

Introducing the Greenhouse Effect

EES 3310/5310

Global Climate Change

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Class #4: Monday, Feb. 1 2021

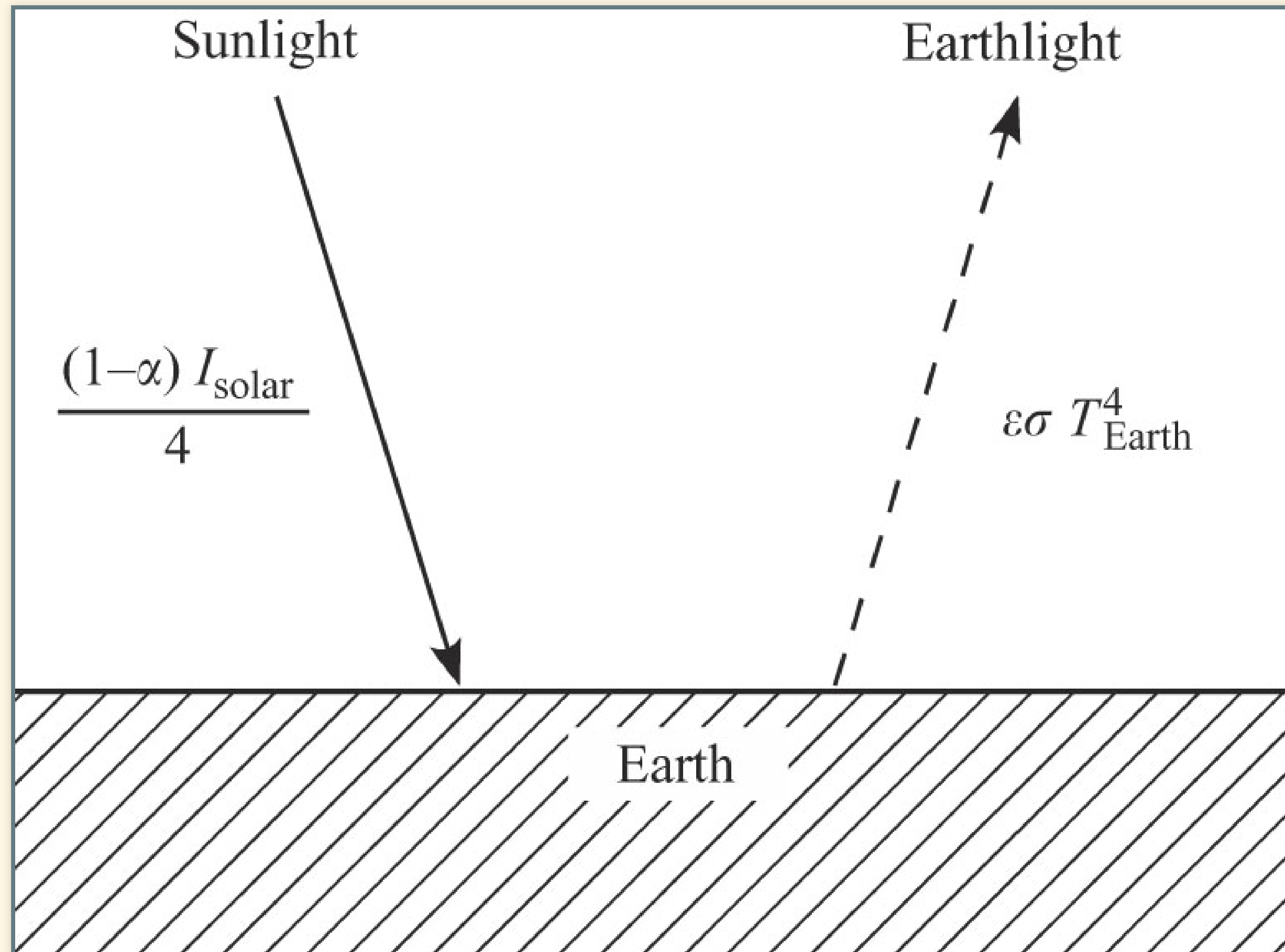
Basic Principles from Friday

- **Steady temperature means:**
 - $\text{Heat}_{\text{out}} = \text{Heat}_{\text{in}}$
- **Heat in:**
 - Sunlight (**shortwave**)
 - Does not depend on temperature
- **Heat out:**
 - Emitted radiation (**longwave**)
 - Depends on temperature
- If $\text{Heat}_{\text{out}} \neq \text{Heat}_{\text{in}}$,
 - Temperature rises or falls until

$$\text{Heat}_{\text{out}} = \text{Heat}_{\text{in}}$$

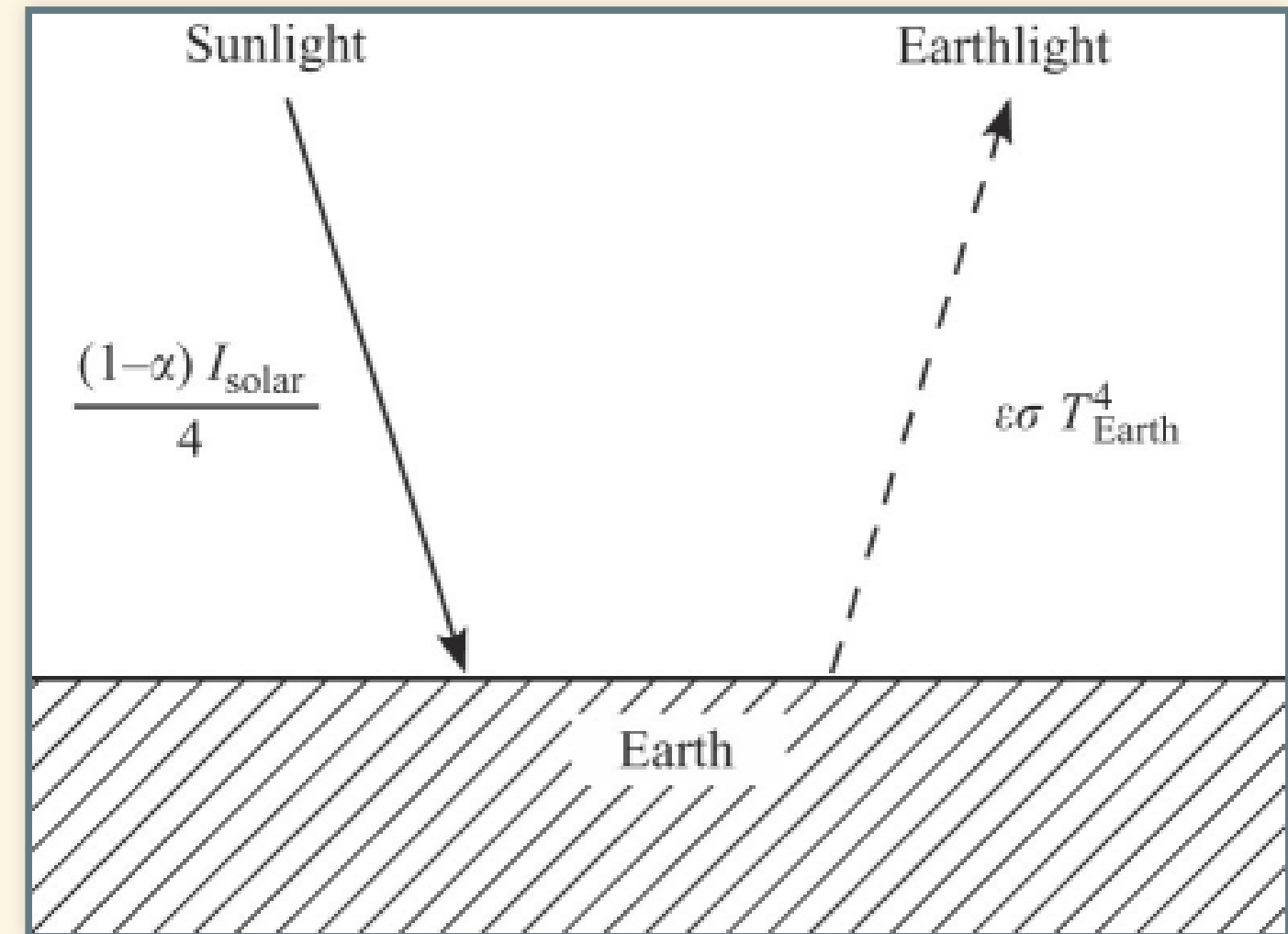
Temperature of the Earth

Bare-Rock Model: No Atmosphere



A subtle point...

- Emissivity ε is fraction absorbed
- Albedo α is fraction reflected
- For an opaque surface, $\alpha + \varepsilon = 1$
- So how is $\alpha = 0.30$ and $\varepsilon = 1.00$?
- α & ε are different for shortwave & longwave.
- Shortwave: $\alpha = 0.30$, $\varepsilon = 0.70$
- Longwave: $\alpha = 0.00$, $\varepsilon = 1.00$



Temperature of Earth (Bare Rock Model)

1. $F_{\text{out}} = F_{\text{in}}$ (Heat flux balances)

2. On average,

$$F_{\text{in}} = \frac{(1 - \alpha)}{4} I_{\text{solar}}$$

3. $F_{\text{out}} = \varepsilon \sigma T^4$.

