

# Energy Balance and Climate

EES 3310/5310

Global Climate Change

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Class #3: Friday January 10 2020

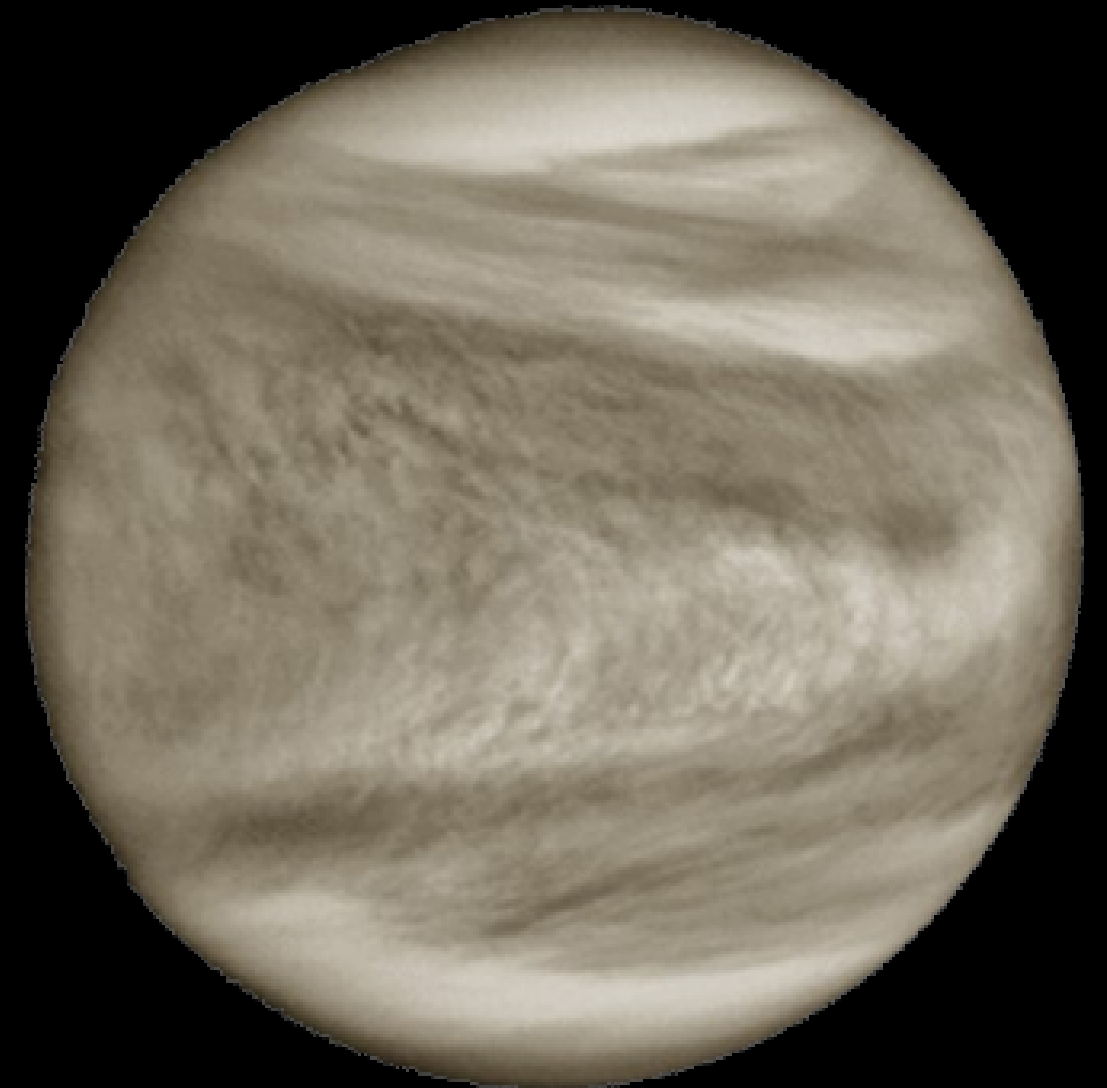
# Looking for a Good Home



Bad  
−28°F



Good  
71°F



Worst  
800°F

# Basic Concepts

# Vocabulary

- **Energy, Heat:**
  - Heat = energy flowing spontaneously from hot to cold
- **Power:** speed at which energy flows or transforms

$$\text{Power, Flux} = \text{Heat flow} / \text{Time}$$

$$\text{Heat, Energy} = \text{Power} \times \text{Time}$$

- **Intensity:** Concentration of power

$$\text{Intensity} = \text{Power} / \text{Area}$$

$$\text{Power} = \text{Intensity} \times \text{Area}$$

# Temperature of a planet

- **Basic principle:**

Steady temperature if and only if

$$\text{Power}_{\text{in}} = \text{Power}_{\text{out}}$$

- **How can heat get in or out?**
- Electromagnetic radiation

# Electromagnetic Waves

- **Color and brightness**
- **Color:**
  - Two ways to measure **color**:
  - Wavelength ( $\lambda$ )
  - Wavenumber ( $n = 1/\lambda$ )
- Archer mostly uses wavenumber
  - Math is simpler that way
- **Brightness:**
  - Intensity (power/area, Watts/square meter)

# Colors

Color	wavelengths	wavenumbers
infrared	$> 0.70 \mu\text{m}$	$< 14,000$
red	$\sim 0.70\text{--}0.64 \mu\text{m}$	$\sim 14,000\text{--}16,000$
orange	$\sim 0.64\text{--}0.59 \mu\text{m}$	$\sim 16,000\text{--}17,000$
yellow	$\sim 0.59\text{--}0.56 \mu\text{m}$	$\sim 17,000\text{--}18,000$
green	$\sim 0.56\text{--}0.49 \mu\text{m}$	$\sim 18,000\text{--}20,000$
blue	$\sim 0.49\text{--}0.45 \mu\text{m}$	$\sim 20,000\text{--}22,000$
violet	$\sim 0.45\text{--}0.40 \mu\text{m}$	$\sim 22,000\text{--}25,000$
ultraviolet	$< 0.40 \mu\text{m}$	$> 25,000$

All you need to think about is  
**shortwave** vs. **longwave** radiation.

