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## **Chapter 1**

# Main Page

This is the main page for the Ginkgo library pdf documentation. The repository is hosted on github. Documentation on aspects such as the build system, can be found at the Installation Instructions page. The Example programs can help you get started with using Ginkgo.

#### 1.0.0.1 Modules

The Ginkgo library can be grouped into modules and these modules form the basic building blocks of Ginkgo. The modules can be summarized as follows:

- Executors: Where do you want your code to be executed?
- · Linear Operators: What kind of operation do you want Ginkgo to perform?
  - Solvers : Solve a linear system for a given matrix.
  - Preconditioners: Precondition a system for a solve.
  - SpMV employing different Matrix formats: Perform a sparse matrix vector multiplication with a particular matrix format.
- Logging : Monitor your code execution.
- Stopping criteria: Manage your iteration stopping criteria.

2 Main Page

## **Chapter 2**

## **Installation Instructions**

## 2.0.1 Building

Use the standard CMake build procedure:

```
mkdir build; cd build cmake [OPTIONS] .. && cmake --build .
```

For Microsoft Visual Studio, use cmake --build . --config <build\_type> to decide the build type. The possible options are Debug, Release, RelWithDebInfo and MinSizeRel.

Replace [OPTIONS] with desired cmake options for your build. Ginkgo adds the following additional switches to control what is being built:

- -DGINKGO\_DEVEL\_TOOLS={ON, OFF} sets up the build system for development (requires pre-commit, will also download the clang-format pre-commit hook), default is OFF. The default behavior installs a pre-commit hook, which disables git commits. If it is set to ON, a new pre-commit hook for formatting will be installed (enabling commits again). In both cases the hook may overwrite a user defined pre-commit hook when Ginkgo is used as a submodule.
- -DGINKGO\_MIXED\_PRECISION={ON, OFF} compiles true mixed-precision kernels instead of converting data on the fly, default is OFF. Enabling this flag increases the library size, but improves performance of mixed-precision kernels.
- -DGINKGO\_BUILD\_TESTS={ON, OFF} builds Ginkgo's tests (will download googletest), default is ON.
- -DGINKGO\_FAST\_TESTS={ON, OFF} reduces the input sizes for a few slow tests to speed them up, default is OFF.
- -DGINKGO\_BUILD\_BENCHMARKS={ON, OFF} builds Ginkgo's benchmarks (will download gflags and nlohmann-json), default is ON.
- -DGINKGO\_BUILD\_EXAMPLES={ON, OFF} builds Ginkgo's examples, default is ON
- -DGINKGO\_BUILD\_EXTLIB\_EXAMPLE={ON, OFF} builds the interfacing example with deal.II, default is OFF.
- -DGINKGO\_BUILD\_REFERENCE={ON, OFF} build reference implementations of the kernels, useful for testing, default is ON
- -DGINKGO\_BUILD\_OMP={ON, OFF} builds optimized OpenMP versions of the kernels, default is ON if the selected C++ compiler supports OpenMP, OFF otherwise.
- -DGINKGO\_BUILD\_CUDA={ON, OFF} builds optimized cuda versions of the kernels (requires CUDA), default is ON if a CUDA compiler could be detected, OFF otherwise.

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• -DGINKGO\_BUILD\_DPCPP={ON, OFF} is deprecated. Please use GINKGO\_BUILD\_SYCL instead.

- -DGINKGO\_BUILD\_SYCL={ON, OFF} builds optimized SYCL versions of the kernels (requires CM← AKE\_CXX\_COMPILER to be set to the dpcpp or icpx compiler). The default is ON if CMAKE\_CX← X\_COMPILER is a SYCL compiler, OFF otherwise. Due to some differences in IEEE 754 floating point numberhandling in the Intel SYCL compilers, Ginkgo tests may fail unless compiled with -DCMAKE\_CXX← \_FLAGS=-ffp-model=precise
- -DGINKGO\_BUILD\_HIP={ON, OFF} builds optimized HIP versions of the kernels (requires HIP), default is ON if an installation of HIP could be detected, OFF otherwise.
- -DCMAKE\_HIP\_ARCHITECTURES="gpuarch1; gpuarch2" the AMDGPU targets to be passed to the compiler. If empty, compiler chooses based on the available GPUs.
- -DGINKGO\_BUILD\_HWLOC={ON, OFF} builds Ginkgo with HWLOC. Default is OFF.
- -DGINKGO\_BUILD\_DOC={ON, OFF} creates an HTML version of Ginkgo's documentation from inline comments in the code. The default is OFF.
- -DGINKGO\_DOC\_GENERATE\_EXAMPLES={ON, OFF} generates the documentation of examples in Ginkgo. The default is ON.
- -DGINKGO\_DOC\_GENERATE\_PDF={ON, OFF} generates a PDF version of Ginkgo's documentation from inline comments in the code. The default is OFF.
- -DGINKGO\_DOC\_GENERATE\_DEV={ON, OFF} generates the developer version of Ginkgo's documentation. The default is OFF.
- -DGINKGO\_WITH\_CLANG\_TIDY={ON, OFF} makes Ginkgo call clang-tidy to find programming issues. The path can be manually controlled with the CMake variable -DGINKGO\_CLANG\_TIDY\_PA← TH=<path>. The default is OFF.
- -DGINKGO\_WITH\_IWYU={ON, OFF} makes Ginkgo call iwyu to find include issues. The path can be manually controlled with the CMake variable -DGINKGO\_IWYU\_PATH=<path>. The default is OFF.
- -DGINKGO\_CHECK\_CIRCULAR\_DEPS={ON, OFF} enables compile-time checks for circular dependencies between different Ginkgo libraries and self-sufficient headers. Should only be used for development purposes. The default is OFF.
- -DGINKGO\_VERBOSE\_LEVEL=integer sets the verbosity of Ginkgo.
  - 0 disables all output in the main libraries,
  - 1 enables a few important messages related to unexpected behavior (default).
- GINKGO\_INSTALL\_RPATH allows setting any RPATH information when installing the Ginkgo libraries. If this is OFF, the behavior is the same as if all other RPATH flags are set to OFF as well. The default is ON.
- GINKGO\_INSTALL\_RPATH\_ORIGIN adds \$ORIGIN (Linux) or @loader\_path (MacOS) to the installation RPATH. The default is ON.
- GINKGO\_INSTALL\_RPATH\_DEPENDENCIES adds the dependencies to the installation RPATH. The default is OFF.
- -DCMAKE\_INSTALL\_PREFIX=path sets the installation path for make install. The default value is usually something like /usr/local.
- -DCMAKE\_BUILD\_TYPE=type specifies which configuration will be used for this build of Ginkgo. The
  default is RELEASE. Supported values are CMake's standard build types such as DEBUG and RELEASE and
  the Ginkgo specific COVERAGE, ASAN (AddressSanitizer), LSAN (LeakSanitizer), TSAN (ThreadSanitizer)
  and UBSAN (undefined behavior sanitizer) types.
- -DBUILD\_SHARED\_LIBS={ON, OFF} builds ginkgo as shared libraries (OFF) or as dynamic libraries (ON), default is ON.

- -DGINKGO\_JACOBI\_FULL\_OPTIMIZATIONS={ON, OFF} use all the optimizations for the CUDA Jacobi algorithm. OFF by default. Setting this option to ON may lead to very slow compile time (>20 minutes) for the jacobi\_generate\_kernels.cu file and high memory usage.
- -DCMAKE\_CUDA\_HOST\_COMPILER=path instructs the build system to explicitly set CUDA's host compiler to the path given as argument. By default, CUDA uses its toolchain's host compiler. Setting this option may help if you're experiencing linking errors due to ABI incompatibilities. This option is supported since CMake 3.8 but documented starting from 3.10.
- -DGINKGO\_CUDA\_ARCHITECTURES=<list> where <list> is a semicolon (;) separated list of architectures. Supported values are:
  - Auto
  - Kepler, Maxwell, Pascal, Volta, Turing, Ampere
  - CODE, CODE (COMPUTE), (COMPUTE)

Auto will automatically detect the present CUDA-enabled GPU architectures in the system. Kepler, Maxwell, Pascal, Volta and Ampere will add flags for all architectures of that particular NVIDIA GPU generation. COMPUTE and CODE are placeholders that should be replaced with compute and code numbers (e.g. for compute\_70 and sm\_70 COMPUTE and CODE should be replaced with 70. Default is Auto. For a more detailed explanation of this option see the ARCHITECTURES specification list section in the documentation of the CudaArchitectureSelector CMake module.

Additionally, the following CMake options have effect on the build process:

• -DCMAKE\_EXPORT\_PACKAGE\_REGISTRY={ON,OFF} if set to ON the build directory will be stored in the current user's CMake package registry.

```
For example, to build everything (in debug mode), use:
```

```
cmake .. -BDebug -DCMAKE_BUILD_TYPE=Debug -DGINKGO_DEVEL_TOOLS=ON \
-DGINKGO_BUILD_TESTS=ON -DGINKGO_BUILD_REFERENCE=ON -DGINKGO_BUILD_OMP=ON \
-DGINKGO_BUILD_CUDA=ON -DGINKGO_BUILD_HIP=ON
cmake --build Debug
```

NOTE: Ginkgo is known to work with the Unix Makefiles, Ninja, MinGW Makefiles and Visual Studio 16 2019 based generators. Other CMake generators are untested.

### 2.0.2 Building Ginkgo in Windows

Depending on the configuration settings, some manual work might be required:

- Build Ginkgo with Debug mode: Some Debug build specific issues can appear depending on the machine and environment: When you encounter the error message ld: error: export ordinal too large, add the compilation flag -O1 by adding -DCMAKE\_CXX\_FLAGS=-O1 to the CMake invocation.
- Build Ginkgo in *MinGW*:\ If encountering the issue cclplus.exe: out of memory allocating 65536 bytes, please follow the workaround in reference, or trying to compile ginkgo again might work.

#### 2.0.3 Building Ginkgo with HIP support

Ginkgo provides a HIP backend. This allows to compile optimized versions of the kernels for either AMD or NV  $\leftarrow$  IDIA GPUs. The CMake configuration step will try to auto-detect the presence of HIP either at /opt/rocm/hip or at the path specified by HIP\_PATH as a CMake parameter (-DHIP\_PATH=) or environment variable (export HIP\_PATH=), unless -DGINKGO\_BUILD\_HIP=ON/OFF is set explicitly.

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#### 2.0.3.1 Changing the paths to search for HIP and other packages

All HIP installation paths can be configured through the use of environment variables or CMake variables. This way of configuring the paths is currently imposed by the HIP tool suite. The variables are the following:

- CMake -DROCM\_PATH= or environment export ROCM\_PATH=: sets the ROCM installation path. The default value is /opt/rocm/.
- CMake -DHIP\_CLANG\_PATH or environment export HIP\_CLANG\_PATH=: sets the HIP compatible clang binary path. The default value is \${ROCM\_PATH}/llvm/bin.
- CMake -DHIP\_PATH= or environment export HIP\_PATH=: sets the HIP installation path. The default value is \${ROCM\_PATH}/hip.
- CMake -DHIPBLAS\_PATH= or environment export HIPBLAS\_PATH=: sets the hipBLAS installation path. The default value is \$ {ROCM\_PATH} / hipblas.
- CMake -DHIPSPARSE\_PATH= or environment export HIPSPARSE\_PATH=: sets the hipSPARSE installation path. The default value is \${ROCM\_PATH}/hipsparse.
- CMake -DHIPFFT\_PATH= or environment export HIPFFT\_PATH=: sets the hipFFT installation path. The default value is \${ROCM\_PATH}/hipfft.
- CMake -DROCRAND\_PATH= or environment export ROCRAND\_PATH=: sets the rocRAND installation path. The default value is \${ROCM\_PATH}/rocrand.
- CMake -DHIPRAND\_PATH= or environment export HIPRAND\_PATH=: sets the hipRAND installation path. The default value is \${ROCM\_PATH}/hiprand.
- environment export CUDA\_PATH=: where hipcc can find CUDA if it is not in the default /usr/local/cuda path.

## 2.0.3.2 HIP platform detection of AMD and NVIDIA

Ginkgo relies on CMake to decide which compiler to use for HIP. To choose nvcc instead of the default ROCm clang++, set the corresponding environment variable:

export HIPCXX=nvcc

Note that this option is currently not being tested in our CI pipelines.

### 2.0.4 Third party libraries and packages

Ginkgo relies on third party packages in different cases. These third party packages can be turned off by disabling the relevant options.

- GINKGO\_BUILD\_TESTS=ON: Our tests are implemented with Google Test;
- GINKGO\_BUILD\_BENCHMARKS=ON: For argument management we use gflags and for JSON parsing we use nlohmann-json;
- GINKGO BUILD HWLOC=ON: hwloc to detect and control cores and devices.
- GINKGO\_BUILD\_HWLOC=ON and GINKGO\_BUILD\_TESTS=ON: libnuma is required when testing the functions provided through MachineTopology.
- GINKGO\_BUILD\_EXAMPLES=ON: OpenCV is required for some examples, they are disabled when OpenCV is not available.

- GINKGO\_BUILD\_DOC=ON: doxygen is required to build the documentation and additionally graphviz is required to build the class hierarchy graphs.
- METIS is required when using the NestedDissection reordering functionality. If METIS is not found, the functionality is disabled.
- PAPI (>= 7.1.0) is required when using the Papi logger. If PAPI is not found, the functionality is disabled.

Ginkgo attempts to use pre-installed versions of these package if they match version requirements using find-package. Otherwise, the configuration step will download the files for each of the packages GTest, gflags, nlohmann-json and hwloc and build them internally.

Note that, if the external packages were not installed to the default location, the CMake option <code>-DCMAKE\_</code> <code>PREFIX\_PATH=<path-list></code> needs to be set to the semicolon (;) separated list of install paths of these external packages. For more Information, see the <code>CMake documentation</code> for <code>CMAKE\_PREFIX\_PATH</code> for details.

For convenience, the options GINKGO\_INSTALL\_RPATH [\_.\*] can be used to bind the installed Ginkgo shared libraries to the path of its dependencies.

### 2.0.5 Installing Ginkgo

To install Ginkgo into the specified folder, execute the following command in the build folder make install

If the installation prefix (see  $\texttt{CMAKE\_INSTALL\_PREFIX}$ ) is not writable for your user, e.g. when installing Ginkgo system-wide, it might be necessary to prefix the call with sudo.

After the installation, CMake can find ginkgo with  $find\_package$  (Ginkgo). An example can be found in the test\_install.

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## Chapter 3

# **Testing Instructions**

### 3.0.1 Running the unit tests

You need to compile ginkgo with -DGINKGO\_BUILD\_TESTS=ON option to be able to run the tests.

#### 3.0.1.1 Using make test

After configuring Ginkgo, use the following command inside the build folder to run all tests:

The output should contain several lines of the form:

To run only a specific test and see more details results (e.g. if a test failed) run the following from the build folder:

where path/to/test is the path returned by make test.

#### 3.0.1.2 Using make quick\_test

After compiling Ginkgo, use the following command inside the build folder to run a small subset of tests that should execute quickly:

make quick\_test

These tests do not use GPU features except for a few device property queries, so they may still fail if Ginkgo was compiled with GPU support, but no such GPU is available. The output is equivalent to make test.

#### 3.0.1.3 Using CTest

The tests can also be ran through CTest from the command line, for example when in a configured build directory: CTEST - T start -T build -T test -T submit

Will start a new test campaign (usually in Experimental mode), build Ginkgo with the set configuration, run the tests and submit the results to our CDash dashboard.

Another option is to use Ginkgo's CTest script which is configured to build Ginkgo with default settings, runs the tests and submits the test to our CDash dashboard automatically.

To run the script, use the following command:

```
ctest -S cmake/CTestScript.cmake
```

The default settings are for our own CI system. Feel free to configure the script before launching it through variables or by directly changing its values. A documentation can be found in the script itself.

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# **Chapter 4**

# Running the benchmarks

In addition to the unit tests designed to verify correctness, Ginkgo also includes an extensive benchmark suite for checking its performance on all Ginkgo supported systems. The purpose of Ginkgo's benchmarking suite is to allow easy and complete reproduction of Ginkgo's performance, and to facilitate performance debugging as well. Most results published in Ginkgo papers are generated thanks to this benchmarking suite and are accessible online under the ginkgo-data repository. These results can also be used for performance comparison in order to ensure that you get similar performance as what is published on this repository.

To compile the benchmarks, the flag <code>-DGINKGO\_BUILD\_BENCHMARKS=ON</code> has to be set during the <code>cmake</code> step. In addition, the <code>ssget command-line utility</code> has to be installed on the system. The purpose of this file is to explain in detail the capacities of this benchmarking suite as well as how to properly setup everything.

There are two ways to benchmark Ginkgo. When compiling the benchmark suite, executables are generated for collecting matrix statistics, running sparse-matrix vector product, solvers (possibly distributed) benchmarks. Another way to run benchmarks is through the convenience script run\_all\_benchmarks.sh, but not all features are exposed through this tool!

Here is a short description of the content of this file:

- 1. Ginkgo setup and best practice guidelines
- 2. Installing and using the ssget tool to fetch the SuiteSparse matrices.
- 3. Running benchmarks manually
- 4. Benchmarking with the script utility
- 5. How to publish the benchmark results online and use the Ginkgo Performance Explorer (GPE) for performance analysis (optional).
- 6. Using the benchmark suite for performance debugging thanks to the loggers.
- 7. Available benchmark customization options with the script utility.

# 4.0.1 1: Ginkgo setup and best practice guidelines

Before benchmarking Ginkgo, make sure that you follow the general guidelines in order to ensure best performance.

1. The code should be compiled in Release mode.

- 2. Make sure the machine has no competing jobs. On a Linux machine multiple commands can be used, last shows the currently opened sessions, top or htop allows to show the current machine load, and if considering using specific GPUs, nvidia-smi or room-smi can be used to check their load.
- 3. By default, Ginkgo's benchmarks will always do at least one warm-up run. For better accuracy, every benchmark is also averaged over 10 runs, except for the solver benchmark which are usually fairly long. These parameters can be tuned at the command line to either shorten benchmarking time or improve benchmarking accuracy.

In addition, the following specific options can be considered:

- 1. When specifically using the adaptive block jacobi preconditioner, enable the GINKGO\_JACOBI\_FULL\_O← PTIMIZATIONS CMake flag. Be careful that this will use much more memory and time for the compilation due to compiler performance issues with register optimizations, in particular.
- 2. The current benchmarking setup also allows to benchmark only the overhead by using as either (or for all) preconditioner/spmv/solver, the special overhead LinOp. If your purpose is to check Ginkgo's overhead, make sure to try this mode.

# 4.0.2 2: Using ssget to fetch the matrices

To benchmark ginkgo, matrices need to be provided as input in the Matrix Market format. A convenient way is to run benchmark with the SuiteSparse matrix collection. A helper tool, the ssget command—line utility can be used to facilitate downloading and extracting matrices from the suitesparse collection. When running the benchmarks with the helper script run\_all\_benchmarks.sh (or calling make benchmark), the ssget tool is required.

To install ssget, access the repository and copy the file ssget into a directory present in your PATH variable as per the tool's README.md instructions. The tool can be installed either in a global system path or a local directory such as \$HOME/.local/bin. After installing the tool, it is important to review the ssget script and configure as needed the variable ARCHIVE LOCATION on line 39. This is where the matrices will be stored into.

The Ginkgo benchmark can be set to run on only a portion of the SuiteSparse matrix collection as we will see in the following section. Please note that the entire collection requires roughly 100GB of disk storage in its compressed format, and roughly 25GB of additional disk space for intermediate data (such us uncompressing the archive). Additionally, the benchmark runs usually take a long time (SpMV benchmarks on the complete collection take roughly 24h using the K20 GPU), and will stress the system.

Before proceeding, it can be useful in order to save time to download the matrices as preparation. This can be done by using the ssget -f -i i command where i is the ID of the matrix to be downloaded. The following loop allows to download the full SuiteSparse matrix collection:

```
for i in $(seq 0 $(ssget -n)); do
    ssget -f -i ${i}
done
```

Note that ssget can also be used to query properties of the matrix and filter the matrices which are downloaded. For example, the following will download only positive definite matrices with less than 500M non zero elements and 10M columns. Please refer to the ssget documentation for more information.

```
for i in $(seq 0 $(ssget -n)); do
    posdef=$(ssget -p posdef -i ${i})
    cols=$(ssget -p cols -i ${i})
    nnz=$(ssget -p nonzeros -i ${i})
    if [ "$posdef" -eq 1 -a "$cols" -lt 10000000 -a "$nnz" -lt 500000000 ]; then
        ssget -f -i ${i}
    fi
done
```

# 4.0.3 3: Running benchmarks manually

When compiling Ginkgo with the flag  $-\mathrm{DGINKGO\_BUILD\_BENCHMARKS=ON}$ , a suite of executables will be generated depending on the CMake configuration. These executables are the backbone of the benchmarking suite. Note that all of these executables describe the available options and the required input format when running them with the --help option. All executables have multiple variants depending on the precision, by default double precision is used for the type of values, but variants with single and complex (single and double) value types are also available. Here is a non exhaustive list of the available benchmarks:

- blas/blas: supports benchmarking many of Ginkgo's BLAS operations: dot products, axpy, copy, etc.
- conversion/conversion: conversion between matrix formats.
- matrix\_generator/matrix\_generator: mostly allows generating block diagonal matrices (to benchmark the block-jacobi preconditioner).
- matrix\_statistics/matrix\_statistics: computes size and other matrix statistics (such as variance, load imbalance, ...).
- preconditioner/preconditioner: benchmarks most Ginkgo preconditioner.
- solver/solver: benchmark most of Ginkgo's solvers in a non distributed setting.
- sparse\_blas/sparse\_blas: benchmarks Sparse BLAS operations, such as SpGEMM, SpGEAM, transpose.
- spmv/spmv: benchmarks Ginkgo's matrix formats (Sparse-Matrix Vector product).

Optionally when compiling with MPI support:

- blas/distributed/multi\_vector: measures BLAS performance on (distributed) multi-vectors.
- solver/distributed/solver: distributed solver benchmarks.
- spmv/distributed/spmv: distributed matrix Sparse-Matrix Vector (SpMV) product benchmark.

All benchmarks require input data as in a  $\tt JSON$  format. The json file has to consist of exactly one array, and within that array the test cases are defined. The exact syntax can change between executables, the --help option will explain the necessary  $\tt JSON$  input format. For example for the  $\tt spmv$  benchmark case, and many other benchmarks the following minimal input should be provided:

```
{
    "filename": "path/to/your/matrix",
    "rhs": "path/to/your/rhs"
},
{ ... }
```

The files have to be in matrix market format.

Some benchmarks require some extra fields. For example the solver benchmarks requires the field "optimal"  $\leftarrow$  : {"spmv": "matrix format (such as csr)"}. This is automatically populated when running the spmv benchmark which finds the optimal (fastest) format among all requested formats.

After writing the necessary data in a JSON file, the benchmark can be called by passing in the input via stdin, i.e. ./solver < input.json

The output of our benchmarks is again JSON, and it is printed to stdout, while our status messages are printed to stderr. So, the output can be stored with

```
./solver < input.json > output.json
```

Note that in most cases, the JSON output by our benchmarks is compatible with other benchmarks, therefore it is possible to first call the spmv benchmark, use the resulting output JSON as input to the solver benchmark, and finally use the resulting solver JSON output as input to the preconditioner benchmark.

# 4.0.4 4: Benchmarking overview

The benchmark suite is invoked using the make <code>benchmark</code> command in the build directory. Under the hood, this command simply calls the script <code>benchmark/run\_all\_benchmarks.sh</code> so it is possible to manually launch this script as well. The behavior of the suite can be modified using environment variables. Assuming the <code>bash</code> shell is used, these can either be specified via the <code>export</code> command to persist between multiple runs: <code>export VARIABLE="value"</code>

make benchmark

VARIABLE="value" ... make benchmark

Since make sets any variables passed to it as temporary environment variables, the following shorthand can also be used:

make benchmark VARIABLE="value" ...

A combination of the above approaches is also possible (e.g. it may be useful to <code>export</code> the <code>SYSTEM\_NAME</code> variable, and specify the others at every benchmark run).

The benchmark suite can take a number of configuration parameters. Benchmarks can be run only for sparse matrix vector products (spmv), for full solvers (with or without preconditioners), or for preconditioners only when supported. The benchmark suite also allows to target a sub-part of the SuiteSparse matrix collection. For details, see the available benchmark options. Here are the most important options:

- BENCHMARK={spmv, solver, preconditioner} allows to select the type of benchmark to be ran.
- EXECUTOR={reference, cuda, hip, omp, dpcpp} select the executor and platform the benchmarks should be ran on.
- SYSTEM\_NAME=<name> a name which will be used to designate this platform (e.g. V100, RadeonVII, ...).
- SEGMENTS=<N> Split the benchmarked matrix space into <N> segments. If specified, SEGMENT\_ID also has to be set.
- SEGMENT\_ID=<I> used in combination with the SEGMENTS variable. <I> should be an integer between 1 and <N>, the number of SEGMENTS. If specified, only the <I>-th segment of the benchmark suite will be run.
- BENCHMARK\_PRECISION defines the precision the benchmarks are run in. Supported values are ←: "double" (default), "single", "dcomplex" and "scomplex"
- MATRIX\_LIST\_FILE=/path/to/matrix\_list.file allows to list SuiteSparse matrix id or name to benchmark. As an example, a matrix list file containing the following will ensure that benchmarks are ran for only those three matrices:

"1903 Freescale/circuit5M thermal2"

# 4.0.5 5: Publishing the results on Github and analyze the results with the GPE (optional)

The previous experiments generated json files for each matrices, each containing timing, iteration count, achieved precision, ... depending on the type of benchmark run. These files are available in the directory \${ginkgo} \_build\_dir}/benchmark/results/. These files can be analyzed and processed through any tool (e.g. python). In this section, we describe how to generate the plots by using Ginkgo's GPE tool. First, we need to publish the experiments into a Github repository which will be then linked as source input to the GPE. For this, we can simply fork the ginkgo-data repository. To do so, we can go to the github repository and use the forking interface: https://github.com/ginkgo-project/ginkgo-data/

Once it's done, we want to clone the repository locally, put all results online and access the GPE for plotting the results. Here are the detailed steps:

```
git clone https://github.com/<username>/ginkgo-data.git $HOME/ginkgo_benchmark/ginkgo-data # send the benchmarked data to the ginkgo-data repository # If needed, remove the old data so that no previous data is left. # rm -r ${HOME}/ginkgo_benchmark/ginkgo-data/data/${SYSTEM_NAME} rsync -rtv ${ginkgo_build_dir}/benchmark/results/ $HOME/ginkgo_benchmark/ginkgo-data/data/ data/ginkgo_benchmark/ginkgo-data/data/ # The following updates the main `.json` files with the list of data. # Ensure a python 3 installation is available. ./build-list . > list.json ./agregate < list.json > agregate.json ./represent . > represent.json git config --local user.name "<Name>" git config --local user.name "<Name>" git commit -am "Ginkgo benchmark ${BENCHMARK} of ${SYSTEM_NAME}..." git push
```

Note that depending on what data is of interest, you may need to update the scripts build-list or agregate to change which files you want to agglomerate and summarize (depending on the system name), or which data you want to select (solver results, spmv results, ...).

For the generating the plots in the GPE, here are the steps to go through:

- 1. Access the GPE: https://ginkgo-project.github.io/gpe/
- 2. Update data root URL, from https://raw.githubusercontent.com/ginkgo-project/ginkgo-data/mas to https://raw.githubusercontent.com/<username>/ginkgo-data/<br/>branch>/data
- 3. Click on the arrow to load the data, select the Result Summary entry above.
- 4. Click on select an example to choose a plotting script. Multiple scripts are available by default in different branches. You can use the jsonata and chart js languages to develop your own as well.
- 5. The results should be available in the tab "plot" on the right side. Other tabs allow to access the result of the processed data after invoking the processing script.

# 4.0.6 6: Detailed performance analysis and debugging

Detailed performance analysis can be ran by passing the environment variable DETAILED=1 to the benchmarking script. This detailed run is available for solvers and allows to log the internal residual after every iteration as well as log the time taken by all operations. These features are also available in the performance-debugging example which can be used instead and modified as needed to analyze Ginkgo's performance.

These features are implemented thanks to the loggers located in the file \${ginkgo\_src\_dir}/benchmark/utils/loggers Ginkgo possesses hooks at all important code location points which can be inspected thanks to the logger. In this fashion, it is easy to use these loggers also for tracking memory allocation sizes and other important library aspects.

# 4.0.7 7: Available benchmark options

There are a set amount of options available for benchmarking. Most important options can be configured through the benchmarking script itself thanks to environment variables. Otherwise, some specific options are not available through the benchmarking scripts but can be directly configured when running the benchmarking program itself. For a list of all options, run for example \${ginkgo\_build\_dir}/benchmark/solver/solver --help.

The supported environment variables are described in the following list:

• BENCHMARK={spmv, solver, preconditioner} - allows to select the type of benchmark to be ran. Default is spmv.

- spmv Runs the sparse matrix-vector product benchmarks on the SuiteSparse collection.
- solver Runs the solver benchmarks on the SuiteSparse collection. The matrix format is determined by running the spmv benchmarks first, and using the fastest format determined by that benchmark.
- preconditioner Runs the preconditioner benchmarks on artificially generated block-diagonal matrices.
- EXECUTOR={reference, cuda, hip, omp, dpcpp} select the executor and platform the benchmarks should be ran on. Default is cuda.
- SYSTEM\_NAME=<name> a name which will be used to designate this platform (e.g. V100, RadeonVII, ...) and not overwrite previous results. Default is unknown.
- SEGMENTS=<N> Split the benchmarked matrix space into <N> segments. If specified, SEGMENT\_ID also has to be set. Default is 1.
- SEGMENT\_ID=<I>- used in combination with the SEGMENTS variable. <I> should be an integer between 1 and <N>, the number of SEGMENTS. If specified, only the <I>-th segment of the benchmark suite will be run. Default is 1.
- MATRIX\_LIST\_FILE=/path/to/matrix\_list.file allows to list SuiteSparse matrix id or name to benchmark. As an example, a matrix list file containing the following will ensure that benchmarks are ran for only those three matrices: ``` 1903 Freescale/circuit5M thermal2 ``\*DEVICE\_ID- the accelerator device ID to target for the benchmark. The default is0. \*DRY\_RUN={true, false}- If set totrue`, prepares the system for the benchmark runs (downloads the collections, creates the result structure, etc.) and outputs the list of commands that would normally be run, but does not run the benchmarks themselves. Default is false.
- PRECONDS={ jacobi, ic, ilu, paric, parict, parilu, parilut, ic-isai, ilu-isai, paric-isai, parithe preconditioners to use for either solver or preconditioner benchmarks. Multiple options can be passed to this variable. Default is none.
- FORMATS={csr, coo, ell, hybrid, sellp, hybridxx, cusparse\_xx, hipsparse\_xx} the matrix formats to benchmark for the spmv phase of the benchmark. Run \${ginkgo\_build\_← dir}/benchmark/spmv/spmv --help for a full list. If needed, multiple options for hybrid with different optimization parameters are available. Depending on the libraries available at build time, vendor library formats (cuSPARSE with cusparse\_prefix or hipSPARSE with hipsparse\_prefix) can be used as well. Multiple options can be passed. The default is csr, coo, ell, hybrid, sellp.
- SOLVERS={bicgstab,bicg,cg,cgs,fcg,gmres,cb\_gmres\_{keep,reduce1,reduce2,integer,ireduce2,integer,ireduce3,integer,
  - the solvers which should be benchmarked. Multiple options can be passed. The default is bicgstab,cg,cgs,fcg,gmres,idr. Note that lower/upper\_trs by default don't use a preconditioner, as they are by default exact direct solvers.
- SOLVERS\_PRECISION=<precision> the minimal residual reduction before which the solver should stop. The default is 1e-6.
- SOLVERS\_MAX\_ITERATIONS=<number> the maximum number of iterations with which a solver should be ran. The default is 10000.
- SOLVERS\_RHS={1, random, sinus} whether to use a vector of all ones, random values or b = A \* (s / |s|)\$ with s(idx) = sin(idx) (for complex numbers, s(idx) = sin(2\*idx) + i \* sin(2\*idx+1)) as the right-hand side in solver benchmarks. Default is 1.
- SOLVERS\_INITIAL\_GUESS={rhs,0,random} the initial guess generation of the solvers. rhs uses the right-hand side, 0 uses a zero vector and random generates a random vector as the initial guess.
- DETAILED={0,1} selects whether detailed benchmarks should be ran. This generally provides extra, verbose information at the cost of one or more extra benchmark runs. It can be either 0 (off) or 1 (on).
- GPU\_TIMER={true, false} If set to true, use the gpu timer, which is valid for cuda/hip executor, to measure the timing. Default is false.

- SOLVERS\_JACOBI\_MAX\_BS sets the maximum block size for the Jacobi preconditioner (if used, otherwise, it does nothing) in the solvers benchmark. The default is '32'.
- SOLVERS\_GMRES\_RESTART the maximum dimension of the Krylov space to use in GMRES. The default is 100.

# **Chapter 5**

# **Contributing guidelines**

We are glad that you are interested in contributing to Ginkgo. Please have a look at our coding guidelines before proposing a pull request.

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# 5.2 Most important stuff (A TL;DR)

- GINKGO\_DEVEL\_TOOLS needs to be set to on to commit. This requires clang-format to be installed. See Automatic code formatting for more details. Once installed, you can run make format in your build/ folder to automatically format your modified files. As make format unstages your files post-formatting, you must stage the files again once you have verified that make format has done the appropriate formatting, before committing the files.
- See Our git workflow to get a quick overview of our workflow.
- See Creating, Reviewing and Merging Pull Requests on how to create a Pull request.

# 5.3 Project structure

Ginkgo is divided into a core module with common functionalities independent of the architecture, and several kernel modules (reference, omp, cuda, hip, dpcpp) which contain low-level computational routines for each supported architecture.

#### 5.3.1 Extended header files

Some header files from the core module have to be extended to include special functionality for specific architectures. An example of this is core/base/math.hpp, which has a GPU counterpart in cuda/base/math.co
hpp. For such files you should always include the version from the module you are working on, and this file will internally include its core counterpart.

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# 5.3.2 Using library classes

You can use and call functions of existing classes inside a kernel (that are defined and not just declared in a header file), however, you are not allowed to create new instances of a polymorphic class inside a kernel (or in general inside any kernel module like cuda/hip/omp/reference) as this creates circular dependencies between the core and the backend library. With this in mind, our CI contains a job which checks if such a circular dependency exists. These checks can be run manually using the <code>-DGINKGO\_CHECK\_CIRCULAR\_DEPS=ON</code> option in the CMake configuration.

For example, when creating a new matrix class AB by combining existing classes A and B, the AB::apply() function composed of invocations to A::apply() and B::apply() can only be defined in the core module, it is not possible to create instances of A and B inside the AB kernel files. This is to avoid the aforementioned circular dependency issue. An example for such a class is the Hybrid matrix format, which uses the apply() of the Ell and Coo matrix formats. Nevertheless, it is possible to call the kernels themselves directly within the same executor. For example, cuda::dense::add\_scaled() can be called from any other cuda kernel.

# 5.4 Git related

Ginkgo uses git, the distributed version control system to track code changes and coordinate work among its developers. A general guide to git can be found in its extensive documentation.

# 5.4.1 Our git workflow

In Ginkgo, we prioritize keeping a clean history over accurate tracking of commits. <code>git rebase</code> is hence our command of choice to make sure that we have a nice and linear history, especially for pulling the latest changes from the <code>develop</code> branch. More importantly, rebasing upon develop is **required** before the commits of the PR are merged into the <code>develop</code> branch.

### 5.4.2 Writing good commit messages

With software sustainability and maintainability in mind, it is important to write commit messages that are short, clear and informative. Ideally, this would be the format to prefer:

```
Summary of the changes in a sentence, max 50 chars.

More detailed comments:
+ Changes that have been added.
- Changes that been removed.

Related PR: https://github.com/ginkgo-project/ginkgo/pull/<PR-number>
```

You can refer to this informative guide for more details.

# 5.4.2.1 Attributing credit

Git has a nice feature where it allows you to add a co-author for your commit, if you would like to attribute credits for the changes made in the commit. This can be done by:

```
Commit message.
Co-authored-by: Name <email@domain>
```

In the Ginkgo commit history, this is most common associated with suggested improvements from code reviews.

# 5.4.3 Creating, Reviewing and Merging Pull Requests

- The develop branch is the default branch to submit PR's to. From time to time, we merge the develop branch to the master branch and create tags on the master to create new releases of Ginkgo. Therefore, all pull requests must be merged into develop.
- Please have a look at the labels and make sure to add the relevant labels.
- You can mark the PR as a WIP if you are still working on it, Ready for Review when it is ready for others to review it.
- Assignees to the PR should be the ones responsible for merging that PR. Currently, it is only possible to assign members within the ginkgo-project.
- · Each pull request requires at least two approvals before merging.
- PR's created from within the repository will automatically trigger two CI pipelines on pushing to the branch from the which the PR has been created. The Github Actions pipeline tests our framework on Mac OSX and on Windows platforms. Another comprehensive Linux based pipeline is run from a mirror on gitlab and contains additional checks like static analysis and test coverage.
- Once a PR has been approved and the build has passed, one of the reviewers can mark the PR as READY TO MERGE. At this point the creator/assignee of the PR needs to verify that the branch is up to date with develop and rebase it on develop if it is not.

# 5.5 Code style

### 5.5.1 Automatic code formatting

Ginkgo uses <code>pre-commit</code> to automatically apply code formatting when committing changes to git. What formatting is applied is managed through <code>ClangFormat</code> with a custom <code>.clang-format</code> configuration file (mostly based on ClangFormat's <code>Google</code> style). Make sure you have pre-commit set up and running properly before committing anything that will end up in a pull request against <code>ginkgo-project/ginkgo</code> repository. In addition, you should <code>never</code> modify the <code>.clang-format</code> configuration file shipped with Ginkgo. E.g. if ClangFormat has trouble reading this file on your system, you should install a newer version of ClangFormat, and avoid commenting out parts of the configuration file.

ClangFormat is the primary tool that helps us achieve a uniform look of Ginkgo's codebase, while reducing the learning curve of potential contributors. However, ClangFormat configuration is not expressive enough to incorporate the entire coding style, so there are several additional rules that all contributed code should follow.

*Note*: To learn more about how ClangFormat will format your code, see existing files in Ginkgo, .clang-format configuration file shipped with Ginkgo, and ClangFormat's documentation.

### 5.5.2 Naming scheme

#### 5.5.2.1 Filenames

Filenames use snake\_case and use the following extensions:

- C++ source files: .cpp
- C++ header files: .hpp

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- CUDA source files: .cu
- CUDA header files: .cuh
- HIP source files: .hip.cpp
- HIP header files: .hip.hpp
- Common source files used by both CUDA and HIP: .hpp.inc
- CMake utility files: .cmake
- Shell scripts: .sh

Note: A C++ source/header file is considered a CUDA file if it contains CUDA code that is not guarded with #if guards that disable this code in non-CUDA compilers. I.e. if a file can be compiled by a general C++ compiler, it is not considered a CUDA file.

#### 5.5.2.2 Macros

Macros (both object-like and function-like macros) use CAPITAL\_CASE. They have to start with GKO\_ to avoid name clashes (even if they are #undef-ed in the same file!).

#### 5.5.2.3 Variables

Variables use snake\_case.

#### 5.5.2.4 Constants

Constants use snake\_case.

#### 5.5.2.5 Functions

Functions use snake\_case.

#### 5.5.2.6 Structures and classes

Structures and classes which do not experience polymorphic behavior (i.e. do not contain virtual methods, nor members which experience polymorphic behavior) use snake case.

All other structures and classes use CamelCase.

# 5.5.2.7 **Members**

All structure / class members use the same naming scheme as they would if they were not members:

- · methods use the naming scheme for functions
- · data members the naming scheme for variables or constants
- type members for classes / structures

Additionally, non-public data members end with an underscore (\_).

#### 5.5.2.8 Namespaces

Namespaces use snake\_case.

# 5.5.2.9 Template parameters

- Type template parameters use CamelCase, for example ValueType.
- Non-type template parameters use snake\_case, for example subwarp\_size.

### 5.5.3 Whitespace

Spaces and tabs are handled by ClangFormat, but blank lines are only partially handled (the current configuration doesn't allow for more than 2 blank lines). Thus, contributors should be aware of the following rules for blank lines:

- Top-level statements and statements directly within namespaces are separated with 2 blank lines. The first
  / last statement of a namespace is separated by two blank lines from the opening / closing brace of the
  namespace.
  - (a) exception: if the first **or** the last statement in the namespace is another namespace, then no blank lines are required example: ```c++ namespace foo {

```
struct x {
    };
    } // namespace foo
    namespace bar {
    namespace baz {
    void f();
       // namespace baz
    } // namespace bar
2. _exception_: in header files whose only purpose is to _declare_ a bunch
    of functions (e.g. the '*_kernel.hpp' files) these declarations can be
    separated by only 1 blank line (note: standard rules apply for all other
    statements that might be present in that file)
3. _exception_: "related" statement can have 1 blank line between them.

"Related" is not a strictly defined adjective in this sense, but is in
    general one of:
    1. overload of a same function,
        function / class template and it's specializations,
    3. macro that modifies the meaning or adds functionality to the % \left( 1\right) =\left( 1\right) \left( 1\right) 
         previous / following statement.
    However, simply calling function 'f' from function 'g' does not imply
    that 'f' and 'g' are "related".
```

1. Statements within structures / classes are separated with 1 blank line. There are no blank lines between the first / last statement in the structure / class.

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```
(a) exception: there is no blank line between an access modifier (private, protected, public) and
the following statement. example: ```c++ class foo { public: int get_x() const noexcept { return x_; }
int &get_x() noexcept { return x_; }
private: int x_; }; ```
```

- 2. Function bodies cannot have multiple consecutive blank lines, and a single blank line can only appear between two logical sections of the function.
- 3. Unit tests should follow the AAA pattern, and a single blank line must appear between consecutive "A" sections. No other blank lines are allowed in unit tests.
- 4. Enumeration definitions should have no blank lines between consecutive enumerators.

# 5.5.4 Include statement grouping

The concrete ordering will be done by clang-format. Here are the rules that clang-format will follow. In general, all include statements should be present on the top of the file, ordered in the following groups, with *one* blank lines between each group:

- Main header file (e.g. core/foo/bar.hpp included in core/foo/bar.cpp, or in the unit testcore/test/foo/bar.cpp)
- 2. Standard library headers (e.g. vector)
- 3. Executor specific library headers (e.g. omp.h)
- 4. System third-party library headers (e.g. papi.h)
- 5. Public Ginkgo headers
- 6. Local headers

Example: A file core/base/my\_file.cpp might have an include list like this:

```
{c++}
#include "ginkgo/core/base/my_file.hpp"
#include <algorithm>
#include <vector>
#include <omp.h>
#include <omp.h>
#include <third_party/blas/cblas.hpp>
#include <third_party/lapack/lapack.hpp>
#include <ginkgo/core/base/executor.hpp>
#include <ginkgo/core/base/lin_op.hpp>
#include <ginkgo/core/base/lin_op.hpp>
#include <ginkgo/core/base/lin_op.hpp>
#include <ginkgo/core/base/lin_op.hpp>
#include "core/base/my_file_kernels.hpp"
```

#### 5.5.4.1 Main header

This section presents the handling of the main header attributed to a file. For a given file, the main header is the header that contains the declarations of the functions, classes, etc., which are implemented in this file. In the previous example, this would be #include "ginkgo/core/base/my\_file.hpp". The clang-format tool figures out the main header. The only intervention form a contributor is to *always* include the main header using "...".

Please note that this only applies to implementation files, so files ending in .cpp or .cu.

#### 5.5.4.2 Some general comments.

- 1. Private headers of Ginkgo should not be included within the public Ginkgo header.
- 2. It is a good idea to keep the headers self-sufficient, See Google Style guide for reasoning. When compiling with GINKGO\_CHECK\_CIRCULAR\_DEPS enabled, this property is explicitly checked.
- 3. The recommendations of the <code>iwyu</code> (Include what you use) tool can be used to make sure that the headers are self-sufficient and that the compiled files (<code>.cu</code>, <code>.cpp</code>, <code>.hip.cpp</code>) include only what they use. A <code>CI pipeline</code> is available that runs with the <code>iwyu</code> tool. Please be aware that this tool can be incorrect in some cases.

# 5.5.5 Other Code Formatting not handled by ClangFormat

#### 5.5.5.1 Control flow constructs

Single line statements should be avoided in all cases. Use of brackets is mandatory for all control flow constructs (e.g. if, for, while, ...).

#### 5.5.5.2 Variable declarations

C++ supports declaring / defining multiple variables using a single *type-specifier*. However, this is often very confusing as references and pointers exhibit strange behavior:

```
{c++} template <typename T> using pointer = T \star; int \star x, y; // x is a pointer, y is not pointer<int> x, y; // both x and y are pointers
```

For this reason, always declare each variable on a separate line, with its own type-specifier.

### 5.5.6 CMake coding style

#### 5.5.6.1 Whitespaces

All alignment in CMake files should use four spaces.

#### 5.5.6.2 Use of macros vs functions

Macros in CMake do not have a scope. This means that any variable set in this macro will be available to the whole project. In contrast, functions in CMake have local scope and therefore all set variables are local only. In general, wrap all piece of algorithms using temporary variables in a function and use macros to propagate variables to the whole project.

### 5.5.6.3 Naming style

All Ginkgo specific variables should be prefixed with a GINKGO\_ and all functions by ginkgo\_.

5.6 Helper scripts 27

# 5.6 Helper scripts

To facilitate easy development within Ginkgo and to encourage coders and scientists who do not want get bogged down by the details of the Ginkgo library, but rather focus on writing the algorithms and the kernels, Ginkgo provides the developers with a few helper scripts.

#### 5.6.1 Create a new algorithm

A create\_new\_algorithm.sh script is available for developers to facilitate easy addition of new algorithms. The options it provides can be queried with ./create\_new\_algorithm.sh --help

The main objective of this script is to add files and boiler plate code for the new algorithm using a model and an instance of that model. For example, models can be any one of factorization, matrix, preconditioner or solver. For example to create a new solver named my\_solver similar to gmres, you would set the ModelType to solver and set the ModelName to gmres. This would duplicate the core algorithm and kernels of the gmres algorithm and replace the naming to my\_solver. Additionally, all the kernels of the new my\_colver are marked as GKO\_NOT\_IMPLEMENTED. For easy navigation and .txt file is created in the folder where the script is run, which lists all the TODO's. These TODO's can also be found in the corresponding files.

# 5.6.2 Converting CUDA code to HIP code

We provide a cuda2hip script that converts cuda kernel code into hip kernel code. Internally, this script calls the hipify script provided by HIP, converting the CUDA syntax to HIP syntax. Additionally, it also automatically replaces the instances of CUDA with HIP as appropriate. Hence, this script can be called on a Ginkgo CUDA file. You can find this script in the dev\_tools/scripts/ folder.

# 5.7 Writing Tests

Ginkgo uses the GTest framework for the unit test framework within Ginkgo. Writing good tests are extremely important to verify the functionality of the new code and to make sure that none of the existing code has been broken.

### 5.7.1 Testing know-how

- GTest provides a comprehensive documentation of the functionality available within Gtest.
- Reduce code duplication with Testing Fixtures, TEST\_F
- Write templated tests using TYPED\_TEST.

# 5.7.2 Some general rules.

- Unit tests must follow the KISS principle.
- Unit tests must follow the AAA pattern, and a single blank line must appear between consecutive "A" sections.

# 5.7.3 Writing tests for kernels

- Reference kernels, kernels on the ReferenceExecutor, are meant to be single threaded reference implementations. Therefore, tests for reference kernels need to be performed with data that can be as small as possible. For example, matrices lesser than 5x5 are acceptable. This allows the reviewers to verify the results for exactness with tools such as MATLAB.
- OpenMP, CUDA, HIP and DPC++ kernels have to be tested against the reference kernels. Hence data for the tests of these kernels can be generated in the test files using helper functions or by using external files to be read through the standard input. In particular for CUDA, HIP and DPC++ the data size should be at least bigger than the architecture's warp size to ensure there is no corner case in the kernels.

# 5.8 Documentation style

Documentation uses standard Doxygen.

# 5.8.1 Developer targeted notes

Make use of @internal doxygen tag. This can be used for any comment which is not intended for users, but is useful to better understand a piece of code.

# 5.8.2 Whitespaces

#### 5.8.2.1 After named tags such as <tt>@param foo</tt>

The documentation tags which use an additional name should be followed by two spaces in order to better distinguish the text from the doxygen tag. It is also possible to use a line break instead.

#### 5.8.3 Documenting examples

There are two main steps:

- 1. First, you can just copy over the doc/ folder (you can copy it from the example most relevant to you) and adapt your example names and such, then you can modify the actual documentation.
- In tooltip: A short description of the example.
- In short-intro: The name of the example.
- In results.dox: Run the example and write the output you get.
- In kind: The kind of the example. For different kinds see the documentation. Examples can be of basic, techniques, logging, stopping\_criteria or preconditioners. If your example does not fit any of these categories, feel free to create one.
- In intro.dox: You write an explanation of your code with some introduction similar to what you see in an existing example most relevant to you.
- In builds-on: You write the examples it builds on.
- 1. You also need to modify the examples.hpp.in file. You add the name of the example in the main section and in the section that you specified in the doc/kind file in the example documentation.

# 5.9 Other programming comments

# 5.9.1 C++ standard stream objects

These are global objects and are shared inside the same translation unit. Therefore, whenever its state or formatting is changed (e.g. using std::hex or floating point formatting) inside library code, make sure to restore the state before returning the control to the user. See this stackoverflow question for examples on how to do it correctly. This is extremely important for header files.

# 5.9.2 Warnings

By default, the -DCMAKE\_CXX\_FLAGS should be set to -Wpedantic to emit pedantic warnings by default. The CI system additionally also has a step where it compiles for pedantic warnings to be errors.

# 5.9.3 Avoiding circular dependencies

To facilitate finding circular dependencies issues (see Using library classes for more details), a CI step no-circular-deps was created. For more details on its usage, see this pipeline, where Ginkgo did not abide to this policy and PR #278 which fixed this. Note that doing so is not enough to guarantee with 100% accuracy that no circular dependency is present. For an example of such a case, take a look at this pipeline where one of the compiler setups detected an incorrect dependency of the cuda module (due to jacobi) on the core module.

# **Chapter 6**

# **Citing Ginkgo**

The main Ginkgo paper describing Ginkgo's purpose, design and interface is available through the following reference:

```
@article{ginkgo-toms-2022,
title = {{Ginkgo: A Modern Linear Operator Algebra Framework for High Performance Computing}},
volume = {48},
copyright = {All rights reserved},
issn = {0098-3500},
shorttitle = {Ginkgo},
url = {https://doi.org/10.1145/3480935},
doi = {10.1145/3480935},
number = {1},
urldate = {2022-02-17},
journal = {ACM Transactions on Mathematical Software},
author = {Anzt, Hartwig and Cojean, Terry and Flegar, Goran and Göbel, Fritz and Grützmacher, Thomas and
Nayak, Pratik and Ribizel, Tobias and Tsai, Yuhsiang Mike and Quintana-Ortí, Enrique S.},
month = feb,
year = {2022},
keywords = {ginkgo, healthy software lifecycle, High performance computing, multi-core and manycore
architectures},
pages = {2:1--2:33}
}
```

Multiple topical papers exist on Ginkgo and its algorithms. The following papers can be used to cite specific aspects of the Ginkgo project.

# 6.0.1 The Ginkgo Software

The Ginkgo software itself was reviewed and has a paper published in the Journal of Open Source Software, which can be cited with the following reference:

```
@article{GinkgoJoss2020,
    doi = {10.21105/joss.02260},
    url = {https://doi.org/10.21105/joss.02260},
    year = {2020},
    publisher = {The Open Journal},
    volume = {5},
    number = {52},
    pages = {2260},
    author = {Hartwig Anzt and Terry Cojean and Yen-Chen Chen and Goran Flegar and Fritz G\"{0}bel and Thomas
        Gr\"{u}tzmacher and Pratik Nayak and Tobias Ribizel and Yu-Hsiang Tsai},
    title = {Ginkgo: A high performance numerical linear algebra library},
    journal = {Journal of Open Source Software}
}
```

# 6.0.2 On Portability

```
@misc{tsai2020amdportability,
    title={Preparing Ginkgo for AMD GPUs -- A Testimonial on Porting CUDA Code to HIP},
    author={Yuhsiang M. Tsai and Terry Cojean and Tobias Ribizel and Hartwig Anzt},
    year={2020},
    eprint={2006.14290},
    archivePrefix={arXiv},
    primaryClass={cs.MS}
}
```

32 Citing Ginkgo

# 6.0.3 On Software Sustainability

```
@inproceedings{anzt2019pasccb,
author = {Anzt, Hartwig and Chen, Yen-Chen and Cojean, Terry and Dongarra, Jack and Flegar, Goran and Nayak,
      Pratik and Quintana-Ort\'{\i}, Enrique S. and Tsai, Yuhsiang M. and Wang, Weichung},
title = {Towards Continuous Benchmarking: An Automated Performance Evaluation Framework for High
      Performance Software},
year = \{2019\},
isbn = \{9781450367707\},
publisher = {Association for Computing Machinery},
address = {New York, NY, USA},
url = {https://doi.org/10.1145/3324989.3325719},
doi = \{10.1145/3324989.3325719\},
booktitle = {Proceedings of the Platform for Advanced Scientific Computing Conference},
articleno = {9},
numpages = \{11\}.
keywords = {interactive performance visualization, healthy software lifecycle, continuous integration,
     automated performance benchmarking},
location = {Zurich, Switzerland},
series = {PASC '19}
```

# 6.0.4 On SpMV or solvers performance

```
@InProceedings{tsai2020amdspmv,
author="Tsai, Yuhsiang M.
and Cojean, Terry
and Anzt, Hartwig",
editor="Sadayappan, Ponnuswamy
and Chamberlain, Bradford L.
and Juckeland, Guido
and Ltaief, Hatem",
title="Sparse Linear Algebra on AMD and  NVIDIA GPUs -- The Race Is On",
booktitle="High Performance Computing",
year="2020",
publisher="Springer International Publishing",
address="Cham",
pages="309--327"
abstract="Efficiently processing sparse matrices is a central and performance-critical part of many
      scientific simulation codes. Recognizing the adoption of manycore accelerators in HPC, we evaluate in this paper the performance of the currently best sparse matrix-vector product (SpMV) implementations
      on high-end GPUs from AMD and NVIDIA. Specifically, we optimize SpMV kernels for the CSR, COO, ELL,
      and HYB format taking the hardware characteristics of the latest GPU technologies into account. We
      compare for 2,800 test matrices the performance of our kernels against AMD's hipSPARSE library and
      NVIDIA's cuSPARSE library, and ultimately assess how the GPU technologies from AMD and NVIDIA compare
in terms of SpMV performance.", isbn="978-3-030-50743-5"
@article{anzt2020spmv,
author = {Anzt, Hartwig and Cojean, Terry and Yen-Chen, Chen and Dongarra, Jack and Flegar, Goran and Nayak,
      Pratik and Tomov, Stanimire and Tsai, Yuhsiang M. and Wang, Weichung},
title = {Load-Balancing Sparse Matrix Vector Product Kernels on GPUs},
year = {2020},
issue_date = {March 2020},
publisher = {Association for Computing Machinery},
address = {New York, NY, USA},
volume = \{7\},
number = \{1\},
issn = \{2329-4949\},
url = {https://doi.org/10.1145/3380930},
doi = {10.1145/3380930},
journal = {ACM Trans. Parallel Comput.},
month = mar,
articleno = {2},
numpages = \{26\},
keywords = {irregular matrices, GPUs, Sparse Matrix Vector Product (SpMV)}
    title={Evaluating the Performance of NVIDIA's A100 Ampere GPU for Sparse Linear Algebra Computations},
    author={Yuhsiang Mike Tsai and Terry Cojean and Hartwig Anzt},
    vear={2020},
    eprint={2008.08478}.
    archivePrefix={arXiv},
    primaryClass={cs.MS}
```

# **Chapter 7**

# **Example programs**

Here you can find example programs that demonstrate the usage of Ginkgo. Some examples are built on one another and some are stand-alone and demonstrate a concept of Ginkgo, which can be used in your own code.

You can browse the available example programs

- 1. as a graph that shows how example programs build upon each other.
- 2. as a list that provides a short synopsis of each program.
- 3. or grouped by topic.

By default, all Ginkgo examples are built using CMake.

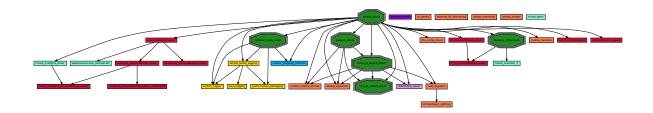
An example for building the examples and using Ginkgo as an external library without CMake can be found in the script provided for each example, which should be called with the form: ./build.sh PATH\_TO\_GINKGO\_B UILD\_DIR

By default, Ginkgo is compiled with at least <code>-DGINKGO\_BUILD\_REFERENCE=ON</code>. Ginkgo also tries to detect your environment setup (presence of CUDA, ...) to enable the relevant accelerator modules. If you want to target a specific GPU, make sure that Ginkgo is compiled with the accelerator specific module enabled, such as:

- 1. -DGINKGO\_BUILD\_CUDA=ON option for NVIDIA GPUs.
- 2. -DGINKGO\_BUILD\_HIP=ON option for AMD or NVIDIA GPUs.
- 3. -DGINKGO\_BUILD\_SYCL=ON option for Intel GPUs (and possibly any other platform).

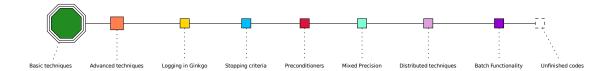
### Connections between example programs

The following graph shows the connections between example programs and how they build on each other. Click on any of the boxes to go to one of the programs. If you hover your mouse pointer over a box, a brief description of the program should appear.



34 Example programs

# Legend:



# **Example programs**

The simple-solver program	A minimal CG solver in Ginkgo, which reads a matrix from a file.
The minimal-cuda-solver program	A minimal solver on the CUDA executor than can be run on N← VIDIA GPU's.
The poisson-solver program	Solve an actual physically relevant problem, the poisson problem. The matrix is generated within Ginkgo.
The preconditioned-solver program	Using a Jacobi preconditioner to solve a linear system.
The ilu-preconditioned-solver program	Using an ILU preconditioner to solve a linear system.
The performance-debugging program	Using Loggers to debug the performance within Ginkgo.
The three-pt-stencil-solver program	Using a three point stencil to solve the poisson equation with array views.
The nine-pt-stencil-solver program	Using a nine point 2D stencil to solve the poisson equation with array views.
The external-lib-interfacing program	Using Ginkgo's solver with the external library deal.II.
The custom-logger program	Creating a custom logger specifically for comparing the recurrent and the real residual norms.
The custom-matrix-format program	Creating a matrix-free stencil solver by using Ginkgo's advanced methods to build your own custom matrix format.
The inverse-iteration program	Using Ginkgo to compute eigenvalues of a matrix with the inverse iteration method.
The simple-solver-logging program	Using the logging functionality in Ginkgo to get solver and other information to diagnose and debug your code.
The papi-logging program	Using the PAPI logging library in Ginkgo to get advanced information about your code and its behaviour.
The ginkgo-overhead program	Measuring the overhead of the Ginkgo library.
The custom-stopping-criterion program	Creating a custom stopping criterion for the iterative solution process.
The ginkgo-ranges program	Using the ranges concept to factorize a matrix with the LU factorization.

The mixed-spmv program	Shows the Ginkgo mixed precision spmv functionality.
The mixed-precision-ir program	Manual implementation of a Mixed Precision Iterative Refinement (MPIR) solver.
The adaptiveprecision-blockjacobi program	Shows how to use the adaptive precision block-Jacobi preconditioner.
The cb-gmres program	Using the Ginkgo CB-GMRES solver (Compressed Basis GM→ RES).
The heat-equation program	Solving a 2D heat equation and showing matrix assembly, vector initialization and solver setup in a more complex setting with output visualization.
The iterative-refinement program	Using a low accuracy CG solver as an inner solver to an iterative refinement (IR) method which solves a linear system.
The ir-ilu-preconditioned-solver program	Combining iterative refinement with the adaptive precision block- Jacobi preconditioner to approximate triangular systems occur- ring in ILU preconditioning.
The par-ilu-convergence program	Convergence analysis at the examples of parallel incomplete factorization solver.
The preconditioner-export program	Explicit generation and storage of preconditioners for given matrices.
The multigrid-preconditioned-solver program	Use multigrid as preconditioner to a solver.
The mixed-multigrid-solver program	Use multigrid with different precision multigrid_level as a solver.
The distributed-solver program	Use a distributed solver to solve a 1D Laplace equation.

# **Example programs grouped by topics**

Solving a simple linear system with choice of executors	The simple-solver program
Debug the performance of a solver or preconditioner	The performance-debugging program
	The preconditioner-export program
Using the CUDA executor	The minimal-cuda-solver program
Using preconditioners	The preconditioned-solver program,
	The ilu-preconditioned-solver program,
	The ir-ilu-preconditioned-solver program,
	The adaptiveprecision-blockjacobi program,
	The par-ilu-convergence program,
	The preconditioner-export program
	The multigrid-preconditioned-solver program
Iterative refinement	The iterative-refinement program,
	The mixed-precision-ir program,
	The ir-ilu-preconditioned-solver program
Solving a physically relevant problem	The poisson-solver program,
	The three-pt-stencil-solver program,
	The nine-pt-stencil-solver program,
	The custom-matrix-format program

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Reading in a matrix and right hand side from a file	The simple-solver program,
	The minimal-cuda-solver program,
	The preconditioned-solver program,
	The ilu-preconditioned-solver program,
	The inverse-iteration program,
	The simple-solver-logging program,
	The papi-logging program,
	The custom-stopping-criterion program,
	The custom-logger program

# Basic techniques

Using Ginkgo with external libraries	The external-lib-interfacing program
Customizing Ginkgo	The custom-logger program,
	The custom-stopping-criterion program,
	The custom-matrix-format program
Writing your own matrix format	The custom-matrix-format program
Using Ginkgo to construct more complex linear algebra routines	The inverse-iteration program
Logging within Ginkgo	The simple-solver-logging program,
	The papi-logging program,
	The performance-debugging program
	The custom-logger program
Constructing your own stopping criterion	The custom-stopping-criterion program
Using ranges in Ginkgo	The ginkgo-ranges program
Mixed precision	The mixed-spmv program,
	The mixed-precision-ir program,
	The adaptiveprecision-blockjacobi program
	The mixed-multigrid-solver program
Multigrid	The multigrid-preconditioned-solver program
	The mixed-multigrid-solver program
Configure a solver from a config file	The file-config-solver program
Distributed	The distributed-solver program

# **Advanced techniques**

# **Chapter 8**

# The adaptive precision-block jacobi program

The preconditioned solver example..

This example depends on preconditioned-solver.

# This example shows how to use the adaptive precision block-Jacobi preconditioner.

In this example, we first read in a matrix from file, then generate a right-hand side and an initial guess. The preconditioned CG solver is enhanced with a block-Jacobi preconditioner that optimizes the storage format for the distinct inverted diagonal blocks to the numerical requirements. The example features the iteration count and runtime of the CG solver.

# The commented program

```
const auto executor_string = argc >= 2 ? argv[1] : "reference";
Figure out where to run the code
std::map<std::string, std::function<std::shared_ptr<gko::Executor>()>
   exec map{
        {"omp", [] { return gko::OmpExecutor::create(); }},
        {"cuda",
             return gko::CudaExecutor::create(0,
                                              gko::OmpExecutor::create());
        {"hip",
         [] {
            return gko::HipExecutor::create(0, gko::OmpExecutor::create());
        { "dpcpp",
            return gko::DpcppExecutor::create(0,
                                               gko::OmpExecutor::create());
        {"reference", [] { return gko::ReferenceExecutor::create(); }}};
executor where Ginkgo will perform the computation
const auto exec = exec_map.at(executor_string)(); // throws if not valid
Read data
auto A = share(gko::read<mtx>(std::ifstream("data/A.mtx"), exec));
Create RHS and initial guess as 1
gko::size_type size = A->get_size()[0];
```

```
auto host_x = vec::create(exec->get_master(), gko::dim<2>(size, 1));
for (auto i = 0; i < size; i++) {
    host_x->at(i, 0) = 1.;
auto x = gko::clone(exec, host_x);
auto b = gko::clone(exec, host_x);
Calculate initial residual by overwriting b
auto one = gko::initialize<vec>({1.0}, exec);
auto neg_one = gko::initialize<vec>({-1.0}, exec);
auto initres = gko::initialize<real_vec>({0.0}, exec);
A->apply(one, x, neg_one, b);
b->compute_norm2(initres);
copy b again
b->copy_from(host_x);
Create solver factory
const RealValueType reduction_factor = 1e-7;
auto solver_gen
    cg::build()
        . with\_criteria (gko::stop::Iteration::build().with\_max\_iters(10000u),\\
                        gko::stop::ResidualNorm<ValueType>::build()
                            .with_reduction_factor(reduction_factor))
Add preconditioner, these 2 lines are the only difference from the simple solver example
.with_preconditioner(
    bj::build().with_max_block_size(16u).with_storage_optimization(
        gko::precision_reduction::autodetect()))
.on(exec);
Create solver
std::shared_ptr<const gko::log::Convergence<ValueType» logger =
    gko::log::Convergence<ValueType>::create();
solver_gen->add_logger(logger);
auto solver = solver_gen->generate(A);
Solve system
exec->synchronize();
std::chrono::nanoseconds time(0);
auto tic = std::chrono::steady_clock::now();
solver->apply(b, x);
auto toc = std::chrono::steady_clock::now();
time += std::chrono::duration_cast<std::chrono::nanoseconds>(toc - tic);
Get residual
auto res = gko::as<real_vec>(logger->get_residual_norm());
auto impl_res = gko::as<real_vec>(logger->get_implicit_sq_resnorm());
std::cout « "Initial residual norm sqrt(r^T r):\n";
write(std::cout, initres);
std::cout « "Final residual norm sqrt(r^T r):\n";
write(std::cout, res);
std::cout « "Implicit residual norm squared (r^2):\n";
write(std::cout, impl_res);
Print solver statistics
    std::cout « "CG iteration count:
                                                 " « logger->get_num_iterations()
              « std::endl;
    std::cout « "CG execution time [ms]: "
              « static_cast<double>(time.count()) / 1000000.0 « std::endl;
}
```

# **Results**

## This is the expected output:

```
Initial residual norm sqrt(r^T r):
%%MatrixMarket matrix array real general
1 1
194.679
Final residual norm sqrt(r^T r):
%%MatrixMarket matrix array real general
1 1
5.69384e-06
Implicit residual norm squared (r^2):
%%MatrixMarket matrix array real general
1 1
1.27043e-15
CG iteration count: 5
CG execution time [ms]: 0.080041
```

#### Comments about programming and debugging

# The plain program

```
#include <fstream>
#include <iomanip>
#include <iostream>
#include <map>
#include <string>
#include <ginkgo/ginkgo.hpp>
int main(int argc, char* argv[])
       using ValueType = double;
       using RealValueType = gko::remove_complex<ValueType>;
       using IndexType = int;
       using vec = gko::matrix::Dense<ValueType>;
       using real_vec = gko::matrix::Dense<RealValueType>;
       using mtx = gko::matrix::Csr<ValueType, IndexType>;
       using cg = gko::solver::Cg<ValueType>;
using bj = gko::preconditioner::Jacobi<ValueType, IndexType>;
       std::cout « gko::version_info::get() « std::endl;
       if (argc == 2 && (std::string(argy[1]) == "--help")) {
   std::cerr « "Usage: " « argv[0] « " [executor]" « std::endl;
              std::exit(-1);
       const auto executor_string = argc >= 2 ? argv[1] : "reference";
       std::map<std::string, std::function<std::shared_ptr<gko::Executor>()»
                      "" ("omp", [] { return gko::OmpExecutor::create(); }},
{"cuda",
                       [] {
                              return gko::CudaExecutor::create(0,
                                                                                            gko::OmpExecutor::create());
                        [] {
                               return gko::HipExecutor::create(0, gko::OmpExecutor::create());
                       }}.
                      { "dpcpp",
                       [] {
                               return gko::DpcppExecutor::create(0,
                                                                                              gko::OmpExecutor::create());
                      {"reference", [] { return gko::ReferenceExecutor::create(); }}};
       const auto exec = exec map.at(executor string)(); // throws if not valid
       auto A = share(gko::read<mtx>(std::ifstream("data/A.mtx"), exec));
       gko::size_type size = A->get_size()[0];
       auto host_x = vec::create(exec-yet_master(), gko::dim<2>(size, 1));
for (auto i = 0; i < size; i++) {</pre>
              host_x->at(i, 0) = 1.;
       auto x = gko::clone(exec, host x);
       auto b = gko::clone(exec, host_x);
       auto one = gko::initialize<vec>({1.0}, exec);
       auto neg_one = gko::initialize<vec>({-1.0}, exec);
       auto initres = gko::initialize<real_vec>({0.0}, exec);
       A->apply(one, x, neg_one, b);
       b->compute_norm2(initres);
       b->copy_from(host_x);
       const RealValueType reduction_factor = 1e-7;
       auto solver_gen
              cg::build()
                      .with_criteria(gko::stop::Iteration::build().with_max_iters(10000u),
                                                 gko::stop::ResidualNorm<ValueType>::build()
                                                        .with_reduction_factor(reduction_factor))
                      .with_preconditioner(
                            \verb|bj::build().with_max_block_size(16u).with_storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(||storage_optimization(|
                                   gko::precision_reduction::autodetect()))
                      .on(exec);
       std::shared ptr<const qko::loq::Convergence<ValueType> logger =
              gko::log::Convergence<ValueType>::create();
       solver_gen->add_logger(logger);
       auto solver = solver_gen->generate(A);
       exec->synchronize();
       std::chrono::nanoseconds time(0);
       auto tic = std::chrono::steady_clock::now();
       solver->apply(b, x);
       auto toc = std::chrono::steady_clock::now();
       time += std::chrono::duration_cast<std::chrono::nanoseconds>(toc - tic);
       auto res = gko::as<real_vec>(logger->get_residual_norm());
       auto impl_res = gko::as<real_vec>(logger->get_implicit_sq_resnorm()); std::cout « "Initial residual norm sqrt(r^T r):\n";
       write(std::cout, initres);
       std::cout « "Final residual norm sqrt(r^T r):\n";
```

# **Chapter 9**

# The batched-solver program

Using and interfacing with a batched solver..

# **Using batched solvers**

This example shows how to use Ginkgo batched solvers with data coming from an application. The "application" in this case is just a function in the example itself; nevertheless, the steps to be taken are shown.

A 'batch' here means a set of small linear systems that can be solved independently, but each system is too small to use an entire computing device. A requirement is that all the systems need to have the same sparsity pattern.

# The commented program

#### 'Application' structures and functions

Structure to simulate application data related to the linear systems to be solved.

We use raw pointers below to demonstrate how to handle the situation when the application only gives us raw pointers. Ideally, one should use Ginkgo's gko::Array class here. In this example, we assume that the data is in a format that can directly be given to a batch::matrix::Csr object.

```
struct ApplSysData {
```

Number of small systems in the batch.

```
size_type nsystems;
```

#### Number of rows in each system.

```
int nrows
```

Number of non-zeros in each system matrix.

int nnz

#### Row pointers for one matrix

const index\_type\* row\_ptrs;

#### Column indices of non-zeros for one matrix

const index\_type\* col\_idxs;

#### Nonzero values for all matrices in the batch, concatenated

const value\_type\* all\_values;

#### RHS vectors for all systems in the batch, concatenated

#### Deallocate application data.

```
void appl_clean_up(ApplSysData& appl_data, std::shared_ptr<gko::Executor> exec);
int main(int argc, char* argv[])
```

### Print ginkgo version information

#### Where do you want to run your solver?

The gko::Executor class is one of the cornerstones of Ginkgo. Currently, we have support for an gko::OmpExecutor, which uses OpenMP multi-threading in most of its kernels, a gko::ReferenceExecutor, a single threaded specialization of the OpenMP executor, gko::CudaExecutor, gko::HipExecutor, gko::DpcppExecutor which runs the code on a NVIDIA, AMD and Intel GPUs, respectively.

Note

With the help of C++, you see that you only ever need to change the executor and all the other functions/routines within Ginkgo should automatically work and run on the executor with any other changes.

