

# Geometric model extraction from 3D medical data with Visus+LAR architecture \*

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## Abstract

This document describes the Visuspy+LAR architecture.

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\*This document is part of the *Linear Algebraic Representation with CoChains* (LAR-CC) framework.  
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# 1 Visuspy+LAR streaming architecture

## Data preparation

- the visus query on the *idx* file extracts slabs of 3D venous/neural data at finest resolution as a three-dimensional row-major matrix;
- application of a threshold on the data;
- denoising via median filter, if needed.

## Model generation

- at a certain time only three adjacent slabs of the dataset are loaded into memory. They are managed by different processes.
- every slab is divided into bricks;
- boundary extraction within every brick through an operation of SpMV multiplication between the CSR representation of  $[\partial_3]$  and the CSC representation of the 3-chain;
- double faces removal of the median slab, where the upper slab has already been cleaned and smoothed;
- laplacian smoothing on the median slab. The slab that lays downwards has been cleaned only in its upper part;
- use of obj format to save the extracted model.

## Visualization layer

- at a certain moment the upper slab is ready and can be loaded and visualized on the fly;
- lar or pyplasm visualization.

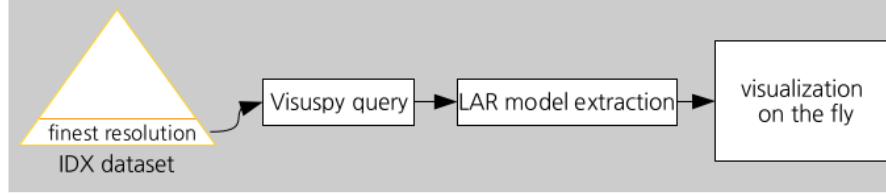


Figure 1: *Visuspy+LAR software architecture*

## 2 Prerequisites installation

Recompile Visus and activate the python flag.

```

⟨Prerequisites 3a⟩ ≡
    cd path/to/nvisusio/build/linux
    cmake ../../
    # activate the option VISUS_BUILD_SWIG_PYTHON
    # configure
    # exit
    # generate
    # quit
    make -j 8
    make install
  ◇

```

Macro never referenced.

## 3 Introduction to visuspy query

### 3.1 Prepare the dataset with Visus Convert

Use Visus Convert to create the *idx* dataset for the next examples.

```

⟨Create IDX 3b⟩ ≡

    cd path/to/nvisusio
    CONVERT="build/linux/visusconvert"
    RESOURCES="resources"
    $CONVERT --import $RESOURCES/tutorials/cat_rgb.tga --create temp/cat_rgb.idx
  ◇

```

Macro never referenced.

### 3.2 Basic 2D query

This first example creates a 2D box, performs the query and visualizes the image of the cat through *matplotlib*. Select the *idx* dataset file, the field and the size of the box. The *set* method takes as parameters the dimension and the coordinate: 0 is x, 1 is y, 2 is z. The box is 256 on x and 256 on y. The query output is a row-major array.

⟨ Visuspy query 4 ⟩ ≡

```
#cd path/to/nvisusio
#python docs/examples/visuspy/query.py
from visuspy import *
import matplotlib.pyplot as plt

def query(self):

    #input file & dataset
    filename="temp/cat_rgb.idx"
    dataset=Dataset_loadDataset(filename)

    logic_box=dataset.getLogicBox()
    field=Field("data",DType("uint8[3]"))
    access=dataset.createAccess()

    #box dimension
    box=NdBox(logic_box)
    box.setP1(0,0)
    box.setP1(1,0)
    box.setP2(0,255)
    box.setP2(1,255)

    #perform the query
    query=Query(dataset,ord('r'))
    query.setLogicPosition(Position(box))
    query.setAccess(access)

    query.begin()
    self.assert_(query.execute())
    data=query.getBuffer().get().asNumPyArray()
    print data

    #visualize the image
    plt.imshow(data)
    plt.show()
```

◇

Macro never referenced.

### 3.3 Manage different resolutions

Decide the resolution of the query output. Visualize the cat at coarser and then full resolution.

⟨ Different resolutions 5 ⟩ ≡

```
from visuspy import *
import matplotlib.pyplot as plt
def resolution(self):

    #input file & dataset
    filename="temp/cat_rgb.idx"
    dataset=Dataset_loadDataset(filename)
    self.assert_(dataset)

    logic_box=dataset.getLogicBox()
    field=Field("data",DType("uint8[3]"))
    access=dataset.createAccess()

    #box dimension
    box=NdBox(logic_box)
    box.setP1(0,0)
    box.setP1(1,0)
    box.setP2(0,255)
    box.setP2(1,255)

    #get the maximum resolution
    MaxH=dataset.getBitmask().getMaxResolution()
    print "MaxH = "+str(MaxH)

    #perform the query
    query=Query(dataset,ord('r'))
    query.setLogicPosition(Position(box))
    query.setAccess(access)
    query.addEndResolution(MaxH-4)
    query.addEndResolution(MaxH)
    query.setMergeMode(Query.InsertSamples)

    #query 1
    query.begin()
    self.assert_(query.execute())
    data=query.getBuffer().get().asNumPyArray()
    print data

    #visualize the image
```

```

plt.imshow(data)
plt.show()

query.next()

#query 2
    self.assert_(query.execute())
data2=query.getBuffer().get().asNumPyArray()
    print data2

#visualize the image
plt.imshow(data2)
plt.show()

```

◇

Macro never referenced.

### 3.4 3D box scan

This sample extract from *IDX* a 3D box and manages the 3D array as a stack of 2D images. The neural dataset is made of two fields: neurons and vessels. Visualize the first 5 images.