# Shortwave and longwave:

- **Shortwave:**
  - Near-infrared, visible, ultraviolet
  - $\lambda < 3\mu\text{m}$
  - $n > 3, 300\text{cm}^{-1}$  (cycles per centimeter)
- **Longwave:**
  - Mid-infrared, far-infrared
  - $\lambda > 3\mu\text{m}$
  - $n < 3, 300\text{cm}^{-1}$

More on this in the next class ...



# 4 Laws of Radiation

1. All objects continually radiate energy
2. Hotter objects are brighter
3. Hotter objects radiate at shorter wavelengths
4. Objects that are good absorbers are also good emitters
  - Black objects emit & absorb the most
  - Transparent and white objects emit & absorb the least

# Blackbody Radiation

# Blackbody Radiation

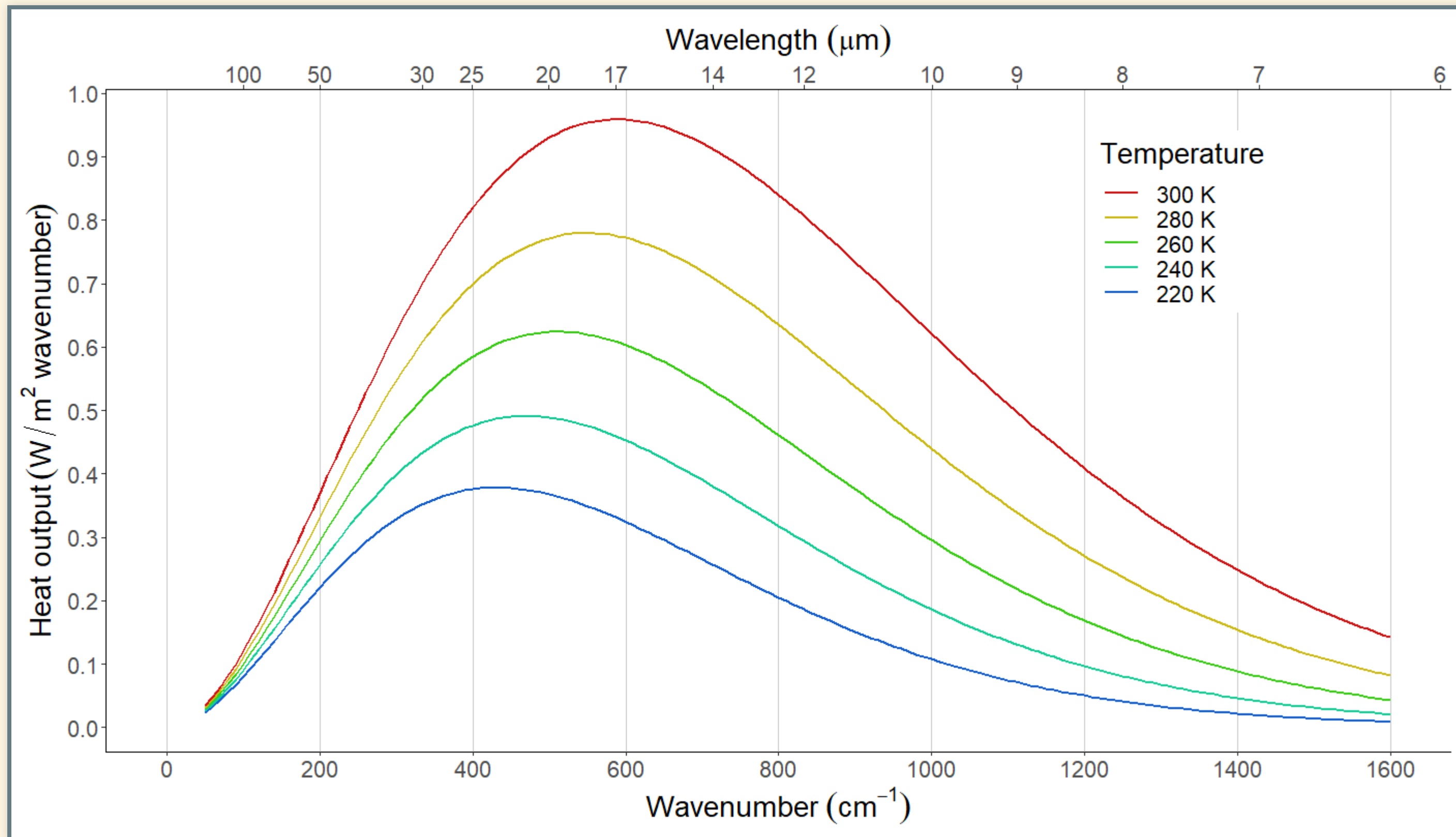
**Emissivity** ( $\varepsilon$ ) measures how black something is:

- $\varepsilon = 1$  for perfectly black
- $\varepsilon = 0$  for perfectly white or transparent
- In between for gray.
- Black, white, and gray:  $\varepsilon$  is the same for all wavelengths.
- Colored objects:  $\varepsilon$  is a function of wavelength.
- **For simplicity:** start by assuming everything is black, white, or gray.

