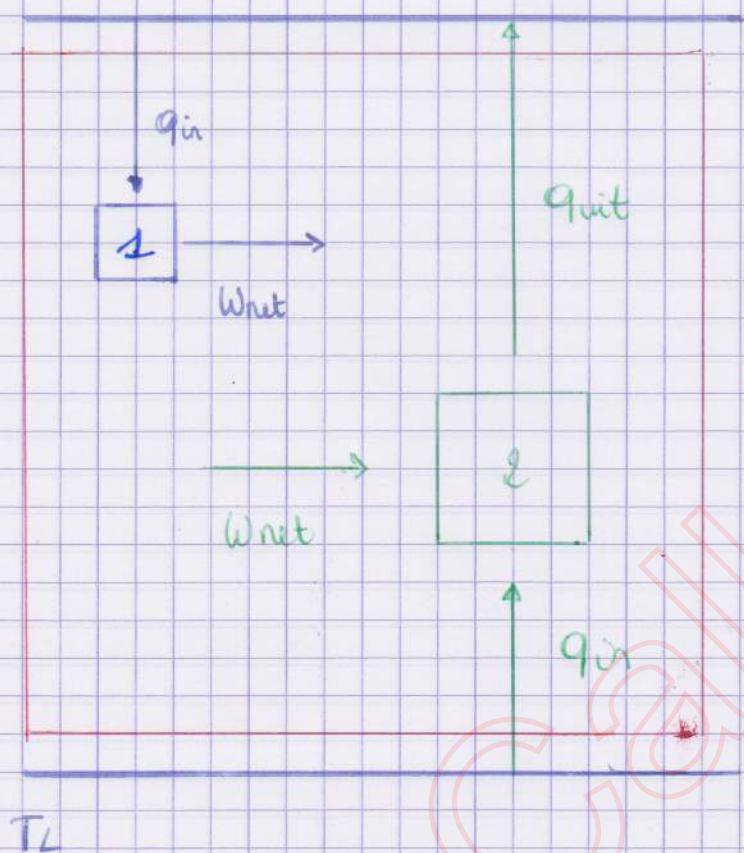
$$\epsilon = \frac{q_{in}}{W_{net}} = \frac{q_{in}}{q_{out} - q_{in}}$$

$$\epsilon_w = \frac{q_{out}}{W_{net}}$$

Arbeid nodig . thermische energie lage temp  $\rightarrow$  hogere

$\Rightarrow$  energieomzettingen zijn beperkt ook al  $\bar{w}$  voldoan aan de wet van behoud van energie.

T<sub>H</sub>



$$\Rightarrow |W_{net}| = 0$$

↑  
HW II ?

①  ~~$\eta_{ch} = 100\%$~~   $\rightarrow q_{in} = W_{net}$

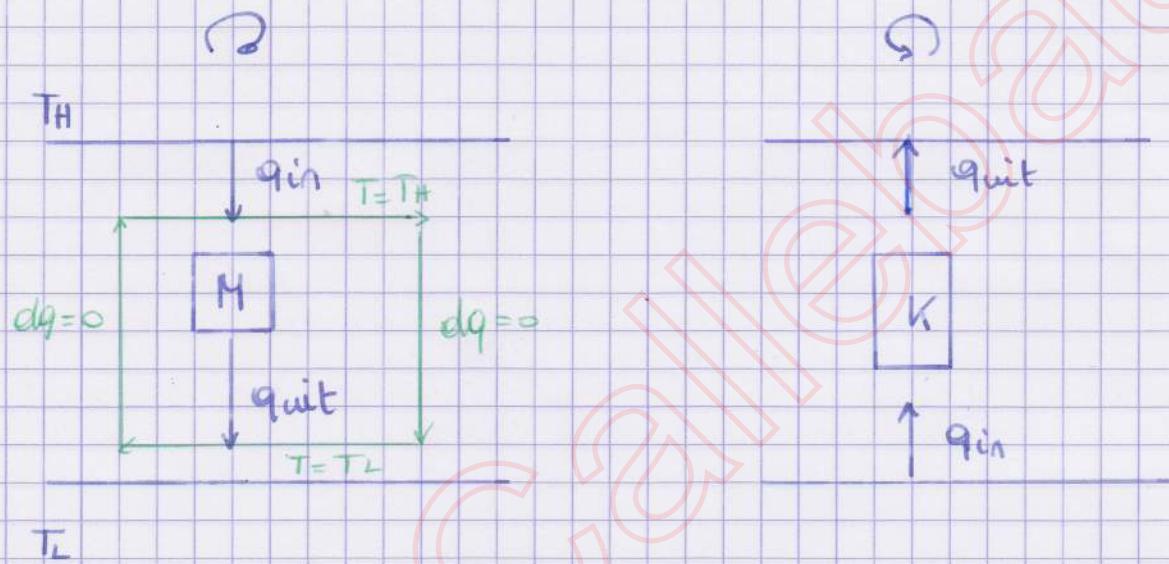
②  ~~$E \neq \infty$~~   $\Rightarrow |q_{out}| = q_{in} + |W_{net}|$

Koppelen ① & ② :  $W_{net,1} = W_{net,2}$

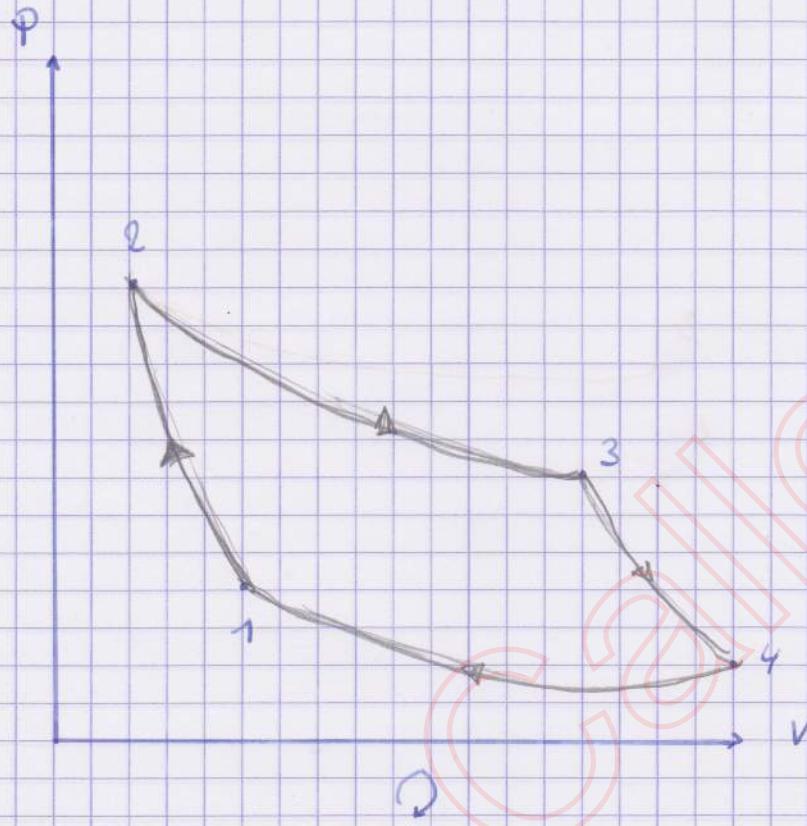
$$|q_{out,2}| = |q_{in,2} + q_{in,1}|$$

# Het kringproces van Carnot

Een ideaal kringproces



# Een omkeerbaar kringproces



$1 \rightarrow 2$

ISENTROPE compresie

$$\rightarrow q_{1 \rightarrow 2} = 0$$

$$w_{1 \rightarrow 2} < 0$$

exp.

$$w_{2 \rightarrow 1} > 0$$

$$q = 0$$

$2 \rightarrow 3$

ISOTHERME expansie

$$\rightarrow q_{2 \rightarrow 3} = w_{2 \rightarrow 3} = p_2 v_2 \ln\left(\frac{v_3}{v_2}\right)$$

$$= (RgT_H) \ln\left(\frac{v_3}{v_2}\right) > 0$$

$$q_{3 \rightarrow 2} = w_{3 \rightarrow 2} < 0$$

compr.

$3 \rightarrow 4$

ISENTROPE expansie

$$\rightarrow w_{3 \rightarrow 4} > 0$$

$$q_{3 \rightarrow 4} = 0$$

compr.

$$w_{4 \rightarrow 3} < 0$$

$$q = 0$$

$4 \rightarrow 1$

ISOTHERME compresie

$$\rightarrow q_{4 \rightarrow 1} = w_{4 \rightarrow 1} = p_4 v_4 \ln\left(\frac{v_1}{v_4}\right)$$

$$= RgT_L \ln\left(\frac{v_1}{v_4}\right) < 0$$

exp.

$$q_{4 \rightarrow 4} = RgT_L \ln\left(\frac{v_4}{v_3}\right)$$

# Rendement vr. Carnot - kringproces

(ideel gas)

## Thermisch rendement

$$\eta_{th}^c = 1 - \frac{1 q_{uit1}}{q_{in}} \rightarrow = w_{8 \rightarrow 1} = Rg T_L \ln \left( \frac{v_1}{v_8} \right)$$

$$\rightarrow = w_{2 \rightarrow 3} = Rg T_H \ln \left( \frac{v_3}{v_2} \right)$$

Isentropen  $\rightarrow$  formule van Poisson

$$T_L v_1^{k-1} = T_H v_2^{k-1} \quad T_L v_4^{k-1} = T_H v_3^{k-1}$$

$$\left( \frac{v_8}{v_1} \right)^{k-1} = \left( \frac{v_3}{v_2} \right)^{k-1}$$

$$\frac{1 q_{uit1}}{q_{in}} = \frac{T_L}{T_H}$$

$$\Rightarrow \eta_{th}^c = 1 - \frac{T_L}{T_H}$$

warmte toevoer  $\rightarrow$  hoog mogelijke temp.

warmte afvoeren  $\rightarrow$  laag " "

## Het kooleffect of koude factor

$$\epsilon^c = \frac{q_{in}}{|q_{uit}| - q_{in}}$$

$$q_{in} = R_p T_L \ln\left(\frac{v_u}{v_i}\right)$$

$$|q_{uit}| = \dot{W}_{3 \rightarrow 2}$$

$$= R_p T_H \ln\left(\frac{v_u}{v_3}\right)$$

$$\epsilon^c = \frac{T_L}{T_H - T_L}$$

## Het warmteproductiegetal

$$\epsilon_w^c = \frac{|q_{uit}|}{|q_{uit}| - q_{in}} = \frac{T_H}{T_H - T_L}$$

## Carnot, hoogst rendement

motor N eff. dan carnot-motor

$$R_{th} > R_{th}^c \quad \text{bij } q_{in}$$

inverse carnot-motor (koelmach.) gekoppeld aan M

$$|W_{net,K}| = |q_{out,K}| - q_{in,K}$$

$$|q_{out,K}| = q_{in,M}$$

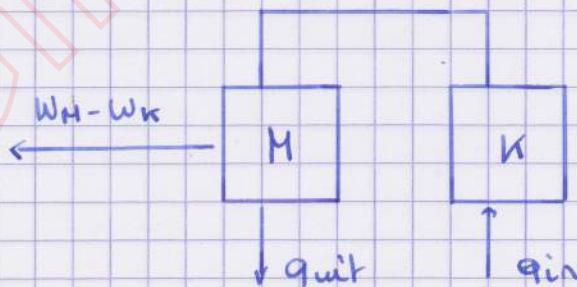
indien  $R_{th}^{\eta} > R_{th}^K$

$$\Rightarrow W_{net,M} > W_{net,K}$$

$$\Rightarrow W_{net} = W_{net,\eta} - W_{net,K}$$

$\hookrightarrow$  met 1 warmtebron  $\rightarrow$  arbeid

$\hookrightarrow$  HWII ! steeds



# Andere kring processen

## Omkeerbaar

$$\eta_{th} = \eta_{th}^c \quad (\text{kan bewegen } \bar{w})$$

$$1 - \frac{|q_{uitH}|}{q_{in}} = 1 - \frac{T_L}{T_H}$$

$$\frac{|q_{uitH}|}{T_L} = \frac{q_{in}}{T_H}$$

$$\Rightarrow \frac{q_{uit}}{T_L} + \frac{q_{in}}{T_H} = 0$$

$$\Rightarrow \oint \underbrace{\frac{dq}{T}}_{ds} = 0$$

## Non keerbaar

$$\eta_{th} < \eta_{th}^c$$

$$\frac{|q_{uitH}|}{T_L} > \frac{q_{in}}{T_H}$$

$$\Rightarrow \oint \frac{dq}{T} = \frac{q_{in}}{T_H} + \frac{q_{uit}}{T_L} < 0$$

# De toestandsgroothed, Entropie

Def & basisform.

