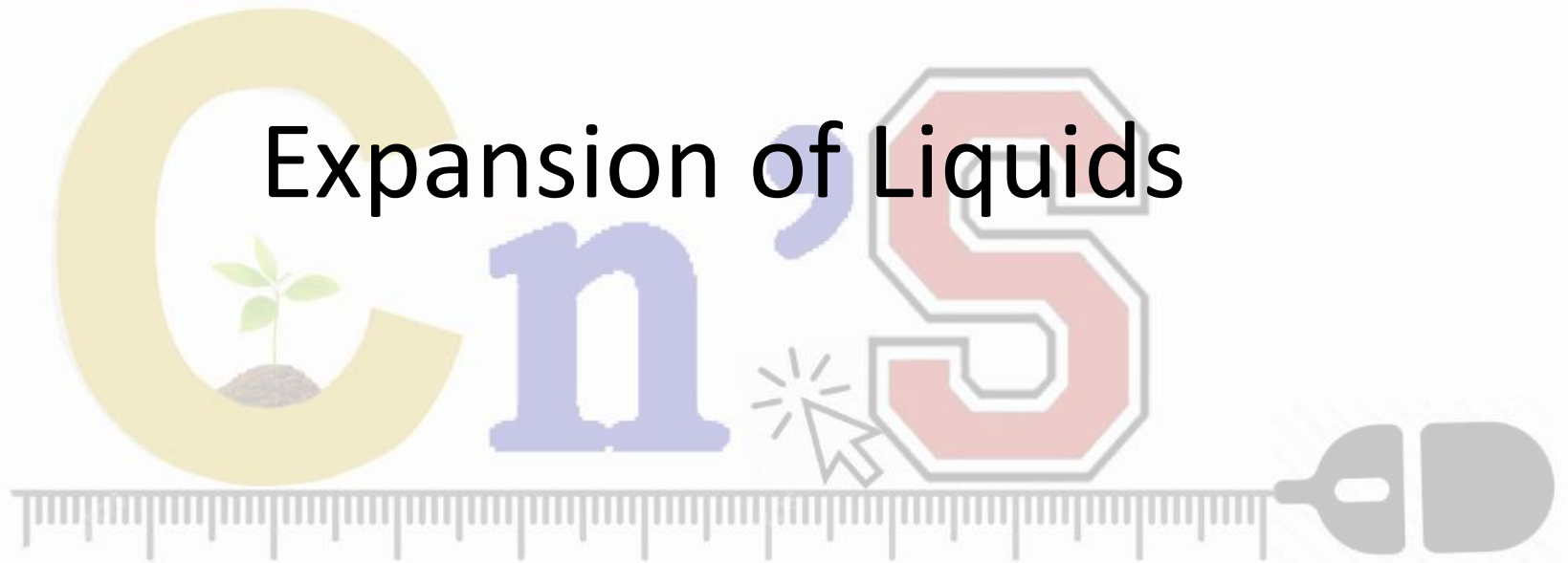


# Expansion of Liquids



# Expansion of Liquids

In liquids only expansion in volume takes place on heating.

## Apparent Expansion of Liquids

When expansion of the container containing liquid, on heating is not taken into account then observed expansion is called apparent expansion of liquids.