⟨3D box 6⟩ ≡

```

from visuspy import *
import matplotlib.pyplot as plt
def 3Dbox(self):
    #input file & dataset
    filename="/home/manuel/Scrivania/microscopy_data/file.idx"
    dataset=Dataset_loadDataset(filename)
    self.assert_(dataset)

    logic_box=dataset.getLogicBox()
    field=Field("vessels",DType("uint8"))
    access=dataset.createAccess()

    #box dimension
    box=NdBox(logic_box)
    box.setP1(0,500)
    box.setP1(1,500)
    box.setP1(2,500)
    box.setP2(0,550)
    box.setP2(1,550)
    box.setP2(2,550)

    #get the maximum resolution

```

```

MaxH=dataset.getBitmask().getMaxResolution()
print "MaxH = "
print MaxH

#perform the query
query=Query(dataset,ord('r'))
query.setLogicPosition(Position(box))
query.setAccess(access)
query.addEndResolution(MaxH)
query.begin()
self.assert_(query.execute())
data3d=query.getBuffer().get().asNumPyArray()

for Z in range(0,5):
    image=data3d[Z]
    plt.imshow(image)
    plt.show()

```

◇

Macro never referenced.

## 4 Multithreading example

This first iteration is characterized by few main points, that help performance improvent from the first *larVolumeToObj*:

- The entire dataset must not be loaded into memory. The *query* tool allows the loading of slices of the volume;
- We don't want to write the entire dataset on disk in *pklz* format. Data load and 2-chain extraction must have been done at the same time without further writings;
- The slices will be processed in parallel.

In this piece of code we reach this aims through multithreading. Each thread performs the query to obtain a slice of the entire volume and computes the 2-chain of 2-quads for every brick in the slice. The remaining part of the application stays the same, it will be taken into analysis in the next sections.

⟨Multithreading 7⟩ ≡

```

from visuspy import *
import larVolumeToObj
import threading

def example(self):

```

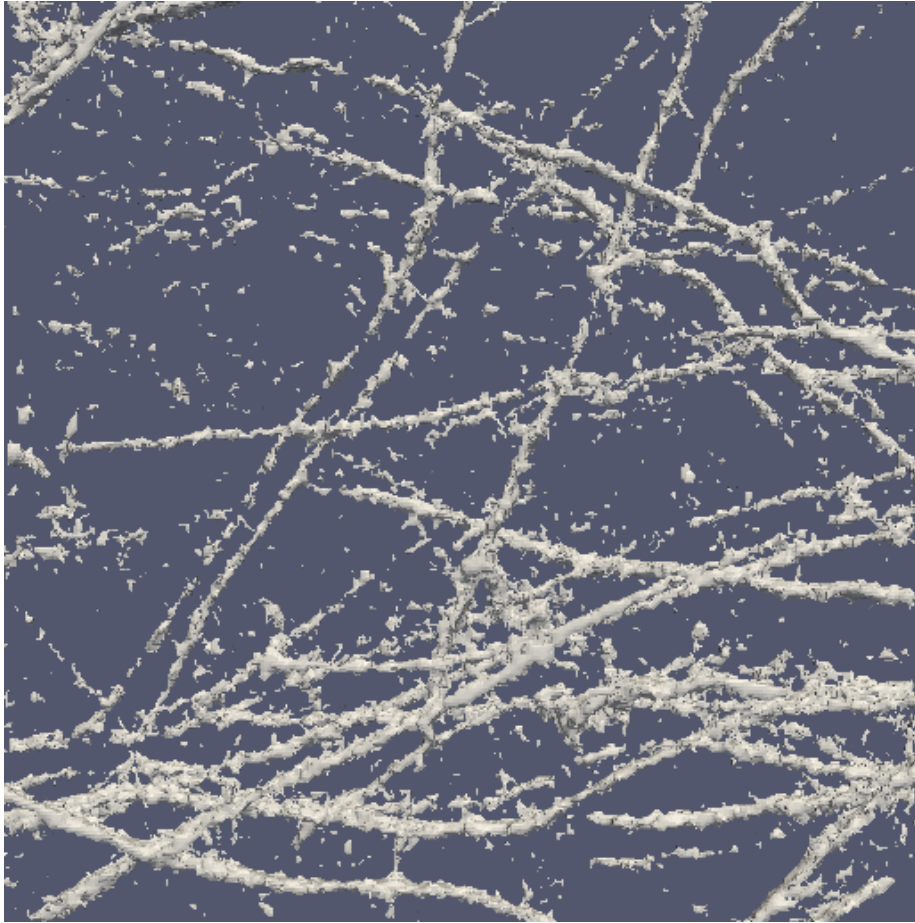


Figure 2: *Model at finest resolution of the venous system of the brain.*



```

#visuspy initialization
app=Application()

#definition of the paths
outputdir='output'
borderdir='output/border'
stldir = os.path.join(outputdir, 'stl')
bindir = os.path.join(outputdir, 'compbin')
binfile = os.path.join(bindir, 'model-2.bin')
stlfile = os.path.join(stldir, 'model-2.obj')

#delete the old output directory
if os.path.exists(outputdir):
    shutil.rmtree(outputdir)

#create the new output directories
self.mkdir_p(stldir)
self.mkdir_p(bindir)
self.mkdir_p(borderdir)

#generate the border matrix
bordo3path = gbmatrix.getOrientedBordo3Path(5, 5, 5,borderdir)

#create and start the threads
#every thread creates the poupout binary
#files with the 2-chain of 2-quads for every brick
threads = []
for n in xrange(5):
    t = myThread(n)
    t.start()
    threads.append(t)

# join all threads
for t in threads:
    t.join()

#concatenate all binary files in model-2.bin
larVolumeToObj.computation.pklzToSmoothObj.concatenate_files(
    "output/*.bin",
    binfile)

#convert model-2.bin in model-2.obj
sq.make_obj(
    5, 5, 5,
    binfile,
    stldir)