4. Solve for T :

$$T = \sqrt[4]{\frac{(1 - \alpha) I_{\text{solar}}}{4 \varepsilon \sigma}}$$

$$I_{\text{solar}} = 1350 \text{ W/m}^2$$

$$\alpha = 0.30$$

$$\varepsilon = 1$$

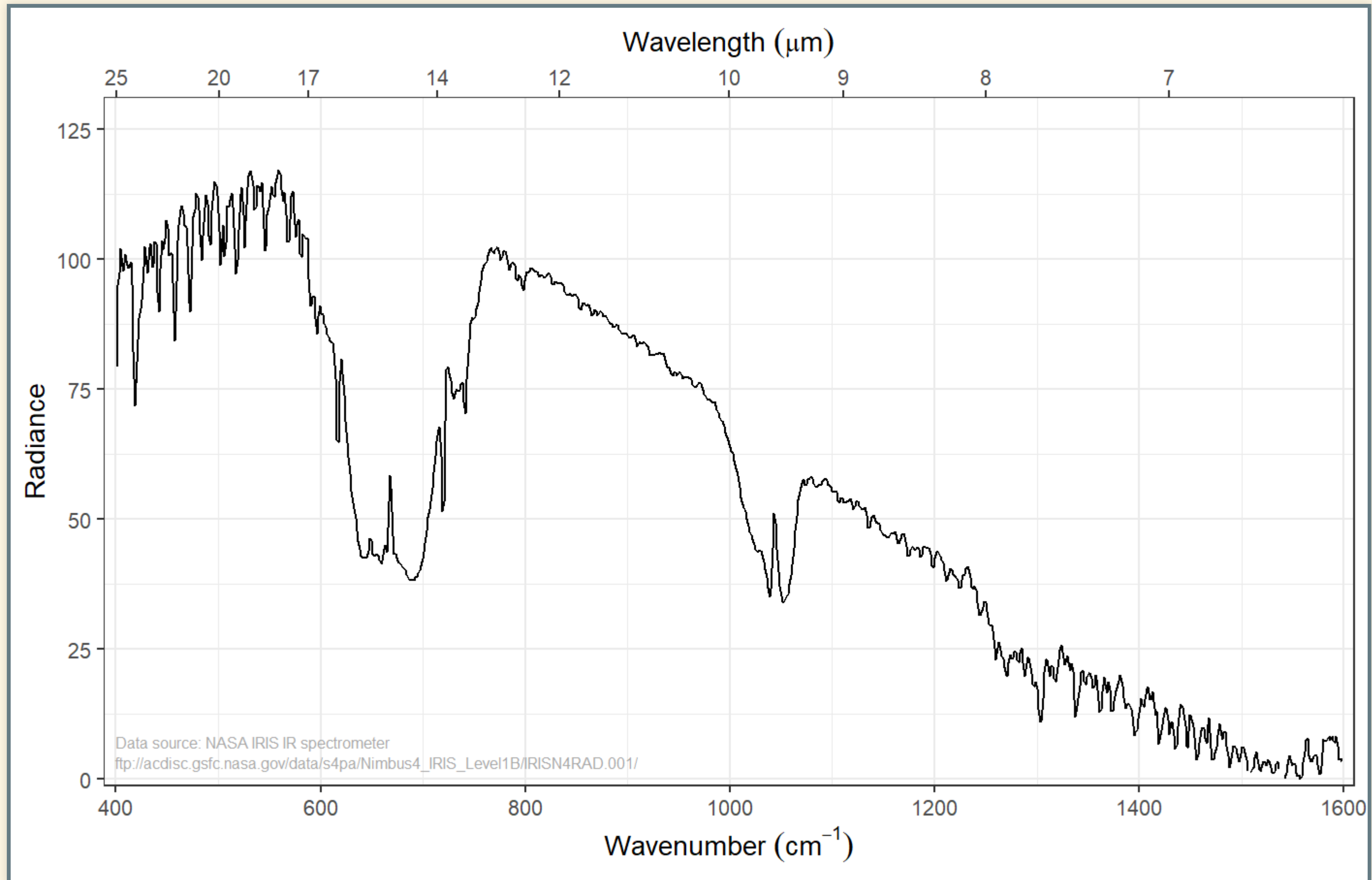
$$\sigma = 5.67 \times 10^{-8} \text{ W m}^{-2} \text{ K}^{-4}$$

$$T = 254 \text{ K} = -19^\circ \text{C} = -2^\circ \text{F}$$

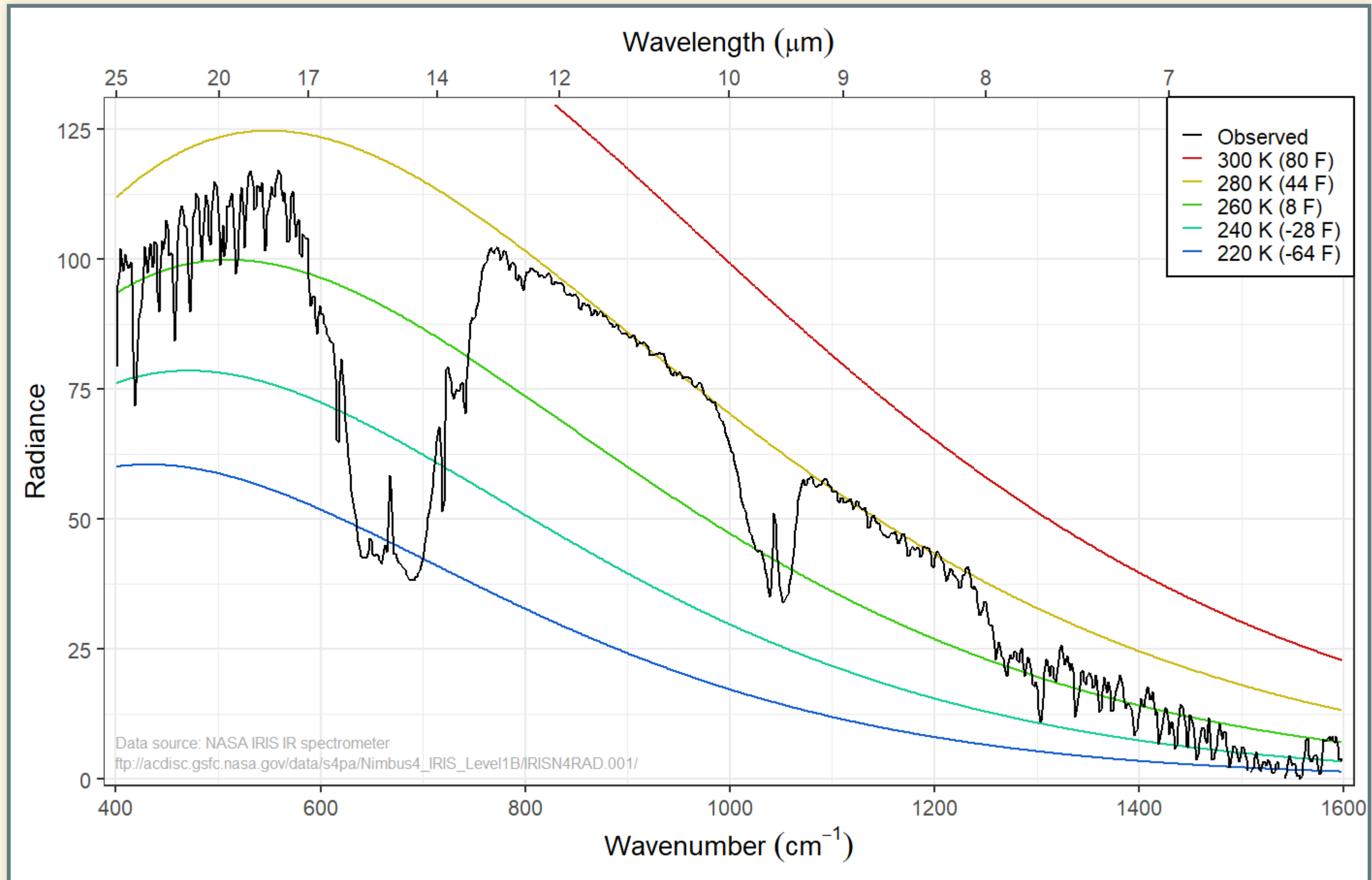
Terrestrial Planets

	Earth	Mars	Venus
Distance from sun	1 AU	1.5 AU	0.72 AU
1 / Distance ²	1.00	0.44	1.9
Solar constant	1350 W / m ²	600 W / m ²	2604 W / m ²
Albedo	0.30	0.17	0.71
$T_{\text{bare rock}}$	254 K (− 2 °F)	216 K (− 70 °F)	240 K (− 27 °F)
T_{surface}	295 K (71 °F)	240 K (− 28 °F)	700 K (800 °F)
Δ_T	41 K (74 °F)	24 K (42 °F)	460 K (828 °F)

Oops! We forgot the atmosphere!