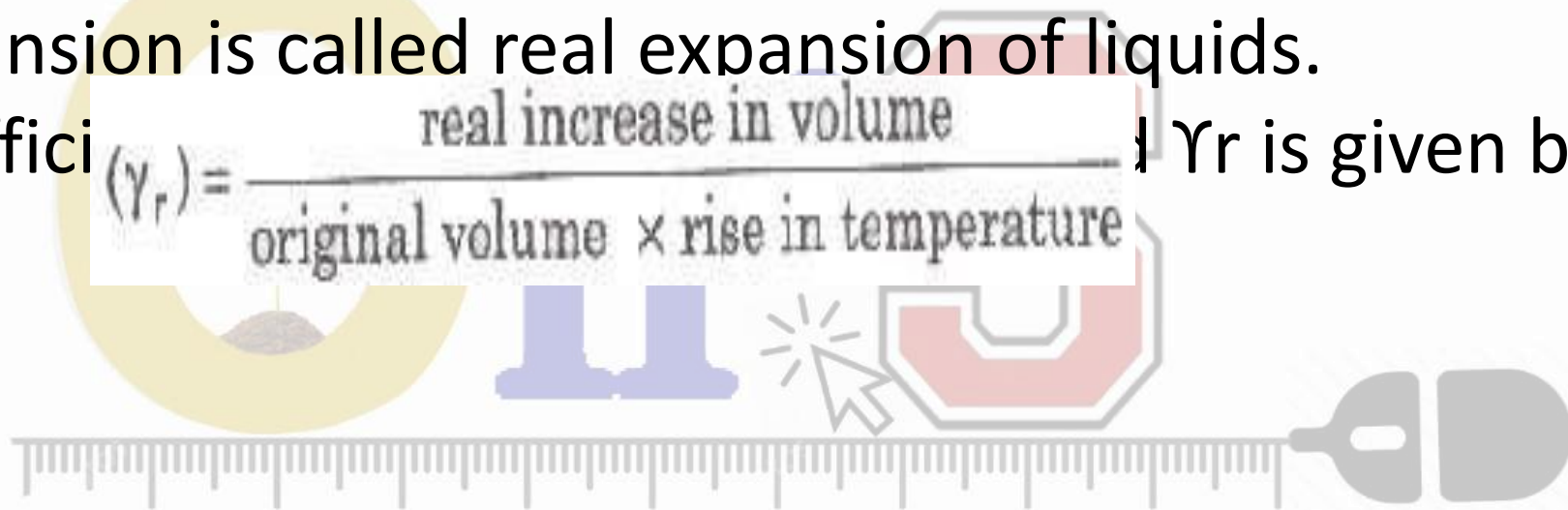
- Coefficient of apparent expansion of liquid  $\gamma_a$  is given by

$$(\gamma_a) = \frac{\text{apparent increase in volume}}{\text{original volume} \times \text{rise in temperature}}$$

# Real Expansion of Liquids

When expansion of the container, containing liquid, on heating is also taken into account, then observed expansion is called real expansion of liquids.

Coefficient  $(\gamma_r) = \frac{\text{real increase in volume}}{\text{original volume} \times \text{rise in temperature}}$   $\gamma_r$  is given by



- Both  $\gamma_r$ , and  $\gamma_a$  are measured in  $^{\circ}\text{C}^{-1}$ .
- We can show that  $\gamma_r = \gamma_a + \gamma_g$
- where  $\gamma_r$  and  $\gamma_a$  are coefficient of real and

# VARIATION OF DENSITY WITH TEMPERATURE

$$d_{\theta} = d_0 / (1 + \gamma_{\theta})$$

- Where  $d_0$  is the density at  $0^{\circ}\text{C}$

- $d_2 - d_1 = d_1 \gamma (t_2 - t_1)$

Where  $d_2$  &  $d_1$  are densities at  $t_2$  &  $t_1$

# Expansion of Gases

- Pressure coefficient of a gas is the ratio of increase in pressure for  $1^{\circ}\text{C}$  rise in temperature to the pressure at  $0^{\circ}\text{C}$ , provided the volume of the gas is kept constant.

$$\gamma_p = \frac{P_t - P_0}{P_0 \Delta \theta}$$

$$P_0 \Delta \theta$$

# Volume coefficient of a Gas

Volume coefficient of a gas is the ratio of increase in volume for  $1^{\circ}\text{C}$  rise in temperature to the volume at  $0^{\circ}\text{C}$ , provided the pressure of the gas is kept constant.

$$\gamma_v = \frac{V_t - V_0}{V_0 \Delta \theta}$$

$$V_0 \Delta \theta$$

$$\gamma_p = \gamma_v = 1/273$$

## 2. Expansion of Gases

There are two types of coefficient of expansion in gases

(i) Volume Coefficient ( $\gamma_v$ ) At constant pressure, the change in volume per unit volume per degree celsius is called volume coefficient.

$$\gamma_v = \frac{V_2 - V_1}{V_0 (t_2 - t_1)}$$

where  $V_0$ ,  $V_1$ , and  $V_2$  are volumes of the gas at  $0^\circ\text{C}$ ,  $t_1^\circ\text{C}$  and  $t_2^\circ\text{C}$ .

(ii) Pressure Coefficient ( $\gamma_p$ ) At constant volume, the change in pressure per unit pressure per degree celsius is called pressure coefficient.

$$\gamma_p = \frac{p_2 - p_1}{p_0 (t_2 - t_1)}$$

where  $p_0$ ,  $p_1$  and  $p_2$  are pressure of the gas at  $0^\circ\text{C}$ ,  $t_1^\circ\text{C}$  and  $t_2^\circ\text{C}$ .

# •Thermal expansion of water

Water has an anomalous property: betwn 0 °C and 4 °C its coefficient expansion is *negative*.

Happens in  
most solids,  
liquids & gases

Increase in  
the size due to  
an increase in  
temperature

If tem↓ then↓  
size

But Water is an exception, it  
expands as it becomes a solid!



