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SVEPM WORKSHOP, UTRECHT 27.03.2019

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# BAYESIAN NETWORKS MEET OBSERVATIONAL DATA



## Credit Card Fraud Detection Using Bayesian and Neural Networks

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### Abstract

This paper discusses automated credit card fraud detection by means of machine learning. In an era of digitalization, credit card fraud detection is of great importance to financial institutions. We apply two machine learning techniques suited for reasoning under uncertainty: artificial neural networks and

do the fraud detection. After a process of learning, the program is supposed to be able to correctly classify a transaction it has never seen before as fraudulent or not fraudulent, given some features of that transaction.

The structure of this paper is as follows: first we introduce the reader to the domain of credit card fraud detection. In Sections 3 and 4 we briefly ex-

Credit Card Fraud Detection  
Using Bayesian and Neural Networks

Sam Maes                      Karl Tuyls                      Bram Vanschoenwinkel

experiment	$\pm 10\%$ false pos	$\pm 15\%$ false pos
ANN-fig 2(a)	60% true pos	70% true pos
ANN-fig 2(a)	47% true pos	58% true pos
ANN-fig 2(c)	60% true pos	70% true pos
BBN-fig 2(e)	68% true pos	74% true pos
BBN-fig 2(g)	68% true pos	74% true pos

Abstract

This paper discusses credit card fraud detection by means of machine learning. Due to digitalization, credit card fraud has gained great importance to financial institutions. We compare two machine learning techniques suited for reasoning under uncertainty: artificial neural networks and

Table 1: This table compares the results achieved with ANN and BBN, for a false positive rate of respectively 10% and 15%.

process of learning, we aim to correctly classify transactions before as fraudulent. The features of that process are as follows: first we introduce the reader to the domain of credit card fraud detection. In Sections 3 and 4 we briefly ex-

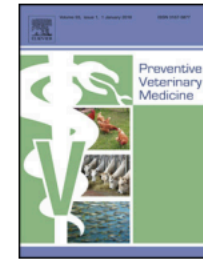
# MOTIVATIONAL EXAMPLE: VETERINARY EPIDEMIOLOGY DATA VISUALISATION



Contents lists available at [SciVerse ScienceDirect](https://www.sciencedirect.com)

## Preventive Veterinary Medicine

journal homepage: [www.elsevier.com/locate/prevetmed](http://www.elsevier.com/locate/prevetmed)



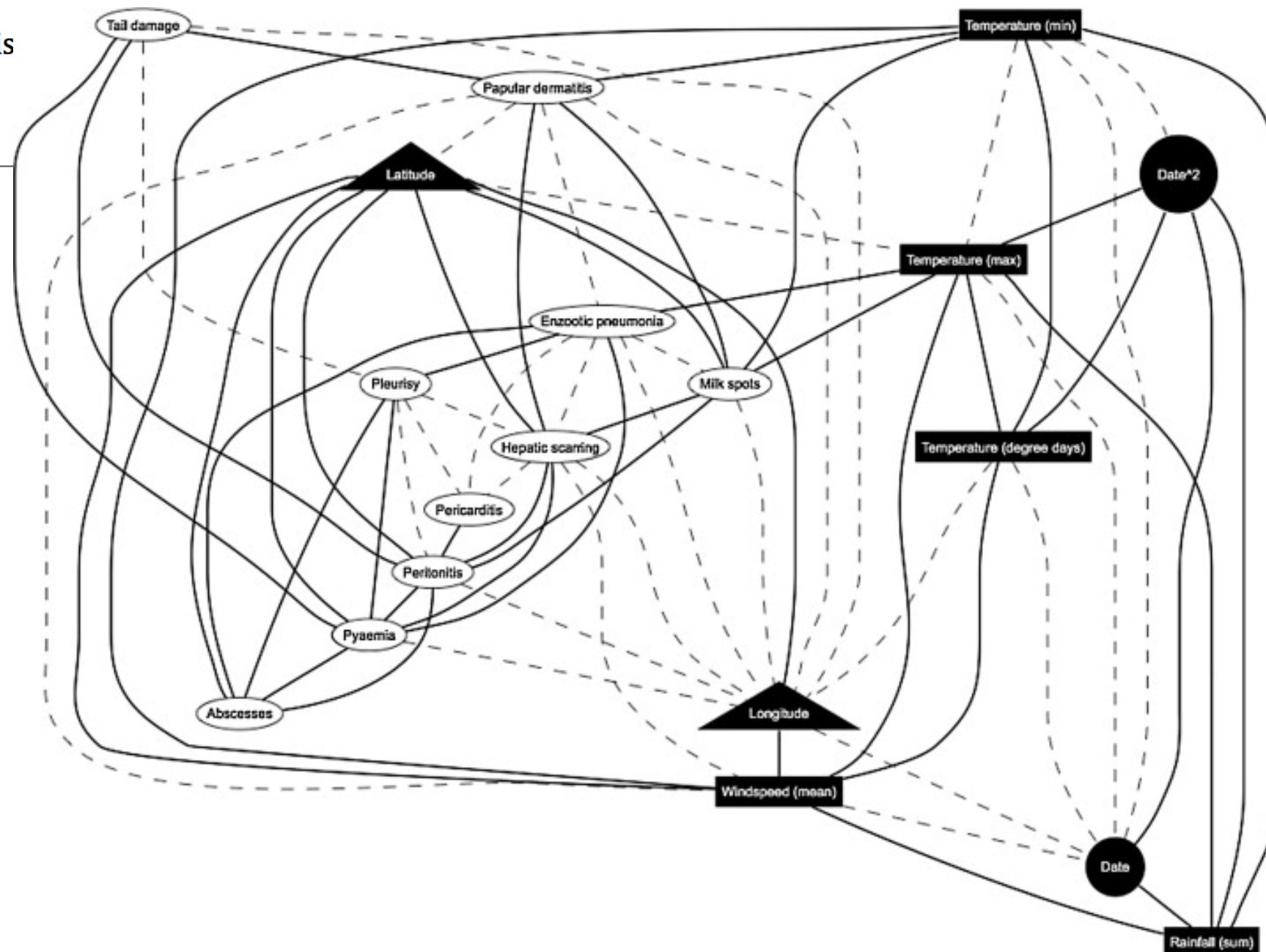
### Using Bayesian networks to explore the role of weather as a potential determinant of disease in pigs

B.J.J. McCormick<sup>a</sup>, M.J. Sanchez-Vazquez<sup>b</sup>, F.I. Lewis

<sup>a</sup> Fogarty International Center, National Institutes of Health, Bethesda, MD 20892, USA

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<sup>c</sup> Section of Epidemiology, University of Zurich, Zurich, Switzerland