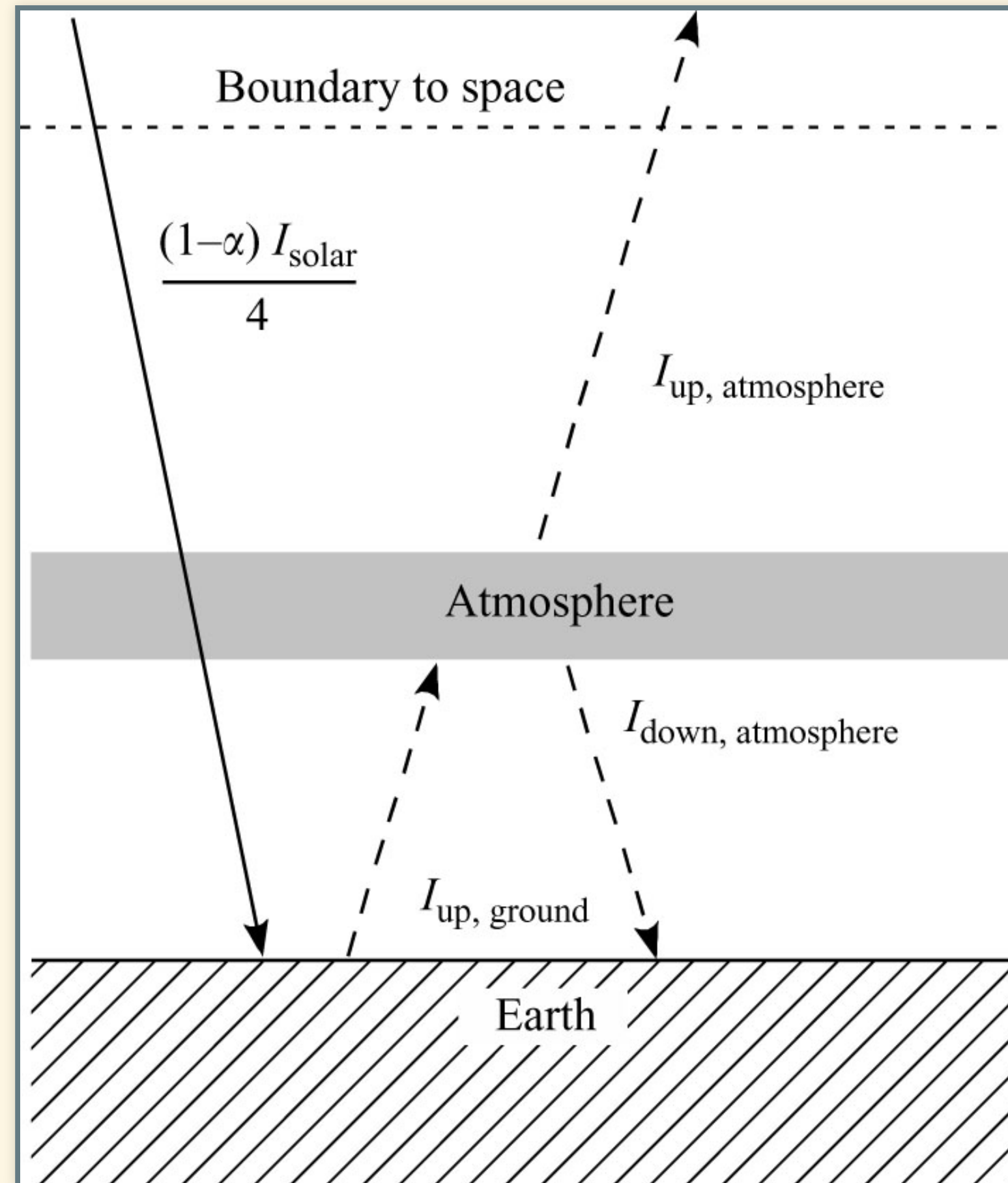


Does Earth look like a blackbody?

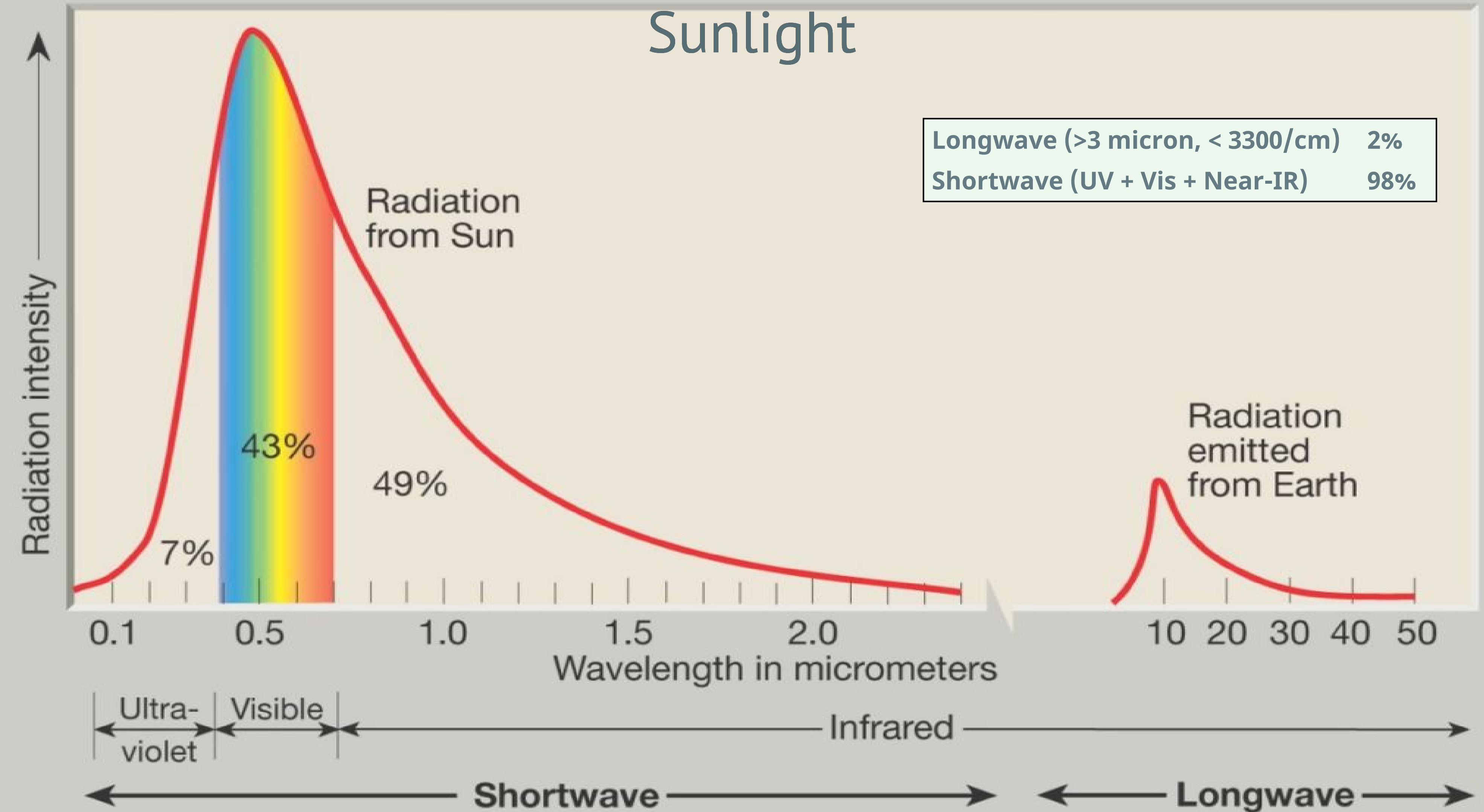


One-Layer Model of the Greenhouse Effect

Layer Model



Sunlight



Atmosphere

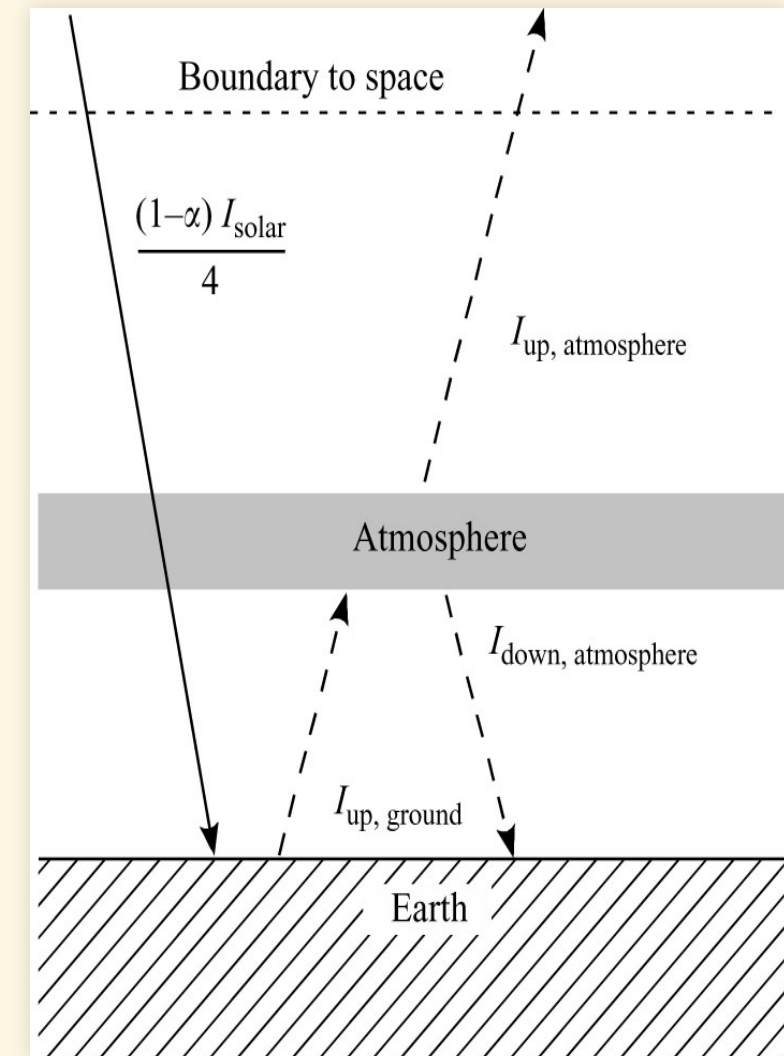
Make **simplifying assumptions**:

- Perfectly **transparent** to **shortwave** light
 - Like a pane of glass: $\varepsilon = 0$
- Perfectly **opaque** to **longwave** light
 - Like a blackbody: $\varepsilon = 1$

**Anything that
transmits most shortwave
and
absorbs most longwave
is a greenhouse gas**

Balance of energy for earth system

- Always start analyzing from the top down
 - Look at energy balance at the boundary to space, above the top of the atmosphere.