```
const auto executor_string = argc >= 2 ? argv[1] : "reference";
std::map<std::string, std::function<std::shared_ptr<gko::Executor>()»
    exec map{
               [] { return gko::OmpExecutor::create(); }},
        { "omp",
         [] {
             return gko::CudaExecutor::create(0,
                                              gko::OmpExecutor::create());
         }},
        {"hip",
         [] {
             return gko::HipExecutor::create(0, gko::OmpExecutor::create());
        { "dpcpp",
         [] {
             return gko::DpcppExecutor::create(0,
                                                gko::OmpExecutor::create());
```

```
}},
{"reference", [] { return gko::ReferenceExecutor::create(); }};

executor where Ginkgo will perform the computation
const auto exec = exec_map.at(executor_string)(); // throws if not valid
const size_type num_systems = argc >= 3 ? std::atoi(argv[2]) : 2;
const int num_rows = argc >= 4 ? std::atoi(argv[3]) : 32; // per system

Whether to print the residuals or not.
const bool print_residuals =
    argc >= 5 ? (std::string(argv[4]) == "true") : false;

The number of repetitions for the timing.
```

#### Generate data

The "application" generates the batch of linear systems on the device auto appl\_sys = appl\_generate\_system(num\_rows, num\_systems, exec);

const int num\_reps = argc >= 6 ? std::atoi(argv[5]) : 20;

Create batch\_dim object to describe the dimensions of the batch matrix.

```
auto batch_mat_size =
    gko::batch_dim<2>(num_systems, gko::dim<2>(num_rows, num_rows));
auto batch_vec_size =
    gko::batch_dim<2>(num_systems, gko::dim<2>(num_rows, 1));
```

#### Use of application-allocated memory

We can either work on the existing memory allocated in the application, or we can copy it for the linear solve. Ginkgo expects the nonzero values for all the small matrices to be allocated contiguously, one matrix after the other.

# RHS and solution vectors

batch\_stride object specifies the access stride within the individual matrices (vectors) in the batch. In this case, we specify a stride of 1 as the common value for all the matrices. Create RHS, again reusing application allocation

```
auto b_view = gko::array<value_type>::const_view(
    exec, num_systems * num_rows, appl_sys.all_rhs);
auto b = vec_type::create_const(exec, batch_vec_size, std::move(b_view));
```

#### Create initial guess as 0 and copy to device

```
auto x = vec_type::create(exec);
auto host_x = vec_type::create(exec->get_master(), batch_vec_size);
for (size_type isys = 0; isys < num_systems; isys++) {
    for (int irow = 0; irow < num_rows; irow++) {
        host_x->at(isys, irow, 0) = gko::zero<value_type>();
    }
}
x->copy from(host x.get());
```

### Create the batch solver factory

```
const real_type reduction_factor{1e-10};
```

Create a batched solver factory with relevant parameters.

```
auto solver =
  bicgstab::build()
    .with_max_iterations(500)
    .with_tolerance(reduction_factor)
    .with_tolerance_type(gko::batch::stop::tolerance_type::relative)
    .on(exec)
    ->generate(A);
```

#### **Batch logger**

Create a logger to obtain the iteration counts and "implicit" residual norms for every system after the solve.

```
std::shared_ptr<const gko::batch::log::BatchConvergence<value_type>
    logger = gko::batch::log::BatchConvergence<value_type>::create();
```

#### Generate and solve

```
add the logger to the solver
solver->add_logger(logger);
Solve the batch system
auto x_clone = gko::clone(x);
Warmup
for (int i = 0; i < 3; ++i) {
    x_clone->copy_from(x.get());
    solver->apply(b, x_clone);
double apply_time = 0.0;
for (int i = 0; i < num_reps; ++i) {</pre>
    x_clone->copy_from(x.get());
    exec->synchronize();
    std::chrono::steady_clock::time_point t1 =
        std::chrono::steady_clock::now();
    solver->apply(b, x_clone);
    exec->synchronize();
    std::chrono::steady_clock::time_point t2 =
        std::chrono::steady_clock::now();
    auto time_span =
        std::chrono::duration_cast<std::chrono::duration<double»(t2 - t1);</pre>
    apply_time += time_span.count();
x->copy_from(x_clone.get());
```

This is not necessary, but one might want to remove the logger before the next solve using the same solver object. solver->remove\_logger(logger.get());

#### **Check result**

```
Compute norm of RHS on the device and automatically copy to host
```

```
auto norm_dim = gko::batch_dim<2>(num_systems, gko::dim<2>(1, 1));
auto host_b_norm = real_vec_type::create(exec->get_master(), norm_dim);
host_b_norm->fill(0.0);
b->compute_norm2(host_b_norm);
```

#### we need constants on the device

```
auto one = vec_type::create(exec, norm_dim);
one->fill(1.0);
auto neg_one = vec_type::create(exec, norm_dim);
neg_one->fill(-1.0);
```

# allocate and compute the residual

```
auto res = vec_type::create(exec, batch_vec_size);
res->copy_from(b);
A->apply(one, x, neg_one, res);
```

### allocate and compute residual norm

"unbatch" converts a batch object into a vector of objects of the corresponding single type, eg. batch::matrix::Dense --> std::vector<Dense>.

Ginkgo objects are cleaned up automatically; but the "application" still needs to clean up its data in this case.

```
appl_clean_up(appl_sys, exec);
return 0;
```

Generate the matrix and the vectors. This function emulates the generation of the data from the application.

```
ApplSysData appl_generate_system(const int nrows, const size_type nsystems,
                                        std::shared ptr<gko::Executor> exec)
    const int nnz = nrows * 3 - 2;
    std::default_random_engine rgen(15);
    std::normal_distribution<real_type> distb(0.5, 0.1);
    std::vector<real_type> spacings(nsystems * nrows);
    std::generate(spacings.begin(), spacings.end(),
                      [&]() { return distb(rgen); });
    std::vector<value_type> allvalues(nnz * nsystems);
    for (size_type isys = 0; isys < nsystems; isys++) {
   allvalues.at(isys * nnz) = 2.0 / spacings.at(isys * nrows);
   allvalues.at(isys * nnz + 1) = -1.0;</pre>
         for (int irow = 0; irow < nrows - 2; irow++) {</pre>
              allvalues.at(isys * nnz + 2 + irow * 3) = -1.0;
allvalues.at(isys * nnz + 2 + irow * 3 + 1) =
                   2.0 / spacings.at(isys * nrows + irow + 1);
              allvalues.at(isys * nnz + 2 + irow * 3 + 2) = -1.0;
         allvalues.at(isys * nnz + 2 + (nrows - 2) * 3) = -1.0;
         allvalues.at(isys * nnz + 2 + (nrows - 2) * 3 + 1) = 2.0 / spacings.at((isys + 1) * nrows - 1);
          assert(isys * nnz + 2 + (nrows - 2) * 3 + 2 == (isys + 1) * nnz);
    std::vector<index_type> rowptrs(nrows + 1);
    rowptrs.at(0) = 0;
    rowptrs.at(1) = 2;
    for (int i = 2; i < nrows; i++) {</pre>
         rowptrs.at(i) = rowptrs.at(i - 1) + 3;
    rowptrs.at(nrows) = rowptrs.at(nrows - 1) + 2;
    assert(rowptrs.at(nrows) == nnz);
    std::vector<index_type> colidxs(nnz);
    colidxs.at(0) = 0;
    colidxs.at(1) = 1;
    const int nnz_per_row = 3;
     for (int irow = 1; irow < nrows - 1; irow++) {</pre>
         colidxs.at(2 + (irow - 1) * nnz_per_row) = irow - 1;
colidxs.at(2 + (irow - 1) * nnz_per_row + 1) = irow;
         colidxs.at(2 + (irow - 1) * nnz_per_row + 2) = irow + 1;
    colidxs.at(2 + (nrows - 2) * nnz_per_row) = nrows - 2;
colidxs.at(2 + (nrows - 2) * nnz_per_row + 1) = nrows - 1;
    assert(2 + (nrows - 2) * nnz_per_row + 1 == nnz - 1);
    std::vector<value_type> allb(nrows * nsystems);
for (size_type isys = 0; isys < nsystems; isys++) {</pre>
          const value_type bval = distb(rgen);
         std::fill(allb.begin() + isys * nrows,
allb.begin() + (isys + 1) * nrows, bval);
    index type* const row ptrs = exec->alloc<index type>(nrows + 1);
    exec->copy_from(exec->get_master().get(), static_cast<size_type>(nrows + 1),
                        rowptrs.data(), row_ptrs);
```

```
index_type* const col_idxs = exec->alloc<index_type>(nnz);
   exec->copy_from(exec->get_master().get(), static_cast<size_type>(nnz),
                  colidxs.data(), col_idxs);
   value_type* const all_values = exec->alloc<value_type>(nsystems * nnz);
   all_values);
   value_type* const all_b = exec->alloc<value_type>(nsystems * nrows);
   exec->copy_from(exec->get_master().get(), nsystems * nrows, allb.data(),
                  all_b);
   return {nsystems, nrows, nnz, row_ptrs, col_idxs, all_values, all_b};
void appl_clean_up(ApplSysData& appl_data, std::shared_ptr<gko::Executor> exec)
In general, the application would control non-const pointers; the const casts below would not be needed.
    exec->free(const_cast<index_type*>(appl_data.row_ptrs));
   exec->free(const_cast<index_type*>(appl_data.col_idxs));
   exec->free(const_cast<value_type*>(appl_data.all_values));
   exec->free(const_cast<value_type*>(appl_data.all_rhs));
```

### Results

The following is the expected result on the reference executor:

```
Solver type: batch::bicgstab
Matrix size: (32, 32)
Num batch entries: 2
Entire solve took: 2.18558e-05 seconds.
```

#### Comments about programming and debugging

# The plain program

```
#include <fstream>
#include <iostream>
#include <map>
#include <random>
#include <string>
#include <ginkgo/ginkgo.hpp>
using value_type = double;
using real_type = gko::remove_complex<value_type>;
using index_type = int;
using size_type = gko::size_type;
using vec_type = gko::batch::MultiVector<value_type>;
using real_vec_type = gko::batch::MultiVector<real_type>;
using mtx_type = gko::batch::matrix::Csr<value_type, index_type>;
using bicgstab = gko::batch::solver::Bicgstab<value_type>;
namespace detail {
template <typename InputType>
auto unbatch(const InputType* batch_object)
    auto unbatched_mats =
        std::vector<std::unique_ptr<typename InputType::unbatch_type»{};</pre>
    for (size_type b = 0; b < batch_object->get_num_batch_items(); ++b) {
         unbatched_mats.emplace_back(
             batch_object->create_const_view_for_item(b)->clone());
    return unbatched_mats;
   // namespace detail
struct ApplSysData {
    size_type nsystems;
    int nrows;
    int nnz;
    const index_type* row_ptrs;
    const index_type* col_idxs;
    const value_type* all_values;
    const value_type* all_rhs;
* Generates a batch of tridiagonal systems.
* @param nrows Number of rows in each system.
* @param nsystems Number of systems in the batch.
```

```
* @param exec The device executor to use for the solver.
* @note Normally, the application may not deal with Ginkgo executors, nor do * we need it to. Here, we use the executor for backend-independent device * memory allocation. The application, for example, might assume Hip (for AMD
* GPUs) and use 'hipMalloc' directly.
ApplSysData appl_generate_system(const int nrows, const size_type nsystems,
                                      std::shared_ptr<gko::Executor> exec);
void appl_clean_up(ApplSysData& appl_data, std::shared_ptr<gko::Executor> exec);
int main(int argc, char* argv[])
    std::cout « gko::version_info::get() « std::endl;
if (argc == 2 && (std::string(argv[1]) == "--help")) {
    std::cerr « "Usage: " « argv[0]
                    « " [executor] [num_systems] [num_rows] [print_residuals] "
    "[num_reps]"
                     « std::endl;
         std::exit(-1);
    const auto executor_string = argc >= 2 ? argv[1] : "reference";
    std::map<std::string, std::function<std::shared_ptr<gko::Executor>()>
         exec_map{
              {"omp", [] { return gko::OmpExecutor::create(); }},
              {"cuda".
               [] {
                   return gko::CudaExecutor::create(0,
                                                           gko::OmpExecutor::create());
               } } ,
              {"hip",
               [] {
                   return gko::HipExecutor::create(0, gko::OmpExecutor::create());
              {"dpcpp",
               [] {
                    return gko::DpcppExecutor::create(0,
                                                            gko::OmpExecutor::create());
              {"reference", [] { return gko::ReferenceExecutor::create(); }}};
    const auto exec = exec_map.at(executor_string)(); // throws if not valid
    const size_type num_systems = argc >= 3 ? std::atoi(argv[2]) :
    const int num_rows = argc >= 4 ? std::atoi(argv[3]) : 32; // per system
    const bool print_residuals =
    argc >= 5 ? (std::string(argv[4]) == "true") : false;
const int num_reps = argc >= 6 ? std::atoi(argv[5]) : 20;
    auto appl_sys = appl_generate_system(num_rows, num_systems, exec);
    auto batch_mat_size =
         gko::batch_dim<2>(num_systems, gko::dim<2>(num_rows, num_rows));
    auto batch_vec_size =
         gko::batch_dim<2>(num_systems, gko::dim<2>(num_rows, 1));
    auto vals_view = gko::array<value_type>::const_view(
         exec, num_systems * appl_sys.nnz, appl_sys.all_values);
    auto rowptrs_view = gko::array<index_type>::const_view(exec, num_rows + 1,
                                                                      appl_sys.row_ptrs);
    auto colidxs_view = gko::array<index_type>::const_view(exec, appl_sys.nnz,
                                                                     appl_sys.col_idxs);
    auto A = gko::share(mtx_type::create_const(
         exec, batch_mat_size, std::move(vals_view), std::move(colidxs_view),
         std::move(rowptrs_view)));
     auto b_view = gko::array<value_type>::const_view(
         exec, num_systems * num_rows, appl_sys.all_rhs);
    auto b = vec_type::create_const(exec, batch_vec_size, std::move(b_view));
    auto b = vec_type::create(exec);
auto x = vec_type::create(exec);
auto host_x = vec_type::create(exec->get_master(), batch_vec_size);
    for (size_type isys = 0; isys < num_systems; isys++) {
   for (int irow = 0; irow < num_rows; irow++) {</pre>
             host_x->at(isys, irow, 0) = gko::zero<value_type>();
    x->copy_from(host_x.get());
    const real_type reduction_factor{1e-10};
     auto solver
         bicgstab::build()
              .with_max_iterations(500)
              .with_tolerance(reduction_factor)
              . \verb|with_tolerance_type(gko::batch::stop::tolerance_type::relative)|\\
              .on(exec)
              ->generate(A);
     std::shared_ptr<const gko::batch::log::BatchConvergence<value_type>
         logger = gko::batch::log::BatchConvergence<value_type>::create();
    solver->add_logger(logger);
    auto x_clone = gko::clone(x);
for (int i = 0; i < 3; ++i) {</pre>
         x_clone->copy_from(x.get());
         solver->apply(b, x_clone);
    double apply_time = 0.0;
for (int i = 0; i < num_reps; ++i) {</pre>
```

```
x_clone->copy_from(x.get());
        exec->synchronize();
        std::chrono::steady_clock::time_point t1 =
            std::chrono::steady_clock::now();
        solver->apply(b, x_clone);
        exec->svnchronize();
        std::chrono::steady_clock::time_point t2 =
            std::chrono::steady_clock::now();
        auto time_span =
            std::chrono::duration_cast<std::chrono::duration<double»(t2 - t1);</pre>
        apply_time += time_span.count();
    x->copy from(x clone.get());
    solver->remove_logger(logger.get());
    auto norm_dim = gko::batch_dim<2>(num_systems, gko::dim<2>(1, 1));
    auto host_b_norm = real_vec_type::create(exec->get_master(), norm_dim);
    host b norm->fill(0.0);
    b->compute_norm2(host_b_norm);
    auto one = vec_type::create(exec, norm_dim);
    one->fill(1.0);
    auto neg_one = vec_type::create(exec, norm_dim);
    neg_one->fill(-1.0);
    auto res = vec_type::create(exec, batch_vec_size);
    res->copy_from(b);
    A->apply(one, x, neg_one, res);
    auto host_res_norm = real_vec_type::create(exec->get_master(), norm_dim);
    host_res_norm->fill(0.0);
    res->compute_norm2(host_res_norm);
    auto host_log_resid = gko::make_temporary_clone(
        exec->get_master(), &logger->get_residual_norm());
    auto host_log_iters = gko::make_temporary_clone(
        exec->get_master(), &logger->get_num_iterations());
    if (print_residuals) {
        std::cout « "Residual norm sqrt(r^T r):\n";
        auto unb_res = detail::unbatch(host_res_norm.get());
        auto unb_bnorm = detail::unbatch(host_b_norm.get());
        « host_log_resid->get_const_data()[i]
                       « ", iterations =
                       « host_log_iters->get_const_data()[i] « std::endl;
             const real_type relresnorm =
                 unb_res[i]->at(0, 0) / unb_bnorm[i]->at(0, 0);
            }
        }
    std::cout « "Solver type: "
              "\nMatrix size: " « A->get_common_size()
"\nNum batch entries: " « A->get_num_batch_items()
"\nEntire solve took: " « apply_time / num_reps « " seconds."
               « std::endl;
    appl_clean_up(appl_sys, exec);
    return 0;
ApplSysData appl_generate_system(const int nrows, const size_type nsystems,
                                   std::shared_ptr<gko::Executor> exec)
    const int nnz = nrows * 3 - 2;
    std::default_random_engine rgen(15);
    std::normal_distribution<real_type> distb(0.5, 0.1);
    std::vector<real_type> spacings(nsystems * nrows);
    std::vector<value_type> allvalues(nnz * nsystems);
    for (size_type isys = 0; isys < nsystems; isys++) {
   allvalues.at(isys * nnz) = 2.0 / spacings.at(isys * nrows);
   allvalues.at(isys * nnz + 1) = -1.0;
   for (int irow = 0; irow < nrows - 2; irow++) {</pre>
            allvalues.at(isys * nnz + 2 + irow * 3) = -1.0;
allvalues.at(isys * nnz + 2 + irow * 3 + 1) =
                2.0 / spacings.at(isys * nrows + irow + 1);
             allvalues.at(isys * nnz + 2 + irow * 3 + 2) = -1.0;
        allvalues.at(isys * nnz + 2 + (nrows - 2) * 3) = -1.0;
        all values. at (isys * mz + 2 + (mrows - 2) * 3 + 1) = 2.0 / spacings. at ((isys + 1) * mrows - 1);
        assert(isys * nnz + 2 + (nrows - 2) * 3 + 2 == (isys + 1) * nnz);
    std::vector<index_type> rowptrs(nrows + 1);
    rowptrs.at(0) = 0;
    rowptrs.at(1) = 2;
```

```
for (int i = 2; i < nrows; i++) {</pre>
         rowptrs.at(i) = rowptrs.at(i - 1) + 3;
    rowptrs.at(nrows) = rowptrs.at(nrows - 1) + 2;
    assert(rowptrs.at(nrows) == nnz);
    std::vector<index_type> colidxs(nnz);
    colidxs.at(0) = 0;
    colidxs.at(1) = 1;
    const int nnz_per_row = 3;
    for (int irow = 1; irow < nrows - 1; irow++) {</pre>
         colidxs.at(2 + (irow - 1) * nnz_per_row) = irow - 1;
colidxs.at(2 + (irow - 1) * nnz_per_row + 1) = irow;
         colidxs.at(2 + (irow - 1) * nnz_per_row + 2) = irow + 1;
    colidxs.at(2 + (nrows - 2) * nnz_per_row) = nrows - 2;
colidxs.at(2 + (nrows - 2) * nnz_per_row + 1) = nrows - 1;
assert(2 + (nrows - 2) * nnz_per_row + 1 == nnz - 1);
    std::vector<value_type> allb(nrows * nsystems);
    for (size_type isys = 0; isys < nsystems; isys++) {</pre>
         const value_type bval = distb(rgen);
         std::fill(allb.begin() + isys * nrows,
allb.begin() + (isys + 1) * nrows, bval);
    index_type* const row_ptrs = exec->alloc<index_type>(nrows + 1);
exec->copy_from(exec->get_master().get(), static_cast<size_type>(nrows + 1),
                      rowptrs.data(), row_ptrs);
    index_type* const col_idxs = exec->alloc<index_type>(nnz);
    exec->copy_from(exec->get_master().get(), static_cast<size_type>(nnz),
                       colidxs.data(), col_idxs);
    value_type* const all_values = exec->alloc<value_type>(nsystems * nnz);
    exec->copy_from(exec->get_master().get(), nsystems * nnz, allvalues.data(),
                       all_values);
    value_type* const all_b = exec->alloc<value_type>(nsystems * nrows);
    \verb|exec->copy_from(exec->get_master().get(), nsystems * nrows, allb.data(), |
                       all_b);
    return {nsystems, nrows, nnz, row_ptrs, col_idxs, all_values, all_b};
void appl_clean_up(ApplSysData& appl_data, std::shared_ptr<gko::Executor> exec)
    exec->free(const_cast<index_type*>(appl_data.row_ptrs));
    exec->free(const_cast<index_type*>(appl_data.col_idxs));
    exec->free(const_cast<value_type*>(appl_data.all_values));
    exec->free(const_cast<value_type*>(appl_data.all_rhs));
```

# The cb-gmres program

The CB-GMRES solver example..

### Introduction

### About the example

This example showcases the usage of the Ginkgo solver CB-GMRES (Compressed Basis GMRES). A small system is solved with two un-preconditioned CB-GMRES solvers:

- 1. without compressing the krylov basis; it uses double precision for both the matrix and the krylov basis, and
- 2. with a compression of the krylov basis; it uses double precision for the matrix and all arithmetic operations, while using single precision for the storage of the krylov basis

Both solves are timed and the residual norm of each solution is computed to show that both solutions are correct.

### The commented program

Make sure all previous executor operations have finished before starting the time

```
exec->synchronize();
auto tic = std::chrono::steady_clock::now();
solver->apply(b, x_copy);
```

Make sure all computations are done before stopping the time

```
exec->synchronize();
auto tac = std::chrono::steady_clock::now();
duration += std::chrono::duration<double>(tac - tic).count();
```

Copy the solution back to x, so the caller has the result

```
x->copy_from(x_copy);
  return duration / static_cast<double>(repeats);
}
int main(int argc, char* argv[])
{
```

Use some shortcuts. In Ginkgo, vectors are seen as a gko::matrix::Dense with one column/one row. The advantage of this concept is that using multiple vectors is a now a natural extension of adding columns/rows are necessary.

```
using ValueType = double;
using RealValueType = gko::remove_complex<ValueType>;
using IndexType = int;
using vec = gko::matrix::Dense<ValueType>;
using real_vec = gko::matrix::Dense<RealValueType>;
```

The gko::matrix::Csr class is used here, but any other matrix class such as gko::matrix::Coo, gko::matrix::Hybrid, gko::matrix::Ell or gko::matrix::Sellp could also be used.

```
using mtx = gko::matrix::Csr<ValueType, IndexType>;
```

The gko::solver::CbGmres is used here, but any other solver class can also be used.

using cb gmres = gko::solver::CbGmres<ValueType>;

```
Print the ginkgo version information.
```

```
std::cout « gko::version_info::get() « std::endl;
if (argc == 2 && (std::string(argv[1]) == "--help")) {
    std::cerr « "Usage: " « argv[0] « " [executor] " « std::endl;
    std::exit(-1);
}
```

### Map which generates the appropriate executor

```
const auto executor_string = argc >= 2 ? argv[1] : "reference";
std::map<std::string, std::function<std::shared_ptr<gko::Executor>()»
    exec_map{
         {"omp", [] { return gko::OmpExecutor::create(); }},
         {"cuda",
          [] {
              return gko::CudaExecutor::create(0,
                                                     gko::OmpExecutor::create());
          } },
         {"hip",
          [] {
              return gko::HipExecutor::create(0, gko::OmpExecutor::create());
          }},
         {"dpcpp",
          [] {
               return gko::DpcppExecutor::create(0,
                                                       gko::OmpExecutor::create());
         {"reference", [] { return gko::ReferenceExecutor::create(); }}};
```

### executor where Ginkgo will perform the computation

```
const auto exec = exec_map.at(executor_string)(); // throws if not valid
```

Note: this matrix is copied from "SOURCE\_DIR/matrices" instead of from the local directory. For details, see "examples/cb-gmres/CMakeLists.txt"

```
auto A = share(gko::read<mtx>(std::ifstream("data/A.mtx"), exec));
```

Create a uniform right-hand side with a norm2 of 1 on the host (norm2(b) == 1), followed by copying it to the actual executor (to make sure it also works for GPUs)

### As an initial guess, use the right-hand side

```
auto x_keep = clone(b);
auto x_reduce = clone(x_keep);
const RealValueType reduction_factor{1e-6};
```

Generate two solver factories: \_keep uses the same precision for the krylov basis as the matrix, and \_reduce uses one precision below it. If ValueType is double, then \_reduce uses float as the krylov basis storage type

#### Generate the actual solver from the factory and the matrix.

```
auto solver_keep = solver_gen_keep->generate(A);
auto solver_reduce = solver_gen_reduce->generate(A);
```

### Solve both system and measure the time for each.

### Make sure the output is in scientific notation for easier comparison

std::cout « std::scientific;

### Note: The time might not be significantly different since the matrix is quite small

```
std::cout « "Solve time without compression: " « time_keep « " s\n" « "Solve time with compression: " « time_reduce « " s\n";
```

To measure if your solution has actually converged, the error of the solution is measured. one, neg\_one are objects that represent the numbers which allow for a uniform interface when computing on any device. To compute the residual, the (advanced) apply method is used.

```
tmp = Ax - tmp
A->apply(one, x_keep, neg_one, tmp);
tmp->compute_norm2(res_norm_keep);
std::cout ("\nResidual norm with compression:\n";
tmp->compute_norm2(res_norm_keep);
tmp->compute_norm2(res_norm_keep);
tmp->compute_norm2(res_norm_keep);
tmp->compute_norm2(res_norm_reduce);
std::cout ("\nResidual norm with compression:\n";
write(std::cout, res_norm_reduce);
std::cout, res_norm_reduce);
}
```

### Results

### The following is the expected result:

```
Solve time without compression: 1.842690e-04 s
Solve time with compression: 1.589936e-04 s
Residual norm without compression:
%*MatrixMarket matrix array real general
1 1
2.430544e-07
Residual norm with compression:
%*MatrixMarket matrix array real general
1 1
3.437257e-07
```

### Comments about programming and debugging

```
#include <chrono>
#include <cmath>
#include <fstream>
#include <iostream>
#include <map>
#include <string>
#include <ginkgo/ginkgo.hpp>
double measure_solve_time_in_s(std::shared_ptr<const gko::Executor> exec,
                                   gko::LinOp* solver, const gko::LinOp* b,
                                   gko::LinOp* x)
    constexpr int repeats{5};
    double duration{0};
    auto x_copy = clone(x);
for (int i = 0; i < repeats; ++i) {
   if (i != 0) {</pre>
             x_copy->copy_from(x);
         exec->synchronize();
         auto tic = std::chrono::steady_clock::now();
         solver->apply(b, x_copy);
         exec->svnchronize();
         auto tac = std::chrono::steady_clock::now();
         duration += std::chrono::duration<double>(tac - tic).count();
    x->copy_from(x_copy);
    return duration / static_cast<double>(repeats);
int main(int argc, char* argv[])
    using ValueType = double;
    using RealValueType = gko::remove_complex<ValueType>;
    using IndexType = int;
    using vec = gko::matrix::Dense<ValueType>;
    using real_vec = gko::matrix::Dense<RealValueType>;
    using mtx = gko::matrix::Csr<ValueType, IndexType>;
    using cb_gmres = gko::solver::CbGmres<ValueType>;
    std::cout « gko::version_info::get() « std::endl;
if (argc == 2 && (std::string(argv[1]) == "--help")) {
    std::cerr « "Usage: " « argv[0] « " [executor] " « std::endl;
         std::exit(-1);
    const auto executor_string = argc >= 2 ? argv[1] : "reference";
    std::map<std::string, std::function<std::shared_ptr<gko::Executor>()»
         exec_map{
              {"omp", [] { return gko::OmpExecutor::create(); }},
              {"cuda",
              [] {
                   return gko::CudaExecutor::create(0,
                                                         gko::OmpExecutor::create());
              }},
              {"hip",
               [] {
                   return gko::HipExecutor::create(0, gko::OmpExecutor::create());
              {"dpcpp",
                   return gko::DpcppExecutor::create(0,
                                                          gko::OmpExecutor::create());
              {"reference", [] { return gko::ReferenceExecutor::create(); }}};
    const auto exec = exec_map.at(executor_string)(); // throws if not valid
auto A = share(gko::read<mtx>(std::ifstream("data/A.mtx"), exec));
    const auto A_size = A->get_size();
    auto b_host = vec::create(exec->get_master(), gko::dim<2>{A_size[0], 1});
for (gko::size_type i = 0; i < A_size[0]; ++i) {
   b_host->at(i, 0) =
              ValueType{1} / std::sqrt(static_cast<ValueType>(A_size[0]));
    auto b_norm = gko::initialize<real_vec>({0.0}, exec);
    b_host->compute_norm2(b_norm);
    auto b = clone(exec, b_host);
    auto x_keep = clone(b);
    auto x_reduce = clone(x_keep);
    const RealValueType reduction_factor{1e-6};
    auto solver_gen_keep =
         cb_gmres::build()
              .with criteria(gko::stop::Iteration::build().with max iters(1000u),
                              gko::stop::ResidualNorm<ValueType>::build()
                                   .with_baseline(gko::stop::mode::rhs_norm)
```

```
.with_reduction_factor(reduction_factor))
        .with_krylov_dim(100u)
        .with_storage_precision(
            gko::solver::cb_gmres::storage_precision::keep)
        .on(exec);
auto solver_gen_reduce
    cb_gmres::build()
        .with_criteria(gko::stop::Iteration::build().with_max_iters(1000u),
                       gko::stop::ResidualNorm<ValueType>::build()
                           .with_baseline(gko::stop::mode::rhs_norm)
                           . \verb|with_reduction_factor(reduction_factor)||\\
        .with_krylov_dim(100u)
        .with_storage_precision(
            gko::solver::cb_gmres::storage_precision::reduce1)
         on (exec);
auto solver_keep = solver_gen_keep->generate(A);
auto solver_reduce = solver_gen_reduce->generate(A);
auto time keep =
   measure_solve_time_in_s(exec, solver_keep.get(), b.get(), x_keep.get());
auto time_reduce = measure_solve_time_in_s(exec, solver_reduce.get(),
                                           b.get(), x_reduce.get());
std::cout « std::scientific;
auto res_norm_keep = gko::initialize<real_vec>({0.0}, exec);
auto res_norm_reduce = gko::initialize<real_vec>({0.0}, exec);
auto tmp = gko::clone(b);
A->apply(one, x_keep, neg_one, tmp);
tmp->compute_norm2(res_norm_keep);
std::cout « "\nResidual norm without compression:\n";
write(std::cout, res_norm_keep);
tmp->copy_from(b);
A->apply(one, x_reduce, neg_one, tmp);
tmp->compute_norm2(res_norm_reduce);
std::cout « "\nResidual norm with compression:\n";
write(std::cout, res_norm_reduce);
```

# The custom-logger program

The simple solver with a custom logger example..

This example depends on simple-solver, simple-solver-logging, minimal-cuda-solver.

### Introduction

The custom-logger example shows how Ginkgo's API can be leveraged to implement application-specific callbacks for Ginkgo's events. This is the most basic way of extending Ginkgo and a good first step for any application developer who wants to adapt Ginkgo to his specific needs.

Ginkgo's gko::log::Logger abstraction provides hooks to the events that happen during the library execution. These hooks concern any low-level event such as memory allocations, deallocations, copies and kernel launches up to high-level events such as linear operator applications and completion of solver iterations.

In this example, a simple logger is implemented to track the solver's recurrent residual norm and compute the true residual norm. At the end of the solver execution, a comparison table is shown on-screen.

### About the example

Each example has the following sections:

- 1. **Introduction:**This gives an overview of the example and mentions any interesting aspects in the example that might help the reader.
- 2. **The commented program:** This section is intended for you to understand the details of the example so that you can play with it and understand Ginkgo and its features better.
- 3. **Results:** This section shows the results of the code when run. Though the results may not be completely the same, you can expect the behaviour to be similar.
- 4. **The plain program:** This is the complete code without any comments to have an complete overview of the code.

### The commented program

```
return mtx->get_executor()->copy_val_to_host(mtx->get_const_values());

Utility function which computes the norm of a Ginkgo gko::matrix::Dense vector.
template <typename ValueType>
gko::remove_complex<ValueType> compute_norm(
    const gko::matrix::Dense<ValueType>* b)
{

Get the executor of the vector
auto exec = b->get_executor();

Initialize a result scalar containing the value 0.0.
auto b_norm =
    gko::initialize<gko::matrix::Dense<gko::remove_complex<ValueType>>(
    {0.0}, exec);
```

Use the dense compute\_norm2 function to compute the norm. b->compute\_norm2 (b\_norm);

```
Use the other utility function to return the norm contained in b_norm return get_first_element(b_norm.get());
```

Custom logger class which intercepts the residual norm scalar and solution vector in order to print a table of real vs recurrent (internal to the solvers) residual norms.

```
template <typename ValueType>
struct ResidualLogger : gko::log::Logger {
    using RealValueType = gko::remove_complex<ValueType>;
```

### Output the logger's data in a table format

```
void write()const
```

### Print a header for the table

Print a separation line. Note that for creating 10 characters std::setw() should be set to 11.

### Print the data one by one in the form

std::defaultfloat could be used here but some compilers do not support it properly, e.g. the Intel compiler std::cout.unsetf(std::ios\_base::floatfield);

### Print a separation line

### Customize the logging hook which is called everytime an iteration is completed

```
const gko::LinOp* residual_norm,
                           const gko::LinOp* implicit_sq_residual_norm,
                           const gko::array<gko::stopping_status>*,
                           bool)const override
If the solver shares a residual norm, log its value
if (residual_norm) {
    auto dense_norm = gko::as<gko_real_dense>(residual_norm);
Add the norm to the recurrent_norms vector
recurrent_norms.push_back(get_first_element(dense_norm));
Otherwise, use the recurrent residual vector
} else {
    auto dense_residual = gko::as<gko_dense>(residual);
Compute the residual vector's norm
auto norm = compute_norm(dense_residual);
Add the computed norm to the recurrent_norms vector
    recurrent_norms.push_back(norm);
If the solver shares the current solution vector
if (solution) {
Extract the matrix from the solver
auto matrix = gko::as<gko::solver::detail::SolverBaseLinOp>(solver)
                  ->get_system_matrix();
Store the matrix's executor
auto exec = matrix->get_executor();
Create a scalar containing the value 1.0
auto one = gko::initialize<gko_dense>({1.0}, exec);
Create a scalar containing the value -1.0
auto neg_one = gko::initialize<gko_dense>({-1.0}, exec);
Instantiate a temporary result variable
auto res = gko::as<gko_dense>(gko::clone(b));
Compute the real residual vector by calling apply on the system matrix
matrix->apply(one, solution, neg_one, res);
Compute the norm of the residual vector and add it to the real_norms vector
    real_norms.push_back(compute_norm(res.get()));
} else {
Add to the real_norms vector the value -1.0 if it could not be computed
    real_norms.push_back(-1.0);
if (implicit_sq_residual_norm) {
    auto dense norm =
        gko::as<gko_real_dense>(implicit_sq_residual_norm);
Add the norm to the implicit_norms vector
    implicit_norms.push_back(std::sqrt(get_first_element(dense_norm)));
Add to the implicit_norms vector the value -1.0 if it could not be computed
    implicit_norms.push_back(-1.0);
Add the current iteration number to the iterations vector
    iterations.push_back(iteration);
```

Construct the logger

#### Vector which stores all the recurrent residual norms

mutable std::vector<RealValueType> recurrent\_norms{};

### Vector which stores all the real residual norms

mutable std::vector<RealValueType> real\_norms{};

### Vector which stores all the implicit residual norms

mutable std::vector<RealValueType> implicit\_norms{};

### Vector which stores all the iteration numbers

```
mutable std::vector<std::size_t> iterations{};
};
int main(int argc, char* argv[])
{
```

Use some shortcuts. In Ginkgo, vectors are seen as a gko::matrix::Dense with one column/one row. The advantage of this concept is that using multiple vectors is a now a natural extension of adding columns/rows are necessary.

```
using ValueType = double;
using RealValueType = gko::remove_complex<ValueType>;
using IndexType = int;
using vec = gko::matrix::Dense<ValueType>;
using real_vec = gko::matrix::Dense<RealValueType>;
```

The gko::matrix::Csr class is used here, but any other matrix class such as gko::matrix::Coo, gko::matrix::Hybrid, gko::matrix::Ell or gko::matrix::Sellp could also be used.

using mtx = gko::matrix::Csr<ValueType, IndexType>;

The gko::solver::Cg is used here, but any other solver class can also be used.

using cg = gko::solver::Cg<ValueType>;

### Print the ginkgo version information.

std::cout « gko::version\_info::get() « std::endl;

### Where do you want to run your solver?

The gko::Executor class is one of the cornerstones of Ginkgo. Currently, we have support for an gko::OmpExecutor, which uses OpenMP multi-threading in most of its kernels, a gko::ReferenceExecutor, a single threaded specialization of the OpenMP executor and a gko::CudaExecutor which runs the code on a NVIDIA GPU if available.

Note

With the help of C++, you see that you only ever need to change the executor and all the other functions/routines within Ginkgo should automatically work and run on the executor with any other changes.

```
if (argc == 2 && (std::string(argv[1]) == "--help")) {
    std::cerr « "Usage: " « argv[0] « " [executor]" « std::endl;
    std::exit(-1);
}
const auto executor_string = argc >= 2 ? argv[1] : "reference";
```

### Figure out where to run the code

### executor where Ginkgo will perform the computation

const auto exec = exec\_map.at(executor\_string)(); // throws if not valid

### Reading your data and transfer to the proper device.

Read the matrix, right hand side and the initial solution using the read function.

Note

Ginkgo uses C++ smart pointers to automatically manage memory. To this end, we use our own object ownership transfer functions that under the hood call the required smart pointer functions to manage object ownership. gko::share and gko::give are the functions that you would need to use.

```
auto A = share(gko::read<mtx>(std::ifstream("data/A.mtx"), exec));
auto b = gko::read<vec>(std::ifstream("data/b.mtx"), exec);
auto x = gko::read<vec>(std::ifstream("data/x0.mtx"), exec);
const RealValueType reduction_factor = 1e-7;
```

### Creating the solver

Generate the gko::solver factory. Ginkgo uses the concept of Factories to build solvers with certain properties. Observe the Fluent interface used here. Here a cg solver is generated with a stopping criteria of maximum iterations of 20 and a residual norm reduction of 1e-15. You also observe that the stopping criteria(gko::stop) are also generated from factories using their build methods. You need to specify the executors which each of the object needs to be built on.

### Instantiate a ResidualLogger logger.

auto logger = std::make\_shared<ResidualLogger<ValueType»();</pre>

Add the previously created logger to the solver factory. The logger will be automatically propagated to all solvers created from this factory.

```
solver_gen->add_logger(logger);
```

Generate the solver from the matrix. The solver factory built in the previous step takes a "matrix"(a gko::LinOp to be more general) as an input. In this case we provide it with a full matrix that we previously read, but as the solver only effectively uses the apply() method within the provided "matrix" object, you can effectively create a gko::LinOp class with your own apply implementation to accomplish more tasks. We will see an example of how this can be done in the custom-matrix-format example

```
auto solver = solver_gen->generate(A);
```

Finally, solve the system. The solver, being a gko::LinOp, can be applied to a right hand side, b to obtain the solution, x.

```
solver->apply(b, x);
```

Print the solution to the command line.

```
std::cout « "Solution (x):\n";
write(std::cout, x);
```

### Print the table of the residuals obtained from the logger

```
logger->write();
```

To measure if your solution has actually converged, you can measure the error of the solution. one, neg\_one are objects that represent the numbers which allow for a uniform interface when computing on any device. To compute the residual, all you need to do is call the apply method, which in this case is an spmv and equivalent to the LAPACK z\_spmv routine. Finally, you compute the euclidean 2-norm with the compute\_norm2 function.

```
auto one = gko::initialize<vec>({1.0}, exec);
auto neg_one = gko::initialize<vec>({-1.0}, exec);
auto res = gko::initialize<real_vec>({0.0}, exec);
A->apply(one, x, neg_one, b);
b->compute_norm2(res);
std::cout « "Residual norm sqrt(r^T r):\n";
write(std::cout, res);
```

# Results

```
The following is the expected result:
Solution (x):
%%MatrixMarket matrix array real general
19 1
0.252218
0.108645
0.0662811
0.0630433
0.0384088
0.0396536
0.0402648
0.0338935
0.0193098
0.0234653
0.0211499
0.0196413
0.0199151
0.0181674
0.0162722
0.0150714
0.0107016
0.0121141
0.0123025
Recurrent vs true vs implicit residual norm:
| Iteration| Recurrent Residual Norm|
                                              True Residual Norm| Implicit Residual Norm|
          0.1
                          4.358899e+001
                                                     4.358899e+001
                                                                                4.358899e+00
          1 I
                         2.304548e+00|
                                                     2.304548e+001
                                                                                2.304548e+00
                          1.467706e+00|
                                                     1.467706e+00|
                                                                                1.467706e+00|
          21
                          9.848751e-01|
                                                                                9.848751e-01|
                                                    9.848751e-01|
                          7.418330e-01|
                                                     7.418330e-01|
                                                                                7.418330e-01|
                                                   5.136231e-01|
3.841650e-01|
          5 I
                         5.136231e-01|
                                                                                5.136231e-01
                          3.841650e-01|
                                                                                3.841650e-01
                          3.164394e-011
                                                     3.164394e-011
                                                                                3.164394e-011
                          2.277088e-01|
                                                   2.277088e-01|
                                                                                2.277088e-01|
          81
                          1.703121e-01|
                                                     1.703121e-01|
                                                                                1.703121e-01|
         10
                          9.737220e-02|
                                                     9.737220e-02|
                                                                                9.737220e-02
         11|
                          6.168306e-02|
                                                    6.168306e-02|
                                                                                6.168306e-02
                                                    4.541231e-02|
3.195304e-02|
         12|
                          4.541231e-02|
                                                                                4.541231e-02
         131
                          3.195304e-021
                                                                                3.195304e-02
                          1.616058e-02|
                                                    1.616058e-02|
                                                                                1.616058e-02
         141
                         6.570152e-03|
                                                   6.570152e-03|
         15|
                                                                                6.570152e-03|
         16|
                          2.643669e-03|
                                                     2.643669e-03|
                                                                                2.643669e-03|
         17
                          8.588089e-04|
                                                     8.588089e-04|
                                                                                8.588089e-04|
         181
                          2.864613e-041
                                                     2.864613e-041
                                                                                2.864613e-04
         191
                         1.641952e-15|
                                                     2.107881e-15|
                                                                                1.641952e-15|
Residual norm sqrt(r^T r):
%%MatrixMarket matrix array real general
2.10788e-15
```

### Comments about programming and debugging

```
#include <ginkgo/ginkgo.hpp>
#include <fstream>
#include <map>
#include <iomanip>
#include <ios>
#include <iostream>
#include <string>
#include <vector>
template <typename ValueType>
ValueType get_first_element(const gko::matrix::Dense<ValueType>* mtx)
    return mtx->get_executor()->copy_val_to_host(mtx->get_const_values());
template <typename ValueType>
gko::remove_complex<ValueType> compute_norm(
    const gko::matrix::Dense<ValueType>* b)
    auto exec = b->get_executor();
    auto b norm =
       gko::initialize<gko::matrix::Dense<gko::remove_complex<ValueType>>(
            {0.0}, exec);
```

```
b->compute_norm2 (b_norm);
    return get_first_element(b_norm.get());
template <typename ValueType>
void write()const
        std::cout « "Recurrent vs true vs implicit residual norm:"
                 « std::endl;
       std::cout « '|' « std::setw(10) « "Iteration" « '|' « std::setw(25)
                 "Recurrent Residual Norm" « '|' « std::setw(25)
"True Residual Norm" « '|' « std::setw(25)
"Implicit Residual Norm" « '|' « std::endl;
        std::cout « ' | ' « std::setfill('-') « std::setw(11) « '
                 std::cout « std::scientific;
       for (std::size_t i = 0; i < iterations.size(); i++) {
    std::cout «'|' « std::setw(10) « iterations[i] « '|'</pre>
                     std::cout.unsetf(std::ios_base::floatfield);
       using gko_dense = gko::matrix::Dense<ValueType>;
    using gko_real_dense = gko::matrix::Dense<RealValueType>;
    void on_iteration_complete(const gko::LinOp* solver, const gko::LinOp* b,
                              const gko::LinOp* solution,
                              const gko::size_type& iteration,
                              const gko::LinOp* residual,
                              const gko::LinOp* residual_norm,
                              const gko::LinOp* implicit_sq_residual_norm,
                              const gko::array<gko::stopping_status>*,
                              bool)const override
       if (residual_norm) {
           recurrent_norms.push_back(get_first_element(dense_norm));
        } else {
           auto dense_residual = gko::as<gko_dense>(residual);
           auto norm = compute_norm(dense_residual);
           recurrent_norms.push_back(norm);
        if (solution) {
           auto matrix = gko::as<gko::solver::detail::SolverBaseLinOp>(solver)
                             ->get_system_matrix();
           auto exec = matrix->get_executor();
           auto one = gko::initialize<gko_dense>({1.0}, exec);
           auto neg_one = gko::initialize<gko_dense>({-1.0}, exec);
           auto res = gko::as<gko_dense>(gko::clone(b));
           matrix->apply(one, solution, neg_one, res);
           real_norms.push_back(compute_norm(res.get()));
           real_norms.push_back(-1.0);
        if (implicit_sq_residual_norm) {
           auto dense norm =
               gko::as<gko_real_dense>(implicit_sq_residual_norm);
           implicit_norms.push_back(std::sqrt(get_first_element(dense_norm)));
        } else {
           implicit_norms.push_back(-1.0);
       iterations.push back(iteration);
    ResidualLogger()
       : gko::log::Logger(gko::log::Logger::iteration_complete_mask)
    { }
private:
   mutable std::vector<RealValueType> recurrent_norms{};
    mutable std::vector<RealValueType> real_norms{};
    mutable std::vector<RealValueType> implicit_norms{};
    mutable std::vector<std::size_t> iterations{};
int main(int argc, char* argv[])
    using ValueType = double;
    using RealValueType = gko::remove_complex<ValueType>;
    using IndexType = int;
    using vec = gko::matrix::Dense<ValueType>;
    using real_vec = gko::matrix::Dense<RealValueType>;
    using mtx = gko::matrix::Csr<ValueType, IndexType>;
    using cg = gko::solver::Cg<ValueType>;
```

```
std::cout « gko::version_info::get() « std::endl;
if (argc == 2 && (std::string(argv[1]) == "--help")) {
    std::cerr « "Usage: " « argv[0] « " [executor]" « std::endl;
     std::exit(-1);
const auto executor_string = argc >= 2 ? argv[1] : "reference";
std::map<std::string, std::function<std::shared_ptr<gko::Executor>()»
     exec_map{
          {"omp",
                   [] { return gko::OmpExecutor::create(); }},
          {"cuda",
           [] {
                return gko::CudaExecutor::create(0,
                                                         gko::OmpExecutor::create());
           } } ,
          {"hip",
                return gko::HipExecutor::create(0, gko::OmpExecutor::create());
          {"dpcpp",
           [] {
                return gko::DpcppExecutor::create(0,
                                                           gko::OmpExecutor::create());
}},
{"reference", [] { return gko::ReferenceExecutor::create(); }};
const auto exec = exec_map.at(executor_string)(); // throws if not valid
auto A = share(gko::read<mtx>(std::ifstream("data/A.mtx"), exec));
auto b = gko::read<vec>(std::ifstream("data/b.mtx"), exec);
auto x = gko::read<vec>(std::ifstream("data/x0.mtx"), exec);
const RealValueType reduction_factor = 1e-7;
auto solver_gen =
     cg::build()
          .with_criteria(gko::stop::Iteration::build().with_max_iters(20u),
                            gko::stop::ResidualNorm<ValueType>::build()
                                  . \verb|with_reduction_factor(reduction_factor)||\\
          .on(exec);
auto logger = std::make_shared<ResidualLogger<ValueType»();</pre>
solver_gen->add_logger(logger);
auto solver = solver_gen->generate(A);
solver->apply(b, x);
std::cout « "Solution (x):\n";
write(std::cout, x);
logger->write();
auto one = gko::initialize<vec>({1.0}, exec);
auto neg_one = gko::initialize<vec>({-1.0}, exec);
auto res = gko::initialize<real_vec>({0.0}, exec);
A->apply(one, x, neg_one, b);
b->compute_norm2(res);
std::cout « "Residual norm sqrt(r^T r):\n";
write(std::cout, res);
```

# The custom-matrix-format program

The custom matrix format example..

This example depends on simple-solver, poisson-solver, three-pt-stencil-solver, .

### Introduction

This example solves a 1D Poisson equation:

$$\begin{aligned} u:[0,1] &\to R \\ u'' &= f \\ u(0) &= u0 \\ u(1) &= u1 \end{aligned}$$

using a finite difference method on an equidistant grid with K discretization points (K can be controlled with a command line parameter). The discretization is done via the second order Taylor polynomial:

For an equidistant grid with K "inner" discretization points x1,...,xk,and step size h=1/(K+1), the formula produces a system of linear equations

$$2u_1 - u_2 = -f_1h^2 + u0$$
  
-  $u(k-1) + 2u_k - u(k+1) = -f_kh^2, k = 2, ..., K-1$   
-  $u(K-1) + 2u_K = -f_Kh^2 + u1$ 

which is then solved using Ginkgo's implementation of the CG method preconditioned with block-Jacobi. It is also possible to specify on which executor Ginkgo will solve the system via the command line. The function 'f'is set to 'f(x) = 6x' (making the solution ' $u(x) = x^3$ '), but that can be changed in the main function.

The intention of this example is to show how a custom linear operator can be created and integrated into Ginkgo to achieve performance benefits.

### About the example

### The commented program

This constructor will be called by the create method. Here we initialize the coefficients of the stencil.

Here we implement the application of the linear operator, x = A \* b. apply\_impl will be called by the apply method, after the arguments have been moved to the correct executor and the operators checked for conforming sizes.

For simplicity, we assume that there is always only one right hand side and the stride of consecutive elements in the vectors is 1 (both of these are always true in this example).

```
void apply_impl(const gko::LinOp* b, gko::LinOp* x)const override {
```

we only implement the operator for dense RHS. gko::as will throw an exception if its argument is not Dense.

```
auto dense_b = gko::as<vec>(b);
auto dense_x = gko::as<vec>(x);
```

we need separate implementations depending on the executor, so we create an operation which maps the call to the correct implementation

### OpenMP implementation

```
void run(std::shared_ptr<const gko::OmpExecutor>)const override
{
    auto b_values = b->get_const_values();
    auto x_values = x->get_values();

#pragma omp parallel for
    for (std::size_t i = 0; i < x->get_size()[0]; ++i) {
        auto coefs = coefficients.get_const_data();
        auto result = coefs[1] * b_values[i];
        if (i > 0) {
            result += coefs[0] * b_values[i - 1];
        }
        if (i < x->get_size()[0] - 1) {
            result += coefs[2] * b_values[i + 1];
        }
        x_values[i] = result;
    }
}
```

### **CUDA** implementation

}

We do not provide an implementation for reference executor. If not provided, Ginkgo will use the implementation for the OpenMP executor when calling it in the reference executor.

```
const coef_type& coefficients;
const vec* b;
vec* x;
};
this->get_executor()->run(
stencil_operation(coefficients, dense_b, dense_x));
```

There is also a version of the apply function which does the operation x = alpha \* A \* b + beta \* x. This function is commonly used and can often be better optimized than implementing it using x = A \* b. However, for simplicity, we will implement it exactly like that in this example.

Creates a stencil matrix in CSR format for the given number of discretization points.

### Generates the RHS vector given f and the boundary conditions.

### Prints the solution u.

Computes the 1-norm of the error given the computed u and the correct solution function correct\_u.

```
return error;
int main(int argc, char* argv[])
Some shortcuts
using ValueType = double;
using RealValueType = gko::remove_complex<ValueType>;
using IndexType = gko::remove_comprex<valueType
using IndexType = int;
using vec = gko::matrix::Dense<ValueType>;
using mtx = gko::matrix::Csr<ValueType, IndexType>;
using cg = gko::solver::Cg<ValueType>;
Figure out where to run the code
if (argc == 2 && (std::string(argv[1]) == "--help")) {
   std::cerr « "Usage: " « argv[0] « " [executor]" « std::endl;
     std::exit(-1);
const auto executor_string = argc >= 2 ? argv[1] : "reference";
const unsigned int discretization_points =
    argc >= 3 ? std::atoi(argv[2]) : 100u;
std::map<std::string, std::function<std::shared_ptr<gko::Executor>()>
     exec_map{
         {"omp", [] { return gko::OmpExecutor::create(); }},
          {"cuda",
          [] {
               return gko::CudaExecutor::create(0,
                                                      gko::OmpExecutor::create());
         }},
{"hip",
          [] {
              return gko::HipExecutor::create(0, gko::OmpExecutor::create());
          { "dpcpp",
          [] {
               return gko::DpcppExecutor::create(0,
                                                       gko::OmpExecutor::create());
          {"reference", [] { return gko::ReferenceExecutor::create(); }}};
executor where Ginkgo will perform the computation
const auto exec = exec_map.at(executor_string)(); // throws if not valid
executor used by the application
const auto app_exec = exec->get_master();
problem:
auto correct_u = [](ValueType x) { return x * x * x; };
auto f = [](ValueType x) { return ValueType{6} * x; };
auto u0 = correct_u(0);
auto u1 = correct_u(1);
initialize vectors
auto rhs = vec::create(app_exec, gko::dim<2>(discretization_points, 1));
generate_rhs(f, u0, u1, rhs.get());
auto u = vec::create(app_exec, gko::dim<2>(discretization_points, 1));
for (int i = 0; i < u->get_size()[0]; ++i) {
    u->get_values()[i] = 0.0;
const RealValueType reduction_factor{1e-7};
Generate solver and solve the system
cg::build()
     .with criteria(
         gko::stop::Iteration::build().with_max_iters(discretization_points),
         gko::stop::ResidualNorm<ValueType>::build().with_reduction_factor(
              reduction_factor))
     .on(exec)
notice how our custom StencilMatrix can be used in the same way as any built-in type
         ->generate(StencilMatrix<ValueType>::create(exec, discretization_points,
         ->apply(rhs, u);
     std::cout « "\nSolve complete."
« "\nThe average relative error is "
                « calculate_error(discretization_points, u.get(), correct_u) /
                        discretization_points
                « std::endl;
}
```

### Results

### Comments about programming and debugging

```
#include <map>
 #include <string>
 #include <omp.h>
#include <ginkgo/ginkgo.hpp>
template <typename ValueType>
void stencil_kernel(std::size_t size, const ValueType* coefs,
                                         const ValueType* b, ValueType* x);
template <typename ValueType>
\verb|class StencilMatrix|: public gko::EnableLinOp < StencilMatrix < ValueType >>, the public gko::Enable < StencilMatrix < ValueType >>, the 
                                            public gko::EnableCreateMethod<StencilMatrix<ValueType» {</pre>
public:
        StencilMatrix(std::shared_ptr<const gko::Executor> exec,
                                    gko::size_type size = 0, ValueType left = -1.0,
ValueType center = 2.0, ValueType right = -1.0)
                 : gko::EnableLinOp<StencilMatrix>(exec, gko::dim<2>{size}),
                    coefficients(exec, {left, center, right})
        {}
protected:
        using vec = gko::matrix::Dense<ValueType>;
        using coef_type = gko::array<ValueType>
        void apply_impl(const gko::LinOp* b, gko::LinOp* x)const override
                auto dense_b = gko::as<vec>(b);
auto dense_x = gko::as<vec>(x);
                struct stencil_operation: gko::Operation {
    stencil_operation(const coef_type& coefficients, const vec* b,
                                                             vec* x)
                                 : coefficients{coefficients}, b{b}, x{x}
                        {}
                        void run(std::shared_ptr<const gko::OmpExecutor>)const override
                                auto b_values = b->get_const_values();
                                auto x_values = x->get_values();
 #pragma omp parallel for
                                for (std::size t i = 0; i < x->get size()[0]; ++i) {
                                         auto coefs = coefficients.get_const_data();
                                         auto result = coefs[1] * b_values[i];
                                         if (i > 0) {
                                                 result += coefs[0] * b_values[i - 1];
                                         if (i < x->get_size()[0] - 1) {
                                                 result += coefs[2] * b_values[i + 1];
                                         x_values[i] = result;
                         void run(std::shared_ptr<const qko::CudaExecutor>)const override
                                stencil_kernel(x->get_size()[0], coefficients.get_const_data(),
                                                               b->get_const_values(), x->get_values());
                         const coef_type& coefficients;
                        const vec* b;
                         vec* x;
                this->get_executor()->run(
                        stencil_operation(coefficients, dense_b, dense_x));
        {
                auto dense_b = gko::as<vec>(b);
                auto dense_x = gko::as<vec>(x);
                 auto tmp_x = dense_x->clone();
                this->apply_impl(b, tmp_x.get());
                dense_x->scale(beta);
                dense_x->add_scaled(alpha, tmp_x);
private:
        coef_type coefficients;
template <typename ValueType, typename IndexType>
void generate_stencil_matrix(gko::matrix::Csr<ValueType, IndexType>* matrix)
        const auto discretization_points = matrix->get_size()[0];
```

```
auto row_ptrs = matrix->get_row_ptrs();
     auto col_idxs = matrix->get_col_idxs();
     auto values = matrix->get_values();
     IndexType pos = 0;
     const ValueType coefs[] = \{-1, 2, -1\};
     row_ptrs[0] = pos;
for (int i = 0; i < discretization_points; ++i) {</pre>
          for (auto ofs: {-1, 0, 1}) {
   if (0 <= i + ofs && i + ofs < discretization_points) {
      values[pos] = coefs[ofs + 1];
      col_idxs[pos] = i + ofs;</pre>
                    ++pos;
          row_ptrs[i + 1] = pos;
     }
template <typename Closure, typename ValueType>
void generate_rhs(Closure f, ValueType u0, ValueType u1,
                      gko::matrix::Dense<ValueType>* rhs)
     const auto discretization_points = rhs->get_size()[0];
     auto values = rhs->get_values();
const ValueType h = 1.0 / (discretization_points + 1);
for (int i = 0; i < discretization_points; ++i) {</pre>
          const ValueType xi = ValueType(i + 1) * h;
          values[i] = -f(xi) * h * h;
     values[0] += u0;
     values[discretization_points - 1] += u1;
template <typename ValueType>
void print_solution(ValueType u0, ValueType u1,
                         const gko::matrix::Dense<ValueType>* u)
     std::cout « u0 « '\n';
for (int i = 0; i < u->get_size()[0]; ++i) {
    std::cout « u->get_const_values()[i] « '\n';
     std::cout « u1 « std::endl;
template <typename Closure, typename ValueType>
double calculate_error(int discretization_points,
                             const gko::matrix::Dense<ValueType>* u,
                             Closure correct u)
     const auto h = 1.0 / (discretization_points + 1);
     auto error = 0.0;
for (int i = 0; i < discretization_points; ++i) {</pre>
         using std::abs;
          const auto xi = (i + 1) * h;
          error +=
              abs(u->get_const_values()[i] - correct_u(xi)) / abs(correct_u(xi));
     return error:
int main(int argc, char* argv[])
     using ValueType = double;
     using RealValueType = gko::remove_complex<ValueType>;
     using IndexType = int;
using vec = gko::matrix::Dense<ValueType>;
     using mtx = gko::matrix::Csr<ValueType, IndexType>;
     using cg = gko::solver::Cg<ValueType>;
     if (argc == 2 && (std::string(argv[1]) == "--help")) {
    std::cerr « "Usage: " « argv[0] « " [executor]" « std::endl;
          std::exit(-1);
     const auto executor_string = argc >= 2 ? argv[1] : "reference";
     const unsigned int discretization_points =
          argc >= 3 ? std::atoi(argv[2]) : 100u;
     std::map<std::string, std::function<std::shared_ptr<gko::Executor>()»
          exec_map{
               {"omp", [] { return gko::OmpExecutor::create(); }},
               {"cuda",
                [] {
                     return gko::CudaExecutor::create(0,
                                                              gko::OmpExecutor::create());
                } } ,
               {"hip".
                     return gko::HipExecutor::create(0, gko::OmpExecutor::create());
               {"dpcpp",
                [] {
                     return gko::DpcppExecutor::create(0,
                                                                gko::OmpExecutor::create());
```

```
} } ,
                {"reference", [] { return gko::ReferenceExecutor::create(); }};
     const auto exec = exec_map.at(executor_string)(); // throws if not valid
    const auto app_exec = exec_>get_master();
auto correct_u = [](ValueType x) { return x * x * x; };
auto f = [](ValueType x) { return ValueType{6} * x; };
auto u0 = correct_u(0);
     auto u1 = correct_u(1);
     auto rhs = vec::create(app_exec, gko::dim<2>(discretization_points, 1));
    generate_rhs(f, u0, u1, rhs.get());
auto u = vec::create(app_exec, gko::dim<2>(discretization_points, 1));
for (int i = 0; i < u->get_size()[0]; ++i) {
    u->get_values()[i] = 0.0;
}
     const RealValueType reduction_factor{1e-7};
     cg::build()
          .with_criteria(
               gko::stop::Iteration::build().with_max_iters(discretization_points),
gko::stop::ResidualNorm<ValueType>::build().with_reduction_factor(
                     reduction_factor))
          .on(exec)
          \verb|->generate(StencilMatrix<ValueType>::create(exec, discretization\_points,
                                                                     -1, 2, -1))
     « calculate_error(discretization_points, u.get(), correct_u) /
                           discretization_points
                  « std::endl;
}
```

# The custom-stopping-criterion program

The custom stopping criterion creation example..

This example depends on simple-solver, minimal-cuda-solver.

### Introduction

### About the example

## The commented program

```
GKO_ENABLE_CRITERION_FACTORY(ByInteraction, parameters, Factory);
    GKO_ENABLE_BUILD_METHOD (Factory);
    bool check_impl(gko::uint8 stoppingId, bool setFinalized,
                    gko::array<gko::stopping_status>* stop_status,
                     bool* one_changed, const Criterion::Updater&)override
        bool result = *(parameters_.stop_iteration_process);
        if (result) {
            this->set_all_statuses(stoppingId, setFinalized, stop_status);
            *one_changed = true;
        return result;
    explicit ByInteraction(std::shared_ptr<const gko::Executor> exec)
        : EnablePolymorphicObject<ByInteraction, Criterion>(std::move(exec))
    explicit ByInteraction(const Factory* factory,
        const gko::stop::CriterionArgs& args)
: EnablePolymorphicObject<ByInteraction, Criterion>(
              factory->get_executor()),
          parameters_{factory->get_parameters()}
    { }
void run_solver(volatile bool* stop_iteration_process,
                std::shared_ptr<gko::Executor> exec)
Some shortcuts
using ValueType = double;
using RealValueType = gko::remove_complex<ValueType>;
using IndexType = int;
using mtx = gko::matrix::Csr<ValueType, IndexType>;
using vec = gko::matrix::Dense<ValueType>;
using real_vec = gko::matrix::Dense<RealValueType>;
using bicg = gko::solver::Bicgstab<ValueType>;
```

### Read Data

```
auto A = share(gko::read<mtx>(std::ifstream("data/A.mtx"), exec));
auto b = gko::read<vec>(std::ifstream("data/b.mtx"), exec);
auto x = gko::read<vec>(std::ifstream("data/x0.mtx"), exec);
Create solver factory and solve system
    bicg::build()
        .with_criteria(ByInteraction::build().with_stop_iteration_process(
            stop_iteration_process))
         .on(exec)
         ->generate(A);
solver->add_logger(gko::log::Stream<ValueType>::create(
    gko::log::Logger::iteration_complete_mask, std::cout, true));
solver->apply(b, x);
std::cout « "Solver stopped" « std::endl;
Print solution
std::cout « "Solution (x): \n";
write(std::cout, x);
Calculate residual
    auto one = gko::initialize<vec>({1.0}, exec);
    auto neg_one = gko::initialize<vec>({-1.0}, exec);
    auto res = gko::initialize<real_vec>({0.0}, exec);
    A->apply(one, x, neg_one, b);
b->compute_norm2(res);
std::cout « "Residual norm sqrt(r^T r): \n";
    write(std::cout, res);
int main(int argc, char* argv[])
Print version information
std::cout « gko::version_info::get() « std::endl;
Figure out where to run the code
   (argc == 2 && (std::string(argv[1]) == "--help")) {
  std::cerr « "Usage: " « argv[0] « " [executor]" « std::endl;
    std::exit(-1);
Figure out where to run the code
const auto executor_string = argc >= 2 ? argv[1] : "reference";
Figure out where to run the code
std::map<std::string, std::function<std::shared_ptr<gko::Executor>()»
    exec_map{
         {"omp", [] { return gko::OmpExecutor::create(); }},
         {"cuda",
          [] {
              return gko::CudaExecutor::create(0,
                                                 gko::OmpExecutor::create());
         {"hip",
              return gko::HipExecutor::create(0, gko::OmpExecutor::create());
          }},
         { "dpcpp",
          [] {
             return gko::DpcppExecutor::create(0,
                                                  gko::OmpExecutor::create());
         {"reference", [] { return gko::ReferenceExecutor::create(); }};
executor where Ginkgo will perform the computation
const auto exec = exec_map.at(executor_string)(); // throws if not valid
Declare a user controlled boolean for the iteration process
volatile bool stop_iteration_process{};
Create a new a thread to launch the solver
std::thread t(run_solver, &stop_iteration_process, exec);
Look for an input command "stop" in the console, which sets the boolean to true
    std::cout « "Type 'stop' to stop the iteration process" « std::endl;
```

std::string command;
while (std::cin » command) {

### Results

```
This is the expected output:
```

```
[LOG] >> iteration 22516 completed with solver LinOp[gko::solver::Bicgstab<double>,0x7fe6a4003710] with
      residual LinOp[gko::matrix::Dense<double>,0x7fe6a40048e0] and residual_norm LinOp[gko::LinOp const*,0]
LinOp[gko::matrix::Dense<double>,0x7fe6a40050b0][
    5.17803e-164
    -7.6865e-165
    -2.06149e-164
    -4.84737e-165
    -3.36597e-164
    2.22353e-164
    1.47594e-165
    -1.78592e-165
    -6.17274e-166
    -3.02681e-166
    7.82009e-166
    8.57102e-165
     -1.28879e-164
    -2.62076e-165
    2.55329e-165
    -5.95988e-166
    -5.79273e-166
    -5.20172e-166
    -6.79458e-166
// Typing 'stop' stops the solver.
User input command 'stop' - The solver will stop
LinOp[gko::matrix::Dense<double>,0x7fe6a40048e0][
    0.252218
    0.108645
    0.0662811
    0.0630433
    0.0384088
    0.0396536
    0.0402648
    0.0338935
    0.0193098
    0.0234653
    0.0211499
    0.0196413
    0.0199151
    0.0181674
    0.0162722
    0.0150714
    0.0107016
    0.0121141
    0.0123025
Solution (x):
%%MatrixMarket matrix array real general
19 1
0.252218
0.108645
0.0662811
0.0630433
0.0384088
0.0396536
0.0402648
0.0338935
```

0.0193098

```
0.0234653

0.0211499

0.0196413

0.0199151

0.0181674

0.0162722

0.0150714

0.0107016

0.0121141

0.0123025

Residual norm sqrt(r^T r):

%%MatrixMarket matrix array real general

1 1

6.50306e-16
```

### Comments about programming and debugging

```
#include <fstream>
#include <iostream>
#include <map>
#include <string>
#include <thread>
#include <ginkgo/ginkgo.hpp>
class ByInteraction
    : public gko::EnablePolymorphicObject<ByInteraction, gko::stop::Criterion> {
friend class gko::EnablePolymorphicObject<ByInteraction,</pre>
                                                 gko::stop::Criterion>;
    using Criterion = gko::stop::Criterion;
public:
    GKO_CREATE_FACTORY_PARAMETERS(parameters, Factory)
    {
        std::add_pointer<volatile bool>::type GKO_FACTORY_PARAMETER_SCALAR(
            stop_iteration_process, nullptr);
    };
    GKO_ENABLE_CRITERION_FACTORY(ByInteraction, parameters, Factory);
    GKO_ENABLE_BUILD_METHOD (Factory);
protected:
    bool check_impl(gko::uint8 stoppingId, bool setFinalized,
                     gko::array<gko::stopping_status>* stop_status,
bool* one_changed, const Criterion::Updater&)override
{
        bool result = *(parameters_.stop_iteration_process);
        if (result) {
             this->set_all_statuses(stoppingId, setFinalized, stop_status);
             *one_changed = true;
        return result;
    explicit ByInteraction(std::shared_ptr<const gko::Executor> exec)
        : EnablePolymorphicObject<ByInteraction, Criterion>(std::move(exec))
    { }
    : EnablePolymorphicObject<ByInteraction, Criterion>(
               factory->get_executor()),
          parameters_{factory->get_parameters()}
    { }
};
void run_solver(volatile bool* stop_iteration_process,
                 std::shared_ptr<gko::Executor> exec)
    using ValueType = double;
    using RealValueType = gko::remove_complex<ValueType>;
    using IndexType = int;
    using mtx = gko::matrix::Csr<ValueType, IndexType>;
    using vec = gko::matrix::Dense<ValueType>;
    using real_vec = gko::matrix::Dense<RealValueType>;
    using bicg = gko::solver::Bicgstab<ValueType>;
auto A = share(gko::read<mtx>(std::ifstream("data/A.mtx"), exec));
    auto b = gko::read<vec>(std::ifstream("data/b.mtx"), exec);
    auto x = gko::read<vec>(std::ifstream("data/x0.mtx"), exec);
        bicg::build()
            .with_criteria(ByInteraction::build().with_stop_iteration_process(
                 stop_iteration_process))
             .on(exec)
             ->generate(A);
    solver->add_logger(gko::log::Stream<ValueType>::create(
        gko::log::Logger::iteration_complete_mask, std::cout, true));
```

```
solver->apply(b, x);
std::cout « "Solver stopped" « std::endl;
std::cout « "Solution (x): \n";
    write(std::cout, x);
    auto one = gko::initialize<vec>({1.0}, exec);
auto neg_one = gko::initialize<vec>({-1.0}, exec);
    auto res = gko::initialize<real_vec>({0.0}, exec);
    A->apply(one, x, neg_one, b);
    b->compute_norm2(res);
    std::cout « "Residual norm sqrt(r^T r): \n";
    write(std::cout, res);
int main(int argc, char* argv[])
    std::cout « gko::version_info::get() « std::endl;
    if (argc == 2 && (std::string(argv[1]) == "--help")) {
    std::cerr « "Usage: " « argv[0] « " [executor]" « std::endl;
         std::exit(-1);
    const auto executor_string = argc >= 2 ? argv[1] : "reference";
    std::map<std::string, std::function<std::shared_ptr<gko::Executor>()>
         exec_map{
              {"omp", [] { return gko::OmpExecutor::create(); }},
              {"cuda",
               [] {
                   return gko::CudaExecutor::create(0,
                                                          gko::OmpExecutor::create());
              {"hip",
               [] {
                   return gko::HipExecutor::create(0, gko::OmpExecutor::create());
              {"dpcpp",
               [] {
                   return gko::DpcppExecutor::create(0,
                                                            gko::OmpExecutor::create());
              }},
{"reference", [] { return gko::ReferenceExecutor::create(); }}};
    const auto exec = exec_map.at(executor_string)(); // throws if not valid
    volatile bool stop_iteration_process{};
    std::thread t(run_solver, &stop_iteration_process, exec);
std::cout « "Type 'stop' to stop the iteration process" « std::endl;
    std::string command;
    while (std::cin » command) {
   if (command == "stop") {
              break;
         } else {
             std::cout « "Unknown command" « std::endl;
    std::cout « "User input command 'stop' - The solver will stop!"
                « std::endl;
    stop_iteration_process = true;
    t.join();
```

# The distributed-solver program

The distributed solver example..

This example depends on simple-solver, three-pt-stencil-solver.

### Introduction

This distributed solver example should help you understand the basics of using Ginkgo in a distributed setting. The example will solve a simple 1D Laplace equation where the system can be distributed row-wise to multiple processes. To run the solver with multiple processes, use mpirun -n NUM\_PROCS ./distributed-solver [executor] [num\_grid\_points] [num\_iterations].

If you are using GPU devices, please make sure that you run this example with at most as many processes as you have GPU devices available.

## The commented program

As vector type we use the following, which implements a subset of gko::matrix::Dense. using dist\_vec = gko::experimental::distributed::Vector<ValueType>;

As matrix type we simply use the following type, which can read distributed data and be applied to a distributed vector.

We still need a localized vector type to be used as scalars in the advanced apply operations.

using vec = gko::matrix::Dense<ValueType>;

The partition type describes how the rows of the matrices are distributed.

We can use here the same solver type as you would use in a non-distributed program. Please note that not all solvers support distributed systems at the moment.

```
using solver = gko::solver::Cg<ValueType>;
using schwarz = gko::experimental::distributed::preconditioner::Schwarz<
    ValueType, LocalIndexType, GlobalIndexType>;
using bj = gko::preconditioner::JacobicValueType, LocalIndexType>;
```

Create an MPI communicator get the rank of the calling process.