# MOTIVATIONAL EXAMPLE: SOCIAL SCIENCES

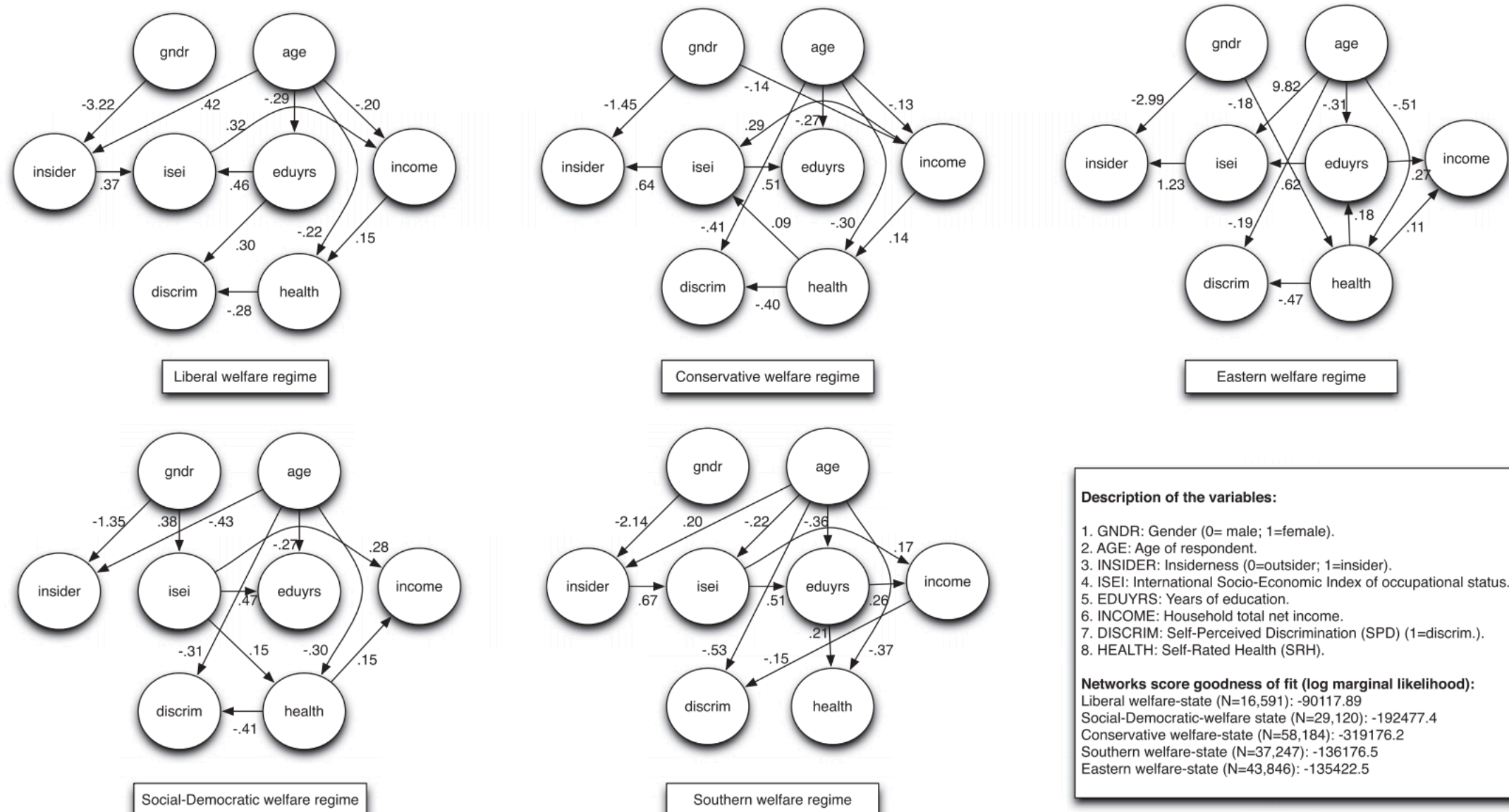
## DATA INTERPRETATION

### Discovering complex interrelationships between socioeconomic status and health in Europe: A case study applying Bayesian Networks

Javier Alvarez-Galvez <sup>a, b, \*</sup>

<sup>a</sup> Loyola University Andalusia, Department of International Studies, Campus de Palmas Altas, Faculty of Political Sciences and Law, Seville 41014, Spain

<sup>b</sup> Complutense University of Madrid, Department of Sociology IV (Research Methodology and Communication Theory), Campus de Somosaguas, Faculty of Political