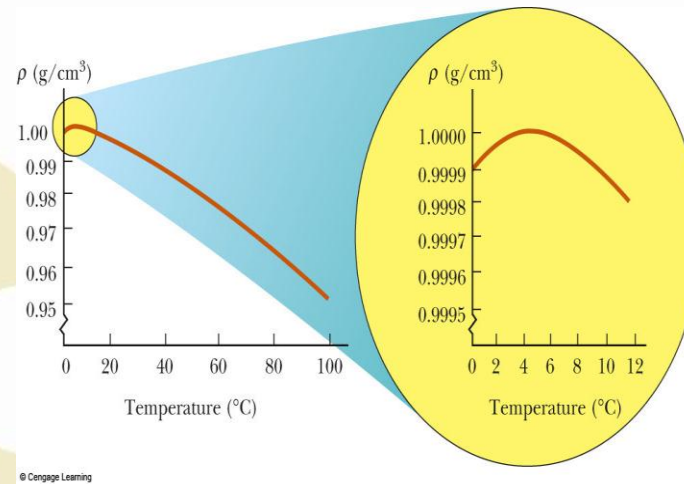
# Anomalous Expansion of Water.

(1) Generally matter expands on heating and contracts on cooling. In case of water, it expands on heating if its temperature is greater than  $4^{\circ}\text{C}$ . In the range  $0^{\circ}\text{C}$  to  $4^{\circ}\text{C}$ , water contracts on heating and expands on cooling, i.e.  $\gamma$  is negative. This behaviour of water in the range from  $0^{\circ}\text{C}$  to  $4^{\circ}\text{C}$  is called anomalous expansion.

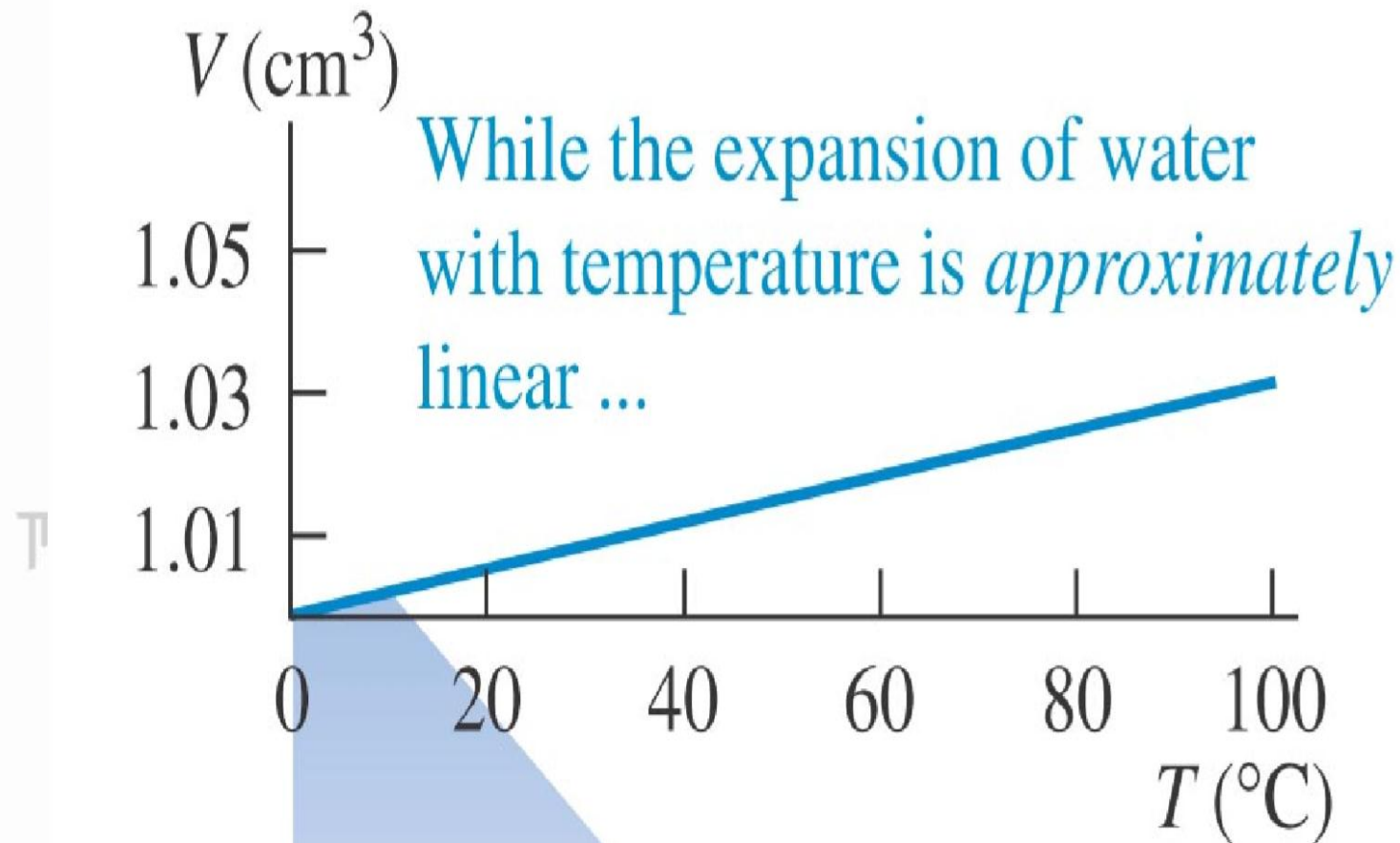
(2) The anomalous behaviour of water arises due to the fact that water has three types of