**Remember:** Good emitters are good absorbers

**Fundamental rule:** Temperature and emissivity determine radiation.

# Heating Up: What Changes??



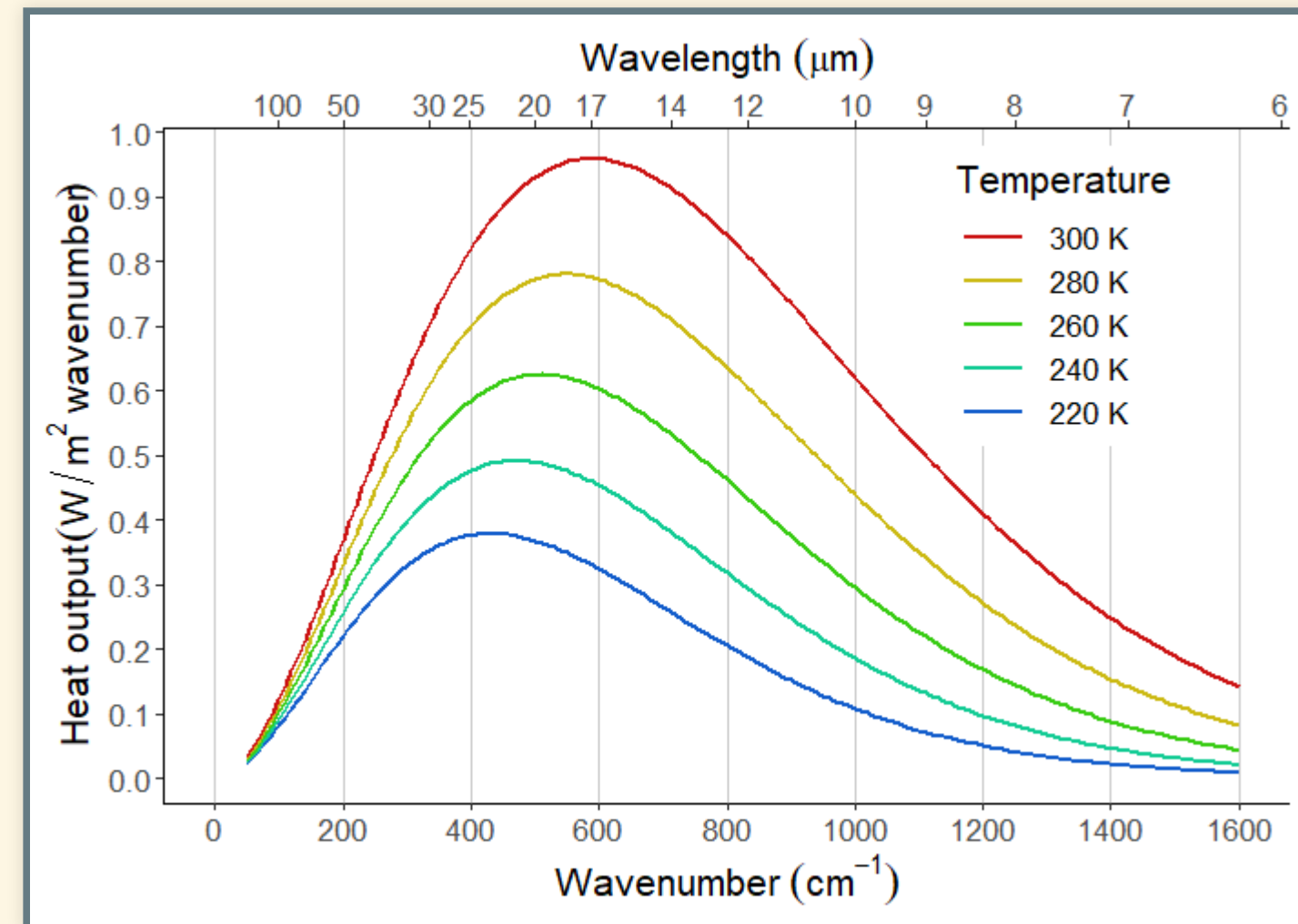
# Heating Up: What Changes?

- Hotter temperature:
  - Brighter (greater intensity)
  - Bluer (greater wavenumber, shorter wavelength)

A curious thing:

- A hot black object glows with color!

**Total intensity =  
area under curve**



# Mathematical Description

# Blackbody Radiation

Intensity (brightness):

Stefan-Boltzmann law

$$I = \varepsilon \sigma T^4$$

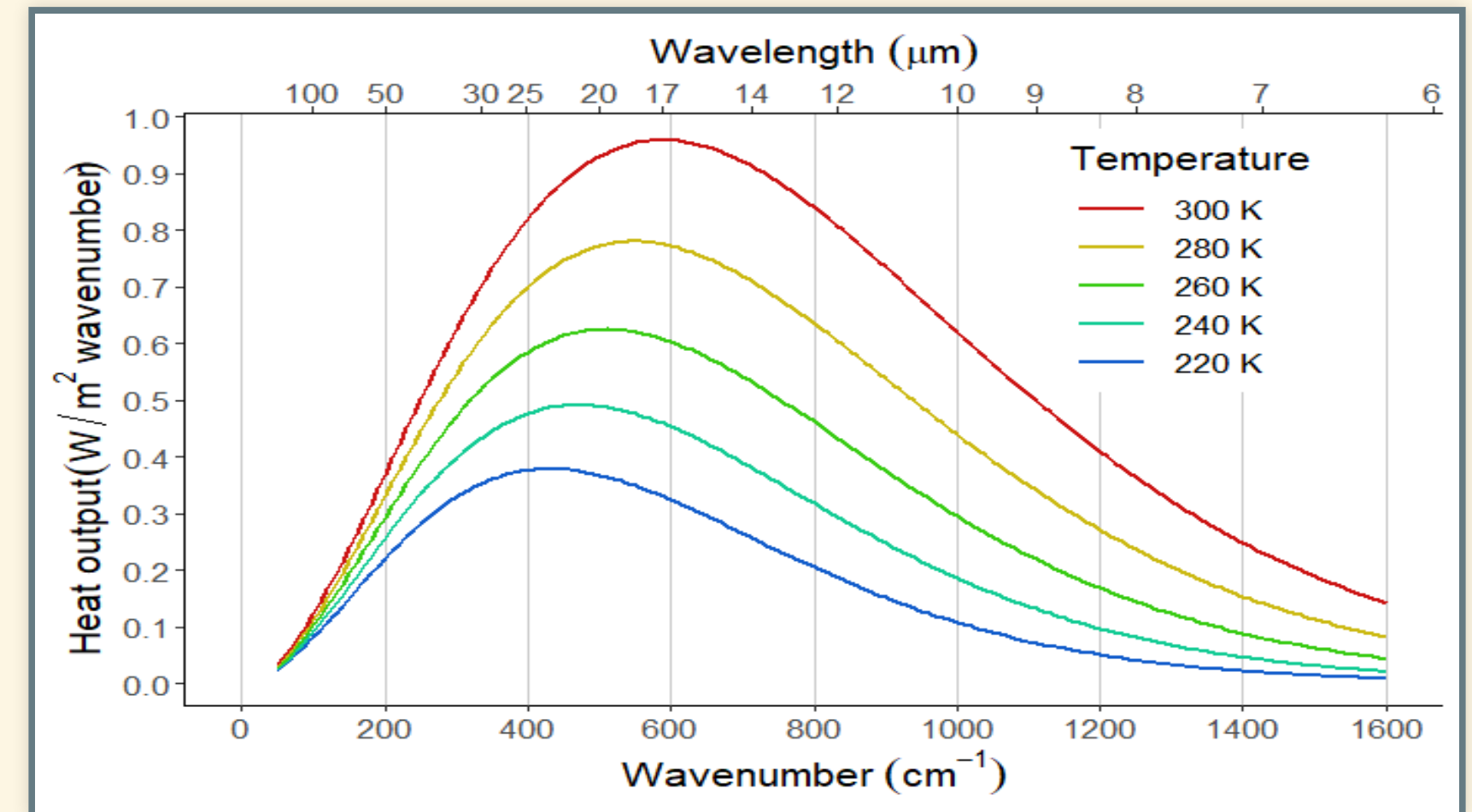
after Josef Stefan  
and Ludwig Boltzmann