**Fig. 1.** Bayesian networks describing interrelationships between SES and health in five European welfare states.

# BAYESIAN NETWORKS IN THE MACHINE LEARNING WORLD

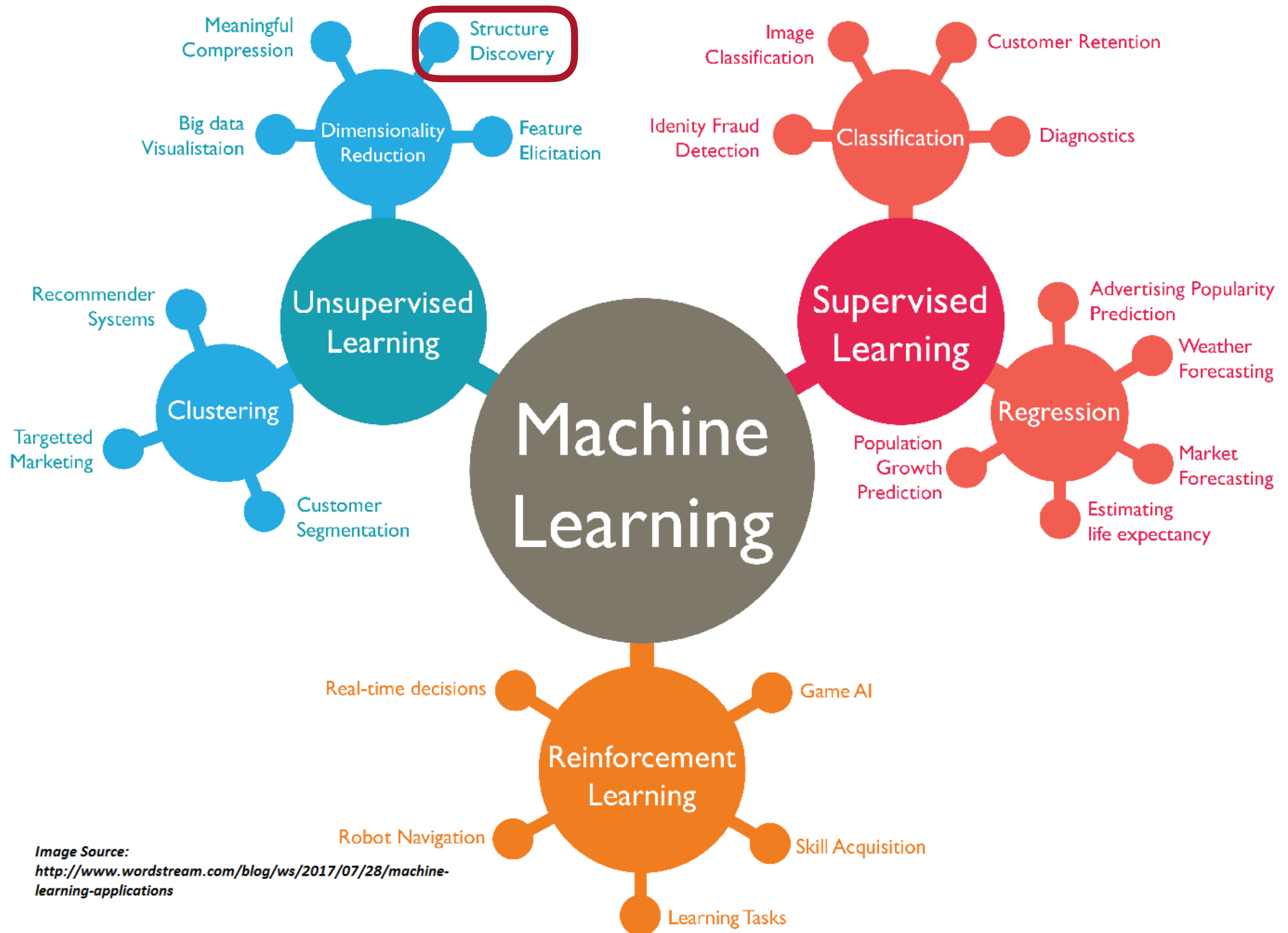


Image Source:

<http://www.wordstream.com/blog/ws/2017/07/28/machine-learning-applications>

# OUTLINE OF THE TALK

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## **Objectif of the workshop:**

How to **learn Bayesian networks** from observational data?

# OUTLINE OF THE TALK

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## Objectif of the workshop:

select

How to ~~learn~~ Bayesian networks from observational data?

Bayesian Networks are defined by two elements:

Network structure:

Directed Acyclic Graph (DAG):  $G = (V, A)$

in which each node  $v_i \in V$  corresponds to a random variable  $X_i$

Probability distribution:

Probability distribution  $X$  with parameters  $\Theta$ , which can be factorised into smaller local probability distributions according to the arcs  $a_{ij} \in A$  present in the graph.

A BN encodes the factorisation of the joint distribution

$$P(\mathbf{X}) = \prod_{j=1}^n P(X_j \mid \mathbf{Pa}_j, \Theta_j), \text{ where } \mathbf{Pa}_j \text{ is the set of parents of } X_j$$



# PLAN

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1. From observationnal dataset deduce probabilistic model
  - Usually discrete BN or jointly Gaussian
  - Epidemiological constrain: mixture of distributions
2. From probabilistic model deduce structure

**EXPONENTIAL FAMILY**

Observational dataset

X1	X2	X3	...
12	23	53	...
32	31	23	...
10	16	45	...
...	...	...	...

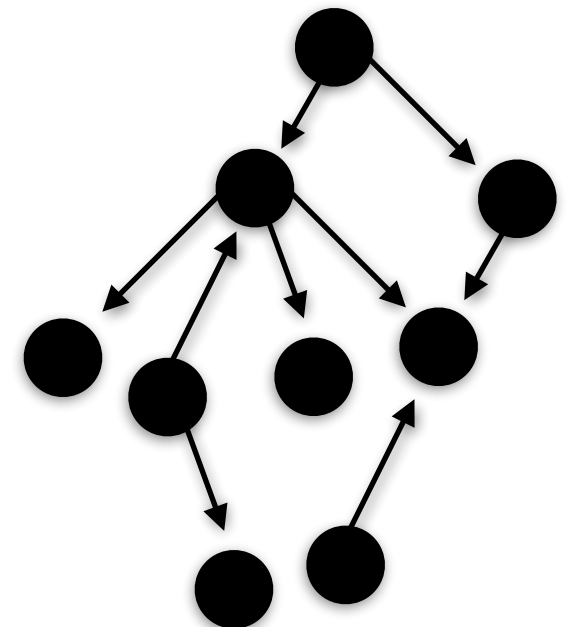


Probabilistic model

$$P(X_1, \dots, X_n) = P(X_i | X_j, \dots) \dots$$



Network structure



# COMBINATORIAL WALL

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# Nodes	# DAGs	Inference	Typical domain of interest
1 - 15 Nodes	$< 10^{41}$ DAGs	Exact inference	EPIDEMIOLOGY GENOMICS PROTEOMICS
16 - 25 Nodes	$< 10^{100}$ DAGs	Exact inference possible	
26 - 50 Nodes	$< 10^{400}$ DAGs	Approximate inference	
51 - 100 Nodes	$< 10^{1700}$ DAGs	Approximate inference	
101 - 1000 Nodes	$< 10^{100000}$ DAGs	(very) approximative inference	

## Approximations:

- ▶ limiting number of parents per node
- ▶ Decomposable scores/efficient algorithm
- ▶ Score equivalence

## SOME ELEMENTS OF PROBABILITY THEORY

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The **conditional probability** of A given B is:  $P(A \mid B) = \frac{P(A, B)}{P(B)}$

Bayes theorem:  $P(A \mid B) = \frac{P(B \mid A)P(A)}{P(B)}$

Let A, B and C non intersecting subsets of nodes in a DAG G

A is **conditionally independent** of B given C if:  $A \perp\!\!\!\perp_P B \mid C$