```
const auto comm = gko::experimental::mpi::communicator(MPI_COMM_WORLD);
const auto rank = comm.rank();
```

### **User Input Handling**

User input settings:

- · The executor, defaults to reference.
- The number of grid points, defaults to 100.
- The number of iterations, defaults to 1000.

```
if (argc == 2 && (std::string(argv[1]) == "--help")) {
    if (rank == 0) {
        std::cerr « "Usage: " « argv[0]
                   « " [executor] [num_grid_points] [num_iterations] "
                   « std::endl;
    std::exit(-1);
ValueType t_init = gko::experimental::mpi::get_walltime();
const auto executor_string = argc >= 2 ? argv[1] : "reference";
const auto grid dim =
    static_cast<gko::size_type>(argc >= 3 ? std::atoi(argv[2]) : 100);
const auto num iters =
    static cast<qko::size type>(argc >= 4 ? std::atoi(argv[3]) : 1000);
const std::map<std::string,
                std::function<std::shared_ptr<gko::Executor>(MPI_Comm)»
    executor_factory_mpi{
        {"reference".
        [](MPI_Comm) { return gko::ReferenceExecutor::create(); }}, {"omp", [](MPI_Comm) { return gko::OmpExecutor::create(); }}, {"cuda",
          [](MPI_Comm comm) {
              int device_id = gko::experimental::mpi::map_rank_to_device_id(
                  comm, gko::CudaExecutor::get_num_devices());
              return gko::CudaExecutor::create(
                  device id, gko::ReferenceExecutor::create());
         }},
         {"hip",
          [](MPI_Comm comm) {
              int device_id = gko::experimental::mpi::map_rank_to_device_id(
              comm, gko::HipExecutor::get_num_devices());
return gko::HipExecutor::create(
                  device id, gko::ReferenceExecutor::create());
         {"dpcpp", [](MPI_Comm comm) {
              int device_id = 0;
              if (gko::DpcppExecutor::get_num_devices("gpu")) {
                  device_id = gko::experimental::mpi::map_rank_to_device_id(
    comm, gko::DpcppExecutor::get_num_devices("gpu"));
              } else if (gko::DpcppExecutor::get_num_devices("cpu")) {
                  device_id = gko::experimental::mpi::map_rank_to_device_id(
                       comm, gko::DpcppExecutor::get_num_devices("cpu"));
              } else {
                  throw std::runtime error("No suitable DPC++ devices");
              return gko::DpcppExecutor::create(
                  device_id, gko::ReferenceExecutor::create());
auto exec = executor_factory_mpi.at(executor_string)(MPI_COMM_WORLD);
```

### **Creating the Distributed Matrix and Vectors**

As a first step, we create a partition of the rows. The partition consists of ranges of consecutive rows which are assigned a part-id. These part-ids will be used for the distributed data structures to determine which rows will be stored locally. In this example each rank has (nearly) the same number of rows, so we can use the following specialized constructor. See gko::distributed::Partition for other modes of creating a partition.

```
const auto num_rows = grid_dim;
auto partition = gko::share(part_type::build_from_global_size_uniform(
    exec->get_master(), comm.size(),
    static_cast<GlobalIndexType>(num_rows)));
```

Assemble the matrix using a 3-pt stencil and fill the right-hand-side with a sine value. The distributed matrix supports only constructing an empty matrix of zero size and filling in the values with gko::experimental::distributed::Matrix::read\_distributed.

Only the data that belongs to the rows by this rank will be assembled.

gko::matrix\_data<ValueType, GlobalIndexType> A\_data;

```
gko::matrix_data<ValueType, GlobalIndexType> b_data;
gko::matrix_data<ValueType, GlobalIndexType> x_data;
A_data.size = {num_rows, num_rows};
b_data.size = {num_rows, 1};
x_data.size = {num_rows, 1};
const auto range_start = partition->get_range_bounds()[rank];
const auto range_end = partition->get_range_bounds()[rank + 1];
for (int i = range_start; i < range_end; i++) {</pre>
    if (i > 0) {
        A_data.nonzeros.emplace_back(i, i - 1, -1);
    A_data.nonzeros.emplace_back(i, i, 2);
    if (i < grid_dim - 1) {</pre>
        A_data.nonzeros.emplace_back(i, i + 1, -1);
    b\_data.nonzeros.emplace\_back(i, 0, std::sin(i * 0.01));\\
    x_data.nonzeros.emplace_back(i, 0, gko::zero<ValueType>());
}
Take timings.
comm.synchronize();
```

ValueType t\_init\_end = gko::experimental::mpi::get\_walltime();

Read the matrix data, currently this is only supported on CPU executors. This will also set up the communication pattern needed for the distributed matrix-vector multiplication.

```
auto A_host = gko::share(dist_mtx::create(exec->get_master(), comm));
auto x_host = dist_vec::create(exec->get_master(), comm);
auto b_host = dist_vec::create(exec->get_master(), comm);
A_host->read_distributed(A_data, partition);
b_host->read_distributed(b_data, partition);
x_host->read_distributed(x_data, partition);
```

After reading, the matrix and vector can be moved to the chosen executor, since the distributed matrix supports SpMV also on devices.

```
auto A = gko::share(dist_mtx::create(exec, comm));
auto x = dist_vec::create(exec, comm);
auto b = dist_vec::create(exec, comm);
A->copy_from(A_host);
b->copy_from(b_host);
x->copy_from(x_host);
Take timings.
comm.synchronize();
ValueType t_read_setup_end = gko::experimental::mpi::get_walltime();
```

### Solve the Distributed System

Generate the solver, this is the same as in the non-distributed case. with a local block diagonal preconditioner.

```
Setup the local block diagonal solver factory.
```

```
auto local_solver = gko::share(bj::build().on(exec));
```

### Setup the stopping criterion and logger

Add logger to the generated solver to log the iteration count and residual norm

```
Ainv->add_logger(logger);
```

### Take timings.

```
comm.synchronize();
ValueType t_solver_generate_end = gko::experimental::mpi::get_walltime();
```

Apply the distributed solver, this is the same as in the non-distributed case.

```
Ainv->apply(b, x);
```

### Take timings.

```
comm.synchronize();
ValueType t_end = gko::experimental::mpi::get_walltime();
```

### Get the residual.

### **Printing Results**

Print the achieved residual norm and timings on rank 0.

### Results

```
This is the expected output for mpirun -n 4 ./distributed-solver:
```

```
Num rows in matrix: 100

Num ranks: 4

Final Res norm: 5.58392e-12

Iteration count: 7

Init time: 0.0663887

Read time: 0.0729806

Solver generate time: 7.6348e-05

Solver apply time: 0.0680783

Total time: 0.141351
```

The timings may vary depending on the machine.

```
#include <ginkgo/ginkgo.hpp>
#include <iostream>
#include <map>
#include <string>
int main(int argc, char* argv[])
    const gko::experimental::mpi::environment env(argc, argv);
    using GlobalIndexType = gko::int64;
using LocalIndexType = gko::int32;
    using ValueType = double;
    using dist_vec = gko::experimental::distributed::Vector<ValueType>;
    using dist_mtx =
        gko::experimental::distributed::Matrix<ValueType, LocalIndexType,</pre>
                                                GlobalIndexTvpe>:
    using vec = gko::matrix::Dense<ValueType>;
    using part_type =
        gko::experimental::distributed::Partition<LocalIndexType,</pre>
                                                    GlobalIndexType>;
    using solver = gko::solver::Cg<ValueType>;
    using schwarz = gko::experimental::distributed::preconditioner::Schwarz<
        ValueType, LocalIndexType, GlobalIndexType>;
    using bj = gko::preconditioner::Jacobi<ValueType, LocalIndexType>;
    const auto comm = gko::experimental::mpi::communicator(MPI_COMM_WORLD);
const auto rank = comm.rank();
    if (argc == 2 && (std::string(argv[1]) == "--help")) {
   if (rank == 0) {
            « std::endl;
        std::exit(-1);
    ValueType t_init = gko::experimental::mpi::get_walltime();
    const auto executor_string = argc >= 2 ? argv[1] : "reference";
```

```
const auto grid_dim =
   static_cast<gko::size_type>(argc >= 3 ? std::atoi(argv[2]) : 100);
const auto num_iters =
   static_cast<gko::size_type>(argc >= 4 ? std::atoi(argv[3]) : 1000);
const std::map<std::string,
               std::function<std::shared ptr<qko::Executor>(MPI Comm)»
    executor_factory_mpi{
        {"reference",
         [](MPI_Comm) { return gko::ReferenceExecutor::create(); }},
        {"omp", [] (MPI_Comm) { return gko::OmpExecutor::create(); }},
{"cuda",
         [] (MPI Comm comm) {
             int device_id = gko::experimental::mpi::map_rank_to_device_id(
                 comm, gko::CudaExecutor::get_num_devices());
             return gko::CudaExecutor::create(
                 device_id, gko::ReferenceExecutor::create());
         }},
        {"hip",
         [] (MPI_Comm comm) {
             int device_id = gko::experimental::mpi::map_rank_to_device_id(
                 comm, gko::HipExecutor::get_num_devices());
             return gko::HipExecutor::create(
                 device_id, gko::ReferenceExecutor::create());
        {"dpcpp", [](MPI_Comm comm) {
             int device_id = 0;
             if (gko::DpcppExecutor::get_num_devices("gpu")) {
                 device_id = gko::experimental::mpi::map_rank_to_device_id(
             comm, gko::DpcppExecutor::get_num_devices("gpu"));
} else if (gko::DpcppExecutor::get_num_devices("cpu")) {
                 device_id = gko::experimental::mpi::map_rank_to_device_id(
                     comm, gko::DpcppExecutor::get_num_devices("cpu"));
                 throw std::runtime_error("No suitable DPC++ devices");
             return gko::DpcppExecutor::create(
                 device_id, gko::ReferenceExecutor::create());
auto exec = executor_factory_mpi.at(executor_string)(MPI_COMM_WORLD);
const auto num_rows = grid_dim;
auto partition = gko::share(part_type::build_from_global_size_uniform()
   exec->get_master(), comm.size(),
    static_cast<GlobalIndexType>(num_rows)));
gko::matrix_data<ValueType, GlobalIndexType> A_data;
gko::matrix_data<ValueType, GlobalIndexType> b_data;
gko::matrix_data<ValueType, GlobalIndexType> x_data;
A_data.size = {num_rows, num_rows};
b_data.size = {num_rows, 1};
x_data.size = {num_rows, 1};
const auto range_start = partition->get_range_bounds()[rank];
const auto range_end = partition->get_range_bounds()[rank + 1];
for (int i = range_start; i < range_end; i++) {</pre>
    if (i > 0) {
        A_data.nonzeros.emplace_back(i, i - 1, -1);
   A data.nonzeros.emplace back(i, i, 2);
    if (i < grid_dim - 1) {</pre>
        A_data.nonzeros.emplace_back(i, i + 1, -1);
   b\_data.nonzeros.emplace\_back(i, 0, std::sin(i * 0.01));\\
    x_data.nonzeros.emplace_back(i, 0, gko::zero<ValueType>());
comm.synchronize();
ValueType t_init_end = gko::experimental::mpi::get_walltime();
auto A_host = gko::share(dist_mtx::create(exec->get_master(), comm));
auto x_host = dist_vec::create(exec->get_master(), comm);
auto b_host = dist_vec::create(exec->get_master(), comm);
A_host->read_distributed(A_data, partition);
b_host->read_distributed(b_data, partition);
x_host->read_distributed(x_data, partition);
auto A = gko::share(dist_mtx::create(exec, comm));
auto x = dist_vec::create(exec, comm);
auto b = dist_vec::create(exec, comm);
A->copy_from(A_host);
b->copy_from(b_host);
x->copy_from(x_host);
comm.synchronize();
ValueType t_read_setup_end = gko::experimental::mpi::get_walltime();
auto local_solver = gko::share(bj::build().on(exec));
const gko::remove_complex<ValueType> reduction_factor{1e-8};
std::shared_ptr<const gko::log::Convergence<ValueType» logger =</pre>
   gko::log::Convergence<ValueType>::create();
auto Ainv = solver::build()
                .with_preconditioner(
                    schwarz::build().with_local_solver(local_solver))
                .with criteria(
                    gko::stop::Iteration::build().with max iters(num iters),
```

# **Chapter 15**

# The external-lib-interfacing program

The external library(deal.II) interfacing example..

### Introduction

About the example

# The commented program

```
#include <deal.II/base/function.h>
#include <deal.II/base/logstream.h>
#include <deal.II/base/quadrature_lib.h>
#include <deal.II/dofs/dof_accessor.h>
#include <deal.II/dofs/dof_handler.h>
#include <deal.II/dofs/dof_tools.h>
#include <deal.II/fe/fe_q.h>
#include <deal.II/fe/fe_values.h>
#include <deal.II/grid/grid_generator.h>
#include <deal.II/grid/grid_out.h>
#include <deal.II/grid/grid_refinement.h>
#include <deal.II/grid/tria.h>
#include <deal.II/grid/tria_accessor.h>
#include <deal.II/grid/tria_iterator.h>
#include <deal.II/lac/constraint_matrix.h>
#include <deal.II/lac/dynamic_sparsity_pattern.h>
#include <deal.II/lac/full_matrix.h>
#include <deal.II/lac/precondition.h>
#include <deal.II/lac/solver_bicgstab.h>
#include <deal.II/lac/sparse_matrix.h>
#include <deal.II/lac/vector.h>
#include <deal.II/numerics/data_out.h>
#include <deal.II/numerics/matrix_tools.h>
#include <deal.II/numerics/vector_tools.h>
```

The following two files provide classes and information for multithreaded programs. In the first one, the classes and functions are declared which we need to do assembly in parallel (i.e. the WorkStream namespace). The second file has a class MultithreadInfo which can be used to query the number of processors in your system, which is often useful when deciding how many threads to start in parallel.

```
#include <deal.II/base/multithread_info.h>
#include <deal.II/base/work_stream.h>
```

The next new include file declares a base class <code>TensorFunction</code> not unlike the <code>Function</code> class, but with the difference that the return value is tensor-valued rather than scalar of vector-valued.

```
#include <deal.II/base/tensor_function.h>
#include <deal.II/numerics/error_estimator.h>
```

#### Ginkgo's header file

#include <ginkgo/ginkgo.hpp>

This is C++, as we want to write some output to disk:

```
#include <fstream>
#include <iostream>
```

#### The last step is as in previous programs:

```
namespace Step9 {
using namespace dealii;
```

#### AdvectionProblem class declaration

Following we declare the main class of this program. It is very much like the main classes of previous examples, so we again only comment on the differences.

```
template <int dim>
class AdvectionProblem {
public:
   AdvectionProblem();
   AdvectionProblem();
   void run();
private:
   void setup system();
```

The next set of functions will be used to assemble the matrix. However, unlike in the previous examples, the <code>assemble\_system()</code> function will not do the work itself, but rather will delegate the actual assembly to helper functions <code>assemble\_local\_system()</code> and <code>copy\_local\_to\_global()</code>. The rationale is that matrix assembly can be parallelized quite well, as the computation of the local contributions on each cell is entirely independent of other cells, and we only have to synchronize when we add the contribution of a cell to the global matrix.

The strategy for parallelization we choose here is one of the possibilities mentioned in detail in the threads module in the documentation. Specifically, we will use the WorkStream approach discussed there. Since there is so much documentation in this module, we will not repeat the rationale for the design choices here (for example, if you read through the module mentioned above, you will understand what the purpose of the <code>AssemblyScratchData</code> and <code>AssemblyCopyData</code> structures is). Rather, we will only discuss the specific implementation.

If you read the page mentioned above, you will find that in order to parallelize assembly, we need two data structures – one that corresponds to data that we need during local integration ("scratch data", i.e., things we only need as temporary storage), and one that carries information from the local integration to the function that then adds the local contributions to the corresponding elements of the global matrix. The former of these typically contains the FEValues and FEFaceValues objects, whereas the latter has the local matrix, local right hand side, and information about which degrees of freedom live on the cell for which we are assembling a local contribution. With this information, the following should be relatively self-explanatory:

```
struct AssemblyScratchData {
    AssemblyScratchData(const FiniteElement<dim>& fe);
    AssemblyScratchData(const AssemblyScratchData& scratch_data);
    FEValues<dim> fe_values;
    FEFaceValues<dim> fe_face_values;
};
struct AssemblyCopyData {
    FullMatrix<double> cell_matrix;
    Vector<double> cell_rhs;
    std::vector<types::global_dof_index> local_dof_indices;
};
void assemble_system();
void local_assemble_system(
    const typename DoFHandler<dim>::active_cell_iterator& cell,
    AssemblyScratchData& scratch, AssemblyCopyData& copy_data);
void copy_local_to_global(const AssemblyCopyData& copy_data);
```

The following functions again are as in previous examples, as are the subsequent variables.

```
void solve();
void refine_grid();
void output_results(const unsigned int cycle) const;
Triangulation<dim> triangulation;
DoFHandler<dim> dof_handler;
FE_Q<dim> fe;
ConstraintMatrix hanging_node_constraints;
SparsityPattern sparsity_pattern;
SparseMatrix<double> system_matrix;
Vector<double> solution;
Vector<double> system_rhs;
```

#### **Equation data declaration**

};

Next we declare a class that describes the advection field. This, of course, is a vector field with as many components as there are space dimensions. One could now use a class derived from the Function base class, as we have done for boundary values and coefficients in previous examples, but there is another possibility in the library, namely

a base class that describes tensor valued functions. In contrast to the usual Function objects, we provide the compiler with knowledge on the size of the objects of the return type. This enables the compiler to generate efficient code, which is not so simple for usual vector-valued functions where memory has to be allocated on the heap (thus, the Function::vector\_value function has to be given the address of an object into which the result is to be written, in order to avoid copying and memory allocation and deallocation on the heap). In addition to the known size, it is possible not only to return vectors, but also tensors of higher rank; however, this is not very often requested by applications, to be honest...

The interface of the TensorFunction class is relatively close to that of the Function class, so there is probably no need to comment in detail the following declaration:

In previous examples, we have used assertions that throw exceptions in several places. However, we have never seen how such exceptions are declared. This can be done as follows:

The syntax may look a little strange, but is reasonable. The format is basically as follows: use the name of one of the macros <code>DeclexceptionN</code>, where <code>N</code> denotes the number of additional parameters which the exception object shall take. In this case, as we want to throw the exception when the sizes of two vectors differ, we need two arguments, so we use <code>Declexception2</code>. The first parameter then describes the name of the exception, while the following declare the data types of the parameters. The last argument is a sequence of output directives that will be piped into the <code>std::cerr</code> object, thus the strange format with the leading <code><<</code> operator and the like. Note that we can access the parameters which are passed to the exception upon construction (i.e. within the <code>Assert call</code>) by using the names <code>arg1</code> through <code>argN</code>, where <code>N</code> is the number of arguments as defined by the use of the respective macro <code>DeclexceptionN</code>.

To learn how the preprocessor expands this macro into actual code, please refer to the documentation of the exception classes in the base library. Suffice it to say that by this macro call, the respective exception class is declared, which also has error output functions already implemented.

The following two functions implement the interface described above. The first simply implements the function as described in the introduction, while the second uses the same trick to avoid calling a virtual function as has already been introduced in the previous example program. Note the check for the right sizes of the arguments in the second function, which should always be present in such functions; it is our experience that many if not most programming errors result from incorrectly initialized arrays, incompatible parameters to functions and the like; using assertion as in this case can eliminate many of these problems.

Besides the advection field, we need two functions describing the source terms (right hand side) and the boundary values. First for the right hand side, which follows the same pattern as in previous examples. As described in the introduction, the source is a constant function in the vicinity of a source point, which we denote by the constant static variable center\_point. We set the values of this center using the same template tricks as we have shown

in the step-7 example program. The rest is simple and has been shown previously, including the way to avoid virtual function calls in the value\_list function.

The only new thing here is that we check for the value of the component parameter. As this is a scalar function, it is obvious that it only makes sense if the desired component has the index zero, so we assert that this is indeed the case. ExcIndexRange is a global predefined exception (probably the one most often used, we therefore made it global instead of local to some class), that takes three parameters: the index that is outside the allowed range, the first element of the valid range and the one past the last (i.e. again the half-open interval so often used in the C++ standard library):

Finally for the boundary values, which is just another class derived from the Function base class:

```
template <int dim>
class BoundaryValues : public Function<dim> {
public:
    BoundaryValues() : Function<dim>() {}
    virtual double value(const Point<dim>& p,
                         const unsigned int component = 0) const;
    virtual void value_list(const std::vector<Point<dim>& points,
                            std::vector<double>& values,
                            const unsigned int component = 0) const;
template <int dim>
double BoundaryValues<dim>::value(const Point<dim>& p,
                                  const unsigned int component) const
    (void) component;
    Assert (component == 0, ExcIndexRange (component, 0, 1));
    const double sine term =
       std::sin(16 * numbers::PI * std::sqrt(p.norm_square()));
    const double weight = std::exp(-5 * p.norm_square()) / std::exp(-5.);
    return sine_term * weight;
template <int dim>
void BoundaryValues<dim>::value_list(const std::vector<Point<dim>& points,
                                     std::vector<double>& values,
                                     const unsigned int component) const
    Assert(values.size() == points.size(),
          ExcDimensionMismatch(values.size(), points.size()));
    for (unsigned int i = 0; i < points.size(); ++i)</pre>
        values[i] = BoundaryValues<dim>::value(points[i], component);
}
```

#### **GradientEstimation class declaration**

Now, finally, here comes the class that will compute the difference approximation of the gradient on each cell and weighs that with a power of the mesh size, as described in the introduction. This class is a simple version of the <code>DerivativeApproximation</code> class in the library, that uses similar techniques to obtain finite difference approximations of the gradient of a finite element field, or of higher derivatives.

The class has one public static function <code>estimate</code> that is called to compute a vector of error indicators, and a few private functions that do the actual work on all active cells. As in other parts of the library, we follow an informal convention to use vectors of floats for error indicators rather than the common vectors of doubles, as the additional accuracy is not necessary for estimated values.

In addition to these two functions, the class declares two exceptions which are raised when a cell has no neighbors in each of the space directions (in which case the matrix described in the introduction would be singular and can't be inverted), while the other one is used in the more common case of invalid parameters to a function, namely a vector of wrong size.

Two other comments: first, the class has no non-static member functions or variables, so this is not really a class, but rather serves the purpose of a namespace in C++. The reason that we chose a class over a namespace is that this way we can declare functions that are private. This can be done with namespaces as well, if one declares some functions in header files in the namespace and implements these and other functions in the implementation file. The functions not declared in the header file are still in the namespace but are not callable from outside. However, as we have only one file here, it is not possible to hide functions in the present case.

The second comment is that the dimension template parameter is attached to the function rather than to the class itself. This way, you don't have to specify the template parameter yourself as in most other cases, but the compiler can figure its value out itself from the dimension of the DoF handler object that one passes as first argument.

Before jumping into the fray with the implementation, let us also comment on the parallelization strategy. We have already introduced the necessary framework for using the WorkStream concept in the declaration of the main class of this program above. We will use it again here. In the current context, this means that we have to define (i) classes for scratch and copy objects, (ii) a function that does the local computation on one cell, and (iii) a function that copies the local result into a global object. Given this general framework, we will, however, deviate from it a bit. In particular, WorkStream was generally invented for cases where each local computation on a cell adds to a global object - for example, when assembling linear systems where we add local contributions into a global matrix and right hand side. WorkStream is designed to handle the potential conflict of multiple threads trying to do this addition at the same time, and consequently has to provide for some way to ensure that only thread gets to do this at a time. Here, however, the situation is slightly different: we compute contributions from every cell individually, but then all we need to do is put them into an element of an output vector that is unique to each cell. Consequently, there is no risk that the write operations from two cells might conflict, and the elaborate machinery of WorkStream to avoid conflicting writes is not necessary. Consequently, what we will do is this: We still need a scratch object that holds, for example, the FEValues object. However, we only create a fake, empty copy data structure. Likewise, we do need the function that computes local contributions, but since it can already put the result into its final location, we do not need a copy-local-to-global function and will instead give the WorkStream::run() function an empty function object - the equivalent to a NULL function pointer.

```
class GradientEstimation {
    template <int dim>
    static void estimate(const DoFHandler<dim>& dof,
                          const Vector<double>& solution.
                          Vector<float>& error per cell);
    DeclException2(ExcInvalidVectorLength, int, int, "Vector has length " « arg1 « ", but should have "
                    « arg2);
    DeclException0(ExcInsufficientDirections);
private:
    template <int dim>
    struct EstimateScratchData {
        EstimateScratchData(const FiniteElement<dim>& fe,
                              const Vector<double>& solution,
                              Vector<float>& error_per_cell);
        EstimateScratchData(const EstimateScratchData& data);
        FEValues<dim> fe midpoint value;
        const Vector<double>& solution;
        Vector<float>& error_per_cell;
```

```
};
struct EstimateCopyData {};
template <int dim>
static void estimate_cell(
    const typename DoFHandler<dim>::active_cell_iterator& cell,
    EstimateScratchData<dim>& scratch_data,
    const EstimateCopyData& copy_data);
```

#### AdvectionProblem class implementation

Now for the implementation of the main class. Constructor, destructor and the function <code>setup\_system</code> follow the same pattern that was used previously, so we need not comment on these three function:

```
template <int dim>
AdvectionProblem<dim>::AdvectionProblem() : dof_handler(triangulation), fe(1)
template <int dim>
AdvectionProblem < dim>:: AdvectionProblem ()
   dof handler.clear();
template <int dim>
void AdvectionProblem < dim > :: setup system ()
    dof_handler.distribute_dofs(fe);
    hanging node constraints.clear();
    DoFTools::make hanging node constraints(dof handler.
                                             hanging_node_constraints);
    hanging_node_constraints.close();
    DynamicSparsityPattern dsp(dof_handler.n_dofs(), dof_handler.n_dofs());
    DoFTools::make_sparsity_pattern(dof_handler, dsp, hanging_node_constraints,
                                      *keep_constrained_dofs = * / true);
    sparsity pattern.copy from(dsp);
    system matrix.reinit(sparsity pattern);
    solution.reinit(dof_handler.n_dofs());
    system_rhs.reinit(dof_handler.n_dofs());
```

In the following function, the matrix and right hand side are assembled. As stated in the documentation of the main class above, it does not do this itself, but rather delegates to the function following next, utilizing the WorkStream concept discussed in threads .

If you have looked through the threads module, you will have seen that assembling in parallel does not take an incredible amount of extra code as long as you diligently describe what the scratch and copy data objects are, and if you define suitable functions for the local assembly and the copy operation from local contributions to global objects. This done, the following will do all the heavy lifting to get these operations done on multiple threads on as many cores as you have in your system:

After the matrix has been assembled in parallel, we still have to eliminate hanging node constraints. This is something that can't be done on each of the threads separately, so we have to do it now. Note also, that unlike in previous examples, there are no boundary conditions to be applied to the system of equations. This, of course, is due to the fact that we have included them into the weak formulation of the problem.

```
hanging_node_constraints.condense(system_matrix);
hanging_node_constraints.condense(system_rhs);
```

As already mentioned above, we need to have scratch objects for the parallel computation of local contributions. These objects contain FEValues and FEFaceValues objects, and so we will need to have constructors and copy constructors that allow us to create them. In initializing them, note first that we use bilinear elements, soGauss formulae with two points in each space direction are sufficient. For the cell terms we need the values and gradients of the shape functions, the quadrature points in order to determine the source density and the advection field at a given point, and the weights of the quadrature points times the determinant of the Jacobian at these points. In contrast, for the boundary integrals, we don't need the gradients, but rather the normal vectors to the cells. This determines which update flags we will have to pass to the constructors of the members of the class:

```
template <int dim>
{\tt AdvectionProblem < dim > :: Assembly Scratch Data:: Assembly Scratch Data() }
    const FiniteElement<dim>& fe)
    : fe_values(fe, QGauss<dim>(2),
               update_values | update_gradients | update_quadrature_points |
                    update JxW values),
      fe_face_values(fe, QGauss<dim - 1>(2),
                     update_values | update_quadrature_points |
                         update_JxW_values | update_normal_vectors)
template <int dim>
AdvectionProblem<dim>::AssemblyScratchData::AssemblyScratchData(
    const AssemblyScratchData& scratch data)
    : fe_values(scratch_data.fe_values.get_fe(),
                scratch_data.fe_values.get_quadrature(),
                update_values | update_gradients | update_quadrature_points |
                    update_JxW_values),
      fe_face_values(scratch_data.fe_face_values.get_fe(),
                     scratch_data.fe_face_values.get_quadrature(),
                     update_values | update_quadrature_points |
                         update_JxW_values | update_normal_vectors)
{ }
```

Now, this is the function that does the actual work. It is not very different from the assemble\_system functions of previous example programs, so we will again only comment on the differences. The mathematical stuff follows closely what we have said in the introduction.

There are a number of points worth mentioning here, though. The first one is that we have moved the FEValues and FEFaceValues objects into the ScratchData object. We have done so because the alternative would have been to simply create one every time we get into this function – i.e., on every cell. It now turns out that the FEValues classes were written with the explicit goal of moving everything that remains the same from cell to cell into the construction of the object, and only do as little work as possible in FEValues::reinit() whenever we move to a new cell. What this means is that it would be very expensive to create a new object of this kind in this function as we would have to do it for every cell – exactly the thing we wanted to avoid with the FEValues class. Instead, what we do is create it only once (or a small number of times) in the scratch objects and then re-use it as often as we can.

This begs the question of whether there are other objects we create in this function whose creation is expensive compared to its use. Indeed, at the top of the function, we declare all sorts of objects. The <code>AdvectionField</code>, <code>RightHandSide</code> and <code>BoundaryValues</code> do not cost much to create, so there is no harm here. However, allocating memory in creating the <code>rhs\_values</code> and similar variables below typically costs a significant amount of time, compared to just accessing the (temporary) values we store in them. Consequently, these would be candidates for moving into the <code>AssemblyScratchData</code> class. We will leave this as an exercise.

```
template <int dim>
void AdvectionProblem<dim>::local_assemble_system(
   const typename DoFHandler<dim>::active_cell_iterator& cell,
   AssemblyScratchData& scratch_data, AssemblyCopyData& copy_data)
{
```

First of all, we will need some objects that describe boundary values, right hand side function and the advection field. As we will only perform actions on these objects that do not change them, we declare them as constant, which can enable the compiler in some cases to perform additional optimizations.

```
const AdvectionField<dim> advection_field;
const RightHandSide<dim> right_hand_side;
const BoundaryValues<dim> boundary_values;
```

Then we define some abbreviations to avoid unnecessarily long lines:

```
const unsigned int dofs_per_cell = fe.dofs_per_cell;
const unsigned int n_q_points =
    scratch_data.fe_values.get_quadrature().size();
const unsigned int n_face_q_points =
    scratch_data.fe_face_values.get_quadrature().size();
```

We declare cell matrix and cell right hand side...

```
copy_data.cell_matrix.reinit(dofs_per_cell, dofs_per_cell);
copy_data.cell_rhs.reinit(dofs_per_cell);
```

... an array to hold the global indices of the degrees of freedom of the cell on which we are presently working...

... and array in which the values of right hand side, advection direction, and boundary values will be stored, for cell and face integrals respectively:

... and assemble the local contributions to the system matrix and right hand side as also discussed above:

Besides the cell terms which we have built up now, the bilinear form of the present problem also contains terms on the boundary of the domain. Therefore, we have to check whether any of the faces of this cell are on the boundary of the domain, and if so assemble the contributions of this face as well. Of course, the bilinear form only contains contributions from the inflow part of the boundary, but to find out whether a certain part of a face of the present cell is part of the inflow boundary, we have to have information on the exact location of the quadrature points and on the direction of flow at this point; we obtain this information using the FEFaceValues object and only decide within the main loop whether a quadrature point is on the inflow boundary.

Ok, this face of the present cell is on the boundary of the domain. Just as for the usual FEValues object which we have used in previous examples and also above, we have to reinitialize the FEFaceValues object for the present face:

```
scratch_data.fe_face_values.reinit(cell, face);
```

For the quadrature points at hand, we ask for the values of the inflow function and for the direction of flow:

```
boundary_values.value_list(
    scratch_data.fe_face_values.get_quadrature_points(),
    face_boundary_values);
advection_field.value_list(
    scratch_data.fe_face_values.get_quadrature_points(),
    face_advection_directions);
```

Now loop over all quadrature points and see whether it is on the inflow or outflow part of the boundary. This is determined by a test whether the advection direction points inwards or outwards of the domain (note that the normal vector points outwards of the cell, and since the cell is at the boundary, the normal vector points outward of the domain, so if the advection direction points into the domain, its scalar product with the normal vector must be negative):

If the is part of the inflow boundary, then compute the contributions of this face to the global matrix and right hand side, using the values obtained from the FEFaceValues object and the formulae discussed in the introduction:

```
for (unsigned int i = 0; i < dofs_per_cell; ++i) {</pre>
    for (unsigned int j = 0; j < dofs_per_cell; ++j)</pre>
         copy_data.cell_matrix(i, j) -
              (\texttt{face\_advection\_directions} \, [\, \underline{q} \, \underline{\hspace{0.1cm}} \, point \, ] \  \, \star \\
               scratch_data.fe_face_values.normal_vector(
                   a point) *
               scratch_data.fe_face_values.shape_value(
                   i, q_point)
               scratch_data.fe_face_values.shape_value(
                   j, q_point)
               scratch_data.fe_face_values.JxW(q_point));
    copy_data.cell_rhs(i) -=
         (face advection directions[g point] *
          scratch_data.fe_face_values.normal_vector(
              q_point) *
          face_boundary_values[q_point] *
          scratch_data.fe_face_values.shape_value(i,
                                                         q_point) *
          scratch_data.fe_face_values.JxW(q_point));
```

Now go on by transferring the local contributions to the system of equations into the global objects. The first step was to obtain the global indices of the degrees of freedom on this cell.

```
cell->get_dof_indices(copy_data.local_dof_indices);
```

The second function we needed to write was the one that copies the local contributions the previous function has computed and put into the copy data object, into the global matrix and right hand side vector objects. This is essentially what we always had as the last block of code when assembling something on every cell. The following should therefore be pretty obvious:

Following is the function that solves the linear system of equations. As the system is no more symmetric positive definite as in all the previous examples, we can't use the Conjugate Gradients method anymore. Rather, we use a solver that is tailored to nonsymmetric systems like the one at hand, the BiCGStab method. As preconditioner, we use the Block Jacobi method.

```
template <int dim>
void AdvectionProblem<dim>::solve()
{
```

#### Assert that the system be symmetric.

```
Assert(system_matrix.m() == system_matrix.n(), ExcNotQuadratic());
auto num_rows = system_matrix.m();
```

#### Make a copy of the rhs to use with Ginkgo.

```
std::vector<double> rhs(num_rows);
std::copy(system_rhs.begin(), system_rhs.begin() + num_rows, rhs.begin());
```

Ginkgo setup Some shortcuts: A vector is a Dense matrix with co-dimension 1. The matrix is setup in CSR. But various formats can be used. Look at Ginkgo's documentation.

```
using vec = gko::matrix::Dense<>;
using mtx = gko::matrix::Csr<>;
using bicgstab = gko::solver::Bicgstab<>;
using bj = gko::preconditioner::Jacobi<>;
using val_array = gko::array<double>;
```

Where the code is to be executed. Can be changed to omp or cuda to run on multiple threads or on gpu's std::shared\_ptr<gko::Executor> exec = gko::ReferenceExecutor::create();

#### Setup Ginkgo's data structures

```
system_matrix.n_nonzero_elements());
mtx::value_type* values = A->get_values();
mtx::index_type* row_ptr = A->get_row_ptrs();
mtx::index_type* col_idx = A->get_col_idxs();
```

Convert to standard CSR format As deal.ii does not expose its system matrix pointers, we construct them individually.

#### write entry into the first free one for this row

```
col_idx[ptrs[row]] = p->column();
values[ptrs[row]] = p->value();
```

#### then move pointer ahead

```
++ptrs[row];
}
```

Ginkgo solve The stopping criteria is set at maximum iterations of 1000 and a reduction factor of 1e-12. For other options, refer to Ginkgo's documentation.

#### Solve system

solver->apply(b, x);

Copy the solution vector back to deal.ii's data structures.

#### Distribute the possible hanging nodes constraints

```
hanging_node_constraints.distribute(solution);
```

The following function refines the grid according to the quantity described in the introduction. The respective computations are made in the class <code>GradientEstimation</code>. The only difference to previous examples is that we refine a little more aggressively (0.5 instead of 0.3 of the number of cells).

Writing output to disk is done in the same way as in the previous examples. Indeed, the function is identical to the one in step-6.

```
template <int dim>
void AdvectionProblem<dim>::output_results(const unsigned int cycle)const
{
```

```
{
        GridOut grid out;
        std::ofstream output("grid-" + std::to_string(cycle) + ".eps");
        grid_out.write_eps(triangulation, output);
        DataOut<dim> data_out;
        data_out.attach_dof_handler(dof_handler);
        data_out.add_data_vector(solution, "solution");
        data_out.build_patches();
        std::ofstream output("solution-" + std::to_string(cycle) + ".vtk");
        data_out.write_vtk(output);
... as is the main loop (setup – solve – refine)
template <int dim>
void AdvectionProblem < dim >:: run ()
    for (unsigned int cycle = 0; cycle < 6; ++cycle) {</pre>
        std::cout « "Cycle " « cycle « ':' « std::endl;
        if (cycle == 0) {
            GridGenerator::hyper_cube(triangulation, -1, 1);
            triangulation.refine_global(4);
        } else {
            refine_grid();
        std::cout « " Number of active cells:
                  « triangulation.n_active_cells() « std::endl;
        setup_system();
std::cout « " Number of degrees of freedom: " « dof_handler.n_dofs()
                  « std::endl;
        assemble_system();
        solve();
        output_results(cycle);
```

#### GradientEstimation class implementation

Now for the implementation of the GradientEstimation class. Let us start by defining constructors for the EstimateScratchData class used by the estimate\_cell() function:

```
template <int dim>
GradientEstimation::EstimateScratchData<dim>::EstimateScratchData(
    const FiniteElement<dim>& fe, const Vector<double>& solution,
    Vector<float>& error_per_cell)
    : fe_midpoint_value(fe, QMidpoint<dim>(),
                       update_values | update_quadrature_points),
      solution(solution),
     error_per_cell(error_per_cell)
{ }
template <int dim>
GradientEstimation::EstimateScratchData<dim>::EstimateScratchData(
   const EstimateScratchData& scratch_data)
    : fe_midpoint_value(scratch_data.fe_midpoint_value.get_fe(),
                        scratch_data.fe_midpoint_value.get_quadrature(),
                        update_values | update_quadrature_points),
      solution(scratch data.solution),
      error_per_cell(scratch_data.error_per_cell)
```

Next for the implementation of the <code>GradientEstimation</code> class. The first function does not much except for delegating work to the other function, but there is a bit of setup at the top.

Before starting with the work, we check that the vector into which the results are written has the right size. Programming mistakes in which one forgets to size arguments correctly at the calling site are quite common. Because the resulting damage from not catching such errors is often subtle (e.g., corruption of data somewhere in memory, or non-reproducible results), it is well worth the effort to check for such things.

Following now the function that actually computes the finite difference approximation to the gradient. The general outline of the function is to first compute the list of active neighbors of the present cell and then compute the quantities described in the introduction for each of the neighbors. The reason for this order is that it is not a one-liner to find a given neighbor with locally refined meshes. In principle, an optimized implementation would find neighbors and the quantities depending on them in one step, rather than first building a list of neighbors and in a second step their contributions but we will gladly leave this as an exercise. As discussed before, the worker function passed to WorkStream::run works on "scratch" objects that keep all temporary objects. This way, we do not need to create and initialize objects that are expensive to initialize within the function that does the work, every time it is called for a given cell. Such an argument is passed as the second argument. The third argument would be a "copy-data" object (see threads for more information) but we do not actually use any of these here. Because WorkStream::run() insists on passing three arguments, we declare this function with three arguments, but simply ignore the last one.

(This is unsatisfactory from an esthetic perspective. It can be avoided, at the cost of some other trickery. If you allow, let us here show how. First, assume that we had declared this function to only take two arguments by omitting the unused last one. Now, WorkStream::run still wants to call this function with three arguments, so we need to find a way to "forget" the third argument in the call. Simply passing WorkStream::run the pointer to the function as we do above will not do this – the compiler will complain that a function declared to have two arguments is called with three arguments. However, we can do this by passing the following as the third argument when calling WorkStream::run() above:

This creates a function object taking three arguments, but when it calls the underlying function object, it simply only uses the first and second argument – we simply "forget" to use the third argument :-) In the end, this isn't completely obvious either, and so we didn't implement it, but hey – it can be done!)

#### Now for the details:

```
template <int dim>
void GradientEstimation::estimate_cell(
   const typename DoFHandler<dim>::active_cell_iterator& cell,
   EstimateScratchData<dim>& scratch_data, const EstimateCopyData&)
{
```

We need space for the tensor Y, which is the sum of outer products of the y-vectors.

```
Tensor<2, dim> Y;
```

Then we allocate a vector to hold iterators to all active neighbors of a cell. We reserve the maximal number of active neighbors in order to avoid later reallocations. Note how this maximal number of active neighbors is computed here. std::vector<typename DoFHandler<dim>::active cell iterator>

#### First initialize the ${\tt FEValues}$ object, as well as the ${\tt Y}$ tensor:

```
scratch_data.fe_midpoint_value.reinit(cell);
```

Then allocate the vector that will be the sum over the y-vectors times the approximate directional derivative: Tensor<1, dim> projected\_gradient;

Now before going on first compute a list of all active neighbors of the present cell. We do so by first looping over all faces and see whether the neighbor there is active, which would be the case if it is on the same level as the present cell or one level coarser (note that a neighbor can only be once coarser than the present cell, as we only allow a

maximal difference of one refinement over a face in deal.II). Alternatively, the neighbor could be on the same level and be further refined; then we have to find which of its children are next to the present cell and select these (note that if a child of a neighbor of an active cell that is next to this active cell, needs necessarily be active itself, due to the one-refinement rule cited above).

Things are slightly different in one space dimension, as there the one-refinement rule does not exist: neighboring active cells may differ in as many refinement levels as they like. In this case, the computation becomes a little more difficult, but we will explain this below.

Before starting the loop over all neighbors of the present cell, we have to clear the array storing the iterators to the active neighbors, of course.

First define an abbreviation for the iterator to the face and the neighbor

```
const typename DoFHandler<dim>::face_iterator face =
   cell->face(face_no);
const typename DoFHandler<dim>::cell_iterator neighbor =
   cell->neighbor(face_no);
```

Then check whether the neighbor is active. If it is, then it is on the same level or one level coarser (if we are not in 1D), and we are interested in it in any case.

```
if (neighbor->active())
    active_neighbors.push_back(neighbor);
else {
```

If the neighbor is not active, then check its children.

```
if (dim == 1) {
```

To find the child of the neighbor which bounds to the present cell, successively go to its right child if we are left of the present cell (n==0), or go to the left child if we are on the right (n==1), until we find an active cell.

```
typename DoFHandler<dim>::cell_iterator neighbor_child =
    neighbor;
while (neighbor_child=>has_children())
    neighbor_child =
        neighbor_child->child(face_no == 0 ? 1 : 0);
```

As this used some non-trivial geometrical intuition, we might want to check whether we did it right, i.e. check whether the neighbor of the cell we found is indeed the cell we are presently working on. Checks like this are often useful and have frequently uncovered errors both in algorithms like the line above (where it is simple to involuntarily exchange n=1 for n=0 or the like) and in the library (the assumptions underlying the algorithm above could either be wrong, wrongly documented, or are violated due to an error in the library). One could in principle remove such checks after the program works for some time, but it might be a good things to leave it in anyway to check for changes in the library or in the algorithm above.

Note that if this check fails, then this is certainly an error that is irrecoverable and probably qualifies as an internal error. We therefore use a predefined exception class to throw here.

```
Assert(
  neighbor_child->neighbor(face_no == 0 ? 1 : 0) == cell,
  ExcInternalError());
```

If the check succeeded, we push the active neighbor we just found to the stack we keep:

If we are not in 1d, we collect all neighbor children 'behind' the subfaces of the current face

OK, now that we have all the neighbors, lets start the computation on each of them. First we do some preliminaries: find out about the center of the present cell and the solution at this point. The latter is obtained as a vector of

function values at the quadrature points, of which there are only one, of course. Likewise, the position of the center is the position of the first (and only) quadrature point in real space.

Now loop over all active neighbors and collect the data we need. Allocate a vector just like this\_midpoint\_  $\leftarrow$  value which we will use to store the value of the solution in the midpoint of the neighbor cell. We allocate it here already, since that way we don't have to allocate memory repeatedly in each iteration of this inner loop (memory allocation is a rather expensive operation):

```
std::vector<double> neighbor_midpoint_value(1);
typename std::vector<typename DoFHandler<dim>::active_cell_iterator>::
    const_iterator neighbor_ptr = active_neighbors.begin();
for (; neighbor_ptr != active_neighbors.end(); ++neighbor_ptr) {
```

First define an abbreviation for the iterator to the active neighbor cell:

```
const typename DoFHandler<dim>::active_cell_iterator neighbor =
   *neighbor_ptr;
```

Then get the center of the neighbor cell and the value of the finite element function thereon. Note that for this information we have to reinitialize the FEValues object for the neighbor cell.

```
scratch_data.fe_midpoint_value.reinit(neighbor);
const Point<dim> neighbor_center =
    scratch_data.fe_midpoint_value.quadrature_point(0);
scratch_data.fe_midpoint_value.get_function_values(
    scratch_data.solution, neighbor_midpoint_value);
```

Compute the vector y connecting the centers of the two cells. Note that as opposed to the introduction, we denote by y the normalized difference vector, as this is the quantity used everywhere in the computations.

Tensor<1, dim> y = neighbor\_center - this\_center;

```
const double distance = y.norm();
y /= distance;

Then add up the contribution of this cell to the Y matrix...
for (unsigned int i = 0; i < dim; ++i)
    for (unsigned int j = 0; j < dim; ++j) Y[i][j] += y[i] * y[j];

... and update the sum of difference quotients:
    projected_gradient +=</pre>
```

(neighbor\_midpoint\_value[0] - this\_midpoint\_value[0]) / distance \*

If now, after collecting all the information from the neighbors, we can determine an approximation of the gradient for the present cell, then we need to have passed over vectors y which span the whole space, otherwise we would not have all components of the gradient. This is indicated by the invertibility of the matrix.

If the matrix should not be invertible, this means that the present cell had an insufficient number of active neighbors. In contrast to all previous cases, where we raised exceptions, this is, however, not a programming error: it is a runtime error that can happen in optimized mode even if it ran well in debug mode, so it is reasonable to try to catch this error also in optimized mode. For this case, there is the <code>AssertThrow</code> macro: it checks the condition like the <code>Assert</code> macro, but not only in debug mode; it then outputs an error message, but instead of terminating the program as in the case of the <code>Assert</code> macro, the exception is thrown using the <code>throw</code> command of C++. This way, one has the possibility to catch this error and take reasonable counter actions. One such measure would be to refine the grid globally, as the case of insufficient directions can not occur if every cell of the initial grid has been refined at least once.

```
AssertThrow(determinant(Y) != 0, ExcInsufficientDirections());
```

If, on the other hand the matrix is invertible, then invert it, multiply the other quantity with it and compute the estimated error using this quantity and the right powers of the mesh width:

```
const Tensor<2, dim> Y_inverse = invert(Y);
Tensor<1, dim> gradient = Y_inverse * projected_gradient;
```

The last part of this function is the one where we write into the element of the output vector what we have just computed. The address of this vector has been stored in the scratch data object, and all we have to do is know how to get at the correct element inside this vector – but we can ask the cell we're on the how-manyth active cell it is for this:

```
scratch_data.error_per_cell(cell->active_cell_index()) =
   (std::pow(cell->diameter(), 1 + 1.0 * dim / 2) *
        std::sqrt(gradient.norm_square()));
// namespace Step9
```

#### **Main function**

The main function is similar to the previous examples. The main difference is that we use MultithreadInfo to set the maximum number of threads (see Parallel computing with multiple processors accessing shared memory" documentation module for more explanation). The number of threads used is the minimum of the environment variable DEAL\_II\_NUM\_THREADS and the parameter of set\_thread\_limit. If no value is given to set thread\_limit, the default value from the Intel Threading Building Blocks (TBB) library is used. If the call to set\_thread\_limit is omitted, the number of threads will be chosen by TBB independently of DEAL\_II\_NU  $\leftarrow$  M THREADS.

```
int main()
        dealii::MultithreadInfo::set thread limit();
        Step9::AdvectionProblem<2> advection_problem_2d;
        advection_problem_2d.run();
    } catch (std::exception& exc) {
        std::cerr « std::endl
                   « std::endl
« "-----
                   « std::endl;
        std::cerr « "Exception on processing: " « std::endl
                   « exc.what() « std::endl
« "Aborting!" « std::endl
                   « "-
                   « std::endl;
        return 1:
    } catch (...)
        std::cerr « std::endl
                   « std::endl
                   « std::endl;
        std::cerr « "Unknown exception!" « std::endl
                   « "Aborting!" « std::endl
                   « std::endl;
        return 1;
    return 0:
```

### Results

#### Comments about programming and debugging

# The plain program

```
/*

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* it, and/or modify it under the terms of the GNU Lesser General

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* the top level of the deal.II distribution.

*

* Author: Wolfgang Bangerth, University of Heidelberg, 2000

*/
/*

* This file has been taken verbatim from the deal.ii (version 9.0)

* examples directory and modified.

* This example aims to demonstrate the ease with which Ginkgo can

* be interfaced with other libraries. The only modification/ addition

* has been to the AdvectionProblem::solve () function.
```

```
#include <deal.II/base/function.h>
#include <deal.II/base/logstream.h>
#include <deal.II/base/quadrature_lib.h>
#include <deal.II/dofs/dof_accessor.h>
#include <deal.II/dofs/dof_handler.h>
#include <deal.II/dofs/dof_tools.h>
#include <deal.II/fe/fe_q.h>
#include <deal.II/fe/fe_values.h>
#include <deal.II/grid/grid_generator.h>
#include <deal.II/grid/grid_out.h>
#include <deal.II/grid/grid_refinement.h>
#include <deal.II/grid/tria.h>
#include <deal.II/grid/tria_accessor.h>
#include <deal.II/grid/tria_iterator.h>
#include <deal.II/lac/constraint_matrix.h>
#include <deal.II/lac/dynamic_sparsity_pattern.h>
#include <deal.II/lac/full_matrix.h>
#include <deal.II/lac/precondition.h>
#include <deal.II/lac/solver_bicgstab.h>
#include <deal.II/lac/sparse_matrix.h>
#include <deal.II/lac/vector.h>
#include <deal.II/numerics/data_out.h>
#include <deal.II/numerics/matrix tools.h>
#include <deal.II/numerics/vector_tools.h>
#include <deal.II/base/multithread_info.h>
#include <deal.II/base/work_stream.h>
#include <deal.II/base/tensor_function.h>
#include <deal.II/numerics/error_estimator.h>
#include <ginkgo/ginkgo.hpp>
#include <fstream>
#include <iostream>
namespace Step9 {
using namespace dealii;
template <int dim>
class AdvectionProblem {
public:
    AdvectionProblem();
     AdvectionProblem();
    void run();
private:
    void setup_system();
    struct AssemblyScratchData {
        AssemblyScratchData(const FiniteElement<dim>& fe);
        AssemblyScratchData(const AssemblyScratchData& scratch_data);
        FEValues<dim> fe_values;
        FEFaceValues<dim> fe_face_values;
    struct AssemblyCopyData {
        FullMatrix<double> cell_matrix;
        Vector<double> cell_rhs;
        std::vector<types::global_dof_index> local_dof_indices;
    void assemble_system();
    void local_assemble_system(
        const typename DoFHandler<dim>::active_cell_iterator& cell,
        AssemblyScratchData& scratch, AssemblyCopyData& copy_data);
    void copy_local_to_global(const AssemblyCopyData& copy_data);
    void solve();
    void refine_grid();
    void output_results(const unsigned int cycle) const;
    Triangulation<dim> triangulation;
    DoFHandler<dim> dof_handler;
    FE_Q<dim> fe;
    ConstraintMatrix hanging_node_constraints;
    SparsityPattern sparsity_pattern;
    SparseMatrix<double> system_matrix;
    Vector<double> solution:
    Vector<double> system_rhs;
};
template <int dim>
class AdvectionField : public TensorFunction<1, dim> {
public:
    AdvectionField() : TensorFunction<1, dim>() {}
    virtual Tensor<1, dim> value(const Point<dim>& p) const;
    virtual void value_list(const std::vector<Point<dim>& points,
                           std::vector<Tensor<1, dim>& values) const;
    template <int dim>
Tensor<1, dim> AdvectionField<dim>::value(const Point<dim>& p)const
    Point<dim> value;
value[0] = 2;
    for (unsigned int i = 1; i < dim; ++i)</pre>
```

```
value[i] = 1 + 0.8 * std::sin(8 * numbers::PI * p[0]);
template <int dim>
void AdvectionField<dim>::value_list(const std::vector<Point<dim>& points,
                                     std::vector<Tensor<1, dim>& values)const
    Assert(values.size() == points.size(),
           ExcDimensionMismatch(values.size(), points.size()));
    for (unsigned int i = 0; i < points.size(); ++i)</pre>
       values[i] = AdvectionField<dim>::value(points[i]);
template <int dim>
class RightHandSide : public Function<dim> {
public:
    RightHandSide() : Function<dim>() {}
    virtual double value(const Point<dim>& p,
                         const unsigned int component = 0) const;
    virtual void value_list(const std::vector<Point<dim>& points,
                            std::vector<double>& values,
                            const unsigned int component = 0) const;
private:
    static const Point<dim> center_point;
template <>
const Point<1> RightHandSide<1>::center_point = Point<1>(-0.75);
const Point<2> RightHandSide<2>::center_point = Point<2>(-0.75, -0.75);
template <>
const Point<3> RightHandSide<3>::center_point = Point<3>(-0.75, -0.75, -0.75);
template <int dim>
double RightHandSide<dim>::value(const Point<dim>& p,
                                 const unsigned int component) const
    (void) component;
    Assert(component == 0, ExcIndexRange(component, 0, 1));
const double diameter = 0.1;
    return ((p - center_point).norm_square() < diameter * diameter</pre>
                ? .1 / std::pow(diameter, dim) : 0);
template <int dim>
void RightHandSide<dim>::value_list(const std::vector<Point<dim>& points,
                                     std::vector<double>& values,
                                     const unsigned int component) const
    Assert(values.size() == points.size(),
          ExcDimensionMismatch(values.size(), points.size()));
    for (unsigned int i = 0; i < points.size(); ++i)</pre>
       values[i] = RightHandSide<dim>::value(points[i], component);
template <int dim>
class BoundaryValues : public Function<dim> {
public:
    BoundaryValues() : Function<dim>() {}
    virtual void value_list(const std::vector<Point<dim>& points,
                            std::vector<double>& values,
                            const unsigned int component = 0) const;
template <int dim>
double BoundaryValues<dim>::value(const Point<dim>& p,
                                  const unsigned int component) const
    (void) component;
    Assert(component == 0, ExcIndexRange(component, 0, 1));
    const double sine_term =
       std::sin(16 * numbers::PI * std::sqrt(p.norm_square()));
    const double weight = std::exp(-5 * p.norm_square()) / std::exp(-5.);
    return sine_term * weight;
template <int dim>
void BoundaryValues<dim>::value_list(const std::vector<Point<dim>& points,
                                     std::vector<double>& values,
                                     const unsigned int component) const
    Assert(values.size() == points.size(),
          ExcDimensionMismatch(values.size(), points.size()));
    for (unsigned int i = 0; i < points.size(); ++i)
  values[i] = BoundaryValues<dim>::value(points[i], component);
class GradientEstimation {
public:
    template <int dim>
    static void estimate(const DoFHandler<dim>& dof,
                         const Vector<double>& solution.
```

```
Vector<float>& error_per_cell);
    DeclException2(ExcInvalidVectorLength, int, int, "Vector has length " « arg1 « ", but should have "
                   « arg2);
    DeclException0 (ExcInsufficientDirections);
private:
    template <int dim>
    struct EstimateScratchData {
        EstimateScratchData(const FiniteElement<dim>& fe,
                            const Vector<double>& solution,
                            Vector<float>& error_per_cell);
        EstimateScratchData(const EstimateScratchData& data):
        FEValues<dim> fe_midpoint_value;
        const Vector<double>& solution;
        Vector<float>& error_per_cell;
    };
    struct EstimateCopyData {};
    template <int dim>
    static void estimate_cell(
        const typename DoFHandler<dim>::active_cell_iterator& cell,
        EstimateScratchData<dim>& scratch_data,
        const EstimateCopyData& copy_data);
template <int dim>
AdvectionProblem<dim>::AdvectionProblem() : dof_handler(triangulation), fe(1)
{ }
template <int dim>
AdvectionProblem < dim > :: AdvectionProblem ()
    dof handler.clear();
template <int dim>
void AdvectionProblem<dim>::setup_system()
    dof_handler.distribute_dofs(fe);
    hanging_node_constraints.clear();
    DoFTools::make_hanging_node_constraints(dof_handler,
                                             hanging_node_constraints);
    hanging_node_constraints.close();
    DynamicSparsityPattern dsp(dof_handler.n_dofs(), dof_handler.n_dofs());
    DoFTools::make_sparsity_pattern(dof_handler, dsp, hanging_node_constraints,
                                    /*keep_constrained_dofs = */ true);
    sparsity_pattern.copy_from(dsp);
    system_matrix.reinit(sparsity_pattern);
    solution.reinit(dof_handler.n_dofs());
    system_rhs.reinit(dof_handler.n_dofs());
template <int dim>
void AdvectionProblem<dim>::assemble_system()
    WorkStream::run(dof_handler.begin_active(), dof_handler.end(), *this,
                    &AdvectionProblem::local_assemble_system,
                    &AdvectionProblem::copy_local_to_global,
                    AssemblyScratchData(fe), AssemblyCopyData());
    hanging_node_constraints.condense(system_matrix);
    hanging_node_constraints.condense(system_rhs);
template <int dim>
AdvectionProblem<dim>::AssemblyScratchData::AssemblyScratchData(
    const FiniteElement<dim>& fe)
    : fe_values(fe, QGauss<dim>(2),
                update_values | update_gradients | update_quadrature_points |
      update_JxW_values),
fe_face_values(fe, QGauss<dim - 1>(2),
                     update_values | update_quadrature_points |
                         update_JxW_values | update_normal_vectors)
template <int dim>
AdvectionProblem<dim>::AssemblyScratchData::AssemblyScratchData(
    const AssemblyScratchData& scratch_data)
    : fe_values(scratch_data.fe_values.get_fe(),
                scratch_data.fe_values.get_quadrature(),
                fe_face_values(scratch_data.fe_face_values.get_fe(),
                     scratch_data.fe_face_values.get_quadrature(),
                     update_values | update_quadrature_points |
                         update_JxW_values | update_normal_vectors)
template <int dim>
void AdvectionProblem<dim>::local_assemble_system(
    const typename DoFHandler<dim>::active_cell_iterator& cell,
    AssemblyScratchData& scratch_data, AssemblyCopyData& copy_data)
    const AdvectionField<dim> advection_field;
    const RightHandSide<dim> right_hand_side;
const BoundaryValues<dim> boundary_values;
```

```
const unsigned int dofs_per_cell = fe.dofs_per_cell;
    const unsigned int n_q_points =
        scratch_data.fe_values.get_quadrature().size();
    const unsigned int n_face_q_points =
       scratch_data.fe_face_values.get_quadrature().size();
    copy_data.cell_matrix.reinit(dofs_per_cell, dofs_per_cell);
    copy_data.cell_rhs.reinit(dofs_per_cell);
    copy_data.local_dof_indices.resize(dofs_per_cell);
    std::vector<double> rhs_values(n_q_points);
    std::vector<Tensor<1, dim» advection_directions(n_q_points);
std::vector<double> face_boundary_values(n_face_q_points);
    std::vector<Tensor<1, dim» face_advection_directions(n_face_q_points);
    scratch_data.fe_values.reinit(cell);
    advection_field.value_list(scratch_data.fe_values.get_quadrature_points(),
                                advection_directions);
    right_hand_side.value_list(scratch_data.fe_values.get_quadrature_points(),
                                rhs_values);
    const double delta = 0.1 * cell->diameter();
    for (unsigned int q_point = 0; q_point < n_q_points; ++q_point)</pre>
        for (unsigned int i = 0; i < dofs_per_cell; ++i) {</pre>
            for (unsigned int j = 0; j < dofs_per_cell; ++j)</pre>
                copy_data.cell_matrix(i, j) +=
                     ((advection\_directions[q\_point] *
                      \verb|scratch_data.fe_values.shape_grad(j, q_point)| *
                       (scratch_data.fe_values.shape_value(i, q_point) +
                       delta *
                            (advection_directions[q_point]
                             scratch_data.fe_values.shape_grad(i, q_point)))) *
                     scratch_data.fe_values.JxW(q_point));
            copy_data.cell_rhs(i) +=
                delta * (advection_directions[q_point] *
                            scratch_data.fe_values.shape_grad(i, q_point))) *
                 rhs_values[q_point] * scratch_data.fe_values.JxW(q_point));
    for (unsigned int face = 0; face < GeometryInfo<dim>::faces_per_cell;
         ++face)
        if (cell->face(face)->at_boundary()) {
            scratch_data.fe_face_values.reinit(cell, face);
            boundary_values.value_list(
                scratch_data.fe_face_values.get_quadrature_points(),
                face_boundary_values);
            advection field.value list (
                scratch_data.fe_face_values.get_quadrature_points(),
                face_advection_directions);
            for (unsigned int q_point = 0; q_point < n_face_q_points; ++q_point)</pre>
                if (scratch_data.fe_face_values.normal_vector(q_point) *
                         face_advection_directions[q_point] <</pre>
                     for (unsigned int i = 0; i < dofs_per_cell; ++i) {</pre>
                         for (unsigned int j = 0; j < dofs_per_cell; ++j)</pre>
                             copy_data.cell_matrix(i, j) -=
                                 (face_advection_directions[q_point] *
                                  scratch_data.fe_face_values.normal_vector(
                                      q_point) *
                                  scratch data.fe face values.shape value(
                                      i, q_point) *
                                  scratch_data.fe_face_values.shape_value(
                                      j, q_point) *
                                  \verb|scratch_data.fe_face_values.JxW(q_point)|;\\
                         copy_data.cell_rhs(i) -=
                             (face_advection_directions[q_point] *
                              scratch_data.fe_face_values.normal_vector(
                                  q_point) *
                              face_boundary_values[q_point] *
                              scratch_data.fe_face_values.shape_value(i,
                                                                        q_point) *
                              scratch_data.fe_face_values.JxW(q_point));
    cell->get_dof_indices(copy_data.local_dof_indices);
template <int dim>
void AdvectionProblem<dim>::copy_local_to_global(
    const AssemblyCopyData& copy_data)
    for (unsigned int i = 0; i < copy_data.local_dof_indices.size(); ++i) {</pre>
        for (unsigned int j = 0; j < copy_data.local_dof_indices.size(); ++j)</pre>
            system_matrix.add(copy_data.local_dof_indices[i],
                               copy_data.local_dof_indices[j],
        copy_data.cell_matrix(i, j));
system_rhs(copy_data.local_dof_indices[i]) += copy_data.cell_rhs(i);
template <int dim>
void AdvectionProblem<dim>::solve()
```

```
Assert(system_matrix.m() == system_matrix.n(), ExcNotQuadratic());
    auto num_rows = system_matrix.m();
    std::vector<double> rhs(num_rows);
    std::copy(system_rhs.begin(), system_rhs.begin() + num_rows, rhs.begin());
    using vec = gko::matrix::Dense<>;
using mtx = gko::matrix::Csr<>;
    using bicgstab = gko::solver::Bicgstab<>;
    using bj = gko::preconditioner::Jacobi<>;
    using val_array = gko::array<double>;
    std::shared_ptr<gko::Executor> exec = gko::ReferenceExecutor::create();
    auto b = vec::create(exec, gko::dim<2>(num_rows, 1),
                         val_array::view(exec, num_rows, rhs.data()), 1);
    auto x = vec::create(exec, gko::dim<2>(num_rows, 1));
auto A = mtx::create(exec, gko::dim<2>(num_rows),
                          system_matrix.n_nonzero_elements());
    mtx::value_type* values = A->get_values();
mtx::index_type* row_ptr = A->get_row_ptrs();
    mtx::index_type* col_idx = A->get_col_idxs();
    row_ptr[0] = 0;
    for (auto row = 1; row <= num_rows; ++row) {</pre>
        row_ptr[row] = row_ptr[row - 1] + system_matrix.get_row_length(row - 1);
    std::vector<mtx::index_type> ptrs(num_rows + 1);
    \verb|std::copy(A->get_row_ptrs(), A->get_row_ptrs() + num_rows + 1|,\\
              ptrs.begin());
    for (auto row = 0; row < system_matrix.m(); ++row) {</pre>
        for (auto p = system_matrix.begin(row); p != system_matrix.end(row);
             col_idx[ptrs[row]] = p->column();
             values[ptrs[row]] = p->value();
             ++ptrs[row];
        1
    auto solver_gen =
        bicgstab::build()
             .with criteria(
                 gko::stop::Iteration::build().with_max_iters(1000),
                 gko::stop::ResidualNorm<>::build().with_reduction_factor(1e-12))
             .with_preconditioner(bj::build())
             .on(exec);
    auto solver = solver_gen->generate(gko::give(A));
    solver->apply(b, x);
    std::copy(x->get_values(), x->get_values() + num_rows, solution.begin());
/*********
* deal.ii internal solver. Here for reference.
SolverControl
                         solver_control (1000, 1e-12);
SolverBicgstab<>
                        bicgstab (solver_control);
PreconditionJacobi<> preconditioner;
preconditioner.initialize(system_matrix, 1.0);
bicgstab.solve (system_matrix, solution, system_rhs,
preconditioner);
hanging_node_constraints.distribute(solution);
template <int dim>
void AdvectionProblem<dim>::refine_grid()
    Vector<float> estimated_error_per_cell(triangulation.n_active_cells());
    {\tt GradientEstimation::estimate(dof\_handler, solution,}
                                  estimated error per cell);
    GridRefinement::refine_and_coarsen_fixed_number(
        triangulation, estimated_error_per_cell, 0.5, 0.03);
    triangulation.execute_coarsening_and_refinement();
template <int dim>
void AdvectionProblem < dim >:: output results (const unsigned int cycle) const
    {
        GridOut grid_out;
        std::ofstream output("grid-" + std::to_string(cycle) + ".eps");
        grid_out.write_eps(triangulation, output);
        DataOut<dim> data_out;
        data_out.attach_dof_handler(dof_handler);
        data_out.add_data_vector(solution, "solution");
        data_out.build_patches();
std::ofstream output("solution-" + std::to_string(cycle) + ".vtk");
        data_out.write_vtk(output);
template <int dim>
void AdvectionProblem<dim>::run()
    for (unsigned int cycle = 0; cycle < 6; ++cycle) {</pre>
```

```
std::cout « "Cycle " « cycle « ':' « std::endl;
        if (cycle == 0) {
            GridGenerator::hyper_cube(triangulation, -1, 1);
            triangulation.refine_global(4);
        } else {
           refine_grid();
        std::cout « " Number of active cells:
                  « triangulation.n_active_cells() « std::endl;
        setup_system();
std::cout « "
                       Number of degrees of freedom: " « dof_handler.n_dofs()
                 « std::endl;
        assemble_system();
        solve();
        output_results(cycle);
template <int dim>
GradientEstimation::EstimateScratchData<dim>::EstimateScratchData(
    const FiniteElement<dim>& fe, const Vector<double>& solution,
    Vector<float>& error_per_cell)
    : fe_midpoint_value(fe, QMidpoint<dim>(),
                       update_values | update_quadrature_points),
      solution(solution),
      error_per_cell(error_per_cell)
{ }
template <int dim>
GradientEstimation::EstimateScratchData<dim>::EstimateScratchData(
    const EstimateScratchData& scratch_data)
    : fe_midpoint_value(scratch_data.fe_midpoint_value.get_fe(),
                        scratch_data.fe_midpoint_value.get_quadrature(),
                        update_values | update_quadrature_points),
      solution(scratch_data.solution),
      error_per_cell(scratch_data.error_per_cell)
template <int dim>
void GradientEstimation::estimate(const DoFHandler<dim>& dof_handler,
                                  const Vector<double>& solution,
                                  Vector<float>& error_per_cell)
    Assert(error_per_cell.size() ==
               {\tt dof\_handler.get\_triangulation().n\_active\_cells(),}
           ExcInvalidVectorLength(
               error_per_cell.size(),
               dof_handler.get_triangulation().n_active_cells()));
    WorkStream::run(dof_handler.begin_active(), dof_handler.end(),
                    &GradientEstimation::template estimate_cell<dim>,
                    std::function<void(const EstimateCopyData&)>(),
                    EstimateScratchData<dim>(dof_handler.get_fe(), solution,
                                             error_per_cell),
                    EstimateCopyData());
template <int dim>
void GradientEstimation::estimate_cell(
    const typename DoFHandler<dim>::active_cell_iterator& cell,
    EstimateScratchData<dim>& scratch_data, const EstimateCopyData&)
    std::vector<typename DoFHandler<dim>::active_cell_iterator>
       active_neighbors;
    active_neighbors.reserve(GeometryInfo<dim>::faces_per_cell \star
                            GeometryInfo<dim>::max_children_per_face);
    scratch_data.fe_midpoint_value.reinit(cell);
    Tensor<1, dim> projected_gradient;
    active_neighbors.clear();
    for (unsigned int face_no = 0; face_no < GeometryInfo<dim>::faces_per_cell;
         ++face no)
        if (!cell->at boundary(face no)) {
            const typename DoFHandler<dim>::face_iterator face =
                cell->face(face_no);
            const typename DoFHandler<dim>::cell_iterator neighbor =
                cell->neighbor(face_no);
            if (neighbor->active())
                active_neighbors.push_back(neighbor);
            else {
                if (dim == 1) {
                    typename DoFHandler<dim>::cell_iterator neighbor_child =
                        neighbor;
                    while (neighbor_child->has_children())
                        neighbor child =
                           neighbor_child->child(face_no == 0 ? 1 : 0);
                    Assert (
                        neighbor_child->neighbor(face_no == 0 ? 1 : 0) == cell,
                        ExcInternalError());
                    active_neighbors.push_back(neighbor_child);
                } else
                    for (unsigned int subface no = 0;
```

```
subface_no < face->n_children(); ++subface_no)
                         active_neighbors.push_back(
                              cell->neighbor_child_on_subface(face_no,
                                                                 subface_no));
    const Point<dim> this_center =
        scratch_data.fe_midpoint_value.quadrature_point(0);
    std::vector<double> this_midpoint_value(1);
    scratch_data.fe_midpoint_value.get_function_values(scratch_data.solution,
                                                           this_midpoint_value);
    std::vector<double> neighbor midpoint value(1);
    typename std::vector<typename DoFHandler<dim>::active_cell_iterator>::
        const_iterator neighbor_ptr = active_neighbors.begin();
    for (; neighbor_ptr != active_neighbors.end(); ++neighbor_ptr) {
        const typename DoFHandler<dim>::active_cell_iterator neighbor =
            *neighbor_ptr;
        scratch_data.fe_midpoint_value.reinit(neighbor);
        const Point<dim> neighbor_center =
            scratch_data.fe_midpoint_value.quadrature_point(0);
        scratch_data.fe_midpoint_value.get_function_values(
            scratch_data.solution, neighbor_midpoint_value);
        Tensor<1, dim> y = neighbor_center - this_center;
        const double distance = y.norm();
        y /= distance;
        for (unsigned int i = 0; i < dim; ++i)</pre>
             for (unsigned int j = 0; j < dim; ++j) Y[i][j] += y[i] * y[j];
        projected_gradient +=
             (neighbor_midpoint_value[0] - this_midpoint_value[0]) / distance *
    AssertThrow(determinant(Y) != 0, ExcInsufficientDirections());
const Tensor<2, dim> Y_inverse = invert(Y);
    Tensor<1, dim> gradient = Y_inverse * projected_gradient;
    scratch_data.error_per_cell(cell->active_cell_index()) =
   (std::pow(cell->diameter(), 1 + 1.0 * dim / 2) *
         std::sqrt(gradient.norm_square()));
   // namespace Step9
int main()
        dealii::MultithreadInfo::set thread limit():
        Step9::AdvectionProblem<2> advection_problem_2d;
        advection_problem_2d.run();
    } catch (std::exception& exc)
        std::cerr « std::endl
                   « std::endl
                   «
                   « std::endl;
        std::cerr « "Exception on processing: " « std::endl
                   « exc.what() « std::endl
« "Aborting!" « std::endl
                   « std::endl;
        return 1;
    } catch (...) {
        std::cerr « std::endl
                   « std::endl
« "-----
                   « std::endl:
        std::cerr « "Unknown exception!" « std::endl
                   « "Aborting!" « std::endl
                   « std::endl;
        return 1:
    return 0:
```

# **Chapter 16**

# The file-config-solver program

The file config solver example..

This example depends on simple-solver.

# This example shows how to use file to configure solver.

In this example, we first read in a matrix from a file. Then we read the config file to configure the solver. The example application reports the generation and run time of the solver.

# The commented program

```
const std::string matrix_path = argc >= 4 ? argv[3] : "data/A.mtx";
Figure out where to run the code
std::map<std::string, std::function<std::shared_ptr<gko::Executor>()»
                [] { return gko::OmpExecutor::create(); }},
         {"cuda",
             return gko::CudaExecutor::create(0,
                                                gko::OmpExecutor::create());
             return gko::HipExecutor::create(0, gko::OmpExecutor::create());
         }},
        { "dpcpp",
             return gko::DpcppExecutor::create(
                  0, gko::ReferenceExecutor::create());
        {"reference", [] { return gko::ReferenceExecutor::create(); }}};
executor where Ginkgo will perform the computation
const auto exec = exec_map.at(executor_string)(); // throws if not valid
Read data
auto A = share(gko::read<mtx>(std::ifstream(matrix_path), exec));
Create RHS as 1 and initial guess as 0
gko::size_type size = A->get_size()[0];
auto host_x = vec::create(exec->get_master(), gko::dim<2>(size, 1));
auto host_b = vec::create(exec->get_master(), gko::dim<2>(size, 1));
for (auto i = 0; i < size; i++) {
    host_x->at(i, 0) = 0.;
    host_b->at(i, 0) = 1.;
```

```
auto x = vec::create(exec);
auto b = vec::create(exec);
x->copy_from(host_x);
b->copy_from(host_b);
```

#### Calculate initial residual by overwriting b

```
auto one = gko::initialize<vec>({1.0}, exec);
auto neg_one = gko::initialize<vec>({-1.0}, exec);
auto initres = gko::initialize<vec>({0.0}, exec);
A->apply(one, x, neg_one, b);
b->compute_norm2(initres);
```

#### Copy b again

```
b->copy_from(host_b);
```

Read the json config file to configure the ginkgo solver. The following files, which are mapped to corresponding examples, are available cg.json: simple-solver blockjacobi-cg.json: preconditioned-solver ir.json: iterative-refinement parilu.json: ilu-preconditioned-solver (by using factoization parameter directly) pgm-multigrid-cg.json: multigrid-preconditioned-solver (set min\_coarse\_rows additionally due to this small example matrix) mixed-pgm-multigrid-cg.json: mixed-multigrid-preconditioned-solver (assuming there are always more than one level)

auto config = gko::ext::config::parse\_json\_file(configfile);

Create the registry, which allows passing the existing data into config This example does not use existing data.

auto reg = gko::config::registry();

Create the default type descriptor, which gives the default common type (value/index) for solver generation. If the solver does not specify value type, the solver will use these types.