Balance of energy for earth system

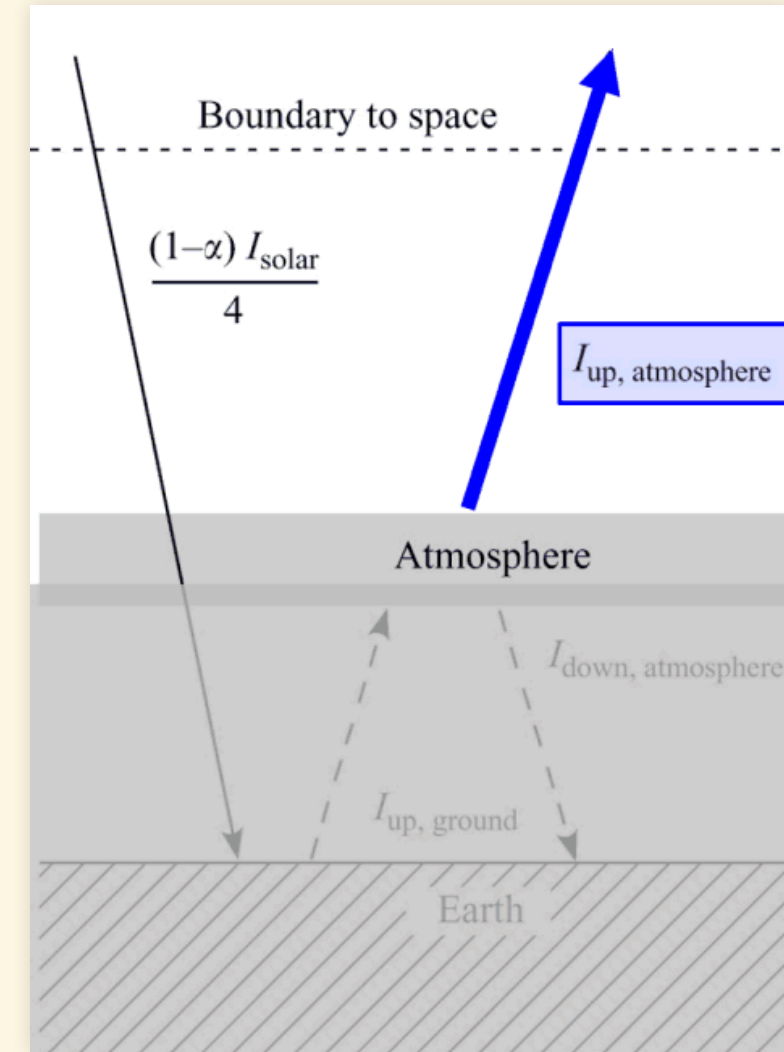
- At top of atmosphere: $F_{\text{out}} = F_{\text{in}}$

$$I_{\text{up, atmos}} = I_{\text{in}} \quad (\text{intensity of absorbed sunlight})$$

$$\varepsilon\sigma T_{\text{atmos}}^4 = \frac{(1 - \alpha)I_{\text{solar}}}{4}$$

- Aha! We can find T_{atmos} !

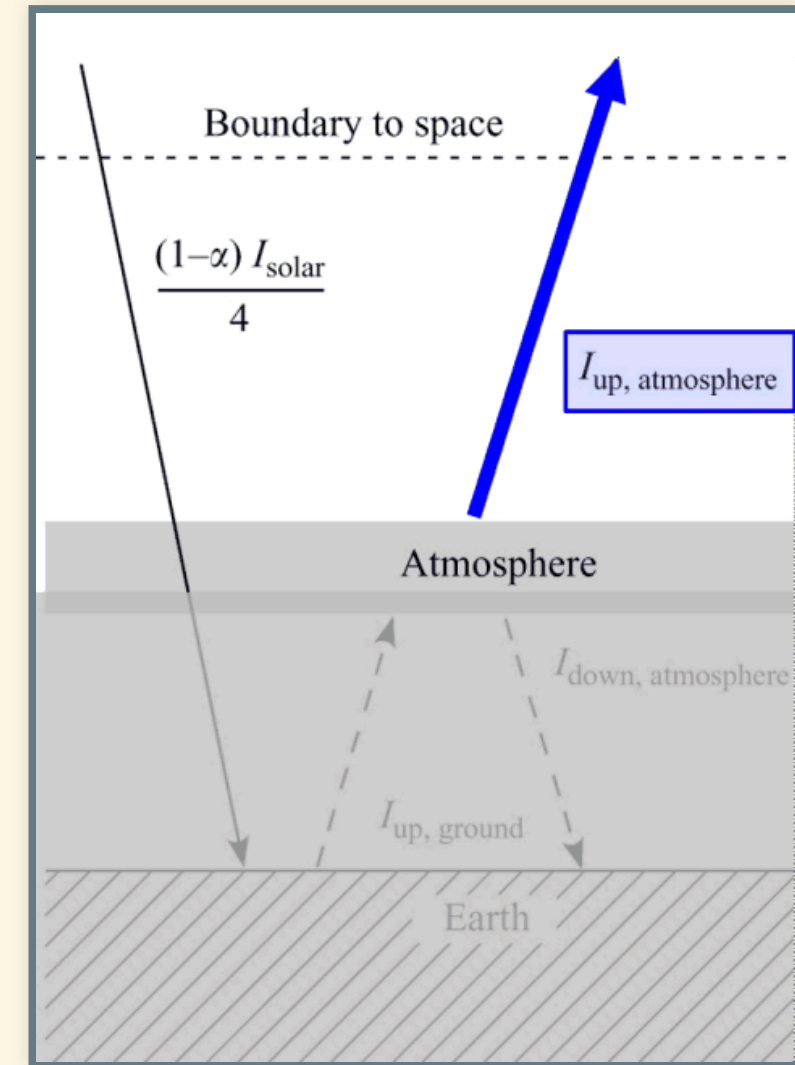
$$T_{\text{atmos}} = \sqrt[4]{\frac{(1 - \alpha)I_{\text{solar}}}{4\varepsilon\sigma}}$$



Balance of energy for earth system

$$T_{\text{atmos}} = \sqrt[4]{\frac{(1 - \alpha) I_{\text{solar}}}{4\varepsilon\sigma}}$$

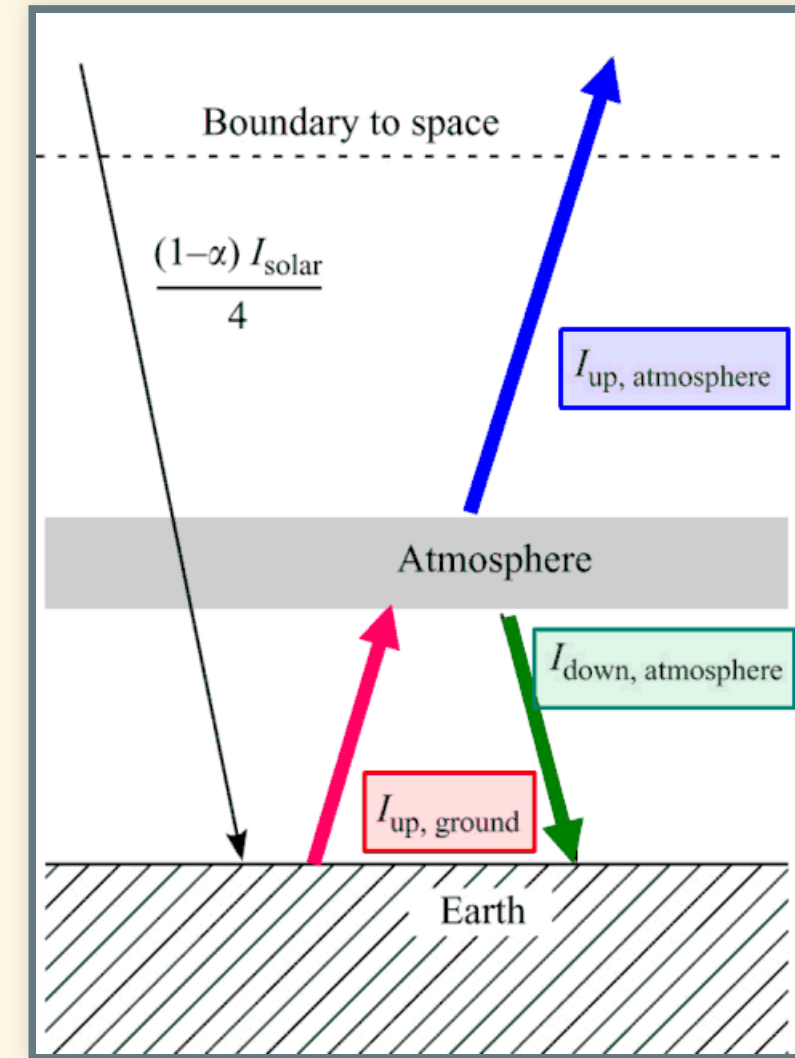
- Just like bare rock model!
- We call this the **skin temperature**