```

```

outputfile='out'
obj_input = 'stl/model-2.obj'
    larVolumeToObj.computation.pklzToSmoothObj.concatenate_files(
stldir + '/output-*-.stl', stlfile)

#load the model in model-2.obj and print information
V, F = fileio.readFile(os.path.join(outputdir, obj_input))
print "Before"
    print "Number of vertexes: %i    Number of faces %i" % (len(V), len(F))

#make double faces removal and smoothing
    V, F = pklzToSmoothObj.makeCleaningAndSmoothing(
        V, F,
        os.path.join('output/stl', outputfile))

#print information
    print "After"
    print "Number of vertexes: %i    Number of faces %i" % (len(V), len(F))

# fill empty vertexes
V = [v if len(v) == 3 else [0, 0, 0] for v in V]

# scaling: make ten times bigger
Vint = (numpy.asarray(V) * 10).astype(numpy.int).tolist()

#write after scaling
    fileio.writeFile(
        os.path.join(outputdir, outputfile + "_sm_i.obj"),
        Vint, F,
        ignore_empty_vertex_warning=True)

#triangulate after scaling and save
    Ftr = pklzToSmoothObj.save_triangulated(V, Vint, F, outputdir, outputfile)

#pyplasm visualization
    larVolumeToObjParallello.computation.visualization.visualize(V, F, explode=False)

class myThread (threading.Thread):

    def __init__(self, threadID):
        threading.Thread.__init__(self)
        self.threadID = threadID

    def run(self):
#visus query

```

```

        filename="/home/manuel/Scrivania/microscopy_data/file.idx"
dataset=Dataset_loadDataset(filename)
logic_box=dataset.getLogicBox()
field=Field("vessels",DType("uint8"))
access=dataset.createAccess()

#parametric box
box=NdBox(logic_box)
box.setP1(0,500)
box.setP1(1,500)
box.setP1(2,500+10*self.threadID)
box.setP2(0,600)
box.setP2(1,600)
box.setP2(2,500+10*self.threadID+10)

#get the maximum resolution
MaxH=dataset.getBitmask().getMaxResolution()

#perform the query
query=Query(dataset,ord('r'))
query.setLogicPosition(Position(box))
query.setAccess(access)
query.addEndResolution(MaxH)
query.begin()
query.execute()
data3d=query.getBuffer().get().asNumPyArray()

#parameters label and threshold
label=2
threshold=10

#data structure initialization
metadata = {} # reader.get_metaData()
metadata['series_number'] = 0 # reader.series_number
metadata['datadir'] = "/home/manuel/Scrivania/microscopy_data/"
metadata['voxelsize_mm'] = [100,100,10]
datap = {}
datap['data3d']=data3d
datap['metadata']=metadata

#median filter application
NOISE_SHAPE_DETECT=3
for page in xrange(datap['data3d'].shape[0]):
    datap['data3d'][page] = ndimage.median_filter(
        datap['data3d'][page], NOISE_SHAPE_DETECT)

```

```

#thresholding data
datap['segmentation'] = (datap['data3d'] > threshold).astype(numpy.uint8) * label

print 'Processing data'

#2-chain of 2-quad computation
s2bin.calcchains_main(idslice=self.threadID,
nx=5, ny=5, nz=5,
calculateout=True,
datap=datap,
BORDER_FILE='output/border/bordo3_5-5-5.json',
DIR_0='output/compbin',
coloridx=label,
label=label,
)

```

◇

Macro defined by 7, 14.  
Macro never referenced.

## 5 Partitioning and cover of a set

The aim of this part is to perform double faces removal and smoothing in parallel for the slabs. We exploit the difference between partition and cover of a set. Following the definitions.

**Partition of a set.** *A family of sets  $P$  is a partition of  $X$  if and only if all of the following conditions hold:*

- *$P$  does not contain the empty set;*
- *The union of the sets in  $P$  is equal to  $X$ . The sets in  $P$  are said to cover  $X$ ;*
- *The intersection of any two distinct sets in  $P$  is empty.*

**Cover of a set.** *A family of sets  $P$  is a cover of  $X$  if and only if all of the following conditions hold:*

- *$P$  does not contain the empty set;*
- *The union of the sets in  $P$  is equal to  $X$ .*

### 5.1 Algorithm idea

- Create the covering for each partition;
- Apply to the covering the standard algorithms;

- Remove what is outside the slab;
- Merge the new part and visualize.

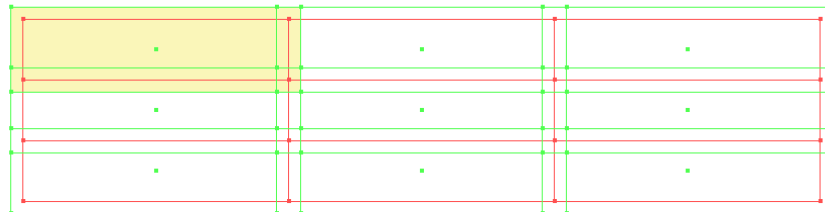


Figure 3: *2D description. red: partitioning on data space (voxels); green: cover, extension of a slab; yellow: one extended slab.*

## 6 JSON configuration file

Parameters can be set through json configuration file. Here is a very simple sample about decoding data from JSON file.

⟨JSON decode 13a⟩ ≡

```
import json

with open('conf.json') as data_file:
    data = json.load(data_file)
    crop = data['crop']
    print crop[0]
    print crop[0][0]
    print crop[0][1]
◇
```

Macro never referenced.

⟨JSON file 13b⟩ ≡

```
{
  "crop": [[1,800],[1,600],[1,50]]
}
◇
```

Macro never referenced.

## 7 Nested multithreading and shared data structures

The job is divided between threads. Each thread creates a square, but this square is created by two nested threads. Each nested thread writes a triangle in the same data structure, a list representing a LAR model.