$$\left\{ \begin{array}{l} ds = \frac{dq}{T} \end{array} \right. \quad (1)$$

$$dq = du + dw \quad (2)$$

$$dq = dh + dw_T \quad (3)$$

(1) & (2)

$$ds = \frac{du}{T} + \frac{dw}{T}$$

$$= \frac{C_v dT}{T} + \frac{PdV}{T}$$

$$ds = \underbrace{\frac{C_v dT}{T}}_{v} + \underbrace{\frac{Rg dv}{v}}$$

toest. grootheden

$$\underbrace{\cdot C_p}_{-} - \underbrace{\cdot C_v}_{+}$$

$$\underbrace{(C_p - C_v)}_{Rg} ds = C_p Rg \frac{dv}{v} + C_v Rg \frac{dp}{p}$$

$$ds = C_p \frac{dv}{v} + C_v \frac{dp}{p}$$

## Entropic berekenen

$$ds = \frac{dq}{T}$$

Als  $T = ct.$

$$\Delta S_2 - \Delta S_1 = \frac{q_{1 \rightarrow 2}}{T}$$

open  
systemen

geleiden

$$S = m s$$

$[kJ/K]$

$$\dot{S} = \dot{m} s$$

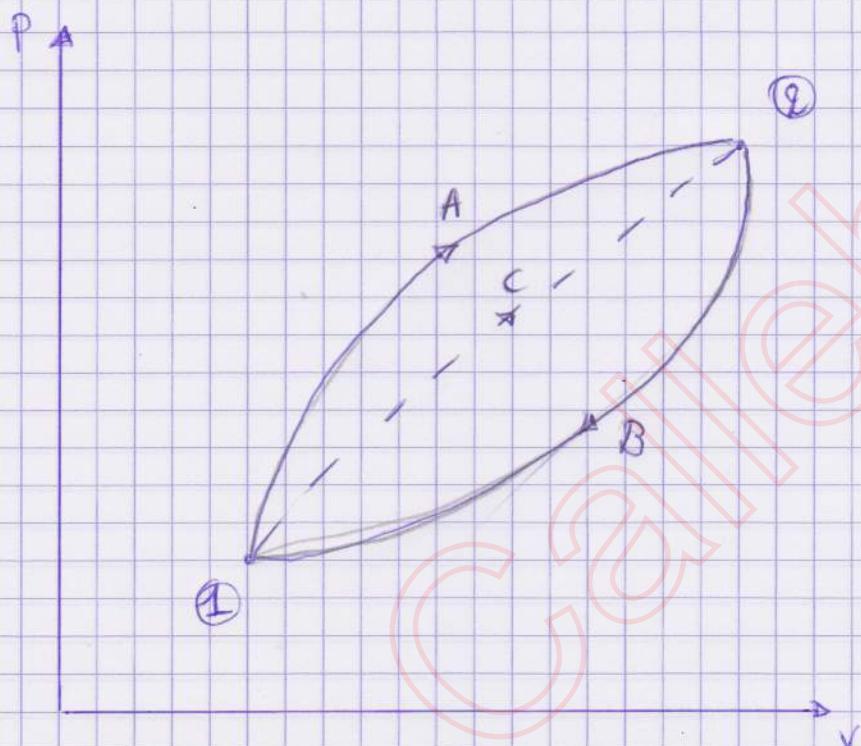
$[kW/K]$

Als  $T \neq ct.$

$$\Delta S_2 - \Delta S_1 = \int \frac{C dT}{T}$$
$$= C \ln\left(\frac{T_2}{T_1}\right)$$

$$[kJ/kgK]$$

# Entropieverandering



## Inkeerbaar

$$\int \frac{dq}{T} = \underbrace{\int_1^2 \frac{dq}{T}}_{A} + \underbrace{\int_2^1 \frac{dq}{T}}_{B} = 0$$

$$\Rightarrow \int_B \frac{dq}{T} = \Delta S_2 - \Delta S_1 = (\Delta S_{rev})$$

## Oninkeerbaar

$$\int \frac{dq}{T} = \underbrace{\int_1^2 \frac{dq}{T}}_{C} + \underbrace{\int_2^1 \frac{dq}{T}}_{B} < 0$$

$$\Rightarrow \int_C \frac{dq}{T} < \Delta S_2 - \Delta S_1$$

$$\Rightarrow \Delta S_2 - \Delta S_1 = \int_C \frac{dq}{T} + \underbrace{\Delta S_{irr.}}_{>0} > 0$$

$\Delta S_{irr.} < 0 \Rightarrow$  onmog.  
 $\Delta S_{irr.} = 0 \Rightarrow$  omkeerbaar  
 $\Delta S_{irr.} > 0 \Rightarrow$  onomkeerbaar

## Adiabatische toestandsver.

↳ praktische, oneenkeerbare en niet-evenwichtige toestandsverandering waarbij geen (gewilde) warmtewisseling optreedt.

$1 \rightarrow 2$  (adiab.)

$$\int_1^2 \frac{dq}{T} = 0 \quad \text{of} \quad P_2 > P_1$$

⇒ reek toest. zonder warmtewisseling  $\rightarrow$  entropiestijging

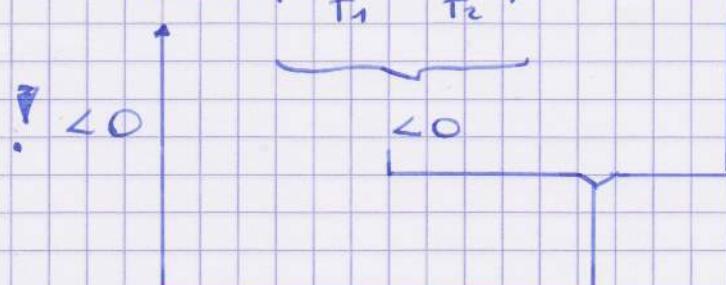
(b)



met  $T_1 > T_2$

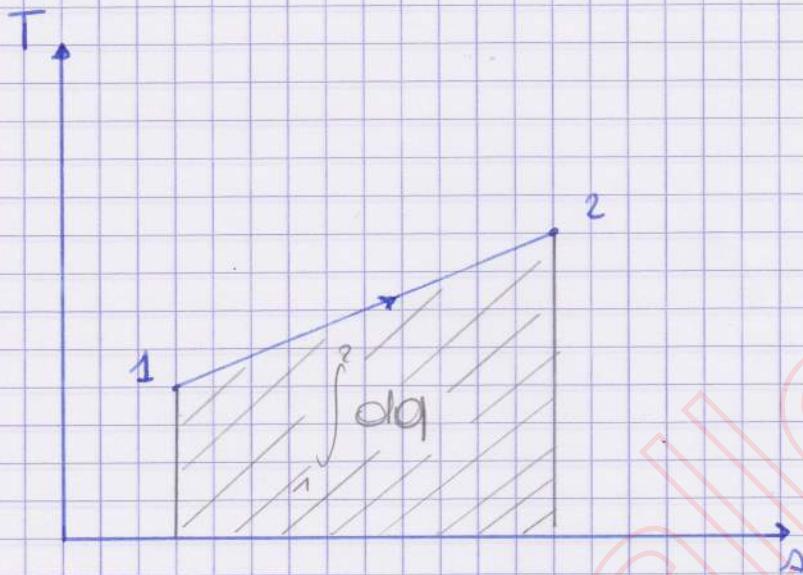
$$\Delta S = \underbrace{\Delta S_{\text{rev}}}_{=0} + \underbrace{\Delta S_{\text{irr}}}_{>0}$$

$$\Delta S_{\text{irr}} = q_{\text{adib}} \left( \frac{1}{T_1} - \frac{1}{T_2} \right) > 0$$



$$\Delta S_{\text{irr}} = \Delta S_a + \Delta S_b$$

# Het ( $T,s$ ) diagram



$$ds = \frac{dq}{T}$$

$$dq = T ds$$

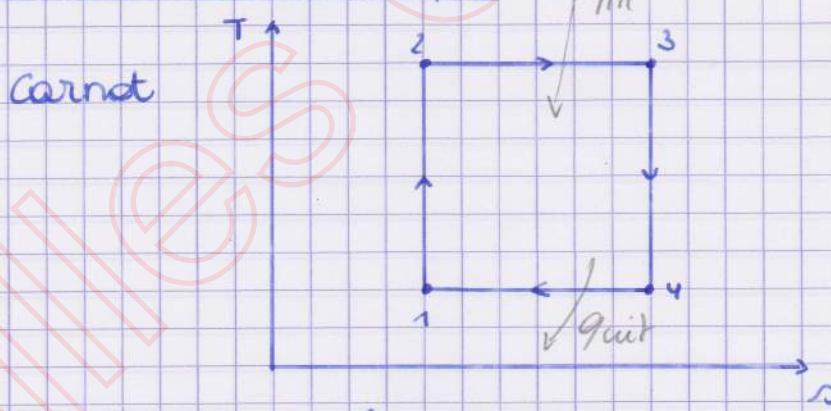
$$= T(ds_{rev} + ds_{irr})$$

$$\downarrow ds_{irr} = 0$$

$$\int dq = q_{1 \rightarrow 2} = \int_1^2 T ds$$

## Polytrope toest.

Isothermen en isentropen



$$q_{in} = q_{2 \rightarrow 3} = \int_2^3 T_H \cdot ds = T_H (\delta_3 - \delta_2)$$

$$q_{out} = q_{4 \rightarrow 1} = \int_4^1 T_L \cdot ds = T_L (\delta_1 - \delta_4)$$

$$\eta_{th}^c = 1 - \frac{|q_{out}|}{q_{in}} = 1 - \frac{T_L (\delta_4 - \delta_1)}{T_H (\delta_3 - \delta_2)}$$

$$\eta_{th}^c = 1 - \frac{T_L}{T_H}$$

## Isobaren

$$ds = Cp \frac{dT}{T} - Rg \frac{dp}{p}$$

f isobaar

$$\Delta s = Cp \ln$$

$$\left( \frac{\Delta s}{C_p} \right)$$

$$T = T_1 e^{\Delta s}$$

ligging hver et haar.

- $T = ct.$

$$\Delta s = -Rg \ln \left( \frac{P_b}{P_a} \right)$$

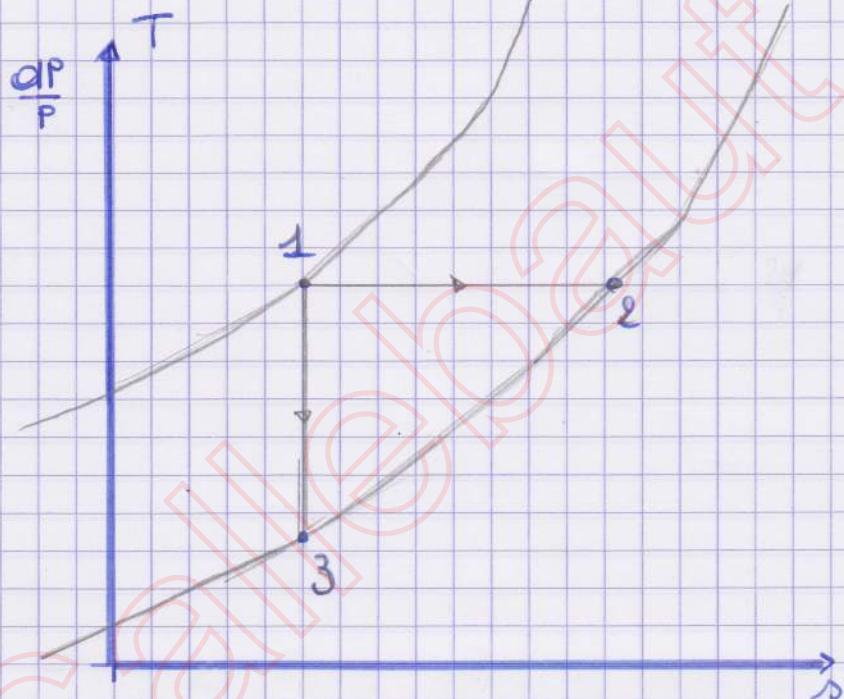
$\underbrace{> 0}_{< 0}$

$$\frac{P_b}{P_a} < 1$$

- $\frac{T}{P} = ct.$

$$\Delta s = \underbrace{C_p \ln \left( \frac{T_3}{T_1} \right)}_{= 0} - \underbrace{Rg \ln \left( \frac{P_b}{P_a} \right)}_{< 0}$$

$$\frac{P_b}{P_a} < 1$$



P<sub>a</sub>

P<sub>b</sub>

## Isochoren

$$ds = C_V \frac{dT}{T} + Rg \frac{dv}{v}$$

↳ isochor

$$ds = C_V \frac{dT}{T} \quad (\Delta s / \omega)$$

$$\Rightarrow T = T_1 \cdot c$$

ligging:

- $T = ct.$

$$\Delta s = Rg \ln\left(\frac{V_2}{V_1}\right)$$

$$> 0 \rightarrow > 0$$

$$\frac{V_2}{V_1} > 1$$

- $\Delta s = ct.$

$$\Delta s = \underbrace{C_V \ln\left(\frac{T_3}{T_1}\right)}_{=0} + \underbrace{Rg \ln\left(\frac{V_3}{V_1}\right)}_{<0 \rightarrow >0}$$

$$\frac{V_3}{V_1} > 1$$

## Onderlinge ligging

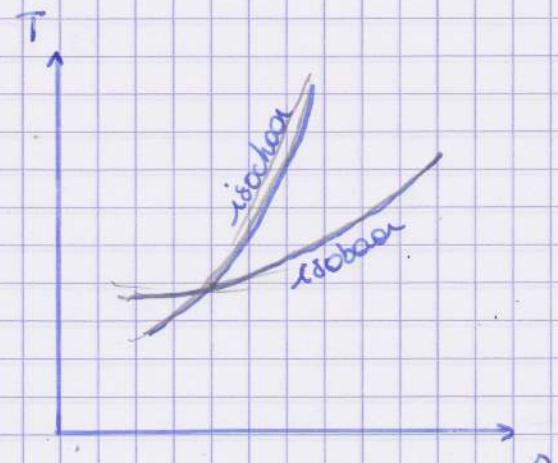
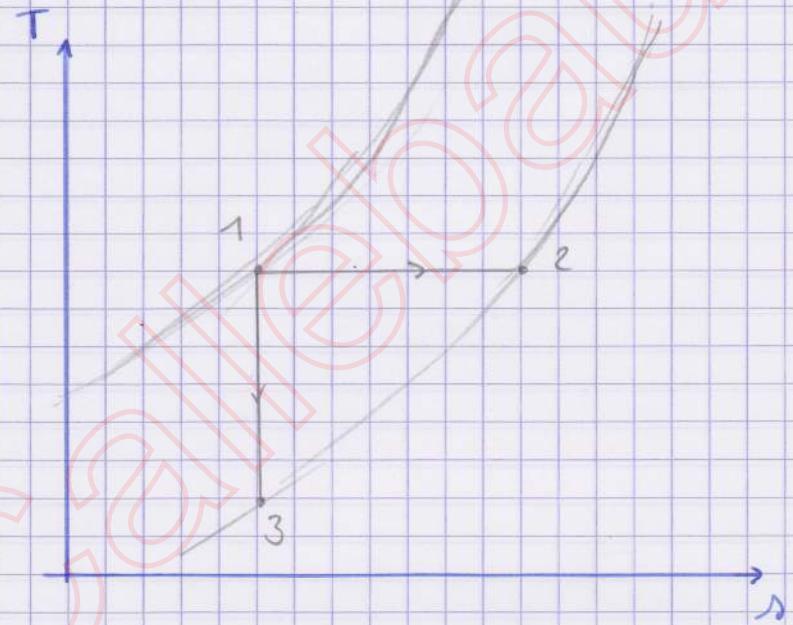
isobar:  $ds = C_p \frac{dT}{T}$