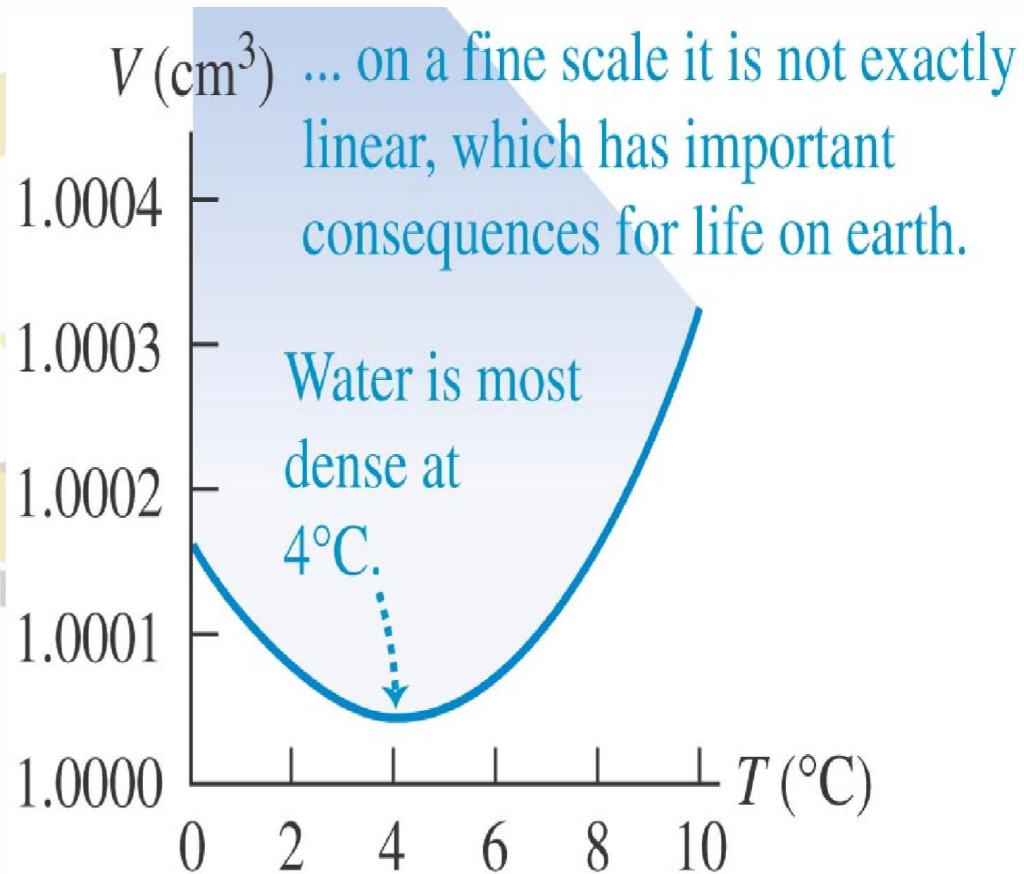
. (3) At  $4^{\circ}\text{C}$ , density of water is maximum while its specific volume is minimum. During winter when the water at the surface of a lake cools below  $4^{\circ}\text{C}$  by cool air, it expands and becomes lighter than water below. Therefore the water cooled below  $4^{\circ}\text{C}$  stays on the surface and freezes when the temperature of surroundings falls below  $0^{\circ}\text{C}$ . Thus the lake freezes first at the surface and water in contact with ice has temperature  $0^{\circ}\text{C}$  while at the bottom of the lake  $4^{\circ}\text{C}$  [as