$$P(A, B \mid C) = P(A \mid C)P(B \mid C)$$

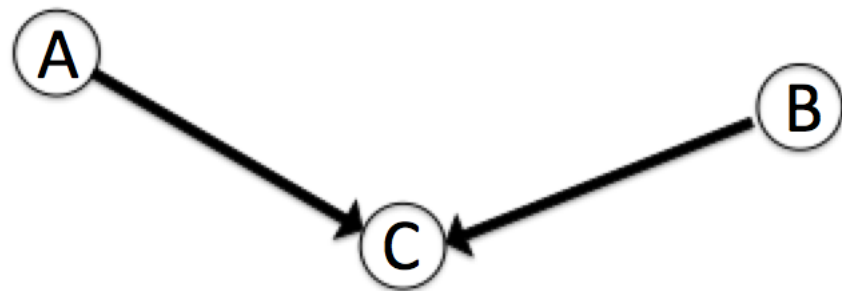
## ELEMENT OF GRAPH THEORY

Let  $A$ ,  $B$  and  $C$  non intersecting subsets of nodes in a DAG  $G$

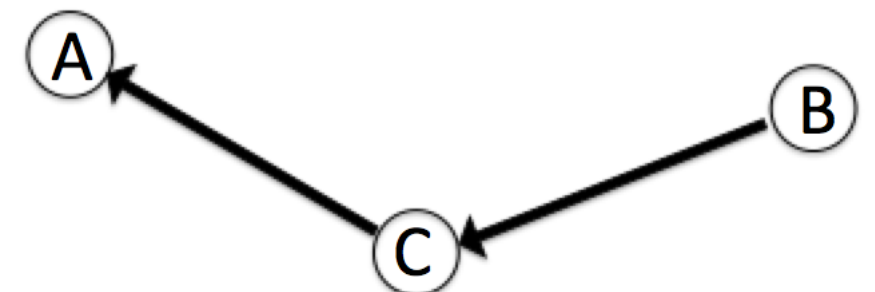
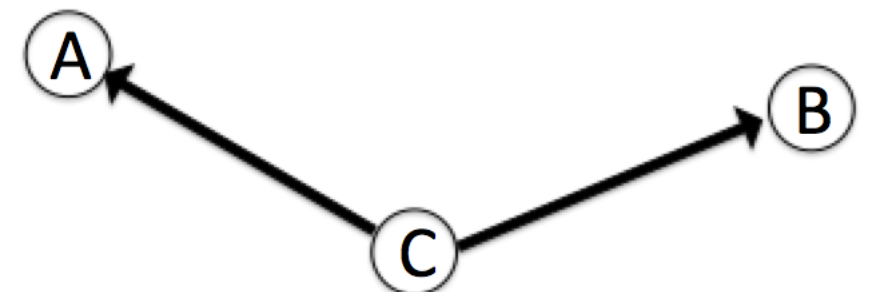
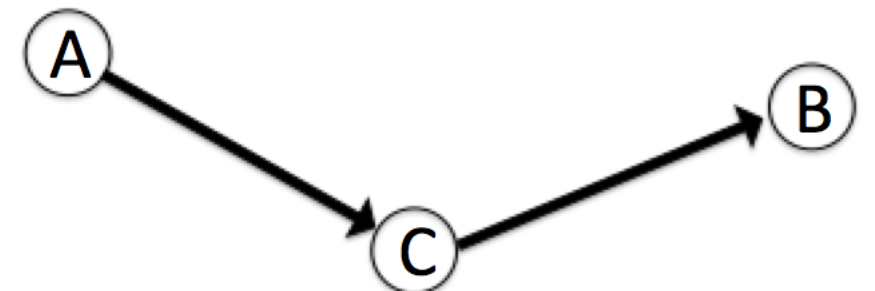
$A$  is **conditionally independent** of  $B$  given  $C$  if:  $A \perp\!\!\!\perp_P B | C$

$$P(A, B | C) = P(A | C)P(B | C)$$

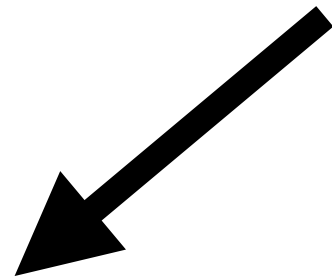
$$A \not\perp\!\!\!\perp_P B | C$$



$$A \perp\!\!\!\perp_P B | C$$

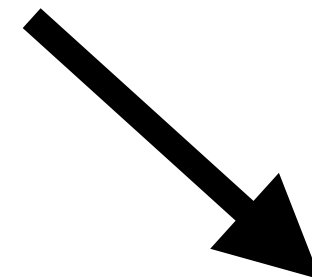


$$\mathcal{M} = (\mathcal{S}, \Theta_{\mathcal{M}})$$



Model selection

Structure learning



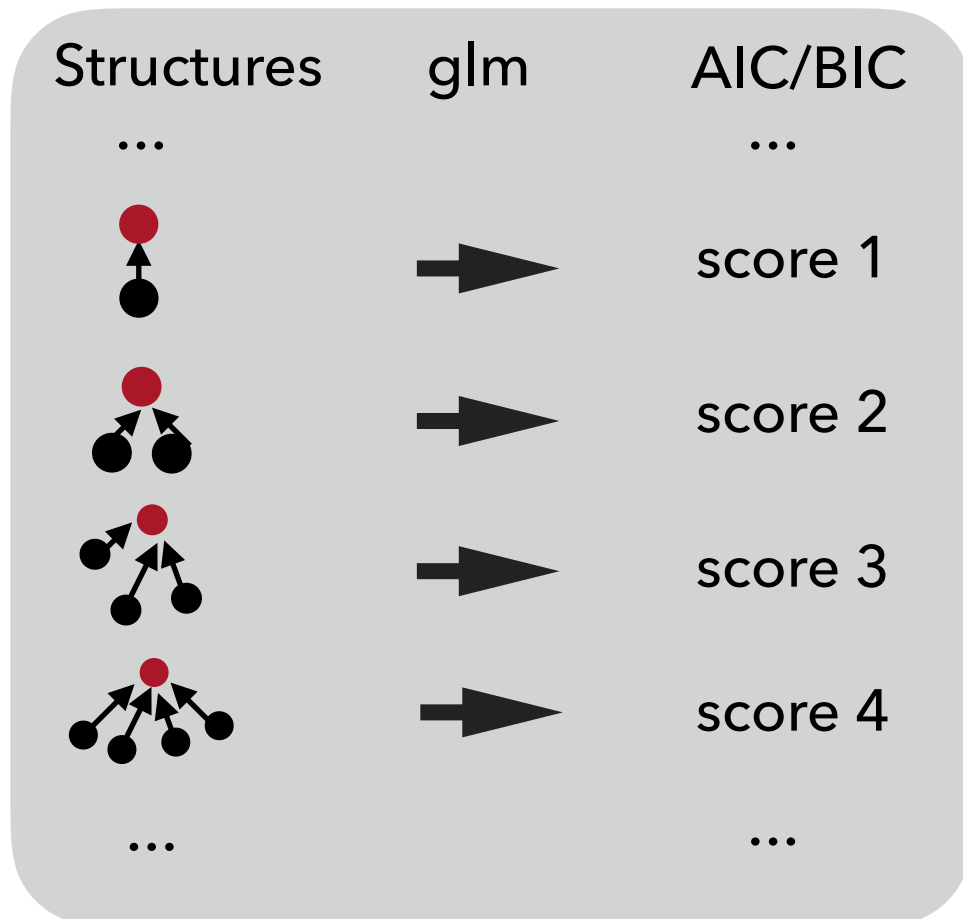
Parameter estimation

Parameter learning

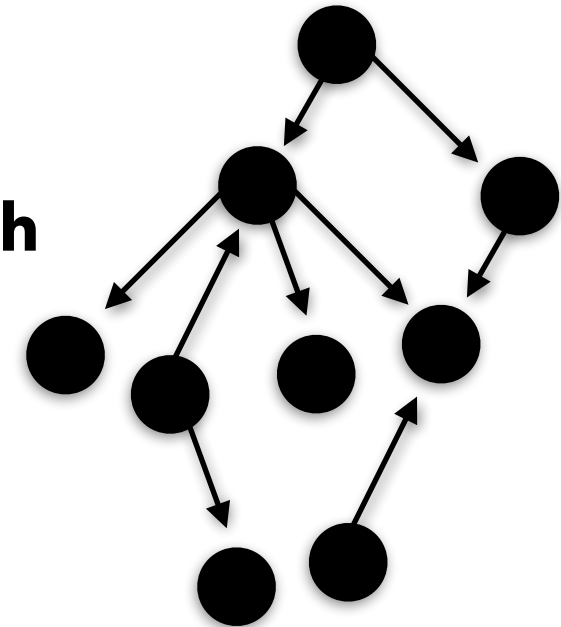
$$P(\mathcal{M}|\mathcal{D}) = \underbrace{P(\Theta_{\mathcal{M}}, \mathcal{S}|\mathcal{D})}_{\text{model learning}} = \underbrace{P(\Theta_{\mathcal{M}}|\mathcal{S}, \mathcal{D})}_{\text{parameter learning}} \cdot \underbrace{P(\mathcal{S}|\mathcal{D})}_{\text{structure learning}}$$



