

# Bank capital and capital regulation

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# Overview

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## **Bank capital**

- Balance sheet capital accumulation
- Internal and external capital flows
- Regulatory capital

## **Internal and external capital flows**

- Components of period profit/loss
- External flows

## **Capital adequacy and bank behavior**

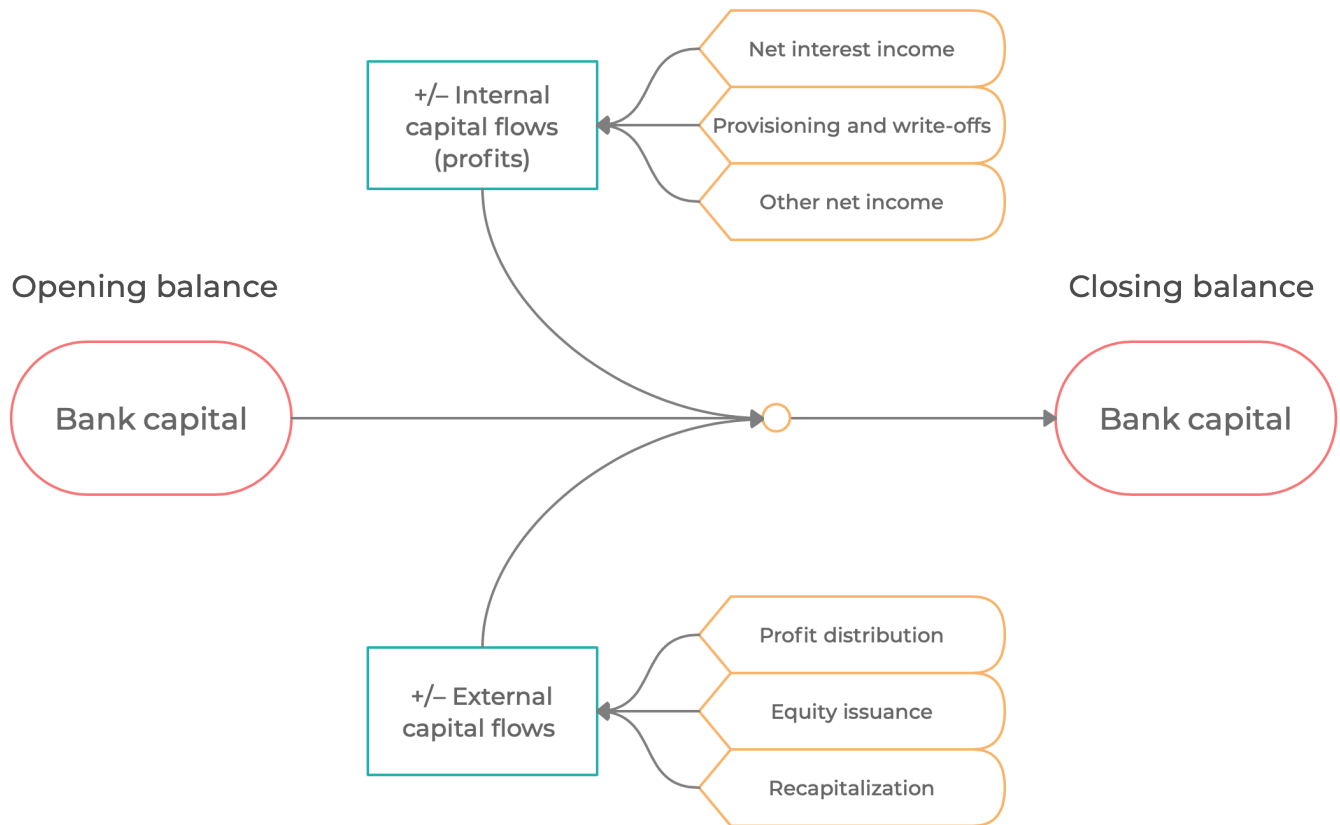
- Regulatory capital
- Target capital levels

## **Feedback to bank lending**

- Regulatory capital shortfall
- Nonlinear cost of bank capital

# Bank capital accumulation

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## Bank capital accumulation

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$$bk_t = bk_{t-1} + prof_t + xcf_t$$

- $bk_t$  is bank capital (balance sheet capital)
- $prof_t$  is an internal flow of capital (retained profit or loss, PnL) recorded on the closing balance of the balance sheets at  $t - 1$  and credit events throughout  $t$
- $xcf_t$  is an external flow of capital throughout  $t$ : dividends paid out (–), new equity issuance (+), equity withdrawals by parents (–), recapitalization flows (+), etc.