```
auto td = gko::config::make_type_descriptor<ValueType, IndexType>();
```

#### generate the linopfactory on the given executors

```
auto solver_gen = gko::config::parse(config, reg, td).on(exec);
```

#### Create solver

#### Add logger

```
std::shared_ptr<const gko::log::Convergence<ValueType» logger =
    gko::log::Convergence<ValueType>::create();
solver->add_logger(logger);
```

#### Solve system

```
exec->synchronize();
const auto tic = std::chrono::steady_clock::now();
solver->apply(b, x);
exec->synchronize();
const auto toc = std::chrono::steady_clock::now();
const auto time =
    std::chrono::duration_cast<std::chrono::milliseconds>(toc - tic);
```

#### Print out the solver config

```
std::cout « "Config file: " « configfile « std::endl;
std::ifstream f(configfile);
std::cout « f.rdbuf() « std::endl;
```

#### Calculate residual

```
auto res = gko::as<vec>(logger->get_residual_norm());
std::cout « "Initial residual norm sqrt(r^T r): \n";
write(std::cout, initres);
std::cout « "Final residual norm sqrt(r^T r): \n";
write(std::cout, res);
```

#### Print solver statistics

#### Results

```
This is the expected output:
Config file: config/cg.json
    "type": "solver::Cg",
    "criteria": [
             "type": "Iteration",
             "max_iters": 20
             "type": "ResidualNorm",
             "reduction_factor": 1e-7
    ]
Initial residual norm sqrt(r^T r):
%%MatrixMarket matrix array real general
25.9808
Final residual norm sqrt(r^T r):
%%MatrixMarket matrix array real general
Solver iteration count:
Solver generation time [ms]: 0.065244
Solver execution time [ms]: 0.793764
Solver execution time per iteration[ms]: 0.0396882
```

#### Comments about programming and debugging

# The plain program

```
#include <fstream>
#include <iomanip>
#include <iostream>
#include <map>
#include <string>
#include <ginkgo/ginkgo.hpp>
#include <ginkgo/extensions/config/json_config.hpp>
int main(int argc, char* argv[])
     using ValueType = double;
     using IndexType = int;
     using vec = gko::matrix::Dense<ValueType>;
     using mtx = gko::matrix::Csr<ValueType, IndexType>;
    std::cout « gko::version_info::get() « std::endl;
std::cout « argv[0] « " executor configfile matrix" « std::endl;
const auto executor_string = argc >= 2 ? argv[1] : "reference";
const auto configfile = argc >= 3 ? argv[2] : "config/cg.json";
const std::string matrix_path = argc >= 4 ? argv[3] : "data/A.mtx";
     std::map<std::string, std::function<std::shared_ptr<gko::Executor>()»
                {"omp", [] { return gko::OmpExecutor::create(); }},
                {"cuda",
                 [] {
                      return gko::CudaExecutor::create(0,
                                                                   gko::OmpExecutor::create());
                {"hip",
                 [] {
                      return gko::HipExecutor::create(0, gko::OmpExecutor::create());
                { "dpcpp",
                 [] {
                     return gko::DpcppExecutor::create(
                            0, gko::ReferenceExecutor::create());
                {"reference", [] { return gko::ReferenceExecutor::create(); }}};
     const auto exec = exec_map.at(executor_string)(); // throws if not valid
     auto A = share(gko::read<mtx>(std::ifstream(matrix_path), exec));
     gko::size_type size = A->get_size()[0];
     auto host_x = vec::create(exec->get_master(), gko::dim<2>(size, 1));
auto host_b = vec::create(exec->get_master(), gko::dim<2>(size, 1));
for (auto i = 0; i < size; i++) {
   host_x->at(i, 0) = 0.;
          host_b->at(i, 0) = 1.;
```

```
auto x = vec::create(exec);
auto b = vec::create(exec);
x->copy_from(host_x);
b->copy_from(host_b);
auto one = gko::initialize<vec>({1.0}, exec);
auto neg_one = gko::initialize<vec>((-1.0), exec);
auto initres = gko::initialize<vec>({0.0}, exec);
A->apply(one, x, neg_one, b);
b->compute_norm2(initres);
b->copy_from(host_b);
auto config = gko::ext::config::parse_json_file(configfile);
auto reg = gko::config::registry();
auto td = gko::config::make_type_descriptor<ValueType, IndexType>();
auto solver_gen = gko::config::parse(config, reg, td).on(exec);
const auto gen_tic = std::chrono::steady_clock::now();
auto solver = solver_gen->generate(A);
exec->synchronize();
const auto gen_toc = std::chrono::steady_clock::now();
const auto gen_time = std::chrono::duration_cast<std::chrono::milliseconds>(
   gen_toc - gen_tic);
std::shared_ptr<const gko::log::Convergence<ValueType» logger =</pre>
   gko::log::Convergence<ValueType>::create();
solver->add_logger(logger);
exec->synchronize();
const auto tic = std::chrono::steady_clock::now();
solver->apply(b, x);
exec->synchronize();
const auto toc = std::chrono::steady_clock::now();
const auto time =
   std::chrono::duration_cast<std::chrono::milliseconds>(toc - tic);
std::cout « "Config file:
                           " « configfile « std::endl;
std::ifstream f(configfile);
std::cout « f.rdbuf() « std::endl;
auto res = gko::as<vec>(logger->get_residual_norm()); std::cout « "Initial residual norm sqrt(r^T r): \n";
write(std::cout, initres);
std::cout « "Final residual norm sqrt(r^T r): \n";
write(std::cout, res);
std::cout « "Solver iteration count:
                                              " « logger->get_num_iterations()
« static_cast<double>(gen_time.count()) « std::endl;
std::cout « "Solver execution time [ms]:
« static_cast<double>(time.count()) /
                logger->get_num_iterations()
          « std::endl;
```

# **Chapter 17**

# The ginkgo-overhead program

The ginkgo overhead measurement example..

### Introduction

About the example

# The commented program

```
num_iters = std::atol(argv[1]);
    if (num_iters == 0) {
        print_usage_and_exit(argv[0]);
std::cout « gko::version_info::get() « std::endl;
auto exec = gko::ReferenceExecutor::create();
auto cg_factory =
  cg::build()
       .with_criteria(
            gko::stop::Iteration::build().with_max_iters(num_iters))
        .on(exec);
auto A = gko::initialize<mtx>({1.0}, exec);
auto b = gko::initialize<vec>({std::nan("")}, exec);
auto x = gko::initialize<vec>((0.0), exec);
auto tic = std::chrono::steady_clock::now();
auto solver = cg_factory->generate(gko::give(A));
solver->apply(x, b);
exec->synchronize();
auto tac = std::chrono::steady_clock::now();
auto time = std::chrono::duration_cast<std::chrono::nanoseconds>(tac - tic);
std::cout « "Running " « num_iters
          « " iterations of the CG solver took a total of "
          « static_cast<double>(time.count()) /
                  static_cast<double>(std::nano::den)
           « " seconds." « std::endl
           « "\tAverage library overhead:
```

### Results

#### This is the expected output:

```
Running 1000000 iterations of the CG solver took a total of 1.60337 seconds.

Average library overhead: 1603.37 [nanoseconds / iteration]
```

#### Comments about programming and debugging

## The plain program

```
#include <chrono>
#include <cmath>
#include <iostream>
#include <ginkgo/ginkgo.hpp>
[[noreturn]] void print_usage_and_exit(const char* name)
    std::cerr « "Usage: " « name « " [NUM_ITERS]" « std::endl;
    std::exit(-1);
int main(int argc, char* argv[])
    using ValueType = double;
    using IndexType = int;
using vec = gko::matrix::Dense<ValueType>;
    using mtx = gko::matrix::Csr<ValueType, IndexType>;
    using cg = gko::solver::Cg<ValueType>;
    long unsigned num_iters = 1000000;
    if (argc > 2) {
        print_usage_and_exit(argv[0]);
    if (argc == 2) {
        num_iters = std::atol(argv[1]);
        if (num_iters == 0) {
            print_usage_and_exit(argv[0]);
    std::cout « gko::version_info::get() « std::endl;
    auto exec = gko::ReferenceExecutor::create();
    auto cg_factory =
       cg::build()
            .with_criteria(
                gko::stop::Iteration::build().with_max_iters(num_iters))
            .on(exec);
    auto A = gko::initialize<mtx>({1.0}, exec);
    auto b = gko::initialize<vec>({std::nan("")}, exec);
    auto x = gko::initialize<vec>((0.0), exec);
auto tic = std::chrono::steady_clock::now();
auto solver = cg_factory->generate(gko::give(A));
    solver->apply(x, b);
    exec->synchronize();
    auto tac = std::chrono::steady_clock::now();
    « static_cast<double>(time.count()) /
                     static_cast<double>(std::nano::den)
              « " seconds." « std::endl
              « "\tAverage library overhead:
              « static_cast<double>(time.count()) /
              static_cast<double>(num_iters)
« " [nanoseconds / iteration] " « std::endl;
```

# **Chapter 18**

# The ginkgo-ranges program

The ranges and accessor example..

### Introduction

About the example

## The commented program

```
a utility function for printing the factorization on screen
```

```
template <typename Accessor>
void print_lu(const gko::range<Accessor>& A)
{
    std::cout « std::setprecision(2) « std::fixed;
    std::cout « "L = [";
    for (int i = 0; i < A.length(0); ++i) {
        std::cout « "\n ";
        for (int j = 0; j < A.length(1); ++j) {
            std::cout « (i > j ? A(i, j) : (i == j) * 1.) « " ";
        }
    }
    std::cout « "\n]\n\nU = [";
    for (int i = 0; i < A.length(0); ++i) {
        std::cout « "\n ";
        for (int j = 0; j < A.length(1); ++j) {
            std::cout « (i <= j ? A(i, j) : 0.) « " ";
        }
    }
    std::cout « "\n] " « std::endl;
}
int main(int argc, char* argv[])
{
    using ValueType = double;
    using IndexType = int;</pre>
```

#### Print version information

```
std::cout « gko::version_info::get() « std::endl;
```

Create some test data, add some padding just to demonstrate how to use it with ranges. clang-format off

```
ValueType data[] = {
    2., 4., 5., -1.0,
    4., 11., 12., -1.0,
    6., 24., 24., -1.0
};
```

clang-format on

Create a 3-by-3 range, with a 2D row-major accessor using data as the underlying storage. Set the stride (a.k.a. "LDA") to 4.

```
auto \hat{A} = gko::range<gko::accessor::row_major<ValueType, 2>>(data, 3u, 3u, 4u);
```

use the LU factorization routine defined above to factorize the matrix

factorize(A);

print the factorization on screen

```
print_lu(A);
```

### Results

This is the expected output:

```
L = [
    1.00 0.00 0.00
    2.00 1.00 0.00
]
U = [
    2.00 4.00 5.00
    0.00 3.00 2.00
    0.00 0.00 1.00
```

#### Comments about programming and debugging

### The plain program

```
#include <iomanip>
#include <iostream>
#include <ginkgo/ginkgo.hpp>
template <typename Accessor>
void factorize(const gko::range<Accessor>& A)
      using gko::span;
      assert(A.length(0) == A.length(1));
     asser(A.length(0) == A.length(1));
for (gko::size_type i = 0; i < A.length(0) - 1; ++i) {
   const auto trail = span{i + 1, A.length(0)};
   A(trail, i) = A(trail, i) / A(i, i);
   A(trail, trail) = A(trail, trail) - mmul(A(trail, i), A(i, trail));</pre>
template <typename Accessor>
void print_lu(const gko::range<Accessor>& A)
      std::cout « std::setprecision(2) « std::fixed;
      std::cout « "L = [";
for (int i = 0; i < A.length(0); ++i) {</pre>
           for (int j = 0; j < A.length(0); ++j) {
    std::cout « "\n ";
    for (int j = 0; j < A.length(1); ++j) {
        std::cout « (i > j ? A(i, j) : (i == j) * 1.) « " ";
    }
}
     std::cout « "\n]\n\nU = [";
for (int i = 0; i < A.length(0); ++i) {
    std::cout « "\n ";
    for (int j = 0; j < A.length(1); ++j) {</pre>
                 std::cout « (i <= j ? A(i, j) : 0.) « " ";
      std::cout « "\n]" « std::endl;
int main(int argc, char* argv[])
      using ValueType = double;
      using IndexType = int;
      std::cout « gko::version_info::get() « std::endl;
      ValueType data[] = {
           2., 4., 5., -1.0,
4., 11., 12., -1.0,
            6., 24., 24., -1.0
           gko::range<gko::accessor::row_major<ValueType, 2>>(data, 3u, 3u, 4u);
      factorize(A);
     print_lu(A);
```

# **Chapter 19**

# The heat-equation program

The heat equation example..

This example depends on simple-solver, three-pt-stencil-solver.

### Introduction

This example solves a 2D heat conduction equation

$$u: [0, d]^2 \to R$$
  
 $\partial_t u = \delta u + f$ 

with Dirichlet boundary conditions and given initial condition and constant-in-time source function f.

The partial differential equation (PDE) is solved with a finite difference spatial discretization on an equidistant grid: For n grid points, and grid distance h=1/n we write

$$u_{i,j}' = \alpha \frac{u_{i-1,j} + u_{i+1,j} + u_{i,j-1} + u_{i,j+1} - 4u_{i,j}}{h^2} + f_{i,j}$$

We then build an implicit Euler integrator by discretizing with time step au

$$\frac{u_{i,j}^{k+1} - u_{i,j}^k}{\tau} = \alpha \frac{u_{i-1,j}^{k+1} + u_{i+1,j}^{k+1} - u_{i,j-1}^{k+1} - u_{i,j+1}^{k+1} + 4u_{i,j}^{k+1}}{h^2} + f_{i,j}$$

and solve the resulting linear system for  $u^{k+1}$  using Ginkgo's CG solver preconditioned with an incomplete Cholesky factorization for each time step, occasionally writing the resulting grid values into a video file using OpenCV and a custom color mapping.

The intention of this example is to provide a mini-app showing matrix assembly, vector initialization, solver setup and the use of Ginkgo in a more complex setting.

#### About the example

### The commented program

```
The intention of this example is to provide a mini-app showing matrix assembly,
vector initialization, solver setup and the use of Ginkgo in a more complex
setting.
#include <chrono>
#include <fstream>
#include <iostream>
#include <opencv2/core.hpp>
#include <opencv2/videoio.hpp>
#include <ginkgo/ginkgo.hpp>
This function implements a simple Ginkgo-themed clamped color mapping for values in the range [0,5].
void set_val(unsigned char* data, double value)
RGB values for the 6 colors used for values 0, 1, ..., 5 We will interpolate linearly between these values.
double col_r[] = {255, 221, 129, 201, 249, 255}; double col_g[] = {255, 220, 130, 161, 158, 204};
double col_b[] = {255, 220, 133, 93, 24, 8};
value = std::max(0.0, value);
auto i = std::max(0, std::min(4, int(value)));
auto d = std::max(0.0, std::min(1.0, value - i));
OpenCV uses BGR instead of RGB by default, revert indices
    \label{eq:data0} \texttt{data[0]} = \texttt{static\_cast} < \texttt{unsigned char} > (\texttt{col\_b[i + 1]} * \texttt{d + col\_b[i]} * (1 - \texttt{d}));
Initialize video output with given dimension and FPS (frames per seconds)
std::pair<cv::VideoWriter, cv::Mat> build_output(int n, double fps)
    cv::Size videosize{n, n};
    auto output =
       std::make_pair(cv::VideoWriter{}, cv::Mat{videosize, CV_8UC3});
    auto fourcc = cv::VideoWriter::fourcc('a', 'v', 'c', '1');
    output.first.open("heat.mp4", fourcc, fps, videosize);
Write the current frame to video output using the above color mapping
void output_timestep(std::pair<cv::VideoWriter, cv::Mat>& output, int n,
                      const double* data)
    for (int i = 0; i < n; i++) {</pre>
        auto row = output.second.ptr(i);
for (int j = 0; j < n; j++) {
            set_val(&row[3 * j], data[i * n + j]);
    output.first.write(output.second);
int main(int argc, char* argv[])
    using mtx = gko::matrix::Csr<>;
    using vec = gko::matrix::Dense<>;
Problem parameters: simulation length
diffusion factor
auto diffusion = 0.0005;
scaling factor for heat source
auto source_scale = 2.5;
Simulation parameters: inner grid points per discretization direction
```

number of simulation steps per second

auto steps\_per\_sec = 500;

auto n = 256;

```
number of video frames per second
auto fps = 25;
number of grid points
auto n2 = n * n;
grid point distance (ignoring boundary points)
auto h = 1.0 / (n + 1);
auto h2 = h * h;
time step size for the simulation
auto tau = 1.0 / steps_per_sec;
create a CUDA executor with an associated OpenMP host executor
auto exec = gko::CudaExecutor::create(0, gko::OmpExecutor::create());
load heat source and initial state vectors
std::ifstream initial_stream("data/gko_logo_2d.mtx");
std::ifstream source_stream("data/gko_text_2d.mtx");
auto source = gko::read<vec>(source_stream, exec);
auto in_vector = gko::read<vec>(initial_stream, exec);
create output vector with initial guess for
auto out_vector = in_vector->clone();
create scalar for source update
auto tau source scalar = gko::initialize<vec>({source scale * tau}, exec);
create stencil matrix as shared_ptr for solver
auto stencil_matrix = gko::share(mtx::create(exec));
assemble matrix
gko::matrix_data<> mtx_data{gko::dim<2>(n2, n2)};
for (int i = 0; i < n; i++) {
    for (int j = 0; j < n; j++) {
        auto c = i * n + j;
        auto c_val = diffusion * tau * 4.0 / h2 + 1.0;
        auto off_val = -diffusion * tau / h2;
for each grid point: insert 5 stencil points with Dirichlet boundary conditions, i.e. with zero boundary value
            mtx_data.nonzeros.emplace_back(c, c - n, off_val);
         if (j > 0) {
             mtx_data.nonzeros.emplace_back(c, c - 1, off_val);
        mtx data.nonzeros.emplace back(c, c, c val);
        if (j < n - 1) {
            mtx_data.nonzeros.emplace_back(c, c + 1, off_val);
         if (i < n - 1) {
             mtx_data.nonzeros.emplace_back(c, c + n, off_val);
stencil_matrix->read(mtx_data);
prepare video output
auto output = build_output(n, fps);
build CG solver on stencil with incomplete Cholesky preconditioner stopping at 1e-10 relative accuracy
auto solver =
    gko::solver::Cq<>::build()
        .with_preconditioner(gko::preconditioner::Ic<>::build())
         .with_criteria(gko::stop::ResidualNorm<>::build()
                             .with_baseline(gko::stop::mode::rhs_norm)
                             .with_reduction_factor(1e-10))
         .on(exec)
         ->generate(stencil matrix);
```

time stamp of the last output frame (initialized to a sentinel value)

double last\_t = -t0;

execute implicit Euler method: for each timestep, solve stencil system

```
for (double t = 0; t < t0; t += tau) {</pre>
if enough time has passed, output the next video frame
if (t - last_t > 1.0 / fps) {
    last_t = t;
    std::cout « t « std::endl;
    output_timestep(
        output, n,
        gko::make_temporary_clone(exec->get_master(), in_vector)
            ->get_const_values());
add heat source contribution
in vector->add scaled(tau source scalar, source);
execute Euler step
solver->apply(in_vector, out_vector);
swap input and output
        std::swap(in_vector, out_vector);
}
```

#### Results

The program will generate a video file named heat.mp4 and output the timestamp of each generated frame.

#### Comments about programming and debugging

## The plain program

```
This example solves a 2D heat conduction equation
u : [0, d]^2 \rightarrow R 
\partial_t u = \det u + f
with Dirichlet boundary conditions and given initial condition and
constant-in-time source function f.
The partial differential equation (PDE) is solved with a finite difference
spatial discretization on an equidistant grid: For 'n' grid points,
and grid distance @f$h = 1/n@f$ we write
u_{i,j}' = \alpha(u_{i-1,j} + u_{i+1,j} + u_{i,j-1} + u_{i,j+1})
 4 u_{i,j}) / h^2
+ f_{i,j}
We then build an implicit Euler integrator by discretizing with time step @f$\to.011
(u_{i,j}^{k+1} - u_{i,j}^k) / tau =
\alpha = u_{i+1,j}^{k+1} - u_{i+1,j}^{k+1}
 u_{i,j-1}^{k+1} - u_{i,j+1}^{k+1} - 4 u_{i,j}^{k+1}) / h^2
and solve the resulting linear system for @f$ u_{\c^{k+1}}@f$ using Ginkgo's CG solver preconditioned with an incomplete Cholesky factorization for each time
step, occasionally writing the resulting grid values into a video file using
OpenCV and a custom color mapping.
The intention of this example is to provide a mini-app showing matrix assembly,
vector initialization, solver setup and the use of Ginkgo in a more complex
setting.
#include <chrono>
#include <fstream>
#include <iostream>
#include <opencv2/core.hpp>
#include <opencv2/videoio.hpp>
#include <ginkgo/ginkgo.hpp>
void set_val(unsigned char* data, double value)
```

```
double col_r[] = \{255, 221, 129, 201, 249, 255\};
     double col_g[] = {255, 220, 130, 161, 158, 204}; double col_b[] = {255, 220, 133, 93, 24, 8};
     value = std::max(0.0, value);
     auto i = std::max(0, std::min(4, int(value)));
auto d = std::max(0.0, std::min(1.0, value - i));
data[2] = static_cast<unsigned char>(col_r[i + 1] * d + col_r[i] * (1 - d));
     \label{eq:data} \texttt{data[1] = static\_cast} < \texttt{unsigned char} < (\texttt{col\_g[i + 1]} * \texttt{d + col\_g[i]} * (1 - \texttt{d}));
     \label{eq:data0} \texttt{data[0]} = \texttt{static\_cast} < \texttt{unsigned char} > (\texttt{col\_b[i + 1]} * \texttt{d + col\_b[i]} * (1 - \texttt{d}));
std::pair<cv::VideoWriter, cv::Mat> build_output(int n, double fps)
     cv::Size videosize{n, n};
     auto output
         std::make_pair(cv::VideoWriter{}, cv::Mat{videosize, CV_8UC3});
     auto fourcc = cv::VideoWriter::fourcc('a', 'v', 'c', 'l');
output.first.open("heat.mp4", fourcc, fps, videosize);
     return output;
void output_timestep(std::pair<cv::VideoWriter, cv::Mat>& output, int n,
     for (int i = 0; i < n; i++) {</pre>
          auto row = output.second.ptr(i);
for (int j = 0; j < n; j++) {</pre>
              set_val(&row[3 * j], data[i * n + j]);
     output.first.write(output.second);
int main(int argc, char* argv[])
     using mtx = gko::matrix::Csr<>;
     using vec = gko::matrix::Dense<>;
     auto t0 = 5.0;
     auto diffusion = 0.0005;
     auto source scale = 2.5;
     auto n = 256;
     auto steps_per_sec = 500;
     auto fps = 25;
     auto n2 = n * n;
auto h = 1.0 / (n + 1);
     auto h2 = h * h;
     auto tau = 1.0 / steps_per_sec;
     auto exec = gko::CudaExecutor::create(0, gko::OmpExecutor::create());
     std::ifstream initial_stream("data/gko_logo_2d.mtx");
     std::ifstream source_stream("data/gko_text_2d.mtx");
     auto source = gko::read<vec>(source_stream, exec);
     auto in_vector = gko::read<vec>(initial_stream, exec);
auto out_vector = in_vector->clone();
     auto tau_source_scalar = gko::initialize<vec>((source_scale * tau), exec);
     auto stencil_matrix = gko::share(mtx::create(exec));
     gko::matrix_data<> mtx_data{gko::dim<2>(n2, n2)};
     for (int i = 0; i < n; i++) {
   for (int j = 0; j < n; j++) {
     auto c = i * n + j;
     auto c_val = diffusion * tau * 4.0 / h2 + 1.0;</pre>
               auto off_val = -diffusion * tau / h2;
               if (i > 0) {
                    mtx_data.nonzeros.emplace_back(c, c - n, off_val);
               if (j > 0) {
                    mtx_data.nonzeros.emplace_back(c, c - 1, off_val);
               mtx_data.nonzeros.emplace_back(c, c, c_val);
               if (j < n - 1) {</pre>
                    mtx_data.nonzeros.emplace_back(c, c + 1, off_val);
               if (i < n - 1) {
                    mtx_data.nonzeros.emplace_back(c, c + n, off_val);
     stencil matrix->read(mtx data);
     auto output = build_output(n, fps);
     auto solver =
          gko::solver::Cq<>::build()
              .with_preconditioner(gko::preconditioner::Ic<>::build())
               .with_criteria(gko::stop::ResidualNorm<>::build()
                                       .with baseline (gko::stop::mode::rhs norm)
                                       .with reduction factor(1e-10))
               .on(exec)
               ->generate(stencil_matrix);
     double last_t = -t0;
for (double t = 0; t < t0; t += tau) {
   if (t - last_t > 1.0 / fps) {
               last t = t;
```

# The ilu-preconditioned-solver program

The ILU-preconditioned solver example..

This example depends on simple-solver.

## Introduction

### About the example

This example shows how to use incomplete factors generated via the ParlLU algorithm to generate an incomplete factorization (ILU) preconditioner, how to specify the sparse triangular solves in the ILU preconditioner application, and how to generate an ILU-preconditioned solver and apply it to a specific problem.

```
const auto executor_string = argc >= 2 ? argv[1] : "reference";
Figure out where to run the code
std::map<std::string, std::function<std::shared_ptr<gko::Executor>()»
    exec_map{
         {"omp", [] { return gko::OmpExecutor::create(); }},
         {"cuda",
              return gko::CudaExecutor::create(0,
                                                 gko::OmpExecutor::create());
         {"hip",
              return gko::HipExecutor::create(0, gko::OmpExecutor::create());
         {"dpcpp",
              return gko::DpcppExecutor::create(0,
                                                  gko::OmpExecutor::create());
         {"reference", [] { return gko::ReferenceExecutor::create(); }};
executor where Ginkgo will perform the computation
const auto exec = exec_map.at(executor_string)(); // throws if not valid
Read data
auto A = gko::share(gko::read<mtx>(std::ifstream("data/A.mtx"), exec));
auto b = gko::read<vec>(std::ifstream("data/b.mtx"), exec);
auto x = gko::read<vec>(std::ifstream("data/x0.mtx"), exec);
```

### Generate incomplete factors using ParILU

```
auto par_ilu_fact =
    gko::factorization::ParIlu<ValueType, IndexType>::build().on(exec);
```

#### Generate concrete factorization for input matrix

```
auto par_ilu = gko::share(par_ilu_fact->generate(A));
```

Generate an ILU preconditioner factory by setting lower and upper triangular solver - in this case the exact triangular solves

### Use incomplete factors to generate ILU preconditioner

```
auto ilu_preconditioner = gko::share(ilu_pre_factory->generate(par_ilu));
```

Use preconditioner inside GMRES solver factory Generating a solver factory tied to a specific preconditioner makes sense if there are several very similar systems to solve, and the same solver+preconditioner combination is expected to be effective.

### Generate preconditioned solver for a specific target system

```
auto ilu_gmres = ilu_gmres_factory->generate(A);
```

#### Solve system

```
ilu_gmres->apply(b, x);
```

#### Print solution

```
std::cout « "Solution (x):\n";
write(std::cout, x);
```

#### Calculate residual

```
auto one = gko::initialize<vec>({1.0}, exec);
auto neg_one = gko::initialize<vec>({-1.0}, exec);
auto res = gko::initialize<real_vec>({0.0}, exec);
A->apply(one, x, neg_one, b);
b->compute_norm2(res);
std::cout « "Residual norm sqrt(r^T r):\n";
write(std::cout, res);
```

## Results

## This is the expected output:

```
Solution (x):
%%MatrixMarket matrix array real general
19 1
0.252218
0.108645
0.0662811
0.0630433
0.0384088
0.0396536
0.0402648
0.0338935
0.0193098
0.0234653
0.0211499
0.0196413
0.0199151
0.0181674
0.0162722
0.0150714
0.0107016
0.0121141
0.0123025
Residual norm sqrt(r^T r):
%%MatrixMarket matrix array real general
1 1
1.46249e-08
```

#### Comments about programming and debugging

```
#include <cstdlib>
#include <fstream>
#include <iostream>
#include <map>
#include <string>
#include <ginkgo/ginkgo.hpp>
int main(int argc, char* argv[])
    using ValueType = double;
    using RealValueType = gko::remove_complex<ValueType>;
    using IndexType = int;
    using vec = gko::matrix::Dense<ValueType>;
    using real_vec = gko::matrix::Dense<RealValueType>;
    using mtx = gko::matrix::Csr<ValueType, IndexType>;
    using gmres = gko::solver::Gmres<ValueType>;
    std::cout « gko::version_info::get() « std::endl;
    if (argc == 2 && (std::string(argv[1]) == "--help")) {
   std::cerr « "Usage: " « argv[0] « " [executor]" « std::endl;
        std::exit(-1);
    const auto executor_string = argc >= 2 ? argv[1] : "reference";
    std::map<std::string, std::function<std::shared_ptr<gko::Executor>()»
        exec_map{
             {"omp", [] { return gko::OmpExecutor::create(); }},
{"cuda",
              [] {
                  return gko::CudaExecutor::create(0,
                                                      gko::OmpExecutor::create());
             {"hip",
              [] {
                  return gko::HipExecutor::create(0, gko::OmpExecutor::create());
             { "dpcpp",
                  return gko::DpcppExecutor::create(0,
                                                        gko::OmpExecutor::create());
             {"reference", [] { return gko::ReferenceExecutor::create(); }}};
    const auto exec = exec_map.at(executor_string)(); // throws if not valid auto A = gko::share(gko::read<mtx>(std::ifstream("data/A.mtx"), exec));
    auto b = gko::read<vec>(std::ifstream("data/b.mtx"), exec);
    auto x = gko::read<vec>(std::ifstream("data/x0.mtx"), exec);
    auto par_ilu_fact =
        gko::factorization::ParIlu<ValueType, IndexType>::build().on(exec);
    auto par_ilu = gko::share(par_ilu_fact->generate(A));
    auto ilu_pre_factory =
        gko::preconditioner::Ilu<gko::solver::LowerTrs<ValueType, IndexType>,
                                    gko::solver::UpperTrs<ValueType, IndexType>,
false>::build()
             .on(exec);
    auto ilu_preconditioner = gko::share(ilu_pre_factory->generate(par_ilu));
    const RealValueType reduction_factor{1e-7};
    auto ilu_gmres_factory =
        gmres::build()
             .with_criteria(gko::stop::Iteration::build().with_max_iters(1000u),
                             gko::stop::ResidualNorm<ValueType>::build()
                                  .with_reduction_factor(reduction_factor))
             .with_generated_preconditioner(ilu_preconditioner)
             .on(exec);
    auto ilu_gmres = ilu_gmres_factory->generate(A);
    ilu_gmres->apply(b, x);
std::cout « "Solution (x):\n";
    write(std::cout, x);
    auto one = gko::initialize<vec>({1.0}, exec);
    auto neg_one = gko::initialize<vec>({-1.0}, exec);
    auto res = gko::initialize<real_vec>({0.0}, exec);
    A->apply(one, x, neg_one, b); b->compute_norm2(res);
    std::cout « "Residual norm sqrt(r^T r):\n";
    write(std::cout, res);
```

## The inverse-iteration program

The inverse iteration example..

This example depends on simple-solver, .

## Introduction

This example shows how components available in Ginkgo can be used to implement higher-level numerical methods. The method used here will be the shifted inverse iteration method for eigenvalue computation which find the eigenvalue and eigenvector of A closest to z, for some scalar z. The method requires repeatedly solving the shifted linear system (A - zI)x = b, as well as performing matrix-vector products with the matrix A. Here is the complete pseudocode of the method:

## About the example

we avoid duplicating memory by not storing both A and A - zI, but compute A - zI on the fly by using Ginkgo's
utilities for creating linear combinations of operators

```
auto one = share(gko::initialize<vec>({precision{1.0}}), exec));
auto neg_one = share(gko::initialize<vec>({-precision{1.0}}, exec));
auto neg_z = gko::initialize<vec>({-z}, exec);
auto system_matrix = share(gko::Combinationprecision>::create(
    one, A, gko::initialize<vec>((-z), exec),
    gko::matrix::Identity<precision>::create(exec, A->get_size()[0])));
Generate solver operator (A - zI)^-1
auto solver
    solver_type::build()
         . with\_criteria (gko::stop::Iteration::build().with\_max\_iters(
                          system_max_iterations),
qko::stop::ResidualNormprecision>::build()
                              .with_reduction_factor(system_residual_goal))
         .on(exec)
         ->generate(system_matrix);
inverse iterations
start with guess [1, 1, ..., 1]
auto x = [\&] { auto work = vec::create(this_exec, gko::dim<2>{A->get_size()[0], 1});
    const auto n = work->get_size()[0];
    for (int i = 0; i < n; ++i) {
         work->get_values()[i] = precision{1.0} / sqrt(n);
    return clone(exec, work);
}();
auto y = clone(x);
auto tmp = clone(x);
auto norm = gko::initialize<real_vec>({1.0}, exec);
auto inv_norm = clone(this_exec, one);
auto g = clone(one);
for (auto i = Ou; i < max_iterations; ++i) {
    std::cout « "{ ";</pre>
(A - zI)y = x
solver->apply(x, y);
system_matrix->apply(one, y, neg_one, x);
x->compute_norm2(norm);
std::cout « "\"system_residual\": "
           « clone(this_exec, norm)->get_values()[0] « ", ";
x->copy_from(y);
x = y / || y ||
x->compute_norm2(norm);
inv_norm->get_values()[0] =
    real_precision{1.0} / clone(this_exec, norm)->get_values()[0];
x->scale(clone(exec, inv_norm));
```

## Results

```
This is the expected output:
{ "system_residual":
                        +1.61736920e-14, "eigenvalue": (+2.03741410e+01,-1.17744356e-16), "residual":
(+2.92231055e-01,+1.68883476e-18) }, { "system_residual": +4.98014795e-15, "eigenvalue": (+1.94878474e+01,+1.25948378e-15), "residual":
      (+7.94370276e-02,-5.13395071e-18) },
stem_residual": +3.39296916e-15, "eigenvalue": (+1.93282121e+01,-1.19329332e-15), "residual":
{ "system_residual":
      (+4.11149623e-02,+2.53837290e-18) },
{ "system_residual": +3.35953656e-15,
                                          "eigenvalue": (+1.92638912e+01,+3.28657016e-16), "residual":
      (+2.34717040e-02,-4.00445585e-19) },
{ "system_residual": +2.91474009e-15, "eigenvalue": (+1.92409166e+01,+3.65597737e-16), "residual":
(+1.34709547e-02,-2.55962367e-19) }, { "system_residual": +3.09863953e-15, "eigenvalue": (+1.92331106e+01,-1.07919176e-15), "residual":
      (+7.72060707e-03,+4.33212063e-19) },
{ "system_residual": +2.31198069e-15, "eigenvalue": (+1.92305014e+01,-2.89755360e-16), "residual":
      (+4.42106625e-03,+6.66143651e-20) },
{ "system_residual": +3.02771202e-15, "eigenvalue": (+1.92296339e+01,+8.04259901e-16), "residual":
(+2.53081312e-03,-1.05848687e-19) }, { "system_residual": +2.02954523e-15, "eigenvalue": (+1.92293461e+01,+7.81834016e-16), "residual":
      (+1.44862114e-03,-5.88985854e-20) },
 "system_residual":
                       +2.31762332e-15,
                                          "eigenvalue": (+1.92292506e+01,-1.11718775e-16), "residual":
      (+8.29183451e-04,+4.81741912e-21) },
{ "system_residual": +8.12541038e-15, "eigenvalue": (+1.92292190e+01,-6.55606254e-16), "residual":
      (+4.74636702e-04,+1.61823936e-20) },
{ "system_residual": +2.77259926e-15, "eigenvalue": (+1.92292085e+01,+4.30588140e-16), "residual":
      (+2.71701077e-04,-6.08403935e-21) },
{ "system_residual": +8.87888675e-14, "eigenvalue": (+1.92292051e+01,+9.67936313e-18), "residual":
(+1.55539937e-04,-7.82937998e-23) }, { "system_residual": +2.85077117e-15, "eigenvalue": (+1.92292039e+01,-4.52923128e-16), "residual":
      (+8.90457139e-05,+2.09737561e-21) },
{ "system_residual": +6.46865302e-14, "eigenvalue": (+1.92292035e+01,+1.58710681e-17), "residual":
      (+5.09805252e-05,-4.20774259e-23) },
                       +4.18913713e-15, "eigenvalue": (+1.92292034e+01,+1.06839590e-15), "residual":
{ "system_residual":
      (+2.91887365e-05,-1.62175862e-21) },
{ "system_residual": +1.06421578e-11, "eigenvalue": (+1.92292034e+01,+3.26089685e-17), "residual":
(+1.67126561e-05,-2.83413965e-23) }, { "system_residual": +2.97434420e-13, "eigenvalue": (+1.92292034e+01,-7.85427712e-16), "residual":
      (+9.56961199e-06,+3.90876227e-22) },
{ "system_residual": +1.63230281e-11, "eigenvalue": (+1.92292033e+01,+3.69307000e-16), "residual":
(+5.47975753e-06,-1.05241636e-22) }, { "system_residual": +6.14939758e-14, "eigenvalue": (+1.92292033e+01,+1.36057865e-15), "residual":
      (+3.13794996e-06,-2.22028320e-22) },
```

### Comments about programming and debugging

```
#include <cmath>
#include <complex>
#include <fstream>
#include <iomanip>
#include <iostream>
#include <map>
#include <string>
#include <ginkgo/ginkgo.hpp>
```

```
int main(int argc, char* argv[])
    using precision = std::complex<double>;
    using real_precision = gko::remove_complex<precision>;
    using vec = gko::matrix::Dense<precision>;
    using real_vec = gko::matrix::Dense<real_precision>;
    using mtx = gko::matrix::Csr<precision>;
    using solver_type = gko::solver::Bicgstab<precision>;
    using std::abs;
    using std::sgrt;
    std::cout « gko::version_info::get() « std::endl;
    std::cout « std::scientific « std::setprecision(8) « std::showpos;
if (argc == 2 && (std::string(argv[1]) == "--help")) {
    std::cerr « "Usage: " « argv[0] « " [executor]" « std::endl;
         std::exit(-1);
    const auto executor_string = argc >= 2 ? argv[1] : "reference";
std::map<std::string, std::function<std::shared_ptr<gko::Executor>()»
        exec_map{
             {"omp",
                     [] { return gko::OmpExecutor::create(); }},
              {"cuda",
              [] {
                   return gko::CudaExecutor::create(0,
                                                         gko::OmpExecutor::create());
               }},
             {"hip",
              [] {
                   return gko::HipExecutor::create(0, gko::OmpExecutor::create());
             {"dpcpp",
              [] {
                   return gko::DpcppExecutor::create(0,
                                                          gko::OmpExecutor::create());
             {"reference", [] { return gko::ReferenceExecutor::create(); }}};
    const auto exec = exec_map.at(executor_string)(); // throws if not valid
auto this_exec = exec->get_master();
    auto system_max_iterations = 100u;
    auto system_residual_goal = real_precision{1e-16};
    auto max_iterations = 20u;
auto residual_goal = real_precision{1e-8};
    auto z = precision\{20.0, 2.0\};
    auto A = share(gko::read<mtx>(std::ifstream("data/A.mtx"), exec));
    auto one = share(gko::initialize<vec>({precision{1.0}}), exec));
    auto neg_one = share(gko::initialize<vec>({-precision{1.0}}, exec));
    auto neg_z = gko::initialize<vec>((-z), exec);
    auto system_matrix = share(gko::Combination<precision>::create(
        one, A, gko::initialize < vec > ({-z}, exec),
        gko::matrix::Identity<precision>::create(exec, A->get_size()[0])));
    auto solver =
        solver_type::build()
             .with_criteria(gko::stop::Iteration::build().with_max_iters(
                                   system_max_iterations),
                               gko::stop::ResidualNorm<precision>::build()
                                   . \verb|with_reduction_factor(system_residual_goal)||\\
             .on(exec)
             ->generate(system_matrix);
    auto x = [\&] {
         auto work = vec::create(this_exec, gko::dim<2>{A->get_size()[0], 1});
        const auto n = work->get_size()[0];
for (int i = 0; i < n; ++i) {</pre>
             work->get_values()[i] = precision{1.0} / sqrt(n);
        return clone(exec, work);
    }();
    auto y = clone(x);
    auto tmp = clone(x);
    auto norm = gko::initialize<real_vec>({1.0}, exec);
    auto inv_norm = clone(this_exec, one);
    auto g = clone(one);
    for (auto i = Ou; i < max_iterations; ++i) {
    std::cout « "{ ";</pre>
         solver->apply(x, y);
         system_matrix->apply(one, y, neg_one, x);
         x->compute_norm2(norm);
         std::cout « "\"system_residual\": "
                   « clone(this_exec, norm)->get_values()[0] « ", ";
         x->copy_from(y);
         x->compute_norm2(norm);
         inv_norm->get_values()[0] =
            real_precision{1.0} / clone(this_exec, norm)->get_values()[0];
         x->scale(clone(exec, inv_norm));
         A->apply(x, tmp);
         x->compute_dot(tmp, g);
        auto g_val = clone(this_exec, g)->get_values()[0];
std::cout « "\"eigenvalue\": " « g_val « ", ";
         auto v = gko::initialize<vec>({-g_val}, exec);
```

```
tmp->add_scaled(v, x);
tmp->compute_norm2(norm);
auto res_val = clone(exec->get_master(), norm)->get_values()[0];
std::cout « "\"residual\": " « res_val / g_val « " }," « std::endl;
if (abs(res_val) < residual_goal * abs(g_val)) {
    break;
}
}</pre>
```

# The ir-ilu-preconditioned-solver program

The IR-ILU preconditioned solver example..

This example depends on ilu-preconditioned-solver, iterative-refinement.

## Introduction

### About the example

This example shows how to combine iterative refinement with the adaptive precision block-Jacobi preconditioner in order to approximately solve the triangular systems occurring in ILU preconditioning. Using an adaptive precision block-Jacobi preconditioner matrix as inner solver for the iterative refinement method is equivalent to doing adaptive precision block-Jacobi relaxation in the triangular solves. This example roughly approximates the triangular solves with five adaptive precision block-Jacobi sweeps with a maximum block size of 16.

This example is motivated by "Multiprecision block-Jacobi for Iterative Triangular Solves" (Göbel, Anzt, Cojean, Flegar, Quintana-Ortí, Euro-Par 2020). The theory and a detailed analysis can be found there.

## The commented program

executor where Ginkgo will perform the computation

```
Create RHS and initial guess as 1
gko::size_type num_rows = A->get_size()[0];
auto host_x = vec::create(exec->get_master(), gko::dim<2>(num_rows, 1));
for (gko::size_type i = 0; i < num_rows; i++) {
    host_x->at(i, 0) = 1.;
}
auto x = gko::clone(exec, host_x);
auto b = gko::clone(exec, host_x);
auto clone_x = gko::clone(exec, x);
Generate incomplete factors using ParILU
auto par_ilu_fact =
    gko::factorization::ParIlu<ValueType, IndexType>::build().on(exec);
```

## Generate concrete factorization for input matrix

auto par\_ilu = gko::share(par\_ilu\_fact->generate(A));

Generate an iterative refinement factory to be used as a triangular solver in the preconditioner application. The generated method is equivalent to doing five block-Jacobi sweeps with a maximum block size of 16.

```
auto bj_factory = gko::share(
   bj::build()
        .with_max_block_size(16u)
        .with_storage_optimization(gko::precision_reduction::autodetect())
        .on(exec));
auto trisolve_factory =
   ir::build()
        .with_solver(bj_factory)
        .with_criteria(gko::stop::Iteration::build().with_max_iters(sweeps))
        .on(exec);
```

Generate an ILU preconditioner factory by setting lower and upper triangular solver - in this case the previously defined iterative refinement method.

### Use incomplete factors to generate ILU preconditioner

auto ilu\_preconditioner = gko::share(ilu\_pre\_factory->generate(par\_ilu));

#### Create stopping criteria for Gmres

Use preconditioner inside GMRES solver factory Generating a solver factory tied to a specific preconditioner makes sense if there are several very similar systems to solve, and the same solver+preconditioner combination is expected to be effective.

```
auto ilu_gmres_factory =
   gmres::build()
        .with_criteria(iter_stop, tol_stop)
        .with_generated_preconditioner(ilu_preconditioner)
        .on(exec);
```

#### Generate preconditioned solver for a specific target system

```
auto ilu_gmres = ilu_gmres_factory->generate(A);
```

## Add logger

```
std::shared_ptr<const gko::log::Convergence<ValueType> logger =
    gko::log::Convergence<ValueType>::create();
ilu_gmres->add_logger(logger);
```

#### Warmup run

```
ilu_gmres->apply(b, x);
```

### Solve system 100 times and take the average time.

```
std::chrono::nanoseconds time(0);

for (int i = 0; i < 100; i++) {
    x->copy_from(clone_x);
    auto tic = std::chrono::high_resolution_clock::now();
    ilu_gmres->apply(b, x);
    auto toc = std::chrono::high_resolution_clock::now();
    time += std::chrono::duration_cast<std::chrono::nanoseconds>(toc - tic);
std::cout « "Using " « sweeps « " block-Jacobi sweeps.\n";
Print solution
std::cout « "Solution (x):\n";
write(std::cout, x);
Get residual
    auto res = gko::as<vec>(logger->get_residual_norm());
    " « logger->get_num_iterations()
    std::cout « "GMRES execution time [ms]: "
             « static_cast<double>(time.count()) / 100000000.0 « "\n";
    std::cout « "Residual norm sqrt(r^T r):\n";
    write(std::cout, res);
```

## Results

### This is the expected output:

```
Using 5 block-Jacobi sweeps.
Solution (x):
%%MatrixMarket matrix array real general
19 1
0.252218
0.108645
0.0662811
0.0630433
0.0384088
0.0396536
0.0402648
0.0338935
0.0193098
0.0234653
0.0211499
0.0196413
0.0199151
0.0181674
0.0162722
0.0150714
0.0107016
0.0121141
0.0123025
GMRES iteration count:
GMRES execution time [ms]: 0.377673
Residual norm sqrt(r^T r):
%%MatrixMarket matrix array real general
1.65303e-12
```

#### Comments about programming and debugging

```
#include <cstdlib>
#include <fstream>
#include <iostream>
#include <map>
#include <string>
#include <ginkgo/ginkgo.hpp>
int main(int argc, char* argv[]) {
    using ValueType = double;
    using RealValueType = gko::remove_complex<ValueType>;
    using IndexType = int;
    using vec = gko::matrix::Dense<ValueType>;
```

```
using real_vec = gko::matrix::Dense<RealValueType>;
using mtx = gko::matrix::Csr<ValueType, IndexType>;
using gmres = gko::solver::Gmres<ValueType>;
using ir = gko::solver::Ir<ValueType>;
using bj = gko::preconditioner::Jacobi<ValueType, IndexType>;
std::cout « gko::version_info::get() « std::endl;
if (argc == 2 && (std::string(argv[1]) == "--help")) {
   std::cerr « "Usage: " « argv[0] « " [executor]" « std::endl;
    std::exit(-1);
const auto executor_string = argc >= 2 ? argv[1] : "reference";
const unsigned int sweeps = argc == 3 ? std::atoi(argv[2]) : 5u;
std::map<std::string, std::function<std::shared_ptr<gko::Executor>()»
    exec_map{
         {"omp", [] { return gko::OmpExecutor::create(); }},
         {"cuda",
         [] {
              return gko::CudaExecutor::create(0,
                                                  gko::OmpExecutor::create());
          }},
         {"hip",
         return gko::HipExecutor::create(0, gko::OmpExecutor::create());
}},
        { "dpcpp",
         [] {
              return gko::DpcppExecutor::create(0,
                                                   gko::OmpExecutor::create());
        {"reference", [] { return gko::ReferenceExecutor::create(); }}};
const auto exec = exec_map.at(executor_string)(); // throws if not valid
auto A = gko::share(gko::read<mtx>(std::ifstream("data/A.mtx"), exec));
gko::size_type num_rows = A->get_size()[0];
auto host_x = vec::create(exec->get_master(), gko::dim<2>(num_rows, 1));
for (gko::size_type i = 0; i < num_rows; i++) {
   host_x->at(i, 0) = 1.;
auto x = gko::clone(exec, host_x);
auto b = gko::clone(exec, host_x);
auto clone_x = gko::clone(exec, x);
auto par_ilu_fact =
gko::factorization::ParIlu<ValueType, IndexType>::build().on(exec);
auto par_ilu = gko::share(par_ilu_fact->generate(A));
auto bj_factory = gko::share(
    bj::build()
        .with_max_block_size(16u)
        .with_storage_optimization(gko::precision_reduction::autodetect())
        .on(exec));
auto trisolve factory
    ir::build()
        .with_solver(bj_factory)
        .with_criteria(gko::stop::Iteration::build().with_max_iters(sweeps))
         on (exec);
auto ilu_pre_factory = gko::preconditioner::Ilu<ir, ir>::build()
                             .with_l_solver(gko::clone(trisolve_factory))
                             .with_u_solver(gko::clone(trisolve_factory))
                             .on(exec);
auto ilu_preconditioner = gko::share(ilu_pre_factory->generate(par_ilu));
const RealValueType reduction_factor{1e-12};
auto iter_stop = gko::share(
    gko::stop::Iteration::build().with_max_iters(1000u).on(exec));
auto tol_stop = gko::share(gko::stop::ResidualNorm<ValueType>::build()
                                 .with_reduction_factor(reduction_factor)
                                  .on(exec));
auto ilu_gmres_factory =
    gmres::build()
        .with_criteria(iter_stop, tol_stop)
.with_generated_preconditioner(ilu_preconditioner)
        .on(exec);
auto ilu_gmres = ilu_gmres_factory->generate(A);
std::shared_ptr<const gko::log::Convergence<ValueType» logger =
    gko::log::Convergence<ValueType>::create();
ilu_gmres->add_logger(logger);
ilu_gmres->apply(b, x);
std::chrono::nanoseconds time(0);
for (int i = 0; i < 100; i++) {
    x->copy_from(clone_x);
    auto tic = std::chrono::high_resolution_clock::now();
    ilu_gmres->apply(b, x);
    auto toc = std::chrono::high_resolution_clock::now();
    time += std::chrono::duration cast<std::chrono::nanoseconds>(toc - tic);
, std::cout \ll "Using " \ll sweeps \ll " block-Jacobi sweeps.\n"; std::cout \ll "Solution (x):\n";
write(std::cout, x);
« logger->get num iterations()
```

# The iterative-refinement program

The iterative refinement solver example..

This example depends on simple-solver.

## This example shows how to use the iterative refinement solver.

In this example, we first read in a matrix from file, then generate a right-hand side and an initial guess. An inaccurate CG solver is used as the inner solver to an iterative refinement (IR) method which solves a linear system. The example features the iteration count and runtime of the IR solver.

```
const auto executor_string = argc >= 2 ? argv[1] : "reference";
std::map<std::string, std::function<std::shared_ptr<gko::Executor>()»
        {"omp", [] { return gko::OmpExecutor::create(); }},
        {"cuda",
             return gko::CudaExecutor::create(0,
                                                gko::OmpExecutor::create());
        }},
{"hip",
             return gko::HipExecutor::create(0, gko::OmpExecutor::create());
        {"dpcpp",
             return gko::DpcppExecutor::create(0,
                                                gko::OmpExecutor::create());
        {"reference", [] { return gko::ReferenceExecutor::create(); }}};
executor where Ginkgo will perform the computation
const auto exec = exec_map.at(executor_string)(); // throws if not valid
Read data
auto A = share(gko::read<mtx>(std::ifstream("data/A.mtx"), exec));
Create RHS and initial guess as 1
gko::size_type size = A->get_size()[0];
auto host_x = gko::matrix::Dense<ValueType>::create(exec->get_master(),
                                                     gko::dim<2>(size, 1));
for (auto i = 0; i < size; i++) {
   host_x->at(i, 0) = 1.;
auto x = gko::clone(exec, host_x);
```

```
auto b = gko::clone(exec, host_x);
Calculate initial residual by overwriting b
auto one = gko::initialize<vec>({1.0}, exec);
auto neg_one = gko::initialize<vec>({-1.0}, exec);
auto initres = gko::initialize<real_vec>({0.0}, exec);
A->apply(one, x, neg_one, b);
b->compute_norm2(initres);
copy b again
b->copy_from(host_x);
Create solver factory
gko::size_type max_iters = 10000u;
RealValueType outer_reduction_factor{1e-12};
RealValueType inner_reduction_factor{1e-2};
auto solver_gen =
    ir::build()
        .with_reduction_factor(inner_reduction_factor)))
         .with_criteria(
             gko::stop::Iteration::build().with_max_iters(max_iters),
             gko::stop::ResidualNorm<ValueType>::build()
                 .with_reduction_factor(outer_reduction_factor))
         .on(exec);
Create solver
auto solver = solver_gen->generate(A);
std::shared_ptr<const gko::log::Convergence<ValueType» logger =
    gko::log::Convergence<ValueType>::create();
solver->add_logger(logger);
Solve system
exec->synchronize();
std::chrono::nanoseconds time(0);
auto tic = std::chrono::steady_clock::now();
solver->apply(b, x);
auto toc = std::chrono::steady_clock::now();
time += std::chrono::duration_cast<std::chrono::nanoseconds>(toc - tic);
Get residual
auto res = gko::as<real_vec>(logger->get_residual_norm());
std::cout « "Initial residual norm sqrt(r^T r):\n";
write(std::cout, initres);
std::cout « "Final residual norm sqrt(r^T r):\n";
write(std::cout, res);
Print solver statistics
    std::cout « "IR iteration count:
                                                 " « logger->get_num_iterations()
              « std::endl;
    std::cout « "IR execution time [ms]: "
               « static_cast<double>(time.count()) / 1000000.0 « std::endl;
```

## Results

### This is the expected output:

```
Initial residual norm sqrt(r^T r):
%%MatrixMarket matrix array real general
1 1
194.679
Final residual norm sqrt(r^T r):
%%MatrixMarket matrix array real general
1 1
4.23821e-11
IR iteration count: 24
IR execution time [ms]: 0.794962
```

#### Comments about programming and debugging

```
#include <fstream>
#include <iomanip>
#include <iostream>
#include <map>
#include <string>
#include <ginkgo/ginkgo.hpp>
int main(int argc, char* argv[])
    using ValueType = double;
    using RealValueType = gko::remove_complex<ValueType>;
    using IndexType = int;
    using vec = gko::matrix::Dense<ValueType>;
    using real_vec = gko::matrix::Dense<RealValueType>;
    using mtx = gko::matrix::Csr<ValueType, IndexType>;
    using cg = gko::solver::Cg<ValueType>;
using ir = gko::solver::Ir<ValueType>;
    std::cout « gko::version_info::get() « std::endl;
    if (argc == 2 && (std::string(argy[1]) == "--help")) {
   std::cerr « "Usage: " « argv[0] « " [executor]" « std::endl;
        std::exit(-1);
    const auto executor_string = argc >= 2 ? argv[1] : "reference";
    std::map<std::string, std::function<std::shared_ptr<gko::Executor>()»
             {"omp", [] { return gko::OmpExecutor::create(); }},
{"cuda",
              [] {
                  return gko::CudaExecutor::create(0,
                                                       gko::OmpExecutor::create());
              [] {
                  return gko::HipExecutor::create(0, gko::OmpExecutor::create());
              }}.
             { "dpcpp",
              [] {
                  return gko::DpcppExecutor::create(0,
                                                        gko::OmpExecutor::create());
             {"reference", [] { return gko::ReferenceExecutor::create(); }}};
    const auto exec = exec map.at(executor string)(); // throws if not valid
    auto A = share(gko::read<mtx>(std::ifstream("data/A.mtx"), exec));
    gko::size_type size = A->get_size()[0];
    auto host_x = gko::matrix::Dense<ValueType>::create(exec->get_master(),
                                                              gko::dim<2>(size, 1));
    for (auto i = 0; i < size; i++) {</pre>
        host x->at(i, 0) = 1.;
    auto x = gko::clone(exec, host_x);
    auto b = gko::clone(exec, host_x);
    auto one = gko::initialize<vec>({1.0}, exec);
    auto neg_one = gko::initializevec>({-1.0}, exec);
auto initres = gko::initialize<real_vec>({0.0}, exec);
    A->apply(one, x, neg_one, b);
b->compute_norm2(initres);
    b->copy_from(host_x);
    gko::size_type max_iters = 10000u;
    RealValueType outer_reduction_factor{1e-12};
    RealValueType inner_reduction_factor{1e-2};
    auto solver_gen =
        ir::build()
            .with_solver(cg::build().with_criteria(
                 gko::stop::ResidualNorm<ValueType>::build()
                      .with_reduction_factor(inner_reduction_factor)))
             .with criteria(
                 gko::stop::Iteration::build().with max iters(max iters),
                 gko::stop::ResidualNorm<ValueType>::build()
                      .with_reduction_factor(outer_reduction_factor))
             .on(exec);
    auto solver = solver_gen->generate(A);
    std::shared_ptr<const gko::log::Convergence<ValueType» logger =
    gko::log::Convergence<ValueType>::create();
    solver->add_logger(logger);
    exec->synchronize();
    std::chrono::nanoseconds time(0);
    auto tic = std::chrono::steady_clock::now();
    solver->apply(b, x);
    auto toc = std::chrono::steadv clock::now();
    time += std::chrono::duration_cast<std::chrono::nanoseconds>(toc - tic);
    auto res = gko::as<real_vec>(logger->get_residual_norm());
```

# The kokkos-assembly program

The Kokkos assembly example..

This example depends on simple-solver, poisson-solver, three-pt-stencil-solver, .

## Introduction

This example solves a 1D Poisson equation:

$$u:[0,1] \to Ru" = fu(0) = u0u(1) = u1$$

using a finite difference method on an equidistant grid with  ${\tt K}$  discretization points ( ${\tt K}$  can be controlled with a command line parameter).

The resulting CSR matrix is assembled using Kokkos kernels. This example show how to use Ginkgo data with Kokkos kernels.

## Notes

If this example is built as part of Ginkgo, it is advised to configure Ginkgo with <code>-DGINKGO\_WITH\_CCACHE=OFF</code> to prevent incompabilities with Kokkos' compiler wrapper for <code>nvcc</code>.

```
* @param values Pointer to the values
      * @return An object which has each gko::array of the
                 device_matrix_data mapped to a Kokkos view
     static type map(size_type size, IndexType_c* row_idxs,
                     IndexType_c* col_idxs, ValueType_c* values)
     {
         return {index_mapper::map(row_idxs, size),
                 index_mapper::map(col_idxs, size),
                 value_mapper::map(values, size));
     index array row idxs;
     index_array col_idxs;
     value_array values;
 static type<ValueType, IndexType> map(
     device_matrix_data<ValueType, IndexType>& md)
     assert_compatibility<MemorySpace>(md);
     return type<ValueType, IndexType>::map(
         md.get_num_stored_elements(), md.get_row_idxs(), md.get_col_idxs(),
         md.get_values());
 static type<const ValueType, const IndexType> map(
     const device_matrix_data<ValueType, IndexType>& md)
     assert_compatibility<MemorySpace> (md);
     return type<const ValueType, const IndexType>::map(
         md.get_num_stored_elements(), md.get_const_row_idxs(),
         md.get_const_col_idxs(), md.get_const_values());
 }
// namespace gko::ext::kokkos::detail
```

#### Creates a stencil matrix in CSR format for the given number of discretization points.

```
template <typename ValueType, typename IndexType>
void generate_stencil_matrix(gko::matrix::Csr<ValueType, IndexType>* matrix)
{
    auto exec = matrix->get_executor();
    const auto discretization_points = matrix->get_size()[0];
```

Over-allocate storage for the matrix elements. Each row has 3 entries, except for the first and last one. To handle each row uniformly, we allocate space for 3x the number of rows.

#### Create Kokkos views on Ginkgo data.

auto k\_md = gko::ext::kokkos::map\_data(md);

Create the matrix entries. This also creates zero entries for the first and second row to handle all rows uniformly.

```
Kokkos::parallel_for(
   "generate_stencil_matrix", md.get_num_stored_elements(),
   KOKKOS_LAMBDA(int i) {
      const ValueType coefs[] = {-1, 2, -1};
      auto ofs = static_cast<IndexType>((i % 3) - 1);
      auto row = static_cast<IndexType>(i / 3);
      auto col = row + ofs;
```

To prevent branching, a mask is used to set the entry to zero, if the column is out-of-bounds

#### Add up duplicate (zero) entries.

```
md.sum_duplicates();
```

## Build Csr matrix.

```
matrix->read(std::move(md));
```

### Generates the RHS vector given f and the boundary conditions.

```
const auto discretization_points = rhs->get_size()[0];
    auto k_rhs = gko::ext::kokkos::map_data(rhs);
    Kokkos::parallel_for(
         "generate_rhs", discretization_points, KOKKOS_LAMBDA(int i) {
            const ValueType h = 1.0 / (discretization_points + 1);
const ValueType xi = ValueType(i + 1) * h;
            k_{rhs}(i, 0) = -f(xi) * h * h;
            if (i == 0) {
                k_{rhs(i, 0)} += u0;
            if (i == discretization_points - 1) {
                k_{rhs}(i, 0) += u1;
Computes the 1-norm of the error given the computed u and the correct solution function \mathtt{correct\_u}.
template <typename Closure, typename ValueType>
double calculate_error(int discretization_points,
                        const gko::matrix::Dense<ValueType>* u,
                        Closure&& correct_u)
    auto k_u = gko::ext::kokkos::map_data(u);
    auto error = 0.0;
    Kokkos::parallel_reduce(
        "calculate_error", discretization_points,
KOKKOS_LAMBDA(int i, double& lsum) {
            const auto xi = (i + 1) * h;
            lsum += Kokkos::abs((k_u(i, 0) - correct_u(xi)) /
                                 Kokkos::abs(correct_u(xi)));
        },
        error);
    return error;
int main(int argc, char* argv[])
Some shortcuts
using ValueType = double;
using RealValueType = gko::remove_complex<ValueType>;
using IndexType = int;
using vec = gko::matrix::Dense<ValueType>;
using mtx = gko::matrix::Csr<ValueType, IndexType>;
using cg = gko::solver::Cg<ValueType>;
using bj = gko::preconditioner::Jacobi<ValueType>;
Print help message. For details on the kokkos-options see https://kokkos.github.io/kokkos-core-wiki/←
ProgrammingGuide/Initialization.html#initialization-by-command-line-arguments
if (argc == 2 && (std::string(argv[1]) == "--help")) {
   std::cerr w "Usage: " w argv[0]
              « " [discretization_points] [kokkos-options] " « std::endl;
    Kokkos::ScopeGuard kokkos(argc, argv); // print Kokkos help
    std::exit(1);
Kokkos::ScopeGuard kokkos(argc, argv);
const auto discretization_points =
    static_cast<gko::size_type>(argc >= 2 ? std::atoi(argv[1]) : 100u);
chooses the executor that corresponds to the Kokkos DefaultExecutionSpace
auto exec = gko::ext::kokkos::create_default_executor();
auto correct_u = [] KOKKOS_FUNCTION(ValueType x) { return x * x * x; };
auto f = [] KOKKOS_FUNCTION(ValueType x) { return ValueType{6} * x; };
auto u0 = correct_u(0);
auto u1 = correct_u(1);
initialize vectors
auto rhs = vec::create(exec, gko::dim<2>(discretization_points, 1));
generate_rhs(f, u0, u1, rhs.get());
auto u = vec::create(exec, gko::dim<2>(discretization_points, 1));
u->fill(0.0);
initialize the stencil matrix
auto A = share(mtx::create(
    exec, gko::dim<2>{discretization_points, discretization_points}));
generate_stencil_matrix(A.get());
```

const RealValueType reduction\_factor{1e-7};

#### Generate solver and solve the system

## Results

#### Example output:

```
> ./kokkos-assembly
Solve complete.
The average relative error is 1.05488e-11
```

The actual error depends on the used hardware.

```
#include <iostream>
#include <string>
#include <Kokkos_Core.hpp>
#include <ginkgo/ginkgo.hpp>
#include <ginkgo/extensions/kokkos.hpp>
namespace gko::ext::kokkos::detail {
template <typename ValueType, typename IndexType, typename MemorySpace>
struct mapper<device_matrix_data<ValueType, IndexType>, MemorySpace> {
    using index_mapper = mapper<array<IndexType>, MemorySpace>;
    using value_mapper = mapper<array<ValueType>, MemorySpace>;
    template <typename ValueType_c, typename IndexType_c>
    struct type {
         using index_array = typename index_mapper::template type<IndexType_c>;
         using value_array = typename value_mapper::template type<ValueType_c>;
         static type map(size_type size, IndexType_c* row_idxs,
IndexType_c* col_idxs, ValueType_c* values)
         {
              return {index_mapper::map(row_idxs, size),
                        index_mapper::map(col_idxs, size),
                        value_mapper::map(values, size));
         index_array row_idxs;
         index_array col_idxs;
         value_array values;
    static type<ValueType, IndexType> map(
    device_matrix_data<ValueType, IndexType>& md)
         assert_compatibility<MemorySpace>(md);
         return type<ValueType, IndexType>::map(
              md.get_num_stored_elements(), md.get_row_idxs(), md.get_col_idxs(),
              md.get_values());
    static type<const ValueType, const IndexType> map(
         const device_matrix_data<ValueType, IndexType>& md)
         assert_compatibility<MemorySpace>(md);
         return type<const ValueType, const IndexType>::map(
              md.get_num_stored_elements(), md.get_const_row_idxs(),
              md.get_const_col_idxs(), md.get_const_values());
} // namespace gko::ext::kokkos::detail
template <typename ValueType, typename IndexType>
void generate_stencil_matrix(gko::matrix::Csr<ValueType, IndexType>* matrix)
    auto exec = matrix->get_executor();
    const auto discretization_points = matrix->get_size()[0];
```

```
gko::device_matrix_data<ValueType, IndexType> md(exec, matrix->get_size(),
                                                       discretization points * 3);
    auto k_md = gko::ext::kokkos::map_data(md);
    Kokkos::parallel_for(
        "generate_stencil_matrix", md.get_num_stored_elements(),
        KOKKOS_LAMBDA(int i) {
            const ValueType coefs[] = \{-1, 2, -1\};
            auto ofs = static_cast<IndexType>((i % 3) - 1);
            auto row = static_cast<IndexType>(i / 3);
            auto col = row + ofs;
            auto mask =
               static_cast<IndexType>(0 <= col && col < discretization_points);</pre>
            k_md.row_idxs[i] = mask * row;
k_md.col_idxs[i] = mask * col;
            k_md.values[i] = mask * coefs[ofs + 1];
        });
    md.sum_duplicates();
   matrix->read(std::move(md));
template <typename Closure, typename ValueType>
void generate_rhs(Closure&& f, ValueType u0, ValueType u1,
                  gko::matrix::Dense<ValueType>* rhs)
   const auto discretization_points = rhs->get_size()[0];
    auto k_rhs = gko::ext::kokkos::map_data(rhs);
    Kokkos::parallel_for(
        "generate_rhs", discretization_points, KOKKOS_LAMBDA(int i) {
            const ValueType h = 1.0 / (discretization_points + 1);
const ValueType xi = ValueType(i + 1) * h;
            k_{rhs}(i, 0) = -f(xi) * h * h;
if (i == 0) {
                k_{rhs}(i, 0) += u0;
            if (i == discretization_points - 1) {
                k_{rhs(i, 0)} += u1;
        });
template <typename Closure, typename ValueType>
double calculate_error(int discretization_points,
                       const gko::matrix::Dense<ValueType>* u,
                       Closure&& correct u)
    auto k_u = gko::ext::kokkos::map_data(u);
    auto error = 0.0;
    Kokkos::parallel_reduce(
        "calculate_error", discretization_points,
        KOKKOS_LAMBDA(int i, double& lsum) {
            const auto h = 1.0 / (discretization_points + 1); const auto xi = (i + 1) * h;
            lsum += Kokkos::abs((k_u(i, 0) - correct_u(xi)) /
                                 Kokkos::abs(correct_u(xi)));
        error);
    return error;
int main(int argc, char* argv[])
    using ValueType = double;
    using RealValueType = gko::remove_complex<ValueType>;
    using IndexType = int;
using vec = gko::matrix::Dense<ValueType>;
    using mtx = gko::matrix::Csr<ValueType, IndexType>;
    using cg = gko::solver::Cg<ValueType>;
    using bj = gko::preconditioner::Jacobi<ValueType>;
    Kokkos::ScopeGuard kokkos(argc, argv); // print Kokkos help
        std::exit(1);
    Kokkos::ScopeGuard kokkos(argc, argv);
    const auto discretization_points =
       static_cast<gko::size_type>(argc >= 2 ? std::atoi(argv[1]) : 100u);
    auto exec = gko::ext::kokkos::create_default_executor();
    auto correct_u = [] KOKKOS_FUNCTION(ValueType x) { return x * x * x; };
    auto f = [] KOKKOS_FUNCTION(ValueType x) { return ValueType{6} * x; };
    auto u0 = correct_u(0);
    auto u1 = correct_u(1);
    auto rhs = vec::create(exec, gko::dim<2>(discretization_points, 1));
    generate_rhs(f, u0, u1, rhs.get());
    auto u = vec::create(exec, gko::dim<2>(discretization_points, 1));
    u->fill(0.0);
    auto A = share(mtx::create(
        exec, gko::dim<2>{discretization_points, discretization_points}));
    generate_stencil_matrix(A.get());
    const RealValueType reduction_factor{1e-7};
```

# The minimal-cuda-solver program

The minimal CUDA solver example..

This example depends on simple-solver.

## Introduction

This is a minimal example that solves a system with Ginkgo. The matrix, right hand side and initial guess are read from standard input, and the result is written to standard output. The system matrix is stored in CSR format, and the system solved using the CG method, preconditioned with the block-Jacobi preconditioner. All computations are done on the GPU.

The easiest way to use the example data from the data/ folder is to concatenate the matrix, the right hand side and the initial solution (in that exact order), and pipe the result to the minimal\_solver\_cuda executable:

cat data/A.mtx data/b.mtx data/x0.mtx | ./minimal-cuda-solver

## About the example

## The commented program

## Results

0.0123025

The following is the expected result when using the data contained in the folder data as input:

```
%%MatrixMarket matrix array real general
0.252218
0.108645
0.0662811
0.0630433
0.0384088
0.0396536
0.0402648
0.0338935
0.0193098
0.0234653
0.0211499
0.0196413
0.0199151
0.0181674
0.0162722
0.0150714
0.0107016
0.0121141
```

## Comments about programming and debugging

# The mixed-multigrid-preconditioned-solver program

The preconditioned solver example..

This example depends on multigrid-preconditioned-solver, mixed-multigrid-solver.

# This example shows how to use the mixed-precision multigrid preconditioner.

In this example, we first read in a matrix from a file. The preconditioned CG solver is enhanced with a mixed-precision multigrid preconditioner. The example features the generating time and runtime of the CG solver.