⟨Multithreading 14⟩ ≡

```
import threading
from larlib import *

class CreateTriangle(threading.Thread):
    def __init__(self, idtriangle, idslice, model, lock):
        threading.Thread.__init__(self)
        self.lock = lock
        self.idtriangle = idtriangle
        self.idslice = idslice
        self.model = model
    def run(self):
        self.lock.acquire()
        if self.idtriangle%2==0:
            if [1,0,self.idslice] not in self.model[0]:
                self.model[0].append([1,0,self.idslice])
            if [0,0,self.idslice] not in self.model[0]:
                self.model[0].append([0,0,self.idslice])
            if [0,1,self.idslice] not in self.model[0]:
                self.model[0].append([0,1,self.idslice])
            x = self.model[0].index([1,0,self.idslice])
            y = self.model[0].index([0,0,self.idslice])
            z = self.model[0].index([0,1,self.idslice])
            self.model[1].append([x,y,z])
        else:
            if [1,0,self.idslice] not in self.model[0]:
                self.model[0].append([1,0,self.idslice])
            if [1,1,self.idslice] not in self.model[0]:
                self.model[0].append([1,1,self.idslice])
            if [0,1,self.idslice] not in self.model[0]:
                self.model[0].append([0,1,self.idslice])
            x = self.model[0].index([1,0,self.idslice])
            y = self.model[0].index([0,1,self.idslice])
            z = self.model[0].index([1,1,self.idslice])
            self.model[1].append([x,y,z])
        self.lock.release()

class CreateSlice(threading.Thread):
    def __init__(self, idslice, model, lock):
```

```

        threading.Thread.__init__(self)
        self.lock = lock
        self.idslice = idslice
        self.model = model
    def run(self):
        threads = []
        for idtriangle in xrange(2):
            t = CreateTriangle(idtriangle,self.idslice,self.model,self.lock)
            t.start()
            threads.append(t)
        for t in threads:
            t.join()

class Esempio:
    def main(self):
        model = [[],[ ]]
        lock = threading.Lock()

        threads = []
        for idslice in xrange(10):
            t = CreateSlice(idslice,model,lock)
            t.start()
            threads.append(t)
        for t in threads:
            t.join()

        mkpols = MKPOLs(model)
        VIEW(EXPLODE(1.2, 1.2, 1)(mkpols))

if __name__ == '__main__':
    e = Esempio()
    e.main()

```

◇

Macro defined by 7, 14.  
Macro never referenced.

## 8 Final solution

The idea is to divide the computation on each slab in 3 main parts: read through the query, compute the model and write it. The actions on each slab have to be performed according to the Gant diagram shown in figure.

⟨ Final solution 15 ⟩ ≡

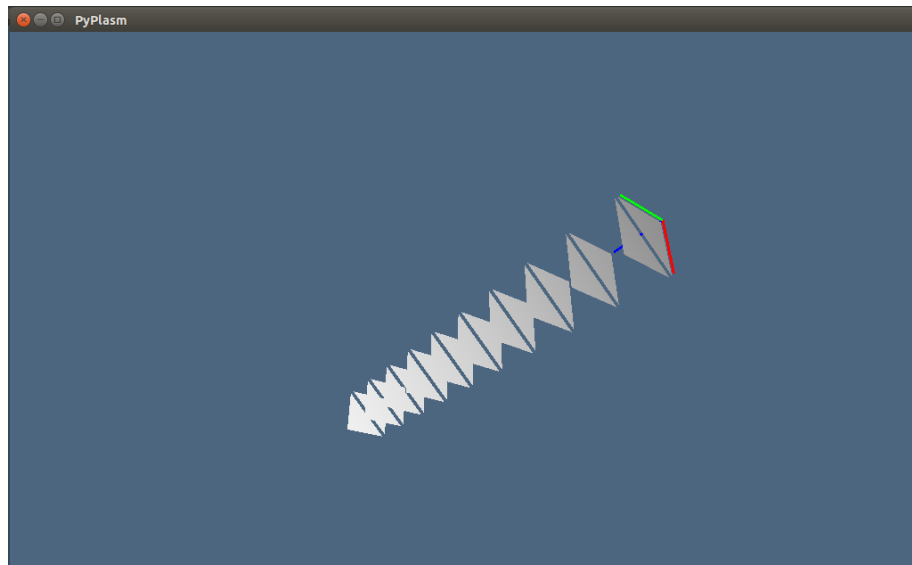


Figure 4: *Output of the nested multithreading sample*

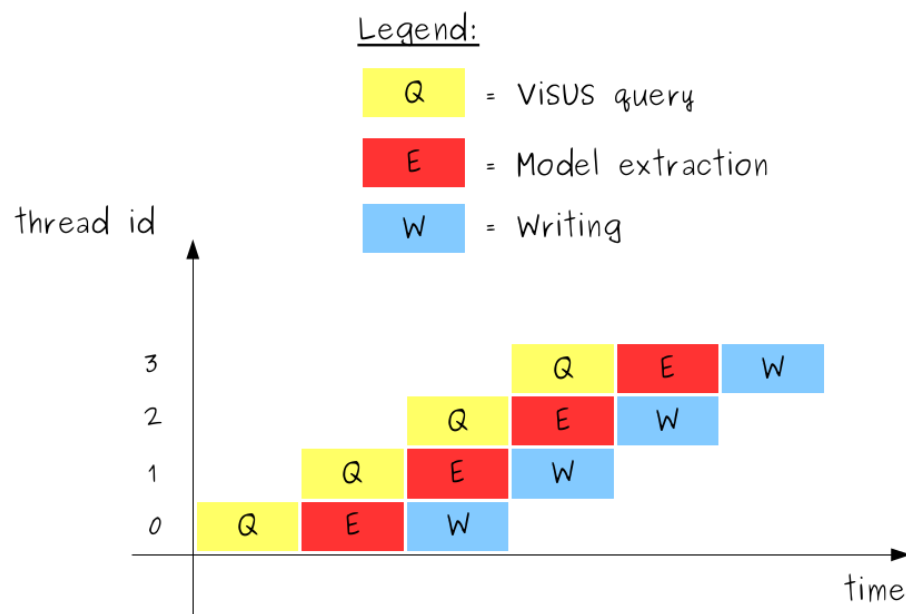


Figure 5: *Gant diagram of the computation.*



◇

Macro never referenced.