## Search and score algorithm

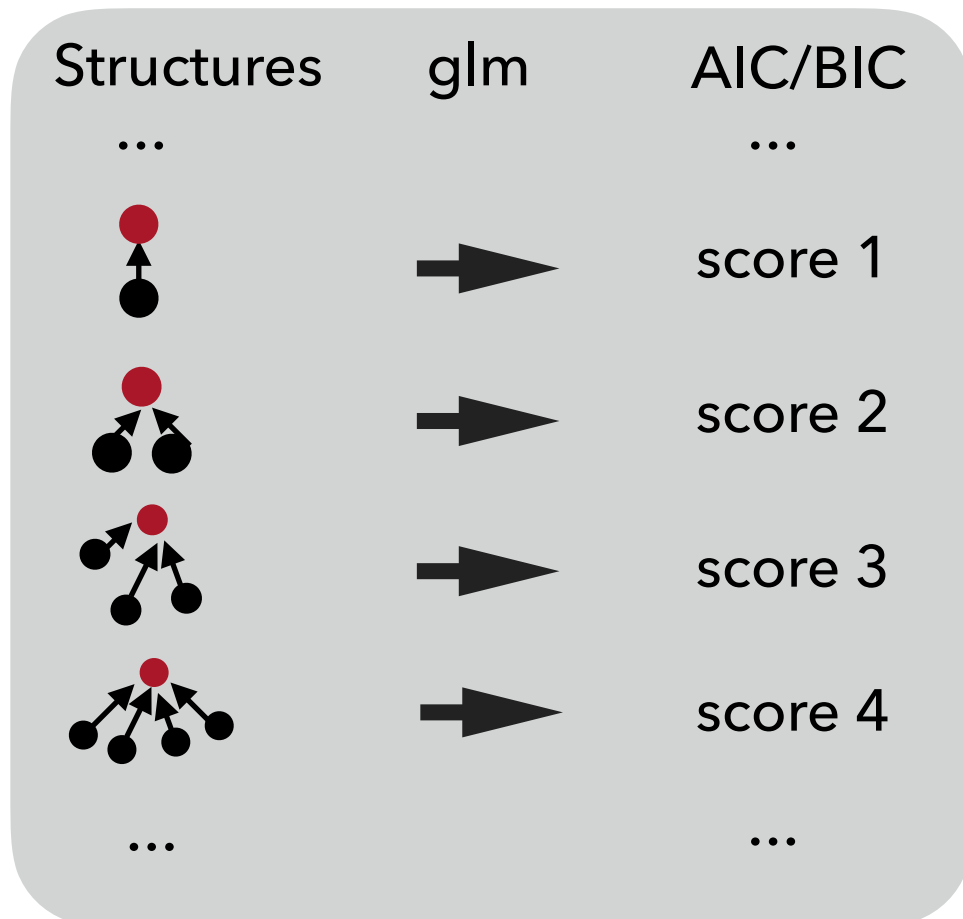


**Exact or heuristic search**

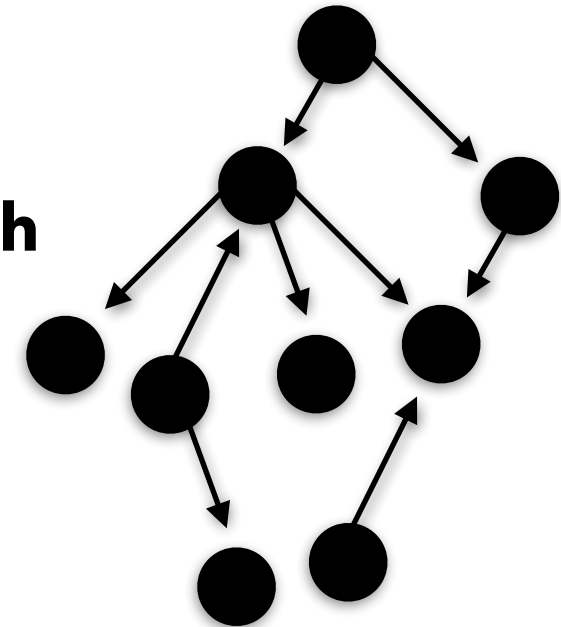


Bayesian network with  
highest posterior  
probability

## Search and score algorithm



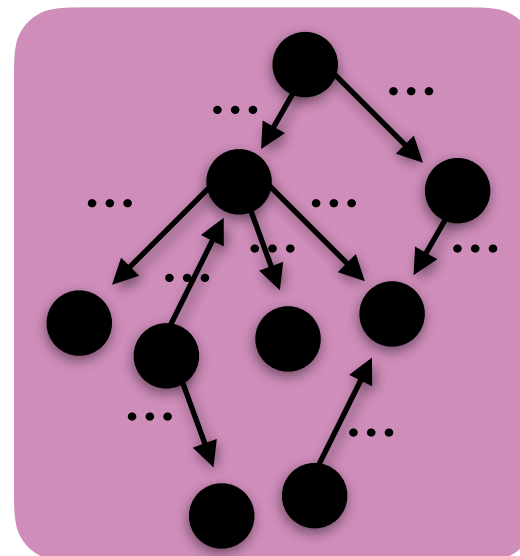
Exact or heuristic search



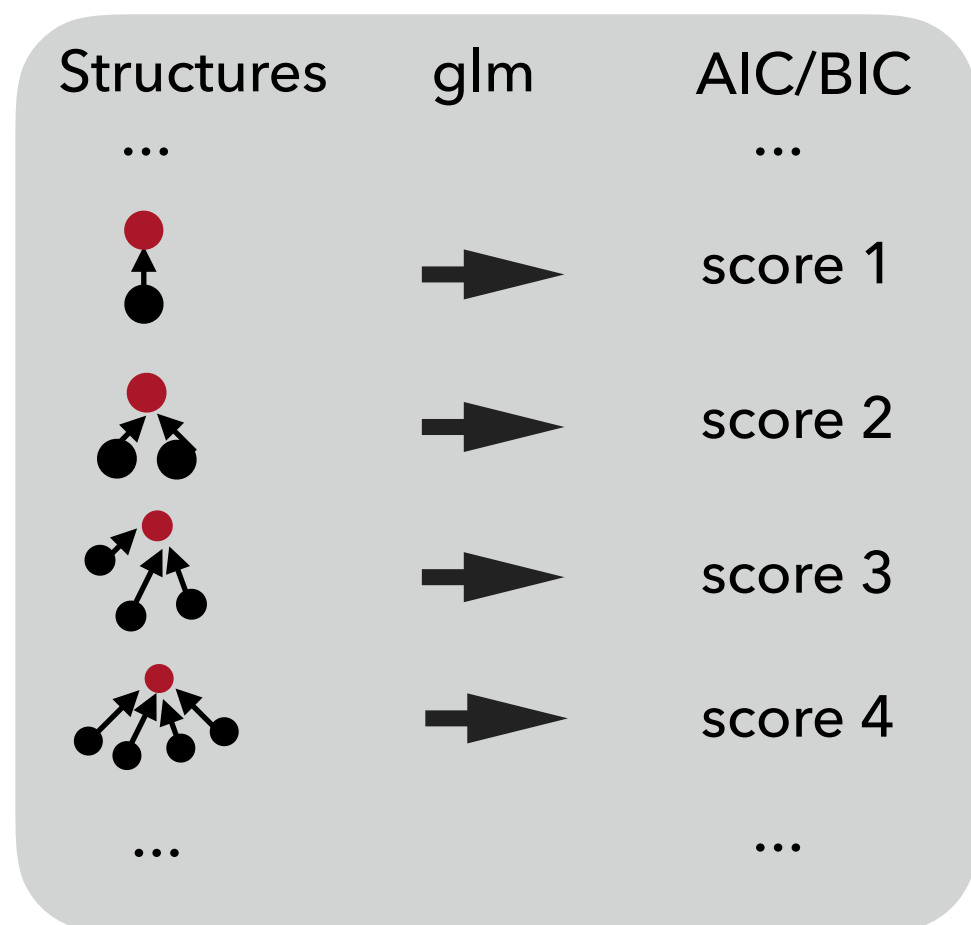
Bayesian network with highest posterior probability

## Parameter estimation

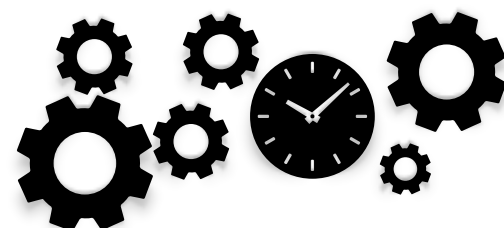
- ▶ compute marginal posterior density
- ▶ regression estimate