$$\hookrightarrow dT = \frac{T}{C_p} ds$$

isochor:  $ds = C_V \frac{dT}{T}$

$$\hookrightarrow dT = \frac{C_V}{T} ds$$

mits  $C_p = C_V + Rg \rightarrow C_p > C_V$



## Willekeurige polytroopen

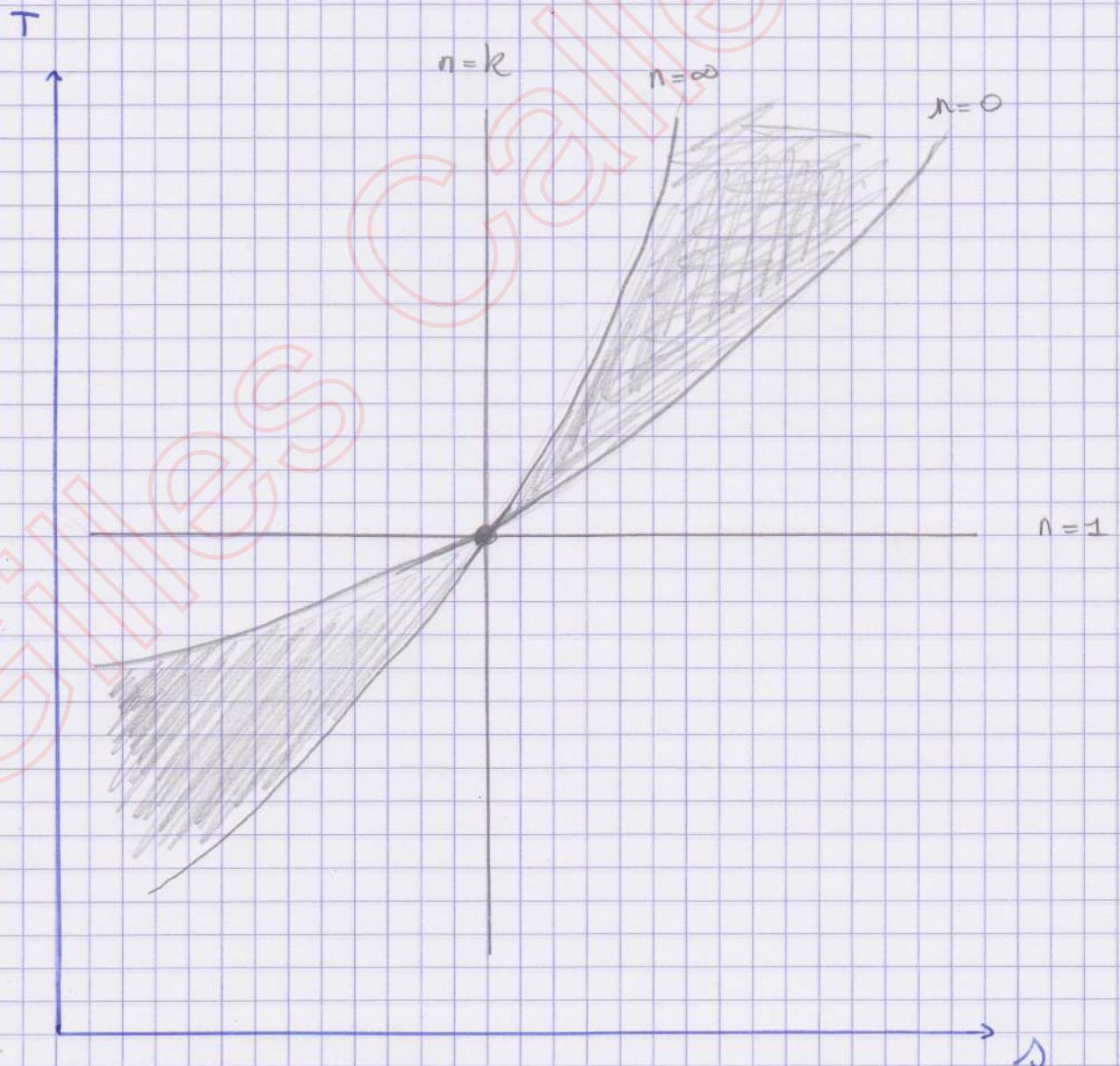
$$ds = c \frac{dT}{T}$$

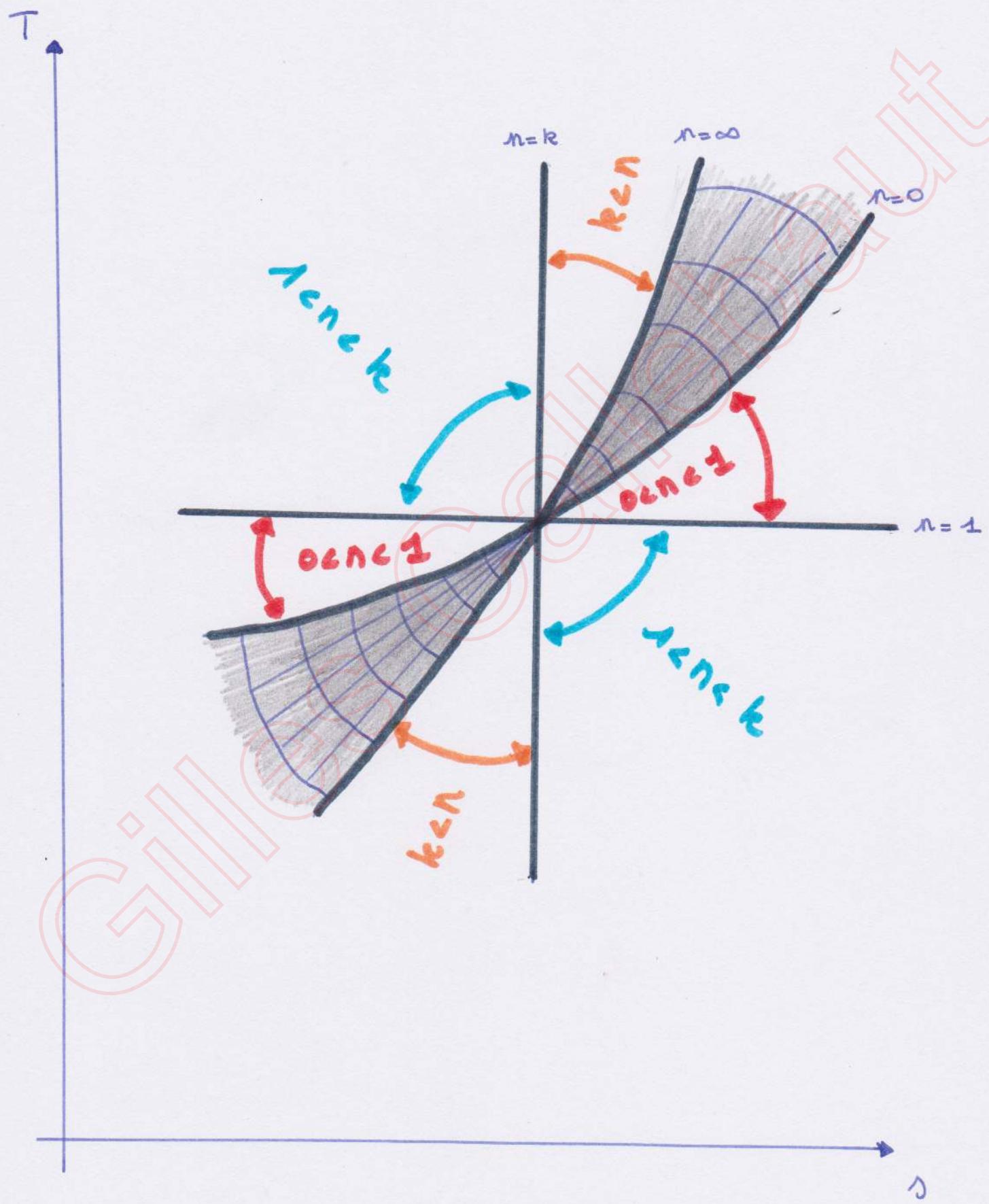
$$\Delta s = c \ln\left(\frac{T_2}{T_1}\right)$$

$$\text{met } n = \frac{C_p - c}{C_v - c}$$

$$\hookrightarrow c = \frac{C_v(n-k)}{(n-1)}$$

$$\Delta s = C_v \left[ \frac{(n-k)}{(n-1)} \right] \ln \left( \frac{T_2}{T_1} \right)$$

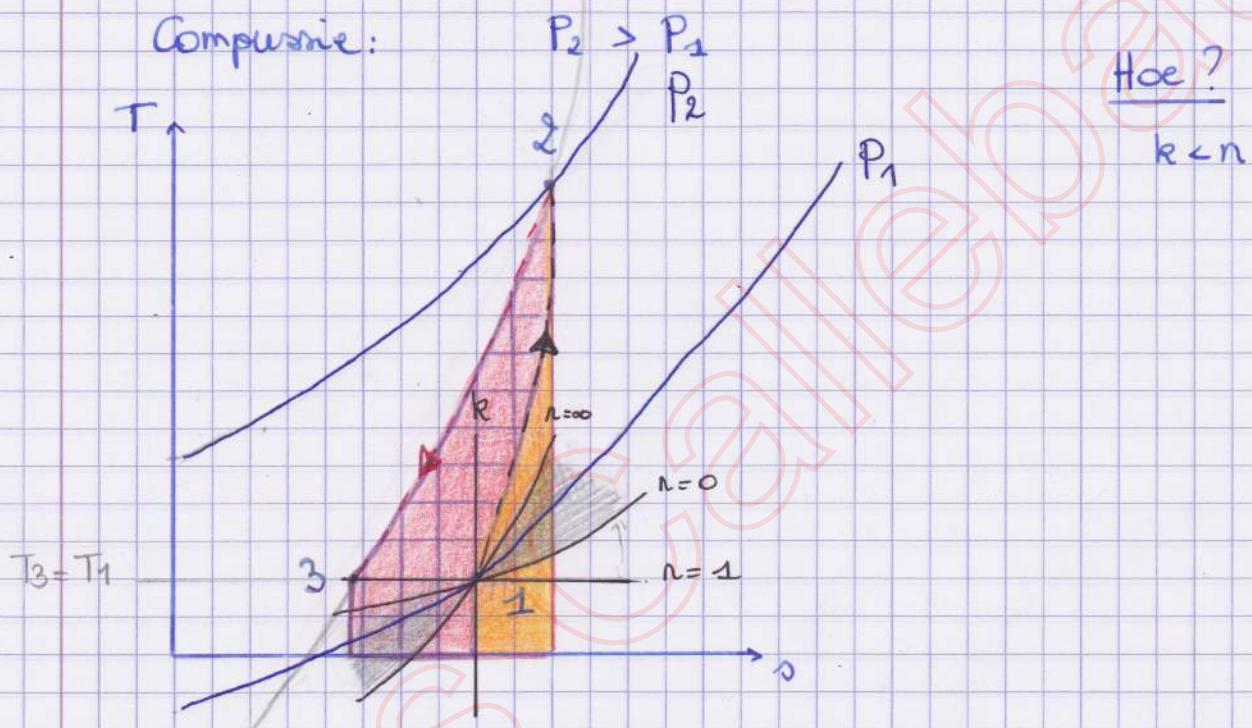




# Arbeit in (T,s) diagram

Volume - Arbeit

Comparative:



$$HWI: q_{1 \rightarrow 2} = (U_2 - U_1) + W_{1 \rightarrow 2}$$

$$W_{1 \rightarrow 2} = q_{1 \rightarrow 2} + (U_1 - U_2)$$

<0      >0      <0

Fiktif prozess 2 → 3:

↪ ? welk prozess → isochor →  $W_{2 \rightarrow 3} = 0$

↪ ? (3) eindeutig →  $U_3 = U_1 \rightarrow T_1 = T_3$

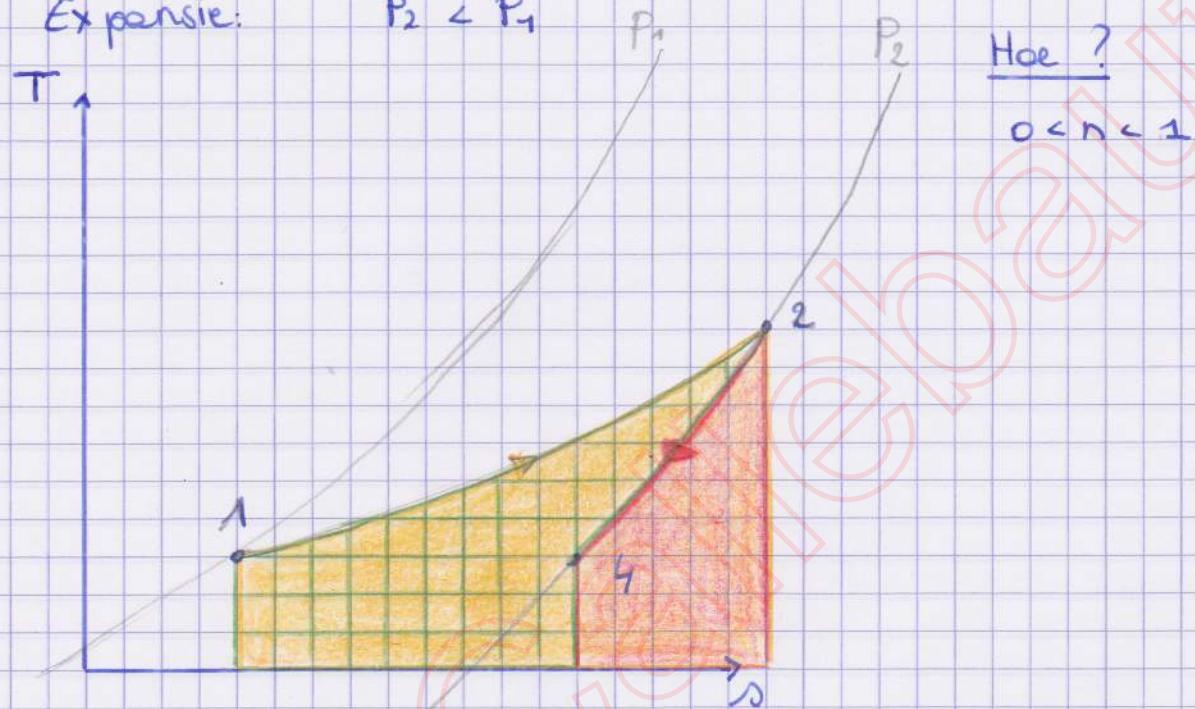
$$q_{2 \rightarrow 3} = (U_3 - U_2) + W_{2 \rightarrow 3}$$

$$q_{2 \rightarrow 3} = (U_1 - U_2)$$

# Technische arbeid

Expansie:

$$P_2 < P_1$$



Hoe?