- $\varepsilon$  = emissivity
  - Different for different objects.
- $\sigma$  = Stefan-Boltzmann constant.
- $T$  = absolute (Kelvin) temperature.

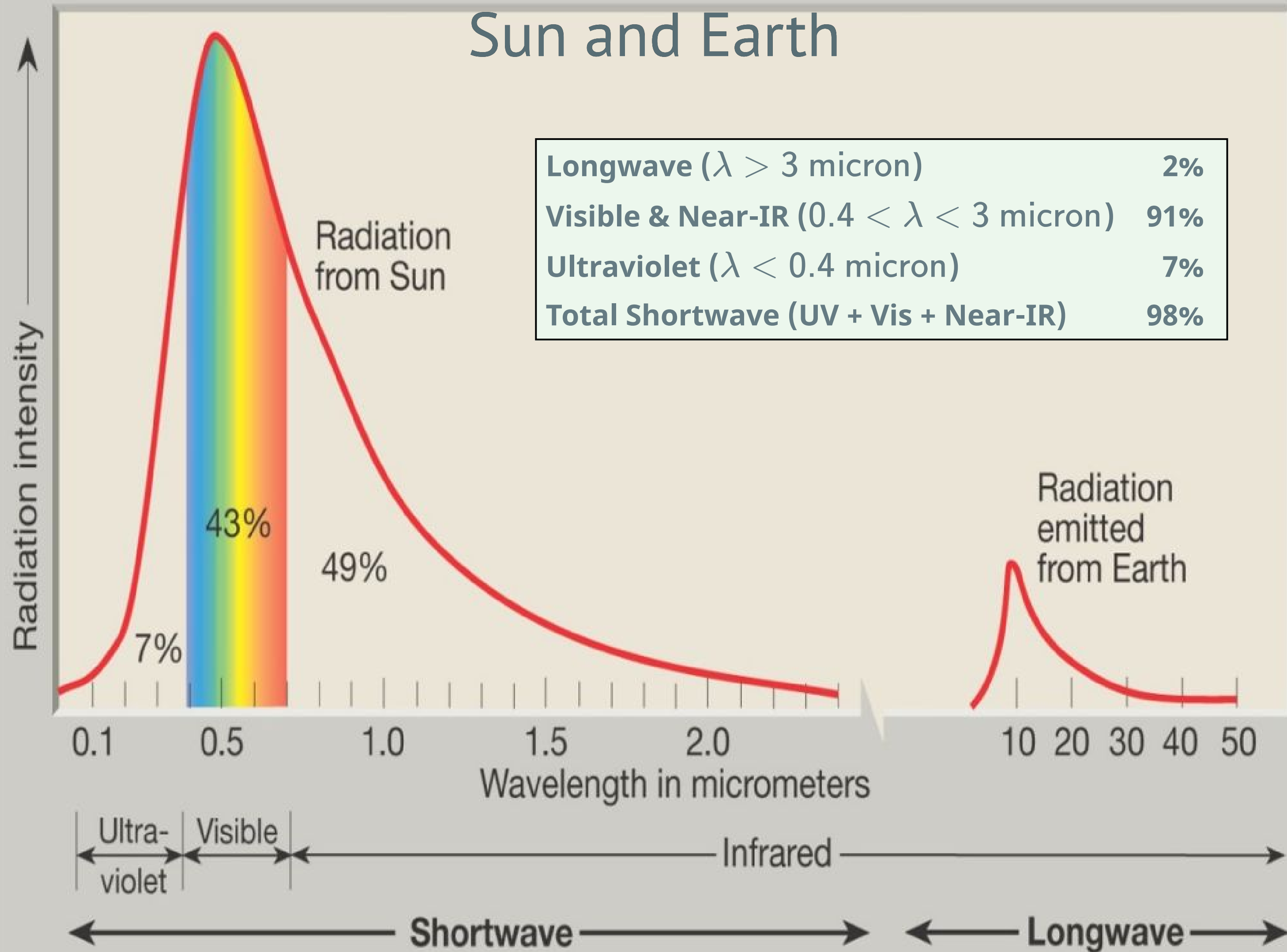
**Color:** Peak wavenumber proportional to (Kelvin) temperature.

**Helpful Hint:**

Fourth power on a calculator: press the  $x^2$  button twice.