## Search and score algorithm

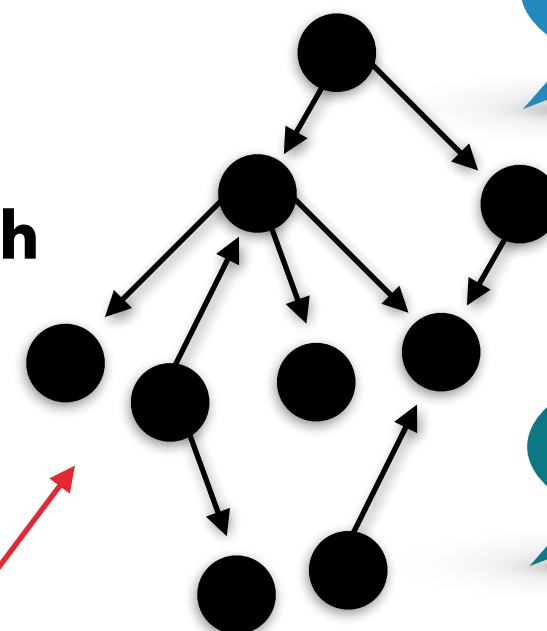


Exact or heuristic search



**Causality!**

*Ban/Retain  
structures*



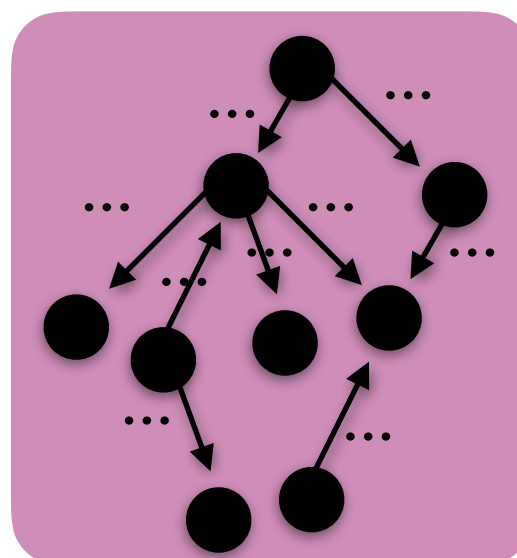
Adjustment

Random effect

Bayesian network with  
highest posterior  
probability

## Parameter estimation

- ▶ compute marginal posterior density