$$0 < n < 1$$

HWI:

$$q_{1 \rightarrow 2} = (h_2 - h_1) + w_{t1 \rightarrow 2}$$

$$w_{t1 \rightarrow 2} = q_{1 \rightarrow 2} + (h_1 - h_2)$$

Fictief proces  $2 \rightarrow 4$ :

$$\hookrightarrow w_{t2 \rightarrow 4} = 0 \text{ als isobar}$$

$$\hookrightarrow h_4 = h_1 \leftrightarrow T_4 = T_1 \text{ (ideaal gas)}$$

$$q_{2 \rightarrow 4} = (h_4 - h_2) + w_{t2 \rightarrow 4}$$

$$q_{2 \rightarrow 4} = (h_1 - h_2)$$

# ISENTROOP RENDEMENT

Expansie:  $P_2 < P_1$

$$\text{HWI: } q_{1 \rightarrow 2} = (h_2 - h_1) + w_{t,1 \rightarrow 2}$$

$\underbrace{\phantom{0}}_{=0}$

$$(h_2 - h_1) = w_{t,1 \rightarrow 2}$$

$$\text{met } (h_2 - h_1) = C_p(T_2 - T_1)$$

HWII:

Omkeerbaar (ideaal)

$$\Delta s = \Delta s_{\text{rw.}} + \Delta s_{\text{irr.}}$$

$\underbrace{=0}_{\text{isentroop}} \quad \underbrace{=0}_{\text{irr.}} \quad \underbrace{=0}_{\text{irr.}}$

$$\Delta s_1 = \Delta s_2$$

Inomkeerbaar (reëel)

← Adiabaat

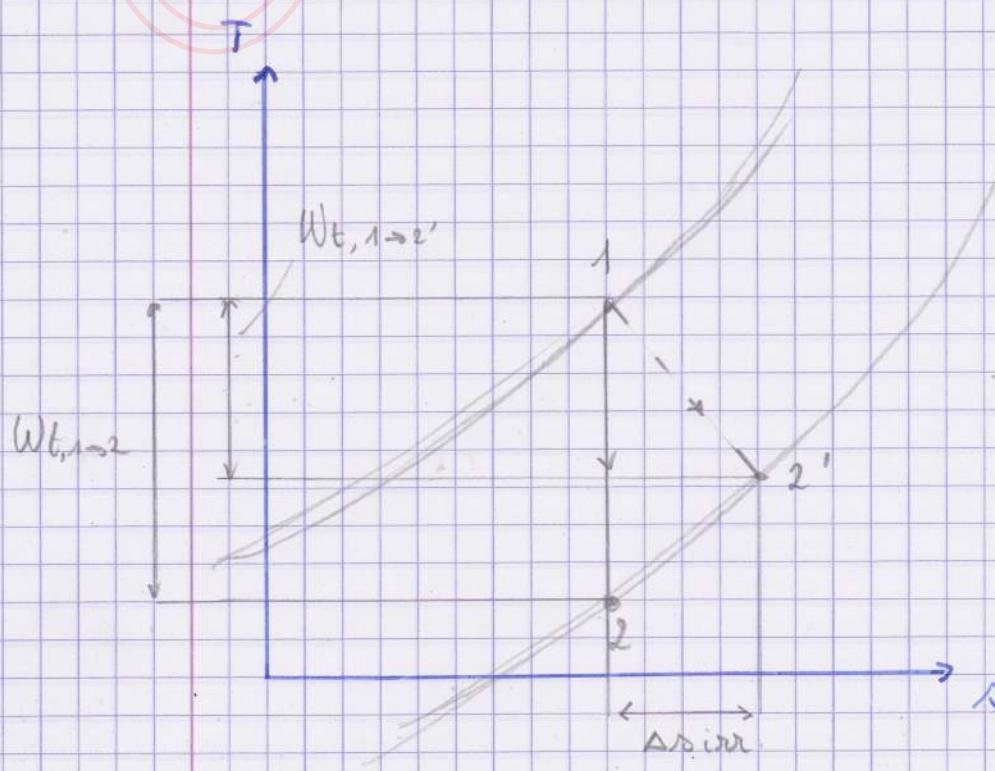
$$\Delta s = \Delta s_{\text{rw.}} + \Delta s_{\text{irr.}}$$

$\neq 0 \quad = 0 \quad \neq 0$

$$\Delta s_2' > \Delta s_1$$

$$\rightarrow \eta_a = \frac{w_{t,1 \rightarrow 2}'}{w_{t,1 \rightarrow 2}} < 1$$

$$\eta_{\text{is.}} = \frac{(T_1 - T_2')}{(T_1 - T_2)}$$



# H8: Kringprocessen met ideale gassen

Ter vereenvoudiging is aangenomen dat het gebruikte fluïdum zich als een ideaal gas gedraagt en dat alle toestandsver. omkeerbaar en dus evenwichtig verlopen.

Compressieverhouding:

$$\pi_v = \rho = \frac{V_{\min}}{V_{\max}} = 1 + \frac{\Delta V}{V_{\min}}$$

met  $\Delta V = \frac{\pi D^2}{4} \cdot n_L$  slaglengte

Referentie energie:

$$RgT_1 \rightarrow q_h^* = \frac{q_{in}}{RgT_1} [-]$$

Arbeid:

$$\frac{W_{net}}{RgT_1} = \int d\omega^* = \int dq^* \\ = \frac{q_{in} - q_{out}}{RgT_1}$$

$$W_{th}^* = q_h^* - |q_{el}^*|$$

Rendement:

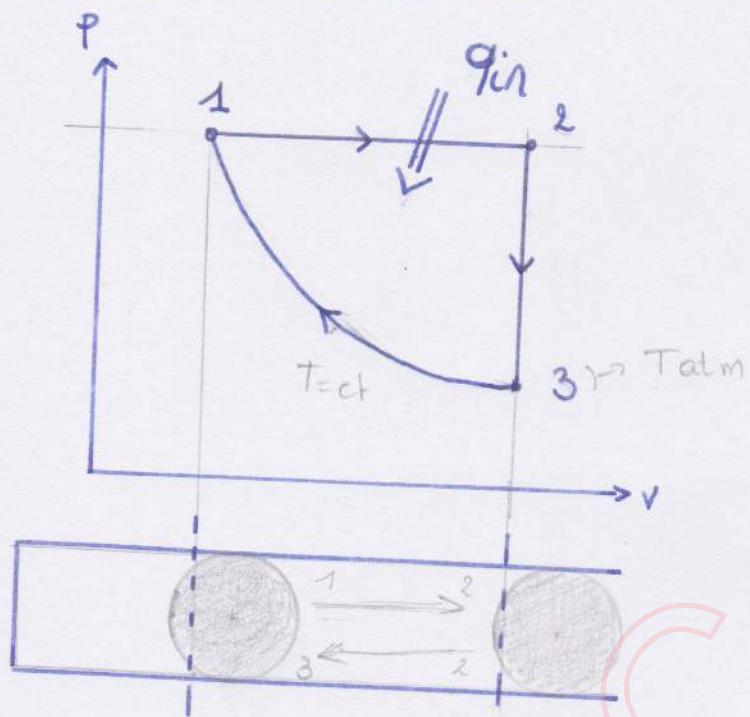
$$\eta_{th} = \frac{W_{net}}{q_{in}} = \frac{W_{th}^*}{q_h^*}$$

Druk:

$$\bar{P} = \frac{W_{th}}{\Delta V} = \frac{W_{th}^*}{\Delta V / RgT_1} \rightarrow$$

$$\frac{\bar{P}}{P_1} = \frac{W_{th}^*}{\frac{P_1}{RgT_1} \cdot \Delta V}$$

# Vacuum-motor



①

$$P_1 = P_{atm}$$

$$V_1 = V_1$$

$$T_1 = T_{atm}$$

$$C = C_p$$

$$n = 0$$

$$P_2 = P_1$$

$$V_2 = \pi_v V_1$$

$$T_2 = \pi_v T_1$$

$$C = \infty$$

$$n = 1$$

②

$$C = C_V$$

$$n = 0$$

$$P_3 = \frac{P_{atm}}{\pi_v}$$

$$V_3 = V_2$$

$$T_3 = T_1$$

③

① → ②

$$q = C_p(T_2 - T_1) = C_p T_1 (\pi_v - 1)$$

$$> 0 \Rightarrow q_{in}$$

② → ③

$$q = C_v(T_3 - T_2) = C_v T_1 (1 - \pi_v)$$

$$< 0$$

③ → ①

$$q = P_1 V_1 \ln\left(\frac{V_1}{V_3}\right)$$

$$< 0$$

$$q_h^* = \frac{q_{in}}{Rg T_1} = \frac{C_p T_1 (\pi_v - 1)}{Rg T_1}$$

$$\therefore \frac{C_p}{Rg} = \frac{C_p}{C_p - C_v} = \frac{k}{k-1}$$

$$q_h^* = \frac{k}{k-1} (\pi_v - 1)$$

$$|q_e^*| = \frac{|q_{in}|}{Rg T_1} \Rightarrow \frac{1}{k-1} (\pi_v - 1) + \ln(\pi_v) = |q_e^*|$$

$$W_{th}^* = q_h^* - |q_e^*| = \frac{k}{k-1} (\pi_v - 1) - \frac{1}{k-1} (\pi_v - 1) - \ln(\pi_v)$$

$$W_{th}^* = (\pi_v - 1) - \ln(\pi_v)$$

$$\eta_{th} = \frac{W_{th}^*}{q_h^*}$$

$$\frac{\bar{P}}{P_1} = \frac{W_{th}^*}{P_1 / Rg T_1 \cdot \Delta V} = \frac{W_{th}^*}{P_1 / Rg T_1 \cdot (\pi_v - 1) V_1} \Rightarrow$$

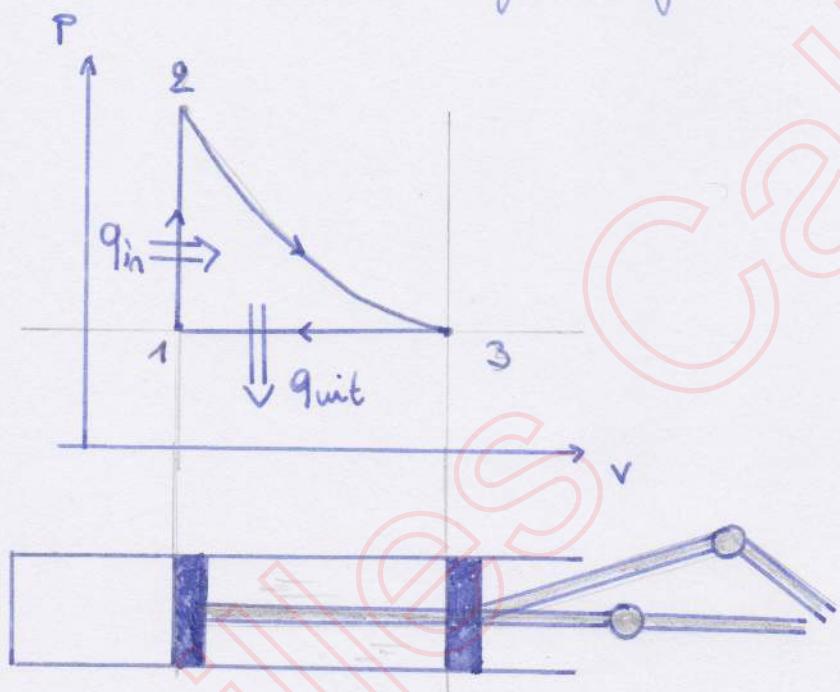
$$\frac{\bar{P}}{P_1} = \frac{W_{th}^*}{\pi_v - 1}$$

