CS303 Homework 7

Due: 3:30 pm, Wednesday, 10/24 Eric Shih collaborated with Mark Pfluger, Ben Kayton, and Michael Trotta

 $1. \ \, \text{Initial Input:} \ \ \, 42 \ \ \, 57 \ \ \, 7 \ \ \, 40 \ \ \, 83 \ \ \, 78 \ \ \, 86 \ \ \, 89 \ \ \, 80 \ \ \, 91 \ \ \, 79 \ \ \, 84$

Quick Sort	42	57	7	40	83	78	86	89	80	91	79	84	left:0, right:11
median3	42	57	7	40	83	79	86	89	80	91	78	84	left:0, right:11
Final Swap	42	57	7	40	78	79	86	89	80	91	83	84	
Quick Sort	42	57	7	40	78	79	86	89	80	91	83	84	left:0, right:3
Insertion Sort(before):	42	57	7	40	78	79	86	89	80	91	83	84	
insertion Sort(after):	7	40	42	57	78	79	86	89	80	91	83	84	
Quick Sort	7	40	42	57	78	79	86	89	80	91	83	84	left:5, right:11
median3	7	40	42	57	78	79	86	89	83	91	80	84	left:5, right:11
Final Swap	7	40	42	57	78	79	80	89	83	91	86	84	
Quick Sort	7	40	42	57	78	79	80	89	83	91	86	84	left:5, right:5
Insertion Sort (before)	7	40	42	57	78	79	80	89	83	91	86	84	
Insertion Sort (after)	7	40	42	57	78	79	80	89	83	91	86	84	
Quick Sort	7	40	42	57	78	79	80	89	83	91	86	84	left: 7, right: 11
Insertion Sort (before)	7	40	42	57	78	79	80	89	83	91	86	84	
Insertion Sort (after)	7	40	42	57	78	79	80	83	84	86	89	91	
Final Array:	7	40	42	57	78	79	80	83	84	86	89	91	

Number of Shifts: 10 Number of Swaps: 4 Total Shifts and Swaps: 14

Quick Sort	42	57	7	40	83	78	86	89	80	91	79	84	left:0, right:11
median3	42	57	7	40	83	79	86	89	80	91	78	84	left:0, right:11
Final Swap	42	57	7	40	78	79	86	89	80	91	83	84	
Quick Sort left: 0 right: 3	42	57	7	40	78	79	86	89	80	91	83	84	
median3	40	7	42	57	78	79	86	89	80	91	83	84	left:0,right:3
Final Swap	40	7	42	57	78	79	86	89	80	91	83	84	
Quick Sort	40	7	42	57	78	79	86	89	80	91	83	84	left:0, right:1
Insertion Sort (before)	40	7	42	57	78	79	86	89	80	91	83	84	
Insertion Sort (after)	7	40	42	57	78	79	86	89	80	91	83	84	
Quick Sort	7	40	42	57	78	79	86	89	80	91	83	84	left: 3, right: 3
Insertion Sort (before)	7	40	42	57	78	79	86	89	80	91	83	84	
Insertion Sort (after)	7	40	42	57	78	79	86	89	80	91	83	84	
Quick Sort	7	40	42	57	78	79	86	89	80	91	83	84	left:5, right:11
median3	7	40	42	57	78	79	86	89	83	91	80	84	left:5, right:11
Final Swap	7	40	42	57	78	79	80	89	83	91	86	84	
Quick Sort	7	40	42	57	78	79	80	89	83	91	86	84	left:5, right:5
Insertion Sort (before)	7	40	42	57	78	79	80	89	83	91	86	84	
Insertion Sort (after)	7	40	42	57	78	79	80	89	83	91	86	84	
Quick Sort	7	40	42	57	78	79	80	89	83	91	86	84	left: 7, right: 11
median3	7	40	42	57	78	79	80	84	83	86	89	91	left:7, right:11
Final Swap	7	40	42	57	78	79	80	84	83	86	89	91	
Quick Sort	7	40	42	57	78	79	80	84	83	86	89	91	left: 7, right: 9
median3	7	40	42	57	78	79	80	83	84	86	89	91	left:7, right:9
Final Swap	7	40	42	57	78	79	80	83	84	86	89	91	
Quick Sort	7	40	42	57	78	79	80	83	84	86	89	91	left:7, right:7
Insertion Sort (before)	7	40	42	57	78	79	80	83	84	86	89	91	
Insertion Sort (after)	7	40	42	57	78	79	80	83	84	86	89	91	
Quick Sort	7	40	42	57	78	79	80	83	84	86	89	91	left:9, right:9
Insertion Sort (before)	7	40	42	57	78	79	80	83	84	86	89	91	
Insertion Sort (after)	7	40	42	57	78	79	80	83	84	86	89	91	
hlineQuick Sort	7	40	42	57	78	79	80	83	84	86	89	91	left: 11, right: 11
Insertion Sort (before)	7	40	42	57	78	79	80	83	84	86	89	91	
Insertion Sort (after)	7	40	42	57	78	79	80	83	84	86	89	91	
Final Array:	7	40	42	57	78	79	80	83	84	86	89	91	

Number of Shifts: 1 Number of Swaps: 15 Total Number of Shifts and Swaps: 16

- 3. It is better to use a hybrid strategy over only having one sort because the best of both algorithms can be used. In our case the insertion sort is better suited to the smaller cases, while quicksort is better for larger cases. The values from the previous questions did not support my assertion, but this is only because there were several unnecessary insertion sort movements done on a partition with only one element. Without the unnecessary swaps, the hybrid strategy can be shown to be more effective.
- 4. The quicksort will still work because it does not matter where the pivot is placed.

```
Quick Sort
                                                                   left:0, right:11
                                                          79
                                                              84
             42
                  57
                          40
                              83
                                   78
                                       86
                                            89
                                                 80
                                                     91
median3
                              83
                                   78
                                       86
                                            89
                                                 80
                                                     91
                                                          79
                                                              84
                                                                   left:0, right:11\\
             42
Final Swap
                  40
                      7
                         79
                              83
                                   78
                                       86
                                            89
                                                80
                                                     91
```

5. As with question 4, the quicksort will still work because it does not matter where the pivot is placed.

```
84 left: 0, right: 11
Quick Sort
            42
                 57
                     7
                        40
                             83
                                 78
                                     86
                                          89
                                              80
                                                  91
                                                       79
                     7
                                                               left:0, right:11
median3
            42
                 57
                        40
                             83
                                 78
                                     86
                                          89
                                              80
                                                  91
                                                       79
                                                           84
            42
Final Swap
                 57
                     7
                        40
                             83
                                 78
                                     80
                                          79
                                              86
                                                  91
                                                       89
                                                           84
```

6. If the initial if statement still reads $left + 2 \le right$ then the quicksort algorithm will work, otherwise it will skip directly to insertion sort because there are not enough elements in the array. Below is the illustration of the first call when the algorithm works:

```
Quick Sort
                                  left:0,right:4\\
              3 4
                     1
                         2
                            5
                         2
median3
              3
                  4
                     5
                             1
                                  left:0,right:4\\
                         2
Final Swap
                  4
                     5
                             3
              1 \quad 4 \quad 5 \quad 2 \quad 3 \quad left:0, right:-1
Quick Sort
```