Balance of energy for atmosphere

Atmosphere: $\text{Heat}_{\text{in}} = \text{Heat}_{\text{out}}$

$$I_{\text{up,ground}} = I_{\text{up,atm}} + I_{\text{down,atm}}$$

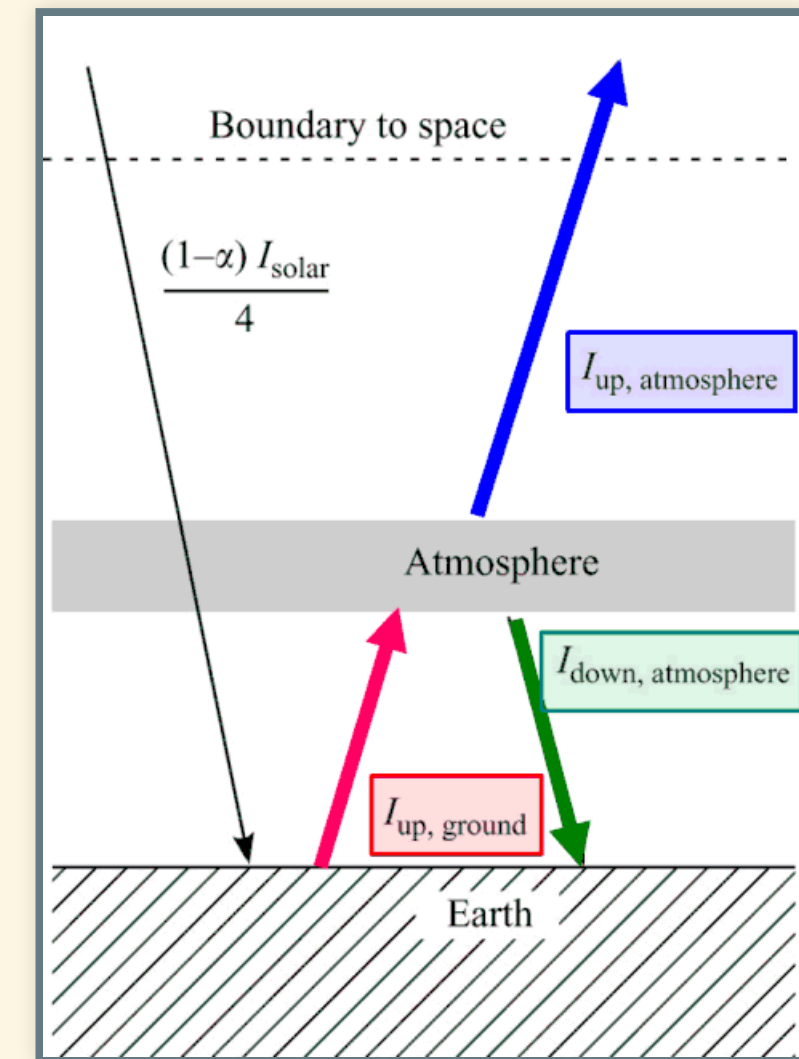


Balance of energy for atmosphere

Atmosphere: heat in = heat out.

$$I_{\text{up,ground}} = I_{\text{up,atm}} + I_{\text{down,atm}}$$

$$I_{\text{up,atm}} = I_{\text{down,atm}} = \varepsilon \sigma T_{\text{atm}}^4$$



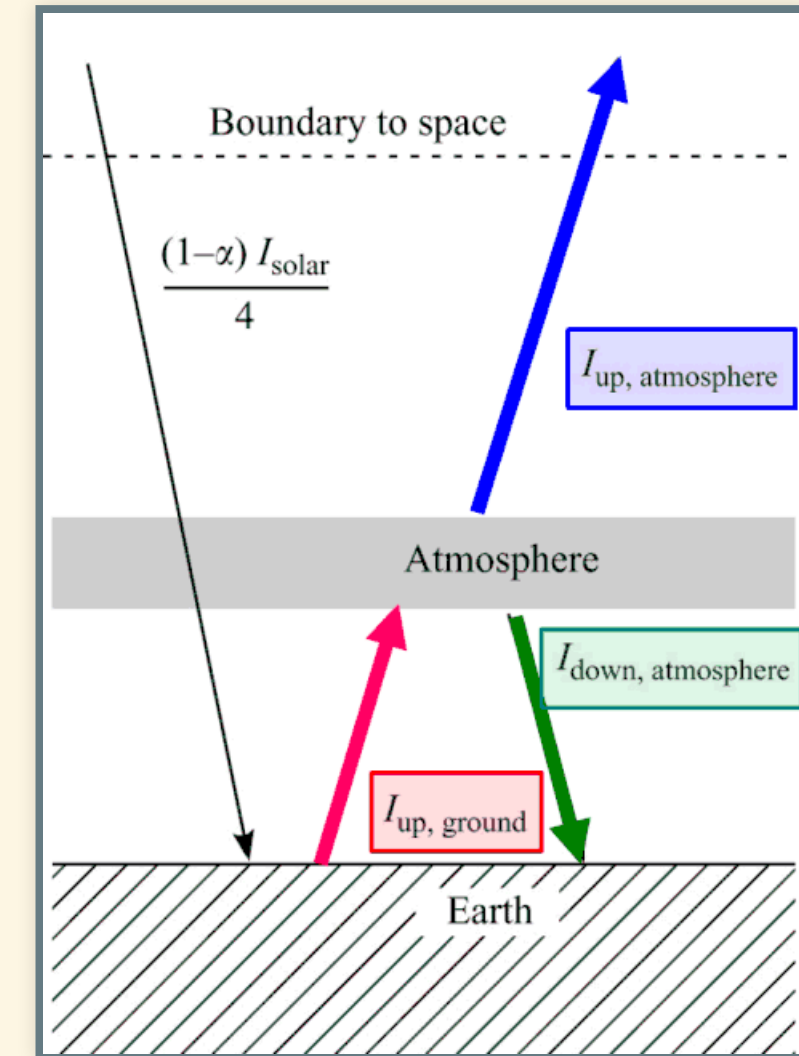
Balance of energy for atmosphere

Atmosphere: heat in = heat out.

$$I_{\text{up,ground}} = I_{\text{up,atm}} + I_{\text{down,atm}}$$

$$I_{\text{up,atm}} = I_{\text{down,atm}} = \varepsilon \sigma T_{\text{atm}}^4$$

$$I_{\text{up,ground}} = \varepsilon \sigma T_{\text{ground}}^4$$



Balance of energy for atmosphere

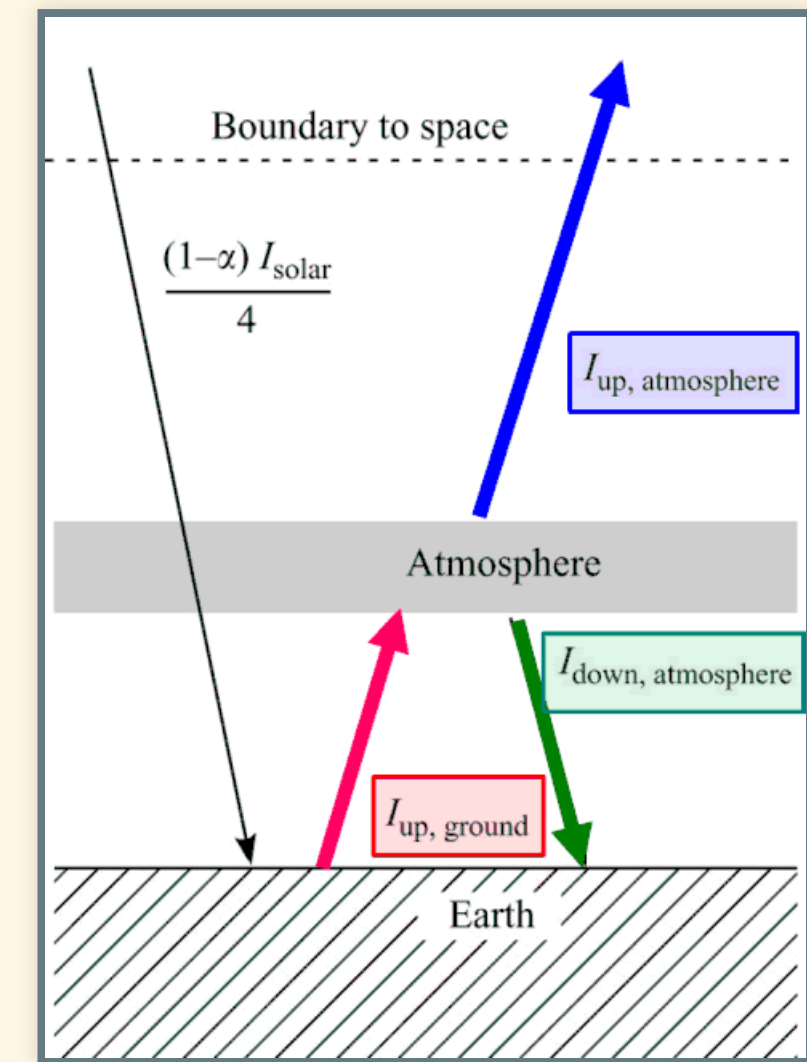
Atmosphere: heat in = heat out.

$$I_{\text{up,ground}} = I_{\text{up,atm}} + I_{\text{down,atm}}$$

$$I_{\text{up,atm}} = I_{\text{down,atm}} = \epsilon\sigma T_{\text{atm}}^4$$

$$I_{\text{up,ground}} = \epsilon\sigma T_{\text{ground}}^4$$

$$\epsilon\sigma T_{\text{ground}}^4 = 2\epsilon\sigma T_{\text{atm}}^4$$



Principles:

- Start at the top.
- For each layer, $\text{Heat}_{\text{out, up}} = \text{Heat}_{\text{out, down}}$
- Each layer balances $\text{Heat}_{\text{in, total}} = \text{Heat}_{\text{out, total}}$
 - Each layer has uniform temperature:
 - The **top** and **bottom** of the layer have the same temperature.
 - So the intensity emitted from the **top** and **bottom** is the same.
- The bottom layer of the atmosphere tells us $\text{Heat}_{\text{up, ground}}$
- Get ground temperature from $\text{Heat}_{\text{up, ground}}$

1, 8, 27, 64

Finish the problem

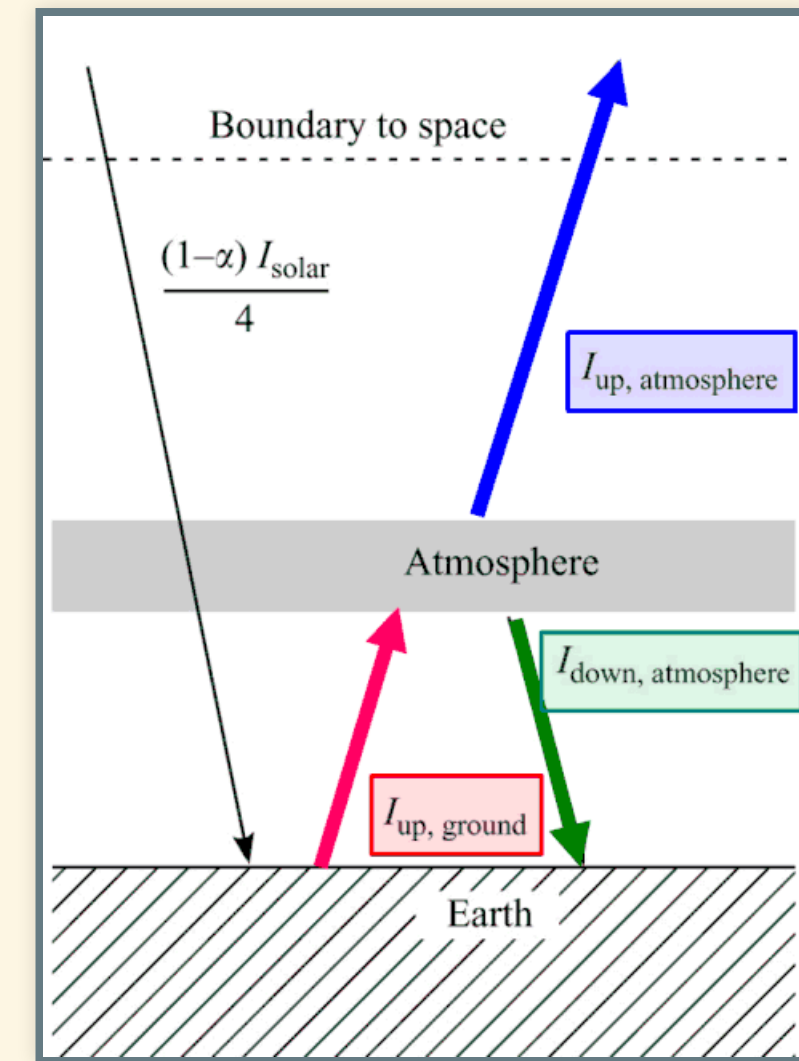
$$\varepsilon\sigma T_{\text{ground}}^4 = 2\varepsilon\sigma T_{\text{atm}}^4$$

$$T_{\text{ground}}^4 = 2T_{\text{atm}}^4$$

$$T_{\text{ground}} = \sqrt[4]{2} T_{\text{atm}} \\ = 1.19 T_{\text{atm}}$$

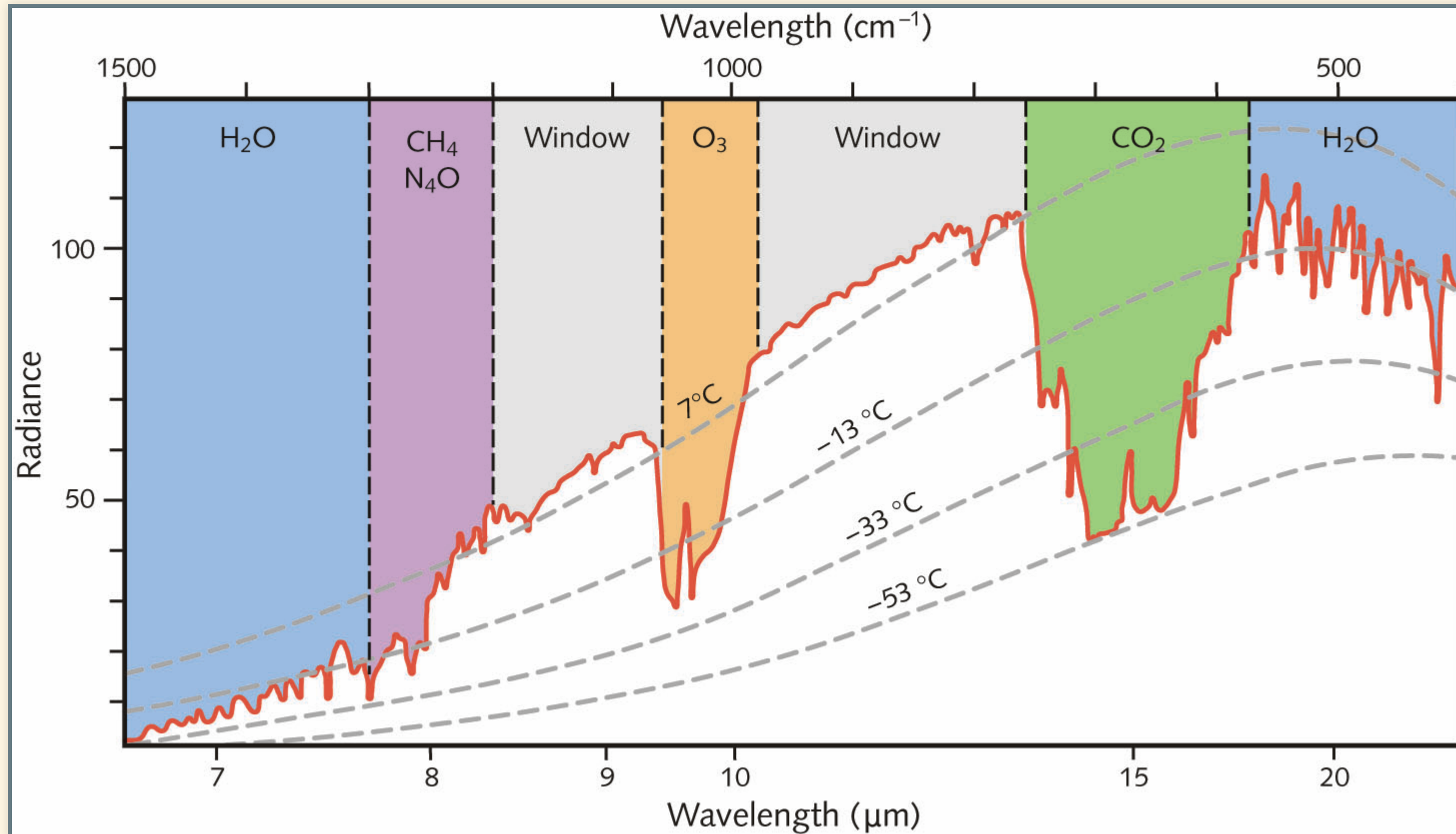
- Skin temp: $T_{\text{atm}} = T_{\text{skin}} = T_{\text{bare rock}} = 254 \text{ K}$
- Ground temp (1-layer): $T_{\text{ground}} = \sqrt[4]{2} T_{\text{atm}} = 302 \text{ K}$
- Difference: Greenhouse effect = 48 K

Note: These numbers are slightly different from what's in the book. Don't worry about that.