# Adenius kringproces

① → ② isochore verhitting

② → ③ adiabatische expansie

③ → ① isobare afkoeling



① →

$$P_1 = P_{atm}$$

$$\begin{matrix} n = \infty \\ c = c_V \end{matrix}$$

$$V_1 =$$

$$T_1 = T_{atm}$$

② →

$$P_2 = P_3 \left( \frac{V_3}{V_2} \right)^k$$

$$\begin{matrix} n = k \\ c = 0 \\ q = 0 \end{matrix}$$

$$V_2 = V_1$$

$$T_2 = T_1 (r_V)^k$$

$$P_3 = P_1$$

$$V_3 = r_V V_1$$

$$T_3 = T_1 \cdot r_V$$

$$\begin{matrix} n = 0 \\ c = c_p \end{matrix}$$

$$P_2 \cdot V_2^k = P_3 \cdot V_3^k$$

$$\frac{T_3}{V_3} = \frac{T_1}{V_1}$$

$$T_2 = T_3 \cdot \left( \frac{V_3}{V_2} \right)^{k-1}$$

① → ②

$$q_{in} = c_V (T_2 - T_1)$$

$$q_{in}^* = \frac{q_{in}}{Rg T_1}$$

$$q_{in}^* = \frac{1}{k-1} (r_V^k - 1)$$

② → ③

$$q = 0$$

③ → ①

$$|q_{uit}| = c_p (T_3 - T_1) \quad |q_e^*| = \frac{|q_{uit}|}{Rg T_1} \Rightarrow |q_e^*| = \frac{k}{k-1} (r_V - 1)$$

$$W_{th}^* = q_h^* - |q_e^*|$$

$$\eta_{th} = 1 - \frac{|q_{uit}|}{q_{in}}$$

$$\eta_{th} = 1 - \frac{k (r_V - 1)}{(r_V)^k - 1}$$

$$\frac{\bar{P}}{P_1} = \frac{W_{th}^*}{\left( \frac{P_1 \cdot 0V}{Rg T_1} \right)} = \frac{W_{th}^*}{\frac{P_1 V_1}{Rg T_1} (r_V - 1)}$$

$$\frac{\bar{P}}{P_1} = \frac{W_{th}^*}{r_V - 1}$$

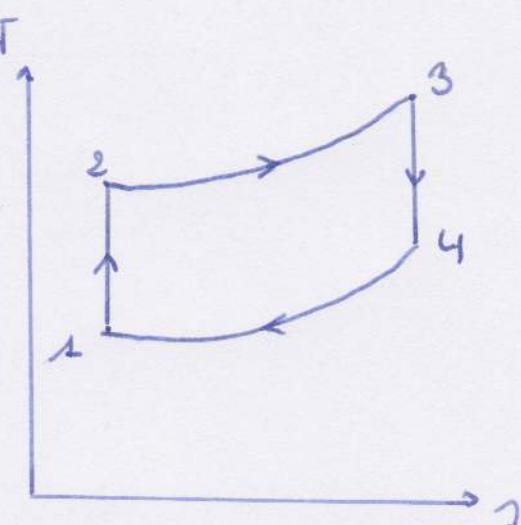
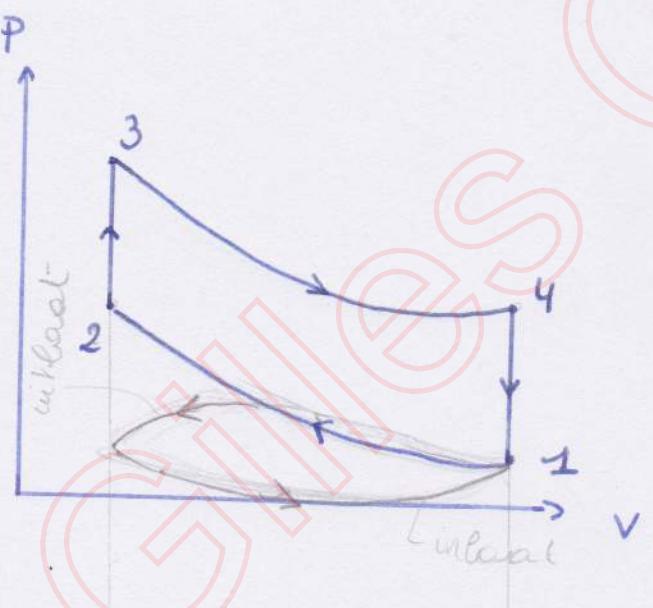
# Otto - cyclus

① → ② Isentrope compressie

② → ③ Isochorre warmte toevoer

③ → ④ Isentrope expansie

④ → ① Isochorre warmte afvoer



2 takt  $\rightarrow$  per 2 slagen arbeid

4 takt  $\rightarrow$  per 4 slagen arbeid

$\hookrightarrow$  extra energie  $\rightarrow$  in-  $\times$  uitlaten stoffen

①

$$P_1 = P_{\text{atm}}$$

$$V_1 =$$

$$T_1 = T_{\text{atm}}$$

$$\begin{array}{l} n=k \\ c=0 \\ q=0 \end{array}$$

②

$$P_2 = P_1 (\gamma_v)^k$$

$$V_2 = \frac{V_1}{\gamma_v}$$

$$T_2 = T_1 (\gamma_v)^{k-1}$$

$$n=\infty$$

$$c=c_v$$

$$q = c_v (T_1 - T_4)$$

$$\begin{array}{l} n=\infty \\ c=c_v \\ q = c_v (T_3 - T_2) \end{array}$$

$$P_3 = P_1 (\gamma_v \frac{T_3}{T_1})$$

$$V_3 = V_2$$

$$T_3 = T_1 \left[ (\gamma_v)^{k-2} + (k-1) q_h^* \right]$$

$$\frac{T_4}{T_1} = \frac{T_4}{T_3} \cdot \frac{T_3}{T_1}$$

$$= (\gamma_v)^{1-k} \left( \frac{T_3}{T_1} \right)$$

$$P_4 V_4^k = P_3 V_3^k$$

$$P_1 V_1^k = P_2 V_2^k$$

$$T_1 V_1^{k-1} = T_2 V_2^{k-1}$$

$$T_3 = T_2 + \frac{q_h}{c_v}$$

$$\frac{T_3}{T_1} = (\gamma_v)^{k-1} + (k-1) q_h^*$$

$$\frac{P_3 V_3}{T_3} = \frac{P_2 V_2}{T_1}$$

$$\begin{array}{l} n=k \\ c=0 \\ q=0 \end{array}$$

④

$$P_4 = P_3 \cdot \gamma_v^{-k}$$

$$V_4 = V_1$$

$$T_4 = T_3 \cdot \gamma_v^{1-k}$$

$$W_{th}^* = q_h^* - 19e^*$$

$$\eta_{th}^* = 1 - \frac{19e}{q_{in}} = 1 - \frac{C_V(T_4 - T_1)}{C_V(T_3 - T_2)} = 1 - \frac{T_1}{T_2} \frac{\left(\frac{T_4}{T_1} - 1\right)}{\left(\frac{T_3}{T_2} + 1\right)}$$

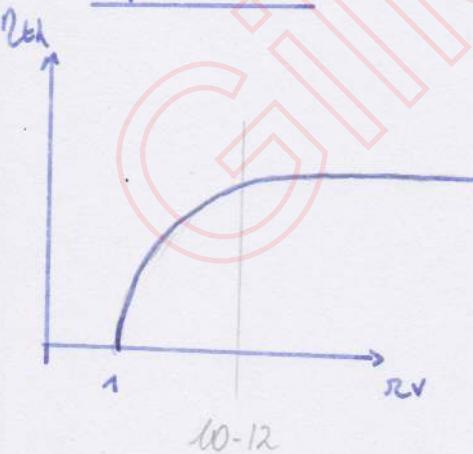
$$\eta_{th}^* = 1 - (\pi_v)^{1-k}$$

$$\begin{aligned} \frac{T_2}{T_1} &= \pi_v^{k-1} \\ \frac{T_3}{T_4} &= \pi_v^{k-1} \end{aligned} \quad \Rightarrow \quad \frac{T_2}{T_1} = \frac{T_3}{T_4} \Rightarrow \frac{T_4}{T_1} = \frac{T_3}{T_2}$$

$$\frac{\bar{P}}{P_1} = \frac{W_{th}}{P_1 \cdot \Delta V} = \frac{W_{th}^*}{\frac{P_1 V_1}{k \pi_v} \left(1 - \frac{V_4}{V_1}\right)}$$

$$\frac{\bar{P}}{P_1} = \frac{W_{th}^*}{\pi_v - 1} \cdot \pi_v$$

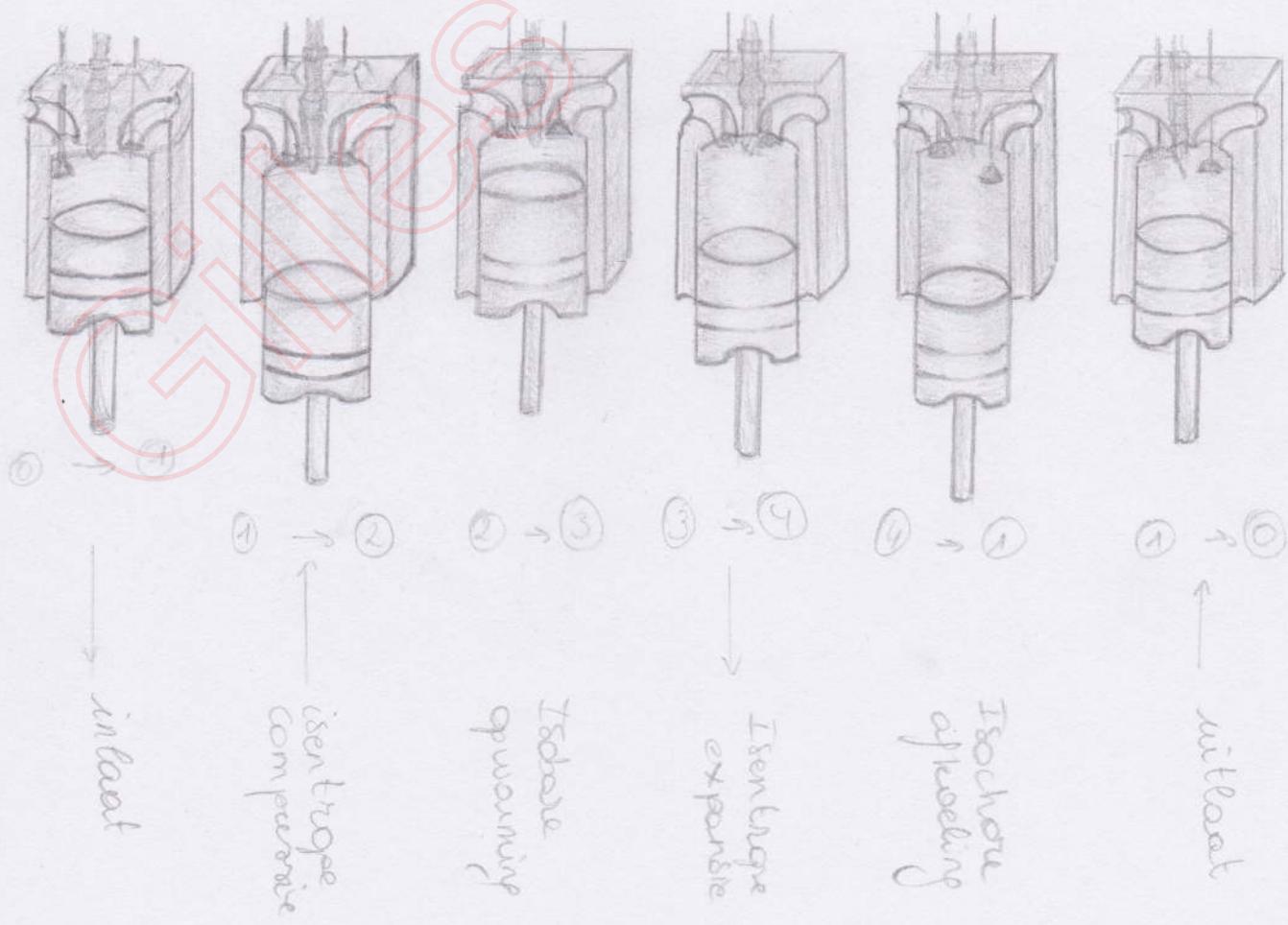
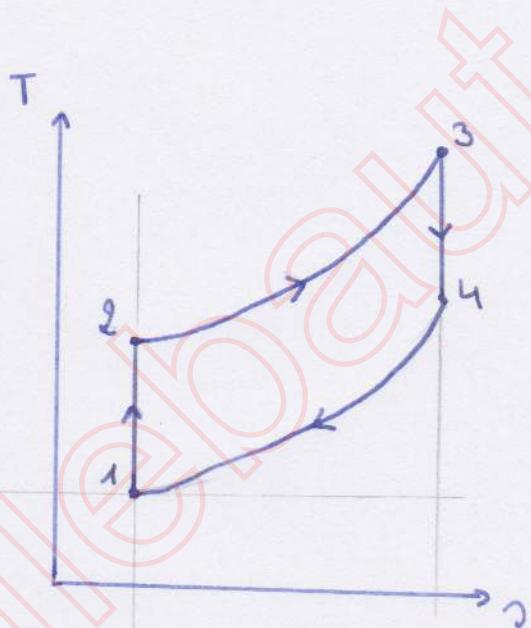
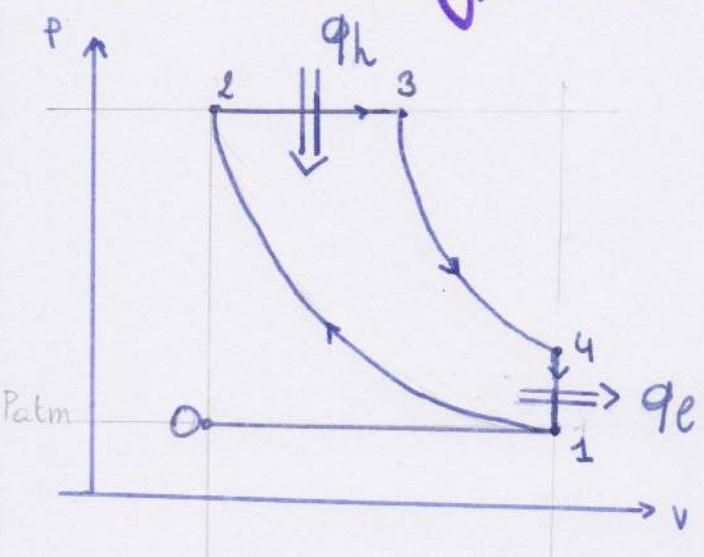
Opvallend:



bij 10 à 12 → comp. verh.  
het proces is v. materiaal  
→ naderen ideaal proces

- De buiksteekte van materiaal zal de max. druk bepalen.
- $T_4$  (= uitlaatgastemp.) mag niet te hoog zijn, anders milieuschade.  
Maar ook niet te laag, anders onvolledige verbranding.