- ▶ regression estimate



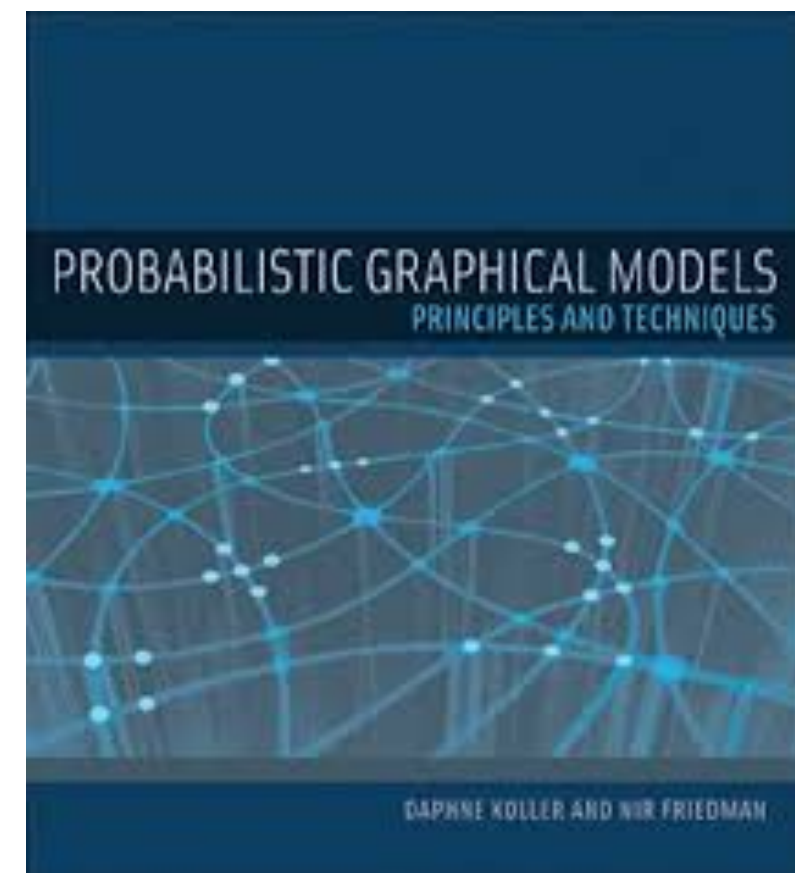
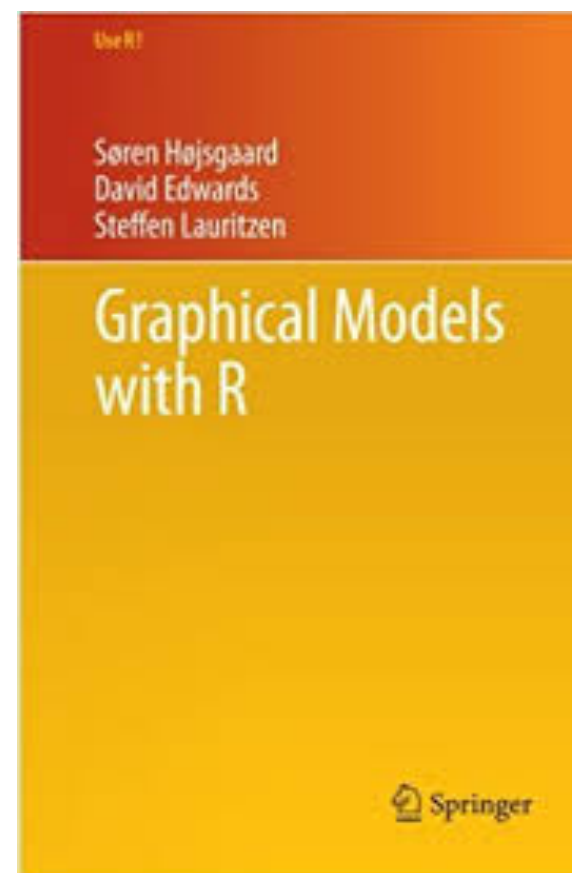
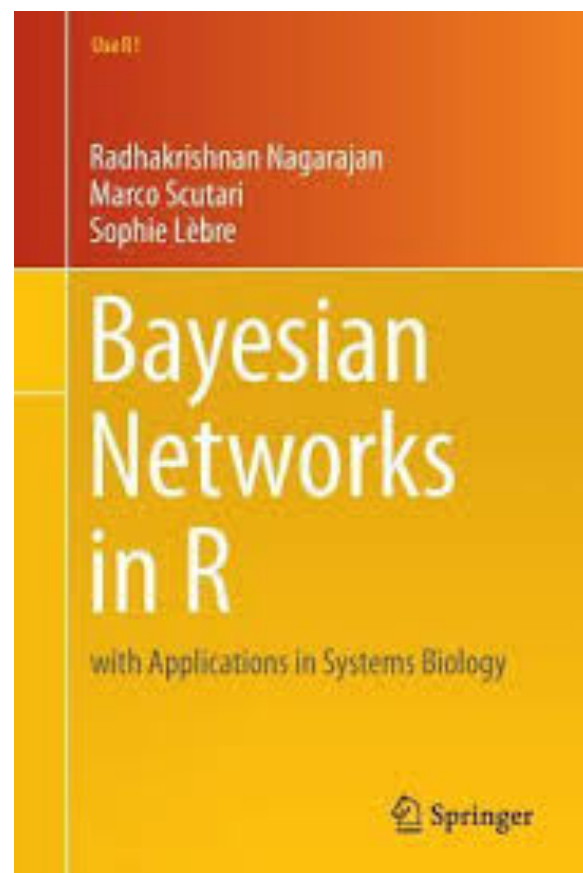
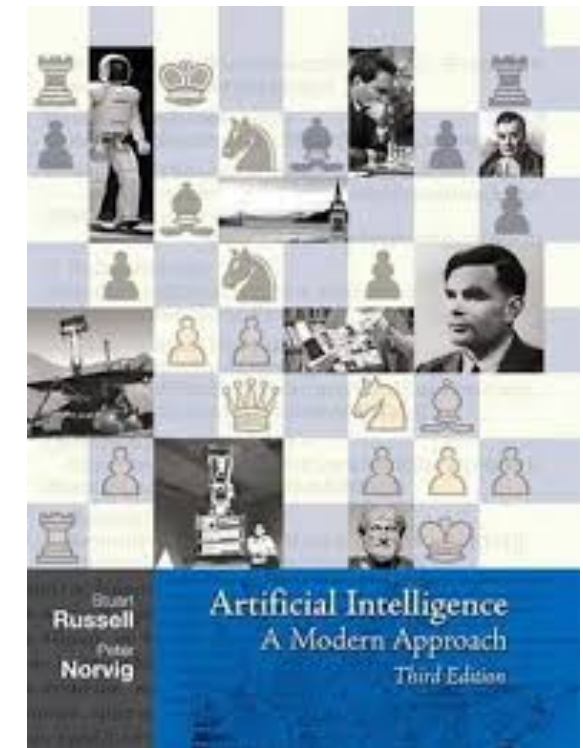
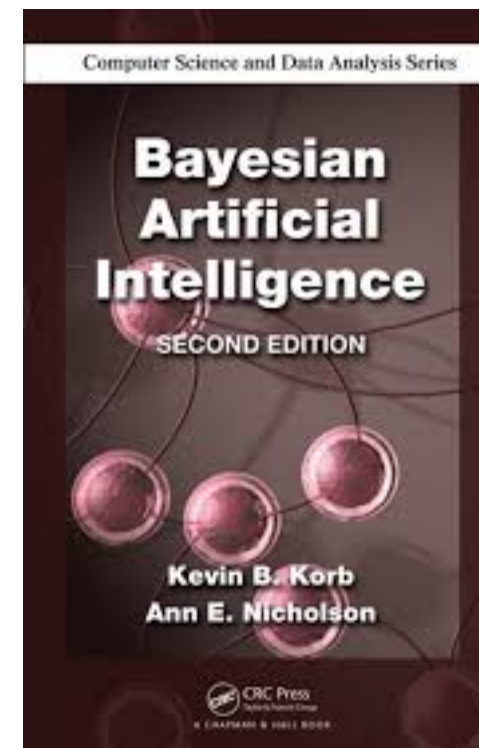
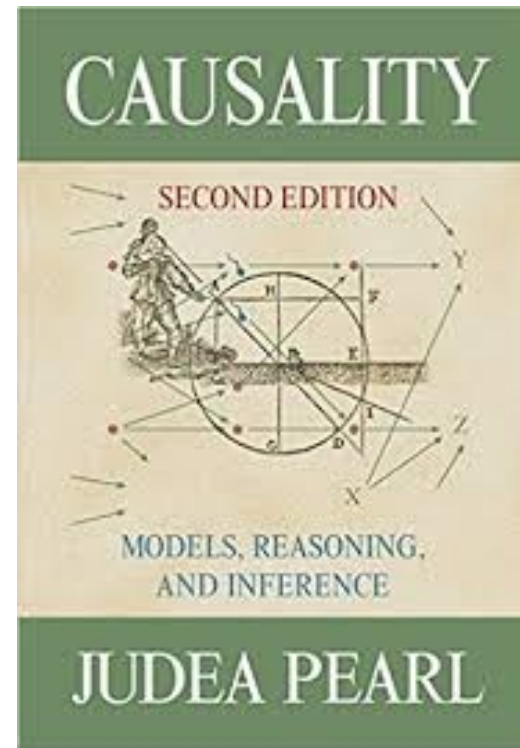
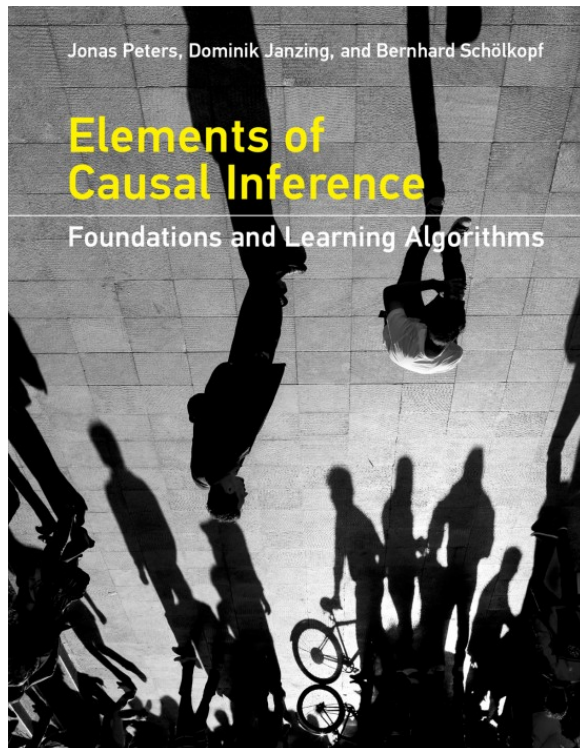
**Using R**