```
Print version information
std::cout « gko::version_info::get() « std::endl;
const auto executor_string = argc >= 2 ? argv[1] : "reference";
Figure out where to run the code
std::map<std::string, std::function<std::shared_ptr<gko::Executor>()»
    exec map{
         {"omp", [] { return gko::OmpExecutor::create(); }},
              return gko::CudaExecutor::create(0,
                                                    gko::OmpExecutor::create());
         {"hip",
             return gko::HipExecutor::create(0, gko::OmpExecutor::create());
         {"dpcpp",
              return gko::DpcppExecutor::create(
                0, gko::ReferenceExecutor::create());
         {"reference", [] { return gko::ReferenceExecutor::create(); }}};
executor where Ginkgo will perform the computation
const auto exec = exec_map.at(executor_string)(); // throws if not valid
const int mixed_int = argc >= 3 ? std::atoi(argv[2]) : 1;
const bool use_mixed = mixed_int != 0; // nonzero uses mixed
std::cout « "Using mixed precision? " « use_mixed « std::endl;
```

```
auto A = share(gko::read<mtx>(std::ifstream("data/A.mtx"), exec));
Create RHS as 1 and initial guess as 0
gko::size_type size = A->get_size()[0];
auto host_x = vec::create(exec->get_master(), gko::dim<2>(size, 1));
auto host_b = vec::create(exec->get_master(), gko::dim<2>(size, 1));
for (auto i = 0; i < size; i++) {</pre>
    host_x->at(i, 0) = 0.;
    host_b->at(i, 0) = 1.;
auto x = vec::create(exec);
auto b = vec::create(exec);
x->copy_from(host_x);
b->copy_from(host_b);
Calculate initial residual by overwriting b
auto one = gko::initialize<vec>({1.0}, exec);
auto neg_one = gko::initialize<vec>({-1.0}, exec);
auto initres = gko::initialize<vec>({0.0}, exec);
A->apply(one, x, neg_one, b);
b->compute_norm2(initres);
copy b again
b->copy_from(host_b);
Prepare the stopping criteria
const gko::remove_complex<ValueType> tolerance = 1e-8;
auto iter_stop =
    gko::share(gko::stop::Iteration::build().with_max_iters(100u).on(exec));
auto tol_stop = gko::share(gko::stop::ResidualNorm<ValueType>::build()
                                 .with_baseline(gko::stop::mode::absolute)
                                 .with_reduction_factor(tolerance)
                                 .on(exec));
std::shared_ptr<const gko::log::Convergence<ValueType» logger =</pre>
    gko::log::Convergence<ValueType>::create();
iter_stop->add_logger(logger);
tol_stop->add_logger(logger);
Create smoother factory (ir with bj)
auto inner_solver_gen =
    gko::share(bj::build().with_max_block_size(lu).on(exec));
auto inner_solver_gen_f
    gko::share(bj_f::build().with_max_block_size(lu).on(exec));
auto smoother_gen = gko::share(
    ir::build()
        .with_solver(inner_solver_gen)
         .with_relaxation_factor(static_cast<ValueType>(0.9))
        .with_criteria(gko::stop::Iteration::build().with_max_iters(lu))
         .on(exec));
auto smoother_gen_f = gko::share(
    ir_f::build()
         .with solver(inner solver gen f)
        .with_relaxation_factor(static_cast<MixedType>(0.9))
         .with_criteria(gko::stop::Iteration::build().with_max_iters(1u))
Create MultigridLevel factory
auto mg_level_gen =
    gko::share(pgm::build().with_deterministic(true).on(exec));
auto mg_level_gen_f =
    gko::share(pgm_f::build().with_deterministic(true).on(exec));
Create CoarsestSolver factory
auto coarsest_gen = gko::share(
    ir::build()
         .with_solver(inner_solver_gen)
         .with_relaxation_factor(static_cast<ValueType>(0.9))
         .with_criteria(gko::stop::Iteration::build().with_max_iters(4u))
         .on(exec));
auto coarsest_gen_f = gko::share(
    ir_f::build()
         .with_solver(inner_solver_gen_f)
         .with_relaxation_factor(static_cast<MixedType>(0.9))
         .with_criteria(gko::stop::Iteration::build().with_max_iters(4u))
         .on(exec));
Create multigrid factory
std::shared_ptr<gko::LinOpFactory> multigrid_gen;
if (use_mixed) {
    multigrid_gen =
```

The first (index 0) level will use the first mg\_level\_gen, smoother\_gen which are the factories with ValueType. The rest of levels (>= 1) will use the second (index 1) mg\_level\_gen2 and smoother\_gen2 which use the MixedType. The rest of levels will use different type than the normal multigrid.

```
return level >= 1 ? 1 : 0;
            .with_coarsest_solver(coarsest_gen_f)
            .with_default_initial_guess(
                gko::solver::initial_guess_mode::zero)
            . \verb|with_criteria(gko::stop::Iteration::build().with_max_iters(1u))|\\
            .on(exec);
} else {
   multigrid gen
        mg::build()
            .with_max_levels(10u)
            .with_min_coarse_rows(2u)
            .with_pre_smoother(smoother_gen)
            .with_post_uses_pre(true)
            .with_mg_level(mg_level_gen)
.with_coarsest_solver(coarsest_gen)
            .with_default_initial_guess(
                gko::solver::initial_guess_mode::zero)
            .with_criteria(gko::stop::Iteration::build().with_max_iters(1u))
            .on(exec);
}
Create solver factory
auto solver_gen = cg::build()
                       .with_criteria(iter_stop, tol_stop)
                       .with_preconditioner(multigrid_gen)
                       .on(exec);
Create solver
std::chrono::nanoseconds gen_time(0);
auto gen_tic = std::chrono::steady_clock::now();
auto solver = solver_gen->generate(A);
exec->synchronize();
auto gen_toc = std::chrono::steady_clock::now();
gen_time +=
    std::chrono::duration cast<std::chrono::nanoseconds>(gen toc - gen tic);
Solve system
exec->svnchronize();
std::chrono::nanoseconds time(0);
auto tic = std::chrono::steady_clock::now();
solver->apply(b, x);
exec->synchronize();
auto toc = std::chrono::steady_clock::now();
time += std::chrono::duration_cast<std::chrono::nanoseconds>(toc - tic);
Calculate residual
auto res = gko::initialize<vec>({0.0}, exec);
A->apply(one, x, neg one, b);
b->compute_norm2(res);
std::cout « "Initial residual norm sqrt(r^T r): \n";
write(std::cout, initres);
std::cout « "Final residual norm sqrt(r^T r): n";
write(std::cout, res);
Print solver statistics
                                                " « logger->get_num_iterations()
    std::cout « "CG iteration count:
              « std::endl;
    std::cout « "CG generation time [ms]: "
              « static_cast<double>(gen_time.count()) / 1000000.0 « std::endl;
    std::cout « "CG execution time [ms]: "
              « static_cast<double>(time.count()) / 1000000.0 « std::endl;
    \verb|std::cout| & \verb|"CG| execution time per iteration[ms]:
              « static_cast<double>(time.count()) / 1000000.0 /
                     logger->get_num_iterations()
              « std::endl;
}
```

## **Results**

```
This is the expected output:
Initial residual norm sqrt(r^T r):
%%MatrixMarket matrix array real general
1 1
4.3589
Final residual norm sqrt(r^T r):
%%MatrixMarket matrix array real general
1 1
1.69858e-09
CG iteration count: 39
CG generation time [ms]: 2.04293
CG execution time [ms]: 22.3874
CG execution time per iteration[ms]: 0.574036
```

#### Comments about programming and debugging

```
#include <fstream>
#include <iomanip>
#include <iostream>
#include <map>
#include <string>
#include <ginkgo/ginkgo.hpp>
int main(int argc, char* argv[])
     using ValueType = double;
     using MixedType = float;
using IndexType = int;
     using vec = gko::matrix::Dense<ValueType>;
using mtx = gko::matrix::Csr<ValueType, IndexType>;
     using fcg = gko::solver::Fcg<ValueType>;
     using cg = gko::solver::Cg<ValueType>;
     using ir = gko::solver::Ir<ValueType>;
     using mg = gko::solver::Multigrid;
using bj = gko::preconditioner::Jacobi<ValueType, IndexType>;
using pgm = gko::multigrid::Pgm<ValueType, IndexType>;
     using cg_f = gko::solver::Cg<MixedType>;
     using ir_f = gko::solver::Ir<MixedType>;
     using bj_f = gko::preconditioner::Jacobi<MixedType, IndexType>;
     using pgm_f = gko::multigrid::Pgm<MixedType, IndexType>;
     std::cout « gko::version_info::get() « std::endl;
const auto executor_string = argc >= 2 ? argv[1] : "reference";
     std::map<std::string, std::function<std::shared_ptr<gko::Executor>()>
          exec map{
               {"omp", [] { return gko::OmpExecutor::create(); }},
               {"cuda",
                      return gko::CudaExecutor::create(0,
                                                                  gko::OmpExecutor::create());
                 }},
               {"hip",
                 [] {
                      return gko::HipExecutor::create(0, gko::OmpExecutor::create());
                 }},
               {"dpcpp",
                 [] {
                      return gko::DpcppExecutor::create(
                           0, gko::ReferenceExecutor::create());
               {"reference", [] { return gko::ReferenceExecutor::create(); }}};
     const auto exec = exec_map.at(executor_string)(); // throws if not valid const int mixed_int = argc >= 3 ? std::atoi(argv[2]) : 1; const bool use_mixed = mixed_int != 0; // nonzero uses mixed std::cout « "Using mixed precision? " « use_mixed « std::endl;
     auto A = share(gko::read<mtx>(std::ifstream("data/A.mtx"), exec));
     gko::size_type size = A->get_size()[0];
     auto host_x = vec::create(exec-yet_master(), gko::dim<2>(size, 1));
auto host_b = vec::create(exec-yet_master(), gko::dim<2>(size, 1));
     for (auto i = 0; i < size; i++) {</pre>
          host_x->at(i, 0) = 0.;
          host_b->at(i, 0) = 1.;
     auto x = vec::create(exec);
     auto b = vec::create(exec);
     x->copy_from(host_x);
     b->copy_from(host_b);
```

```
auto one = gko::initialize<vec>({1.0}, exec);
auto neg_one = gko::initialize<vec>({-1.0}, exec);
auto initres = gko::initialize<vec>({0.0}, exec);
A->apply(one, x, neg_one, b);
b->compute_norm2(initres);
b->copv from(host b);
const gko::remove_complex<ValueType> tolerance = 1e-8;
auto iter_stop =
   gko::share(gko::stop::Iteration::build().with_max_iters(100u).on(exec));
auto tol_stop = gko::share(gko::stop::ResidualNorm<ValueType>::build()
                                .with_baseline(gko::stop::mode::absolute)
                                 .with_reduction_factor(tolerance)
                                 .on(exec));
std::shared_ptr<const gko::log::Convergence<ValueType» logger =
   gko::log::Convergence<ValueType>::create();
iter_stop->add_logger(logger);
tol_stop->add_logger(logger);
auto inner_solver_gen =
    gko::share(bj::build().with_max_block_size(lu).on(exec));
auto inner_solver_gen_f
   gko::share(bj_f::build().with_max_block_size(lu).on(exec));
auto smoother_gen = gko::share(
   ir::build()
        .with_solver(inner_solver_gen)
        .with_relaxation_factor(static_cast<ValueType>(0.9))
        .with_criteria(gko::stop::Iteration::build().with_max_iters(lu))
auto smoother_gen_f = gko::share(
    ir_f::build()
        .with_solver(inner_solver_gen_f)
        .with relaxation factor(static cast<MixedType>(0.9))
        .with_criteria(gko::stop::Iteration::build().with_max_iters(1u))
auto mg_level_gen =
    gko::share(pgm::build().with_deterministic(true).on(exec));
auto mg_level_gen_f =
gko::share(pgm_f::build().with_deterministic(true).on(exec));
auto coarsest_gen = gko::share(
    ir::build()
        .with_solver(inner_solver_gen)
        .with_relaxation_factor(static_cast<ValueType>(0.9))
        .with_criteria(gko::stop::Iteration::build().with_max_iters(4u))
        .on(exec)):
auto coarsest_gen_f = gko::share(
    ir_f::build()
        .with_solver(inner_solver_gen_f)
        .with_relaxation_factor(static_cast<MixedType>(0.9))
        .with_criteria(gko::stop::Iteration::build().with_max_iters(4u))
        .on(exec));
std::shared ptr<gko::LinOpFactorv> multigrid gen;
if (use_mixed) {
    multigrid_gen =
        mg::build()
            .with_max_levels(10u)
            .with_min_coarse_rows(2u)
            .with_pre_smoother(smoother_gen, smoother_gen_f)
            .with_post_uses_pre(true)
            .with_mg_level(mg_level_gen, mg_level_gen_f)
            .with_level_selector([](const gko::size_type level,
                const gko::LinOp*) -> gko::size_type {
return level >= 1 ? 1 : 0;
            })
            .with_coarsest_solver(coarsest_gen_f)
            .with_default_initial_guess(
                 gko::solver::initial_guess_mode::zero)
            .with_criteria(gko::stop::Iteration::build().with_max_iters(lu))
            .on(exec);
} else {
   multigrid_gen =
        mg::build()
            .with_max_levels(10u)
            .with_min_coarse_rows(2u)
             .with_pre_smoother(smoother_gen)
            .with_post_uses_pre(true)
            .with_mg_level(mg_level_gen)
            .with_coarsest_solver(coarsest_gen)
            .with_default_initial_guess(
                 gko::solver::initial_guess_mode::zero)
            .with_criteria(gko::stop::Iteration::build().with_max_iters(1u))
            .on(exec):
auto solver_gen = cg::build()
                       .with_criteria(iter_stop, tol_stop)
                       .with_preconditioner(multigrid_gen)
                       .on(exec);
std::chrono::nanoseconds gen_time(0);
auto gen_tic = std::chrono::steady_clock::now();
```

```
auto solver = solver_gen->generate(A);
   exec->synchronize();
   auto gen_toc = std::chrono::steady_clock::now();
   gen_time +=
      std::chrono::duration_cast<std::chrono::nanoseconds>(gen_toc - gen_tic);
   exec->synchronize();
   std::chrono::nanoseconds time(0);
   auto tic = std::chrono::steady_clock::now();
   solver->apply(b, x);
   exec->synchronize();
   auto toc = std::chrono::steady_clock::now();
   time += std::chrono::duration_cast<std::chrono::nanoseconds>(toc - tic);
   auto res = gko::initialize<vec>({0.0}, exec);
   A->apply(one, x, neg_one, b);
   b->compute_norm2(res);
   std::cout « "Initial residual norm sqrt(r^T r): \n";
   write(std::cout, initres);
std::cout « "Final residual norm sqrt(r^T r): \n";
write(std::cout, res);
   std::cout « "CG iteration count:
                                          " « logger->get_num_iterations()
   « static_cast<double>(time.count()) / 1000000.0 « std::endl;
   std::cout « "CG execution time per iteration[ms]:
            « static_cast<double>(time.count()) / 1000000.0 /
                   logger->get_num_iterations()
             « std::endl;
}
```

# The mixed-multigrid-solver program

The mixed multigrid solver example..

This example depends on simple-solver.

# This example shows how to use the mixed-precision multigrid solver.

In this example, we first read in a matrix from a file, then generate a right-hand side and an initial guess. The multigrid solver can mix different precision of MultigridLevel. The example features the generating time and runtime of the multigrid solver.

## The commented program

```
std::cout « gko::version_info::get() « std::endl;
const auto executor_string = argc >= 2 ? argv[1] : "reference";
Figure out where to run the code
std::map<std::string, std::function<std::shared_ptr<gko::Executor>()»
    exec_map{
                 [] { return gko::OmpExecutor::create(); }},
               return gko::CudaExecutor::create(0,
                                                     gko::OmpExecutor::create());
          }},
         {"hip",
               return gko::HipExecutor::create(0, gko::OmpExecutor::create());
         {"dpcpp",
              return gko::DpcppExecutor::create(
                   0, gko::ReferenceExecutor::create());
         {"reference", [] { return gko::ReferenceExecutor::create(); }}};
executor where Ginkgo will perform the computation
const auto exec = exec_map.at(executor_string)();
const int mixed_int = argc >= 3 ? std::atoi(argv[2]) : 1;
const bool use_mixed = mixed_int != 0; // nonzero uses mixed
std::cout « "Using mixed precision? " « use_mixed « std::endl;
Read data
auto A = share(gko::read<mtx>(std::ifstream("data/A.mtx"), exec));
```

# Create RHS as 1 and initial guess as 0

```
auto host_x = vec::create(exec->get_master(), gko::dim<2>(size, 1));
auto host_b = vec::create(exec->get_master(), gko::dim<2>(size, 1));
for (auto i = 0; i < size; i++) {
   host_x->at(i, 0) = 0.;
host_b->at(i, 0) = 1.;
auto x = vec::create(exec);
auto b = vec::create(exec);
x->copy_from(host_x);
b->copy_from(host_b);
Calculate initial residual by overwriting b
auto one = gko::initialize<vec>({1.0}, exec);
auto neg_one = gko::initialize<vec>({-1.0}, exec);
auto initres = gko::initialize<vec>({0.0}, exec);
A->apply(one, x, neg_one, b);
b->compute_norm2(initres);
copy b again
b->copy_from(host_b);
Prepare the stopping criteria
const gko::remove_complex<ValueType> tolerance = 1e-12;
auto iter_stop =
    gko::share(gko::stop::Iteration::build().with_max_iters(100u).on(exec));
auto tol_stop = gko::share(gko::stop::ResidualNorm<ValueType>::build()
                                .with_baseline(gko::stop::mode::absolute)
                                 .with_reduction_factor(tolerance)
                                 .on(exec));
Create smoother factory (ir with bj)
auto smoother_gen = gko::share(
    ir::build()
        .with_solver(bj::build().with_max_block_size(1u))
        .with_relaxation_factor(static_cast<ValueType>(0.9))
        .with_criteria(gko::stop::Iteration::build().with_max_iters(1u))
         .on(exec));
auto smoother_gen2 = gko::share(
    ir2::build()
        .with_solver(bj2::build().with_max_block_size(1u))
        .with_relaxation_factor(static_cast<MixedType>(0.9))
        .with_criteria(gko::stop::Iteration::build().with_max_iters(1u))
        .on(exec));
Create RestrictProlong factory
auto mg_level_gen
    gko::share(pgm::build().with_deterministic(true).on(exec));
auto mg level gen2 =
    gko::share(pgm2::build().with_deterministic(true).on(exec));
Create CoarsesSolver factory
auto coarsest_solver_gen = gko::share(
    ir::build()
         .with_solver(bj::build().with_max_block_size(1u))
        .with_relaxation_factor(static_cast<ValueType>(0.9))
        .with_criteria(gko::stop::Iteration::build().with_max_iters(4u))
        .on(exec));
auto coarsest_solver_gen2 = gko::share(
    ir2::build()
        .with_solver(bj2::build().with_max_block_size(1u))
        .with\_relaxation\_factor(static\_cast<MixedType>(0.9))\\
        .with_criteria(gko::stop::Iteration::build().with_max_iters(4u))
        .on(exec));
Create multigrid factory
std::shared_ptr<gko::LinOpFactory> multigrid_gen;
if (use_mixed) {
    multigrid_gen =
        mg::build()
             .with_max_levels(10u)
             .with_min_coarse_rows(2u)
             .with_pre_smoother(smoother_gen, smoother_gen2)
            .with_post_uses_pre(true)
             .with_mg_level(mg_level_gen, mg_level_gen2)
             .with_level_selector([](const gko::size_type level,
                                      const gko::LinOp*) -> gko::size_type {
```

The first (index 0) level will use the first mg\_level\_gen, smoother\_gen which are the factories with ValueType. The rest of levels (>= 1) will use the second (index 1) mg\_level\_gen2 and smoother\_gen2 which use the MixedType. The rest of levels will use different type than the normal multigrid.

```
return level >= 1 ? 1 : 0;
            .with_coarsest_solver(coarsest_solver_gen2)
            .with_criteria(iter_stop, tol_stop)
            .on(exec);
} else {
   multigrid_gen = mg::build()
                        .with_max_levels(10u)
                        .with_min_coarse_rows(2u)
                        .with_pre_smoother(smoother_gen)
                        . \verb|with_post_uses_pre| (true)
                        .with_mg_level(mg_level_gen)
                        .with_coarsest_solver(coarsest_solver_gen)
                        .with_criteria(iter_stop, tol_stop)
                        .on(exec);
std::chrono::nanoseconds gen_time(0);
auto gen_tic = std::chrono::steady_clock::now();
auto solver = solver_gen->generate(A);
auto solver = multigrid_gen->generate(A);
exec->svnchronize();
auto gen toc = std::chrono::steady clock::now();
    std::chrono::duration_cast<std::chrono::nanoseconds>(gen_toc - gen_tic);
Add logger
std::shared_ptr<const gko::log::Convergence<ValueType» logger =</pre>
    gko::log::Convergence<ValueType>::create();
solver->add_logger(logger);
Solve system
exec->synchronize();
std::chrono::nanoseconds time(0);
auto tic = std::chrono::steady_clock::now();
solver->apply(b, x);
exec->synchronize();
auto toc = std::chrono::steady_clock::now();
time += std::chrono::duration_cast<std::chrono::nanoseconds>(toc - tic);
Calculate residual explicitly, because the residual is not available inside of the multigrid solver
auto res = gko::initialize<vec>({0.0}, exec);
A->apply(one, x, neg_one, b);
b->compute_norm2(res);
std::cout « "Initial residual norm sqrt(r^T r): \n";
write(std::cout, initres);
std::cout « "Final residual norm sqrt(r^T r): \n";
write(std::cout, res);
Print solver statistics
    std::cout « "Multigrid iteration count:
              « logger->get_num_iterations() « std::endl;
    std::cout « "Multigrid generation time [ms]: "
              « static_cast<double>(gen_time.count()) / 1000000.0 « std::endl;
    std::cout « "Multigrid execution time per iteration[ms]:
             « static_cast<double>(time.count()) / 1000000.0 /
                     logger->get_num_iterations()
              « std::endl;
```

## Results

## This is the expected output:

```
Initial residual norm sqrt(r^T r):
%%MatrixMarket matrix array real general
1 1
4.3589
Final residual norm sqrt(r^T r):
%%MatrixMarket matrix array real general
1 1
6.31088e-14
Multigrid iteration count: 9
Multigrid generation time [ms]: 3.35361
Multigrid execution time [ms]: 10.048
Multigrid execution time per iteration[ms]: 1.11644
```

## Comments about programming and debugging

```
#include <fstream>
#include <iomanip>
#include <iostream>
#include <map>
#include <string>
#include <ginkgo/ginkgo.hpp>
int main(int argc, char* argv[])
    using ValueType = double;
    using MixedType = float;
    using IndexType = int;
    using vec = gko::matrix::Dense<ValueType>;
    using mtx = gko::matrix::Csr<ValueType, IndexType>;
    using fcg = gko::solver::Fcg<ValueType>;
    using cg = gko::solver::Cg<MixedType>;
using ir = gko::solver::Ir<ValueType>;
    using ir2 = gko::solver::Ir<MixedType>;
    using mg = gko::solver::Multigrid;
using bj = gko::preconditioner::Jacobi<ValueType, IndexType>;
    using bj2 = gko::preconditioner::Jacobi<MixedType, IndexType>;
using pgm = gko::multigrid::Pgm<ValueType, IndexType>;
    using pgm2 = gko::multigrid::Pgm<MixedType, IndexType>;
    std::cout « gko::version_info::get() « std::endl;
const auto executor_string = argc >= 2 ? argv[1] : "reference";
    std::map<std::string, std::function<std::shared_ptr<gko::Executor>()>
        exec_map{
                     [] { return gko::OmpExecutor::create(); }},
             { "omp",
             {"cuda",
              [] {
                   return gko::CudaExecutor::create(0,
                                                        gko::OmpExecutor::create());
              } } ,
             { "hip",
                  return gko::HipExecutor::create(0, gko::OmpExecutor::create());
             {"dpcpp",
                   return gko::DpcppExecutor::create(
                       0, gko::ReferenceExecutor::create());
             {"reference", [] { return gko::ReferenceExecutor::create(); }}};
    const auto exec = exec_map.at(executor_string)(); // throws if not valid
    const int mixed_int = argc >= 3 ? std::atoi(argv[2]) : 1;
const bool use_mixed = mixed_int != 0; // nonzero uses mixed
std::cout « "Using mixed precision? " « use_mixed « std::endl;
    auto A = share(gko::read<mtx>(std::ifstream("data/A.mtx"), exec));
    gko::size_type size = A->get_size()[0];
    auto host_x = vec::create(exec->get_master(), gko::dim<2>(size, 1));
    auto host_b = vec::create(exec->get_master(), gko::dim<2>(size, 1));
    for (auto i = 0; i < size; i++) {</pre>
        host_x->at(i, 0) = 0.;
        host_b->at(i, 0) = 1.;
    auto x = vec::create(exec);
    auto b = vec::create(exec);
    x->copy_from(host_x);
    b->copy_from(host_b);
    auto one = gko::initialize<vec>({1.0}, exec);
    auto neg_one = gko::initialize<vec>((-1.0), exec);
    auto initres = gko::initialize<vec>({0.0}, exec);
    A->apply(one, x, neg_one, b);
    b->compute_norm2(initres);
    b->copy_from(host_b);
    const gko::remove_complex<ValueType> tolerance = 1e-12;
    auto iter stop =
        gko::share(gko::stop::Iteration::build().with_max_iters(100u).on(exec));
    auto tol_stop = gko::share(gko::stop::ResidualNorm<ValueType>::build()
                                       .with_baseline(gko::stop::mode::absolute)
                                       .with_reduction_factor(tolerance)
                                       .on(exec));
    auto smoother_gen = gko::share(
             .with_solver(bj::build().with_max_block_size(1u))
             .with_relaxation_factor(static_cast<ValueType>(0.9))
             .with_criteria(gko::stop::Iteration::build().with_max_iters(1u))
             .on(exec));
    auto smoother gen2 = gko::share(
        ir2::build()
             .with_solver(bj2::build().with_max_block_size(1u))
```

```
.with_relaxation_factor(static_cast<MixedType>(0.9))
        .with_criteria(gko::stop::Iteration::build().with_max_iters(1u))
        on (exec));
auto mg_level_gen =
   gko::share(pgm::build().with_deterministic(true).on(exec));
auto mg level gen2 =
   gko::share(pgm2::build().with_deterministic(true).on(exec));
auto coarsest_solver_gen = gko::share(
   ir::build()
        .with_solver(bj::build().with_max_block_size(1u))
        .with_relaxation_factor(static_cast<ValueType>(0.9))
        .with_criteria(qko::stop::Iteration::build().with_max_iters(4u))
        .on(exec));
auto coarsest_solver_gen2 = gko::share(
    ir2::build()
        . \verb|with_solver(bj2::build().with_max_block_size(1u))|\\
        .with_relaxation_factor(static_cast<MixedType>(0.9))
        .with_criteria(gko::stop::Iteration::build().with_max_iters(4u))
        .on(exec));
std::shared_ptr<gko::LinOpFactory> multigrid_gen;
if (use_mixed) {
   multigrid_gen =
       mg::build()
            .with_max_levels(10u)
            .with_min_coarse_rows(2u)
            .with_pre_smoother(smoother_gen, smoother_gen2)
            .with_post_uses_pre(true)
            .with_mg_level(mg_level_gen, mg_level_gen2)
            .with_level_selector([](const gko::size_type level,
                                   const gko::LinOp*) -> gko::size_type {
               return level >= 1 ? 1 : 0;
           1)
            .with_coarsest_solver(coarsest_solver_gen2)
            .with_criteria(iter_stop, tol_stop)
            .on(exec);
} else {
   multigrid gen = mg::build()
                        .with_max_levels(10u)
                        .with_min_coarse_rows(2u)
                        .with_pre_smoother(smoother_gen)
                        .with_post_uses_pre(true)
                        .with_mg_level(mg_level_gen)
                        .with_coarsest_solver(coarsest_solver_gen)
                        .with_criteria(iter_stop, tol_stop)
                        .on(exec);
std::chrono::nanoseconds gen_time(0);
auto gen_tic = std::chrono::steady_clock::now();
auto solver = multigrid_gen->generate(A);
exec->svnchronize();
auto gen_toc = std::chrono::steady_clock::now();
gen_time +=
   std::chrono::duration_cast<std::chrono::nanoseconds>(gen_toc - gen_tic);
std::shared_ptr<const gko::log::Convergence<ValueType» logger =</pre>
   gko::log::Convergence<ValueType>::create();
solver->add_logger(logger);
exec->synchronize();
std::chrono::nanoseconds time(0);
auto tic = std::chrono::steady_clock::now();
solver->apply(b, x);
exec->synchronize();
auto toc = std::chrono::steady_clock::now();
time += std::chrono::duration_cast<std::chrono::nanoseconds>(toc - tic);
auto res = gko::initialize<vec>({0.0}, exec);
A->apply(one, x, neg_one, b);
b->compute_norm2(res);
std::cout \stackrel{-}{\text{``}} "Initial residual norm sqrt(r^T r): \n";
write(std::cout, initres);
std::cout « "Final residual norm sqrt(r^T r): \n";
write(std::cout, res);
std::cout « "Multigrid iteration count:
         « logger->get_num_iterations() « std::endl;
std::cout \ll "Multigrid generation time [ms]: "
« static_cast<double>(time.count()) / 1000000.0 « std::endl;
std::cout « "Multigrid execution time per iteration[ms]:
         « static_cast<double>(time.count()) / 1000000.0 /
                logger->get_num_iterations()
         « std::endl:
```

# The mixed-precision-ir program

The Mixed Precision Iterative Refinement (MPIR) solver example..

This example depends on iterative-refinement.

# This example manually implements a Mixed Precision Iterative Refinement (MPIR) solver.

In this example, we first read in a matrix from file, then generate a right-hand side and an initial guess. An inaccurate CG solver in single precision is used as the inner solver to an iterative refinement (IR) in double precision method which solves a linear system.

# The commented program

```
Print version information
std::cout « gko::version_info::get() « std::endl;
Figure out where to run the code
   (argc == 2 && (std::string(argv[1]) == "--help")) {
  std::cerr « "Usage: " « argv[0] « " [executor]" « std::endl;
    std::exit(-1);
const auto executor_string = argc >= 2 ? argv[1] : "reference";
std::map<std::string, std::function<std::shared_ptr<gko::Executor>()»
    exec_map{
        "" ("omp", [] { return gko::OmpExecutor::create(); }},
"" ("ouda",
              return gko::CudaExecutor::create(0,
                                                 gko::OmpExecutor::create());
        {"hip",
             return gko::HipExecutor::create(0, gko::OmpExecutor::create());
        {"dpcpp",
             return gko::DpcppExecutor::create(
               0, gko::ReferenceExecutor::create());
        {"reference", [] { return gko::ReferenceExecutor::create(); }};
executor where Ginkgo will perform the computation
const auto exec = exec_map.at(executor_string)(); // throws if not valid
```

```
Read data
```

```
auto A = share(gko::read<mtx>(std::ifstream("data/A.mtx"), exec));
Create RHS and initial guess as 1
gko::size_type size = A->get_size()[0];
auto host_x = vec::create(exec->get_master(), gko::dim<2>(size, 1));
for (auto i = 0; i < size; i++) {
    host_x->at(i, 0) = 1.;
auto x = gko::clone(exec, host_x);
auto b = gko::clone(exec, host_x);
Calculate initial residual by overwriting b
auto one = gko::initialize<vec>({1.0}, exec);
auto neq_one = gko::initialize<vec>({-1.0}, exec);
auto initres_vec = gko::initialize<real_vec>({0.0}, exec);
A->apply(one, x, neg_one, b);
b->compute_norm2(initres_vec);
Build lower-precision system matrix and residual
auto solver_A = solver_mtx::create(exec);
auto inner_residual = solver_vec::create(exec);
auto outer_residual = vec::create(exec);
A->convert_to(solver_A);
b->convert_to(outer_residual);
restore b
b->copy_from(host_x);
Create inner solver
auto inner_solver
     cg::build()
         .with_criteria(
              gko::stop::ResidualNorm<SolverType>::build()
              .with_reduction_factor(inner_reduction_factor),
gko::stop::Iteration::build().with_max_iters(max_inner_iters))
         ->generate(give(solver_A));
Solve system
exec->synchronize();
std::chrono::nanoseconds time(0);
auto res_vec = gko::initialize<real_vec>((0.0), exec);
auto initres = exec->copy_val_to_host(initres_vec->get_const_values());
auto inner_solution = solver_vec::create(exec);
auto outer_delta = vec::create(exec);
auto tic = std::chrono::steady_clock::now();
int iter = -1;
while (true) {
    ++iter;
convert residual to inner precision
outer_residual->convert_to(inner_residual);
outer_residual->compute_norm2 (res_vec);
auto res = exec->copy_val_to_host(res_vec->get_const_values());
break if we exceed the number of iterations or have converged
if (iter > max_outer_iters || res / initres < outer_reduction_factor) {</pre>
}
Use the inner solver to solve A * inner_solution = inner_residual with residual as initial guess.
inner_solution->copy_from(inner_residual);
inner_solver->apply(inner_residual, inner_solution);
convert inner solution to outer precision
inner_solution->convert_to(outer_delta);
x = x + inner solution
x->add_scaled(one, outer_delta);
residual = b - A * x
     outer_residual->copy_from(b);
     A->apply(neg_one, x, one, outer_residual);
auto toc = std::chrono::steady_clock::now();
```

```
time += std::chrono::duration_cast<std::chrono::nanoseconds>(toc - tic);
```

#### Calculate residual

## Results

### This is the expected output:

```
Initial residual norm sqrt(r^T r):
%%MatrixMarket matrix array real general
1 1
194.679
Final residual norm sqrt(r^T r):
%%MatrixMarket matrix array real general
1 1
1.22728e-10
MPIR iteration count: 25
MPIR execution time [ms]: 0.846559
```

### Comments about programming and debugging

```
#include <fstream>
#include <iomanip>
#include <iostream>
#include <map>
#include <string>
#include <ginkgo/ginkgo.hpp>
int main(int argc, char* argv[])
    using ValueType = double;
    using RealValueType = gko::remove_complex<ValueType>;
    using SolverType = float;
    using RealSolverType = gko::remove_complex<SolverType>;
    using IndexType = int;
    using vec = gko::matrix::Dense<ValueType>;
    using real_vec = gko::matrix::Dense<RealValueType>;
    using solver_vec = gko::matrix::Dense<SolverType>;
    using mtx = gko::matrix::Csr<ValueType, IndexType>;
    using solver_mtx = gko::matrix::Csr<SolverType, IndexType>;
    using cg = gko::solver::Cg<SolverType>;
    gko::size_type max_outer_iters = 100u;
    gko::size_type max_inner_iters = 100u;
    RealValueType outer_reduction_factor{1e-12};
    RealSolverType inner_reduction_factor{1e-2};
    std::cout « gko::version_info::get() « std::endl;
if (argc == 2 && (std::string(argv[1]) == "--help")) {
    std::cerr « "Usage: " « argv[0] « " [executor]" « std::endl;
        std::exit(-1);
    const auto executor_string = argc >= 2 ? argv[1] : "reference";
    exec_map{
            {"omp",
                    [] { return gko::OmpExecutor::create(); }},
            {"cuda",
                 return gko::CudaExecutor::create(0,
                                                    gko::OmpExecutor::create());
            }},
{"hip",
                 return gko::HipExecutor::create(0, gko::OmpExecutor::create());
```

```
}},
         {"dpcpp",
          [] {
              return gko::DpcppExecutor::create(
                   0, gko::ReferenceExecutor::create());
          11.
         {"reference", [] { return gko::ReferenceExecutor::create(); }};
const auto exec = exec_map.at(executor_string)(); // throws if not valid
auto A = share(gko::read<mtx>(std::ifstream("data/A.mtx"), exec));
gko::size_type size = A->get_size()[0];
auto host_x = vec::create(exec->get_master(), gko::dim<2>(size, 1));
for (auto i = 0; i < size; i++) {
    host_x->at(i, 0) = 1.;
auto x = gko::clone(exec, host_x);
auto b = gko::clone(exec, host_x);
auto one = gko::initialize<vec>((1.0), exec);
auto neg_one = gko::initialize<vec>((-1.0), exec);
auto initres_vec = gko::initialize<real_vec>((0.0), exec);
A->apply(one, x, neg_one, b);
b->compute_norm2(initres_vec);
auto solver_A = solver_mtx::create(exec);
auto inner_residual = solver_vec::create(exec);
auto outer_residual = vec::create(exec);
A->convert_to(solver_A);
b->convert_to(outer_residual);
b->copy_from(host_x);
auto inner_solver =
    cg::build()
         .with_criteria(
             gko::stop::ResidualNorm<SolverType>::build()
                  .with_reduction_factor(inner_reduction_factor),
             gko::stop::Iteration::build().with_max_iters(max_inner_iters))
         .on(exec)
        ->generate(give(solver_A));
exec->synchronize();
std::chrono::nanoseconds time(0);
auto res_vec = gko::initialize<real_vec>({0.0}, exec);
auto initres = exec->copy_val_to_host(initres_vec->get_const_values());
auto inner_solution = solver_vec::create(exec);
auto outer_delta = vec::create(exec);
auto tic = std::chrono::steady_clock::now();
int iter = -1;
while (true) {
    ++iter;
    outer_residual->convert_to(inner_residual);
    outer_residual->compute_norm2 (res_vec);
    auto res = exec->copy_val_to_host(res_vec->get_const_values());
    if (iter > max_outer_iters || res / initres < outer_reduction_factor) {</pre>
        break:
    inner_solution->copy_from(inner_residual);
    inner_solver->apply(inner_residual, inner_solution);
    inner_solution->convert_to(outer_delta);
    x->add_scaled(one, outer_delta);
    outer_residual->copy_from(b);
    A->apply(neg_one, x, one, outer_residual);
auto toc = std::chrono::steady_clock::now();
time += std::chrono::duration_cast<std::chrono::nanoseconds>(toc - tic);
A->apply(one, x, neg_one, b);
b->compute_norm2(res_vec);
std::cout « "Initial residual norm sqrt(r^T r):\n";
write(std::cout, initres_vec);
std::cout « "Final residual norm sqrt(r^T r):\n";
write(std::cout, res_vec);
std::cout « "MPIR iteration count:
std::cout « "MPIR execution time [ms]: "
                                                 " « iter « std::endl;
           « static_cast<double>(time.count()) / 1000000.0 « std::endl;
```

# The mixed-spmv program

The mixed spmv example..

## Introduction

This mixed spmv example should give the usage of Ginkgo mixed precision. This example is meant for you to understand how Ginkgo works with different precision of data. We encourage you to play with the code, change the parameters and see what is best suited for your purposes.

## About the example

Each example has the following sections:

- Introduction: This gives an overview of the example and mentions any interesting aspects in the example that might help the reader.
- 2. **The commented program:** This section is intended for you to understand the details of the example so that you can play with it and understand Ginkgo and its features better.
- 3. **Results:** This section shows the results of the code when run. Though the results may not be completely the same, you can expect the behaviour to be similar.
- 4. **The plain program:** This is the complete code without any comments to have an complete overview of the code.

# The commented program

```
* @param value_dist distribution of array values
* @param engine a random engine

*

* @return ValueType
* /

template <typename ValueType, typename ValueDistribution, typename Engine>
typename std::enable_if<!gko::is_complex_s<ValueType>::value, ValueType>::type
get_rand_value(ValueDistribution&& value_dist, Engine&& gen)
{
    return value_dist(gen);
}
/ **
* Specialization for complex types.
```

```
* @copydoc get_rand_value
template <typename ValueType, typename ValueDistribution, typename Engine>
typename std::enable_if<gko::is_complex_s<ValueType>::value, ValueType>::type
get_rand_value(ValueDistribution&& value_dist, Engine&& gen)
    return ValueType(value_dist(gen), value_dist(gen));
 * timing the apply operation A->apply(b, x). It will runs 2 warmup and get
 * average time among 10 times.
 * @return seconds
double timing(std::shared_ptr<const gko::Executor> exec,
              std::shared_ptr<const gko::LinOp> A,
              std::shared_ptr<const gko::LinOp> b,
              std::shared_ptr<gko::LinOp> x)
{
    int warmup = 2;
    int rep = 10;

for (int i = 0; i < warmup; i++) {
       A->apply(b, x);
    double total_sec = 0;
    for (int i = 0; i < rep; i++) {</pre>
always clone the x in each apply
auto xx = x -> clone();
synchronize to make sure data is already on device
exec->synchronize();
auto start = std::chrono::steadv clock::now();
A->apply(b, xx);
synchronize to make sure the operation is done
exec->synchronize();
auto stop = std::chrono::steady_clock::now();
get the duration in seconds
std::chrono::duration<double> duration_time = stop - start;
total_sec += duration_time.count();
if (i + 1 == rep) {
copy the result back to x
           x->copy_from(xx);
    return total sec / rep;
   // namespace
int main(int argc, char* argv[])
```

Use some shortcuts. In Ginkgo, vectors are seen as a gko::matrix::Dense with one column/one row. The advantage of this concept is that using multiple vectors is a now a natural extension of adding columns/rows are necessary.

```
using HighPrecision = double;
using RealValueType = gko::remove_complex<HighPrecision>;
using LowPrecision = float;
using IndexType = int;
using hp_vec = gko::matrix::Dense<HighPrecision>;
using lp_vec = gko::matrix::Dense<LowPrecision>;
using real_vec = gko::matrix::Dense<RealValueType>;
```

The gko::matrix::Ell class is used here, but any other matrix class such as gko::matrix::Coo, gko::matrix::Hybrid, gko::matrix::Csr or gko::matrix::Sellp could also be used. Note. the behavior will depends GINKGO\_MIXED\_PR← ECISION flags and the actual implementation from different matrices.

```
using hp_mtx = gko::matrix::Ell<HighPrecision, IndexType>;
using lp_mtx = gko::matrix::Ell<LowPrecision, IndexType>;
```

## Print the ginkgo version information.

```
std::cout « gko::version_info::get() « std::endl;
if (argc == 2 && (std::string(argv[1]) == "--help")) {
    std::cerr « "Usage: " « argv[0] « " [executor] " « std::endl;
    std::exit(-1);
```

#### Where do you want to run your operation?

The gko::Executor class is one of the cornerstones of Ginkgo. Currently, we have support for an gko::OmpExecutor, which uses OpenMP multi-threading in most of its kernels, a gko::ReferenceExecutor, a single threaded specialization of the OpenMP executor and a gko::CudaExecutor which runs the code on a NVIDIA GPU if available.

Note

With the help of C++, you see that you only ever need to change the executor and all the other functions/ routines within Ginkgo should automatically work and run on the executor with any other changes.

```
const auto executor_string = argc >= 2 ? argv[1] : "reference";
std::map<std::string, std::function<std::shared_ptr<gko::Executor>()»
    exec_map{
        \{"omp",
               [] { return gko::OmpExecutor::create(); }},
        {"cuda",
         [] {
             return gko::CudaExecutor::create(0,
                                              gko::OmpExecutor::create());
        {"hip",
         [] {
            return gko::HipExecutor::create(0, gko::OmpExecutor::create());
         }},
        { "dpcpp",
             return gko::DpcppExecutor::create(0,
                                               gko::OmpExecutor::create());
        {"reference", [] { return gko::ReferenceExecutor::create(); }}};
executor where Ginkgo will perform the computation
const auto exec = exec_map.at(executor_string)(); // throws if not valid
```

### Preparing your data and transfer to the proper device.

Read the matrix using the read function and set the right hand side randomly.

Note

Ginkgo uses C++ smart pointers to automatically manage memory. To this end, we use our own object ownership transfer functions that under the hood call the required smart pointer functions to manage object ownership. gko::share and gko::give are the functions that you would need to use.

```
read the matrix into HighPrecision and LowPrecision.
auto hp_A = share(gko::read<hp_mtx>(std::ifstream("data/A.mtx"), exec));
auto lp_A = share(gko::read<lp_mtx>(std::ifstream("data/A.mtx"), exec));
Set the shortcut for each dimension
auto A_dim = hp_A->get_size();
auto b_dim = gko::dim<2>{A_dim[1], 1};
auto x_dim = gko::dim<2>{A_dim[0], b_dim[1]};
auto host_b = hp_vec::create(exec->get_master(), b_dim);
fill the b vector with some random data
std::default_random_engine rand_engine(32);
auto dist = std::uniform_real_distribution<RealValueType>(0.0, 1.0);
for (int i = 0; i < host_b->get_size()[0]; i++)
    host_b->at(i, 0) = get_rand_value<HighPrecision>(dist, rand_engine);
copy the data from host to device
auto hp_b = share(gko::clone(exec, host_b));
auto lp_b = share(lp_vec::create(exec));
lp_b->copy_from(hp_b);
create several result x vector in different precision
auto hp_x = share(hp_vec::create(exec, x_dim));
auto lp_x = share(lp_vec::create(exec, x_dim));
auto hplp_x = share(hp_x->clone());
auto lplp_x = share(hp_x->clone());
auto lphp_x = share(hp_x->clone());
```

#### Measure the time of apply

We measure the time among different combination of apply operation.

```
Hp * Hp -> Hp
auto hp_sec = timing(exec, hp_A, hp_b, hp_x);

Lp * Lp -> Lp
auto lp_sec = timing(exec, lp_A, lp_b, lp_x);

Hp * Lp -> Hp
auto hplp_sec = timing(exec, hp_A, lp_b, hplp_x);

Lp * Lp -> Hp
auto lplp_sec = timing(exec, lp_A, lp_b, lplp_x);

Lp * Hp -> Hp
auto lphp_sec = timing(exec, lp_A, hp_b, lphp_x);
```

To measure error of result. neg\_one is an object that represent the number -1.0 which allows for a uniform interface when computing on any device. To compute the residual, all you need to do is call the add\_scaled method, which in this case is an axpy and equivalent to the LAPACK axpy routine. Finally, you compute the euclidean 2-norm with the compute\_norm2 function.

```
auto neg_one = gko::initialize<hp_vec>({-1.0}, exec);
auto hp_x_norm = gko::initialize<real_vec>({0.0}, exec->get_master());
auto lp_diff_norm = gko::initialize<real_vec>({0.0}, exec->get_master());
auto hplp_diff_norm = gko::initialize<real_vec>({0.0}, exec->get_master()); auto lplp_diff_norm = gko::initialize<real_vec>({0.0}, exec->get_master());
auto lphp_diff_norm = gko::initialize<real_vec>({0.0}, exec->get_master());
auto lp_diff = hp_x->clone();
auto hplp_diff = hp_x->clone();
auto lplp_diff = hp_x->clone();
auto lphp_diff = hp_x->clone();
hp_x->compute_norm2(hp_x_norm);
lp_diff->add_scaled(neg_one, lp_x);
lp_diff->compute_norm2(lp_diff_norm);
hplp_diff->add_scaled(neg_one, hplp_x);
hplp_diff->compute_norm2(hplp_diff_norm);
lplp_diff->add_scaled(neg_one, lplp_x);
lplp_diff->compute_norm2(lplp_diff_norm);
lphp_diff->add_scaled(neg_one, lphp_x);
lphp_diff->compute_norm2(lphp_diff_norm);
exec->synchronize();
std::cout.precision(10);
std::cout « std::scientific;
std::cout « "High Precision time(s): " « hp_sec « std::endl; std::cout « "High Precision result norm: " « hp_x_norm->at(0)
           « std::endl;
\verb|std::cout & "Low Precision time(s): " & lp_sec & std::endl;|\\
std::cout « "Hp * Lp -> Hp relative error:
std::cout « "Lp * Hp -> Hp relative error:
           « lphp_diff_norm->at(0) / hp_x_norm->at(0) « "\n";
```

## Results

## The following is the expected result (omp):

```
High Precision time(s): 2.0568800000e-05

High Precision result norm: 1.7725534998e+05

Low Precision time(s): 2.0955600000e-05

Low Precision relative error: 9.1052887738e-08

Hp * Lp -> Hp time(s): 2.1186100000e-05

Hp * Lp -> Hp relative error: 3.7799774251e-08

Lp * Lp -> Hp time(s): 2.0312300000e-05

Lp * Lp -> Hp relative error: 5.7910008031e-08

Lp * Hp -> Hp time(s): 2.0312300000e-05

Lp * Hp -> Hp relative error: 3.7173133506e-08
```

#### Comments about programming and debugging

```
#include <ginkgo/ginkgo.hpp>
#include <fstream>
#include <iostream>
#include <map>
#include <string>
#include <chrono>
#include <random>
namespace {
template <typename ValueType, typename ValueDistribution, typename Engine>
typename std::enable_if<!gko::is_complex_s<ValueType>::value, ValueType>::type
get_rand_value(ValueDistribution&& value_dist, Engine&& gen)
    return value_dist(gen);
template <typename ValueType, typename ValueDistribution, typename Engine> typename std::enable_if<gko::is_complex_s<ValueType>::value, ValueType>::type
get_rand_value(ValueDistribution&& value_dist, Engine&& gen)
    return ValueType(value_dist(gen), value_dist(gen));
double timing(std::shared_ptr<const gko::Executor> exec,
                std::shared_ptr<const gko::LinOp> A, std::shared_ptr<const gko::LinOp> b,
                std::shared_ptr<gko::LinOp> x)
    int warmup = 2;
    int rep = 10;
for (int i = 0; i < warmup; i++) {</pre>
         A->apply(b, x);
    double total_sec = 0;
    for (int i = 0; i < rep; i++) {</pre>
         auto xx = x->clone();
         exec->synchronize();
         auto start = std::chrono::steady_clock::now();
         A->apply(b, xx);
         exec->synchronize();
         auto stop = std::chrono::steady_clock::now();
         std::chrono::duration<double> duration_time = stop - start;
         total_sec += duration_time.count();
if (i + 1 == rep) {
             x->copy_from(xx);
    return total_sec / rep;
   // namespace
int main(int argc, char* argv[])
    using HighPrecision = double;
    using RealValueType = gko::remove_complex<HighPrecision>;
    using LowPrecision = float;
using IndexType = int;
    using hp_vec = gko::matrix::Dense<HighPrecision>;
using lp_vec = gko::matrix::Dense<LowPrecision>;
    using real_vec = gko::matrix::Dense<RealValueType>;
    using hp_mtx = gko::matrix::Ell<HighPrecision, IndexType>;
using lp_mtx = gko::matrix::Ell<LowPrecision, IndexType>;
    std::cout « gko::version_info::get() « std::endl;
    if (argc == 2 && (std::string(argv[1]) == "--help")) {
         std::cerr « "Usage: " « argv[0] « " [executor] " « std::endl;
         std::exit(-1);
    const auto executor_string = argc >= 2 ? argv[1] : "reference";
std::map<std::string, std::function<std::shared_ptr<gko::Executor>()>
         exec map{
              {"omp",
                      [] { return gko::OmpExecutor::create(); }},
              {"cuda",
               [] {
                    return gko::CudaExecutor::create(0,
                                                           gko::OmpExecutor::create());
               }},
              {"hip",
               [] {
                   return gko::HipExecutor::create(0, gko::OmpExecutor::create());
              { "dpcpp",
               [] {
                    return gko::DpcppExecutor::create(0,
                                                             gko::OmpExecutor::create());
```

```
{"reference", [] { return gko::ReferenceExecutor::create(); }}};
const auto exec = exec_map.at(executor_string)(); // throws if not valid
auto hp_A = share(gko::read<hp_mtx>(std::ifstream("data/A.mtx"), exec));
auto lp_A = share(gko::read<lp_mtx>(std::ifstream("data/A.mtx"), exec));
auto A_dim = hp_A->get_size();
auto x_dim = gko::dim<2>{A_dim[1], 1};
auto x_dim = gko::dim<2>{A_dim[0], b_dim[1]};
auto host_b = hp_vec::create(exec->get_master(), b_dim);
std::default_random_engine rand_engine(32);
auto dist = std::uniform_real_distribution<RealValueType>(0.0, 1.0);
for (int i = 0; i < host_b->qet_size()[0]; i++) {
     host_b->at(i, 0) = get_rand_value<HighPrecision>(dist, rand_engine);
auto hp_b = share(gko::clone(exec, host_b));
auto lp_b = share(lp_vec::create(exec));
lp_b->copy_from(hp_b);
auto hp_x = share(hp_vec::create(exec, x_dim));
auto lp_x = share(lp_vec::create(exec, x_dim));
auto hplp_x = share(hp_x->clone());
auto lplp_x = share(hp_x->clone());
auto lphp_x = share(hp_x->clone());
auto hp_sec = timing(exec, hp_A, hp_b, hp_x);
auto lp_sec = timing(exec, lp_A, lp_b, lp_x);
auto hplp_sec = timing(exec, hp_A, lp_b, hplp_x);
auto hplp_sec = timing(exec, hp_A, lp_b, hplp_x);
auto lplp_sec = timing(exec, lp_A, lp_b, lplp_x);
auto lphp_sec = timing(exec, lp_A, hp_b, lphp_x);
auto neg_one = gko::initialize<hp_vec>({-1.0}, exec);
auto hp_x_norm = gko::initialize<real_vec>({0.0}, exec->get_master());
auto lp_diff_norm = gko::initialize<real_vec>({0.0}, exec->get_master());
auto lp_diff_norm = gko::initialize<real_vec>({0.0}, exec->get_master());
auto lplp_diff_norm = gko::initialize<real_vec>({0.0}, exec->get_master());
auto lplp_diff_norm = gko::initialize<real_vec>({0.0}, exec->get_master());
auto lphp_diff_norm = gko::initialize<real_vec>({0.0}, exec->get_master());
auto lp_diff = hp_x->clone();
auto hplp_diff = hp_x->clone();
auto lplp_diff = hp_x->clone();
auto lphp_diff = hp_x->clone();
hp_x->compute_norm2(hp_x_norm);
lp_diff->add_scaled(neg_one, lp_x);
lp_diff->compute_norm2(lp_diff_norm);
hplp_diff->add_scaled(neg_one, hplp_x);
hplp_diff->compute_norm2(hplp_diff_norm);
lplp_diff->add_scaled(neg_one, lplp_x);
lplp_diff->compute_norm2(lplp_diff_norm);
lphp_diff->add_scaled(neg_one, lphp_x);
lphp_diff->compute_norm2(lphp_diff_norm);
exec->synchronize();
std::cout.precision(10);
std::cout « std::scientific;
std::cout « "High Precision time(s): " « hp_sec « std::endl;
std::cout « "High Precision result norm: " « hp_x_norm->at(0)
             « std::endl;
std::cout « "Low Precision time(s): " « lp_sec « std::endl;
« lphp_diff_norm->at(0) / hp_x_norm->at(0) « "\n";
```

# The multigrid-preconditioned-solver program

The preconditioned solver example..

This example depends on preconditioned-solver.

# This example shows how to use the multigrid preconditioner.

In this example, we first read in a matrix from a file. The preconditioned CG solver is enhanced with a multigrid preconditioner. The example features the generating time and runtime of the CG solver.

## The commented program

```
{"cuda",
     return gko::CudaExecutor::create(0,
                                         gko::OmpExecutor::create());
 }},
{"hip",
 [] {
    return gko::HipExecutor::create(0, gko::OmpExecutor::create());
}},
{"dpcpp",
    return gko::DpcppExecutor::create(
         0, gko::ReferenceExecutor::create());
{"reference", [] { return gko::ReferenceExecutor::create(); }}};
executor where Ginkgo will perform the computation
const auto exec = exec_map.at(executor_string)(); // throws if not valid
auto A = share(gko::read<mtx>(std::ifstream("data/A.mtx"), exec));
Create RHS as 1 and initial guess as 0
gko::size_type size = A->get_size()[0];
auto host_x = vec::create(exec->get_master(), gko::dim<2>(size, 1));
auto host_b = vec::create(exec->get_master(), gko::dim<2>(size, 1));
for (auto i = 0; i < size; i++) {
    host_x->at(i, 0) = 0.;
host_b->at(i, 0) = 1.;
auto x = vec::create(exec);
auto b = vec::create(exec);
x->copy_from(host_x);
b->copy_from(host_b);
```

Calculate initial residual by overwriting b

```
auto one = gko::initialize<vec>({1.0}, exec);
auto neg_one = gko::initialize<vec>({-1.0}, exec);
auto initres = gko::initialize<vec>({0.0}, exec);
A->apply(one, x, neg_one, b);
b->compute_norm2(initres);
copy b again
b->copy_from(host_b);
Create multigrid factory
std::shared_ptr<gko::LinOpFactory> multigrid_gen;
multigrid_gen =
    mg::build()
        .with_mg_level(pgm::build().with_deterministic(true))
        .with_criteria(gko::stop::Iteration::build().with_max_iters(lu))
        .on(exec);
const gko::remove_complex<ValueType> tolerance = 1e-8;
auto solver gen =
    cg::build()
        .with_criteria(gko::stop::Iteration::build().with_max_iters(100u),
                        gko::stop::ResidualNorm<ValueType>::build()
                            .with_baseline(gko::stop::mode::absolute)
                            .with_reduction_factor(tolerance))
        .with_preconditioner(multigrid_gen)
        .on(exec);
Create solver
std::chrono::nanoseconds gen_time(0);
auto gen_tic = std::chrono::steady_clock::now();
auto solver = solver_gen->generate(A);
exec->synchronize();
auto gen_toc = std::chrono::steady_clock::now();
    std::chrono::duration_cast<std::chrono::nanoseconds>(gen_toc - gen_tic);
Add logger
std::shared_ptr<const gko::log::Convergence<ValueType» logger =
    gko::log::Convergence<ValueType>::create();
solver->add_logger(logger);
Solve system
exec->synchronize();
std::chrono::nanoseconds time(0);
auto tic = std::chrono::steady_clock::now();
solver->apply(b, x);
exec->synchronize();
auto toc = std::chrono::steady_clock::now();
time += std::chrono::duration_cast<std::chrono::nanoseconds>(toc - tic);
Calculate residual
auto res = gko::as<vec>(logger->get_residual_norm());
std::cout « "Initial residual norm sqrt(r^T r): \n";
write(std::cout, initres);
std::cout « "Final residual norm sqrt(r^T r): \n";
write(std::cout, res);
Print solver statistics
                                                " « logger->get_num_iterations()
    std::cout « "CG iteration count:
              « std::endl;
    std::cout « "CG generation time [ms]: "
              « static_cast<double>(gen_time.count()) / 1000000.0 « std::endl;
    std::cout « "CG execution time [ms]: "
              « static_cast<double>(time.count()) / 1000000.0 « std::endl;
    std::cout « "CG execution time per iteration[ms]:
              « static_cast<double>(time.count()) / 1000000.0 /
                     logger->get_num_iterations()
              « std::endl;
```

## Results

#### This is the expected output:

```
Initial residual norm sqrt(r^T r):
%%MatrixMarket matrix array real general
1 1
```

```
4.3589
Final residual norm sqrt(r^T r):
%%MatrixMarket matrix array real general
1 1
1.69858e-09
CG iteration count: 39
CG generation time [ms]: 2.04293
CG execution time [ms]: 22.3874
CG execution time per iteration[ms]: 0.574036
```

#### Comments about programming and debugging

```
#include <fstream>
#include <iomanip>
#include <iostream>
#include <map>
#include <string>
#include <ginkgo/ginkgo.hpp>
int main(int argc, char* argv[])
    using ValueType = double;
    using IndexType = int;
    using vec = gko::matrix::Dense<ValueType>;
    using mtx = gko::matrix::Csr<ValueType, IndexType>;
    using cg = gko::solver::Cg<ValueType>;
    using mg = gko::solver::Multigrid;
    using pgm = gko::multigrid::Pgm<ValueType, IndexType>;
    std::cout « gko::version_info::get() « std::endl;
const auto executor_string = argc >= 2 ? argv[1] : "reference";
    std::map<std::string, std::function<std::shared_ptr<gko::Executor>()>
        exec_map{
             {"omp", [] { return gko::OmpExecutor::create(); }},
{"cuda",
             [] {
                 return gko::CudaExecutor::create(0,
                                                      gko::OmpExecutor::create());
             } } ,
             {"hip",
             [] {
                 return gko::HipExecutor::create(0, gko::OmpExecutor::create());
             {"dpcpp",
                  return gko::DpcppExecutor::create(
                      0, gko::ReferenceExecutor::create());
             {"reference", [] { return gko::ReferenceExecutor::create(); }}};
    const auto exec = exec_map.at(executor_string)(); // throws if not valid auto A = share(gko::read<mtx>(std::ifstream("data/A.mtx"), exec));
    gko::size_type size = A->get_size()[0];
    auto host_x = vec::create(exec->get_master(), gko::dim<2>(size, 1));
    auto host_b = vec::create(exec->get_master(), gko::dim<2>(size, 1));
    for (auto i = 0; i < size; i++) {</pre>
        host_x->at(i, 0) = 0.;
        host_b->at(i, 0) = 1.;
    auto x = vec::create(exec);
    auto b = vec::create(exec);
    x->copy_from(host_x);
    b->copy_from(host_b);
    auto one = gko::initialize<vec>({1.0}, exec);
    auto neg_one = gko::initialize<vec>({-1.0}, exec);
    auto initres = gko::initialize<vec>({0.0}, exec);
    A->apply(one, x, neg_one, b);
    b->compute_norm2(initres);
    b->copy_from(host_b);
    std::shared_ptr<gko::LinOpFactory> multigrid_gen;
    multigrid_gen =
        mg::build()
             .with_mg_level(pgm::build().with_deterministic(true))
             .with_criteria(gko::stop::Iteration::build().with_max_iters(1u))
             .on(exec);
    const gko::remove_complex<ValueType> tolerance = 1e-8;
    auto solver_gen =
        cq::build()
             .with_criteria(gko::stop::Iteration::build().with_max_iters(100u),
                             gko::stop::ResidualNorm<ValueType>::build()
                                 .with_baseline(gko::stop::mode::absolute)
                                 .with_reduction_factor(tolerance))
```

}

```
.with_preconditioner(multigrid_gen)
        .on(exec);
std::chrono::nanoseconds gen_time(0);
auto gen_tic = std::chrono::steady_clock::now();
auto solver = solver_gen->generate(A);
exec->synchronize();
auto gen_toc = std::chrono::steady_clock::now();
gen_time +=
    std::chrono::duration_cast<std::chrono::nanoseconds>(gen_toc - gen_tic);
std::shared_ptr<const gko::log::Convergence<ValueType» logger =
gko::log::Convergence<ValueType>::create();
solver->add_logger(logger);
exec->synchronize();
std::chrono::nanoseconds time(0);
auto tic = std::chrono::steady_clock::now();
solver->apply(b, x);
exec->synchronize();
auto toc = std::chrono::steady_clock::now();
time += std::chrono::duration_cast<std::chrono::nanoseconds>(toc - tic);
auto res = gko::as<vec>(logger->get_residual_norm());
std::cout « "Initial residual norm sqrt(r^T r): \n";
write(std::cout, initres);
std::cout « "Final residual norm sqrt(r^T r): \n";
" « logger->get_num_iterations()
« static_cast<double>(time.count()) / 1000000.0 « std::endl;
std::cout « "CG execution time per iteration[ms]: "

« static_cast<double>(time.count()) / 1000000.0 /
                 logger->get_num_iterations()
          « std::endl;
```

# The multigrid-preconditioned-solver-customized program

The customized multigrid preconditioned solver example..

This example depends on multigrid-preconditioned-solver.

# This example shows how to customize the multigrid preconditioner.

In this example, we first read in a matrix from a file. The preconditioned CG solver is enhanced with a multigrid preconditioner. Several non-default options are used to create this preconditioner. The example features the generating time and runtime of the CG solver.

## The commented program

```
exec map{
    ["omp", [] { return gko::OmpExecutor::create(); }},
{"cuda",
         return gko::CudaExecutor::create(0,
                                            gko::OmpExecutor::create());
    {"hip",
        return gko::HipExecutor::create(0, gko::OmpExecutor::create());
     } } ,
    {"dpcpp",
     [] {
         return gko::DpcppExecutor::create(
             0, gko::ReferenceExecutor::create());
    {"reference", [] { return gko::ReferenceExecutor::create(); }}};
executor where Ginkgo will perform the computation
const auto exec = exec_map.at(executor_string)(); // throws if not valid
auto A = share(gko::read<mtx>(std::ifstream("data/A.mtx"), exec));
Create RHS as 1 and initial guess as 0
gko::size_type size = A->get_size()[0];
auto host_x = vec::create(exec->get_master(), gko::dim<2>(size, 1));
auto host_b = vec::create(exec->get_master(), gko::dim<2>(size, 1));
for (auto i = 0; i < size; i++) {
    host_x->at(i, 0) = 0.;
   host_b->at(i, 0) = 1.;
```

```
auto x = vec::create(exec);
auto b = vec::create(exec);
x->copy_from(host_x);
b->copy_from(host_b);
Calculate initial residual by overwriting b
auto one = gko::initialize<vec>({1.0}, exec);
auto neg_one = gko::initialize<vec>({-1.0}, exec);
auto initres = gko::initialize<vec>({0.0}, exec);
A->apply(one, x, neg_one, b);
b->compute_norm2(initres);
copy b again
b->copy_from(host_b);
Prepare the stopping criteria
const gko::remove_complex<ValueType> tolerance = 1e-8;
    gko::share(gko::stop::Iteration::build().with_max_iters(100u).on(exec));
auto tol_stop = gko::share(gko::stop::ResidualNorm<ValueType>::build()
                                .with baseline (gko::stop::mode::absolute)
                                .with_reduction_factor(tolerance)
                                .on(exec));
auto exact_tol_stop =
    gko::share(gko::stop::ResidualNorm<ValueType>::build()
                   .with_baseline(gko::stop::mode::rhs_norm)
                   .with_reduction_factor(1e-14)
                   .on(exec));
std::shared_ptr<const gko::log::Convergence<ValueType» logger =</pre>
    gko::log::Convergence<ValueType>::create();
iter_stop->add_logger(logger);
tol_stop->add_logger(logger);
```

Now we customize some settings of the multigrid preconditioner. First we choose a smoother. Since the input matrix is spd, we use iterative refinement with two iterations and an Ic solver.

```
auto ic_gen = gko::share(
    ic::build()
        with_factorization(gko::factorization::Ic<ValueType, int>::build())
        on(exec));
auto smoother_gen = gko::share(
    gko::solver::build_smoother(ic_gen, 2u, static_cast<ValueType>(0.9)));

Use Pgm as the MultigridLevel factory.
auto mg_level_gen =
    gko::share(pgm::build().with_deterministic(true).on(exec));
```

Next we select a CG solver for the coarsest level. Again, since the input matrix is known to be spd, and the Pgm restriction preserves this characteristic, we can safely choose the CG. We reuse the lc factory here to generate an lc preconditioner. It is important to solve until machine precision here to get a good convergence rate.

Here we put the customized options together and create the multigrid factory.

```
std::shared_ptr<gko::LinOpFactory> multigrid_gen;
multigrid_gen =
    mg::build()
    .with_max_levels(10u)
    .with_min_coarse_rows(32u)
    .with_pre_smoother(smoother_gen)
    .with_post_uses_pre(true)
    .with_mg_level(mg_level_gen)
    .with_coarsest_solver(coarsest_gen)
    .with_default_initial_guess(gko::solver::initial_guess_mode::zero)
    .with_criteria(gko::stop::Iteration::build().with_max_iters(1u))
    .on(exec);
```

#### Create solver factory

#### Create solver

std::chrono::nanoseconds gen\_time(0);

```
auto gen_tic = std::chrono::steady_clock::now();
auto solver = solver_gen->generate(A);
exec->synchronize();
auto gen_toc = std::chrono::steady_clock::now();
gen_time +=
    std::chrono::duration cast<std::chrono::nanoseconds>(gen toc - gen tic);
Solve system
exec->synchronize();
std::chrono::nanoseconds time(0);
auto tic = std::chrono::steady_clock::now();
solver->apply(b, x);
exec->synchronize();
auto toc = std::chrono::steady_clock::now();
time += std::chrono::duration_cast<std::chrono::nanoseconds>(toc - tic);
Calculate residual
auto res = gko::initialize<vec>({0.0}, exec);
A->apply(one, x, neg_one, b);
b->compute_norm2(res);
std::cout « "Initial residual norm sqrt(r^T r): \n";
write(std::cout, initres);
std::cout « "Final residual norm sqrt(r^T r): n";
write(std::cout, res);
Print solver statistics
    std::cout « "CG iteration count:
                                               " « logger->get_num_iterations()
              « std::endl;
    std::cout « "CG generation time [ms]: "
              « static_cast<double>(gen_time.count()) / 1000000.0 « std::endl;
    std::cout « "CG execution time [ms]: "
              « static_cast<double>(time.count()) / 1000000.0 « std::endl;
    std::cout « "CG execution time per iteration[ms]:
             « static_cast<double>(time.count()) / 1000000.0 /
                     logger->get_num_iterations()
              « std::endl;
```

## Results

## This is the expected output:

```
Initial residual norm sqrt(r^T r):
%%MatrixMarket matrix array real general
1 1
25.9808
Final residual norm sqrt(r^T r):
%%MatrixMarket matrix array real general
1 1
5.81328e-09
CG iteration count: 12
CG generation time [ms]: 1.41642
CG execution time [ms]: 6.59244
CG execution time per iteration[ms]: 0.54937
```

## Comments about programming and debugging

```
#include <fstream>
#include <iomanip>
#include <iostream>
#include <map>
#include <string>
#include <ginkgo/ginkgo.hpp>
int main(int argc, char* argv[])
{
    using ValueType = double;
    using IndexType = int;
    using vec = gko::matrix::Dense<ValueType>;
    using mtx = gko::matrix::Csr<ValueType, IndexType>;
    using ir = gko::solver::Ir<ValueType>;
    using mg = gko::solver::Multigrid;
```

```
using ic = gko::preconditioner::Ic<gko::solver::LowerTrs<ValueType>>;
using pgm = gko::multigrid::Pgm<ValueType, IndexType>;
std::cout « gko::version_info::get() « std::endl;
const auto executor_string = argc >= 2 ? argv[1] : "reference";
std::map<std::string, std::function<std::shared_ptr<gko::Executor>()>
    exec map{
         {"omp", [] { return gko::OmpExecutor::create(); }},
         {"cuda",
         [] {
              return gko::CudaExecutor::create(0,
                                                  gko::OmpExecutor::create());
         }},
        {"hip",
          [] {
             return gko::HipExecutor::create(0, gko::OmpExecutor::create());
        {"dpcpp",
         [] {
             return gko::DpcppExecutor::create(
                  0, gko::ReferenceExecutor::create());
        {"reference", [] { return gko::ReferenceExecutor::create(); }}};
const auto exec = exec_map.at(executor_string)(); // throws if not valid
auto A = share(gko::read<mtx>(std::ifstream("data/A.mtx"), exec));
gko::size_type size = A->get_size()[0];
auto host_x = vec::create(exec->get_master(), gko::dim<2>(size, 1));
auto host_b = vec::create(exec->get_master(), gko::dim<2>(size, 1));
for (auto i = 0; i < size; i++) {</pre>
    host_x->at(i, 0) = 0.;
    host_b->at(i, 0) = 1.;
auto x = vec::create(exec);
auto b = vec::create(exec);
x->copy_from(host_x);
b->copy_from(host_b);
auto one = gko::initialize<vec>({1.0}, exec);
auto neg_one = gko::initialize<vec>({-1.0}, exec);
auto initres = gko::initialize<vec>({0.0}, exec);
A->apply(one, x, neg_one, b);
b->compute_norm2(initres);
b->copy_from(host_b);
const gko::remove_complex<ValueType> tolerance = 1e-8;
auto iter stop =
    gko::share(gko::stop::Iteration::build().with_max_iters(100u).on(exec));
auto tol_stop = gko::share(gko::stop::ResidualNorm<ValueType>::build()
                                 .with_baseline(gko::stop::mode::absolute)
                                  .with_reduction_factor(tolerance)
                                  .on(exec));
auto exact tol stop =
    gko::share(gko::stop::ResidualNorm<ValueType>::build()
                    .with_baseline(gko::stop::mode::rhs_norm)
                    .with_reduction_factor(1e-14)
                    .on(exec));
std::shared_ptr<const gko::log::Convergence<ValueType» logger =</pre>
   gko::log::Convergence<ValueType>::create();
iter_stop->add_logger(logger);
tol_stop->add_logger(logger);
auto ic_gen = gko::share(
    ic::build()
        .with_factorization(gko::factorization::Ic<ValueType, int>::build())
.on(exec));
auto smoother_gen = gko::share(
   gko::solver::build_smoother(ic_gen, 2u, static_cast<ValueType>(0.9)));
auto mg_level_gen =
    gko::share(pgm::build().with_deterministic(true).on(exec));
auto coarsest_gen = gko::share(cg::build()
                                      . \verb|with_preconditioner(ic_gen)|\\
                                      .with_criteria(iter_stop, exact_tol_stop)
                                      .on(exec));
std::shared_ptr<gko::LinOpFactory> multigrid_gen;
multigrid_gen =
    mg::build()
        .with_max_levels(10u)
        .with_min_coarse_rows(32u)
        .with_pre_smoother(smoother_gen)
        .with_post_uses_pre(true)
        .with_mg_level(mg_level_gen)
        .with_coarsest_solver(coarsest_gen)
         . with\_default\_initial\_guess (gko::solver::initial\_guess\_mode::zero) \\
        .with_criteria(gko::stop::Iteration::build().with_max_iters(lu))
         .on(exec);
auto solver_gen = cg::build()
                        .with_criteria(iter_stop, tol_stop)
                        .with_preconditioner(multigrid_gen)
                        .on(exec);
std::chrono::nanoseconds gen_time(0);
auto gen_tic = std::chrono::steady_clock::now();
```

```
auto solver = solver_gen->generate(A);
   exec->synchronize();
   auto gen_toc = std::chrono::steady_clock::now();
   gen_time +=
      std::chrono::duration_cast<std::chrono::nanoseconds>(gen_toc - gen_tic);
   exec->synchronize();
   std::chrono::nanoseconds time(0);
   auto tic = std::chrono::steady_clock::now();
   solver->apply(b, x);
   exec->synchronize();
   auto toc = std::chrono::steady_clock::now();
   time += std::chrono::duration_cast<std::chrono::nanoseconds>(toc - tic);
   auto res = gko::initialize<vec>({0.0}, exec);
   A->apply(one, x, neg_one, b);
   b->compute_norm2(res);
   std::cout « "Initial residual norm sqrt(r^T r): n";
   write(std::cout, initres);
std::cout « "Final residual norm sqrt(r^T r): \n";
write(std::cout, res);
   std::cout « "CG iteration count:
                                          " « logger->get_num_iterations()
   « static_cast<double>(time.count()) / 1000000.0 « std::endl;
   std::cout « "CG execution time per iteration[ms]:
            « static_cast<double>(time.count()) / 1000000.0 /
                   logger->get_num_iterations()
            « std::endl;
}
```

The multigrid-preconditioned-solver-customized program	

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# The nine-pt-stencil-solver program

The 9-point stencil example..

This example depends on simple-solver, three-pt-stencil-solver, poisson-solver.

## Introduction

This example solves a 2D Poisson equation:

[  $\Omega = (0,1)^2 \ D = [0,1]^2 \ U = (0,1)^2 \ U = (0,1)^2$ 

using a finite difference method on an equidistant grid with K discretization points (K can be controlled with a command line parameter). The discretization may be done by any order Taylor polynomial. For an equidistant grid with K "inner" discretization points ((x1,y1), \ldots, (xk,y1),(x1,y2), \ldots, (xk,yk,z1)) step size (h = 1 / (K + 1)) and a stencil (\in \mathb{R}^{3} \times 3), the formula produces a system of linear equations

 $(\sum_{a,b=-1}^{1} stencil(a,b) * u_{(i+a,j+b)} = -f_k h^2)$ , on any inner node with a neighborhood of inner nodes

On any node, where neighbor is on the border, the neighbor is replaced with a (-stencil(a,b) \* u\_{i+a,j+b}) and added to the right hand side vector. For example a node with a neighborhood of only edge nodes may look like this

```
[\sum_{a,b=-1}^{(1,0)} stencil(a,b) * u_{(i+a,j+b)} = -f_k h^2 - \sum_{a=-1}^{1} stencil(a,1) * u_{(i+a,j+1)}]
```

which is then solved using Ginkgo's implementation of the CG method preconditioned with block-Jacobi. It is also possible to specify on which executor Ginkgo will solve the system via the command line. The function f is set to (f(x,y) = 6x + 6y) (making the solution  $(u(x,y) = x^3)$ 

• y<sup>3</sup>)), but that can be changed in the main function. Also the stencil values for the core, the faces, the edge and the corners can be changed when passing additional parameters.

The intention of this is to show how generation of stencil values and the right hand side vector changes when increasing the dimension.

#### About the example

## The commented program

Stencil values. Ordering can be seen in the main function Can also be changed by passing additional parameter when executing

```
constexpr double default_alpha = 10.0 / 3.0;
constexpr double default_beta = -2.0 / 3.0;
constexpr double default_gamma = -1.0 / 6.0;
/ * Possible alternative default values are
  * default_alpha = 8.0;
  * default_beta = -1.0;
  * default_gamma = -1.0;
  * /
```

Creates a stencil matrix in CSR format for the given number of discretization points.