# Diesel kringproces



①

$$P_1 = P_{atm}$$

$$V_1 =$$

$$T_1 = T_{atm}$$

$$\begin{array}{l} n=k \\ c=0 \\ q=0 \end{array}$$

$$② \quad P_2 = P_1 (\gamma_v)^{k-1}$$

$$V_2 = \frac{V_1}{\gamma_v}$$

$$T_2 = T_1 (\gamma_v)^{k-1}$$

$$T_3 = T_2 + \frac{q_{in}}{c_p}$$

$$\begin{aligned} \frac{T_3}{T_1} &= \frac{T_2}{T_1} + \frac{q_{in}}{c_p T_1} \cdot \frac{R_g}{R_g} \\ &= (\gamma_v)^{k-1} + \frac{k-1}{k} \cdot q_h^* \end{aligned}$$

$$\frac{T_3}{V_3} = \frac{T_2}{V_2}$$

$$\frac{V_3}{V_2} = \frac{T_3}{T_2} = \frac{T_3}{T_1} \cdot \frac{T_1}{T_2}$$

$$= 1 + \frac{k-1}{k} \cdot (\gamma_v)^{1-k} \cdot q_h^*$$

$$\begin{array}{l} n=0 \\ c=c_p \\ q=0 \end{array}$$

$$③ \quad q = c_p(T_3 - T_2) \\ = q_{in}$$

$$P_3 = P_2$$

$$V_3 = \left(1 + \frac{k-1}{k} (\gamma_v)^{1-k} \cdot q_h^*\right) \cdot V_2$$

$$T_3 = \left((\gamma_v)^{k-1} + \frac{k-1}{k} \cdot q_h^*\right) \cdot T_1$$

$$\begin{array}{l} n=k \\ c=0 \\ q=0 \end{array}$$

$$④ \quad P_4 = P_1 \left(\frac{V_3}{V_2}\right)^k$$

$$V_4 = V_1$$

$$T_4 = T_1 \left(\frac{V_3}{V_2}\right)^k$$

$$|q_e^*| = \frac{|q_{in}|}{R_g T_1}$$

$$= \frac{C_V}{R_g} \left(\frac{T_1}{T_4} - 1\right)$$

$$\begin{array}{l} n=0 \\ c=C_V \\ q=q_{in} (T_1 - T_4) \\ = q_{in} \end{array}$$

$$W_{th}^* = q_h^* - |q_e|^*$$

$$\eta_{th} = 1 - \frac{|q_{uit}|}{q_{in}} = 1 - \frac{C_V(T_4/T_1 - 1) \cdot T_1}{C_p(T_b/T_2 - 1) \cdot T_2}$$

$$\eta_{th} = 1 - \frac{1}{k} \left( \frac{(v_3/v_2)^k - 1}{(v_3/v_2) - 1} \right) \cdot \frac{1}{(\lambda_v)^{k-1}}$$

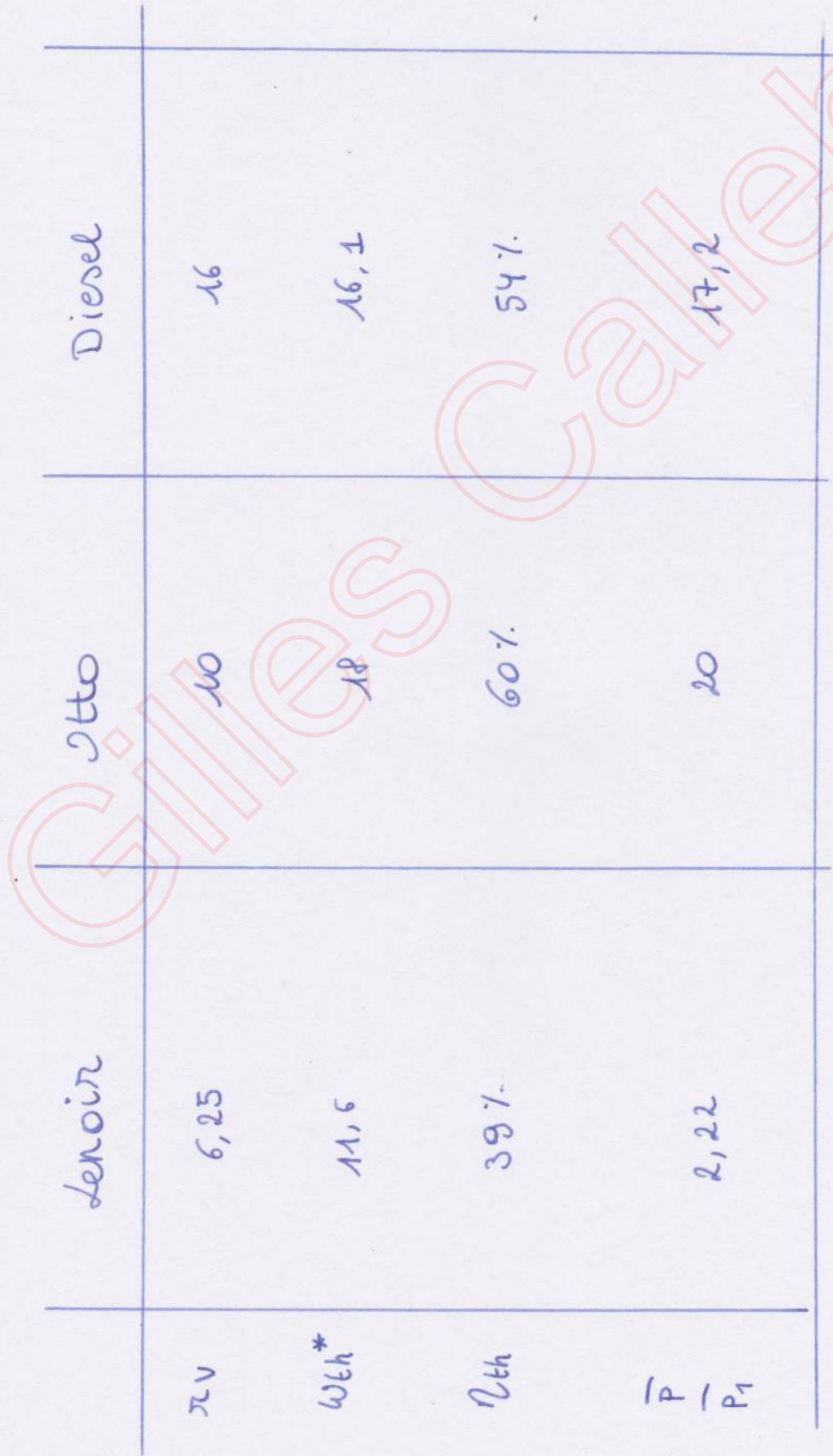
$> 1$ , want  $\frac{v_3}{v_2} > 1$

$\hookrightarrow \underline{\eta_{th, \text{diesel}}} < \underline{\eta_{th, \text{otto}}}$

$$\frac{\bar{P}}{P_1} = \frac{W_{th}}{P_{1, \text{DV}}} = \frac{W_{th} / (R_g \cdot T_1)}{P_1 (v_1 - v_2) / (R_g \cdot T_1)} = \frac{W_{th}^*}{\frac{P_1 v_1}{R_g \cdot T_1} \left( 1 - \frac{1}{\lambda_v} \right)}$$

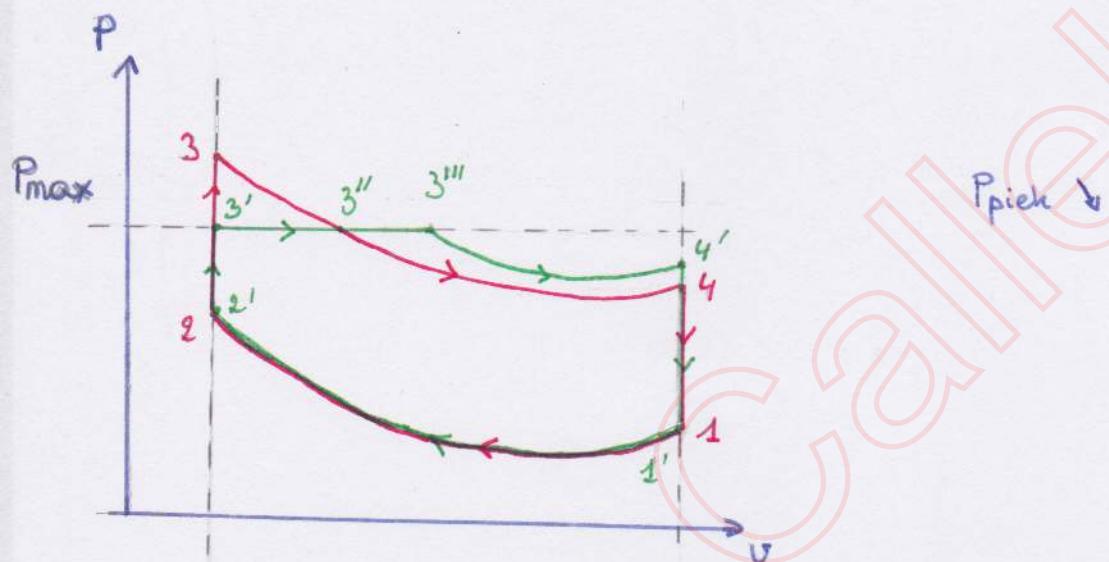
$$\frac{\bar{P}}{P_1} = \frac{R_v \cdot W_{th}^*}{R_v - 1}$$

$$Stel : q_{h^*} = 30 \quad ; \quad k = 1,4$$



## Duaal kringproses

# Otto - Dual



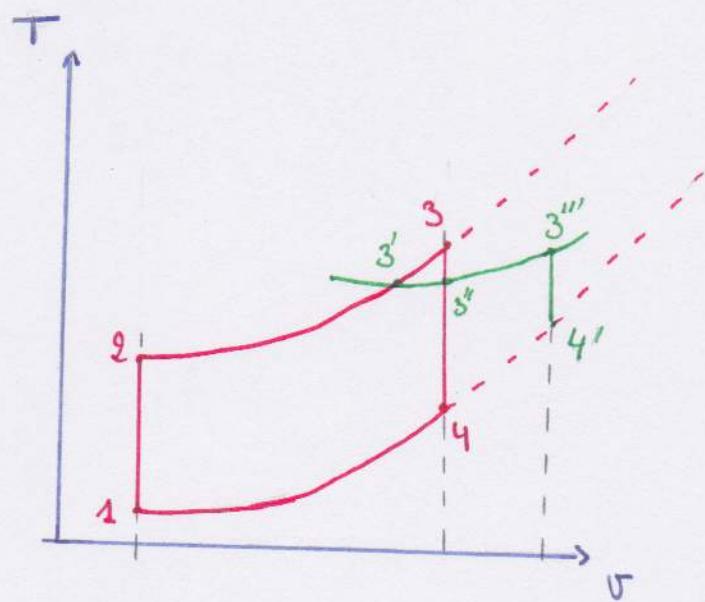
$$q = ct.$$

$\hookrightarrow$  opp ondu grafiek = ct.

$\hookrightarrow 3''$

$4' \rightarrow$  verlengde  $q_{1+4} 4' \alpha$

$T_3'' \rightarrow 4' = ct.$



$$q_h^*, \text{otto} = q_h^*, \text{dual}$$

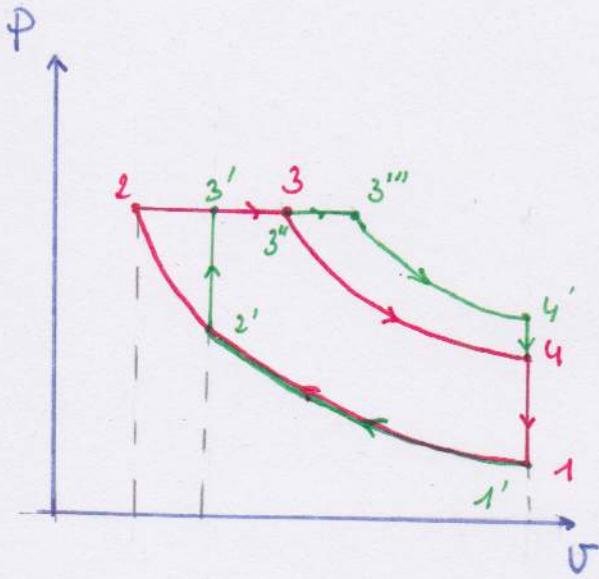
$$\eta_{th, \text{otto}} > \eta_{th, \text{diesel}}$$

19 uit, otto! < 19 uit, dwaal!

