Imperial College London

NOTES

IMPERIAL COLLEGE LONDON

DEPARTMENT OF COMPUTING

422 Computational Finance

Author:

Thomas Teh (CID: 0124 3008)

Date: February 5, 2017

1 Useful Identities

Geometric Progression

$$S_n = \sum_{k=1}^n ar^{k-1} = \frac{a(1-r^n)}{1-r}$$

$$S_{\infty} = \sum_{k=0}^{\infty} ar^{k-1} = \frac{1}{1-r}$$

Arithmetic - Geometric Progression

$$S_n = \sum_{k=1}^n \left[a + (k-1)d \right] r^{k-1} = \frac{a - \left[a + (n-1)d \right] r^n}{1 - r} + \frac{dr(1 - r^{n-1})}{(1 - r)^2}$$

Price of an Annuity

$$a_{\overline{n}|} = \frac{1 - v^n}{i}$$
$$a_{\overline{n}|}^{(m)} = \frac{1 - v^n}{r^m}$$

Price of a Perpetuity

$$a_{\overline{\infty}|} = \frac{1}{i}$$
$$a_{\overline{\infty}|} = \frac{1}{r^m}$$

Price of a varying annuity

$$(Ia)_{\overline{n}|} = Pa_{\overline{n}|} + D\left[\frac{a_{\overline{n}|} - nv^n}{i}\right]$$

Price of a bond

$$P = NCa_{\overline{n}|} + Nv^n$$