```
template <typename ValueType, typename IndexType>
ValueType* coefs)
   IndexType pos = 0;
   const size_t dp_2 = dp * dp;
row_ptrs[0] = pos;
for (IndexType k = 0; k < dp; ++k) {</pre>
       for (IndexType i = 0; i < dp; ++i) {
   const size_t index = i + k * dp;</pre>
           values[pos] = coefs[offset];
                      col_idxs[pos] = index + 1 + dp * j;
                      ++pos;
                  }
              }
           row_ptrs[index + 1] = pos;
      }
   }
}
```

Generates the RHS vector given f and the boundary conditions.

Iterating over the edges to add boundary values and adding the overlapping 3x1 to the rhs

```
for (size_t i = 0; i < dp; ++i) {
    const auto xi = ValueType(i + 1) * h;</pre>
```

```
const auto index_top = i;
     const auto index_bot = i + dp * (dp - 1);

rhs[index_top] -= u(xi - h, 0.0) * coefs[0];

rhs[index_top] -= u(xi, 0.0) * coefs[1];
     rhs[index_top] -= u(xi + h, 0.0) * coefs[2];
rhs[index_bot] -= u(xi - h, 1.0) * coefs[6];
     rhs[index_bot] -= u(xi, 1.0) * coefs[7];
     rhs[index_bot] -= u(xi + h, 1.0) * coefs[8];
for (size_t i = 0; i < dp; ++i) {
    const auto yi = ValueType(i + 1) * h;</pre>
     const auto index_left = i * dp;
const auto index_right = i * dp + (dp - 1);
     rhs[index_left] -= u(0.0, yi - h) * coefs[0];
rhs[index_left] -= u(0.0, yi) * coefs[3];
     rhs[index_left] -= u(0.0, yi + h) * coefs[6];
rhs[index_right] -= u(1.0, yi - h) * coefs[2];
rhs[index_right] -= u(1.0, yi) * coefs[5];
rhs[index_right] -= u(1.0, yi + h) * coefs[8];
}
remove the double corner values
     rhs[0] += u(0.0, 0.0) * coefs[0];

rhs[(dp - 1)] += u(1.0, 0.0) * coefs[2];

rhs[(dp - 1) * dp] += u(0.0, 1.0) * coefs[6];

rhs[dp * dp - 1] += u(1.0, 1.0) * coefs[8];
Prints the solution u.
template <typename ValueType, typename IndexType>
void print_solution(IndexType dp, const ValueType* u)
     for (IndexType i = 0; i < dp; ++i) {
    for (IndexType j = 0; j < dp; ++j)
        std::cout « u[i * dp + j] « '</pre>
          std::cout « '\n';
     std::cout « std::endl;
}
Computes the 1-norm of the error given the computed u and the correct solution function correct_u.
template <typename Closure, typename ValueType, typename IndexType>
gko::remove_complex<ValueType> calculate_error(IndexType dp, const ValueType* u,
                                                               Closure correct u)
     const ValueType h = 1.0 / (dp + 1);
     gko::remove_complex<ValueType> error = 0.0;
     for (IndexType j = 0; j < dp; ++j) {
           const auto xi = ValueType(j + 1) * h;
           for (IndexType i = 0; i < dp; ++i) {</pre>
               using std::abs;
                const auto yi = ValueType(i + 1) * h;
                error +=
                    abs(u[i * dp + j] - correct_u(xi, yi)) / abs(correct_u(xi, yi));
          }
     return error;
template <typename ValueType, typename IndexType>
void solve_system(const std::string& executor_string,
                        unsigned int discretization_points, IndexType* row_ptrs,
                        IndexType* col_idxs, ValueType* values, ValueType* rhs,
                        ValueType* u, gko::remove_complex<ValueType> reduction_factor)
{
Some shortcuts
using vec = gko::matrix::Dense<ValueType>;
using mtx = gko::matrix::Csr<ValueType, IndexType>;
using cg = gko::solver::Cg<ValueType>;
using bj = gko::preconditioner::Jacobi<ValueType, IndexType>;
using val_array = gko::array<ValueType>;
using idx_array = gko::array<IndexType>;
const auto@ dp = discretization_points;
const gko::size_type dp_2 = dp * dp;
Figure out where to run the code
std::map<std::string, std::function<std::shared_ptr<gko::Executor>()»
     exec_map{
           {"omp", [] { return gko::OmpExecutor::create(); }},
           {"cuda",
            [] {
```

```
return gko::CudaExecutor::create(0,
                                               gko::OmpExecutor::create());
         }},
        {"hip".
         [] {
             return gko::HipExecutor::create(0, gko::OmpExecutor::create());
        {"dpcpp",
         [] {
             return gko::DpcppExecutor::create(0,
                                                gko::OmpExecutor::create());
        {"reference", [] { return gko::ReferenceExecutor::create(); }}};
executor where Ginkgo will perform the computation
const auto exec = exec_map.at(executor_string)(); // throws if not valid
executor where the application initialized the data
const auto app_exec =
                      exec->get_master();
```

Tell Ginkgo to use the data in our application

Matrix: we have to set the executor of the matrix to the one where we want SpMVs to run (in this case <code>exec</code>). When creating array views, we have to specify the executor where the data is (in this case <code>app\_exec</code>).

If the two do not match, Ginkgo will automatically create a copy of the data on exec (however, it will not copy the data back once it is done

• here this is not important since we are not modifying the matrix).

Solution: we have to be careful here - if the executors are different, once we compute the solution the array will not be automatically copied back to the original memory locations. Fortunately, whenever  $\mathtt{apply}$  is called on a linear operator (e.g. matrix, solver) the arguments automatically get copied to the executor where the operator is, and copied back once the operation is completed. Thus, in this case, we can just define the solution on  $\mathtt{app\_exec}$ , and it will be automatically transferred to/from  $\mathtt{exec}$  if needed.

```
auto x = vec::create(app_exec, gko::dim<2>(dp_2, 1),
                     val_array::view(app_exec, dp_2, u), 1);
Generate solver
auto solver_gen =
    cg::build()
        .with_criteria(gko::stop::Iteration::build().with_max_iters(dp_2),
                       gko::stop::ResidualNorm<ValueType>::build()
                           .with_reduction_factor(reduction_factor))
        .with_preconditioner(bj::build())
        .on(exec);
auto solver = solver_gen->generate(gko::give(matrix));
Solve system
    solver->apply(b, x);
int main(int argc, char* argv[])
    using ValueType = double;
    using IndexType = int;
Print version information
std::cout « gko::version_info::get() « std::endl;
if (argc == 2 && std::string(argv[1]) == "--help") {
    std::cerr
```

« " [executor] [DISCRETIZATION\_POINTS] [alpha] [beta] [gamma]"

« "Usage: " « argv[0]

« std::endl;

```
std::exit(-1);
const auto executor_string = argc >= 2 ? argv[1] : "reference";
const IndexType discretization_points =
argc >= 3 ? std::atoi(argv[2]) : 100;
const ValueType alpha_c = argc >= 4 ? std::atof(argv[3]) : default_alpha;
const ValueType beta_c = argc >= 5 ? std::atof(argv[4]) : default_beta;
const ValueType gamma_c = argc >= 6 ? std::atof(argv[5]) : default_gamma;
clang-format off
std::array<ValueType, 9> coefs{
    gamma_c, beta_c, gamma_c,
        beta_c, alpha_c, beta_c,
    gamma_c, beta_c, gamma_c);
clang-format on
const auto dp = discretization_points;
const size_t dp_2 = dp * dp;
problem:
auto correct_u = [](ValueType x, ValueType y) {
   return x * x * x + y * y * y;
auto f = [](ValueType x, ValueType y) {
    return ValueType(6) * x + ValueType(6) * y;
matrix
std::vector<IndexType> row_ptrs(dp_2 + 1);
std::vector<IndexType> col_idxs((3 * dp - 2) * (3 * dp - 2));
std::vector<ValueType> values((3 * dp - 2) * (3 * dp - 2));
right hand side
std::vector<ValueType> rhs(dp_2);
std::vector<ValueType> u(dp_2, 0.0);
generate_stencil_matrix(dp, row_ptrs.data(), col_idxs.data(), values.data(),
                           coefs.data());
looking for solution u = x^3: f = 6x, u(0) = 0, u(1) = 1
generate_rhs(dp, f, correct_u, rhs.data(), coefs.data());
const gko::remove_complex<ValueType> reduction_factor = 1e-7;
auto start_time = std::chrono::steady_clock::now();
auto stop_time = std::chrono::steady_clock::now();
auto runtime_duration =
    static cast<double>(
        std::chrono::duration_cast<std::chrono::nanoseconds>(stop_time -
                                                                     start time)
             .count()) *
    1e-6;
Uncomment to print the solution print_solution(dp, u.data());
    std::cout « "The average relative error is "
               « calculate_error(dp, u.data(), correct_u) /
                       static_cast<gko::remove_complex<ValueType>> (dp_2)
               « std::endl;
    std::cout « "The runtime is " « std::to_string(runtime_duration) « " ms"
               « std::endl;
```

### Results

## The expected output should be

The average relative error is 6.35715e-06 The runtime is 167.320520 ms

## Comments about programming and debugging

```
This example solves a 2D Poisson equation:
\Omega = (0,1)^2
\Omega = [0,1]^2 (with boundary)
\partial\Omega = \Omega_b \backslash \Omega
u: \Omega_b -> R
u" = f in \Omega
u = u_D \text{ on } \beta
using a finite difference method on an equidistant grid with 'K' discretization
points ('K' can be controlled with a command line parameter). The discretization
may be done by any order Taylor polynomial.
For an equidistant grid with K "inner" discretization points (x1,y1),
(xk,y1), (x1,y2), ..., (xk,yk) step size h=1 / (K+1) and a stencil \in \R^{3} x 3}, the formula produces a system of linear equations
\sum_{a,b=-1}^1 \text{ stencil}(a,b) * u_{(i+a,j+b)} = -f_k h^2, on any inner node with
a neighborhood of inner nodes
On any node, where neighbor is on the border, the neighbor is replaced with a '-stencil(a,b) * u_{i}-ta,j+b)' and added to the right hand side vector. For
example a node with a neighborhood of only edge nodes may look like this
\sum_{a,b=-1}^{1} (1,0)  stencil(a,b) * u_{(i+a,j+b)} = -f_k h^2 - \sum_{a=-1}^1
stencil(a,1) * u_{(i+a,j+1)}
which is then solved using Ginkgo's implementation of the CG method
preconditioned with block-Jacobi. It is also possible to specify on which
The function 'f' is set to 'f(x,y) = 6x + 6y' (making the solution 'u(x,y) = x^3 + y^3'), but that can be changed in the 'main' function. Also the stencil values
for the core, the faces, the edge and the corners can be changed when passing
additional parameters.
The intention of this is to show how generation of stencil values and the right
hand side vector changes when increasing the dimension.
#include <array>
#include <chrono>
#include <iostream>
#include <map>
#include <string>
#include <vector>
#include <ginkgo/ginkgo.hpp>
constexpr double default_alpha = 10.0 / 3.0;
constexpr double default_beta = -2.0 / 3.0;
constexpr double default_gamma = -1.0 / 6.0;
 /* Possible alternative default values are
* default_alpha = 8.0;
* default_beta = -1.0;
* default_gamma = -1.0;
template <typename ValueType, typename IndexType>
void generate_stencil_matrix(IndexType dp, IndexType* row_ptrs,
                               IndexType* col_idxs, ValueType* values,
                              ValueType* coefs)
    IndexType pos = 0;
    const size_t dp_2 = dp * dp;
    row_ptrs[0] = pos;
    for (IndexType k = 0; k < dp; ++k) {
        if ((k + j) >= 0 & & (k + j) < dp & (i + 1) >= 0 & & (i + 1) < dp)
                         values[pos] = coefs[offset];
                         col_idxs[pos] = index + 1 + dp * j;
                          ++pos;
                     }
             row_ptrs[index + 1] = pos;
template <typename Closure, typename ClosureT, typename ValueType,
```

```
typename IndexType>
void generate_rhs(IndexType dp, Closure f, ClosureT u, ValueType* rhs,
                         ValueType* coefs)
     const size_t dp_2 = dp * dp;
     const ValueType h = 1.0 / (dp + 1.0);

for (IndexType i = 0; i < dp; ++i) {
           const auto yi = ValueType(i + 1) * h;
           for (IndexType j = 0; j < dp; ++j) {
    const auto xi = ValueType(j + 1) * h;</pre>
                 const auto index = i * dp + j;
                 rhs[index] = -f(xi, yi) * h * h;
           }
      for (size_t i = 0; i < dp; ++i) {
           const auto xi = ValueType(i + 1) * h;
           const auto index_top = i;
const auto index_bot = i + dp * (dp - 1);
rhs[index_top] -= u(xi - h, 0.0) * coefs[0];
           rhs[index_top] -= u(xi, 0.0) * coefs[1];
           rhs[index_top] -= u(xi + h, 0.0) * coefs[2];
rhs[index_bot] -= u(xi - h, 1.0) * coefs[6];
           rhs[index_bot] -= u(xi, 1.0) * coefs[7];
           rhs[index_bot] -= u(xi + h, 1.0) * coefs[8];
     for (size_t i = 0; i < dp; ++i) {
    const auto yi = ValueType(i + 1) * h;</pre>
           const auto index_left = i * dp;
const auto index_right = i * dp + (dp - 1);
           rhs[index_left] -= u(0.0, yi - h) * coefs[0];
rhs[index_left] -= u(0.0, yi) * coefs[3];
rhs[index_left] -= u(0.0, yi + h) * coefs[6];
rhs[index_right] -= u(1.0, yi - h) * coefs[2];
rhs[index_right] -= u(1.0, yi) * coefs[5];
           rhs[index\_right] = u(1.0, yi + h) * coefs[8];
     rhs[0] += u(0.0, 0.0) * coefs[0];
rhs[(dp - 1)] += u(1.0, 0.0) * coefs[2];
rhs[(dp - 1) * dp] += u(0.0, 1.0) * coefs[6];
rhs[dp * dp - 1] += u(1.0, 1.0) * coefs[8];
template <typename ValueType, typename IndexType>
void print_solution(IndexType dp, const ValueType* u)
     for (IndexType i = 0; i < dp; ++i) {
    for (IndexType j = 0; j < dp; ++j) {</pre>
                std::cout « u[i * dp + j] « ' ';
           std::cout « '\n';
     std::cout « std::endl;
template <typename Closure, typename ValueType, typename IndexType>
gko::remove_complex<ValueType> calculate_error(IndexType dp, const ValueType* u,
                                                                   Closure correct u)
     const ValueType h = 1.0 / (dp + 1);
     gko::remove_complex<ValueType> error = 0.0;
     for (IndexType j = 0; j < dp; ++j) {
    const auto xi = ValueType(j + 1) * h;</pre>
           for (IndexType i = 0; i < dp; ++i) {</pre>
                using std::abs;
const auto yi = ValueType(i + 1) * h;
                       abs(u[i * dp + j] - correct_u(xi, yi)) / abs(correct_u(xi, yi));
           }
     return error:
template <typename ValueType, typename IndexType>
void solve_system(const std::string& executor_string,
                          unsigned int discretization_points, IndexType* row_ptrs,
                          IndexType* col_idxs, ValueType* values, ValueType* rhs,
                         ValueType* u, gko::remove_complex<ValueType> reduction_factor)
     using vec = gko::matrix::Dense<ValueType>;
     using mtx = gko::matrix::Csr<ValueType, IndexType>;
     using cg = gko::solver::Cg<ValueType>;
using bj = gko::preconditioner::Jacobi<ValueType>;
using val_array = gko::array<ValueType>;
using idx_array = gko::array<IndexType>;
const auto& dp = discretization_points;
     const gko::size_type dp_2 = dp * dp;
     std::map<std::string, std::function<std::shared_ptr<gko::Executor>()»
           exec_map{
                 ("omp", [] { return gko::OmpExecutor::create(); }},
{"cuda",
```

```
return gko::CudaExecutor::create(0,
                                                               gko::OmpExecutor::create());
               }},
{"hip",
                [] {
                     return gko::HipExecutor::create(0, gko::OmpExecutor::create());
                } } ,
               { "dpcpp",
                [] {
                     return gko::DpcppExecutor::create(0,
                                                                gko::OmpExecutor::create());
               {"reference", [] { return gko::ReferenceExecutor::create(); }}};
     const auto exec = exec_map.at(executor_string)(); // throws if not valid
     const auto app_exec = exec->get_master();
     auto matrix = mtx::create(
         exec, gko::dim<2>(dp_2),
          val_array::view(app_exec, (3 * dp - 2) * (3 * dp - 2), values),
          idx_array::view(app_exec, (3 * dp - 2) * (3 * dp - 2), col_idxs),
idx_array::view(app_exec, dp_2 + 1, row_ptrs));
     auto b = vec::create(exec, gko::dim<2>(dp_2, 1),
                               val_array::view(app_exec, dp_2, rhs), 1);
     auto solver_gen
          cg::build()
               .with_criteria(gko::stop::Iteration::build().with_max_iters(dp_2),
                                 gko::stop::ResidualNorm<ValueType>::build()
                                      .with_reduction_factor(reduction_factor))
               .with preconditioner(bi::build())
               .on(exec);
     auto solver = solver_gen->generate(gko::give(matrix));
     solver->apply(b, x);
int main(int argc, char* argv[])
     using ValueType = double;
     using IndexType = int;
     std::cout « gko::version_info::get() « std::endl;
     if (argc == 2 && std::string(argv[1]) == "--help") {
          std::cerr
              « "Usage: " « argv[0]
               « " [executor] [DISCRETIZATION_POINTS] [alpha] [beta] [gamma]"
               « std::endl;
          std::exit(-1);
     const auto executor_string = argc >= 2 ? argv[1] : "reference";
    const duto executor_string = argc >= 2 / argv[i] : "reference";
const IndexType discretization_points =
    argc >= 3 ? std::atoi(argv[2]) : 100;
const ValueType alpha_c = argc >= 4 ? std::atof(argv[3]) : default_alpha;
const ValueType beta_c = argc >= 5 ? std::atof(argv[4]) : default_beta;
const ValueType gamma_c = argc >= 6 ? std::atof(argv[5]) : default_gamma;
     std::array<ValueType, 9> coefs{
         gamma_c, beta_c, gamma_c,
beta_c, alpha_c, beta_c,
gamma_c, beta_c, gamma_c);
     const auto dp = discretization_points;
     const size_t dp_2 = dp * dp;
auto correct_u = [](ValueType x, ValueType y) {
         return x * x * x + y * y * y;
     };
    auto f = [](ValueType x, ValueType y) {
    return ValueType(6) * x + ValueType(6) * y;
     std::vector<IndexType> row_ptrs(dp_2 + 1);
std::vector<IndexType> col_idxs((3 * dp - 2) * (3 * dp - 2));
std::vector<ValueType> values((3 * dp - 2) * (3 * dp - 2));
     std::vector<ValueType> rhs(dp_2);
     std::vector<ValueType> u(dp_2, 0.0);
     generate_stencil_matrix(dp, row_ptrs.data(), col_idxs.data(), values.data(),
                                   coefs.data());
     generate_rhs(dp, f, correct_u, rhs.data(), coefs.data());
const gko::remove_complex<ValueType> reduction_factor = 1e-7;
auto start_time = std::chrono::steady_clock::now();
     solve_system(executor_string, dp, row_ptrs.data(), col_idxs.data(),
                     values.data(), rhs.data(), u.data(), reduction_factor);
     auto stop_time = std::chrono::steady_clock::now();
     auto runtime_duration =
         static cast<double>(
              std::chrono::duration_cast<std::chrono::nanoseconds>(stop_time -
                                                                                  start_time)
                    .count()) *
         1e-6;
     std::cout « "The average relative error is "
                 « calculate_error(dp, u.data(), correct_u) /
                          static_cast<qko::remove_complex<ValueType>> (dp_2)
```

# The papi-logging program

The papi logging example..

This example depends on simple-solver-logging.

#### Introduction

#### About the example

```
template <typename T>
std::string\ to\_string\ (T*\ ptr)
      std::ostringstream os;
     os « reinterpret_cast<gko::uintptr>(ptr);
      return os.str();
int init_papi_counters(std::string solver_name, std::string A_name)
Initialize PAPI, add events and start it up
      int eventset = PAPI_NULL;
int ret_val = PAPI_library_init(PAPI_VER_CURRENT);
if (ret_val != PAPI_VER_CURRENT) {
    std::cerr « "Error at PAPI_library_init()" « std::endl;
            std::exit(-1);
      ret_val = PAPI_create_eventset(&eventset);
      if (PAPI_OK != ret_val) {
   std::cerr « "Error at PAPI_create_eventset()" « std::endl;
            std::exit(-1);
      std::string simple_apply_string("sde:::ginkgo0::linop_apply_completed::");
std::string advanced_apply_string(
    "sde:::ginkgo0::linop_advanced_apply_completed::");
      papi_add_event(simple_apply_string + solver_name, eventset);
papi_add_event(simple_apply_string + A_name, eventset);
      papi_add_event(advanced_apply_string + A_name, eventset);
ret_val = PAPI_start(eventset);
if (PAPI_OK != ret_val) {
            std::cerr « "Error at PAPI_start()" « std::endl;
            std::exit(-1);
      return eventset;
void print_papi_counters(int eventset)
```

```
Stop PAPI and read the linop_apply_completed event for all of them
```

```
long long int values[3];
int ret_val = PAPI_stop(eventset, values);
if (PAPI_OK != ret_val) {
    std::cerr « "Error at PAPI_stop()" « std::endl;
     std::exit(-1);
PAPI_shutdown();
Print all values returned from PAPI
     std::cout « "PAPI SDE counters:" « std::endl;
std::cout « "solver did " « values[0] « " applies." « std::endl;
std::cout « "A did " « values[1] « " simple applies." « std::endl;
std::cout « "A did " « values[2] « " advanced applies." « std::endl;
int main(int argc, char* argv[])
Some shortcuts
using ValueType = double;
using RealValueType = gko::remove_complex<ValueType>;
using IndexType = int;
using vec = gko::matrix::Dense<ValueType>;
using real_vec = gko::matrix::Dense<RealValueType>;
using mtx = gko::matrix::Csr<ValueType, IndexType>;
using cg = gko::solver::Cg<ValueType>;
Print version information
std::cout « gko::version_info::get() « std::endl;
if (argc == 2 && (std::string(argy[1]) == "--help")) {
   std::cerr « "Usage: " « argv[0] « " [executor]" « std::endl;
     std::exit(-1);
Figure out where to run the code
const auto executor_string = argc >= 2 ? argv[1] : "reference";
std::map<std::string, std::function<std::shared_ptr<gko::Executor>()»
     exec map{
          {"omp",
{"cuda",
                  [] { return gko::OmpExecutor::create(); }},
           [] {
               return gko::CudaExecutor::create(0,
                                                        gko::OmpExecutor::create());
           }},
          {"hip",
           [] {
               return gko::HipExecutor::create(0, gko::OmpExecutor::create());
           }},
          { "dpcpp",
           [] {
               return gko::DpcppExecutor::create(0,
                                                         gko::OmpExecutor::create());
          {"reference", [] { return gko::ReferenceExecutor::create(); }}};
executor where Ginkgo will perform the computation
const auto exec = exec_map.at(executor_string)(); // throws if not valid
Read data
auto A = share(gko::read<mtx>(std::ifstream("data/A.mtx"), exec));
auto b = gko::read<vec>(std::ifstream("data/b.mtx"), exec);
auto x = gko::read<vec>(std::ifstream("data/x0.mtx"), exec);
Generate solver
const RealValueType reduction_factor{1e-7};
auto solver_gen =
     cq::build()
          .with_criteria(gko::stop::Iteration::build().with_max_iters(20u),
                           gko::stop::ResidualNorm<ValueType>::build()
                                .with_reduction_factor(reduction_factor))
          .on(exec);
auto solver = solver_gen->generate(A);
```

In this example, we split as much as possible the Ginkgo solver/logger and the PAPI interface. Note that the PAPI ginkgo namespaces are of the form sde:::ginkgo<x> where <x> starts from 0 and is incremented with every new PAPI logger.

```
int eventset =
   init_papi_counters(to_string(solver.get()), to_string(A.get()));
```

```
Create a PAPI logger and add it to relevant LinOps
```

```
auto logger = gko::log::Papi<ValueType>::create(
    gko::log::Logger::linop_apply_completed_mask |
    \verb"gko::log::Logger::linop_advanced_apply_completed_mask");
solver->add_logger(logger);
A->add_logger(logger);
Solve system
solver->apply(b, x);
Stop PAPI event gathering and print the counters
print_papi_counters(eventset);
Print solution
std::cout « "Solution (x): n";
write(std::cout, x);
Calculate residual
    auto one = gko::initialize<vec>({1.0}, exec);
    auto neg_one = gko::initialize<vec>({-1.0}, exec);
    auto res = gko::initialize<real_vec>({0.0}, exec);
    A->apply(one, x, neg_one, b);
b->compute_norm2(res);
std::cout « "Residual norm sqrt(r^T r): \n";
    write(std::cout, res);
```

#### Results

#### The following is the expected result:

```
PAPI SDE counters:
solver did 1 applies.
A did 20 simple applies.
A did 1 advanced applies.
Solution (x):
%%MatrixMarket matrix array real general
0.252218
0.108645
0.0662811
0.0630433
0.0384088
0.0396536
0.0402648
0.0338935
0.0193098
0.0234653
0.0211499
0.0196413
0.0199151
0.0181674
0.0162722
0.0150714
0.0107016
0.0121141
0.0123025
Residual norm sqrt(r^T r):
%%MatrixMarket matrix array real general
8.87107e-16
```

#### Comments about programming and debugging

```
#include <fstream>
#include <iostream>
#include <map>
#include <string>
#include <thread>
#include <papi.h>
#include <ginkgo/ginkgo.hpp>
```

```
void papi_add_event(const std::string& event_name, int& eventset)
    int code;
    int ret_val = PAPI_event_name_to_code(event_name.c_str(), &code);
    if (PAPI_OK != ret_val) {
         std::cerr « "Error at PAPI_name_to_code()" « std::endl;
         std::exit(-1);
    ret_val = PAPI_add_event(eventset, code);
    if (PAPI_OK != ret_val) {
         std::cerr « "Error at PAPI_name_to_code()" « std::endl;
         std::exit(-1);
template <typename T>
std::string to_string(T* ptr)
    std::ostringstream os;
    os « reinterpret_cast<gko::uintptr>(ptr);
    return os.str();
} // namespace
int init_papi_counters(std::string solver_name, std::string A_name)
    int eventset = PAPI_NULL;
    int ret_val = PAPI_library_init(PAPI_VER_CURRENT);
    if (ret_val != PAPI_VER_CURRENT) {
         std::cerr « "Error at PAPI_library_init()" « std::endl;
         std::exit(-1);
    ret_val = PAPI_create_eventset(&eventset);
    if (PAPI_OK != ret_val) {
         std::cerr « "Error at PAPI_create_eventset()" « std::endl;
         std::exit(-1);
    ,std::string simple_apply_string("sde:::ginkgo0::linop_apply_completed::");
std::string advanced_apply_string(
         "sde:::ginkgo0::linop_advanced_apply_completed::");
    papi_add_event(simple_apply_string + solver_name, eventset);
papi_add_event(simple_apply_string + A_name, eventset);
    papi_add_event(advanced_apply_string + A_name, eventset);
    ret_val = PAPI_start(eventset);
    if (PAPI_OK != ret_val) {
         std::cerr « "Error at PAPI_start()" « std::endl;
         std::exit(-1);
    return eventset;
void print_papi_counters(int eventset)
    long long int values[3];
    int ret_val = PAPI_stop(eventset, values);
    if (PAPI_OK != ret_val) {
    std::cerr « "Error at PAPI_stop()" « std::endl;
         std::exit(-1);
    std::cout « "PAPI SDE counters:" « std::endl; std::cout « "solver did " « values[0] « " applies." « std::endl; std::cout « "A did " « values[1] « " simple applies." « std::endl; std::cout « "A did " « values[2] « " advanced applies." « std::endl;
int main(int argc, char* argv[])
    using ValueType = double;
    using RealValueType = gko::remove_complex<ValueType>;
    using IndexType = int;
    using vec = qko::matrix::Dense<ValueType>;
    using real_vec = gko::matrix::Dense<RealValueType>;
    using mtx = gko::matrix::Csr<ValueType, IndexType>;
    using cg = gko::solver::Cg<ValueType>;
    std::cout « gko::version_info::get() « std::endl;
if (argc == 2 && (std::string(argv[1]) == "--help")) {
    std::cerr « "Usage: " « argv[0] « " [executor]" « std::endl;
         std::exit(-1);
    const auto executor_string = argc >= 2 ? argv[1] : "reference";
    std::map<std::string, std::function<std::shared_ptr<gko::Executor>()>
         exec map{
              {"omp"
                       [] { return gko::OmpExecutor::create(); }},
              {"cuda",
               [] {
                    return gko::CudaExecutor::create(0,
                                                           gko::OmpExecutor::create());
              }},
{"hip",
```

```
return gko::HipExecutor::create(0, gko::OmpExecutor::create());
           }},
          {"dpcpp",
           [] {
                return gko::DpcppExecutor::create(0,
                                                           gko::OmpExecutor::create());
          {"reference", [] { return gko::ReferenceExecutor::create(); }}};
const auto exec = exec_map.at(executor_string)(); // throws if not valid
auto A = share(gko::read<mtx>(std::ifstream("data/A.mtx"), exec));
auto b = gko::read<vec>(std::ifstream("data/b.mtx"), exec);
auto x = gko::read<vec>(std::ifstream("data/x0.mtx"), exec);
const RealValueType reduction_factor{1e-7};
auto solver_gen =
     cg::build()
          .with_criteria(gko::stop::Iteration::build().with_max_iters(20u),
                             gko::stop::ResidualNorm<ValueType>::build()
                                 .with_reduction_factor(reduction_factor))
          .on(exec);
auto solver = solver_gen->generate(A);
int eventset =
     \verb|init_papi_counters(to_string(solver.get()), to_string(A.get()));\\
auto logger = gko::log::Papi<ValueType>::create(
    gko::log::Logger::linop_apply_completed_mask |
     gko::log::Logger::linop_advanced_apply_completed_mask);
solver->add_logger(logger);
A->add_logger(logger);
solver->apply(b, x);
print_papi_counters(eventset);
std::cout « "Solution (x): \n";
write(std::cout, x);
auto one = gko::initialize<vec>({1.0}, exec);
auto neg_one = gko::initialize<vec>({-1.0}, exec);
auto res = gko::initialize<real_vec>({0.0}, exec);
A->apply(one, x, neg_one, b);
b->compute_norm2(res);
std::cout « "Residual norm sqrt(r^T r): \n";
write(std::cout, res);
```

# The par-ilu-convergence program

The ParILU convergence example..

This example depends on simple-solver.

#### Introduction

#### About the example

This example can be used to inspect the convergence behavior of parallel incomplete factorizations. \*

```
auto try_generate(Function fun) -> decltype(fun())
      decltype(fun()) result;
     try {
    result = fun();
      } catch (const gko::Error& err) {
   std::cerr « "Error: " « err.what() « '\n';
            std::exit(-1);
      return result;
template <typename ValueType, typename IndexType>
double compute_ilu_residual_norm(
     const gko::matrix::Csr<ValueType, IndexType>* residual,
const gko::matrix::Csr<ValueType, IndexType>* mtx)
     gko::matrix_data<ValueType, IndexType> residual_data;
gko::matrix_data<ValueType, IndexType> mtx_data;
      residual->write(residual_data);
      mtx->write(mtx_data);
     residual_data.sort_row_major();
mtx_data.sort_row_major();
      auto it = mtx_data.nonzeros.begin();
      double residual_norm{};
      for (auto entry : residual_data.nonzeros) {
   auto ref_row = it->row;
   auto ref_col = it->column;
   if (entry.row == ref_row && entry.column == ref_col) {
      residual_norm += gko::squared_norm(entry.value);
   }
}
      return std::sqrt(residual_norm);
int main(int argc, char* argv[])
```

```
using ValueType = double;
    using IndexType = int;
print usage message
   (argc < 2 || executors.find(argv[1]) == executors.end()) {
  std::cerr « "Usage: executable"</pre>
                « " <reference|omp|cuda|hip|dpcpp> [<matrix-file>] '
                    "[<pariu|pariu|pariut|paric|parict] [<martin-11167]
"[<pariu|pariut|paric|parict] [<mar-iterations>] "
"[<num-repetitions>] [<fill-in-limit>]\n";
    return -1;
}
generate executor based on first argument
auto exec = try_generate([&] { return executors.at(argv[1])(); });
set matrix and preconditioner name with default values
std::string matrix = argc < 3 ? "data/A.mtx" : argv[2];
std::string precond = argc < 4 ? "parilu" : argv[3];</pre>
int max_iterations = argc < 5 ? 10 : std::stoi(argv[4]);
int num_repetitions = argc < 6 ? 10 : std::stoi(argv[5]);
double limit = argc < 7 ? 2 : std::stod(argv[6]);</pre>
load matrix file into Csr format
    auto mtx = gko::share(try_generate([&] {
         std::ifstream mtx_stream{matrix};
         if (!mtx_stream) {
              throw GKO_STREAM_ERROR("Unable to open matrix file");
         std::cerr « "Reading " « matrix « std::endl;
         return gko::read<gko::matrix::Csr<ValueType, IndexType»(mtx_stream,</pre>
    }));
    auto factory_generator =
         [&](gko::size_type iteration) -> std::shared_ptr<gko::LinOpFactory> {
   if (precond == "parilu") {
      return gko::factorization::ParIlu<ValueType, IndexType>::build()
                  .with iterations(iteration)
                   .on(exec);
         } else if (precond == "paric") {
              return gko::factorization::ParIc<ValueType, IndexType>::build()
                  .with_iterations(iteration)
                   .on(exec);
         } else if (precond == "parilut") {
              return gko::factorization::ParIlut<ValueType, IndexType>::build()
                   .with_fill_in_limit(limit)
                   .with_iterations(iteration)
                   .on(exec);
         } else if (precond == "parict") {
              return gko::factorization::ParIct<ValueType, IndexType>::build()
                  .with_fill_in_limit(limit)
                   .with_iterations(iteration)
                   .on(exec);
         } else {
              GKO_NOT_IMPLEMENTED;
    auto one = gko::initialize<gko::matrix::Dense<ValueType»({1.0}, exec);</pre>
    auto minus one =
         gko::initialize<gko::matrix::Dense<ValueType»({-1.0}, exec);</pre>
     for (int it = 1; it <= max_iterations; ++it) {</pre>
         auto factory = factory_generator(it);
         std::cout « it « ';';
         std::vector<long> times;
         std::vector<double> residuals;
         for (int rep = 0; rep < num_repetitions; ++rep) {</pre>
              auto tic = std::chrono::high_resolution_clock::now();
              auto result =
                  gko::as<gko::Composition<ValueType»(factory->generate(mtx));
              exec->synchronize();
              auto toc = std::chrono::high_resolution_clock::now();
              auto residual = gko::clone(exec, mtx);
              result->get_operators()[0]->apply(one, result->get_operators()[1],
                                                       minus_one, residual);
              times.push back(
                   std::chrono::duration_cast<std::chrono::nanoseconds>(toc - tic)
                        .count());
              residuals.push_back(
                   compute_ilu_residual_norm(residual.get(), mtx.get()));
         for (auto el : times)
              std::cout « el « ';';
         for (auto el : residuals) {
```

```
std::cout « el « ';';
}
std::cout « '\n';
}
```

#### Results

#### This is the expected output:

```
Usage: executable <reference|omp|cuda|hip|dpcpp> [<matrix-file>] [<parilu|parilut|paric|parict] [<max-iterations>] [<num-repetitions>] [fill-in-limit]
```

#### When specifying an executor:

```
Reading data/A.mtx
1;71800;10300;8800;8200;8000;7700;7500;7500;7500;7500;7400;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0331e-14;1.0312e-16;4.15407e-16;4.15407e-16;4.15407e-16;4.15407e-16;4.1540
```

#### Comments about programming and debugging

```
#include <functional>
#include <iostream>
#include <map>
#include <memorv>
#include <string>
#include <ginkgo/ginkgo.hpp>
const std::map<std::string, std::function<std::shared_ptr<gko::Executor>()>
    executors {
        {"reference", [] { return gko::ReferenceExecutor::create(); }},
        {"omp", [] { return gko::OmpExecutor::create(); }},
{"cuda",
         [] {
             return gko::CudaExecutor::create(0, gko::OmpExecutor::create());
        {"hip",
         [] {
              return gko::HipExecutor::create(0, gko::OmpExecutor::create());
        {"dpcpp", [] {
              return gko::DpcppExecutor::create(0, gko::OmpExecutor::create());
         }}};
template <typename Function>
auto try_generate(Function fun) -> decltype(fun())
    decltype(fun()) result;
    try {
        result = fun();
    } catch (const gko::Error& err) {
   std::cerr « "Error: " « err.what() « '\n';
        std::exit(-1);
template <typename ValueType, typename IndexType>
double compute_ilu_residual_norm(
    const gko::matrix::Csr<ValueType, IndexType>* residual,
    const gko::matrix::Csr<ValueType, IndexType>* mtx)
    gko::matrix_data<ValueType, IndexType> residual_data;
    gko::matrix_data<ValueType, IndexType> mtx_data;
    residual->write(residual data);
    mtx->write(mtx data);
    residual_data.sort_row_major();
    mtx_data.sort_row_major();
```

```
auto it = mtx_data.nonzeros.begin();
    double residual_norm{};
    for (auto entry : residual_data.nonzeros) {
  auto ref_row = it->row;
         auto ref_col = it->column;
          if (entry.row == ref_row && entry.column == ref_col) {
              residual_norm += gko::squared_norm(entry.value);
         }
    return std::sqrt(residual_norm);
int main(int argc, char* argv[])
    using ValueType = double;
    using IndexType = int;
    if (argc < 2 || executors.find(argv[1]) == executors.end()) {</pre>
         std::cerr « "Usage: executable"

« " <reference|omp|cuda|hip|dpcpp> [<matrix-file>] "
                          "[<parilu|parilut|paric|parict] [<max-iterations>] "
                          "[<num-repetitions>] [<fill-in-limit>]\n";
         return -1;
    auto exec = try_generate([&] { return executors.at(argv[1])(); });
std::string matrix = argc < 3 ? "data/A.mtx" : argv[2];
std::string precond = argc < 4 ? "parilu" : argv[3];
int max_iterations = argc < 5 ? 10 : std::stoi(argv[4]);
int num_repetitions = argc < 6 ? 10 : std::stoi(argv[5]);
double limit = argc < 7 ? 2 : std::stod(argv[6]);
auto mtx = drevishere(try_generate([c]));</pre>
    auto mtx = gko::share(try_generate([&] {
         std::ifstream mtx_stream{matrix};
          if (!mtx_stream) {
              throw GKO_STREAM_ERROR("Unable to open matrix file");
          std::cerr « "Reading " « matrix « std::endl;
         return gko::read<gko::matrix::Csr<ValueType, IndexType»(mtx_stream,</pre>
                                                                                 exec);
    auto factory_generator =
         [&] (gko::size_type iteration) -> std::shared_ptr<gko::LinOpFactory> {
   if (precond == "parilu") {
      return gko::factorization::ParIlu<ValueType, IndexType>::build()
                   .with_iterations(iteration)
                    .on(exec);
          } else if (precond == "paric") {
               return gko::factorization::ParIc<ValueType, IndexType>::build()
                   .with_iterations(iteration)
                    .on(exec);
          } else if (precond == "parilut") {
               return gko::factorization::ParIlut<ValueType, IndexType>::build()
                   .with_fill_in_limit(limit)
                    .with_iterations(iteration)
                    .on(exec);
          } else if (precond == "parict") {
               return gko::factorization::ParIct<ValueType, IndexType>::build()
                   .with_fill_in_limit(limit)
                   .with_iterations(iteration)
                   .on(exec);
          } else {
              GKO_NOT_IMPLEMENTED;
    };
    auto one = gko::initialize<gko::matrix::Dense<ValueType»({1.0}, exec);</pre>
    auto minus_one =
         gko::initialize<gko::matrix::Dense<ValueType»({-1.0}, exec);</pre>
     for (int it = 1; it <= max_iterations; ++it) {</pre>
         auto factory = factory_generator(it);
         std::cout « it « ';';
         std::vector<long> times;
          std::vector<double> residuals;
          for (int rep = 0; rep < num_repetitions; ++rep) {
  auto tic = std::chrono::high_resolution_clock::now();</pre>
               auto result =
                   gko::as<gko::Composition<ValueType»(factory->generate(mtx));
               exec->synchronize();
               auto toc = std::chrono::high_resolution_clock::now();
               auto residual = gko::clone(exec, mtx);
               result->get_operators()[0]->apply(one, result->get_operators()[1],
                                                         minus_one, residual);
               times.push back(
                   std::chrono::duration cast<std::chrono::nanoseconds>(toc - tic)
                         .count());
               residuals.push_back(
                   compute_ilu_residual_norm(residual.get(), mtx.get()));
          for (auto el : times) {
   std::cout « el « ';';
```

```
for (auto el : residuals) {
    std::cout « el « ';';
}
std::cout « '\n';
}
```

# The performance-debugging program

The simple solver with performance debugging example..

This example depends on simple-solver-logging, minimal-cuda-solver.

#### Introduction

#### About the example

This example runs a solver on a test problem and shows how to use loggers to debug performance and convergence rate.

```
creates a zero vector
template <typename ValueType>
std::unique_ptr<vec<ValueType» create_vector(</pre>
    std::shared_ptr<const gko::Executor> exec, gko::size_type size,
    ValueType value)
    auto res = vec<ValueType>::create(exec);
    res->read(gko::matrix_data<ValueType>(gko::dim<2>{size, 1}, value));
    return res;
utilities for computing norms and residuals
template <typename ValueType>
ValueType get_first_element(const vec<ValueType>* norm)
    return norm->get_executor()->copy_val_to_host(norm->get_const_values());
template <typename ValueType>
gko::remove_complex<ValueType> compute_norm(const vec<ValueType>* b)
    auto exec = b->get_executor();
    auto b_norm = gko::initialize<real_vec<ValueType»({0.0}, exec);</pre>
    b->compute_norm2(b_norm);
    return get_first_element(b_norm.get());
template <typename ValueType>
gko::remove_complex<ValueType> compute_residual_norm(
    const gko::LinOp* system_matrix, const vec<ValueType>* b,
    const vec<ValueType>* x)
    auto exec = system_matrix->get_executor();
    auto one = gko::initialize<vec<ValueType»({1.0}, exec);</pre>
```

```
auto neg_one = gko::initialize<vec<ValueType»({-1.0}, exec);
auto res = gko::clone(b);
system_matrix->apply(one, x, neg_one, res);
return compute_norm(res.get());
}
// namespace utils
namespace loggers {
```

A logger that accumulates the time of all operations. For each operation type (allocations, free, copy, internal operations i.e. kernels), the timing is taken before and after. This can create significant overhead since to ensure proper timings, calls to synchronize are required.

```
{
        this->start_operation(exec, "allocate");
    void on_allocation_completed(const gko::Executor* exec,
                                 const gko::size type&,
                                 const gko::uintptr&)const override
{
        this->end_operation(exec, "allocate");
    void on_free_started(const gko::Executor* exec,
                         const gko::uintptr&)const override
        this->start_operation(exec, "free");
    void on_free_completed(const gko::Executor* exec,
                           const gko::uintptr&)const override
        this->end_operation(exec, "free");
    void on_copy_started(const gko::Executor* from, const gko::Executor* to,
                         const gko::uintptr&, const gko::uintptr&,
                         const gko::size_type&)const override
{
        from->synchronize();
        this->start_operation(to, "copy");
    void on_copy_completed(const gko::Executor* from, const gko::Executor* to,
                           const gko::uintptr&, const gko::uintptr&,
                           const gko::size_type&)const override
{
        from->synchronize():
        this->end_operation(to, "copy");
    void on_operation_launched(const gko::Executor* exec,
                               const gko::Operation* op)const override
        this->start_operation(exec, op->get name());
    void on_operation_completed(const gko::Executor* exec,
                                const gko::Operation* op)const override
        this->end_operation(exec, op->get_name());
    void write_data(std::ostream& ostream)
        for (const auto& entry : total) {
            ostream « "\t" « entry.first.c_str() « ": "
                    \begin{tabular}{ll} \textbf{$w$} & \textbf{std::chrono::nanoseconds} \\ \end{tabular} \label{table:chrono::nanoseconds} \end{tabular}
                           entry.second)
                           .count()
                    « std::endl;
private:
```

Helper which synchronizes and starts the time before every operation.

Helper to compute the end time and store the operation's time at its end. Also time nested operations.

```
void end_operation(const gko::Executor* exec, const std::string& name)const
{
    exec->synchronize();
    const auto end = std::chrono::steady_clock::now();
```

```
const auto diff = end - start[name];
```

#### make sure timings for nested operations are not counted twice

```
total[name] += diff - nested.back();
  nested.pop_back();
  if (nested.size() > 0) {
      nested.back() += diff;
  }
}
mutable std::map<std::string, std::chrono::steady_clock::time_point> start;
mutable std::map<std::string, std::chrono::steady_clock::duration> total;
```

#### the position i of this vector holds the total time spend on child operations on nesting level i

```
mutable std::vector<std::chrono::steady_clock::duration> nested;
```

#### This logger tracks the persistently allocated data

struct StorageLogger : gko::log::Logger {

#### Store amount of bytes allocated on every allocation

#### Reset the amount of bytes on every free

#### Write the data after summing the total from all allocations

```
void write_data(std::ostream& ostream)
{
      gko::size_type total{};
      for (const auto& e : storage) {
            total += e.second;
      }
        ostream « "Storage: " « total « std::endl;
}
private:
      mutable std::unordered_map<gko::uintptr, gko::size_type> storage;
};
```

#### Logs true and recurrent residuals of the solver

```
template <typename ValueType>
struct ResidualLogger : gko::log::Logger {
```

Depending on the available information, store the norm or compute it from the residual. If the true residual norm could not be computed, store the value -1.0.

```
void on_iteration_complete(const gko::LinOp*, const gko::size_type&,
                                const gko::LinOp* residual,
                                const gko::LinOp* solution,
                                \verb|const| gko:: LinOp*| residual_norm|) const| override|
{
        if (residual norm) {
            rec_res_norms.push_back(utils::get_first_element(
                gko::as<real_vec<ValueType»(residual_norm)));</pre>
        } else {
            rec_res_norms.push_back(
                utils::compute_norm(gko::as<vec<ValueType»(residual)));
        if (solution) {
            true_res_norms.push_back(utils::compute_residual_norm(
                matrix, b, gko::as<vec<ValueType»(solution)));</pre>
        } else {
            true_res_norms.push_back(-1.0);
    ResidualLogger(const gko::LinOp* matrix, const vec<ValueType>* b)
        : gko::log::Logger(gko::log::Logger::iteration_complete_mask),
          matrix{matrix},
          b{b}
    {}
    void write_data(std::ostream& ostream)
```

```
ostream « "Recurrent Residual Norms: " « std::endl;
         ostream « "[" « std::endl;
         for (const auto& entry : rec_res_norms) {
   ostream « "\t" « entry « std::endl;
         ostream « "]; " « std::endl;
         ostream « "True Residual Norms: " « std::endl;
         ostream « "[" « std::endl;
         for (const auto& entry : true_res_norms) {
    ostream « "\t" « entry « std::endl;
        ostream « "]; " « std::endl;
    }
private:
    const gko::LinOp* matrix;
    const vec<ValueType>* b;
    mutable std::vector<gko::remove_complex<ValueType> rec_res_norms;
    mutable std::vector<gko::remove_complex<ValueType> true_res_norms;
   // namespace loggers
namespace {
Print usage help
void print_usage(const char* filename)
    std::cerr « "Usage: " « filename « " [executor] [matrix file]"
               « std::endl;
    std::cerr « "matrix file should be a file in matrix market format. "
                  "The file data/A.mtx is provided as an example."
               « std::endl;
    std::exit(-1);
template <typename ValueType>
void print_vector(const gko::matrix::Dense<ValueType>* vec)
    auto elements_to_print = std::min(gko::size_type(10), vec->get_size()[0]);
    std::cout « "[" « std::endl;
for (int i = 0; i < elements_to_print; ++i) {
    std::cout « "\t" « vec->at(i) « std::endl;
    std::cout « "];" « std::endl;
} // namespace
int main(int argc, char* argv[])
Parametrize the benchmark here Pick a value type
using ValueType = double;
using IndexType = int;
Pick a matrix format
using mtx = gko::matrix::Csr<ValueType, IndexType>;
Pick a solver
using solver = gko::solver::Cg<ValueType>;
Pick a preconditioner type
using preconditioner = gko::matrix::IdentityFactory<ValueType>;
Pick a residual norm reduction value
const gko::remove_complex<ValueType> reduction_factor = 1e-12;
Pick an output file name
const auto of_name = "log.txt";
Simple shortcut
using vec = gko::matrix::Dense<ValueType>;
Print version information
std::cout « gko::version_info::get() « std::endl;
Figure out where to run the code
   (argc = 2 && (std::string(argv[1]) == "--help")) {
   std::cerr « "Usage: " « argv[0] « " [executor]" « std::endl;
    std::exit(-1);
```

```
Figure out where to run the code
const auto executor_string = argc >= 2 ? argv[1] : "reference";
std::map<std::string, std::function<std::shared_ptr<gko::Executor>()»
        {"omp", [] { return gko::OmpExecutor::create(); }},
{"cuda",
    exec_map{
         [] {
             return gko::CudaExecutor::create(0,
                                                gko::OmpExecutor::create());
        {"hip",
         [] {
             return gko::HipExecutor::create(0, gko::OmpExecutor::create());
        {"dpcpp",
             return gko::DpcppExecutor::create(0,
                                                 gko::OmpExecutor::create());
         }},
        {"reference", [] { return gko::ReferenceExecutor::create(); }}};
executor where Ginkgo will perform the computation
const auto exec = exec_map.at(executor_string)(); // throws if not valid
Read the input matrix file directory
std::string input_mtx = "data/A.mtx";
if (argc == 3) {
    input_mtx = std::string(argv[2]);
Read data: A is read from disk Create a StorageLogger to track the size of A
auto storage_logger = std::make_shared<loggers::StorageLogger>();
Add the logger to the executor
exec->add_logger(storage_logger);
Read the matrix A from file
auto A = gko::share(gko::read<mtx>(std::ifstream(input_mtx), exec));
Remove the storage logger
exec->remove_logger(storage_logger);
Pick a maximum iteration count
const auto max_iters = A->get_size()[0];
Generate b and x vectors
auto b = utils::create_vector<ValueType>(exec, A->get_size()[0], 1.0);
auto x = utils::create_vector<ValueType>(exec, A->get_size()[0], 0.0);
Declare the solver factory. The preconditioner's arguments should be adapted if needed.
auto solver_factory
    solver::build()
        .with_criteria(
            gko::stop::ResidualNorm<ValueType>::build()
                .with_reduction_factor(reduction_factor),
            gko::stop::Iteration::build().with_max_iters(max_iters))
        .with_preconditioner(preconditioner::create(exec))
        .on(exec);
Declare the output file for all our loggers
std::ofstream output_file(of_name);
Do a warmup run
Clone x to not overwrite the original one
auto x_clone = gko::clone(x);
Generate and call apply on a solver
    solver_factory->generate(A)->apply(b, x_clone);
exec->synchronize();
```

Do a timed run

{

```
Clone x to not overwrite the original one
```

```
auto x_clone = gko::clone(x);
```

#### Synchronize ensures no operation are ongoing

```
exec->synchronize();
```

#### Time before generate

```
auto g_tic = std::chrono::steady_clock::now();
```

#### Generate a solver

```
auto generated_solver = solver_factory->generate(A);
exec->synchronize();
```

#### Time after generate

```
auto g_tac = std::chrono::steady_clock::now();
```

#### Compute the generation time

```
auto generate_time =
    std::chrono::duration_cast<std::chrono::nanoseconds>(g_tac - g_tic);
```

#### Write the generate time to the output file

#### Similarly time the apply

```
exec->synchronize();
auto a_tic = std::chrono::steady_clock::now();
generated_solver->apply(b, x_clone);
exec->synchronize();
auto a_tac = std::chrono::steady_clock::now();
auto apply_time =
    std::chrono::duration_cast<std::chrono::nanoseconds>(a_tac - a_tic);
output_file « "Apply time (ns): " « apply_time.count() « std::endl;
```

#### Compute the residual norm

```
auto residual =
    utils::compute_residual_norm(A.get(), b.get(), x_clone.get());
    output_file « "Residual_norm: " « residual « std::endl;
}
```

#### Log the internal operations using the OperationLogger without timing

#### Create an OperationLogger to analyze the generate step

```
auto gen_logger = std::make_shared<loggers::OperationLogger>();
```

#### Add the generate logger to the executor

```
exec->add_logger(gen_logger);
```

#### Generate a solver

```
auto generated_solver = solver_factory->generate(A);
```

#### Remove the generate logger from the executor

```
exec->remove_logger(gen_logger);
```

#### Write the data to the output file

```
output_file « "Generate operations times (ns):" « std::endl;
gen_logger->write_data(output_file);
```

#### Create an OperationLogger to analyze the apply step

```
auto apply_logger = std::make_shared<loggers::OperationLogger>();
exec->add_logger(apply_logger);
```

#### Create a ResidualLogger to log the recurent residual

```
auto res_logger = std::make_shared<loggers::ResidualLogger<ValueType»(
    A.get(), b.get());
generated_solver->add_logger(res_logger);
```

```
Solve the system
```

#### Results

```
This is the expected standard output:
```

#### Here is a sample output in the file log.txt:

```
Generate time (ns): 861
Apply time (ns): 108144
Residual_norm: 2.10788e-15
Generate operations times (ns):
Apply operations times (ns):
    allocate: 14991 cg::initialize#8:
    cg::step_1#5: 7683
cg::step_2#7: 7756
copy: 7751
    csr::advanced_spmv#5: 21819
csr::spmv#3: 20429
     dense::compute_dot#3: 18043
     dense::compute_norm2#2: 16726
     free: 8857
     residual_norm::residual_norm#9: 3614
Recurrent Residual Norms:
     4.3589
     2.30455
     1.46771
     0.984875
     0.741833
     0.513623
     0.384165
     0.316439
     0.227709
     0.170312
     0.0973722
     0.0616831
     0.0454123
     0.031953
     0.0161606
     0.00657015
     0.00264367
     0.000858809
     0.000286461
     1.64195e-15
];
```

```
True Residual Norms:
    4.3589
    2.30455
    1.46771
    0.984875
    0.741833
    0.513623
    0.384165
    0.316439
    0.227709
    0.170312
    0.0973722
    0.0616831
    0.0454123
    0.031953
    0.0161606
    0.00657015
    0.00264367
    0.000286461
    2.10788e-15
1;
```

#### Comments about programming and debugging

```
#include <algorithm>
#include <array>
#include <chrono>
#include <cstdlib>
#include <fstream>
#include <iomanip>
#include <iostream>
#include <map>
#include <ostream>
#include <sstream>
#include <string>
#include <unordered_map>
#include <utility>
#include <vector>
#include <ginkgo/ginkgo.hpp>
template <typename ValueType>
using vec = gko::matrix::Dense<ValueType>;
template <typename ValueType>
using real_vec = gko::matrix::Dense<gko::remove_complex<ValueType>>;
namespace utils {
template <typename ValueType>
std::unique_ptr<vec<ValueType» create_vector(
    std::shared_ptr<const gko::Executor> exec, gko::size_type size,
    ValueType value)
{
    auto res = vec<ValueType>::create(exec);
    res->read(gko::matrix_data<ValueType>(gko::dim<2>{size, 1}, value));
template <typename ValueType>
ValueType get_first_element(const vec<ValueType>* norm)
    return norm->get_executor()->copy_val_to_host(norm->get_const_values());
template <typename ValueType>
gko::remove_complex<ValueType> compute_norm(const vec<ValueType>* b)
    auto exec = b->get_executor();
    auto b_norm = gko::initialize<real_vec<ValueType»({0.0}, exec);</pre>
    b->compute_norm2(b_norm);
    return get_first_element(b_norm.get());
template <typename ValueType>
gko::remove_complex<ValueType> compute_residual_norm(
    const gko::LinOp* system_matrix, const vec<ValueType>* b,
    const vec<ValueType>* x)
    auto exec = system_matrix->get_executor();
    auto one = gko::initialize<vec<ValueType»({1.0}, exec);</pre>
    auto neg_one = gko::initialize<vec<ValueType»({-1.0}, exec);</pre>
    auto res = gko::clone(b);
    system_matrix->apply(one, x, neg_one, res);
    return compute_norm(res.get());
```

```
// namespace utils
namespace loggers {
struct OperationLogger : gko::log::Logger {
    void on_allocation_started(const gko::Executor* exec,
                               const gko::size_type&)const override
        this->start_operation(exec, "allocate");
    void on_allocation_completed(const gko::Executor* exec,
                                  const gko::size_type&,
                                  \verb"const gko:: uintptr\&) const override"
{
        this->end_operation(exec, "allocate");
    void on_free_started(const gko::Executor* exec,
                         const gko::uintptr&)const override
{
        this->start_operation(exec, "free");
    void on_free_completed(const gko::Executor* exec,
                           const gko::uintptr&)const override
{
        this->end_operation(exec, "free");
    void on_copy_started(const gko::Executor* from, const gko::Executor* to,
                         const gko::uintptr&, const gko::uintptr&,
                          const gko::size_type&)const override
{
        from->synchronize();
        this->start_operation(to, "copy");
    void on_copy_completed(const gko::Executor* from, const gko::Executor* to,
                           const gko::uintptr&, const gko::uintptr&,
                            const gko::size_type&)const override
{
        from->synchronize();
        this->end_operation(to, "copy");
    void on_operation_launched(const gko::Executor* exec,
                                const gko::Operation* op)const override
{
        this->start_operation(exec, op->get_name());
    void on_operation_completed(const gko::Executor* exec,
                                 const gko::Operation* op)const override
        this->end_operation(exec, op->get_name());
    void write data(std::ostream& ostream)
        for (const auto& entry : total) {
            ostream « "\t" « entry.first.c_str() « ": "
                    « std::chrono::duration_cast<std::chrono::nanoseconds>(
                           entry.second)
                            .count()
                    « std::endl;
    }
private:
    void start_operation(const gko::Executor* exec,
                         const std::string& name)const
{
        nested.emplace_back(0);
        exec->synchronize();
        start[name] = std::chrono::steady_clock::now();
    void end_operation(const gko::Executor* exec, const std::string& name)const
{
        exec->synchronize();
        const auto end = std::chrono::steady_clock::now();
const auto diff = end - start[name];
        total[name] += diff - nested.back();
        nested.pop_back();
if (nested.size() > 0) {
            nested.back() += diff;
    mutable std::map<std::string, std::chrono::steady_clock::time_point> start;
    mutable std::map<std::string, std::chrono::steady_clock::duration> total;
   mutable std::vector<std::chrono::steady_clock::duration> nested;
struct StorageLogger : gko::log::Logger {
    void on_allocation_completed(const gko::Executor*,
                                  const gko::size_type& num_bytes,
                                  const gko::uintptr& location)const override
{
```

```
storage[location] = num_bytes;
    void on_free_completed(const gko::Executor*,
                              const gko::uintptr& location)const override
        storage[location] = 0;
    void write_data(std::ostream& ostream)
         gko::size_type total{};
         for (const auto& e : storage) {
   total += e.second;
        ostream « "Storage: " « total « std::endl;
    }
private:
    mutable std::unordered_map<gko::uintptr, gko::size_type> storage;
};
template <typename ValueType>
struct ResidualLogger : gko::log::Logger {
    void on_iteration_complete(const gko::LinOp*, const gko::size_type&,
                                  const gko::LinOp* residual,
                                  const gko::LinOp* solution,
                                  const gko::LinOp* residual_norm)const override
{
         if (residual_norm) {
             rec_res_norms.push_back(utils::get_first_element()
                 gko::as<real_vec<ValueType»(residual_norm)));</pre>
         } else {
             rec_res_norms.push_back(
                 utils::compute_norm(gko::as<vec<ValueType»(residual)));
             true_res_norms.push_back(utils::compute_residual_norm(
                 matrix, b, gko::as<vec<ValueType»(solution)));</pre>
         } else {
            true_res_norms.push_back(-1.0);
    ResidualLogger(const gko::LinOp* matrix, const vec<ValueType>* b)
         : gko::log::Logger(gko::log::Logger::iteration_complete_mask),
           matrix{matrix},
           b{b}
    {}
    void write_data(std::ostream& ostream)
        ostream \ll "Recurrent Residual Norms: " \ll std::endl; ostream \ll "[" \ll std::endl;
         for (const auto& entry : rec_res_norms) {
    ostream « "\t" « entry « std::endl;
         ostream « "];" « std::endl;
         ostream « "True Residual Norms: " « std::endl;
        for (const auto& entry : true_res_norms) {
    ostream « "\t" « entry « std::endl;
        ostream « "]; " « std::endl;
    }
private:
    const gko::LinOp* matrix;
    const vec<ValueType>* b;
    mutable std::vector<gko::remove_complex<ValueType> rec_res_norms;
    mutable std::vector<gko::remove_complex<ValueType> true_res_norms;
  // namespace loggers
namespace {
void print_usage(const char* filename)
    std::cerr « "Usage: " « filename « " [executor] [matrix file]"
               « std::endl;
    std::cerr « "matrix file should be a file in matrix market format. "
                  "The file data/A.mtx is provided as an example."
               « std::endl;
    std::exit(-1);
template <typename ValueType>
void print_vector(const gko::matrix::Dense<ValueType>* vec)
    auto elements_to_print = std::min(gko::size_type(10), vec->get_size()[0]);
    std::cout « "[" « std::endl;
for (int i = 0; i < elements_to_print; ++i) {
    std::cout « "\t" « vec->at(i) « std::endl;
    std::cout « "];" « std::endl;
  // namespace
```

```
int main(int argc, char* argv[])
    using ValueType = double;
    using IndexType = int;
    using mtx = gko::matrix::Csr<ValueType, IndexType>;
using solver = gko::solver::Cg<ValueType>;
using preconditioner = gko::matrix::IdentityFactory<ValueType>;
    const gko::remove_complex<ValueType> reduction_factor = 1e-12;
    const auto of_name = "log.txt";
    using vec = gko::matrix::Dense<ValueType>;
    if (argc == 2 && (std::string(argv[1]) == "--help")) {
   std::cerr « "Usage: " « argv[0] « " [executor]" « std::endl;
        std::exit(-1);
    const auto executor_string = argc >= 2 ? argv[1] : "reference";
    exec map{
            {"omp", [] { return gko::OmpExecutor::create(); }},
            {"cuda",
             [] {
                  return gko::CudaExecutor::create(0,
                                                     gko::OmpExecutor::create());
            {"hip",
             [] {
                 return gko::HipExecutor::create(0, gko::OmpExecutor::create());
            { "dpcpp",
             [] {
                 return gko::DpcppExecutor::create(0,
                                                      gko::OmpExecutor::create());
             {"reference", [] { return gko::ReferenceExecutor::create(); }}};
    const auto exec = exec_map.at(executor_string)(); // throws if not valid
std::string input_mtx = "data/A.mtx";
if (argc == 3) {
        input_mtx = std::string(argv[2]);
    auto storage_logger = std::make_shared<loggers::StorageLogger>();
    exec->add_logger(storage_logger);
    auto A = gko::share(gko::read<mtx>(std::ifstream(input_mtx), exec));
    exec->remove_logger(storage_logger);
    const auto max_iters = A->get_size()[0];
    auto b = utils::create_vector<ValueType>(exec, A->get_size()[0], 1.0);
    auto x = utils::create_vector<ValueType>(exec, A->get_size()[0], 0.0);
    auto solver_factory =
        solver::build()
            .with_criteria(
                gko::stop::ResidualNorm<ValueType>::build()
                     .with_reduction_factor(reduction_factor),
                gko::stop::Iteration::build().with_max_iters(max_iters))
            .with_preconditioner(preconditioner::create(exec))
             .on(exec);
    std::ofstream output_file(of_name);
        auto x_clone = gko::clone(x);
        solver_factory->generate(A)->apply(b, x_clone);
        exec->synchronize();
        auto x_clone = gko::clone(x);
        exec->synchronize();
        auto g_tic = std::chrono::steady_clock::now();
        auto generated_solver = solver_factory->generate(A);
        exec->synchronize();
        auto g_tac = std::chrono::steady_clock::now();
        auto generate time =
           std::chrono::duration_cast<std::chrono::nanoseconds>(g_tac - g_tic);
        output_file « "Generate time (ns): " « generate_time.count()
                    « std::endl;
        exec->synchronize();
        auto a_tic = std::chrono::steady_clock::now();
        {\tt generated\_solver->apply(b, x\_clone);}
        exec->synchronize();
        auto a_tac = std::chrono::steady_clock::now();
        auto apply_time =
            std::chrono::duration_cast<std::chrono::nanoseconds>(a_tac - a_tic);
        output_file « "Apply time (ns): " « apply_time.count() « std::endl;
auto residual =
           utils::compute_residual_norm(A.get(), b.get(), x_clone.get());
        output_file « "Residual_norm:
                                         " « residual « std::endl;
        auto gen_logger = std::make_shared<loggers::OperationLogger>();
        exec->add_logger(gen_logger);
        auto generated_solver = solver_factory->generate(A);
```

# The poisson-solver program

The poisson solver example..

This example depends on simple-solver.

#### Introduction

This example solves a 1D Poisson equation:

$$u:[0,1]\rightarrow R$$

$$u"=f$$

$$u(0)=u0$$

$$u(1)=u1$$

using a finite difference method on an equidistant grid with  $\mathbb K$  discretization points ( $\mathbb K$  can be controlled with a command line parameter). The discretization is done via the second order Taylor polynomial:

For an equidistant grid with K "inner" discretization points x1,...,xk,and step size h=1/(K+1), the formula produces a system of linear equations

$$2u_1 - u_2 = -f_1h^2 + u0$$
  
-  $u(k-1) + 2u_k - u(k+1) = -f_kh^2, k = 2, ..., K-1$   
-  $u(K-1) + 2u_K = -f_Kh^2 + u1$ 

which is then solved using Ginkgo's implementation of the CG method preconditioned with block-Jacobi. It is also possible to specify on which executor Ginkgo will solve the system via the command line. The function 'f'is set to 'f(x) = 6x' (making the solution ' $u(x) = x^3$ '), but that can be changed in the main function.

The intention of the example is to show how Ginkgo can be used to build an application solving a real-world problem, which includes a solution of a large, sparse linear system as a component.

#### About the example

#### The commented program

```
row_ptrs[i + 1] = pos;
}
Generates the RHS vector given f and the boundary conditions.
template <typename Closure, typename ValueType>
void generate_rhs(Closure f, ValueType u0, ValueType u1,
                      gko::matrix::Dense<ValueType>* rhs)
     const auto discretization_points = rhs->get_size()[0];
     auto values = rhs->get_values();
     const ValueType h = 1.0 / static_cast<ValueType>(discretization_points + 1);
for (gko::size_type i = 0; i < discretization_points; ++i) {
    const auto xi = static_cast<ValueType>(i + 1) * h;
          values[i] = -f(xi) * h * h;
     values[0] += u0;
     values[discretization_points - 1] += u1;
Prints the solution \boldsymbol{u}.
template <typename Closure, typename ValueType>
void print_solution(ValueType u0, ValueType u1,
                         const gko::matrix::Dense<ValueType>* u)
     std::cout « u0 « '\n'; for (int i = 0; i < u->get_size()[0]; ++i) {
         std::cout « u->get_const_values()[i] « '\n';
     std::cout « u1 « std::endl;
Computes the 1-norm of the error given the computed u and the correct solution function correct_u.
template <typename Closure, typename ValueType>
gko::remove_complex<ValueType> calculate_error(
     int discretization_points, const gko::matrix::Dense<ValueType>* u,
     Closure correct_u)
     const ValueType h = 1.0 / static_cast<ValueType>(discretization_points + 1);
     gko::remove_complex<ValueType> error = 0.0;
     for (int i = 0; i < discretization_points; ++i) {</pre>
          using std::abs;
          const auto xi = static_cast<ValueType>(i + 1) * h;
          error +=
               abs(u->get_const_values()[i] - correct_u(xi)) / abs(correct_u(xi));
     return error;
int main(int argc, char* argv[])
Some shortcuts
using ValueType = double;
using IndexType = int;
using vec = gko::matrix::Dense<ValueType>;
using mtx = gko::matrix::Csr<ValueType, IndexType>;
using cg = gko::solver::Cg<ValueType>;
using bj = gko::preconditioner::Jacobi<ValueType, IndexType>;
Print version information
std::cout « gko::version_info::get() « std::endl;
if (argc == 2 && (std::string(argv[1]) == "--help")) {
    std::cerr « "Usage: " « argv[0]
                 « " [executor] [DISCRETIZATION_POINTS]" « std::endl;
     std::exit(-1);
Get number of discretization points
const unsigned int discretization_points =
   argc >= 3 ? std::atoi(argv[2]) : 100;
Get the executor string
```

const auto executor\_string = argc >= 2 ? argv[1] : "reference";

#### Figure out where to run the code

```
std::map<std::string, std::function<std::shared_ptr<gko::Executor>()»
    exec_map{
               [] { return gko::OmpExecutor::create(); }},
        { "omp",
        {"cuda",
         [] {
            return gko::CudaExecutor::create(0,
                                              gko::OmpExecutor::create());
        }},
        {"hip",
         [] {
            return gko::HipExecutor::create(0, gko::OmpExecutor::create());
        {"dpcpp",
         [] {
             return gko::DpcppExecutor::create(0,
                                               gko::OmpExecutor::create());
        {"reference", [] { return gko::ReferenceExecutor::create(); }}};
```

#### executor where Ginkgo will perform the computation

```
const auto exec = exec_map.at(executor_string)(); // throws if not valid
```

#### executor used by the application

```
const auto app_exec = exec->get_master();
```

Set up the problem: define the exact solution, the right hand side and the Dirichlet boundary condition.