## 9 Generate the boundary operator

The computation is faster with the not-oriented boundary operator, computed through the new lar boundary module.

⟨ Get bordo3 path 17a ⟩ ≡

```
def getBordo3Path(nx, ny, nz, DIR_OUT):
    fileName = DIR_OUT+'bordo3_'+str(nx)+'-'+str(ny)+'-'+str(nz)+'.json'
    bordo3 = computeBordo3(nx, ny, nz) ⟨Compute bordo3 17b⟩
    writeBordo3(bordo3, fileName) ⟨Write bordo3 19a⟩
    return fileName
```

◇

Macro never referenced.

⟨ Compute bordo3 17b ⟩ ≡

```
def computeBordo3(nx, ny, nz):
    V, [VV, EV, FV, CV] = getBases(nx, ny, nz) ⟨Get basis 17c⟩
    bordo3 = boundary(CV,FV) #LAR
    return bordo3
```

◇

Macro referenced in 17a.

⟨ Get basis 17c ⟩ ≡

```
def getBases(nx, ny, nz):

    def ind(x,y,z): return x + (nx+1) * (y + (ny+1) * (z))

    def the3Dcell(coords):
        x,y,z = coords
        return [ind(x,y,z),ind(x+1,y,z),ind(x,y+1,z),ind(x,y,z+1),ind(x+1,y+1,z),
                ind(x+1,y,z+1),ind(x,y+1,z+1),ind(x+1,y+1,z+1)]

    # Construction of vertex coordinates (nx * ny * nz)
    # -----

    try:
        V = [[x,y,z] for z in xrange(nz+1) for y in xrange(ny+1) for x in xrange(nx+1) ]
```

```

except:
    import ipdb; ipdb.set_trace() # noqa BREAKPOINT

log(3, ["V = " + str(V)])

# Construction of CV relation (nx * ny * nz)
# -----

CV = [the3Dcell([x,y,z]) for z in xrange(nz) for y in xrange(ny) for x in xrange(nx)]

log(3, ["CV = " + str(CV)])

# Construction of FV relation (nx * ny * nz)
# -----

FV = []

v2coords = invertIndex(nx,ny,nz) <Invert index 18>

for h in xrange(len(V)):
    x,y,z = v2coords(h)
    if (x < nx) and (y < ny): FV.append([h,ind(x+1,y,z),ind(x,y+1,z),ind(x+1,y+1,z)])
    if (x < nx) and (z < nz): FV.append([h,ind(x+1,y,z),ind(x,y,z+1),ind(x+1,y,z+1)])
    if (y < ny) and (z < nz): FV.append([h,ind(x,y+1,z),ind(x,y,z+1),ind(x,y+1,z+1)])

VV = AA(LIST)(range(len(V)))

EV = []
for h in xrange(len(V)):
    x,y,z = v2coords(h)
    if (x < nx): EV.append([h,ind(x+1,y,z)])
    if (y < ny): EV.append([h,ind(x,y+1,z)])
    if (z < nz): EV.append([h,ind(x,y,z+1)])

return V, (VV, EV, FV, CV)

```

◇

Macro referenced in 17b.

<Invert index 18> ≡

```

def invertIndex(nx,ny,nz):
    nx,ny,nz = nx+1,ny+1,nz+1
    def invertIndex0(offset):
        a0, b0 = offset / nx, offset % nx
        a1, b1 = a0 / ny, a0 % ny

```

```

        a2, b2 = a1 / nz, a1 % nz
        return b0,b1,b2
    return invertIndex0

```

◇

Macro referenced in [17c](#), [19b](#), [26b](#).

⟨Write bordo3 19a⟩ ≡

```

def writeBordo3(bordo3, inputFile):
    ROWCOUNT = bordo3.shape[0]
    COLCOUNT = bordo3.shape[1]
    ROW = bordo3.indptr.tolist()
    COL = bordo3.indices.tolist()
    DATA = bordo3.data.tolist()

    with open(inputFile, "w") as file:
        json.dump({
            "ROWCOUNT": ROWCOUNT, "COLCOUNT": COLCOUNT,
            "ROW": ROW, "COL": COL, "DATA": DATA}, file,
            separators=(',', ':'))
        file.flush()

```

◇

Macro referenced in [17a](#).

## 10 Calculate chains

⟨Calculate chains main 19b⟩ ≡

```

def calcchains_main(
    hslice,
    idslice,bin_data,lock,
    nx, ny, nz,
    calculateout,
    datap,
    BORDER_FILE,
    coloridx,
    label
):
    def ind(x, y, z):
        return x + (nx+1) * (y + (ny+1) * (z))

    chunksize = nx * ny + nx * nz + ny * nz + 3 * nx * ny * nz
    V = [[x, y, z]
        for z in xrange(nz + 1)
        for y in xrange(ny + 1)

```

```

        for x in xrange(nx + 1)]

v2coords = invertIndex(nx, ny, nz) ⟨Invert index 18⟩

# construction of vertex grid
FV = []
for h in xrange(len(V)):
    x, y, z = v2coords(h)
    if (x < nx) and (y < ny):
        FV.append([h, ind(x+1, y, z), ind(x, y+1, z), ind(x+1, y+1, z)])
    if (x < nx) and (z < nz):
        FV.append([h, ind(x+1, y, z), ind(x, y, z+1), ind(x+1, y, z+1)])
    if (y < ny) and (z < nz):
        FV.append([h, ind(x, y+1, z), ind(x, y, z+1), ind(x, y+1, z+1)])

return runComputation(hslice,idslice,bin_data,lock, nx, ny, nz,
                      coloridx, calculateout, V, FV, datap,
                      BORDER_FILE, label) ⟨Run computation 20⟩

```

◇

Macro never referenced.