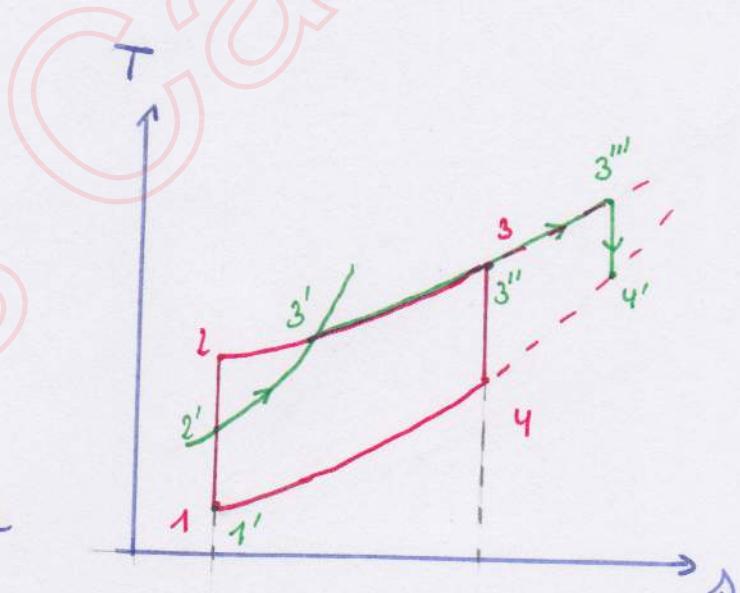
$$C_V(T_4 - T_1) < C_V(T_4' - T_1)$$

$$\rightarrow T_4 < \overline{T_4'}$$

## Diesel - Duaal



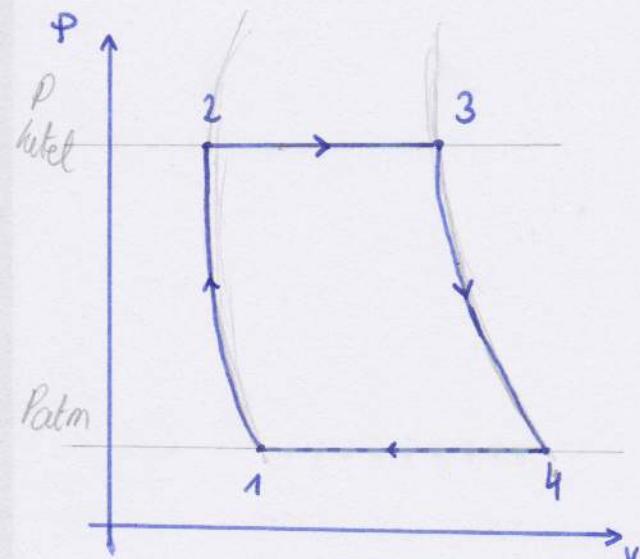
$\pi v \downarrow$



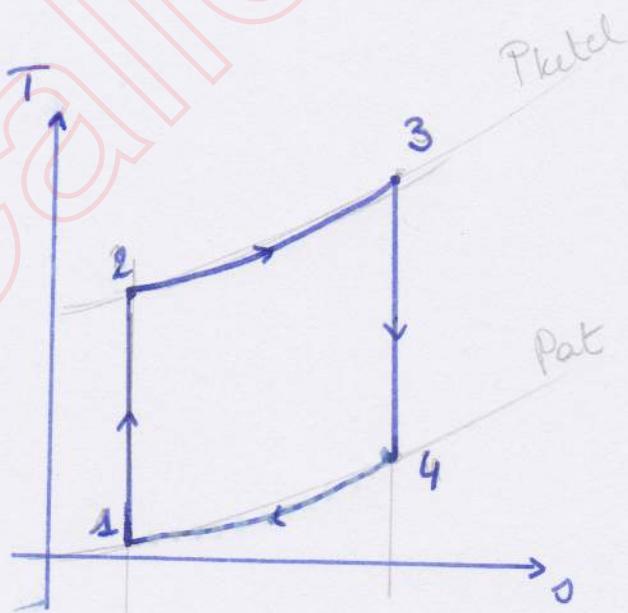
$$q_{h^*}^{\text{diesel}} = q_{h^*}^{\text{duaal}}$$

$$\eta_{th, \text{diesel}} > \eta_{th, \text{duaal}}$$

# Hete lucht motor van Joule



$$\epsilon = \frac{P_{\text{hete}}}{P_{\text{atm}}} = \frac{P_2}{P_1}$$



①

$$P_1 = P_{\text{atm}}$$

$$V_1 =$$

$$T_1 = T_{\text{atm}}$$

$$\begin{array}{l} n=k \\ c=0 \\ q=0 \end{array}$$

$$P_2 = E P_1$$

$$V_2 = V_1 E^{-1/k}$$

$$* \nearrow T_2 = T_1 E^{(k-1)/k}$$

$$\begin{array}{l} n=0 \\ c=C_P \\ q=C_P(T_3 - T_1) \end{array}$$

$$P_3 = P_2$$

$$V_3 = V_2 \frac{T_3}{T_2}$$

$$* \nearrow T_3 = T_2 + \frac{q_{in}}{C_P}$$

$$* T_3 < T_{\max}$$

*material  
limiet*

$$\begin{array}{l} n=k \\ c=0 \\ q=0 \end{array}$$

④

$$P_4 = P_1$$

$$V_4 = V_3 E^{-1/k}$$

$$T_4 = T_3 E^{(1-k)/k}$$

$$\begin{array}{l} n=0 \\ c=C_P \\ q=C_P(T_1 - T_4) \\ \therefore q_{out} \end{array}$$

$$W_{net} = q_{in} - 19_{init}$$

$$W_{net} = Cp [T_3 + T_1 - T_2 - T_4]$$

$$\begin{aligned}\eta_{th} &= 1 - \frac{19_{init}}{q_{in}} = 1 - \frac{(T_4 - T_1)}{(T_3 - T_2)} \\ &= 1 - \frac{T_1}{T_2} \frac{\left(\frac{T_4}{T_1} - 1\right)}{\left(\frac{T_3}{T_2} - 1\right)} \\ &\quad \downarrow \quad \frac{T_2}{T_1} = e^{(k-1)/k} = \frac{T_3}{T_4}\end{aligned}$$

$$= 1 - \frac{T_1}{T_2}$$

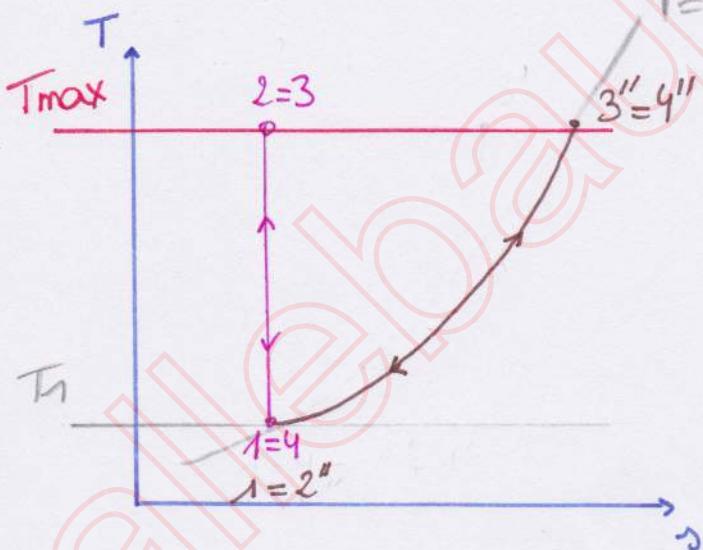
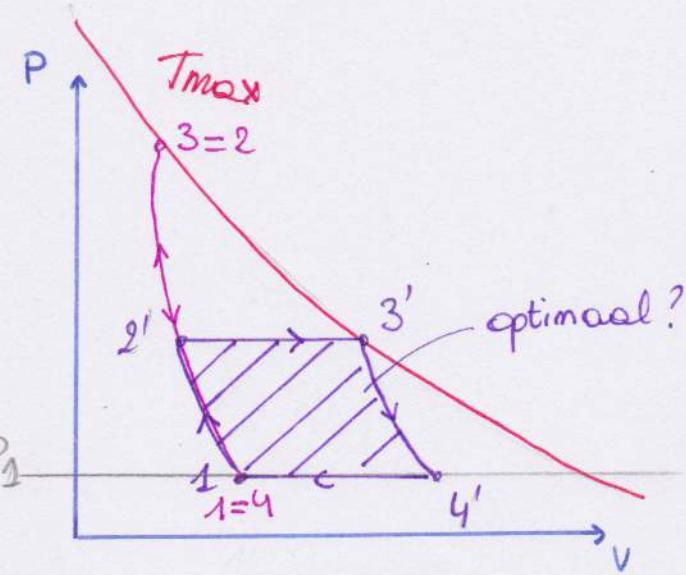
$$\text{vermits } (1-k)/k < 0$$

$\hookrightarrow \eta_{th}$  r ols  $e^x$

maar

\*

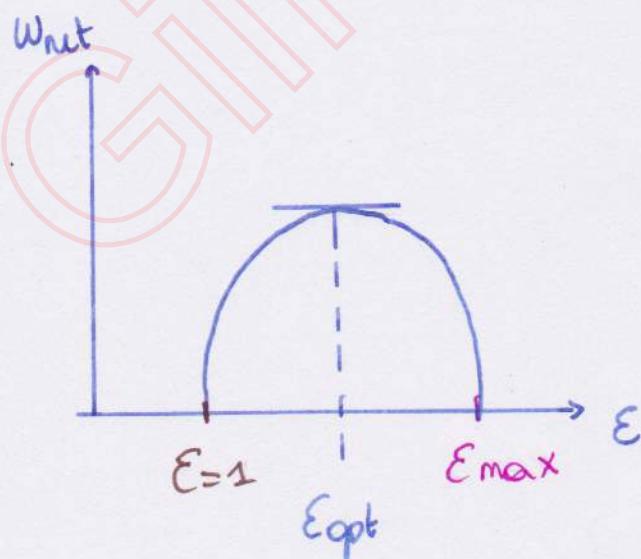
# Gasturbine $\rightarrow \epsilon_{opt}$



$$P_2 \rightarrow \max \quad \Leftrightarrow T_2 = T_3 = T_{\max} \quad \epsilon_{\max}$$

$$\Leftrightarrow q_{in} = 0 \quad w_{net} = 0$$

Vermits  $3 \rightarrow 4$  isentropisch  
 $\Leftrightarrow 4 = 1$



$$\frac{dW_{net}}{dT_2} \Big|_{T_2, opt} = 0$$

$$W_{net} = C_p \left( T_1 - T_2 + T_3 - \frac{T_1 T_3}{T_2} \right)$$

$$\frac{dW_{net}}{dT_2} = -1 + \frac{T_1 T_3}{T_2^2} = 0$$

$$T_{2, opt} = \sqrt{T_1 T_3}$$

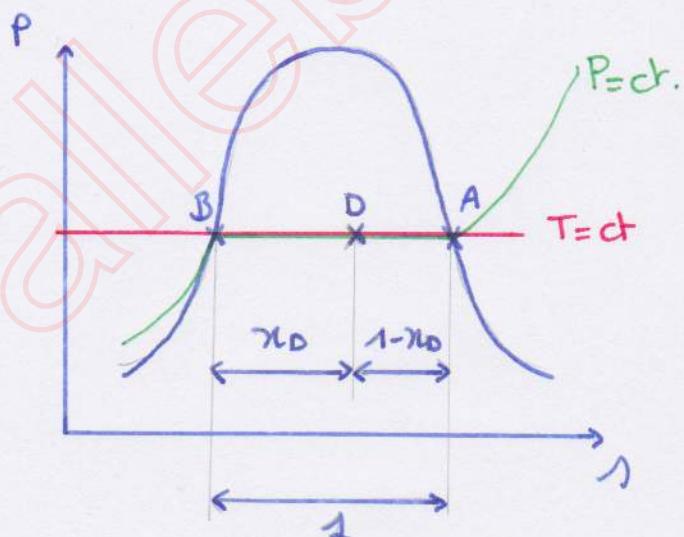
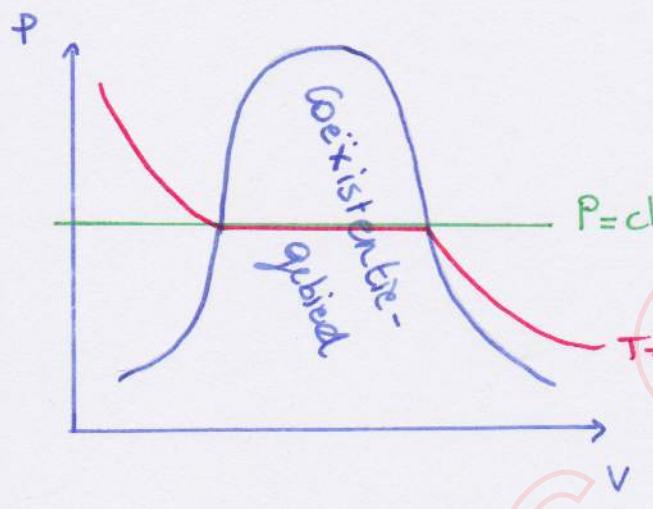
$$\frac{T_2}{T_1} = \epsilon^{\frac{(k-1)}{k}} \quad \Leftrightarrow \epsilon_{opt} = \left( \frac{T_3}{T_1} \right)^{\frac{k}{2(k-1)}}$$