`buildscorecache()`

`mostprobable()`

`fitabn()`

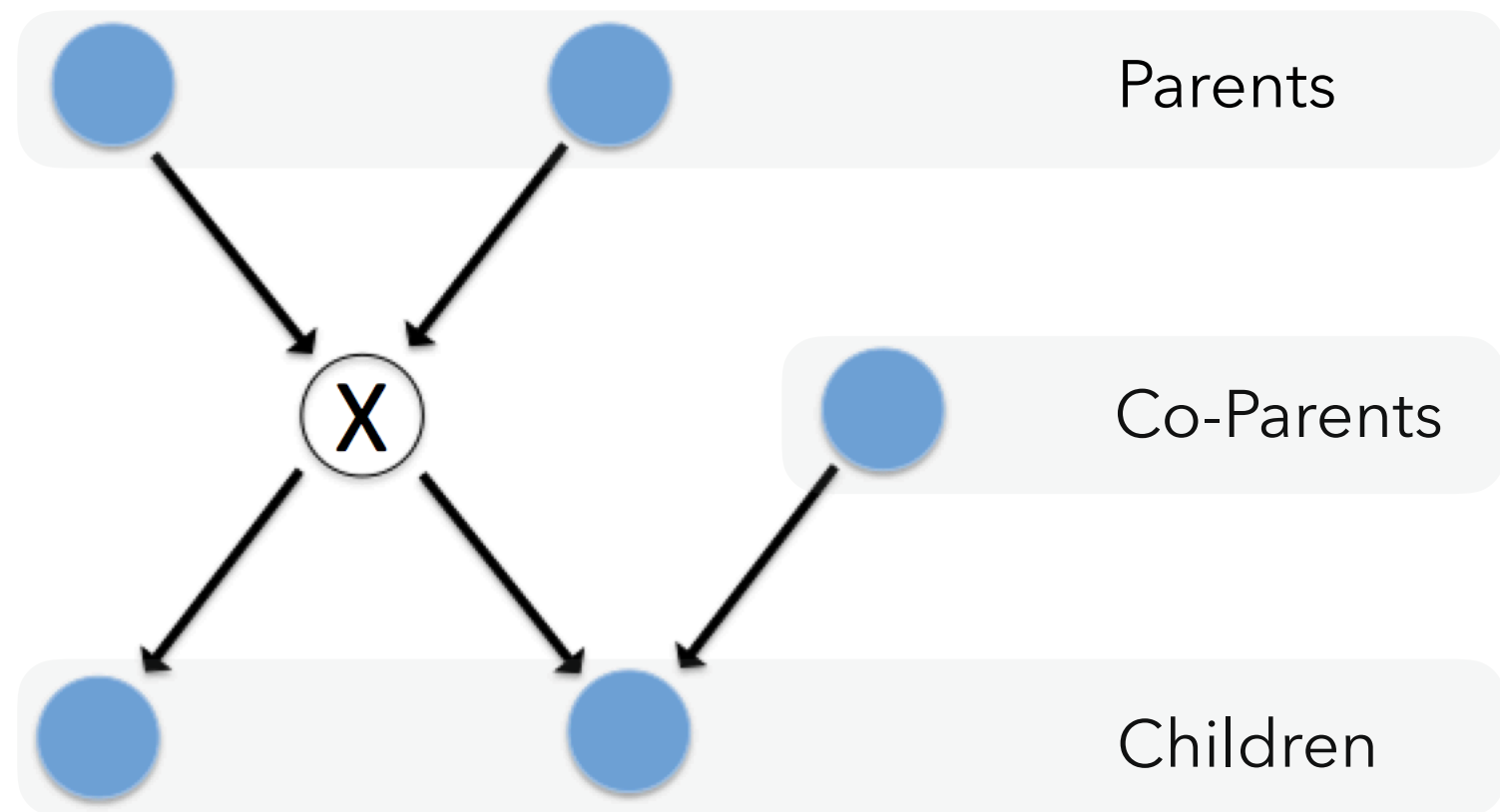
# SELECTED BIBLIOGRAPHY



## ELEMENT OF GRAPH THEORY: MARKOV BLANKET

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The **Markov Blanket** of a node is the set of **parents**, **co-parents** and **children**.



$$P(X_k \mid X_n, k \neq n) = P(X_k \mid X_{\text{MB}(k)}), \forall k$$

The **Markov Blanket** of a node is the set of nodes that **shields** the index node from the rest of the network

**Local Markov property:**

$$X \perp \text{Non-Descendants}(X) \mid Pa(X)$$



# LEARNING BAYESIAN NETWORKS

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- ▶ In a practical perspective, for **observational** data, if learning algorithms rely on **probabilistic learning algorithm**. Then one can learn up to the **Markov equivalence class**.
- ▶ **Markov equivalence class** are the set of DAGs that have the same **skeleton** and **v-structure**.