```
auto correct_u = [](ValueType x) { return x * x * x; };
auto f = [](ValueType x) { return ValueType(6) * x; };
auto u0 = correct_u(0);
auto u1 = correct_u(1);
```

#### initialize matrix and vectors

#### Generate solver and solve the system

#### Uncomment to print the solution print\_solution<ValueType>(u0, u1, u.get());

#### Results

#### This is the expected output:

```
Solve complete. The average relative error is 2.52236e-11
```

#### Comments about programming and debugging

```
#include <iostream>
#include <map>
#include <string>
#include <vector>
#include <ginkgo/ginkgo.hpp>
template <typename ValueType, typename IndexType>
void generate_stencil_matrix(gko::matrix::Csr<ValueType, IndexType>* matrix)
     const auto discretization points = matrix->get size()[0];
    auto row_ptrs = matrix->get_row_ptrs();
auto col_idxs = matrix->get_col_idxs();
     auto values = matrix->get_values();
     int pos = 0;
     const ValueType coefs[] = \{-1, 2, -1\};
     row_ptrs[0] = pos;
for (int i = 0; i < discretization_points; ++i) {</pre>
         for (auto ofs: {-1, 0, 1}) {
    if (0 <= i + ofs && i + ofs < discretization_points) {
                   values[pos] = coefs[ofs + 1];
                   col_idxs[pos] = i + ofs;
                   ++pos;
         row_ptrs[i + 1] = pos;
template <typename Closure, typename ValueType>
void generate_rhs(Closure f, ValueType u0, ValueType u1,
                     gko::matrix::Dense<ValueType>* rhs)
     const auto discretization_points = rhs->get_size()[0];
     auto values = rhs->get_values();
     const ValueType h = 1.0 / static_cast<ValueType>(discretization_points + 1);
for (gko::size_type i = 0; i < discretization_points; ++i) {
    const auto xi = static_cast<ValueType>(i + 1) * h;
         values[i] = -f(xi) * h * h;
     values[0] += u0;
     values[discretization_points - 1] += u1;
template <typename Closure, typename ValueType>
void print_solution(ValueType u0, ValueType u1,
                        const gko::matrix::Dense<ValueType>* u)
     std::cout « u0 « ' \n';
for (int i = 0; i < u->get_size()[0]; ++i) {
         std::cout « u->get_const_values()[i] « '\n';
     std::cout « u1 « std::endl;
template <typename Closure, typename ValueType>
gko::remove_complex<ValueType> calculate_error(
     int discretization_points, const gko::matrix::Dense<ValueType>* u,
     Closure correct_u)
     const ValueType h = 1.0 / static_cast<ValueType>(discretization_points + 1);
     gko::remove_complex<ValueType> error = 0.0;
     for (int i = 0; i < discretization_points; ++i) {</pre>
         using std::abs;
         const auto xi = static_cast<ValueType>(i + 1) * h;
         error +=
             abs(u->get_const_values()[i] - correct_u(xi)) / abs(correct_u(xi));
     return error;
int main(int argc, char* argv[])
     using ValueType = double;
     using IndexType = int;
     using vec = gko::matrix::Dense<ValueType>;
     using mtx = gko::matrix::Csr<ValueType, IndexType>;
using cg = gko::solver::Cg<ValueType>;
using bj = gko::preconditioner::Jacobi<ValueType, IndexType>;
     std::cout « gko::version_info::get() « std::endl;
if (argc == 2 && (std::string(argv[1]) == "--help")) {
    std::cerr « "Usage: " « argv[0]
                     « " [executor] [DISCRETIZATION_POINTS]" « std::endl;
         std::exit(-1);
     const unsigned int discretization_points =
```

```
argc >= 3 ? std::atoi(argv[2]) : 100;
const auto executor_string = argc >= 2 ? argv[1] : "reference";
std::map<std::string, std::function<std::shared_ptr<gko::Executor>()»
    exec_map{
         {"omp",
                [] { return gko::OmpExecutor::create(); }},
         {"cuda",
          [] {
              return gko::CudaExecutor::create(0,
                                                  gko::OmpExecutor::create());
        }},
{"hip",
         return gko::HipExecutor::create(0, gko::OmpExecutor::create());
}},
         {"dpcpp",
          [] {
              return gko::DpcppExecutor::create(0,
                                                   gko::OmpExecutor::create());
          } } ,
         {"reference", [] { return gko::ReferenceExecutor::create(); }}};
const auto exec = exec_map.at(executor_string)(); // throws if not valid
const auto app_exec = exec->get_master();
auto correct_u = [](ValueType x) { return x * x * x; };
auto f = [](ValueType x) { return ValueType(6) * x; };
auto u0 = correct_u(0);
auto u1 = correct_u(1);
auto matrix = mtx::create(app_exec, gko::dim<2>(discretization_points),
                            3 * discretization_points - 2);
generate_stencil_matrix(matrix.get());
auto rhs = vec::create(app_exec, gko::dim<2>(discretization_points, 1));
generate_rhs(f, u0, u1, rhs.get());
auto u = vec::create(app_exec, gko::dim<2>(discretization_points, 1));
for (int i = 0; i < u->get_size()[0]; ++i) {
    u->get\_values()[i] = 0.0;
const gko::remove_complex<ValueType> reduction_factor = 1e-7;
cg::build()
    .with_criteria(
        gko::stop::Iteration::build().with_max_iters(discretization_points),
         gko::stop::ResidualNorm<ValueType>::build().with_reduction_factor(
            reduction_factor))
    .with_preconditioner(bj::build())
    .on(exec)
    ->generate(clone(exec, matrix)) // copy the matrix to the executor
    ->apply(rhs, u);
\verb|std::cout| & \verb|"Solve| complete. \\ | \verb|nThe| average| relative| error is | \verb|"
           « calculate_error(discretization_points, u.get(), correct_u) /
                   static_cast<gko::remove_complex<ValueType>> (
                      discretization_points)
           « std::endl;
```

# The preconditioned-solver program

The preconditioned solver example..

This example depends on simple-solver.

#### Introduction

About the example

#### The commented program

```
Figure out where to run the code
const auto executor_string = argc >= 2 ? argv[1] : "reference";
std::map<std::string, std::function<std::shared_ptr<gko::Executor>()»
          {"omp", [] { return gko::OmpExecutor::create(); }},
          {"cuda",
           [] {
               return gko::CudaExecutor::create(0,
                                                         gko::OmpExecutor::create());
          }},
{"hip",
               return gko::HipExecutor::create(0, gko::OmpExecutor::create());
          {"dpcpp",
               return gko::DpcppExecutor::create(0,
                                                          gko::OmpExecutor::create());
          {"reference", [] { return gko::ReferenceExecutor::create(); }}};
executor where Ginkgo will perform the computation
const auto exec = exec_map.at(executor_string)(); // throws if not valid
Read data
auto A = share(gko::read<mtx>(std::ifstream("data/A.mtx"), exec));
auto b = gko::read<vec>(std::ifstream("data/b.mtx"), exec);
auto x = gko::read<vec>(std::ifstream("data/x0.mtx"), exec);
const RealValueType reduction_factor{1e-7};
Create solver factory
auto solver_gen
    cg::build()
         .with_criteria(gko::stop::Iteration::build().with_max_iters(20u),
```

gko::stop::ResidualNorm<ValueType>::build()

```
.with_reduction_factor(reduction_factor))
```

# Add preconditioner, these 2 lines are the only difference from the simple solver example .with\_preconditioner(bj::build().with\_max\_block\_size(8u)) .on(exec); Create solver auto solver = solver\_gen->generate(A); Solve system solver->apply(b, x); Print solution std::cout « "Solution (x):\n"; write(std::cout, x); Calculate residual auto one = gko::initialize<vec>({1.0}, exec); auto neg\_one = gko::initialize<vec>({-1.0}, exec); auto res = gko::initialize<real\_vec>({0.0}, exec); A->apply(one, x, neg\_one, b); b->compute\_norm2(res); std::cout « "Residual norm sqrt(r^T r):\n";

#### Results

#### This is the expected output:

write(std::cout, res);

```
Solution (x):
%%MatrixMarket matrix array real general
0.252218
0.108645
0.0662811
0.0630433
0.0384088
0.0396536
0.0402648
0.0338935
0.0193098
0.0234653
0.0211499
0.0196413
0.0199151
0.0181674
0.0162722
0.0150714
0.0107016
0.0121141
0.0123025
Residual norm sqrt(r^T r):
%%MatrixMarket matrix array real general
4.82005e-08
```

#### Comments about programming and debugging

```
#include <fstream>
#include <iostream>
#include <map>
#include <string>
#include <ginkgo/ginkgo.hpp>
int main(int argc, char* argv[])
{
    using ValueType = double;
    using RealValueType = gko::remove_complex<ValueType>;
    using IndexType = int;
    using vec = gko::matrix::Dense<ValueType>;
```

```
using real_vec = gko::matrix::Dense<RealValueType>;
using mtx = gko::matrix::Csr<ValueType, IndexType>;
using cg = gko::solver::Cg<ValueType>;
using bj = gko::preconditioner::Jacobi<ValueType, IndexType>;
std::cout « gko::version_info::get() « std::endl;
if (argc == 2 && (std::string(argv[1]) == "--help")) {
    std::cerr « "Usage: " « argv[0] « " [executor]" « std::endl;
    std::exit(-1);
const auto executor_string = argc >= 2 ? argv[1] : "reference";
std::map<std::string, std::function<std::shared_ptr<gko::Executor>()>
    exec_map{
         [] {
              return gko::CudaExecutor::create(0,
                                                    gko::OmpExecutor::create());
         {"hip",
          [] {
              return gko::HipExecutor::create(0, gko::OmpExecutor::create());
          }},
         {"dpcpp",
          [] {
              return gko::DpcppExecutor::create(0,
                                                     gko::OmpExecutor::create());
         {"reference", [] { return gko::ReferenceExecutor::create(); }}};
const auto exec = exec_map.at(executor_string)(); // throws if not valid
auto A = share(gko::read<mtx>(std::ifstream("data/A.mtx"), exec));
auto b = gko::read<vec>(std::ifstream("data/b.mtx"), exec);
auto x = gko::read<vec>(std::ifstream("data/x0.mtx"), exec);
const RealValueType reduction_factor{1e-7};
auto solver_gen
    cg::build()
         .with_criteria(gko::stop::Iteration::build().with_max_iters(20u),
                          gko::stop::ResidualNorm<ValueType>::build()
                             .with_reduction_factor(reduction_factor))
         .with_preconditioner(bj::build().with_max_block_size(8u))
         .on(exec);
auto solver = solver_gen->generate(A);
solver->apply(b, x);
std::cout « "Solution (x):\n";
write(std::cout, x);
auto one = gko::initialize<vec>({1.0}, exec);
auto neg_one = gko::initialize<vec>({-1.0}, exec);
auto res = gko::initialize<real_vec>({0.0}, exec);
A->apply(one, x, neg_one, b);
b->compute_norm2(res);
std::cout « "Residual norm sqrt(r^T r):\n";
write(std::cout, res);
```

# The preconditioner-export program

The preconditioner export example..

This example depends on simple-solver.

#### Introduction

#### About the example

This example shows how to explicitly generate and store preconditioners for a given matrix. It can also be used to inspect and debug the preconditioner generation.

```
void output(gko::ptr_param<const gko::WritableToMatrixData<double, int>> mtx,
             std::string name)
    std::ofstream stream{name};
std::cerr « "Writing " « name « std::endl;
gko::write(stream, mtx, gko::layout_type::coordinate);
template <typename Function>
auto try_generate(Function fun) -> decltype(fun())
     decltype(fun()) result;
         result = fun();
    } catch (const gko::Error& err) {
   std::cerr « "Error: " « err.what() « '\n';
         std::exit(-1);
     return result;
int main(int argc, char* argv[])
print usage message
if (argc < 2 || executors.find(argv[1]) == executors.end()) {
    std::cerr « "Usage: executable"</pre>
                « " <reference|omp|cuda|hip|dpcpp> [<matrix-file>] "
                   "[<jacobi|ilu|parilu|parilut|ilu-isai|parilu-isai|parilut-"
                   "isai] [<preconditioner args>]\n";
     std::cerr « "Jacobi parameters: [<max-block-size>] [<accuracy>] "
                    "[<storage-optimization:auto|0|1|2>]\n"
     std::cerr « "ParILU parameters: [<iteration-count>]\n";
     std::cerr
         « "ParILUT parameters: [<iteration-count>] [<fill-in-limit>]\n";
```

```
std::cerr « "ILU-ISAI parameters: [<sparsity-power>]\n";
    std::cerr « "ParILU-ISAI parameters: [<iteration-count>] "
                 "[<sparsity-power>]\n";
    std::cerr « "ParILUT-ISAI parameters: [<iteration-count>] "
                  "[<fill-in-limit>] [<sparsity-power>]\n";
    return -1:
generate executor based on first argument
auto exec = try_generate([&] { return executors.at(argv[1])(); });
set matrix and preconditioner name with default values
std::string matrix = argc < 3 ? "data/A.mtx" : argv[2];
std::string precond = argc < 4 ? "jacobi" : argv[3];</pre>
load matrix file into Csr format
auto mtx = gko::share(try_generate([&] {
    std::ifstream mtx_stream{matrix};
    if (!mtx_stream) {
        throw GKO_STREAM_ERROR("Unable to open matrix file");
    std::cerr « "Reading " « matrix « std::endl;
    return gko::read<gko::matrix::Csr<»(mtx_stream, exec);</pre>
}));
concatenate remaining arguments for filename
std::string output_suffix;
for (auto i = 4; i < argc; ++i) {</pre>
    output_suffix = output_suffix + "-" + argv[i];
handle different preconditioners
if (precond == "jacobi") {
jacobi: max_block_size, accuracy, storage_optimization
    auto factory_parameter = gko::preconditioner::Jacobi<>::build();
    if (argc >= 5) {
        {\tt factory\_parameter.with\_max\_block\_size} \, (
            static_cast<gko::uint32>(std::stoi(argv[4])));
    if (argc >= 6) {
        factory_parameter.with_accuracy(std::stod(argv[5]));
    if (argc >= 7) {
        {\tt factory\_parameter.with\_storage\_optimization(}
            : gko::precision_reduction(0, std::stoi(argv[6])));
auto factory = factory_parameter.on(exec);
auto jacobi = try_generate([&] { return factory->generate(mtx); });
output(jacobi, matrix + ".jacobi" + output_suffix);
} else if (precond == "ilu") {
ilu: no parameters
    auto ilu = gko::as<gko::Composition<»(try_generate([&] {</pre>
       return gko::factorization::Ilu<>::build().on(exec)->generate(mtx);
    output(gko::as<gko::matrix::Csr<>>(ilu->get_operators()[1]),
           matrix + ".ilu-u");
} else if (precond == "parilu") {
parilu: iterations
    auto factory_parameter = gko::factorization::ParIlu<>::build();
    if (argc >= 5) {
        {\tt factory\_parameter.with\_iterations} \, (
            static_cast<gko::size_type>(std::stoi(argv[4])));
    auto factory = factory_parameter.on(exec);
    auto ilu = gko::as<gko::Composition<»(</pre>
        try_generate([&] { return factory->generate(mtx); }));
    matrix + ".parilu" + output_suffix + "-u");
} else if (precond == "parilut") {
```

```
parilut: iterations, fill-in limit
   auto factory_parameter = gko::factorization::ParIlut<>::build();
   if (argc >= 5) {
       {\tt factory\_parameter.with\_iterations} \ (
          static_cast<gko::size_type>(std::stoi(argv[4])));
   if (argc >= 6) {
       factory_parameter.with_fill_in_limit(std::stod(argv[5]));
   auto factory = factory_parameter.on(exec);
   auto ilut = gko::as<gko::Composition<»(</pre>
   ilu-isai: sparsity power
   auto fact_factory =
      gko::share(gko::factorization::Ilu<>::build().on(exec));
   int sparsity_power = 1;
   if (argc >= 5) {
       sparsity_power = std::stoi(argv[4]);
   auto factory =
       gko::preconditioner::Ilu<gko::preconditioner::LowerIsai<>,
                              gko::preconditioner::UpperIsai<>>::build()
           .with_factorization(fact_factory)
           .with_l_solver(gko::preconditioner::LowerIsai<>::build()
                            .with_sparsity_power(sparsity_power))
           .with_u_solver(gko::preconditioner::UpperIsai<>::build()
                            .with_sparsity_power(sparsity_power))
           .on(exec);
   auto ilu_isai = try_generate([&] { return factory->generate(mtx); });
   output(ilu_isai->get_l_solver()->get_approximate_inverse(),
          matrix + ".ilu-isai" + output_suffix + "-1");
parilu-isai: iterations, sparsity power
   auto fact_parameter = gko::factorization::ParIlu<>::build();
   int sparsity_power = 1;
if (argc >= 5) {
       fact_parameter.with_iterations(
          static_cast<gko::size_type>(std::stoi(argv[4])));
   if (argc >= 6) {
       sparsity_power = std::stoi(argv[5]);
   auto fact_factory = gko::share(fact_parameter.on(exec));
   auto factory =
       gko::preconditioner::Ilu<gko::preconditioner::LowerIsai<>,
                              gko::preconditioner::UpperIsai<>>::build()
           .with_factorization(fact_factory)
           .with_l_solver(gko::preconditioner::LowerIsai<>::build()
                            .with_sparsity_power(sparsity_power))
           .with_u_solver(gko::preconditioner::UpperIsai<>::build()
                            .with_sparsity_power(sparsity_power))
           .on(exec);
   auto ilu_isai = try_generate([&] { return factory->generate(mtx); });
   parilut-isai: iterations, fill-in limit, sparsity power
       auto fact_parameter = gko::factorization::ParIlut<>::build();
int sparsity_power = 1;
if (argc >= 5) {
           fact_parameter.with_iterations(
              static_cast<gko::size_type>(std::stoi(argv[4])));
       if (argc >= 6) {
           fact_parameter.with_fill_in_limit(std::stod(argv[5]));
       if (argc >= 7) {
          sparsity_power = std::stoi(argv[6]);
       auto fact_factory = gko::share(fact_parameter.on(exec));
       auto factory =
           gko::preconditioner::Ilu<gko::preconditioner::LowerIsai<>,
```

#### This is the expected output:

#### When specifying an executor:

Reading data/A.mtx Writing data/A.mtx.jacobi

#### Comments about programming and debugging

```
#include <fstream>
#include <functional>
#include <iostream>
#include <map>
#include <memorv>
#include <string>
#include <ginkgo/ginkgo.hpp>
const std::map<std::string, std::function<std::shared_ptr<gko::Executor>()>
    executors{{"reference", [] { return gko::ReferenceExecutor::create(); }},
              {"omp", [] { return gko::OmpExecutor::create(); }},
{"cuda",
               [] {
                    return gko::CudaExecutor::create(
                        0, gko::ReferenceExecutor::create());
              {"hip",
                [] {
                    return gko::HipExecutor::create(
                       0, gko::ReferenceExecutor::create());
               {"dpcpp", [] {
                    return gko::DpcppExecutor::create(
                       0, gko::ReferenceExecutor::create());
               } } ;
void output(gko::ptr param<const gko::WritableToMatrixData<double, int>> mtx,
            std::string name)
    std::ofstream stream{name};
std::cerr « "Writing " « name « std::endl;
    gko::write(stream, mtx, gko::layout_type::coordinate);
template <typename Function>
auto try_generate(Function fun) -> decltype(fun())
    decltype(fun()) result;
    try {
       result = fun();
     catch (const gko::Error& err) {
        std::cerr « "Error: " « err.what() « '\n';
```

```
std::exit(-1);
    return result:
int main(int argc, char* argv[])
    if (argc < 2 || executors.find(argv[1]) == executors.end()) {</pre>
         std::cerr « "Usage: executable"
                   « " <reference|omp|cuda|hip|dpcpp> [<matrix-file>] "
                       "[<jacobi|ilu|parilu|parilut|ilu-isai|parilu-isai|parilut-"
                       "isai] [preconditioner args>]\n";
        std::cerr « "Jacobi parameters: [<max-block-size>] [<accuracy>] "
                      "[<storage-optimization:auto|0|1|2>]\n";
         std::cerr « "ParILU parameters: [<iteration-count>]\n";
        std::cerr
            « "ParILUT parameters: [<iteration-count>] [<fill-in-limit>]\n";
        std::cerr « "ILU-ISAI parameters: [<sparsity-power>]\n";
std::cerr « "ParILU-ISAI parameters: [<iteration-count>] "
                      "[<sparsity-power>]\n";
         std::cerr « "ParILUT-ISAI parameters: [<iteration-count>] "
                      "[<fill-in-limit>] [<sparsity-power>]\n";
        return -1:
    auto exec = try_generate([&] { return executors.at(argv[1])(); });
std::string matrix = argc < 3 ? "data/A.mtx" : argv[2];
std::string precond = argc < 4 ? "jacobi" : argv[3];</pre>
    auto mtx = gko::share(try_generate([&] {
        std::ifstream mtx_stream{matrix};
         if (!mtx_stream) {
             throw GKO_STREAM_ERROR("Unable to open matrix file");
        std::cerr « "Reading " « matrix « std::endl;
        return gko::read<gko::matrix::Csr<> (mtx_stream, exec);
    }));
    std::string output_suffix;
    for (auto i = 4; i < argc; ++i) {
        output_suffix = output_suffix + "-" + argv[i];
    if (precond == "jacobi") {
        auto factory_parameter = gko::preconditioner::Jacobi<>::build();
         if (argc >= 5) {
             {\tt factory\_parameter.with\_max\_block\_size(}
                 static cast<gko::uint32>(std::stoi(argv[4])));
         if (argc >= 6) {
             factory_parameter.with_accuracy(std::stod(argv[5]));
         if (argc >= 7) {
             factory_parameter.with_storage_optimization(
                 std::string{argv[6]} == "auto"
                     ? gko::precision_reduction::autodetect()
                      : gko::precision_reduction(0, std::stoi(argv[6])));
    auto factory = factory_parameter.on(exec);
auto jacobi = try_generate([&] { return factory->generate(mtx); });
output(jacobi, matrix + ".jacobi" + output_suffix);
} else if (precond == "ilu") {
        auto ilu = gko::as<gko::Composition<> (try_generate([&] {
            return gko::factorization::Ilu<>::build().on(exec)->generate(mtx);
        }));
        output(gko::as<gko::matrix::Csr<>>(ilu->get_operators()[1]),
                matrix + ".ilu-u");
    } else if (precond == "parilu") {
        auto factory_parameter = gko::factorization::ParIlu<>::build();
         if (argc >= 5) {
             factory parameter.with iterations (
                 static_cast<gko::size_type>(std::stoi(argv[4])));
         auto factory = factory_parameter.on(exec);
         auto ilu = gko::as<gko::Composition<»(
        output(gko::as<gko::matrix::Csr<>>(ilu->get_operators()[1]),
    matrix + ".parilu" + output_suffix + "-u");
} else if (precond == "parilut") {
        auto factory_parameter = gko::factorization::ParIlut<>::build();
         if (argc >= 5) {
             factory parameter.with iterations (
                 static_cast<gko::size_type>(std::stoi(argv[4])));
         if (argc >= 6) {
             factory_parameter.with_fill_in_limit(std::stod(argv[5]));
        auto factory = factory parameter.on(exec);
```

```
auto ilut = gko::as<gko::Composition<»(</pre>
       try_generate([&] { return factory->generate(mtx); }));
   auto fact_factory =
      gko::share(gko::factorization::Ilu<>::build().on(exec));
   int sparsity_power = 1;
   if (argc >= 5) {
       sparsity_power = std::stoi(argv[4]);
   auto factory =
       gko::preconditioner::Ilu<gko::preconditioner::LowerIsai<>,
                               gko::preconditioner::UpperIsai<>>::build()
           .with_factorization(fact_factory)
           .with_l_solver(gko::preconditioner::LowerIsai<>::build()
                            .with_sparsity_power(sparsity_power))
           .with_u_solver(gko::preconditioner::UpperIsai<>::build()
                             .with_sparsity_power(sparsity_power))
           .on(exec);
   output(ilu_isai->get_u_solver()->get_approximate_inverse(),
          matrix + ".ilu-isai" + output_suffix + "-u");
} else if (precond == "parilu-isai") {
   auto fact_parameter = gko::factorization::ParIlu<>::build();
   int sparsity_power = 1;
if (argc >= 5) {
       fact_parameter.with_iterations(
           static_cast<gko::size_type>(std::stoi(argv[4])));
   if (argc >= 6) {
       sparsity_power = std::stoi(argv[5]);
   auto fact_factory = gko::share(fact_parameter.on(exec));
   auto factory =
       gko::preconditioner::Ilu<gko::preconditioner::LowerIsai<>,
                               gko::preconditioner::UpperIsai<>>::build()
           .with_factorization(fact_factory)
           .with_l_solver(gko::preconditioner::LowerIsai<>::build()
                             .with_sparsity_power(sparsity_power))
           .with_u_solver(gko::preconditioner::UpperIsai<>::build()
                             .with_sparsity_power(sparsity_power))
   output(ilu_isai->get_u_solver()->get_approximate_inverse(),
matrix + ".parilu-isai" + output_suffix + "-u");
} else if (precond == "parilut-isai") {
   auto fact_parameter = gko::factorization::ParIlut<>::build();
int sparsity_power = 1;
if (argc >= 5) {
       fact_parameter.with_iterations(
           static_cast<gko::size_type>(std::stoi(argv[4])));
   if (argc >= 6) {
       fact_parameter.with_fill_in_limit(std::stod(argv[5]));
   if (argc >= 7) {
       sparsity_power = std::stoi(argv[6]);
   auto fact_factory = gko::share(fact_parameter.on(exec));
   auto factory =
       gko::preconditioner::Ilu<gko::preconditioner::LowerIsai<>,
                              gko::preconditioner::UpperIsai<>>::build()
           .with_factorization(fact_factory)
           .with_l_solver(gko::preconditioner::LowerIsai<>::build()
                             .with_sparsity_power(sparsity_power))
           .with_u_solver(gko::preconditioner::UpperIsai<>::build()
                             .with_sparsity_power(sparsity_power))
           .on(exec);
   auto ilu_isai = try_generate([&] { return factory->generate(mtx); });
   output(ilu_isai->get_l_solver()->get_approximate_inverse(),
    matrix + ".parilut-isai" + output_suffix + "-l");
   }
```

# The reordered-preconditioned-solver program

The reordered preconditioned solver example..

This example depends on preconditioned-solver.

# Introduction

#### About the example

This uses an RCM reordering on an input matrix to construct a ParILU preconditioned solver and solve a linear system.

# The commented program

```
if (argc == 2 && (std::string(argv[1]) == "--help")) {
    std::cerr « "Usage: " « argv[0] « " [executor]" « std::endl;
    std::exit(-1);
Figure out where to run the code
const auto executor_string = argc >= 2 ? argv[1] : "reference";
std::map<std::string, std::function<std::shared_ptr<gko::Executor>()»
    exec_map{
        {"omp", [] { return gko::OmpExecutor::create(); }},
        {"cuda",
         [] {
              return gko::CudaExecutor::create(0,
                                                 gko::OmpExecutor::create());
        {"hip",
         [] {
             return gko::HipExecutor::create(0, gko::OmpExecutor::create());
        {"dpcpp",
          [] {
             return gko::DpcppExecutor::create(0,
                                                  gko::OmpExecutor::create());
        {"reference", [] { return gko::ReferenceExecutor::create(); }}};
executor where Ginkgo will perform the computation
const auto exec = exec_map.at(executor_string)(); // throws if not valid
Read data
auto A = share(gko::read<mtx>(std::ifstream("data/A.mtx"), exec));
auto b = gko::read<vec>(std::ifstream("data/b.mtx"), exec);
```

```
auto x = gko::read<vec>(std::ifstream("data/x0.mtx"), exec);
auto reordering =
    gko::experimental::reorder::Rcm<IndexType>::build().on(exec)->generate(
        A);
Permute matrix and vectors
auto A_reordered = share(A->permute(reordering));
auto b_reordered = b->permute(reordering, gko::matrix::permute_mode::rows);
this reordering is not necessary, but it maps the initial guess to the unreordered case
auto x_reordered = x->permute(reordering, gko::matrix::permute_mode::rows);
const RealValueType reduction_factor{1e-7};
Create solver factory
auto solver_gen :
    cg::build()
         .with_criteria(gko::stop::Iteration::build().with_max_iters(20u),
                         gko::stop::ResidualNorm<ValueType>::build()
    .with_reduction_factor(reduction_factor))
         .with_preconditioner(ilu::build())
         .on(exec);
Create solver
auto solver = solver_gen->generate(A_reordered);
Solve system
solver->apply(b_reordered, x_reordered);
Revert permutation to get the unpermuted solution
x_reordered->permute(reordering, x,
                       gko::matrix::permute_mode::inverse_rows);
Print solution
std::cout « "Solution (x):\n";
write(std::cout, x);
Calculate residual
    auto one = gko::initialize<vec>({1.0}, exec);
    auto neg_one = gko::initialize<vec>((-1.0), exec);
    auto res = gko::initialize<real_vec>({0.0}, exec);
    A->apply(one, x, neg_one, b);
    b->compute_norm2(res);
    std::cout « "Residual norm sqrt(r^T r):\n";
    write(std::cout, res);
```

## This is the expected output:

```
Solution (x):
%%MatrixMarket matrix array real general
19 1
0.252218
0.108645
0.0662811
0.0630433
0.0384088
0.0396536
0.0402648
0.0338935
0.0193098
0.0234653
0.0211499
0.0196413
0.0199151
0.0181674
0.0162722
0.0150714
0.0107016
0.0121141
0.0123025
Residual norm sqrt(r^T r):
%%MatrixMarket matrix array real general
4.82005e-08
```

```
#include <fstream>
#include <iostream>
#include <map>
#include <string>
#include <ginkgo/ginkgo.hpp>
int main(int argc, char* argv[])
    using ValueType = double;
    using RealValueType = gko::remove_complex<ValueType>;
    using IndexType = int;
    using vec = gko::matrix::Dense<ValueType>;
    using real_vec = gko::matrix::Dense<RealValueType>;
    using mtx = gko::matrix::Csr<ValueType, IndexType>;
    using cg = gko::solver::Cg<ValueType>;
    using ilu =
        gko::preconditioner::Ilu<gko::solver::LowerTrs<ValueType, IndexType>,
                                     gko::solver::UpperTrs<ValueType, IndexType>,
                                      false, IndexType>;
    std::cout « gko::version_info::get() « std::endl;
    if (argc == 2 && (std::string(argv[1]) == "--help")) {
   std::cerr « "Usage: " « argv[0] « " [executor]" « std::endl;
         std::exit(-1);
    const auto executor_string = argc >= 2 ? argv[1] : "reference";
    std::map<std::string, std::function<std::shared_ptr<gko::Executor>()»
             "" ("omp", [] { return gko::OmpExecutor::create(); }},
"" ("cuda",
              [] {
                   return gko::CudaExecutor::create(0,
                                                         gko::OmpExecutor::create());
             {"hip",
              [] {
                  return gko::HipExecutor::create(0, gko::OmpExecutor::create());
              { "dpcpp",
              [] {
                   return gko::DpcppExecutor::create(0,
                                                           gko::OmpExecutor::create());
             {"reference", [] { return gko::ReferenceExecutor::create(); }}};
    const auto exec = exec_map.at(executor_string)(); // throws if not valid
auto A = share(gko::read<mtx>(std::ifstream("data/A.mtx"), exec));
    auto b = gko::read<vec>(std::ifstream("data/b.mtx"), exec);
auto x = gko::read<vec>(std::ifstream("data/x0.mtx"), exec);
    auto reordering =
        gko::experimental::reorder::Rcm<IndexType>::build().on(exec)->generate(
    auto A_reordered = share(A->permute(reordering));
    auto b_reordered = b->permute(reordering, gko::matrix::permute_mode::rows);
auto x_reordered = x->permute(reordering, gko::matrix::permute_mode::rows);
const RealValueType reduction_factor{1e-7};
    auto solver gen
        cg::build()
             .with_criteria(gko::stop::Iteration::build().with_max_iters(20u),
                               gko::stop::ResidualNorm<ValueType>::build()
                                   .with_reduction_factor(reduction_factor))
             .with_preconditioner(ilu::build())
              .on(exec);
    auto solver = solver_gen->generate(A_reordered);
    solver->apply(b_reordered, x_reordered);
    x_reordered->permute(reordering, x,
                            gko::matrix::permute_mode::inverse_rows);
    std::cout « "Solution (x):\n";
    write(std::cout, x);
auto one = gko::initialize<vec>({1.0}, exec);
    auto neg_one = gko::initialize<vec>((-1.0), exec);
    auto res = gko::initialize<real_vec>({0.0}, exec);
    A->apply(one, x, neg_one, b);
    b->compute_norm2(res);
    std::cout « "Residual norm sqrt(r^T r):\n";
    write(std::cout, res);
```

# The schroedinger-splitting program

The Schroedinger equation example..

This example depends on heat-equation.

# Introduction

This example shows how to use the FFT and iFFT implementations in Ginkgo to solve the non-linear Schrödinger equation with a splitting method.

The non-linear Schrödinger equation (NLS) is given by

$$i\partial_t \theta = -\delta \theta + |\theta|^2 \theta$$

Here  $\theta$  is the wave function of a single particle in two dimensions. Its magnitude  $|\theta|^2$  describes the probability distribution of the particle's position.

This equation can be split in to its linear (1) and non-linear (2) part

$$(1) \quad i\partial_t \theta = -\delta \theta$$

(2) 
$$i\partial_t \theta = |\theta|^2 \theta$$

For both of these equations, we can compute exact solutions, assuming periodic boundary conditions and using the Fourier series expansion for (1) and using the fact that  $|\theta|^2$  is constant in (2):

$$(\hat{1})$$
  $\partial_t \hat{\theta}_k = -i|k|^2 \theta$ 

$$\begin{aligned} &(\hat{1}) & \partial_t \hat{\theta}_k = -i|k|^2 \theta \\ &(2') & \partial_t |\theta|^2 = i|\theta|^2 (\theta - \theta) = 0 \end{aligned}$$

The exact solutions are then given by

$$(\hat{1}) \quad \hat{\theta}(t) = e^{-i|k|^2 t} \hat{\theta}(0)$$

$$(2') \quad \theta(t) = e^{-i|\theta|^2 t} \theta(0)$$

These partial solutions can be used to approximate a solution to the full NLS by alternating between small time steps for (1) and (2).

For nicer visual results, we add another constant potential term V(x) \theta to the non-linear part, which turns it into the Gross-Pitaevskii equation.

#### About the example

# The commented program

```
The exact solutions are then given by
\f{align*}{
    (\hat 1) \quad \hat\theta(t) &= e^{-i |k|^2 t} \hat{t} 
    (2') \quad \text{quad } \quad \text{theta(t)} \quad \text{\&= e^{-i} | } \quad \text{theta(0)}
These partial solutions can be used to approximate a solution to the full NLS
by alternating between small time steps for (1) and (2).
For nicer visual results, we add another constant potential term V\left(x\right) \theta
to the non-linear part, which turns it into the Gross-Pitaevskii equation.
#include <algorithm>
#include <chrono>
#include <fstream>
#include <iostream>
#include <utility>
#include <opencv2/core.hpp>
#include <opencv2/videoio.hpp>
#include <ginkgo/ginkgo.hpp>
This function implements a simple Ginkgo-themed clamped color mapping for values in the range [0,5].
void set val(unsigned char* data, double value)
RGB values for the 6 colors used for values 0, 1, ..., 5 We will interpolate linearly between these values.
double col_r[] = \{255, 221, 129, 201, 249, 255\}; double col_g[] = \{255, 220, 130, 161, 158, 204\};
double col_b[] = {255, 220, 133, 93, 24, 8};

value = std::max(0.0, value);

auto i = std::max(0, std::min(4, int(value)));
auto d = std::max(0.0, std::min(1.0, value - i));
OpenCV uses BGR instead of RGB by default, revert indices
    data[0] = static\_cast < unsigned char > (col_b[i + 1] * d + col_b[i] * (1 - d));
Initialize video output with given dimension and FPS (frames per seconds)
std::pair<cv::VideoWriter, cv::Mat> build_output(int n, double fps)
    cv::Size videosize{n, n};
    auto output
        std::make_pair(cv::VideoWriter{}, cv::Mat{videosize, CV_8UC3});
    auto fourcc = cv::VideoWriter::fourcc('a', 'v', 'c', '1');
output.first.open("nls.mp4", fourcc, fps, videosize);
    return output;
Write the current frame to video output using the above color mapping
for (int i = 0; i < n; i++) {
        auto row = output.second.ptr(i);
for (int j = 0; j < n; j++) {
    set_val(&row[3 * j], abs(data[i * n + j]));</pre>
    output.first.write(output.second);
int main(int argc, char* argv[])
    using vec = gko::matrix::Dense<std::complex<double>>;
    using real_vec = gko::matrix::Dense<double>;
    using fft2 = gko::matrix::Fft2;
```

Problem parameters: simulation length

```
const auto t0 = 15.0;
scaling factor for non-linearity
const auto nonlinear_scale = 1.0;
scaling factor for potential
const auto potential_scale = 3.0;
Simulation parameters: time scaling factor
const auto time_scale = 0.25;
number of grid points in each dimension
const auto n = 256;
number of simulation steps per second
const auto steps_per_sec = 1000;
number of video frames per second
const auto fps = 25;
number of grid points
const auto n2 = n * n;
phase difference between neighboring grid points
const auto h = 2.0 * gko::pi < double > () / n;
const auto h2 = h * h;
time step size for the simulation
const auto tau = 1.0 / steps_per_sec;
const auto idx = [&](int i, int j) { return i * n + j; };
create an OpenMP executor
auto exec = gko::OmpExecutor::create();
load initial state vector
std::ifstream initial_stream("data/gko_logo_2d.mtx");
std::ifstream potential_stream("data/gko_text_2d.mtx");
auto amplitude = gko::read<vec>(initial_stream, exec);
auto potential = gko::read<real_vec>(potential_stream, exec);
create vector for frequency space representation
auto frequency = vec::create(exec, amplitude->get_size());
create Fourier matrix
auto fft = fft2::create(exec, n, n);
auto ifft = fft->conj_transpose();
prepare video output
auto output = build_output(n, fps);
time stamp of the last output frame (sentinel value)
double last_t = -t0;
execute splitting method: time step in linear part, then non-linear part
for (double t = 0; t < t0; t += tau) {
if enough time has passed, output the next frame
        last_t > 1.0 / fps) {
    last_t = t;
    std::cout « t « std::endl;
    output_timestep(output, n, amplitude->get_const_values());
time step in linear part
fft->apply(amplitude, frequency);
for (int i = 0; i < n; i++) {
   for (int j = 0; j < n; j++) {
     frequency->at(idx(i, j)) *=
             std::polar(1.0, -h2 * (i * i + j * j) * tau * time_scale);
```

The program will generate a video file named nls.mp4 and output the timestamp of each generated frame.

#### Comments about programming and debugging

```
This example shows how to use the FFT and iFFT implementations in Ginkgo
to solve the non-linear Schrödinger equation with a splitting method.
The non-linear Schrödinger equation (NLS) is given by
@f$
i \beta_t = - delta \theta_t + \beta_t^2 \theta_t
Here @f$\theta@f$ is the wave function of a single particle in two dimensions.
Its magnitude ef |\theta|^2ef$ describes the probability distribution of the
particle's position.
This equation can be split in to its linear (1) and non-linear (2) part
\f{align*}{
(1) \quad i \partial_t \theta &= -\delta \theta\\
(2) \quad i \partial_t \theta &= |\theta|^2 \theta
For both of these equations, we can compute exact solutions, assuming periodic
boundary conditions and using the Fourier series expansion for (1) and using the
fact that @f| \theta |^2@f$ is constant in (2):
\f{align*}{
(\hat \) \quad \quad \partial_t \hat\theta_k &= -i |k|^2 \theta \\ (2') \quad \partial_t |\theta|^2 &= i |\theta|^2 (\theta - \theta) = 0
The exact solutions are then given by
\f{align*}{
(\hat 1) \quad \hat\theta(t) &= e^{-i |k|^2 t} \hat\theta(0) \\
(2') \qquad \qquad \qquad \&= e^{-i} \mid \theta^2 t \mid \theta
These partial solutions can be used to approximate a solution to the full NLS
by alternating between small time steps for (1) and (2).
For nicer visual results, we add another constant potential term V\left(x\right) \theta
to the non-linear part, which turns it into the Gross-Pitaevskii equation.
#include <algorithm>
#include <chrono>
#include <fstream>
```

```
#include <iostream>
#include <utility>
#include <opencv2/core.hpp>
#include <opencv2/videoio.hpp>
#include <ginkgo/ginkgo.hpp>
void set_val(unsigned char* data, double value)
     double col_r[] = {255, 221, 129, 201, 249, 255};
     double col_g[] = {255, 220, 130, 161, 158, 204};
double col_b[] = {255, 220, 133, 93, 24, 8};
     value = std::max(0.0, value);
     auto i = std::max(0, std::min(4, int(value)));
     auto 1 = Std:.max(0, Std:.min(1, int(value)),
auto d = std::max(0.0, std::min(1.0, value - i));
data[2] = static_cast<unsigned char>(col_r[i + 1] * d + col_r[i] * (1 - d));
     \label{eq:data} \texttt{data[1] = static\_cast} < \texttt{unsigned char} > (\texttt{col\_g[i + 1]} * \texttt{d + col\_g[i]} * (1 - \texttt{d}));
     \label{eq:data0} \texttt{data[0]} = \texttt{static\_cast} < \texttt{unsigned char} > (\texttt{col\_b[i + 1]} * \texttt{d + col\_b[i]} * (1 - \texttt{d}));
std::pair<cv::VideoWriter, cv::Mat> build output(int n, double fps)
     cv::Size videosize{n, n};
     auto output =
          std::make_pair(cv::VideoWriter{}, cv::Mat{videosize, CV_8UC3});
     auto fourcc = cv::VideoWriter::fourcc('a', 'v', 'c', '1');
output.first.open("nls.mp4", fourcc, fps, videosize);
     return output;
void output_timestep(std::pair<cv::VideoWriter, cv::Mat>& output, int n,
                           const std::complex<double>* data)
     for (int i = 0; i < n; i++) {
          auto row = output.second.ptr(i);
for (int j = 0; j < n; j++) {</pre>
               set_val(&row[3 * j], abs(data[i * n + j]));
     output.first.write(output.second);
int main(int argc, char* argv[])
     using vec = gko::matrix::Dense<std::complex<double>>;
     using real_vec = gko::matrix::Dense<double>;
     using fft2 = gko::matrix::Fft2;
     const auto t0 = 15.0;
     const auto nonlinear_scale = 1.0;
     const auto potential_scale = 3.0;
     const auto time_scale = 0.25;
     const auto n = 256;
     const auto steps_per_sec = 1000;
     const auto fps = 25;
const auto n2 = n * n;
     const auto h = 2.0 * gko::pi<double>() / n;
     const auto h2 = h * h;
     const auto tau = 1.0 / steps_per_sec;
     const auto idx = [\&] (int i, int j) { return i * n + j; };
     auto exec = gko::OmpExecutor::create();
     std::ifstream initial_stream("data/gko_logo_2d.mtx"); std::ifstream potential_stream("data/gko_text_2d.mtx");
     auto amplitude = gko::read<vec>(initial_stream, exec);
     auto potential = gko::read<real_vec>(potential_stream, exec);
     auto frequency = vec::create(exec, amplitude->get_size());
     auto fft = fft2::create(exec, n, n);
auto ifft = fft->conj_transpose();
     auto output = build_output(n, fps);
     double last_t = -t0;
for (double t = 0; t < t0; t += tau) {</pre>
           if (t - last_t > 1.0 / fps) {
                last_t = t;
                std::cout « t « std::endl;
                output_timestep(output, n, amplitude->get_const_values());
           fft->apply(amplitude, frequency);
          for (int i = 0; i < n; i++) {
    for (int j = 0; j < n; j++) {
        frequency->at(idx(i, j)) *=
            std::polar(1.0, -h2 * (i * i + j * j) * tau * time_scale);
        frequency->at(idx(i, j)) *= 1.0 / n2;
           ifft->apply(frequency, amplitude);
           for (int i = 0; i < n; i++) {
    for (int j = 0; j < n; j++) {
        amplitude->at(idx(i, j)) *= std::polar()
                          1.0, -(nonlinear_scale *
                                        gko::squared_norm(amplitude->at(idx(i, j))) +
                                   potential_scale * potential->at(idx(i, j))) *
                                      tau * time_scale);
                }
```

}

# The simple-solver program

The simple solver example..

## Introduction

This simple solver example should help you get started with Ginkgo. This example is meant for you to understand how Ginkgo works and how you can solve a simple linear system with Ginkgo. We encourage you to play with the code, change the parameters and see what is best suited for your purposes.

#### About the example

Each example has the following sections:

- 1. **Introduction:**This gives an overview of the example and mentions any interesting aspects in the example that might help the reader.
- 2. **The commented program:** This section is intended for you to understand the details of the example so that you can play with it and understand Ginkgo and its features better.
- 3. **Results:** This section shows the results of the code when run. Though the results may not be completely the same, you can expect the behaviour to be similar.
- 4. **The plain program:** This is the complete code without any comments to have an complete overview of the code.

# The commented program

```
gko::matrix::Sellp could also be used.
using mtx = gko::matrix::Csr<ValueType, IndexType>;

The gko::solver::Cg is used here, but any other solver class can also be used.
using cg = gko::solver::Cg<ValueType>;

Print the ginkgo version information.
std::cout « gko::version_info::get() « std::endl;

Print help on how to execute this example.
if (argc == 2 && (std::string(argv[1]) == "--help")) {
    std::cerr « "Usage: " « argv[0] « " [executor] " « std::endl;
    std::exit(-1);
}
```

### Where do you want to run your solver?

The gko::Executor class is one of the cornerstones of Ginkgo. Currently, we have support for an gko::OmpExecutor, which uses OpenMP multi-threading in most of its kernels, a gko::ReferenceExecutor, a single threaded specialization of the OpenMP executor and a gko::CudaExecutor which runs the code on a NVIDIA GPU if available.

Note

With the help of C++, you see that you only ever need to change the executor and all the other functions/routines within Ginkgo should automatically work and run on the executor with any other changes.

```
const auto executor_string = argc >= 2 ? argv[1] : "reference";
std::map<std::string, std::function<std::shared_ptr<gko::Executor>()»
    exec_map{
        { "omp",
               [] { return gko::OmpExecutor::create(); }},
        {"cuda",
         [] {
             return gko::CudaExecutor::create(0,
                                              gko::OmpExecutor::create());
        {"hip",
            return gko::HipExecutor::create(0, gko::OmpExecutor::create());
        { "dpcpp",
         [] {
             return gko::DpcppExecutor::create(0,
                                               gko::OmpExecutor::create());
        {"reference", [] { return gko::ReferenceExecutor::create(); }}};
executor where Ginkgo will perform the computation
const auto exec = exec_map.at(executor_string)(); // throws if not valid
```

### Reading your data and transfer to the proper device.

Read the matrix, right hand side and the initial solution using the read function.

Note

Ginkgo uses C++ smart pointers to automatically manage memory. To this end, we use our own object ownership transfer functions that under the hood call the required smart pointer functions to manage object ownership. gko::share and gko::give are the functions that you would need to use.

```
auto A = gko::share(gko::read<mtx>(std::ifstream("data/A.mtx"), exec));
auto b = gko::read<vec>(std::ifstream("data/b.mtx"), exec);
auto x = gko::read<vec>(std::ifstream("data/x0.mtx"), exec);
```

#### Creating the solver

Generate the gko::solver factory. Ginkgo uses the concept of Factories to build solvers with certain properties. Observe the Fluent interface used here. Here a cg solver is generated with a stopping criteria of maximum iterations of 20 and a residual norm reduction of 1e-7. You also observe that the stopping criteria(gko::stop) are also generated from factories using their build methods. You need to specify the executors which each of the object needs to be built on.

Generate the solver from the matrix. The solver factory built in the previous step takes a "matrix" (a gko::LinOp to be more general) as an input. In this case we provide it with a full matrix that we previously read, but as the solver only

effectively uses the apply() method within the provided "matrix" object, you can effectively create a gko::LinOp class with your own apply implementation to accomplish more tasks. We will see an example of how this can be done in the custom-matrix-format example

```
auto solver = solver_gen->generate(A);
```

Finally, solve the system. The solver, being a gko::LinOp, can be applied to a right hand side, b to obtain the solution, x.

```
solver->apply(b, x);
```

Print the solution to the command line.

```
std::cout « "Solution (x):\n";
write(std::cout, x);
```

To measure if your solution has actually converged, you can measure the error of the solution. one, neg\_one are objects that represent the numbers which allow for a uniform interface when computing on any device. To compute the residual, all you need to do is call the apply method, which in this case is an spmv and equivalent to the LAPACK z\_spmv routine. Finally, you compute the euclidean 2-norm with the compute\_norm2 function.

```
auto one = gko::initialize<vec>({1.0}, exec);
auto neg_one = gko::initialize<vec>({-1.0}, exec);
auto res = gko::initialize<real_vec>({0.0}, exec);
A->apply(one, x, neg_one, b);
b->compute_norm2(res);
std::cout « "Residual norm sqrt(r^T r):\n";
write(std::cout, res);
```

### Results

#### The following is the expected result:

```
Solution (x):
%%MatrixMarket matrix array real general
0.252218
0.108645
0.0662811
0.0630433
0.0384088
0.0396536
0.0402648
0.0338935
0.0193098
0.0234653
0.0211499
0.0196413
0.0199151
0.0181674
0.0162722
0.0150714
0.0107016
0.0121141
0.0123025
Residual norm sqrt(r^T r):
%%MatrixMarket matrix array real general
2.10788e-15
```

#### Comments about programming and debugging

```
#include <ginkgo/ginkgo.hpp>
#include <fstream>
#include <iostream>
#include <map>
#include <string>
int main(int argc, char* argv[]) {
    using ValueType = double;
    using RealValueType = gko::remove_complex<ValueType>;
    using IndexType = int;
```

```
using vec = gko::matrix::Dense<ValueType>;
using real_vec = gko::matrix::Dense<RealValueType>;
using mtx = gko::matrix::Csr<ValueType, IndexType>;
using cg = gko::solver::Cg<ValueType>;
std::cout « gko::version_info::get() « std::endl;
if (argc == 2 && (std::string(argv[1]) == "--help")) {
    std::cerr « "Usage: " « argv[0] « " [executor] " « std::endl;
     std::exit(-1);
const auto executor_string = argc >= 2 ? argv[1] : "reference";
std::map<std::string, std::function<std::shared_ptr<gko::Executor>()>
    exec_map{
          [] {
               return gko::CudaExecutor::create(0,
                                                        gko::OmpExecutor::create());
          }},
{"hip",
           [] {
               return gko::HipExecutor::create(0, gko::OmpExecutor::create());
           }},
          {"dpcpp",
           [] {
                return gko::DpcppExecutor::create(0,
                                                         gko::OmpExecutor::create());
          {"reference", [] { return gko::ReferenceExecutor::create(); }}};
const auto exec = exec_map.at(executor_string)(); // throws if not valid auto A = gko::share(gko::read<mtx>(std::ifstream("data/A.mtx"), exec));
auto b = gko::read<vec>(std::ifstream("data/b.mtx"), exec);
auto x = gko::read<vec>(std::ifstream("data/x0.mtx"), exec);
const RealValueType reduction_factor{1e-7};
auto solver_gen
    cg::build()
          .with_criteria(gko::stop::Iteration::build().with_max_iters(20u),
                            gko::stop::ResidualNorm<ValueType>::build()
                                 .with_reduction_factor(reduction_factor))
auto solver = solver_gen->generate(A);
solver->apply(b, x);
std::cout « "Solution (x):\n";
write(std::cout, x);
auto one = gko::initialize<vec>({1.0}, exec);
auto neg_one = gko::initialize<vec>({-1.0}, exec);
auto res = gko::initialize<real_vec>({0.0}, exec);
A->apply(one, x, neg_one, b);
b->compute_norm2(res);
std::cout « "Residual norm sqrt(r^T r):\n";
write(std::cout, res);
```

# The simple-solver-logging program

The simple solver with logging example..

This example depends on simple-solver, minimal-cuda-solver.

## Introduction

About the example

# The commented program

```
Some shortcuts
using ValueType = double;
using RealValueType = gko::remove_complex<ValueType>;
using IndexType = int;
using real_vec = gko::matrix::Dense<ValueType>;
using real_vec = gko::matrix::Dense<RealValueType>;
using mtx = gko::matrix::Csr<ValueType, IndexType>;
using cg = gko::solver::Cg<ValueType>;
Print version information
std::cout « gko::version_info::get() « std::endl;
if (argc == 2 && (std::string(argy[1]) == "--help")) {
    std::cerr « "Usage: " « argv[0] « " [executor]" « std::endl;
    std::exit(-1);
Figure out where to run the code
const auto executor_string = argc >= 2 ? argv[1] : "reference";
std::map<std::string, std::function<std::shared_ptr<gko::Executor>()>
    exec_map{
         {"omp",
                 [] { return gko::OmpExecutor::create(); }},
         {"cuda",
          [] {
              return gko::CudaExecutor::create(0,
                                                    gko::OmpExecutor::create());
         {"hip",
          [] {
              return gko::HipExecutor::create(0, gko::OmpExecutor::create());
         {"dpcpp",
              return gko::DpcppExecutor::create(0,
                                                     gko::OmpExecutor::create());
```

{"reference", [] { return gko::ReferenceExecutor::create(); }}};

#### executor where Ginkgo will perform the computation

```
const auto exec = exec_map.at(executor_string)(); // throws if not valid
```

#### Read data

```
auto A = share(gko::read<mtx>(std::ifstream("data/A.mtx"), exec));
auto b = gko::read<vec>(std::ifstream("data/b.mtx"), exec);
auto x = gko::read<vec>(std::ifstream("data/x0.mtx"), exec);
```

Let's declare a logger which prints to std::cout instead of printing to a file. We log all events except for all linop factory and polymorphic object events. Events masks are group of events which are provided for convenience.

```
std::shared_ptr<gko::log::Stream<ValueType» stream_logger =
    gko::log::Stream<ValueType>::create(
        gko::log::Logger::all_events_mask ^
            gko::log::Logger::linop_factory_events_mask ^
            gko::log::Logger::polymorphic_object_events_mask,
        std::cout);
```

#### Add stream\_logger to the executor

exec->add\_logger(stream\_logger);

.on(exec);

auto solver = solver\_gen->generate(A);

Add stream\_logger only to the ResidualNorm criterion Factory Note that the logger will get automatically propagated to every criterion generated from this factory.

First we add facilities to only print to a file. It's possible to select events, using masks, e.g. only iterations mask: gko::log::Logger::iteration complete mask. See the documentation of Logger class for more information.

This adds a simple logger that only reports convergence state at the end of the solver. Specifically it captures the last residual norm, the final number of iterations, and the converged or not converged status.

```
std::shared_ptr<gko::log::Convergence<ValueType» convergence_logger =
    gko::log::Convergence<ValueType>::create();
solver->add_logger(convergence_logger);
```

Add another logger which puts all the data in an object, we can later retrieve this object in our code. Here we only have want Executor and criterion check completed events.

#### Solve system

}

solver->apply(b, x);

Print the residual of the last criterion check event (where convergence happened)

```
auto residual =
    record_logger->get().iteration_completed.back()->residual.get();
auto residual_d = gko::as<vec>(residual);
print_vector("Residual", residual_d);

Print solution
```

```
This is the expected output:
[LOG] >> apply started on A LinOp[gko::solver::Cg<double>,0x2142d60] with b
            LinOp[gko::matrix::Dense<double>,0x2142140] and x LinOp[gko::matrix::Dense<double>,0x2143450]
[LOG] >> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[8]
[LOG] >> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2142280] with
            Bvtes[8]
[LOG] >> allocation started on Executor[gko::ReferenceExecutor.0x21400d0] with Bytes[8]
[LOG] »> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2143410] with
            Bytes[8]
[LOG] >> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[152]
[LOG] »> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x21480a0] with
            Bytes[152]
[LOG] >> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[152]
[LOG] »> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x21482f0] with
            Bytes[152]
[LOG] »> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[152]
[LOG] »> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x21484d0] with
            Bytes[152]
[LOG] »> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[152]
[LOG] »> allocation completed on Executor[gko::ReferenceExecutor,0x2140d0] at Location[0x21486b0] with
            Bytes[152]
[LOG] >> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[8]
[LOG] >> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2148010] with
            Bytes[8]
[LOG] »> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[8]
[LOG] »> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2148a60] with
            Bytes[8]
[LOG] »> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[8]
[LOG] >> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x21482b0] with
            Bytes[8]
[LOG] »> allocation started on Executor[gko::ReferenceExecutor, 0x21400d0] with Bytes[8]
[LOG] >> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2148a40] with
            Bytes[8]
[LOG] »> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[1]
[LOG] »> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2147c90] with
            Bytes[1]
[LOG] >> Operation[gko::solver::cg::initialize_operation<gko::matrix::Dense<double> const*&,
            gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
            gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] started on
            Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::solver::cg::initialize_operation<gko::matrix::Dense<double> const*&,
            gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
gko::matrix::Dense<double>*,
gko::matrix::Dense<double>*,
            gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] completed on
            Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] »> Operation[gko::matrix::csr::advanced_spmv_operation<gko::matrix::Dense<double> const*,
            gko::matrix::Csr<double, int> const*, gko::matrix::Dense<double> const*, gko::matrix::Dense<double>
            const*, gko::matrix::Dense<double>*>,0x7ffd93d14aa0] started on
            Executor[qko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::csr::advanced spmv operation<gko::matrix::Dense<double> const*,
            gko::matrix::Csr<double, int> const*, gko::matrix::Dense<double> const*, gko::mat
            Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] »> allocation started on Executor[qko::ReferenceExecutor,0x21400d0] with Bytes[2]
[LOG] >> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2148ee0] with
            Bytes[2]
[LOG] >> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[8]
[LOG] »> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2148e50] with
[LOG] »> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[8]
[LOG] \gg allocation \ completed \ on \ Executor[gko::ReferenceExecutor,0x21400d0] \ at \ Location[0x2147ce0] \ with \ constant \ and \ and \ constant \ and \ 
            Bvtes[8]
[LOG] >> Operation(gko::matrix::dense::compute norm2 operation(gko::matrix::Dense(double) const*
            gko::matrix::Dense<double>*>,0x7ffd93d14a20] started on Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] »> Operation[gko::matrix::dense::compute_norm2_operation<gko::matrix::Dense<double> const*,
             gko::matrix::Dense<double>*>,0x7ffd93d14a20] completed on Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x21482f0] with
            Bytes[152]
[LOG] »> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
            Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x21482f0] with
            Bytes[152]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
            \label{lem:gko::matrix::Dense<double>*>,0x7ffd93d14c50]} started on \\ \texttt{Executor[gko::ReferenceExecutor,0x21400d0]}
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
            gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] completed on
            Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> iteration 0 completed with solver LinOp[gko::solver::Cg<double>,0x2142d60] with residual
            \label{linOp} \texttt{LinOp[gko::matrix::Dense<double>,0x2147b30], solution LinOp[gko::matrix::Dense<double>,0x2143450] and the line of the li
            residual norm LinOp[gko::LinOp const*,0]
[LOG] »> check started for stop::Criterion[gko::stop::ResidualNorm<double>,0x2148db0] at iteration 0 with ID
            1 and finalized set to 1
```

```
[LOG] >> Operation[gko::matrix::dense::compute_norm2_operation<gko::matrix::Dense<double> const*,
      gko::matrix::Dense<double>*>,0x7ffd93d14ad0] started on Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_norm2_operation<gko::matrix::Dense<double> const*
      gko::matrix::Dense<double>*>,0x7ffd93d14ad0] completed on Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::stop::residual_norm::residual_norm_operation<gko::matrix::Dense<double> const*&,
     gko::matrix::Dense<double>*, double&, unsigned char&, bool&, gko::array<gko::stopping_status>*&,
gko::array<bool>*, bool*, bool*&>,0x7ffd93d14b90] started on
      Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::stop::residual_norm::residual_norm_operation<gko::matrix::Dense<double> const*&,
      gko::matrix::Dense<double>*, double&, unsigned char&, bool&, gko::array<gko::stopping_status>*&,
gko::array<bool>*, bool*, bool*&>,0x7ffd93d14b90] completed on
      Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] »> check completed for stop::Criterion[gko::stop::ResidualNorm<double>,0x2148db0] at iteration 0 with
      ID 1 and finalized set to 1. It changed one RHS 0, stopped the iteration process 0
[LOG] »> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[152]
[LOG] »> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149550] with
     Bytes[152]
[LOG] »> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
      Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x2149550] with
      Bvtes[152]
[LOG] »> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
      Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x2149550] with
      Bytes[152]
[LOG] >> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[152]
[LOG] »> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149730] with
      Bytes[152]
[LOG] »> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
      Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x2143e90] to Location[0x2149730] with
      Bytes[152]
[LOG] »> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
      Executor[gko::ReferenceExecutor, 0x21400d0] from Location[0x2143e90] to Location[0x2149730] with
      Bytes[152]
[LOG] »> Operation[gko::solver::cg::step_1_operation<gko::matrix::Dense<double>*,
      gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
      gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] started on
      Executor[gko::ReferenceExecutor, 0x21400d0]
gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] completed on
      Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::csr::spmv_operation<gko::matrix::Csr<double, int> const*,
     \label{lem:gko::matrix::Dense<double>*>,0x7ffd93d14b80]} started on \\ \texttt{Executor[gko::ReferenceExecutor,0x21400d0]}
[LOG] >> Operation[gko::matrix::csr::spmv_operation<gko::matrix::Csr<double, int> const*,
      gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14b80] completed on
      Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
      gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] started on
      Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
      gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] completed on
      Executor[gko::ReferenceExecutor,0x21400d0]
gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
gko::matrix::Dense<double>*,
      gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] started on
      Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::solver::cg::step_2_operation<gko::matrix::Dense<double>*&,
      gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
      gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] completed on
      Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> copy started from Executor[gko::ReferenceExecutor, 0x21400d0] to
      Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x21482f0] with
      Bytes [152]
[LOG] \gg copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
      Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x21482f0] with
      Bytes[152]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
      gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] started on
      Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
     gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] completed on
Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> iteration 1 completed with solver LinOp[gko::solver::Cg<double>,0x2142d60] with residual
      LinOp[gko::matrix::Dense<double>,0x2147b30], solution LinOp[gko::matrix::Dense<double>,0x2143450] and
      residual_norm LinOp[gko::LinOp const*,0]
[LOG] »> check started for stop::Criterion[gko::stop::ResidualNorm<double>,0x2148db0] at iteration 1 with ID
      1 and finalized set to 1
[LOG] >> Operation[gko::matrix::dense::compute norm2 operation<gko::matrix::Dense<double> const*,
      gko::matrix::Dense<double>*>,0x7ffd93d14ad0] started on Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] »> Operation[gko::matrix::dense::compute_norm2_operation<gko::matrix::Dense<double> const*,
      gko::matrix::Dense<double>*>,0x7ffd93d14ad0] completed on Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] »> Operation[gko::stop::residual_norm::residual_norm_operation<gko::matrix::Dense<double> const*&,
      gko::matrix::Dense<double>*, double&, unsigned char&, bool&, gko::array<gko::stopping_status>*&,
gko::array<bool>*, bool*, bool*&>,0x7ffd93d14b90] started on
      Executor[gko::ReferenceExecutor,0x21400d0]
```

```
[LOG] >> Operation[gko::stop::residual_norm::residual_norm_operation<gko::matrix::Dense<double> const*&,
         gko::matrix::Dense<double>*, double&, unsigned char&, bool&, gko::array<gko::stopping_status>*&, gko::array<bool>*, bool*, bool*&>,0x7ffd93d14b90] completed on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] \  \  \, \text{``stop::ResidualNorm'} < \text{double'}, 0 \\ \text{``x} 2148 \\ \text{db0}] \  \  \, \text{at iteration 1 with 1} \\ \text{``x} 1 \\ \text{``x} 2 \\ \text{``x} 3 \\ \text{``x} 4 \\ \text{``x
         ID 1 and finalized set to 1. It changed one RHS 0, stopped the iteration process 0
[LOG] >> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[152]
[LOG] »> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149980] with
         Bytes[152]
[LOG] >> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
         Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x2149980] with
         Bytes[152]
[LOG] »> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
         Executor[gko::ReferenceExecutor, 0x21400d0] from Location[0x21480a0] to Location[0x2149980] with
         Bytes[152]
        »> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[152]
[LOG] >> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149b80] with
        Bytes[152]
[LOG] »> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
         Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x2143e90] to Location[0x2149b80] with
         Bytes[152]
[LOG] »> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
         Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x2143e90] to Location[0x2149b80] with
         Bytes[152]
[LOG] >> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149730]
[LOG] >> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149730]
[LOG] »> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149550]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149550]
[LOG] >> Operation[gko::solver::cg::step_1_operation<gko::matrix::Dense<double>*,
        gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] started on
         Executor[gko::ReferenceExecutor, 0x21400d0]
[LOG] >> Operation[gko::solver::cg::step_1_operation<gko::matrix::Dense<double>*,
         gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
         gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] completed on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::csr::spmv_operation<gko::matrix::Csr<double, int> const*,
         gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14b80] started on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::csr::spmv_operation<gko::matrix::Csr<double, int> const*,
        gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14b80] completed on
Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
         gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] started on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
         gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] completed on
         Executor[gko::ReferenceExecutor, 0x21400d0]
[LOG] >> Operation[gko::solver::cg::step_2_operation<gko::matrix::Dense<double>*&,
         gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
gko::matrix::Dense<double>*,
         gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] started on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::solver::cg::step_2_operation<gko::matrix::Dense<double>*&,
        gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
gko::matrix::Dense<double>*,
         gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] completed on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
         Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x21482f0] with
         Bytes[152]
[LOG] »> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
         Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x21482f0] with
[LOG] »> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
         gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] started on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
         qko::matrix::Dense<double> const*, qko::matrix::Dense<double>*>,0x7ffd93d14c50] completed on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> iteration 2 completed with solver LinOp[gko::solver::Cg<double>,0x2142d60] with residual
         LinOp[gko::matrix::Dense<double>,0x2147b30], solution LinOp[gko::matrix::Dense<double>,0x2143450] and
         residual_norm LinOp[gko::LinOp const*,0]
[LOG] >> check started for stop::Criterion[gko::stop::ResidualNorm<double>,0x2148db0] at iteration 2 with ID 1 and finalized set to 1
[LOG] >> Operation[gko::matrix::dense::compute_norm2_operation<gko::matrix::Dense<double> const*,
         gko::matrix::Dense<double>*>,0x7ffd93d14ad0] started on Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] »> Operation[gko::matrix::dense::compute_norm2_operation<gko::matrix::Dense<double> const*,
         gko::matrix::Dense<double>*>,0x7ffd93d14ad0] completed on Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::stop::residual_norm::residual_norm_operation<gko::matrix::Dense<double> const*&,
         gko::matrix::Dense<double>*, double&, unsigned char&, bool&, gko::array<gko::stopping_status>*&,
         gko::array<bool>*, bool*, bool*&>,0x7ffd93d14b90] started on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::stop::residual_norm::residual_norm_operation<gko::matrix::Dense<double> const*&,
         gko::matrix::Dense<double>*, double&, unsigned char&, bool&, gko::array<gko::stopping_status>*&,
gko::array<bool>*, bool*, bool*&>,0x7ffd93d14b90] completed on
         Executor[gko::ReferenceExecutor, 0x21400d0]
```

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[LOG] »> check completed for stop::Criterion[gko::stop::ResidualNorm<double>,0x2148db0] at iteration 2 with
      ID 1 and finalized set to 1. It changed one RHS 0, stopped the iteration process 0
[LOG] >> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[152]
[LOG] »> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149290] with
      Bytes[152]
[LOG] >> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
      Executor[gko::ReferenceExecutor, 0x21400d0] from Location[0x21480a0] to Location[0x2149290] with
      Bytes[152]
[LOG] \gg copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
      Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x2149290] with
      Bytes[152]
[LOG] >> allocation started on Executor[gko::ReferenceExecutor.0x21400d0] with Bytes[152]
[LOG] »> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149690] with
      Bytes[152]
[LOG] >> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
      Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x2143e90] to Location[0x2149690] with
      Bytes[152]
[LOG] >> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
      Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x2143e90] to Location[0x2149690] with
      Bvtes[152]
[LOG] >> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149b80]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149b80]
[LOG] »> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149980]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149980]
[LOG] >> Operation[gko::solver::cg::step_1_operation<gko::matrix::Dense<double>*,
      gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
      gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] started on
      Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::solver::cg::step_1_operation<gko::matrix::Dense<double>*,
      gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
gko::matrix::Dense<double>*,
gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] completed on
      Executor[gko::ReferenceExecutor, 0x21400d0]
[LOG] >> Operation[gko::matrix::csr::spmv_operation<gko::matrix::Csr<double, int> const*,
      gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14b80] started on
      Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::csr::spmv_operation<gko::matrix::Csr<double, int> const*, gko::matrix::Dense<double>*>,0x7ffd93d14b80] completed on
      Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
      gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] started on
      Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
      qko::matrix::Dense<double> const*, qko::matrix::Dense<double>*>,0x7ffd93d14c50] completed on
      Executor[gko::ReferenceExecutor, 0x21400d0]
[LOG] >> Operation[gko::solver::cg::step_2_operation<gko::matrix::Dense<double>*&,
      gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
      gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
      gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] started on
Executor[gko::ReferenceExecutor,0x21400d0]
 [LOG] \  \  \, \hbox{$>$} \  \  \, \hbox{Operation[gko::solver::cg::step\_2\_operation<gko::matrix::Dense<double>*&,} \\
      gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
       gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] completed on
      Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] \gg copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
      Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x21482f0] with
      Bytes[152]
[LOG] >> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
      Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x21482f0] with
      Bytes[152]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
      qko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] started on
      Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
      gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] completed on
      Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] \gg \text{ iteration 3 completed with solver LinOp[gko::solver::Cg<double>,0x2142d60] with residual}
      LinOp[gko::matrix::Dense<double>,0x2147b30], solution LinOp[gko::matrix::Dense<double>,0x2143450] and
      residual_norm LinOp[gko::LinOp const*,0]
[LOG] >> check started for stop::Criterion[gko::stop::ResidualNorm<double>,0x2148db0] at iteration 3 with ID
      1 and finalized set to 1
[LOG] >> Operation[gko::matrix::dense::compute_norm2_operation<gko::matrix::Dense<double> const*,
      gko::matrix::Dense<double>*>,0x7ffd93d14ad0] started on Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] »> Operation[gko::matrix::dense::compute_norm2_operation<gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14ad0] completed on Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] »> Operation[gko::stop::residual_norm::residual_norm_operation<gko::matrix::Dense<double> const*&,
      gko::matrix::Dense<double>*, double&, unsigned char&, bool&, gko::array<gko::stopping_status>*&, gko::array<br/>bool>*, bool*, bool*&>,0x7ffd93d14b90] started on
      Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::stop::residual_norm::residual_norm_operation<gko::matrix::Dense<double> const*&,
      gko::matrix::Dense<double>*, double&, unsigned char&, bool&, gko::array<gko::stopping_status>*&,
gko::array<bool>*, bool*, bool*&>,0x7ffd93d14b90] completed on
      Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] »> check completed for stop::Criterion[gko::stop::ResidualNorm<double>,0x2148db0] at iteration 3 with
      ID 1 and finalized set to 1. It changed one RHS 0, stopped the iteration process 0 \,
[LOG] >> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[152]
[LOG] >> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149890] with
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Bytes[152]
[LOG] \gg copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
          Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x2149890] with
          Bytes[152]
[LOG] >> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
          Executor[gko::ReferenceExecutor, 0x21400d0] from Location[0x21480a0] to Location[0x2149890] with
          Bytes[152]
[LOG] »> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[152]
[LOG] >> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149ae0] with
          Bytes[152]
[LOG] >> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
          Executor[gko::ReferenceExecutor, 0x21400d0] from Location[0x2143e90] to Location[0x2149ae0] with
          Bytes[152]
[LOG] »> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
           Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x2143e90] to Location[0x2149ae0] with
          Bytes[152]
[LOG] >> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149690]
[LOG] >> free completed on Executor[gko::ReferenceExecutor, 0x21400d0] at Location[0x2149690]
[LOG] »> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149290]
[LOG] >> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149290]
[LOG] >> Operation[gko::solver::cg::step_1_operation<gko::matrix::Dense<double>*,
           gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
           gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] started on
          Executor[gko::ReferenceExecutor, 0x21400d0]
[LOG] >> Operation[gko::solver::cg::step_1_operation<gko::matrix::Dense<double>*,
          gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
           gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] completed on
           Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::csr::spmv_operation<gko::matrix::Csr<double, int> const*,
          gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14b80] started on
Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::csr::spmv_operation<gko::matrix::Csr<double, int> const*,
           gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14b80] completed on
           Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] \  \  \, \text{"No Operation} \  \  \, \text{"Sense::compute\_dot\_operation} \  \  \, \text{"Matrix::Dense<double> const*} \  \  \, \text{"Months of the operation} \  \  \, \text{"Months of th
           qko::matrix::Dense<double> const*, qko::matrix::Dense<double>*>,0x7ffd93d14c50] started on
          Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
           gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] completed on
           Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::solver::cg::step_2_operation<gko::matrix::Dense<double>*&,
          gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
gko::matrix::Dense<double>*,
           gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] started on
          Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::solver::cg::step_2_operation<gko::matrix::Dense<double>*&,
           gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
           gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
           gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] completed on
          Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> copy started from Executor[gko::ReferenceExecutor, 0x21400d0] to
           Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x21482f0] with
           Bytes[152]
Bytes[152]
[LOG] »> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
           gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] started on
           Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
          \label{lem:gko::matrix::Dense<double>*>,0x7ffd93d14c50]} completed on \\ \texttt{Executor[gko::ReferenceExecutor,0x21400d0]}
[LOG] >> iteration 4 completed with solver LinOp[gko::solver::Cg<double>,0x2142d60] with residual
           LinOp[gko::matrix::Dense<double>,0x2147b30], solution LinOp[gko::matrix::Dense<double>,0x2143450] and
           residual_norm LinOp[gko::LinOp const*,0]
[LOG] >> check started for stop::Criterion[gko::stop::ResidualNorm<double>,0x2148db0] at iteration 4 with ID
           1 and finalized set to 1
[LOG] »> Operation[gko::matrix::dense::compute_norm2_operation<gko::matrix::Dense<double> const*,
           gko::matrix::Dense<double>*>,0x7ffd93d14ad0] started on Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] »> Operation[gko::matrix::dense::compute_norm2_operation<gko::matrix::Dense<double> const*,
           gko::matrix::Dense<double>*>,0x7ffd93d14ad0] completed on Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::stop::residual_norm::residual_norm_operation<gko::matrix::Dense<double> const*&,
          gko::matrix::Dense<double>*, double&, unsigned char&, bool&, gko::array<gko::stopping_status>*&,
gko::array<bool>*, bool*, bool*&>,0x7ffd93d14b90] started on
          Executor[gko::ReferenceExecutor, 0x21400d0]
[LOG] >> Operation[gko::stop::residual_norm::residual_norm_operation<gko::matrix::Dense<double> const*&,
          gko::matrix::Dense<double>*, double&, unsigned char&, bool&, gko::array<gko::stopping_status>*&,
gko::array<bool>*, bool*, bool*&>,0x7ffd93d14b90] completed on
          Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> check completed for stop::Criterion[gko::stop::ResidualNorm<double>,0x2148db0] at iteration 4 with
ID 1 and finalized set to 1. It changed one RHS 0, stopped the iteration process 0 [LOG] >> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[152]
[LOG] »> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149200] with
          Bytes[152]
[LOG] \gg copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
           \texttt{Executor[gko::ReferenceExecutor,0x21400d0]} \ \ \text{from Location[0x21480a0]} \ \ \text{to Location[0x2149200]} \ \ \text{with loca
          Bytes[152]
```