⟨Run computation 20⟩ ≡

```

def runComputation(hslice,idslice,bin_data, lock, imageDx, imageDy,
                  imageDz, coloridx, calculateout,
                  V, FV, datap, BORDER_FILE, label):

    segmentation = datap['segmentation'].astype(np.uint8)

    segmentation[0, 0, 0] = 0
    segmentation[0, 0, 1] = 1
    datap['segmentation'] = segmentation

    logger.debug("unique %s " %(str(np.unique(datap['segmentation']))))
    imageHeight, imageWidth = datap['segmentation'][:, :, :].shape[1:3]

    imageDepth = datap['segmentation'].shape[0]
    Nx, Ny, Nz = imageHeight/imageDx, imageWidth/imageDx, imageDepth/imageDz

    returnValue = 2

    try:

        centroidsCalc = np.unique(datap['segmentation'])

        returnValue = startComputeChains(hslice,

```

```

        idslice, bin_data, lock, imageHeight, imageWidth, imageDepth,
        imageDx, imageDy, imageDz, Nx, Ny, Nz,
        calculateout, BORDER_FILE,
        centroidsCalc, coloridx,
        datap) (Start compute chains 21)
except:
    exc_type, exc_value, exc_traceback = sys.exc_info()
    lines = traceback.format_exception(exc_type, exc_value, exc_traceback)
    log(1, [ "Error: " + ''.join('!! ' + line for line in lines) ])
    returnValue = 2

return returnValue

```

◇

Macro referenced in 19b.

(Start compute chains 21) ≡

```

def startComputeChains(hslice,idslice, bin_data,lock,
    imageHeight, imageWidth, imageDepth,
    imageDx, imageDy, imageDz,
    Nx, Ny, Nz, calculateout, BORDER_FILE,
    centroidsCalc, colorIdx, datap
):
    beginImageStack = 0
    endImage = beginImageStack
    saveTheColors = centroidsCalc
    log(2, [centroidsCalc])
    saveTheColors = np.array(
        sorted(saveTheColors.reshape(1, len(centroidsCalc))[0]), dtype=np.int)
    log(2, [saveTheColors])

    returnValue = 2

    threads = []
    for j in xrange(imageDepth / imageDz):
        startImage = endImage
        endImage = startImage + imageDz
        log(2, [ "Added task: " + str(j)
+ " -- (" + str(startImage) + "," + str(endImage) + ")" ])

        t1 = ChainsThreadComputation(hslice,idslice, bin_data,lock,
            startImage, endImage, imageHeight, imageWidth,
            imageDx, imageDy, imageDz, Nx, Ny, Nz, calculateout,
            BORDER_FILE, centroidsCalc,
            colorIdx, datap) (Chains thread computation 22)

    t1.start()

```

```

        threads.append(t1)

    for t in threads:
        t.join()

    log(1, [ "Completed: " + str(processRes) ])
    if (sum(processRes) == 0):
        returnValue = 0
    return returnValue

```

◇

Macro referenced in 20.

⟨ Chains thread computation 22 ⟩ ≡

```

class ChainsThreadComputation(threading.Thread):
    def __init__(self, hslice,idslice, bin_data,lock,
        startImage, endImage, imageHeight, imageWidth,
        imageDx, imageDy, imageDz,
        Nx, Ny, Nz,
        calculateout, BORDER_FILE,
        centroidsCalc, colorIdx, datap):
        threading.Thread.__init__(self)
        self.idslice=idslice
        self.bin_data=bin_data
        self.lock=lock
        self.hslice=hslice
        self.startImage=startImage
        self.endImage=endImage
        self.imageHeight=imageHeight
        self.imageWidth=imageWidth
        self.imageDx=imageDx
        self.imageDy=imageDy
        self.imageDz=imageDz
        self.Nx=Nx
        self.Ny=Ny
        self.Nz=Nz
        self.calculateout=calculateout
        self.BORDER_FILE=BORDER_FILE
        self.centroidsCalc=centroidsCalc
        self.colorIdx=colorIdx
        self.datap=datap

    def run(self):
        log(2, [ "Working task: " + str(self.startImage) + "-" + str(self.endImage) + " [" +
            str( self.imageHeight) + "-" + str( self.imageWidth ) + "-" + str(self.imageDx) +
            "-" + str( self.imageDy) + "-" + str (self.imageDz) + "]" ])

```

```

bordo3 = None
if (self.calculateout == True):
    with open(self.BORDER_FILE, "r") as file:
        bordo3_json = json.load(file)
        ROWCOUNT = bordo3_json['ROWCOUNT']
        COLCOUNT = bordo3_json['COLCOUNT']
        ROW = np.asarray(bordo3_json['ROW'], dtype=np.int32)
        COL = np.asarray(bordo3_json['COL'], dtype=np.int32)
        if np.isscalar(bordo3_json['DATA']):
            # in special case, when all numbers are same
            logger.debug('bordermatrix data stored as scalar 1')
            DATA = np.ones(COL.shape, dtype=np.int8) *\
                np.int8(bordo3_json['DATA'])
        else:
            # this is general form
            logger.debug(
                'bordermatrix data stored in general form')
            DATA = np.asarray(bordo3_json['DATA'], dtype=np.int8)
        bordo3 = csr_matrix(
            (DATA, COL, ROW), shape=(ROWCOUNT, COLCOUNT))

xEnd, yEnd = 0, 0
beginImageStack = 0
saveTheColors = self.centroidsCalc
saveTheColors = np.array(
sorted(saveTheColors.reshape(1, len(self.centroidsCalc))[0]), dtype=np.int
)

returnProcess = 0

try:
try:
    log(2, ["Working task: " +
        str(self.startImage) + "-" +
        str(self.endImage) + " [loading colors]"])

    theImage = read_by_block(
        self.datap,
        self.startImage, self.endImage,
        self.centroidsCalc) <Read by block 25a>

    log(2, ["Working task: " +
        str(self.startImage) + "-" +
        str(self.endImage) + " [comp loop]" ])
    for xBlock in xrange(self.imageHeight / self.imageDx):