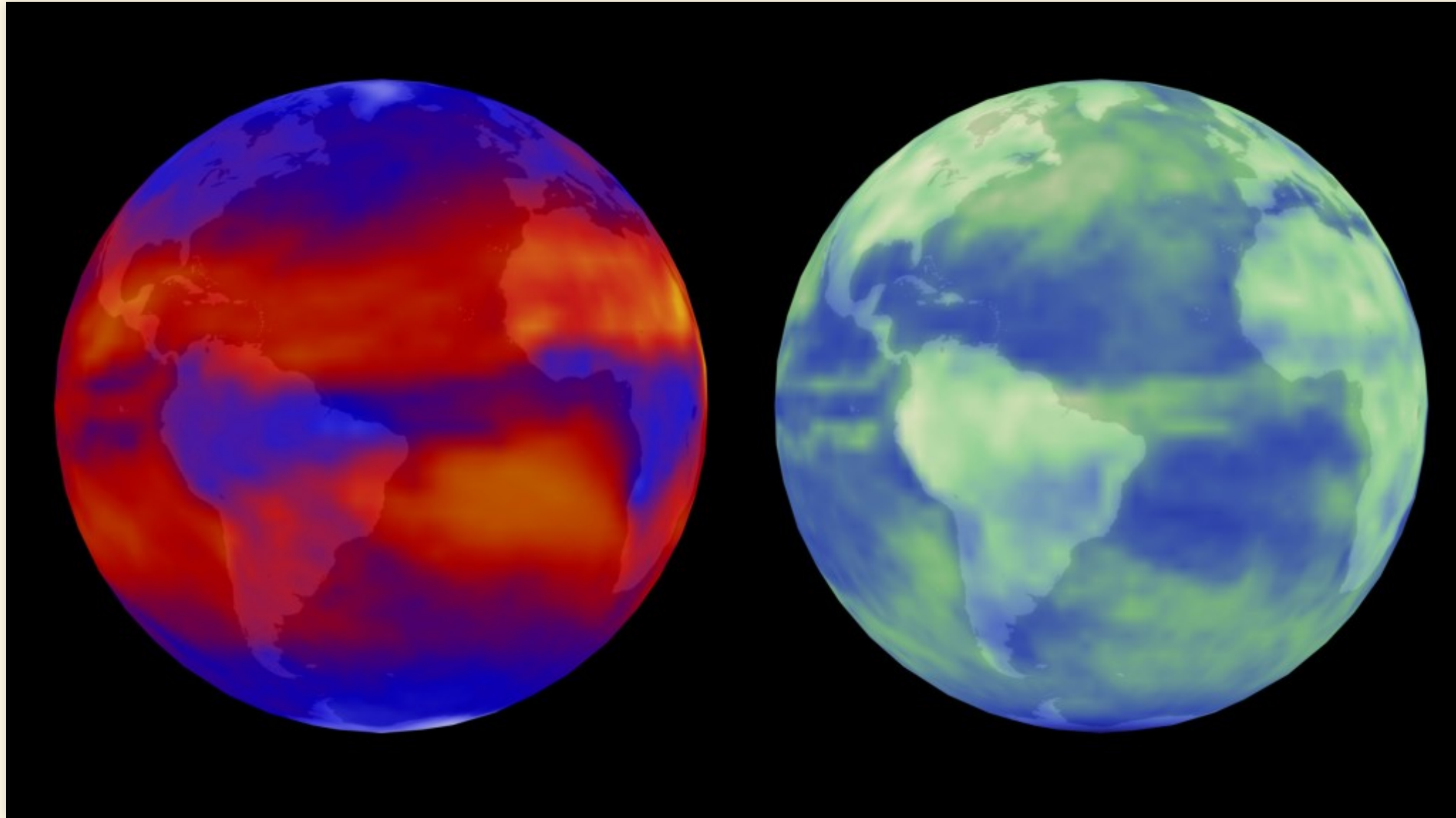


# Sun and Earth





# Earth and Radiation



False-color images of radiation from Earth, seen by NASA Terra satellite:

- Left: Thermal radiation (blue → red → yellow = dim → bright)
- Right: Reflected sunlight (blue → green → white = dim → bright)

# Efficiency of Light Bulbs

Type of Bulb	Efficiency
Standard 40W	1.8%
Standard 60W	2.1%
Standard 100W	2.6%
Quartz Halogen	3.5%
Ideal black body @ 7000K	14.0%
Compact Fluorescent	8–12%
LED	20–44%

- 7000K is the optimal temperature for a black body to emit visible light, but it will melt every known substance.
- Standard light bulbs operate at around 2000–3300 K.

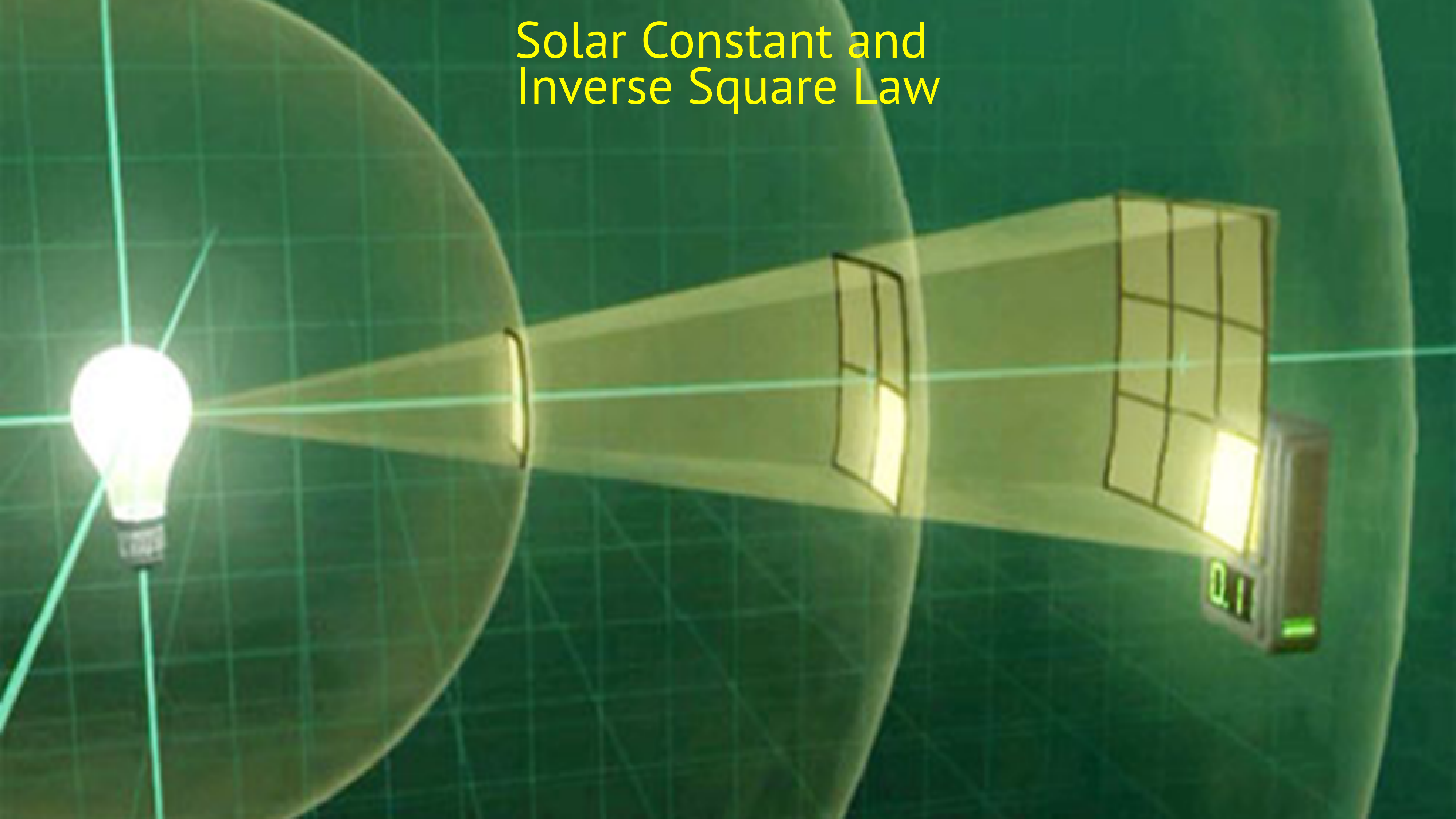
# Calculating Earth's Temperature: Bare-Rock Model