# Unusual Behavior of Water

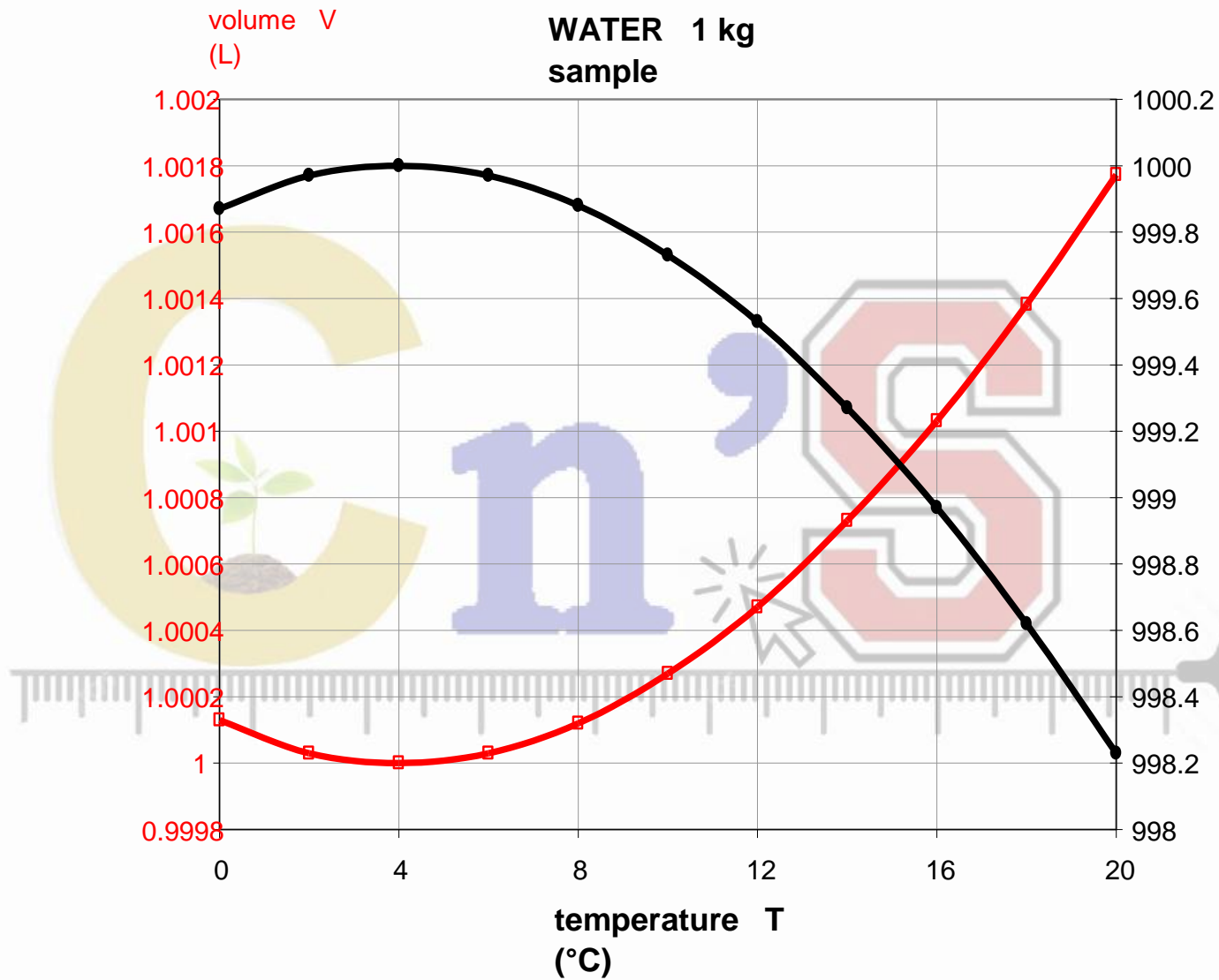


- As the temperature of water increases from 0 $^\circ\text{C}$  to 4  $^\circ\text{C}$ , it contracts and its density increases
- Above 4  $^\circ\text{C}$ , water exhibits the expected expansion with increasing temperature
- Maximum density of water is 1000  $\text{kg/m}^3$  at 4  $^\circ\text{C}$





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# Consequence: lakes freeze from the top down

- Above 4 °C water cools at surface and sinks (greater density)
- Below 4 °C, water cools but stays at surface – Water at bottom stays warmer.
- Below 0 °C ice forms; ice is also less dense than water.
- Life can remain alive under the ice.