```

```

for yBlock in xrange(self.imageWidth/self.imageDy):
    xStart, yStart = xBlock * self.imageDx, yBlock * self.imageDy
    xEnd, yEnd = xStart+self.imageDx, yStart+self.imageDy

    image = theImage[:, xStart:xEnd, yStart:yEnd]

    nz, nx, ny = image.shape

    # Compute a quotient complex of chains with constant field
    # -----

    chains3D_old = []
    chains3D = None
    hasSomeOne = False
    if (self.calculateout != True):
        chains3D = np.zeros(nx * ny * nz, dtype=np.int32)

    zStart = self.startImage - beginImageStack + self.hslices

    chains3D_old = cch.setList(
        nx, ny, nz, self.colorIdx, image, saveTheColors) <Set list 25c>

    # Compute the boundary complex of the quotient cell
    objectBoundaryChain = None
    if (self.calculateout == True) and (len(chains3D_old) > 0):
        objectBoundaryChain = larBoundaryChain(
            bordo3, chains3D_old) #LAR

    # Save
    if (self.calculateout == True):
        if (objectBoundaryChain != None):
            writeData(self.hslices, self.lock, <Write data 25b>
                self.bin_data,
                np.array(
                    [zStart, xStart, yStart], dtype=int32),
                objectBoundaryChain)

except:

    import traceback
    logger.debug(traceback.format_exc())
    exc_type, exc_value, exc_traceback = sys.exc_info()
    lines = traceback.format_exception(
        exc_type, exc_value, exc_traceback)
    # Log it or whatever here
    log(1, ["Error: " + ''.join('!! ' + line for line in lines)])

```



```
returnProcess = 2
```

```
except:
import traceback
exc_type, exc_value, exc_traceback = sys.exc_info()
print sys.exc_info()
lines = traceback.format_exception(exc_type, exc_value, exc_traceback)
log(1, ["Error: " + ''.join('!! ' + line for line in lines)])
returnProcess = 2
```

◇

Macro referenced in 21.

〈Read by block 25a〉≡

```
def read_by_block(datap, startImage, endImage, centroidsCalc):
segmentation = datap['segmentation'][startImage:endImage:, :, :]
return segmentation
```

◇

Macro referenced in 22.

〈Write data 25b〉≡

```
def writeData(hslice,lock,bin_data,offsetCurr, objectBoundaryChain):
lock.acquire()
bin_data.append([[offsetCurr[0],offsetCurr[1],
offsetCurr[2]],objectBoundaryChain.toarray()])
lock.release()
```

◇

Macro referenced in 22.

## 11 Calculate chains helper

〈Set list 25c〉≡

```
def setList(int nx, int ny, int nz, int colorIdx, np.ndarray[np.uint8_t, ndim=3] image,
np.ndarray[np.int_t, ndim=1] saveTheColors):
cdef list chains3D_old = range(0)

for x in xrange(nx):
for y in xrange(ny):
for z in xrange(nz):
if (image[z,x,y] == saveTheColors[colorIdx]):
chains3D_old.append(addr(x,y,z,nx,ny,nz)) 〈Addr 26a〉

return chains3D_old
```

◇

Macro referenced in 22.

⟨Addr 26a⟩ ≡

```
cdef int addr(int x, int y, int z, int nx, int ny, int nz) nogil:
    return x + (nx) * (y + (ny) * (z))
```

◇

Macro referenced in 25c.

## 12 Generate a square mesh

⟨Square mesh 26b⟩ ≡

```
def square_mesh(nx, ny, nz, bin_data):

    def ind(x,y,z): return x + (nx+1) * (y + (ny+1) * (z))

    chunksize = nx * ny + nx * nz + ny * nz + 3 * nx * ny * nz
    V = [[x,y,z] for z in xrange(nz+1) for y in xrange(ny+1) for x in xrange(nx+1) ]

    v2coords = invertIndex(nx,ny,nz) ⟨Invert index 18⟩

    FV = []
    for h in xrange(len(V)):
        x,y,z = v2coords(h)
        if (x < nx) and (y < ny): FV.append([h,ind(x+1,y,z),ind(x,y+1,z),ind(x+1,y+1,z)])
        if (x < nx) and (z < nz): FV.append([h,ind(x+1,y,z),ind(x,y,z+1),ind(x+1,y,z+1)])
        if (y < ny) and (z < nz): FV.append([h,ind(x,y+1,z),ind(x,y,z+1),ind(x,y+1,z+1)])

    logger.debug('before readFile()')
    try:
        V2,F2=read(V,FV,bin_data,chunksize) ⟨Read 26c⟩
    except:
        import traceback
        traceback.print_exc()
        exc_type, exc_value, exc_traceback = sys.exc_info()
        lines = traceback.format_exception(exc_type, exc_value, exc_traceback)
        log(1, [ "Error: " + ''.join('!! ' + line for line in lines) ])
        sys.exit(2)
    logger.debug('after readFile()')
    return V2,F2
```

◇

Macro never referenced.