## Internal capital flows (Period profit/loss)

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Components of period profit/loss

- Interest income on loans (by segments)
- Income on other assets
- Interest expense on non-equity liabilities (by currency of denomination)
- Provisioning and write-offs
- Exchange rate valuation
- Other net income (proxy for fees, commissions, labor costs, etc.)

$$\begin{aligned} prof_t = & \sum r l_{t-1}^k (lp_t^{0k} + lnc_t^{0k}) \\ & + r o n a_{t-1} o n a_{t-1} \\ & - r d_{t-1}^{lcy} d_t^{0lcy} - r d_{t-1}^{fcy} d_t^{0fcy} \\ & - \sum (a_t^k - a_{t-1}^k + w_t^k) \\ & + \sum l_{t-1}^k (j_t - 1) - d_{t-1}^{fcy} \left( \frac{e_t}{e_{t-1}} - 1 \right) \\ & + c_1 \cdot t n a_{t-1} \end{aligned}$$

# External capital flows

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Switch between two extreme cases

- $c_1 \rightarrow 0$  External capital flows do not respond to fluctuations in capital adequacy ratio. Bank owners do not adjust external flows (e.g. dividends) based on the current profit/loss at all.
- $c_1 \rightarrow 1$  External capital flows bring capital adequacy ratio to its target level at all times. Bank owners adjust external flows (e.g. cut dividends, add capital) to always ensure  $car_t = car_t^{\text{tar}}$ .

$$(1 - c_1) \left( \left[ \frac{xcf}{bk} \right]_t - \left[ \frac{xcf}{bk} \right]_{ss} \right) - c_1 (car_t - car_t^{\text{tar}}) = 0$$

# Regulatory capital and CAR

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- Balance sheet capital,  $bk_t$ , and regulatory capital,  $bg_t$ , differ in their definitions and reporting standards
- Either use a mechanical reconciliation process (as is here) or model the details of the differences

## Regulatory capital

$$bg_t = \left[ \frac{bg}{bk} \right]_t bk_t$$

## Standard capital adequacy ratio

$$car_t = \frac{bg_t}{riskw_t \cdot [(l_t - a_t) + ona_t]}$$

- $riskw_t$  is the effective average risk weight, an exogenous variable

## Comfort (target) levels of CAR

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In equilibrium (steady state), banks target a comfort level of CAR

$$car_t \longrightarrow car_t^{\text{tar}}$$

$$car_t^{\text{tar}} = car_t^{\text{min}} + car_t^{\text{exc}}$$

where

- $car_t^{\text{min}}$  is the regulatory minimum including regulatory buffers
- $car_t^{\text{exc}}$  is the excess capital target above the regulatory minimum targeted by banks. Banks are motivated to hold excess capital to avoid approaching regulatory minimum in case of unexpected adverse shocks.



# Feedback to bank lending

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## Capital adequacy risk surcharge