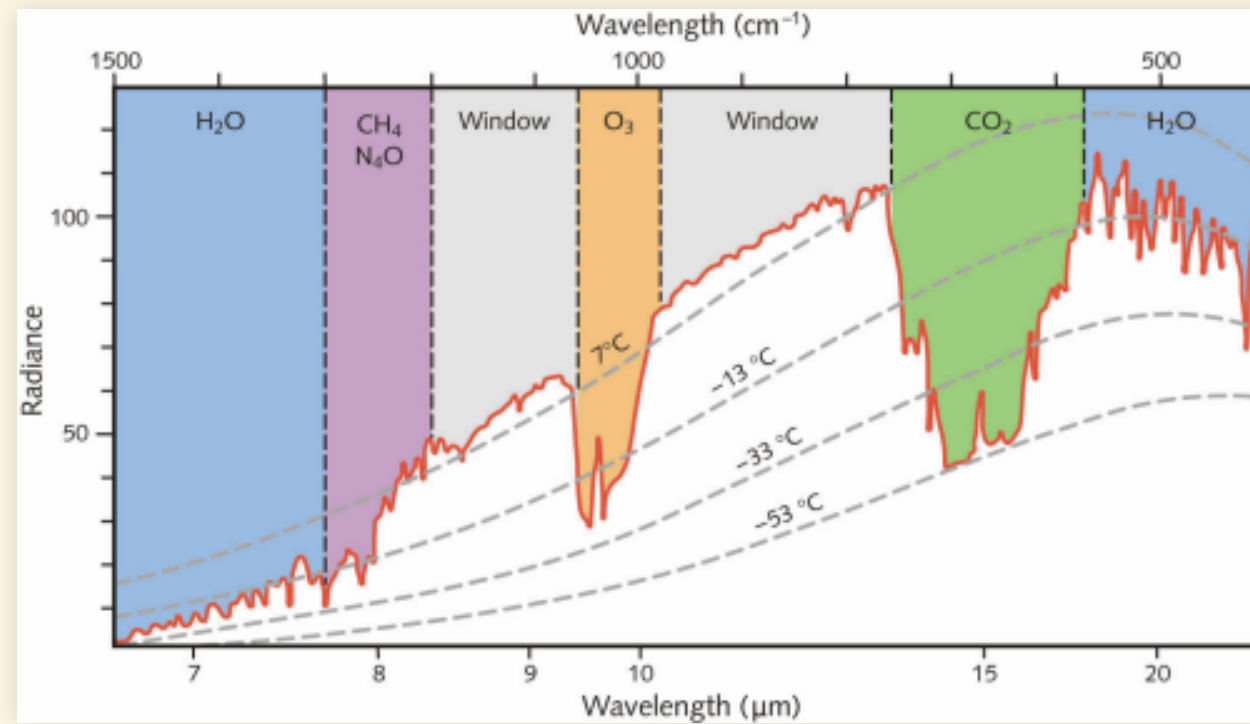


Greenhouse Gases

Greenhouse Gases



Greenhouse Gases



- Brightness: Stefan-Boltzmann law:

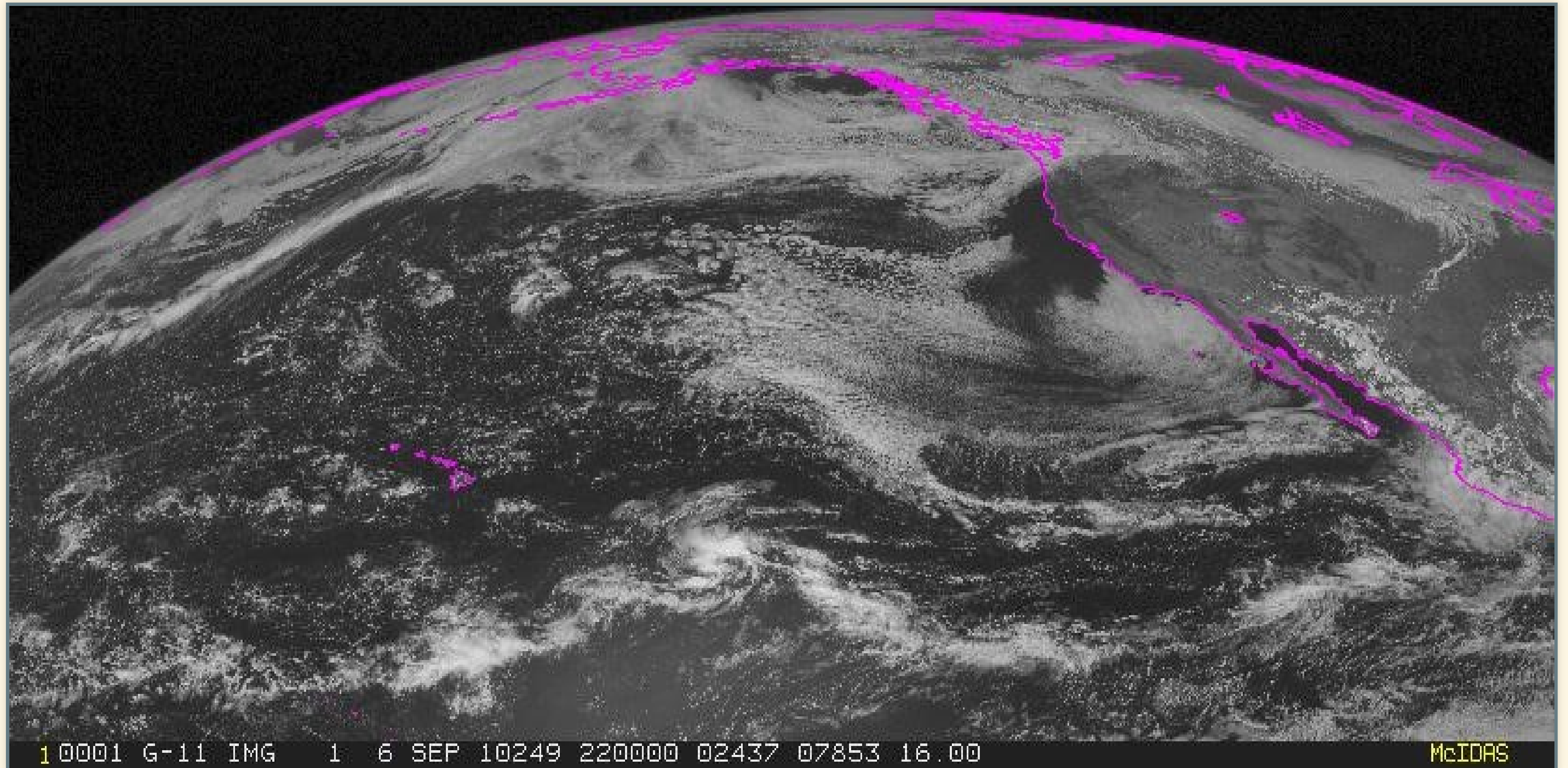
- $I = \varepsilon \sigma T^4$

- $\varepsilon = 1$

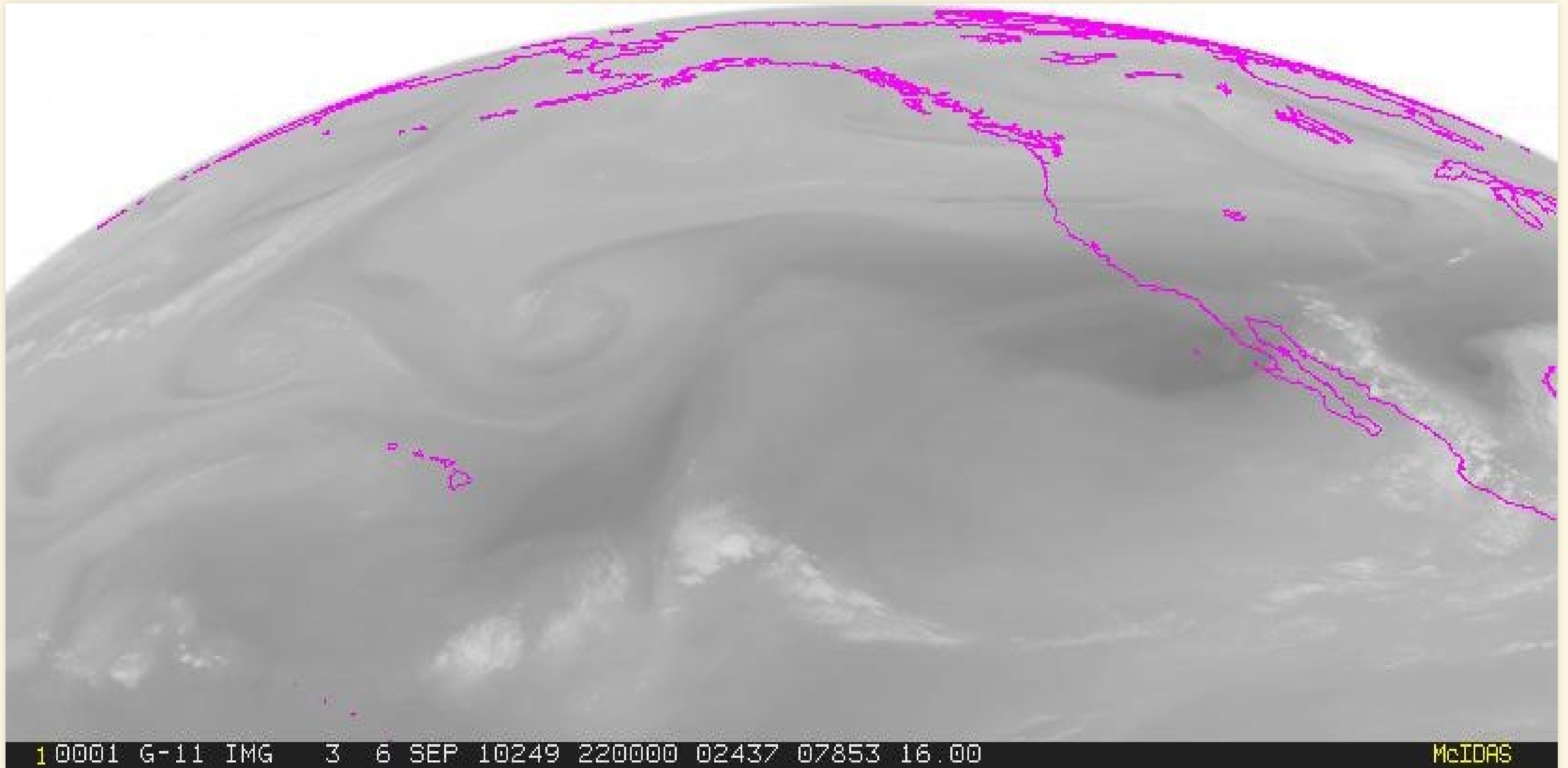
- Brighter = Hotter
- Hotter = closer to ground
 - Satellite can see through atmosphere to low altitude (hot, bright) in “window” region.
 - Satellite can see to middle-troposphere (cold, dimmer) in “water vapor” region
 - Satellite can’t see past top of troposphere (very cold, very dim) in CO₂ region.