$$\eta_{th, opt} = 1 - (E_{opt})^{\frac{1-k}{k}}$$

$$\eta_{th, opt} = 1 - \sqrt{\frac{T_1}{T_3}}$$

# H9: Kleingprocessen met vele fluida

## Diagrammen



## Dampgehalte

$$m_{\text{tot}} = m_d + m_{\text{vl}}$$

$$\eta = \frac{m_d}{m_{\text{tot}}}$$

$$1-\eta = \frac{m_{\text{vl}}}{m_{\text{tot}}}$$

$$V_{\text{tot}} = V_d + V_{\text{vl}}$$

$$m_{\text{tot}} V_{\text{tot}} = m_d V_d + m_{\text{vl}} V_{\text{vl}}$$

$$\eta V_d$$

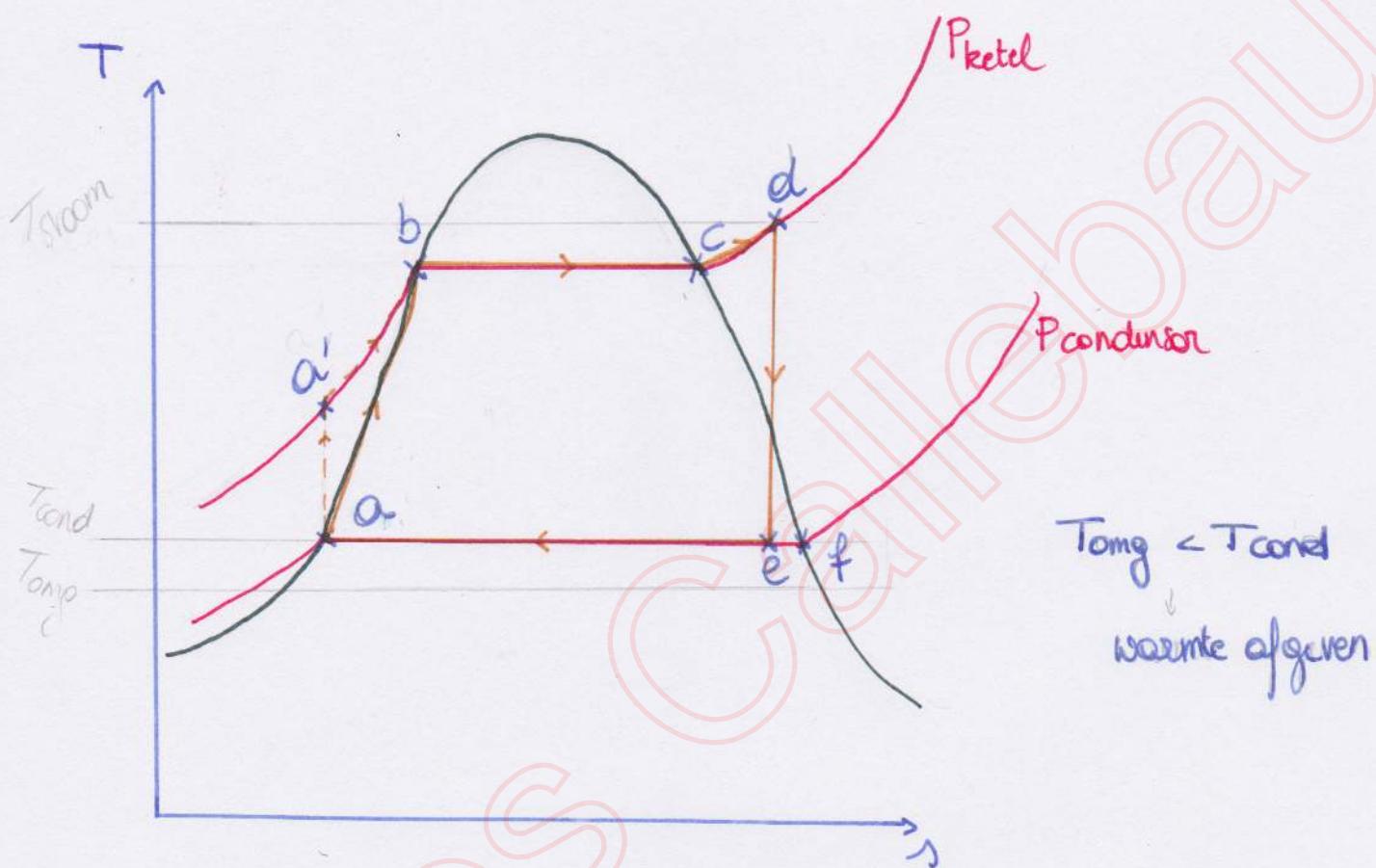
$$V_d = \frac{m_d}{m_{\text{tot}}} V_d + \frac{m_{\text{vl}}}{m_{\text{tot}}} V_{\text{vl}}$$

$$V_d = \eta V_d + (1-\eta) V_{\text{vl}}$$

$$h_d = \eta h_A + (1-\eta) h_B$$

$$\rho_d = \eta \rho_A + (1-\eta) \rho_B$$

# Het kringloop van Rankine → stoomturbine



- ① Pomp  $a \rightarrow a'$  : isentroop  $\rightarrow q=0$   
 $\rightarrow W_t = h_a - h_{a'} < 0$   
 ↳ verwaarlozen  $\rightarrow W_t = 0$
- ② Stoomketel  $\begin{matrix} a' \\ \hline a \end{matrix} \rightarrow d$  : isobaar  $\rightarrow W_t = 0$   
 $\rightarrow q = h_d - h_{a'} > 0 = q_{\text{in}}$
- ③ Stoomturbine  $d \rightarrow e$  : isentroop  $\rightarrow q=0$   
 $\rightarrow W_t = h_d - h_e > 0$
- ④ Condensor  $e \rightarrow a$  : isobaar  $\rightarrow W_t = 0$   
 $\rightarrow q = h_a - h_e < 0 = q_{\text{uit}}$

$$h_a = h_{vl} (P_{cond})$$

$$h_d = h (P_{klet}, T_{room})$$

$$h_c = \eta_e h_f + (1 - \eta_e) h_a$$

$$h_f = h_d (P_{cond})$$

$$\eta_c \rightarrow \eta_e = \eta_d = \eta (P_{klet}, T_{room})$$

$$\eta_e = \eta_e \cdot \frac{h_f}{T} + (1 - \eta_e) \cdot \frac{h_a}{T}$$

$$\eta_d (P_{cond})$$

$$\eta_a (P_{cond})$$

langs  $P = P_{klet}$

$$\hookrightarrow dh = c_p dT \rightarrow \frac{h_d - h_c}{T} = \frac{c_p}{T} (T_d - T_c)$$

$$h_d (P_{klet})$$

$$T_{room}$$

$$T_{back} (P_{klet})$$

$$\hookrightarrow ds = c_p \frac{dT}{T} \rightarrow \frac{\eta_d - \eta_c}{T} = c_p \ln \left( \frac{T_d}{T_c} \right)$$

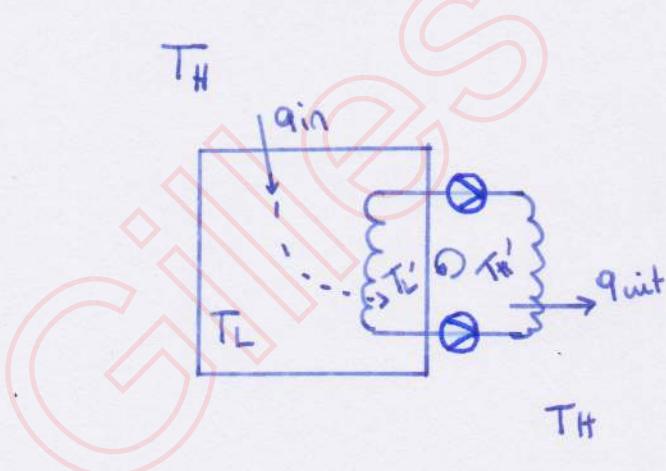
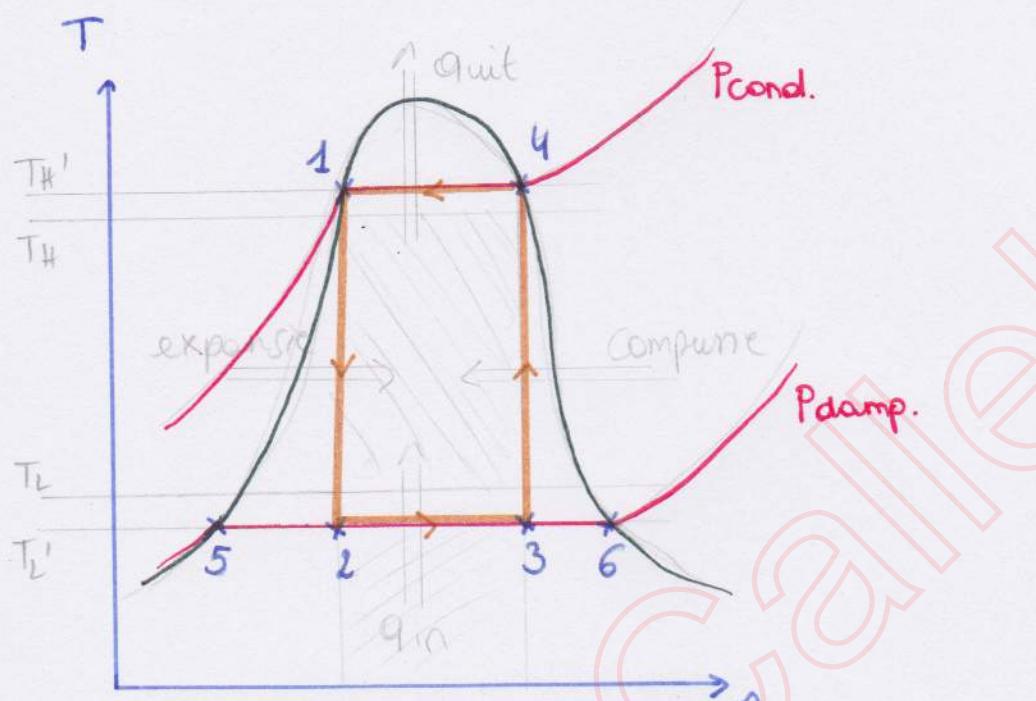
$$\eta_d (P_{klet})$$

$$\eta_{th} = \frac{W_t, \text{turbine}}{q_{in}} \quad (\approx 45\%)$$

$$P = m \cdot W_t \rightarrow m \rightarrow \dot{Q}_{tochter} = m \cdot q_{in}$$

$$\dot{Q}_{afvoer} = m \cdot q_{uit}$$

# Het kringloop voor koelmachines



Carnot kalploes  
→ 2 × isotherm → 2 isobaren  
✓ in coëxistentiegebied  
isotherm = isobar  
→ 2 isentropen → 2 ijdelingen

$T_L' < T_L \rightarrow$  spontaan  $q_{in}$  naar  $T_L'$

$T_H' > T_H \rightarrow$  spontaan  $quit$  naar  $T_H'$

① isentroop expanderen

$$1 \rightarrow 2 : w_t = h_1 - h_2 > 0$$

② isobar verdampen

$$2 \rightarrow 3 : q_{in} = h_3 - h_2 > 0$$

③ isentroop comp.

$$3 \rightarrow 4 : w_t = h_3 - h_4 < 0$$

④ isobar condenseren

$$4 \rightarrow 1 : q_{uit} = h_1 - h_4 < 0$$

$$h_1 = h_{vl} (P_{cond})$$

$$h_4 = h_d (P_{cond})$$

$$h_2 \rightarrow h_2 = \frac{x_2}{\gamma} h_d + \frac{(1-x_2)}{\gamma} h_{vl}$$

$\downarrow$   
 $h_d (P_{verd.}) \qquad \qquad \qquad h_{vl} (P_{verd.})$

$$\gamma_2 = \gamma_1 = \gamma_{vl} (P_{cond.})$$

$$\gamma_2 = \frac{x_2}{\gamma} \gamma_d + \frac{(1-x_2)}{\gamma} \gamma_{vl}$$

$$\gamma_d (P_{verd.})$$

$\} \rightarrow n_2$

$\gamma$

$$\gamma_{vl} (P_{verd.})$$

$h_3 \rightarrow idem$

$$\epsilon = \frac{q_{in}}{|w_{net}|}$$

$$\epsilon_w = \frac{|q_{uit}|}{|w_{net}|}$$

# Expansieventiel x droge compressie

→ sloopproces

$$\hookrightarrow W_t = 0$$

$$\hookrightarrow h_1 = h_7$$

$\hookrightarrow \dot{m}$  omkeerbaar

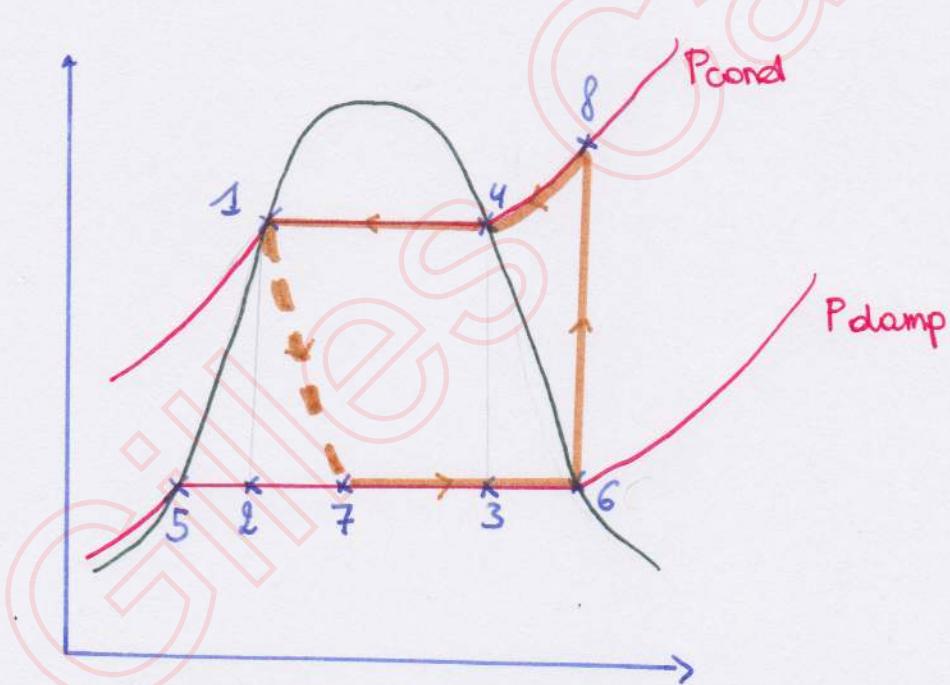
→ vloeistof afschijden

$$\hookrightarrow q_{in} \uparrow \text{ (extra)}$$

$$\hookrightarrow w_t = h_f - h_g \uparrow$$

$$\begin{aligned} q_{in} &\downarrow \\ \propto & \\ |W_{net}| &\uparrow \end{aligned} \quad \rightarrow E \downarrow$$

$$\hookrightarrow E \downarrow$$



langs  $P = P_{cond}$

$$\hookrightarrow h_f = h_u + C_p (T_f - T_u)$$

$$\hookrightarrow s_f = s_u + C_p \ln \left( \frac{T_f}{T_u} \right) \rightarrow T_f$$

↓  
6

$$q_{in} = h_6 - h_7$$

$$|W_{net}| = h_8 - h_6$$

$$|q_{uit}| = h_8 - h_1$$

$$\left. \begin{array}{l} q_{in} \\ |W_{net}| \\ |q_{uit}| \end{array} \right\} \rightarrow E = \frac{q_{in}}{|W_{net}|}$$

$$Q_{in} = m q_{in}$$

$$\downarrow m$$

$$P = m |W_{net}|$$