# Basics

## Steady Temperature

- Heat in must balance heat out
- **Total Heat Flux (Power) = Area  $\times$  Intensity**
  - Total heat flux in ( $F_{\text{in}}$ ):
    - Intensity depends on solar constant and albedo
    - Does not depend on earth's temperature
  - Total heat flux out ( $F_{\text{out}}$ ):
    - Intensity depends on earth's temperature and emissivity
- Strategy:
  1. Figure out  $F_{\text{in}}$ .
  2. Figure out temperature  $T$  that makes  $F_{\text{out}} = F_{\text{in}}$ .

# Solar Constant and Inverse Square Law

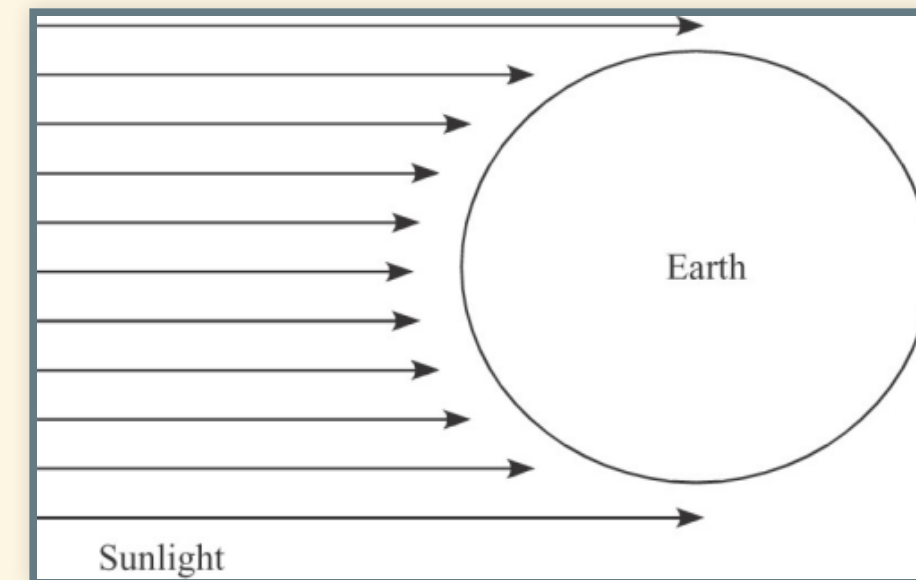


# What is $F_{\text{in}}$ ?

- $F_{\text{in}} = \text{Area} \times \text{Intensity absorbed}$ 
  - Intensity absorbed  $= (1 - \alpha) \times I_{\text{in}}$ 
    - $I_{\text{in}} = 1350 \text{ W/m}^2$
    - Average albedo  $\alpha = 0.30$  (30% of sunlight is reflected)