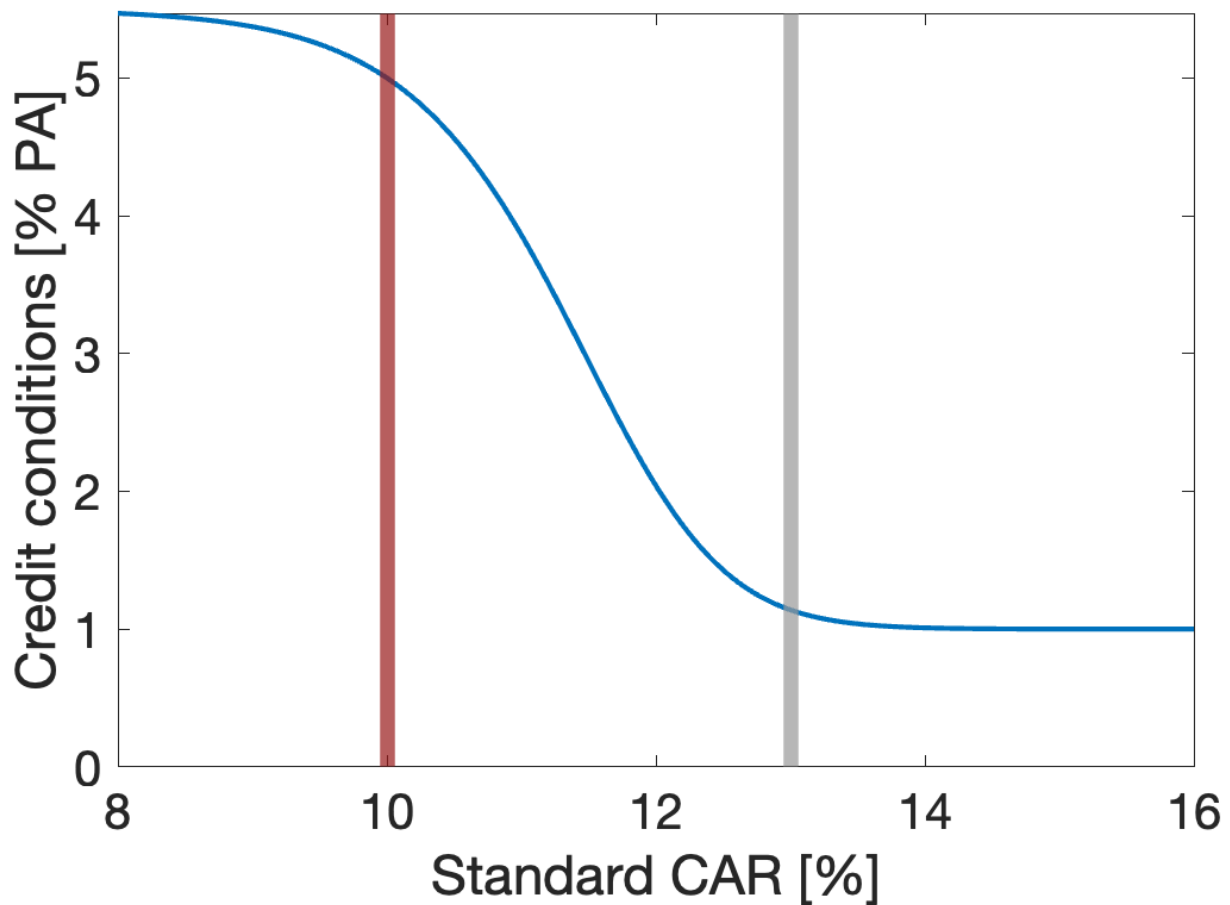
Negative shocks can push the the actual CAR  $car_t$  below the optimal level  $car^{tar}$ . If  $car_t$  approaches regulatory minimum  $car_t^{\min}$ , capital shortfall triggers increase in capital adequacy risk surcharge  $rx_t$ . The surcharge is added to the lending rates as the bank attempts to increase profitability as well as reduce lending to shrink its balance sheet.

- $car_t < car_t^{tar}$  Tighter lending conditions: Increase spreads, reduce leverage
- $car_t > car_t^{tar}$  Lax lending conditions: Reduce spreads, expand balance sheets

## Functional form of risk surcharge

The risk surcharge is a non-linear function of the distance to regulatory capital shortfall (distance to  $car_t^{\min}$ )

$$rx_t = \underline{rx} + (\overline{rx} - \underline{rx}) \left[ 1 + \exp - \frac{car_t - car_t^{\min} - \mu}{\sigma} \right]^{-\exp \nu}$$



Parameter	Meaning
$\mu$	Location parameter: moves the curve left or right
$\sigma$	Scale parameter: makes the curve steeper/flatter
$\nu$	Shape parameter: makes the curve asymmetric, heavy left/heavy right
$\underline{rx}$	Lower bound

Parameter	Meaning
$\bar{r}x$	Upper bound