Earth Seen by Satellites

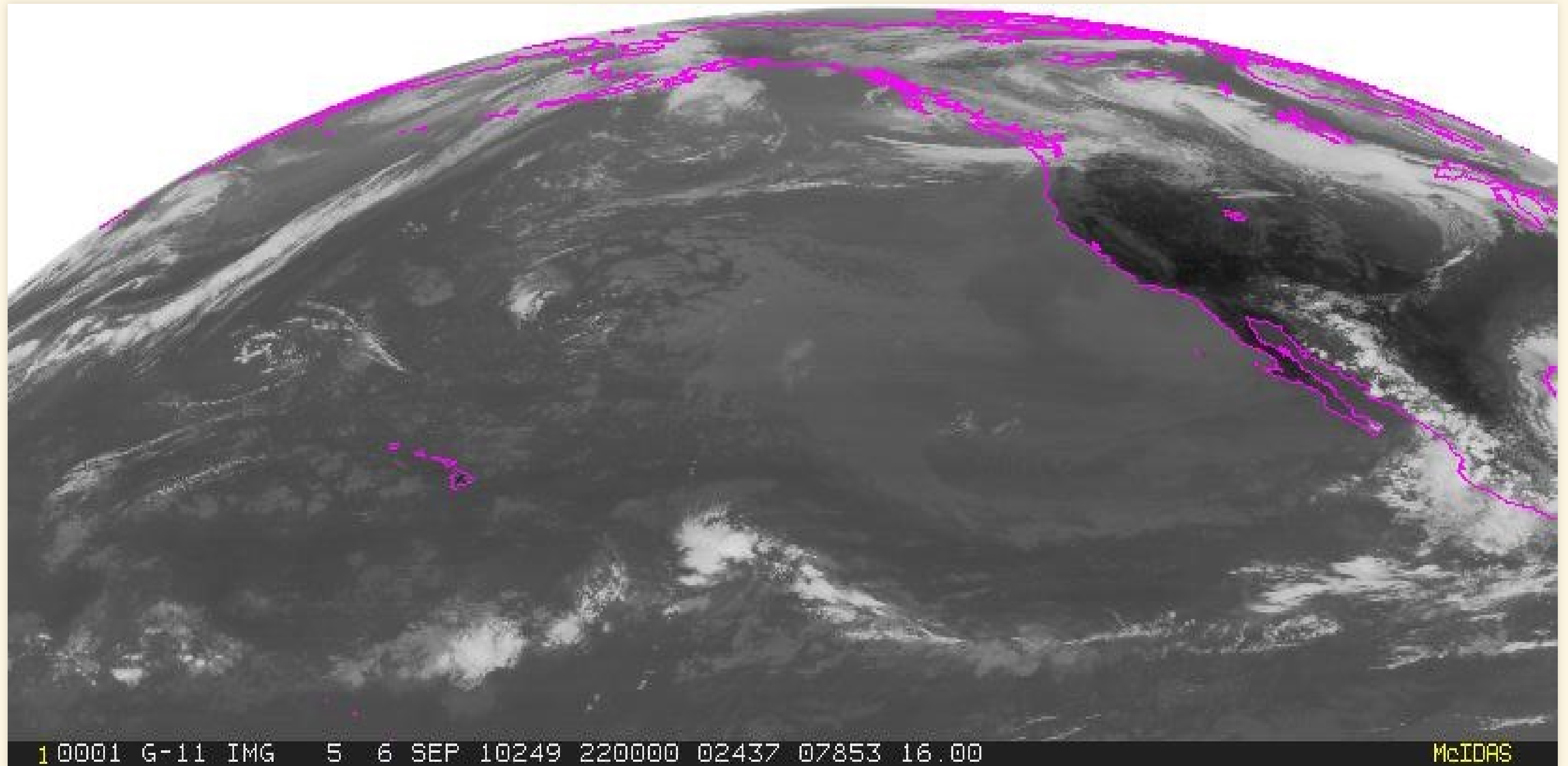
Visible



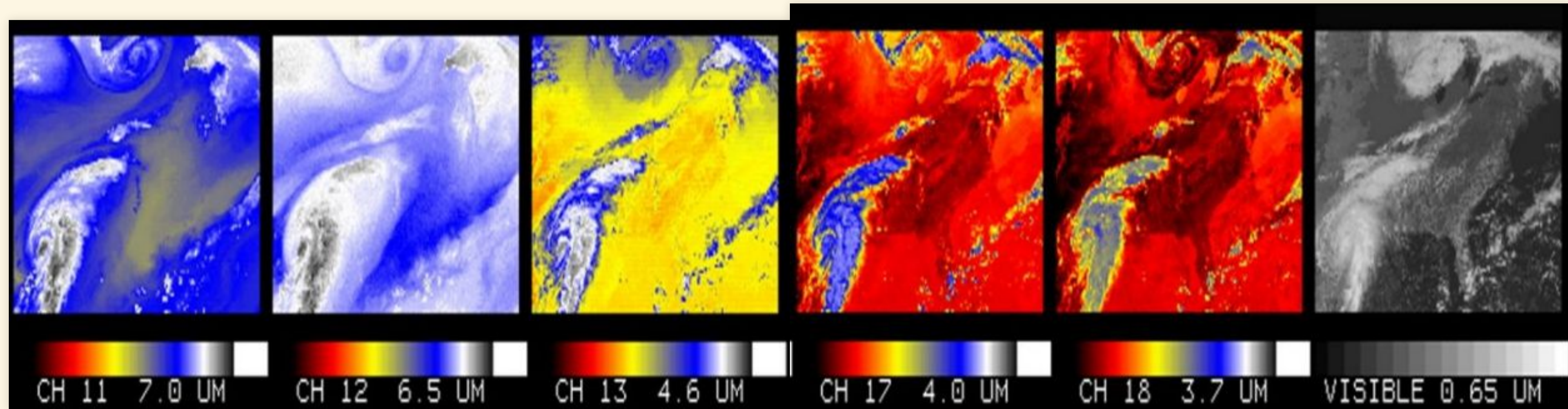
6.8 μm (Water Vapor)



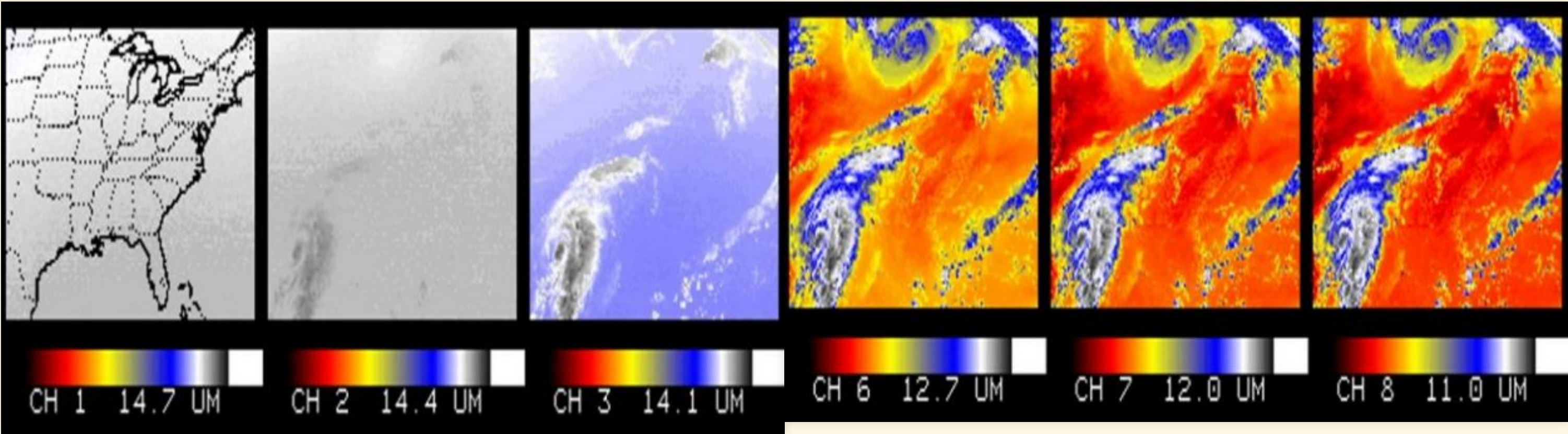
12.0 μm (Window)



Water, Window, Visible



CO₂ peak vs. Window



Terrestrial Planets



Earth, Mars, Venus

	Earth	Mars	Venus
Solar constant	1350 W/m ²	600 W/m ²	2604 W/m ²
Albedo	0.30	0.17	0.71
$T_{\text{radiative}}$	254 K	216 K	240 K
Actual T_{surface}	295 K	240 K	700 K
One-Layer T_{surface}	302 K	257 K	286 K

Vocabulary note:

- “radiative temperature”
 - “skin temperature”
 - “bare rock temperature”
- all mean the same thing.

Earth, Mars, Venus

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$T_{\text{radiative}}$	254 K	216 K	240 K
Actual T_{surface}	295 K	240 K	700 K
One-Layer T_{surface}	302 K	257 K	286 K
Difference	7 K	17 K	−414 K

One-layer model works pretty well for Earth.
Not so well for Mars
Terribly for Venus.

Earth, Mars, Venus

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One-Layer T_{surface}	302 K	257 K	286 K
Difference	7 K	17 K	−414 K
Atmospheric pressure at surface	1013 mb	6 mb	92,000 mb