## What is area?

- Area = silhouette or shadow
- Circle:  $\pi r^2$

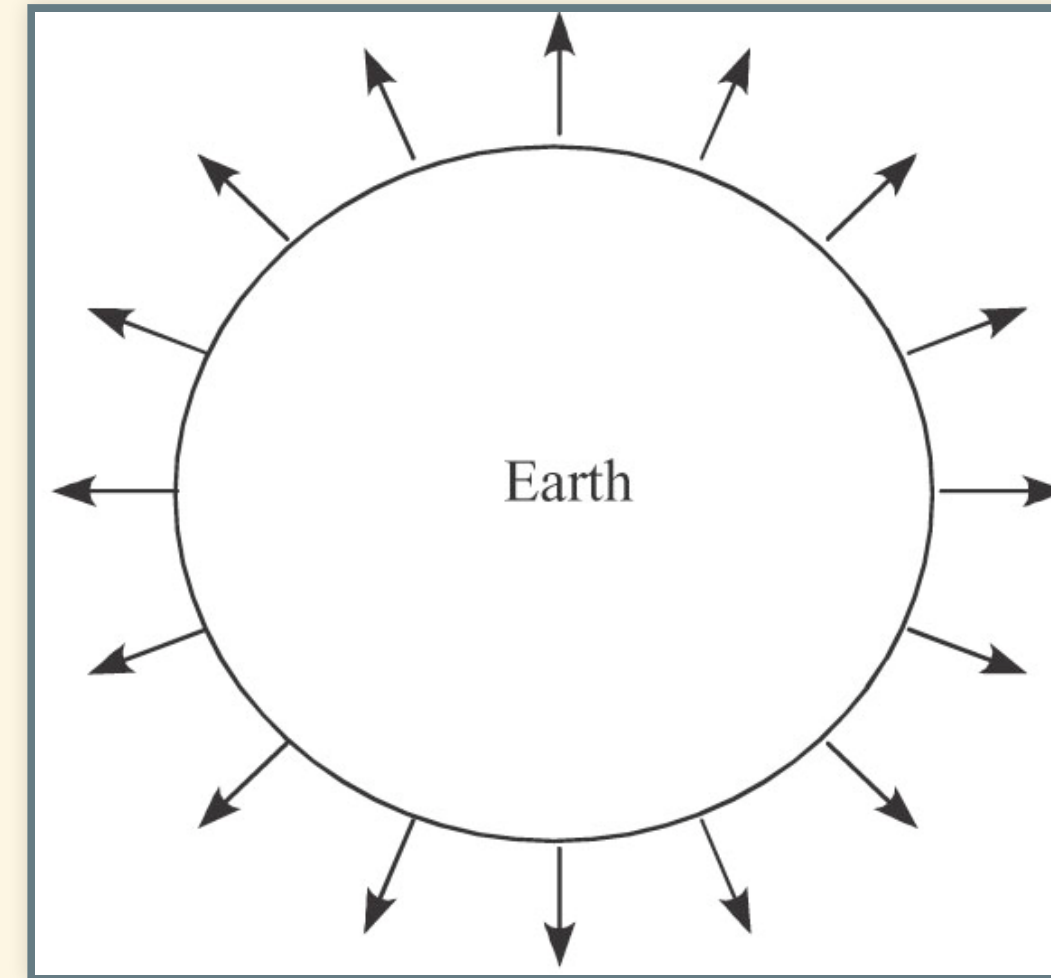


# What is $F_{\text{in}}$ ?

- $F_{\text{in}} = \pi r_{\text{Earth}}^2 \times (1 - \alpha) I_{\text{in}}$ 
  - $\pi r^2 = 1.3 \times 10^{14} \text{ m}^2$
  - $\alpha = 0.30 \Rightarrow (1 - \alpha) = 0.70$
  - $I_{\text{in}} = 1350 \text{ W/m}^2$
- $F_{\text{in}} = 1.2 \times 10^{17} \text{ Watt}$ 
  - 11,000 times total human energy production.

# What is $F_{\text{out}}$ ?

- $F_{\text{out}} = \text{Area} \times I_{\text{out}}$ 
  - $I_{\text{out}} = \varepsilon \sigma T^4$ 
    - $\varepsilon = 1$  (blackbody)
    - $\sigma = 5.67 \times 10^{-8} \text{ W/m}^2/\text{K}^4$
  - What is area?
    - Sphere:  $4\pi r^2$
- $F_{\text{out}} = 4\pi r_{\text{earth}}^2 \times \varepsilon \sigma T^4$





# Putting it all together

$$F_{\text{out}} = F_{\text{in}}$$

$$4\pi r^2 \times \varepsilon\sigma T^4 = \pi r^2(1 - \alpha)l_{\text{in}}$$

$$4\pi r^2 \times \varepsilon\sigma T^4 = \pi r^2(1 - \alpha)l_{\text{in}}$$

$$4\varepsilon\sigma T^4 = (1 - \alpha)l_{\text{in}}$$

$$T^4 = \frac{(1 - \alpha)l_{\text{in}}}{4\varepsilon\sigma}$$

$$T = \sqrt[4]{\frac{(1 - \alpha)l_{\text{in}}}{4\varepsilon\sigma}}$$

# Temperature of Earth

- Steady Temperature:
  - Heat flux in must balance heat flux out ( $F_{\text{out}} = F_{\text{in}}$ ).
  - $F_{\text{in}}$ :
    - Does not depend on earth's temperature.
    - Depends on solar constant and earth's albedo.
  - $F_{\text{out}}$ :
    - Depends on earth's temperature.
  - $T$  adjusts until heat out = heat in

## Helpful hint:

To take the fourth root on a calculator, press the square-root key ( $\sqrt{\phantom{x}}$ ) twice.

$$T = \sqrt[4]{\frac{(1 - \alpha) I_{\text{in}}}{4\epsilon\sigma}}$$



# Temperature of Earth

$$T = \sqrt[4]{\frac{(1 - \alpha) I_{\text{in}}}{4\varepsilon\sigma}}$$

## Earth:

(Note: My numbers are slightly different from Archer's textbook)

- $I_{\text{in}} = 1350 \text{ W/m}^2$
- $\alpha = 0.30$
- $\varepsilon = 1$
- $\sigma = 5.67 \times 10^{-8} \text{ W/(m}^2\text{K}^4)$
- Calculate  $T$ :
- $T = 254 \text{ K} = -19^\circ\text{C} = -2^\circ\text{F}.$

If the sun got 5% brighter,  
how much warmer would the earth become?

$$T = \sqrt[4]{\frac{(1 - \alpha) I_{\text{in}}}{4\epsilon\sigma}}$$

- Normal:  $I_{\text{in}} = 1350 \text{ W/m}^2$ :
  - $T = 254 \text{ K}$
- 5% Brighter:  $I_{\text{in}} = 1.05 \times 1350 \text{ W/m}^2 = 1418 \text{ W/m}^2$ :
  - $T = 257 \text{ K}$
- $\Delta T = 3 \text{ K} = 6^\circ\text{F}$

# Temperature of Earth

$$T = \sqrt[4]{\frac{(1 - \alpha) I_{\text{in}}}{4\varepsilon\sigma}}$$

Earth:

(Note: My numbers are slightly different from Archer's textbook)

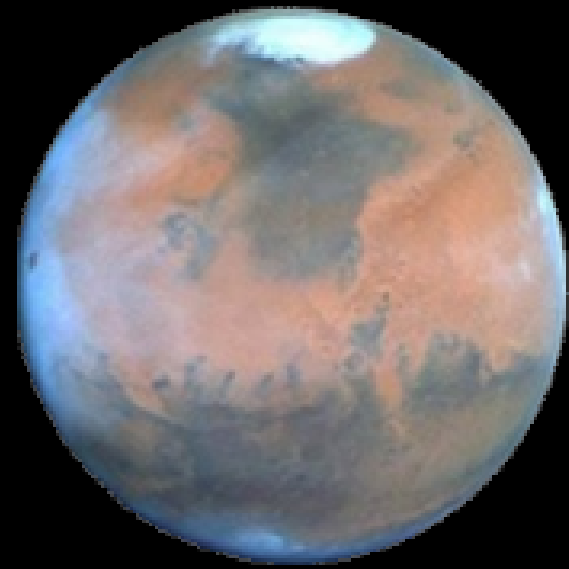
- $I_{\text{in}} = 1350 \text{ W/m}^2$
- $\alpha = 0.30$
- $\varepsilon = 1$
- $\sigma = 5.67 \times 10^{-8} \text{ W/(m}^2\text{K}^4)$
- $T = 254 \text{ K} = -19^\circ\text{C} = -2^\circ\text{F}.$

How does this compare to Earth's actual temperature?