⟨Read 26c⟩ ≡

```

def read(V,FV,bin_data,chunksize):
    V2=[]
    F2=[]
    vertex_count = 1
    old_vertex_count = vertex_count
    count = 0
    try:
        for indice in range(len(bin_data)):
            count += 1
            zStart = bin_data[indice][0][0]
            xStart = bin_data[indice][0][1]
            yStart = bin_data[indice][0][2]
            log(1, ["zStart, xStart, yStart = "
+ str(zStart) + "," + str(xStart) + "," + str(yStart)]);
            LISTA_VETTORI2=bin_data[indice][1]
            lista = LISTA_VETTORI2
            LISTA_VETTORI2 = np.abs(LISTA_VETTORI2)
            timer_stop();
            timer_start("objectBoundaryChain ");
            l = len(LISTA_VETTORI2)
            objectBoundaryChain = scipy.sparse.csr_matrix(LISTA_VETTORI2.reshape((l,1)))
            timer_stop();
            b2cells = csrChainToCellList(objectBoundaryChain) #LAR
            FVn = []
            for i, face in enumerate(FV):
                [v1, v2, v3, v4] = FV[i]
                # face = [v1, v2, v4, v3]
                if lista[i] < 0:
                    FVn.append([v1, v3, v2, v4])
                else:
                    FVn.append([v1, v2, v3, v4])
            vertex_count, old_vertex_count = write(
                V2, F2,
                V, FVn,
                xStart, yStart, zStart,
                vertex_count, old_vertex_count,
                b2cells
            ) < Write 28a >
    except struct.error:
        logger.debug('not importatnt reading error')
    except:
        logger.debug('reading error')
        traceback.print_exc()
        exc_type, exc_value, exc_traceback = sys.exc_info()
        lines = traceback.format_exception(exc_type, exc_value, exc_traceback)

```

```

        log(1, [ "EOF or error: " + ''.join('!! ' + line for line in lines) ])
    return V2,F2

```

◇

Macro referenced in 26b.

⟨ Write 28a ⟩ ≡

```

def write(V2, F2, V, FV,
          xStart, yStart, zStart,
          vertex_count, old_vertex_count,
          b2cells
          ):
    for f in b2cells:
        old_vertex_count = vertex_count

        for vtx in FV[f]:
            x=V[vtx][0] + xStart
            y=V[vtx][1] + yStart
            z=V[vtx][2] + zStart
            V2.append([x,y,z])
            vertex_count = vertex_count + 1

        F2.append([
            old_vertex_count + 0,
            old_vertex_count + 1,
            old_vertex_count + 3,
            old_vertex_count + 2
        ])
    return vertex_count, old_vertex_count

```

◇

Macro referenced in 26c.

## 13 Cleaning and smoothing

⟨ Make cleaning and smoothing 28b ⟩ ≡

```

def makeCleaningAndSmoothing(V, F):
    V, F = rmbox.removeDoubleVertexesAndFaces(V, F, use_dict_algorithm=False)
    V = ls.makeSmoothing(V, F) ⟨ Make smoothing ? ⟩
    V, F = rmbox.removeDoubleVertexesAndFaces(V, F, use_dict_algorithm=False)
    return V, F

```

◇

Macro never referenced.

## 14 Visus+LAR: C++ implementation

Aim of this document is to define the architecture of the C++ implementation of the LAR+Visus application, starting from the existing python prototype.

### Query and data preparation on the upper slab

- Load the parameters of computation from the configuration file;
- the visus query on the *idx* file extracts slabs of 3D venous/neural data at finest resolution as a three-dimensional row-major matrix;
- application of a threshold on the data;
- removal of the small connected components;
- computation of the boundary operator;
- at a certain time three adjacent slabs of the volume are computed by different processes, as shown in figure.

### Model generation on the central slab

- The central slab of the three in memory is divided into bricks;
- boundary extraction within every brick through an SpMV multiplication between  $[\partial_3]$  and the 3-chain;
- double vertices and faces removal;
- computation of the indices for the crop of the cover;
- laplacian or taubin non-shrinking smoothing;
- crop of the cover;
- topology-preserving simplification.

### Writing on the lower slab

- At the end of each slab computation, each process writes vertexes and faces on the same obj file.

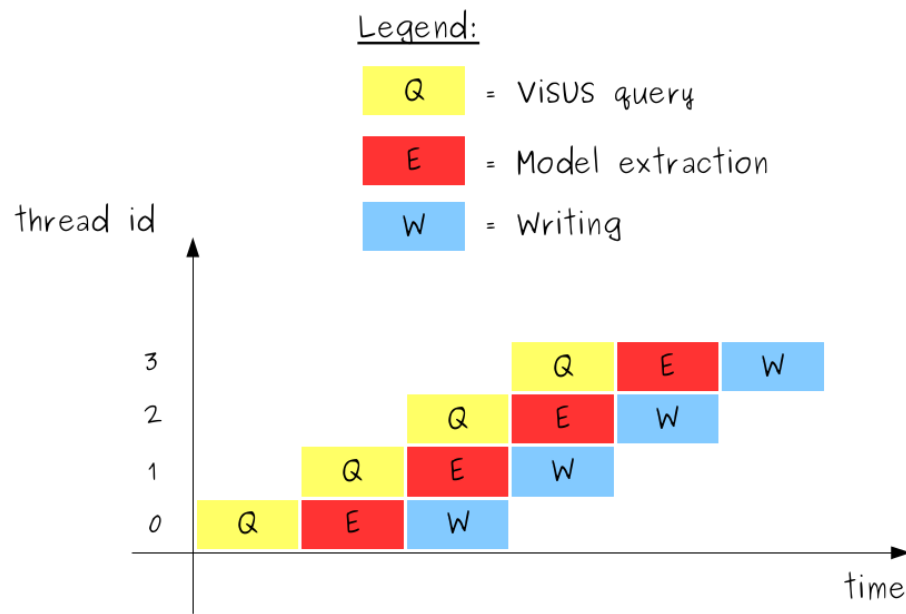


Figure 6: *Gant diagram of the computation.*

### Visualization of the lower slab

- Visualization of the first slab through the *VisusViewer*;
- Update the visualization each time a new slab is ready.

### References

A. PAOLUZZI, A. DI CARLO, F. FURIANI, M. JIRIK, *CAD models from medical images using LAR*, Computer-Aided Design and Applications, 2015. Preliminary version in CAD'15, June 22-25, 2015, London, UK;

F. FURIANI, C. PAOLUZZI, A. PAOLUZZI, *Algebraic extraction of models and properties from images* (in Italian), GeoMedia, Volume 17, Issue 6, December 2013.