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# Bayesian-Adaptive Deep Reinforcement Learning via Ensemble Learning

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## 1 Introduction

While reinforcement learning is capable of controlling complex autonomous systems, RL algorithms typically require huge amounts of data and can overfit to a particular task or to be prone to disturbance. One of main challenges that needs to be addressed is train a policy robust to various model uncertainties and disturbances. In this project, we aim to address this challenge via an ensemble policy for Bayes-Adaptive Reinforcement Learning [1].

We assume that there exists a latent physics variable  $\phi$  which determines the transition function of the underlying MDP, i.e. the transition function  $P(s', \phi' | s, \phi, a)$  is now a function of state, action, and  $\phi$ . We would like to learn a policy which maximizes the long term reward given  $\phi$ . Formally, this is called Bayes-Adaptive MDP [1, 2], defined by a tuple  $\langle \mathcal{S}', \mathcal{A}, P', P_0, R' \rangle$  where

- $\mathcal{S}' = \mathcal{S} \times \Phi$  is the set of (states, physics variable),
- $\mathcal{A}$  is the set of actions,
- $P(\cdot | s, \phi, a)$  is the transition function between hyper-states, conditioned on action  $a$  being taken in hyper-state  $(s, \phi)$ ,
- $P_0 \in \mathcal{P}(\mathcal{S} \times \Phi)$  combines the initial distribution over hyper-states,
- $R'(s, \phi, a)$  represents the reward obtained when action  $a$  is taken in hyper-state  $(s, \phi)$ .

We would like to find the optimal policy for the following Bellman equation:

$$V^*(s, \phi) = \max_a \mathbb{E} \left[ R(s, a, \phi) + \gamma \sum_{s', \phi'} P(s', \phi' | s, \phi, a) V^*(s', \phi') \right] \quad (1)$$

This formulation is often referred as Bayes-Adaptive Reinforcement Learning (BARL) [1].

We make a simplification to BARL formulation. We assume that the dynamics of  $s'$  and  $\phi'$  are independent given  $P(s, \phi, a)$ , i.e.

$$P(s', \phi' | s, \phi, a) = P(s' | s, \phi, a) \cdot P(\phi' | s, \phi, a).$$

This assumption allows us to simplify BARL with a gated ensemble policy learning method. At the high-level, we have a gating network that determines the *belief* of the physics parameters at time  $t$ ,

$$b(\phi_t) = P(\phi_t | s_{t-1}, \phi_{t-1}, a_{t-1})$$

which is then used to compute the best policy from an ensemble of  $\phi$ -dependent optimal policies, i.e.,  $\pi^*(\cdot; \phi)$  and  $V^*(\cdot; \phi)$  are computed with typical RL algorithms for MDPs. Then the remaining task is to compute the one-step best action  $a$ :

$$a^* = \arg \max_a \mathbb{E}_{\phi \sim b(\phi)} \left[ R(s, a, \phi) + \gamma \sum_{s', \phi'} P(s', \phi' | s, \phi, a) V^*(s', \phi') \right] \quad (2)$$

We model  $b_\phi$  as a network capable of modeling evolving state change, e.g. Recurrent Neural Networks, or as a Bayes filter. At the low level, we plan to discretize  $\Phi$  and have one actor-critic network per a discretized value of  $\phi$ : each critic estimates  $V^*(\cdot; \phi)$  and each actor has an optimal policy for a particular discretized value of  $\pi^*(\cdot; \phi)$ . Given  $b_\phi$  and the set of actor-critic networks, it is straightforward to compute (2).

## 2 Background

Our work is closely related to QMDP [3, 4] which is an approximation for POMDP. QMDP approximates POMDP by assuming fully-observable MDP after 1-step, and approximating the Q-value at the current belief state  $b(s)$  as  $Q_a(b) = \sum_s b(s)Q_{MDP}(s, a)$ . In our problem setup, we have a belief over the physics parameters  $\phi$  of the MDP,  $b(\phi)$ , and we compute the policy  $Q_a(s; b) = \sum_{\phi} b(\phi)Q_{MDP}(s, a; \phi)$ .

The BAMDP formulation is also similar to POMDP formulation used in POMDP-lite [5] which assumes that the hidden state variables are constant or only change deterministically. In our case, the hidden state variables correspond to the physics parameters  $\phi$ . The authors of POMDP-lite have shown that such formulation is “equivalent to a set of fully observable Markov decision processes indexed by a hidden parameter” [5], which, in our case, could be viewed as a discretization of  $\phi$ .

## References

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