# Radiative Temperature

- Satellites orbiting in space can measure longwave radiation from earth
- To the satellites, the earth looks very much like a blackbody at the bare-rock temperature (254 K).
- Thus, scientists generally call the bare-rock temperature the **radiative temperature** because it describes the radiation coming off the earth.
- However, the surface temperature of the earth is around  $295\text{ K} = 71^{\circ}\text{F}$ , which is significantly different from the radiative, or bare-rock, temperature.

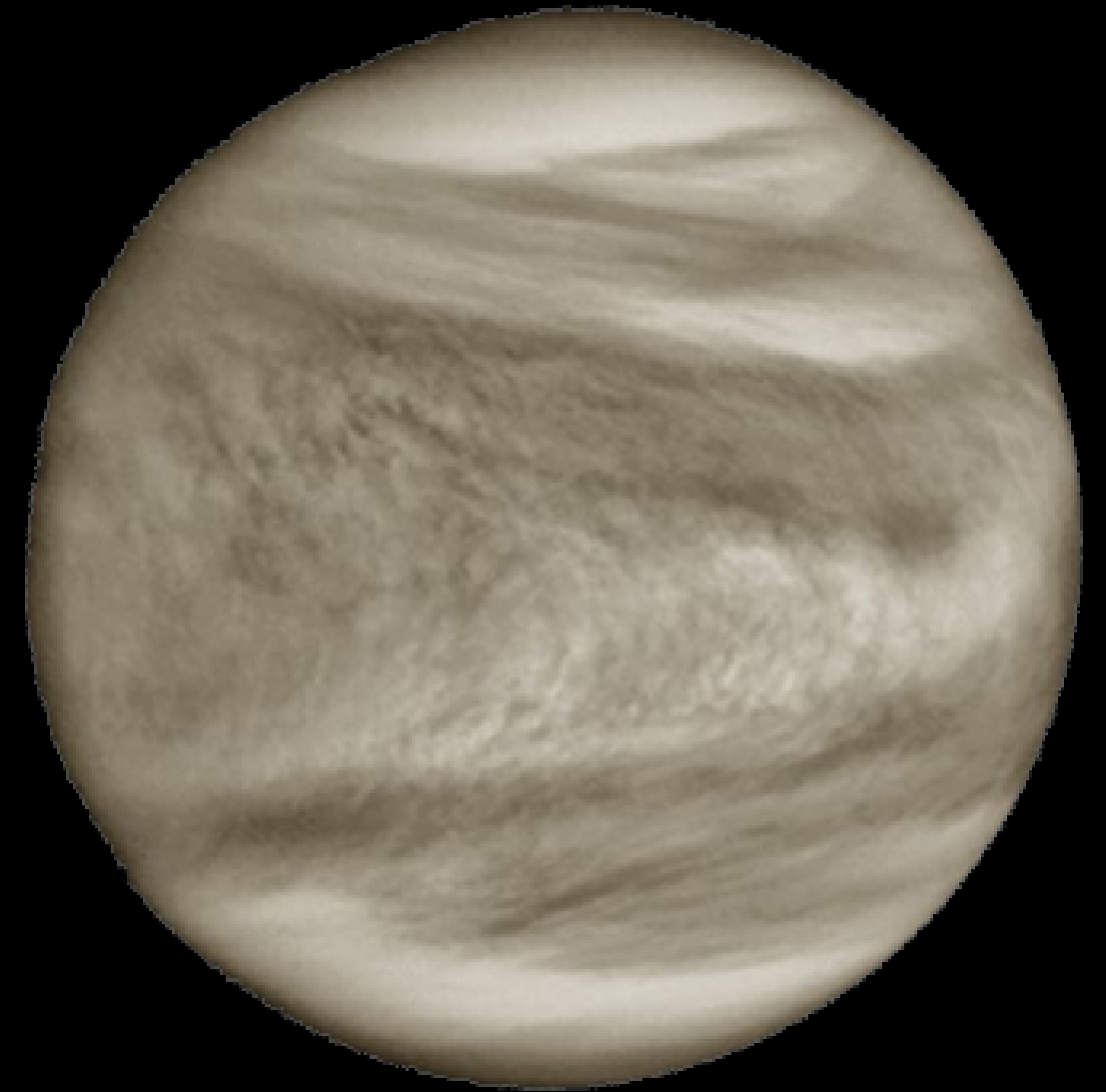
# The Terrestrial Planets



Mars  
240 K



Earth  
295 K



Venus  
700 K



# Terrestrial Planets

	Earth	Mars	Venus
Distance from sun	1 AU	1.5 AU	0.72 AU
$1/\text{Distance}^2$	1.00	0.44	1.9
Solar constant	1350 W/m <sup>2</sup>	600 W/m <sup>2</sup>	2604 W/m <sup>2</sup>
Albedo	0.30	0.17	0.71
$T_{\text{bare rock}}$	254 K (−2°F)	216 K (−70°F)	240 K (−27°F)
$T_{\text{surface}}$	295 K (71°F)	240 K (−28°F)	700 K (800°F)
$\Delta T$	41 K (74°F)	24 K (42°F)	460 K (828°F)

- Total flux (power) radiated from sun doesn't change with distance.
- At a distance  $r$  total flux spreads over sphere of radius  $r$
- Intensity = Total Flux / Area:
  - Proportional to  $1/r^2$ .
- At edge of Earth's atmosphere, solar intensity = 1350 W/m<sup>2</sup>.