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[LOG] >> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
           Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x2149200] with
           Bytes[152]
[LOG] >> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[152]
[LOG] >> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149310] with
          Bytes[152]
[LOG] »> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
           Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x2143e90] to Location[0x2149310] with
           Bytes [152]
[LOG] >> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
           Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x2143e90] to Location[0x2149310] with
           Bytes[152]
[LOG] »> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149ae0]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149ae0]
[LOG] >> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149890]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149890]
Executor[gko::ReferenceExecutor, 0x21400d0]
[LOG] >> Operation[gko::solver::cg::step_1_operation<gko::matrix::Dense<double>*,
           gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] completed on
           Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::csr::spmv_operation<gko::matrix::Csr<double, int> const*,
           gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14b80] started on
           Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::csr::spmv_operation<gko::matrix::Csr<double, int> const*,
           gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14b80] completed on
Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
           gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] started on
           Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
          gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] completed on
Executor[gko::ReferenceExecutor,0x21400d0]
gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] started on
           Executor[gko::ReferenceExecutor,0x21400d0]
 [LOG] \  \, \text{"None of the continuous of the c
           gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
gko::matrix::Dense<double>*,
           gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] completed on
           Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
           Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x21482f0] with
           Bytes[152]
[LOG] »> copy completed from Executor[qko::ReferenceExecutor,0x21400d0] to
           Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x21482f0] with
           Bytes[152]
[LOG] \  \  \, \text{"No Operation} \\ [gko::matrix::dense::compute\_dot\_operation \\ \  \  \, \text{"gko::matrix::Dense \\ \  \, \text{double} \\ \  \  \, \text{const} \\ \  \  \, \text{"const} 
          gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] started on
Executor[gko::ReferenceExecutor,0x21400d0]
Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> iteration 5 completed with solver LinOp[gko::solver::Cg<double>,0x2142d60] with residual
           LinOp[gko::matrix::Dense<double>,0x2147b30], solution LinOp[gko::matrix::Dense<double>,0x2143450] and
           residual_norm LinOp[gko::LinOp const*,0]
[LOG] >> check started for stop::Criterion[gko::stop::ResidualNorm<double>,0x2148db0] at iteration 5 with ID
           1 and finalized set to 1
[LOG] >> Operation[gko::matrix::dense::compute_norm2_operation<gko::matrix::Dense<double> const*,
           gko::matrix::Dense<double>*>,0x7ffd93d14ad0] started on Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_norm2_operation<gko::matrix::Dense<double> const*,
           gko::matrix::Dense<double>*>,0x7ffd93d14ad0] completed on Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] »> Operation[gko::stop::residual_norm::residual_norm_operation<gko::matrix::Dense<double> const*&,
           gko::matrix::Dense<double>*, double&, unsigned char&, bool&, gko::array<gko::stopping_status>*&,
           gko::array<bool>*, bool*, bool*&>,0x7ffd93d14b90] started on
           Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::stop::residual_norm::residual_norm_operation<gko::matrix::Dense<double> const*&,
          gko::matrix::Dense<double>*, double&, unsigned char&, bool&, gko::array<gko::stopping_status>*&,
gko::array<bool>*, bool*, bool*&>,0x7ffd93d14b90] completed on
Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] »> check completed for stop::Criterion[gko::stop::ResidualNorm<double>,0x2148db0] at iteration 5 with
           ID 1 and finalized set to 1. It changed one RHS 0, stopped the iteration process 0
[LOG] »> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[152]
[LOG] >> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149890] with
           Bytes[152]
[LOG] >> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
           Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x2149890] with
           Bytes[152]
[LOG] »> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
           \textbf{Executor}[\textbf{gko}:: \textbf{ReferenceExecutor}, \textbf{0x} \textbf{21400d0}] \text{ from Location}[\textbf{0x} \textbf{21480a0}] \text{ to Location}[\textbf{0x} \textbf{2149890}] \text{ with } \textbf{0x} \textbf{21490d0}]
           Bytes[152]
[LOG] »> allocation started on Executor[gko::ReferenceExecutor.0x21400d0] with Bytes[152]
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[LOG] >> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149cc0] with
      Bytes[152]
[LOG] »> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
     Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x2143e90] to Location[0x2149cc0] with
     Bytes[152]
[LOG] »> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
     Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x2143e90] to Location[0x2149cc0] with
      Bytes [152]
[LOG] >> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149310]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149310]
[LOG] >> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149200]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149200]
[LOG] >> Operation[gko::solver::cg::step_1_operation<gko::matrix::Dense<double>*,
      gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
      gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] started on
      Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::solver::cg::step_1_operation<gko::matrix::Dense<double>*,
     gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
gko::matrix::Dense<double>*,
gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] completed on
      Executor[gko::ReferenceExecutor, 0x21400d0]
[LOG] >> Operation[gko::matrix::csr::spmv_operation<gko::matrix::Csr<double, int> const*,
     gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14b80] started on
Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::csr::spmv_operation<gko::matrix::Csr<double, int> const*,
      gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14b80] completed on
      Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
      gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] started on
     Executor[gko::ReferenceExecutor, 0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
      gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] completed on
     Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::solver::cg::step_2_operation<gko::matrix::Dense<double>*&,
      gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
      gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
      gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] started on
     Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::solver::cg::step_2_operation<gko::matrix::Dense<double>*&,
     gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
      gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
      gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] completed on
     Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] \gg copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
      Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x21482f0] with
     Bytes[152]
[LOG] »> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
     Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x21482f0] with
     Bytes[152]
[LOG] \hspace*{0.2cm} \text{"NOS} \hspace*{0.2cm} \texttt{Operation[gko::matrix::dense::compute\_dot\_operation < gko::matrix::Dense < double > const*,} \\
      gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c501 started on
      Executor[gko::ReferenceExecutor, 0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
      gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] completed on
      Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> iteration 6 completed with solver LinOp[gko::solver::Cg<double>,0x2142d60] with residual
      LinOp[gko::matrix::Dense<double>,0x2147b30], solution LinOp[gko::matrix::Dense<double>,0x2143450] and
      residual_norm LinOp[gko::LinOp const*,0]
[LOG] »> check started for stop::Criterion[gko::stop::ResidualNorm<double>,0x2148db0] at iteration 6 with ID
      1 and finalized set to 1
[LOG] >> Operation[gko::matrix::dense::compute_norm2_operation<gko::matrix::Dense<double> const*
      gko::matrix::Dense<double>*>,0x7ffd93d14ad0] started on Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_norm2_operation<gko::matrix::Dense<double> const*,
      gko::matrix::Dense<double>*>,0x7ffd93d14ad0] completed on Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::stop::residual_norm::residual_norm_operation<gko::matrix::Dense<double> const*&,
      gko::matrix::Dense<double>*, double&, unsigned char&, bool&, gko::array<gko::stopping_status>*&,
      gko::array<bool>*, bool*, bool*&>,0x7ffd93d14b90] started on
     Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::stop::residual_norm::residual_norm_operation<gko::matrix::Dense<double> const*&,
     qko::matrix::Dense<double>*, double&, unsigned char&, bool&, qko::array<qko::stopping_status>*&,
      gko::array<bool>*, bool*, bool*&>,0x7ffd93d14b90] completed on
      Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] »> check completed for stop::Criterion[gko::stop::ResidualNorm<double>,0x2148db0] at iteration 6 with
     ID 1 and finalized set to 1. It changed one RHS 0, stopped the iteration process 0 \,
[LOG] »> allocation started on Executor[gko::ReferenceExecutor, 0x21400d0] with Bytes[152]
[LOG] >> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149450] with
     Bytes[152]
[LOG] >> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
     Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x2149450] with
     Bytes[152]
[LOG] >> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
     Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x2149450] with
     Bytes [152]
[LOG] >> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[152]
[LOG] »> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x21494f0] with
     Bytes[152]
[LOG] >> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
     Executor[gko::ReferenceExecutor, 0x21400d0] from Location[0x2143e90] to Location[0x21494f0] with
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Bytes[152]
[LOG] »> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
         Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x2143e90] to Location[0x21494f0] with
         Bytes[152]
[LOG] »> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149cc0]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149cc0]
[LOG] >> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149890]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149890]
[LOG] >> Operation[gko::solver::cg::step_1_operation<gko::matrix::Dense<double>*,
         gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] started on
         Executor[gko::ReferenceExecutor, 0x21400d0]
[LOG] >> Operation[gko::solver::cg::step_1_operation<gko::matrix::Dense<double>*,
         gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
         gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] completed on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::csr::spmv_operation<gko::matrix::Csr<double, int> const*,
         gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14b80] started on Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::csr::spmv_operation<gko::matrix::Csr<double, int> const*,
         gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14b80] completed on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
         gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] started on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
         gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] completed on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::solver::cg::step_2_operation<gko::matrix::Dense<double>*&,
        gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
gko::matrix::Dense<double>*,
         gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] started on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::solver::cg::step_2_operation<gko::matrix::Dense<double>*&,
         gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
gko::matrix::Dense<double>*,
gko::matrix::Dense<double>*,
gko::matrix::Dense<double>*,
gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] completed on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
         Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x21482f0] with
         Bytes[152]
[LOG] >> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x21482f0] with
         Bytes[152]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
         gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] started on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
        gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] completed on
Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> iteration 7 completed with solver LinOp[gko::solver::Cg<double>,0x2142d60] with residual
         LinOp[gko::matrix::Dense<double>,0x2147b30], solution LinOp[gko::matrix::Dense<double>,0x2143450] and
         residual_norm LinOp[gko::LinOp const*,0]
[LOG] »> check started for stop::Criterion[gko::stop::ResidualNorm<double>,0x2148db0] at iteration 7 with ID 1 and finalized set to 1
[LOG] >> Operation[gko::matrix::dense::compute norm2 operation<gko::matrix::Dense<double> const*
         gko::matrix::Dense<double>*>,0x7ffd93d14ad0] started on Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] »> Operation[gko::matrix::dense::compute_norm2_operation<gko::matrix::Dense<double> const*,
         gko::matrix::Dense<double>*>,0x7ffd93d14ad0] completed on Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::stop::residual_norm::residual_norm_operation<gko::matrix::Dense<double> const*&,
         gko::matrix::Dense<double>*, double&, unsigned char&, bool&, gko::array<gko::stopping_status>*&, gko::array<br/>bool>*, bool*&, 0x7ffd93d14b90] started on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::stop::residual_norm::residual_norm_operation<gko::matrix::Dense<double> const*&,
         gko::matrix::Dense<double>*, double&, unsigned char&, bool&, gko::array<gko::stopping_status>*&,
         gko::array<bool>*, bool*, bool*&>,0x7ffd93d14b90] completed on
         Executor[gko::ReferenceExecutor, 0x21400d0]
[LOG] >> check completed for stop::Criterion[gko::stop::ResidualNorm<double>.0x2148db0] at iteration 7 with
         ID 1 and finalized set to 1. It changed one RHS 0, stopped the iteration process 0
[LOG] >> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[152]
[LOG] »> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149730] with
         Bytes[152]
[LOG] »> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x2149730] with
         Bytes[152]
[LOG] »> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
         Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x2149730] with
         Bytes[152]
[LOG] \  \, \text{">"} \  \, \text{allocation started on Executor} \\ [gko::ReferenceExecutor,0x21400d0] \  \, \text{with Bytes} \\ [152] \  \, \text{(152)} \\ [152] \  \, \text{(1
[LOG] »> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x21497d0] with
         Bytes[152]
[LOG] »> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
         Executor[gko::ReferenceExecutor, 0x21400d0] from Location[0x2143e90] to Location[0x21497d0] with
         Bytes[152]
[LOG] \gg copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
         Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x2143e90] to Location[0x21497d0] with
         Bytes[152]
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[LOG] >> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x21494f0]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x21494f0]
[LOG] >> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149450]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149450]
[LOG] >> Operation[gko::solver::cg::step_1_operation<gko::matrix::Dense<double>*,
         gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] started on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::solver::cg::step_1_operation<gko::matrix::Dense<double>*,
         gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] completed on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::csr::spmv operation<gko::matrix::Csr<double, int> const*,
         gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14b80] started on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::csr::spmv_operation<gko::matrix::Csr<double, int> const*,
          qko::matrix::Dense<double> const*, qko::matrix::Dense<double>*>,0x7ffd93d14b80] completed on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
         gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] started on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
         gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] completed on
         Executor[gko::ReferenceExecutor, 0x21400d0]
[LOG] >> Operation[gko::solver::cg::step_2_operation<gko::matrix::Dense<double>*&,
         gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
         gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
         gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] started on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] \begin{tabular}{l} \verb|MOG| >> Operation[gko::solver::cg::step_2_operation < gko::matrix::Dense < double > * \&, figure = fi
         gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
gko::matrix::Dense<double>*,
         gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] completed on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] \gg copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
         Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x21482f0] with
         Bytes[152]
[LOG] »> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
         Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x21482f0] with
         Bytes[152]
[LOG] » Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
         gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] started on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
         gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] completed on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> iteration 8 completed with solver LinOp[gko::solver::Cg<double>,0x2142d60] with residual
         LinOp[gko::matrix::Dense<double>,0x2147b30], solution LinOp[gko::matrix::Dense<double>,0x2143450] and
         residual_norm LinOp[gko::LinOp const*,0]
[LOG] >> check started for stop::Criterion[gko::stop::ResidualNorm<double>,0x2148db0] at iteration 8 with ID
         1 and finalized set to 1
[LOG] >> Operation[gko::matrix::dense::compute_norm2_operation<gko::matrix::Dense<double> const*,
          gko::matrix::Dense<double>*>,0x7ffd93d14ad0] started on Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_norm2_operation<gko::matrix::Dense<double> const*,
         gko::matrix::Dense<double>*>,0x7ffd93d14ad0] completed on Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::stop::residual_norm::residual_norm_operation<gko::matrix::Dense<double> const*&,
         gko::matrix::Dense<double>*, double&, unsigned char&, bool&, gko::array<gko::stopping_status>*&,
         gko::array<bool>*, bool*, bool*&>,0x7ffd93d14b90] started on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::stop::residual_norm::residual_norm_operation<gko::matrix::Dense<double> const*&,
         gko::matrix::Dense<double>*, double&, unsigned char&, bool&, gko::array<gko::stopping\_status>*&, gko::array<br/>bool>*, bool*&, 0x7ffd93d14b90] completed on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> check completed for stop::Criterion[gko::stop::ResidualNorm<double>,0x2148db0] at iteration 8 with
         ID 1 and finalized set to \hat{1}. It changed one RHS \hat{0}, stopped the iteration process \hat{0}
[LOG] >> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[152]
[LOG] \gg allocation \ completed \ on \ Executor[gko::ReferenceExecutor,0x21400d0] \ at \ Location[0x2149200] \ with \ constant \ co
         Bytes[152]
[LOG] >> copy started from Executor[gko::ReferenceExecutor.0x21400d0] to
         Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x2149200] with
         Bytes[152]
[LOG] >> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
         Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x2149200] with
         Bytes[152]
[LOG] >> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[152]
[LOG] »> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x21492a0] with
         Bytes[152]
[LOG] »> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
         Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x2143e90] to Location[0x21492a0] with
         Bytes[152]
[LOG] »> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
         Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x2143e90] to Location[0x21492a0] with
         Bytes[152]
[LOG] »> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x21497d0]
[LOG] >> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x21497d0]
[LOG] >> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149730]
[LOG] >> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149730]
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[LOG] >> Operation[gko::solver::cg::step_1_operation<gko::matrix::Dense<double>*,
      gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
      gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] started on
      Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::solver::cg::step_1_operation<gko::matrix::Dense<double>*,
      gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
gko::matrix::Dense<double>*,
gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] completed on
      Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::csr::spmv_operation<gko::matrix::Csr<double, int> const*,
      gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14b80] started on
Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::csr::spmv_operation<gko::matrix::Csr<double, int> const*,
      gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14b80] completed on
      Executor[gko::ReferenceExecutor, 0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*
      gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] started on
      Executor[gko::ReferenceExecutor, 0x21400d0]
Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::solver::cg::step_2_operation<gko::matrix::Dense<double>*&,
      gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
      gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] started on
      Executor[gko::ReferenceExecutor, 0x21400d0]
[LOG] >> Operation[gko::solver::cg::step_2_operation<gko::matrix::Dense<double>*&,
      gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
      gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
      gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] completed on
      Executor[gko::ReferenceExecutor, 0x21400d0]
[LOG] >> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
      Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x21482f0] with
      Bytes[152]
[LOG] >> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
      Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x21482f0] with
      Bytes [152]
Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
      gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] completed on
Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] »> iteration 9 completed with solver LinOp[gko::solver::Cg<double>,0x2142d60] with residual
    LinOp[gko::matrix::Dense<double>,0x2147b30], solution LinOp[gko::matrix::Dense<double>,0x2143450] and
      residual_norm LinOp[gko::LinOp const*,0]
[LOG]
      »> check started for stop::Criterion[gko::stop::ResidualNorm<double>,0x2148db0] at iteration 9 with ID
      1 and finalized set to 1
[LOG] >> Operation[gko::matrix::dense::compute_norm2_operation<gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14ad0] started on Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] »> Operation[gko::matrix::dense::compute_norm2_operation<gko::matrix::Dense<double> const*,
      gko::matrix::Dense<double>*>,0x7ffd93d14ad0] completed on Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] »> Operation[gko::stop::residual_norm::residual_norm_operation<gko::matrix::Dense<double> const*&,
      gko::matrix::Dense<double>*, double&, unsigned char&, bool&, gko::array<gko::stopping_status>*&,
gko::array<bool>*, bool*, bool*&>,0x7ffd93d14b90] started on
      Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::stop::residual_norm::residual_norm_operation<gko::matrix::Dense<double> const*&,
      gko::matrix::Dense<double>*, double&, unsigned char&, bool&, gko::array<gko::stopping_status>*&,
      gko::array<bool>*, bool*, bool*&>,0x7ffd93d14b90] completed on
      Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> check completed for stop::Criterion[gko::stop::ResidualNorm<double>,0x2148db0] at iteration 9 with
ID 1 and finalized set to 1. It changed one RHS 0, stopped the iteration process 0 [LOG] »> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[152]
[LOG] »> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149620] with
      Bytes[152]
[LOG] »> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
      \textbf{Executor}[\textbf{gko}:: \textbf{ReferenceExecutor}, \textbf{0x} \textbf{21400d0}] \text{ from Location}[\textbf{0x} \textbf{21480a0}] \text{ to Location}[\textbf{0x} \textbf{2149620}] \text{ with } \textbf{0x} \textbf{21490a0}]
      Bytes[152]
[LOG] »> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
      Executor[gko::ReferenceExecutor, 0x21400d0] from Location[0x21480a0] to Location[0x2149620] with
      Bytes[152]
[LOG] »> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[152]
[LOG] >> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x21496c0] with
      Bytes[152]
[LOG] >> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
      Executor[gko::ReferenceExecutor, 0x21400d0] from Location[0x2143e90] to Location[0x21496c0] with
      Bytes[152]
[LOG] >> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
      Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x2143e90] to Location[0x21496c0] with
      Bytes[152]
[LOG] »> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x21492a0]
[LOG] >> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x21492a0]
[LOG] »> free started on Executor[gko::ReferenceExecutor, 0x21400d0] at Location[0x2149200]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149200]
[LOG] >> Operation[gko::solver::cg::step_1_operation<gko::matrix::Dense<double>*,
      gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
      gko::array<gko::stopping status>*>,0x7ffd93d14ef0] started on
      Executor[qko::ReferenceExecutor,0x21400d0]
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[LOG] >> Operation[gko::solver::cq::step_1_operation<gko::matrix::Dense<double>*,
        gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
        gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] completed on
        Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::csr::spmv_operation<gko::matrix::Csr<double, int> const*,
        gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14b801 started on
        Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::csr::spmv_operation<gko::matrix::Csr<double, int> const*,
        gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14b80] completed on
        Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
        gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c501 started on
        Executor[gko::ReferenceExecutor, 0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
        gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] completed on
        Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::solver::cg::step_2_operation<gko::matrix::Dense<double>*&,
       gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
gko::matrix::Dense<double>*,
        gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] started on
        Executor[gko::ReferenceExecutor, 0x21400d0]
 [LOG] \  \, \hbox{$\tt w$-} \  \, {\tt Operation[gko::solver::cg::step\_2\_operation$< gko::matrix::Dense$< double>*&, } \\
       gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
gko::matrix::Dense<double>*,
        gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] completed on
        Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
        Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x21482f0] with
        Bytes[152]
[LOG] »> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
        Executor[gko::ReferenceExecutor.0x21400d0] from Location[0x21480a0] to Location[0x21482f0] with
        Bytes[152]
[LOG] » Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*
        gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] started on
        Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
        gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] completed on
        Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> iteration 10 completed with solver LinOp[gko::solver::Cg<double>,0x2142d60] with residual
        LinOp[gko::matrix::Dense<double>,0x2147b30], solution LinOp[gko::matrix::Dense<double>,0x2143450] and
        residual_norm LinOp[gko::LinOp const*,0]
[LOG] »> check started for stop::Criterion[gko::stop::ResidualNorm<double>,0x2148db0] at iteration 10 with ID 1 and finalized set to 1
[LOG] >> Operation[gko::matrix::dense::compute_norm2_operation<gko::matrix::Dense<double> const*,
        gko::matrix::Dense<double>*>,0x7ffd93d14ad0] started on Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] »> Operation[gko::matrix::dense::compute_norm2_operation<gko::matrix::Dense<double> const*,
        gko::matrix::Dense<double>*>,0x7ffd93d14ad0] completed on Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] \gg Operation[gko::stop::residual_norm::residual_norm_operation < gko::matrix::Dense < double > const*\&, figure = 
        gko::matrix::Dense<double>*, double&, unsigned char&, bool&, gko::array<gko::stopping_status>*&,
qko::array<bool>*, bool*, bool*&>,0x7ffd93d14b90] started on
        Executor[gko::ReferenceExecutor, 0x21400d0]
[LOG] >> Operation[gko::stop::residual_norm::residual_norm_operation<gko::matrix::Dense<double> const*&,
        gko::matrix::Dense<double>*, double&, unsigned char&, bool&, gko::array<gko::stopping_status>*&,
        gko::array<bool>*, bool*, bool*&>,0x7ffd93d14b90] completed on
        Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> check completed for stop::Criterion[gko::stop::ResidualNorm<double>,0x2148db0] at iteration 10 with
        ID 1 and finalized set to 1. It changed one RHS 0, stopped the iteration process 0
[LOG] >> allocation started on Executor[gko::ReferenceExecutor, 0x21400d0] with Bytes[152]
[LOG] »> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149450] with
       Bytes[152]
[LOG] >> copy started from Executor[gko::ReferenceExecutor, 0x21400d0] to
        Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x2149450] with
        Bytes[152]
[LOG] >> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
        Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x2149450] with
        Bytes[152]
[LOG] >> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[152]
[LOG] »> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149760] with
       Bytes[152]
[LOG] »> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
        Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x2143e90] to Location[0x2149760] with
        Bytes[152]
[LOG] \gg copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
        Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x2143e90] to Location[0x2149760] with
        Bytes[152]
[LOG] »> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x21496c0]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x21496c0]
[LOG] >> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149620]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149620]
\texttt{[LOG] w> Operation[gko::solver::cg::step\_1\_operation < gko::matrix::Dense < double > \star,}
        gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
        gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] started on
        Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::solver::cg::step_1_operation<gko::matrix::Dense<double>*,
        gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
        gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] completed on
        Executor[gko::ReferenceExecutor,0x21400d0]
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[LOG] >> Operation[gko::matrix::csr::spmv_operation<gko::matrix::Csr<double, int> const*,
      gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14b80] started on
      Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::csr::spmv_operation<gko::matrix::Csr<double, int> const*,
      qko::matrix::Dense<double> const*, qko::matrix::Dense<double>*>,0x7ffd93d14b80] completed on
      Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
      gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] started on
      Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
      gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] completed on
Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::solver::cg::step_2_operation<gko::matrix::Dense<double>*&,
      gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
      gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
      gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] started on
      Executor[gko::ReferenceExecutor,0x21400d0]
gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
      gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] completed on
      Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
      Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x21482f0] with
      Bytes [152]
[LOG] »> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
      Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x21482f0] with
      Bytes[152]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
      gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] started on
Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
      gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] completed on
      Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] »> iteration 11 completed with solver LinOp[gko::solver::Cg<double>,0x2142d60] with residual LinOp[gko::matrix::Dense<double>,0x2147b30], solution LinOp[gko::matrix::Dense<double>,0x2143450] and
      residual_norm LinOp[gko::LinOp const*,0]
[LOG] >> check started for stop::Criterion[gko::stop::ResidualNorm<double>,0x2148db0] at iteration 11 with
      ID 1 and finalized set to 1
[LOG] >> Operation[gko::matrix::dense::compute_norm2_operation<gko::matrix::Dense<double> const*,
      gko::matrix::Dense<double>*>,0x7ffd93d14ad0] started on Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_norm2_operation<gko::matrix::Dense<double> const*,
      qko::matrix::Dense<double>*>,0x7ffd93d14ad0] completed on Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] »> Operation[gko::stop::residual_norm::residual_norm_operation<gko::matrix::Dense<double> const*&,
      gko::matrix::Dense<double>*, double&, unsigned char&, bool&, gko::array<gko::stopping_status>*&,
      gko::array<bool>*, bool*, bool*&>,0x7ffd93d14b90] started on
      Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::stop::residual_norm::residual_norm_operation<gko::matrix::Dense<double> const*&,
      gko::matrix::Dense<double>*, double&, unsigned char&, bool&, gko::array<gko::stopping_status>*&,
gko::array<bool>*, bool*, bool*&>,0x7ffd93d14b90] completed on
      Executor[gko::ReferenceExecutor, 0x21400d0]
[LOG] >> check completed for stop::Criterion[gko::stop::ResidualNorm<double>,0x2148db0] at iteration 11 with
      ID 1 and finalized set to 1. It changed one RHS 0, stopped the iteration process 0 \,
[LOG] >> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[152] [LOG] >> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149860] with
      Bytes[152]
[LOG] »> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
      Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x2149860] with
      Bytes[152]
[LOG] \gg copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
      Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x2149860] with
      Bytes[152]
[LOG] »> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[152]
[LOG] »> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149900] with
[LOG] \gg copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
      Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x2143e90] to Location[0x2149900] with
      Bytes[152]
[LOG] »> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
      Executor[gko::ReferenceExecutor, 0x21400d0] from Location[0x2143e90] to Location[0x2149900] with
      Bytes [152]
[LOG] >> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149760]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149760]
[LOG] >> free started on Executor[gko::ReferenceExecutor, 0x21400d0] at Location[0x2149450]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149450]
[LOG] »> Operation[gko::solver::cg::step_1_operation<gko::matrix::Dense<double>*,
      gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
      gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] started on
      Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::solver::cg::step_1_operation<gko::matrix::Dense<double>*,
      gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
      Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::csr::spmv_operation<gko::matrix::Csr<double, int> const*,
      gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14b80] started on
      Executor[gko::ReferenceExecutor, 0x21400d0]
[LOG] >> Operation[gko::matrix::csr::spmv_operation<gko::matrix::Csr<double, int> const*,
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gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14b80] completed on
          Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
          \verb|gko::matrix::Dense<| double>| const*, gko::matrix::Dense<| double>*>,0x7ffd93d14c50| started on the constant of the consta
         Executor[gko::ReferenceExecutor, 0x21400d0]
[LOG] »> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
          gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] completed on
          Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::solver::cg::step_2_operation<gko::matrix::Dense<double>*&,
          gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
          gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
          gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] started on
         Executor[gko::ReferenceExecutor, 0x21400d0]
[LOG] >> Operation[gko::solver::cg::step_2_operation<gko::matrix::Dense<double>*&,
          gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
          gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
          gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] completed on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
          Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x21482f0] with
         Bytes[152]
[LOG] »> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
         Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x21482f0] with
         Bytes[152]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
          gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] started on
          Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
          gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] completed on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> iteration 12 completed with solver LinOp[gko::solver::Cg<double>,0x2142d60] with residual
          LinOp[gko::matrix::Dense<double>,0x2147b30], solution LinOp[gko::matrix::Dense<double>,0x2143450] and
          residual_norm LinOp[gko::LinOp const*,0]
[LOG] »> check started for stop::Criterion[gko::stop::ResidualNorm<double>,0x2148db0] at iteration 12 with
          {\tt ID}\ {\tt 1} and finalized set to 1
[LOG] >> Operation[gko::matrix::dense::compute_norm2_operation<gko::matrix::Dense<double> const*
          gko::matrix::Dense<double>*>,0x7ffd93d14ad0] started on Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] »> Operation[gko::matrix::dense::compute_norm2_operation<gko::matrix::Dense<double> const*,
          gko::matrix::Dense<double>*>,0x7ffd93d14ad0] completed on Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::stop::residual_norm::residual_norm_operation<gko::matrix::Dense<double> const*&,
         gko::matrix::Dense<double>*, double&, unsigned char&, bool&, gko::array<gko::stopping_status>*&,
gko::array<bool>*, bool*, bool*&>,0x7ffd93d14b90] started on
         Executor[qko::ReferenceExecutor, 0x21400d0]
[LOG] >> Operation[gko::stop::residual_norm::residual_norm_operation<gko::matrix::Dense<double> const*&,
         gko::matrix::Dense<double>*, double&, unsigned char&, bool&, gko::array<gko::stopping_status>*&,
          gko::array<bool>*, bool*, bool*&>,0x7ffd93d14b90] completed on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> check completed for stop::Criterion[gko::stop::ResidualNorm<double>,0x2148db0] at iteration 12 with
ID 1 and finalized set to 1. It changed one RHS 0, stopped the iteration process 0 [LOG] >> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[152]
[LOG] »> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x21499a0] with
         Bytes[152]
[LOG] >> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
         Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x21499a0] with
         Bytes[152]
[LOG] >> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
          Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x21499a0] with
[LOG] » allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[152]
[LOG] »> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x21493d0] with
         Bytes[152]
[LOG] >> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
          Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x2143e90] to Location[0x21493d0] with
[LOG] »> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
         Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x2143e90] to Location[0x21493d0] with
         Bytes[152]
[LOG] »> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149900]
[LOG] >> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149900]
[LOG] >> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149860]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149860]
[LOG] >> Operation[gko::solver::cg::step_1_operation<gko::matrix::Dense<double>*,
         gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] started on
         Executor[gko::ReferenceExecutor, 0x21400d0]
[LOG] >> Operation[gko::solver::cg::step_1_operation<gko::matrix::Dense<double>*,
          gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
          gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] completed on
          Executor[gko::ReferenceExecutor, 0x21400d0]
[LOG] \begin{tabular}{l} \verb|MOG| >> Operation[gko::matrix::csr::spmv\_operation < gko::matrix::Csr < double, int > const *, for the const *, f
          gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14b80] started on
          Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::csr::spmv_operation<gko::matrix::Csr<double, int> const*,
          gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14b80] completed on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
          gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] started on
```

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Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
        gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] completed on
        Executor[gko::ReferenceExecutor,0x21400d0]
gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] started on
        Executor[gko::ReferenceExecutor, 0x21400d0]
[LOG] >> Operation[gko::solver::cg::step_2_operation<gko::matrix::Dense<double>*&,
        gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
gko::matrix::Dense<double>*,
        gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] completed on
        Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
        Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x21482f0] with
        Bytes [152]
[LOG] >> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
        Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x21482f0] with
        Bvtes[152]
[LOG] »> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
        gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] started on
        Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*, gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] completed on
        Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> iteration 13 completed with solver LinOp[gko::solver::Cg<double>,0x2142d60] with residual
        LinOp[gko::matrix::Dense<double>,0x2147b30], solution LinOp[gko::matrix::Dense<double>,0x2143450] and
        residual_norm LinOp[gko::LinOp const*,0]
[LOG] \ \textit{""> check started for stop::Criterion[gko::stop::ResidualNorm<double>,0x2148db0] \ \textit{at iteration 13 with 1.5} \ \textit{""> check started for stop::Criterion[gko::stop::ResidualNorm<double>,0x2148db0] \ \textit{"at iteration 13 with 1.5} \ \textit{"> check started for stop::Criterion[gko::stop::ResidualNorm<double>,0x2148db0] \ \textit{"> check stop::Criterion[gko::stop::ResidualNorm<double>,0x2148db0] \ \textit{"> check stop::Criterion[gko::stop::ResidualNorm] \ \textit{"> check stop::Criterion[gko::stop::ResidualNorm] \ \textit{"> check stop::Criterion[gk
        ID 1 and finalized set to 1
[LOG] >> Operation[gko::matrix::dense::compute_norm2_operation<gko::matrix::Dense<double> const*.
        gko::matrix::Dense<double>*>,0x7ffd93d14ad0] started on Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_norm2_operation<gko::matrix::Dense<double> const*,
        gko::matrix::Dense<double>*>,0x7ffd93d14ad0] completed on Executor[gko::ReferenceExecutor,0x21400d0]
Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::stop::residual_norm::residual_norm_operation<gko::matrix::Dense<double> const*&,
        gko::matrix::Dense<double>*, double&, unsigned char&, bool&, gko::array<gko::stopping_status>*&,
gko::array<bool>*, bool*, bool*&>,0x7ffd93d14b90] completed on
        Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] »> check completed for stop::Criterion[gko::stop::ResidualNorm<double>,0x2148db0] at iteration 13 with
        ID 1 and finalized set to 1. It changed one RHS 0, stopped the iteration process 0
[LOG] >> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[152]
[LOG] »> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149490] with
        Bytes[152]
[LOG] >> copy started from Executor[gko::ReferenceExecutor, 0x21400d0] to
        Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x2149490] with
        Bytes[152]
[LOG] »> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
        Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x2149490] with
        Bytes[152]
[LOG] >> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[152]
[LOG] »> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149580] with
        Bytes[152]
[LOG] >> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
        Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x2143e90] to Location[0x2149580] with
        Bytes[152]
[LOG] \gg copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
        Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x2143e90] to Location[0x2149580] with
        Bytes[152]
[LOG] »> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x21493d0]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x21493d0]
[LOG] >> free started on Executor[gko::ReferenceExecutor, 0x21400d0] at Location[0x21499a0]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x21499a0]
[LOG] >> Operation[gko::solver::cg::step_1_operation<gko::matrix::Dense<double>*,
        qko::matrix::Dense<double>*, qko::matrix::Dense<double>*, qko::matrix::Dense<double>*,
        gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] started on
        Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::solver::cg::step_1_operation<gko::matrix::Dense<double>*,
        gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] completed on
        Executor[gko::ReferenceExecutor, 0x21400d0]
[LOG] >> Operation[gko::matrix::csr::spmv_operation<gko::matrix::Csr<double, int> const*,
        gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14b80] started on
        Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::csr::spmv_operation<gko::matrix::Csr<double, int> const*,
        gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14b80] completed on
Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
        gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] started on
        Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
        gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] completed on
Executor[gko::ReferenceExecutor,0x21400d0]
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[LOG] >> Operation[gko::solver::cg::step_2_operation<gko::matrix::Dense<double>*&,
             gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
gko::matrix::Dense<double>*,
             gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] started on
             Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::solver::cg::step 2 operation<gko::matrix::Dense<double>*&.
             gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
             gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
             gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] completed on
             Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] \gg copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
             Executor[gko::ReferenceExecutor, 0x21400d0] from Location[0x21480a0] to Location[0x21482f0] with
             Bytes[152]
[LOG] »> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
             Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x21482f0] with
             Bytes[152]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
             gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] started on
Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
             gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] completed on
             Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> iteration 14 completed with solver LinOp[gko::solver::Cg<double>,0x2142d60] with residual
             \label{linOp} \texttt{LinOp[gko::matrix::Dense<double>,0x2147b30], solution LinOp[gko::matrix::Dense<double>,0x2143450] and the line of the li
             residual_norm LinOp[gko::LinOp const*,0]
[LOG] >> check started for stop::Criterion[gko::stop::ResidualNorm<double>,0x2148db0] at iteration 14 with
             ID 1 and finalized set to 1
[LOG] >> Operation[gko::matrix::dense::compute_norm2_operation<gko::matrix::Dense<double> const*
              gko::matrix::Dense<double>*>,0x7ffd93d14ad0] started on Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_norm2_operation<gko::matrix::Dense<double> const*,
             gko::matrix::Dense<double>*>,0x7ffd93d14ad0] completed on Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] »> Operation[gko::stop::residual_norm::residual_norm_operation<gko::matrix::Dense<double> const*&,
             gko::matrix::Dense<double>*, double&, unsigned char&, bool&, gko::array<gko::stopping_status>*&,
             gko::array<bool>*, bool*, bool*&>,0x7ffd93d14b90] started on
             Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::stop::residual_norm::residual_norm_operation<gko::matrix::Dense<double> const*&,
            gko::matrix::Dense<double>*, double&, unsigned char&, bool&, gko::array<gko::stopping_status>*&,
gko::array<bool>*, bool*, bool*&>,0x7ffd93d14b90] completed on
             Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> check completed for stop::Criterion[gko::stop::ResidualNorm<double>,0x2148db0] at iteration 14 with
             ID 1 and finalized set to 1. It changed one RHS 0, stopped the iteration process 0
[LOG] >> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[152]
[LOG] »> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149b50] with
             Bytes[152]
[LOG] >> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
             Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x2149b50] with
             Bytes [152]
[LOG] \gg copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
             Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x2149b50] with
             Bvtes[152]
[LOG] >> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[152]
[LOG] »> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x21499c0] with
             Bytes[152]
[LOG] >> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
             \textbf{Executor}[\textbf{gko}:: \textbf{ReferenceExecutor}, \textbf{0x21400d0}] \text{ from Location}[\textbf{0x2143e90}] \text{ to Location}[\textbf{0x21499c0}] \text{ with } \textbf{0x2149e0} \textbf{0x214e0} \textbf
             Bytes[152]
[LOG] »> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
             Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x2143e90] to Location[0x21499c0] with
             Bytes[152]
[LOG] >> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149580]
[LOG] »> free completed on Executor[gko::ReferenceExecutor, 0x21400d0] at Location[0x2149580]
[LOG] >> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149490]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149490]
[LOG] >> Operation[gko::solver::cg::step_1_operation<gko::matrix::Dense<double>*,
             gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
             gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] started on
             Executor[gko::ReferenceExecutor, 0x21400d0]
 [LOG] \begin{tabular}{l} \verb|MOG| & \verb|
             qko::matrix::Dense<double>*, qko::matrix::Dense<double>*, qko::matrix::Dense<double>*,
             gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] completed on
             Executor[gko::ReferenceExecutor, 0x21400d0]
[LOG] >> Operation[gko::matrix::csr::spmv_operation<gko::matrix::Csr<double, int> const*,
            gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14b80] started on
Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::csr::spmv_operation<gko::matrix::Csr<double, int> const*,
             gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14b80] completed on
             Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
              gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] started on
             Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
             gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] completed on
             Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::solver::cg::step_2_operation<gko::matrix::Dense<double>*&,
             gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
             gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
             gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] started on
```

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Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::solver::cg::step_2_operation<gko::matrix::Dense<double>*&,
          gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
          gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
          gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] completed on
          Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] »> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
          Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x21482f0] with
          Bytes[152]
[LOG] \gg copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
          Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x21482f0] with
          Bvtes[152]
[LOG] »> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
          gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] started on
          Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
           gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] completed on
          Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> iteration 15 completed with solver LinOp[gko::solver::Cg<double>,0x2142d60] with residual
          LinOp[gko::matrix::Dense<double>,0x2147b30], solution LinOp[gko::matrix::Dense<double>,0x2143450] and
          residual_norm LinOp[gko::LinOp const*,0]
[LOG] >> check started for stop::Criterion[gko::stop::ResidualNorm<double>,0x2148db0] at iteration 15 with
          ID 1 and finalized set to 1 \,
[LOG] >> Operation[gko::matrix::dense::compute_norm2_operation<gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14ad0] started on Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] »> Operation[gko::matrix::dense::compute_norm2_operation<gko::matrix::Dense<double> const*,
          gko::matrix::Dense<double>*>,0x7ffd93d14ad0] completed on Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::stop::residual_norm::residual_norm_operation<gko::matrix::Dense<double> const*&,
          gko::matrix::Dense<double>*, double&, unsigned char&, bool&, gko::array<gko::stopping_status>*&,
gko::array<bool>*, bool*, bool*&>,0x7ffd93d14b90] started on
          Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::stop::residual_norm::residual_norm_operation<gko::matrix::Dense<double> const*&,
          gko::matrix::Dense<double>*, double&, unsigned char&, bool&, gko::array<gko::stopping_status>*&,
          gko::array<bool>*, bool*, bool*&>,0x7ffd93d14b90] completed on
          Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] \  \  \, \text{"Norm} < \text{completed for stop::Criterion} \\ [gko::stop::ResidualNorm < double>, 0x2148db0] \\ \  \  \, \text{at iteration 15 with 15 minus of the complete for stop::Criterion} \\ \  \  \, \text{(pko::stop::ResidualNorm < double>, 0x2148db0)} \\ \  \  \, \text{(pko::stop::ResidualNorm < double>, 0x2148db0)
ID 1 and finalized set to 1. It changed one RHS 0, stopped the iteration process 0 [LOG] »> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[152]
[LOG] >> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149a70] with
          Bytes[152]
[LOG] »> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
          Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x2149a70] with
          Bytes[152]
[LOG] »> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
          Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x2149a70] with
          Bytes[152]
[LOG] >> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[152]
[LOG] »> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149340] with
          Bytes[152]
[LOG] >> copy started from Executor[gko::ReferenceExecutor.0x21400d0] to
          Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x2143e90] to Location[0x2149340] with
          Bytes[152]
[LOG] >> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
          Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x2143e90] to Location[0x2149340] with
          Bytes[152]
[LOG] »> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x21499c0]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x21499c0]
[LOG] >> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149b50]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149b50]
[LOG] >> Operation[gko::solver::cg::step_1_operation<gko::matrix::Dense<double>*,
          gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
gko::matrix::Dense<double>*,
gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] started on
          Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::solver::cg::step_1_operation<gko::matrix::Dense<double>*,
          gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
          gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] completed on
          Executor[gko::ReferenceExecutor, 0x21400d0]
[LOG] >> Operation[gko::matrix::csr::spmv_operation<gko::matrix::Csr<double, int> const*,
          gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14b80] started on
          Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::csr::spmv_operation<gko::matrix::Csr<double, int> const*,
           gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14b80] completed on
          Executor[gko::ReferenceExecutor,0x21400d0]
Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
           gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] completed on
          Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::solver::cg::step_2_operation<gko::matrix::Dense<double>*&,
          gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
          gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
          gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] started on
          Executor[gko::ReferenceExecutor,0x21400d0]
 [LOG] \  \, \text{"None of the continuous of the c
          gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
gko::matrix::Dense<double>*,
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gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] completed on
          Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
         Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x21482f0] with
         Bytes[152]
[LOG] >> copy completed from Executor[gko::ReferenceExecutor.0x21400d0] to
          Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x21482f0] with
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*
         gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] started on
Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
          gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] completed on
          Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> iteration 16 completed with solver LinOp[gko::solver::Cg<double>,0x2142d60] with residual
         LinOp[gko::matrix::Dense<double>,0x2147b30], solution LinOp[gko::matrix::Dense<double>,0x2143450] and
         residual_norm LinOp[gko::LinOp const*,0]
[LOG] »> check started for stop::Criterion[gko::stop::ResidualNorm<double>,0x2148db0] at iteration 16 with
         ID 1 and finalized set to 1
[LOG] >> Operation[gko::matrix::dense::compute_norm2_operation<gko::matrix::Dense<double> const*,
          gko::matrix::Dense<double>*>,0x7ffd93d14ad0] started on Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] »> Operation[gko::matrix::dense::compute_norm2_operation<gko::matrix::Dense<double> const*
          gko::matrix::Dense<double>*>,0x7ffd93d14ad0] completed on Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] »> Operation[gko::stop::residual_norm::residual_norm_operation<gko::matrix::Dense<double> const*&,
         gko::matrix::Dense<double>*, double&, unsigned char&, bool&, gko::array<gko::stopping_status>*&,
gko::array<bool>*, bool*, bool*&>,0x7ffd93d14b90] started on
          Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::stop::residual_norm::residual_norm_operation<gko::matrix::Dense<double> const*&,
         gko::matrix::Dense<double>*, double&, unsigned char&, bool&, gko::array<gko::stopping_status>*&,
gko::array<bool>*, bool*, bool*&>,0x7ffd93d14b90] completed on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> check completed for stop::Criterion[gko::stop::ResidualNorm<double>,0x2148db0] at iteration 16 with
          ID 1 and finalized set to 1. It changed one RHS 0, stopped the iteration process 0
[LOG] >> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[152]
[LOG] >> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149970] with
         Bytes[152]
[LOG] \gg copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
          Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x2149970] with
         Bytes[152]
[LOG] »> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
         Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x2149970] with
         Bytes[152]
[LOG] >> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[152]
[LOG] »> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149b10] with
         Bytes[152]
[LOG] >> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
         Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x2143e90] to Location[0x2149b10] with
         Bytes[152]
[LOG] >> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
         Executor[gko::ReferenceExecutor, 0x21400d0] from Location[0x2143e90] to Location[0x2149b10] with
         Bytes[152]
[LOG] »> free started on Executor[gko::ReferenceExecutor, 0x21400d0] at Location[0x2149340]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149340]
[LOG] »> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149a70]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149a70]
[LOG] \  \, \text{"Normalized of the properties"} \\ \text{(LOG)} \  \, \text{"Normalized of the properties"} \\ \text{(LOG)} \  \, \text{(Solver::cg::step_1_operation < gko::matrix::Dense < double > *, representation < gko::matrix::Dense < gk
         gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
          gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] started on
          Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::solver::cg::step_1_operation<gko::matrix::Dense<double>*,
         gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] completed on
          Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::csr::spmv_operation<gko::matrix::Csr<double, int> const*,
          gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14b80] started on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::csr::spmv_operation<gko::matrix::Csr<double, int> const*,
          gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14b80] completed on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
          gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] started on
          Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
          qko::matrix::Dense<double> const*, qko::matrix::Dense<double>*>,0x7ffd93d14c50] completed on
         Executor[gko::ReferenceExecutor, 0x21400d0]
[LOG] >> Operation[gko::solver::cg::step_2_operation<gko::matrix::Dense<double>*&,
          gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
          gko::matrix::Dense<double>*, gko::matrix::Dense<double>*
          gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] started on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] \  \, \text{"None of the continuous of the co
         gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
gko::matrix::Dense<double>*,
          gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] completed on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
          Executor[gko::ReferenceExecutor, 0x21400d0] from Location[0x21480a0] to Location[0x21482f0] with
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Bytes[152]
[LOG] »> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
         Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x21482f0] with
         Bytes[152]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
         gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c501 started on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
         gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] completed on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> iteration 17 completed with solver LinOp[gko::solver::Cg<double>,0x2142d60] with residual
         LinOp[gko::matrix::Dense<double>,0x2147b30], solution LinOp[gko::matrix::Dense<double>,0x2143450] and
         residual_norm LinOp[gko::LinOp const*,0]
[LOG] >> check started for stop::Criterion[gko::stop::ResidualNorm<double>,0x2148db0] at iteration 17 with
         ID 1 and finalized set to 1
[LOG] >> Operation[gko::matrix::dense::compute_norm2_operation<gko::matrix::Dense<double> const*
          gko::matrix::Dense<double>*>,0x7ffd93d14ad0] started on Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_norm2_operation<gko::matrix::Dense<double> const*,
         gko::matrix::Dense<double>*>,0x7ffd93d14ad0] completed on Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::stop::residual_norm::residual_norm_operation<gko::matrix::Dense<double> const*&,
         gko::matrix::Dense<double>*, double&, unsigned char&, bool&, gko::array<gko::stopping_status>*&, gko::array<br/>bool>*, bool*, bool*&>,0x7ffd93d14b90] started on
         Executor[gko::ReferenceExecutor,0x21400d0]
Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> check completed for stop::Criterion[gko::stop::ResidualNorm<double>,0x2148db0] at iteration 17 with
         ID 1 and finalized set to 1. It changed one RHS 0, stopped the iteration process 0 \,
[LOG] >> allocation started on Executor[gko::ReferenceExecutor, 0x21400d0] with Bytes[152]
[LOG] >> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149780] with
         Bytes[152]
[LOG] »> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
         Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x2149780] with
         Bytes[152]
[LOG] >> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
         Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x2149780] with
         Bytes[152]
[LOG] >> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[152]
[LOG] »> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149890] with
         Bytes[152]
[LOG] \gg copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
         Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x2143e90] to Location[0x2149890] with
         Bytes [152]
[LOG] >> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
         Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x2143e90] to Location[0x2149890] with
         Bytes[152]
[LOG] »> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149b10] [LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149b10] [LOG] »> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149970]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149970]
[LOG] >> Operation[gko::solver::cg::step_1_operation<gko::matrix::Dense<double>*,
         gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
         gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] started on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::solver::cg::step_1_operation<gko::matrix::Dense<double>*,
         gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
         gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] completed on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::csr::spmv_operation<gko::matrix::Csr<double, int> const*,
         gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14b80] started on
Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] »> Operation[gko::matrix::csr::spmv_operation<gko::matrix::Csr<double, int> const*,
         gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14b80] completed on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
          gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] started on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
         gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] completed on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::solver::cg::step_2_operation<gko::matrix::Dense<double>*&,
         gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
gko::matrix::Dense<double>*,
gko::matrix::Dense<double>*,
gko::matrix::Dense<double>*,
gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] started on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::solver::cg::step_2_operation<gko::matrix::Dense<double>*&,
         gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
         gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] completed on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> copy started from Executor[gko::ReferenceExecutor, 0x21400d0] to
         Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x21482f0] with
         Bytes[152]
[LOG] \gg copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
         \textbf{Executor}[\textbf{gko}:: \textbf{ReferenceExecutor}, \textbf{0x21400d0}] \text{ from } \textbf{Location}[\textbf{0x21480a0}] \text{ to } \textbf{Location}[\textbf{0x21482f0}] \text{ with } \textbf{0x21480a0} \text{ and } \textbf{0x21480a0} \text{ or } \textbf{0x21482f0} \text{ 
         Bytes[152]
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[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
          gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] started on
         Executor[gko::ReferenceExecutor, 0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
          gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] completed on
          Executor[gko::ReferenceExecutor, 0x21400d0]
[LOG] >> iteration 18 completed with solver LinOp[gko::solver::Cg<double>,0x2142d60] with residual
          LinOp[gko::matrix::Dense<double>,0x2147b30], solution LinOp[gko::matrix::Dense<double>,0x2143450] and
          residual_norm LinOp[gko::LinOp const*,0]
[LOG] >> check started for stop::Criterion[gko::stop::ResidualNorm<double>,0x2148db0] at iteration 18 with
         ID 1 and finalized set to 1
[LOG] >> Operation[gko::matrix::dense::compute_norm2_operation<gko::matrix::Dense<double> const*,
          gko::matrix::Dense<double>*>,0x7ffd93d14ad0] started on Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] »> Operation(gko::matrix::dense::compute_norm2_operation<gko::matrix::Dense<double> const*,
          gko::matrix::Dense<double>*>,0x7ffd93d14ad0] completed on Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] \gg Operation[gko::stop::residual_norm::residual_norm_operation < gko::matrix::Dense < double > const*\&, figure = 
          gko::matrix::Dense<double>*, double&, unsigned char&, bool&, gko::array<gko::stopping_status>*&,
gko::array<bool>*, bool*, bool*&>,0x7ffd93d14b90] started on
          Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::stop::residual_norm::residual_norm_operation<gko::matrix::Dense<double> const*&,
         gko::matrix::Dense<double>*, double&, unsigned chark, bool&, gko::array<gko::stopping_status>*&, gko::array<bool>*, bool*, bool*&>,0x7ffd93d14b90] completed on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> check completed for stop::Criterion[gko::stop::ResidualNorm<double>,0x2148db0] at iteration 18 with
          ID 1 and finalized set to 1. It changed one RHS 0, stopped the iteration process 0
[LOG] >> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[152]
[LOG] »> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149620] with
         Bytes[152]
[LOG] >> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
         Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x2149620] with
         Bytes[152]
[LOG] >> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
         Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x2149620] with
[LOG] >> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[152]
[LOG] >> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149cf0] with
         Bytes[152]
[LOG] »> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
          Executor[gko::ReferenceExecutor.0x21400d0] from Location[0x2143e90] to Location[0x2149cf0] with
         Bytes[152]
[LOG] »> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
         Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x2143e90] to Location[0x2149cf0] with
         Bytes[152]
[LOG] »> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149890]
[LOG] >> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149890]
[LOG] »> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149780]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149780]
[LOG] >> Operation[gko::solver::cg::step_1_operation<gko::matrix::Dense<double>*,
         gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
qko::array<gko::stopping_status>*>,0x7ffd93d14ef0] started on
          Executor[gko::ReferenceExecutor, 0x21400d0]
[LOG] >> Operation[gko::solver::cg::step_1_operation<gko::matrix::Dense<double>*,
          gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
          gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] completed on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::csr::spmv_operation<gko::matrix::Csr<double, int> const*,
          gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14b80] started on
          Executor[gko::ReferenceExecutor, 0x21400d0]
[LOG] >> Operation[gko::matrix::csr::spmv_operation<gko::matrix::Csr<double, int> const*,
         gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14b80] completed on
Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
          gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] started on
          Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
          gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] completed on
         Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::solver::cg::step_2_operation<gko::matrix::Dense<double>*&,
          gko::matrix::Dense<double>*, gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
         gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
          gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] started on
          Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::solver::cg::step_2_operation<gko::matrix::Dense<double>*&,
         gko::matrix::Dense<double>*, gko::matrix::Dense<double>*,
gko::matrix::Dense<double>*,
gko::matrix::Dense<double>*,
          gko::array<gko::stopping_status>*>,0x7ffd93d14ef0] completed on
          Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
          Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x21482f0] with
         Bytes[152]
[LOG] »> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
          Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x21482f0] with
[LOG] »> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
          gko::matrix::Dense < double > const*, \ gko::matrix::Dense < double > *>, 0x7ffd93d14c50] \ started \ on the started on the 
         Executor[gko::ReferenceExecutor, 0x21400d0]
[LOG] »> Operation[gko::matrix::dense::compute_dot_operation<gko::matrix::Dense<double> const*,
```

```
gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14c50] completed on
      Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> iteration 19 completed with solver LinOp[gko::solver::Cg<double>,0x2142d60] with residual
      LinOp[gko::matrix::Dense<double>,0x2147b30], solution LinOp[gko::matrix::Dense<double>,0x2143450] and
      residual_norm LinOp[gko::LinOp const*,0]
[LOG] >> check started for stop::Criterion[gko::stop::ResidualNorm<double>.0x2148db0] at iteration 19 with
      ID 1 and finalized set to 1
[LOG] >> Operation[gko::matrix::dense::compute_norm2_operation<gko::matrix::Dense<double> const*,
      gko::matrix::Dense<double>*>,0x7ffd93d14ad0] started on Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::dense::compute_norm2_operation<gko::matrix::Dense<double> const*,
      gko::matrix::Dense<double>*>,0x7ffd93d14ad0] completed on Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::stop::residual_norm::residual_norm_operation<gko::matrix::Dense<double> const*&,
      gko::matrix::Dense<double>*, double&, unsigned chark, bool&, gko::array<gko::stopping_status>*&, gko::array<br/>gko::array<br/>bool*, bool*&>,0x7ffd93d14b90] started on
      Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::stop::residual_norm::residual_norm_operation<gko::matrix::Dense<double> const*&,
      gko::matrix::Dense<double>*, double&, unsigned char&, bool&, gko::array<gko::stopping_status>*&,
gko::array<bool>*, bool*, bool*&>,0x7ffd93d14b90] completed on
      Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] »> check completed for stop::Criterion[gko::stop::ResidualNorm<double>,0x2148db0] at iteration 19 with
      ID 1 and finalized set to 1. It changed one RHS 1, stopped the iteration process 1
[LOG] >> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[152]
[LOG] >> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149890] with
      Bytes[152]
[LOG] >> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
      Executor[gko::ReferenceExecutor, 0x21400d0] from Location[0x21480a0] to Location[0x2149890] with
[LOG] >> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
      Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x21480a0] to Location[0x2149890] with
      Bytes[152]
[LOG] >> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[152]
[LOG] »> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149340] with
[LOG] >> copy started from Executor[gko::ReferenceExecutor,0x21400d0] to
      Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x2143e90] to Location[0x2149340] with
      Bytes[152]
[LOG] >> copy completed from Executor[gko::ReferenceExecutor,0x21400d0] to
      Executor[gko::ReferenceExecutor,0x21400d0] from Location[0x2143e90] to Location[0x2149340] with
[LOG] »> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149cf0]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149cf0]
[LOG] >> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149620]
[LOG] »> free completed on Executor[gko::ReferenceExecutor, 0x21400d0] at Location[0x2149620]
[LOG] »> free started on Executor[gko::ReferenceExecutor, 0x21400d0] at Location[0x2148ee0]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2148ee0]
[LOG] >> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2147ce0]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2147ce0]
[LOG] >> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2148e50]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2148e50]
[LOG] >> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2147c90]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2147c90]
[LOG] »> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x21482b0]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x21482b0]
[LOG] »> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2148a40]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2148a40]
[LOG] »> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2148a60]
[LOG] »> free completed on Executor[gko::ReferenceExecutor, 0x21400d0] at Location[0x2148a60]
[LOG] >> free started on Executor[gko::ReferenceExecutor, 0x21400d0] at Location[0x2148010]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2148010]
[LOG] >> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x21486b0]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x21486b0]
[LOG] >> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x21484d0]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x21484d0]
[LOG] >> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x21482f0]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x21482f0]
[LOG] >> free started on Executor[gko::ReferenceExecutor, 0x21400d0] at Location[0x21480a0]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x21480a0]
[LOG] »> free started on Executor[gko::ReferenceExecutor, 0x21400d0] at Location[0x2143410]
[LOG] >> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2143410]
[LOG] >> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2142280]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2142280]
[LOG] >> apply completed on A LinOp[gko::solver::Cg<double>,0x2142d60] with b
     \label{lin0p} \texttt{[gko::matrix::Dense<double>,0x2142140]} \ \ \text{and} \ \ x \ \ \texttt{Lin0p[gko::matrix::Dense<double>,0x2143450]}
Last memory copied was of size 98 FROM executor 0x21400d0 pointer 2143e90 TO executor 0x21400d0 pointer
     2149340
Residual = [
    8.1654e-19
    -1.51449e-17
    2.23854e-17
    -1.0842e-19
    6.09864e-20
    -1.92446e-18
    1.97867e-18
    -4.58075e-18
    -1.55854e-18
    -2.64274e-17
    4.20128e-17
```

```
-8.71427e-18
    -2.62919e-18
    -5.49947e-17
    5.51893e-17
    -1.57022e-16
    -4.2034e-17
    -8.71951e-16
    1.37837e-15
Solution (x):
%%MatrixMarket matrix array real general
19 1
0.252218
0.108645
0.0662811
0.0630433
0.0384088
0.0396536
0.0402648
0.0338935
0.0193098
0.0234653
0.0211499
0.0196413
0.0199151
0.0181674
0.0162722
0.0150714
0.0107016
0.0121141
0.0123025
[LOG] >> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[8]
[LOG] »> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149bb0] with
[LOG] >> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[8]
[LOG] >> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149870] with
      Bytes[8]
[LOG] »> allocation started on Executor[gko::ReferenceExecutor,0x21400d0] with Bytes[8]
[LOG] >> allocation completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149500] with
[LOG] »> Operation[gko::matrix::csr::advanced_spmv_operation<gko::matrix::Dense<double> const*,
      gko::matrix::Csr<double, int> const*, gko::matrix::Dense<double> const*, gko::matrix::Dense<double> const*, gko::matrix::Dense<double>*>,0x7ffd93d14e50] started on
      Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation[gko::matrix::csr::advanced_spmv_operation<gko::matrix::Dense<double> const*,
      gko::matrix::Csr<double, int> const*, gko::matrix::Dense<double> const*, gko::matrix::Dense<double>
      const*, gko::matrix::Dense<double>*>,0x7ffd93d14e50] completed on
      Executor[gko::ReferenceExecutor,0x21400d0]
[LOG] >> Operation(gko::matrix::dense::compute norm2 operation(gko::matrix::Dense<double> const*.
      qko::matrix::Dense<double>*>,0x7ffd93d14f70] started on Executor[qko::ReferenceExecutor,0x21400d0]
[LOG] »> Operation[gko::matrix::dense::compute_norm2_operation<gko::matrix::Dense<double> const*,
      gko::matrix::Dense<double>*>,0x7ffd93d14f70] completed on Executor[gko::ReferenceExecutor,0x21400d0]
Residual norm sqrt(r^T r):
%%MatrixMarket matrix array real general
1 1
2.10788e-15
[LOG] »> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149500]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149500]
[LOG] »> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149870]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149870]
[LOG] »> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149bb0]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2149bb0]
[LOG] »> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2143e90]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2143e90]
[LOG] »> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2143590]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2143590]
[LOG] >> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2142b10]
[LOG] »> free completed on Executor[gko::ReferenceExecutor.0x21400d0] at Location[0x2142b10]
[LOG] >> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2143c30]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2143c30]
[LOG] »> free started on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2143790]
[LOG] »> free completed on Executor[gko::ReferenceExecutor,0x21400d0] at Location[0x2143790]
```

## Comments about programming and debugging

# The plain program

```
#include <fstream>
#include <iomanip>
#include <iostream>
#include <map>
```

```
#include <string>
#include <ginkgo/ginkgo.hpp>
namespace {
template <typename ValueType>
void print_vector(const std::string& name,
                   const gko::matrix::Dense<ValueType>* vec)
    std::cout « name « " = [" « std::endl;
    for (int i = 0; i < vec->get_size()[0]; ++i) {
    std::cout « " " « vec->at(i, 0) « std::endl;
    std::cout « "]; " « std::endl;
   // namespace
int main(int argc, char* argv[])
    using ValueType = double;
    using RealValueType = gko::remove_complex<ValueType>;
    using IndexType = int;
    using vec = gko::matrix::Dense<ValueType>;
    using real_vec = gko::matrix::Dense<RealValueType>;
    using mtx = gko::matrix::Csr<ValueType, IndexType>;
    using cg = gko::solver::Cg<ValueType>;
    std::cout « gko::version_info::get() « std::endl;
if (argc == 2 && (std::string(argv[1]) == "--help")) {
    std::cerr « "Usage: " « argv[0] « " [executor]" « std::endl;
         std::exit(-1);
    const auto executor_string = argc >= 2 ? argv[1] : "reference";
    std::map<std::string, std::function<std::shared_ptr<gko::Executor>()»
        exec map{
             {"omp", [] { return gko::OmpExecutor::create(); }},
              [] {
                   return gko::CudaExecutor::create(0,
                                                        gko::OmpExecutor::create());
             }},
{"hip",
              [] {
                 return gko::HipExecutor::create(0, gko::OmpExecutor::create());
              }},
             { "dpcpp",
              [] {
                  return gko::DpcppExecutor::create(0,
                                                         gko::OmpExecutor::create());
             {"reference", [] { return gko::ReferenceExecutor::create(); }}};
    const auto exec = exec_map.at(executor_string)(); // throws if not valid
auto A = share(gko::read<mtx>(std::ifstream("data/A.mtx"), exec));
    auto b = gko::read<vec>(std::ifstream("data/b.mtx"), exec);
    auto x = gko::read<vec>(std::ifstream("data/x0.mtx"), exec);
    std::shared_ptr<gko::log::Stream<ValueType» stream_logger</pre>
        gko::log::Stream<ValueType>::create(
             gko::log::Logger::all_events_mask
                 gko::log::Logger::linop_factory_events_mask ^
                 gko::log::Logger::polymorphic_object_events_mask,
             std::cout);
    exec->add_logger(stream_logger);
    const RealValueType reduction_factor{1e-7};
    using ResidualCriterionFactory =
    gko::stop::ResidualNorm<ValueType>::Factory;
    std::shared_ptr<ResidualCriterionFactory> residual_criterion =
        ResidualCriterionFactory::create()
             .with_reduction_factor(reduction_factor)
             .on(exec);
    residual_criterion->add_logger(stream_logger);
    auto solver gen =
        ca::build()
             .with_criteria(residual_criterion,
                              gko::stop::Iteration::build().with_max_iters(20u))
    auto solver = solver_gen->generate(A);
    std::ofstream filestream("my_file.txt");
    solver->add_logger(gko::log::Stream<ValueType>::create(
        gko::log::Logger::all_events_mask, filestream));
    solver->add_logger(stream_logger);
    std::shared_ptr<gko::log::Convergence<ValueType» convergence_logger =
        gko::log::Convergence<ValueType>::create();
    solver->add_logger(convergence_logger);
    std::shared_ptr<gko::log::Record> record_logger =
    gko::log::Record::create(gko::log::Logger::executor_events_mask |
                                     gko::log::Logger::iteration_complete_mask);
    exec->add_logger(record_logger);
    solver->add_logger(record_logger);
    solver->apply(b, x);
    auto residual =
        record logger->get().iteration completed.back()->residual.get();
```

# **Chapter 43**

# The three-pt-stencil-solver program

The 3-point stencil example..

This example depends on simple-solver, poisson-solver.

## Introduction

This example solves a 1D Poisson equation:

$$u: [0,1] \to R$$

$$u'' = f$$

$$u(0) = u0$$

$$u(1) = u1$$

using a finite difference method on an equidistant grid with K discretization points (K can be controlled with a command line parameter). The discretization is done via the second order Taylor polynomial:

For an equidistant grid with K "inner" discretization points x1,...,xk,and step size h=1/(K+1), the formula produces a system of linear equations

$$2u_1 - u_2 = -f_1h^2 + u0$$
  
-  $u_(k-1) + 2u_k - u_(k+1) = -f_kh^2, k = 2, ..., K-1$   
-  $u_(K-1) + 2u_K = -f_Kh^2 + u1$ 

which is then solved using Ginkgo's implementation of the CG method preconditioned with block-Jacobi. It is also possible to specify on which executor Ginkgo will solve the system via the command line. The function 'f'is set to 'f(x) = 6x' (making the solution ' $u(x) = x^3$ '), but that can be changed in the main function.

The intention of the example is to show how Ginkgo can be integrated into existing software - the <code>generate</code>—<code>stencil\_matrix</code>, <code>generate\_rhs</code>, <code>print\_solution</code>, <code>compute\_error</code> and <code>main</code> function do not reference Ginkgo at all (i.e. they could have been there before the application developer decided to use Ginkgo, and the only part where Ginkgo is introduced is inside the <code>solve\_system</code> function.

#### About the example

# The commented program

#### Creates a stencil matrix in CSR format for the given number of discretization points.

### Generates the RHS vector given f and the boundary conditions.

#### Prints the solution u.

#### Computes the 1-norm of the error given the computed u and the correct solution function correct\_u.

```
template <typename ValueType, typename IndexType>
void solve_system(const std::string& executor_string,
                    IndexType discretization_points, IndexType* row_ptrs,
                    IndexType* col_idxs, ValueType* values, ValueType* rhs,
ValueType* u, gko::remove_complex<ValueType> reduction_factor)
{
Some shortcuts
using vec = gko::matrix::Dense<ValueType>;
using mtx = gko::matrix::Csr<ValueType, IndexType>;
using cg = gko::solver::Cg<ValueType>;
using bj = gko::preconditioner::Jacobi<ValueType, IndexType>;
using val_array = gko::array<ValueType>;
using idx_array = gko::array<IndexType>;
const auto@ dp = discretization_points;
Figure out where to run the code
std::map<std::string, std::function<std::shared_ptr<gko::Executor>()»
    exec_map{
         {"omp", [] { return gko::OmpExecutor::create(); }},
         {"cuda",
          [] {
              return gko::CudaExecutor::create(0,
                                                    gko::OmpExecutor::create());
         {"hip",
          [] {
              return gko::HipExecutor::create(0, gko::OmpExecutor::create());
         {"dpcpp",
          [] {
               return gko::DpcppExecutor::create(0,
                                                     gko::OmpExecutor::create());
         {"reference", [] { return gko::ReferenceExecutor::create(); }}};
executor where Ginkgo will perform the computation
const auto exec = exec_map.at(executor_string)(); // throws if not valid
executor where the application initialized the data
const auto app_exec =
                        exec->get_master();
```

Tell Ginkgo to use the data in our application

Matrix: we have to set the executor of the matrix to the one where we want SpMVs to run (in this case exec). When creating array views, we have to specify the executor where the data is (in this case  $app\_exec$ ).

If the two do not match, Ginkgo will automatically create a copy of the data on exec (however, it will not copy the data back once it is done

• here this is not important since we are not modifying the matrix).

Solution: we have to be careful here - if the executors are different, once we compute the solution the array will not be automatically copied back to the original memory locations. Fortunately, whenever  $\mathtt{apply}$  is called on a linear operator (e.g. matrix, solver) the arguments automatically get copied to the executor where the operator is, and copied back once the operation is completed. Thus, in this case, we can just define the solution on  $\mathtt{app\_exec}$ , and it will be automatically transferred to/from  $\mathtt{exec}$  if needed.

cg::build()

```
.with_criteria(gko::stop::Iteration::build().with_max_iters(
                        gko::size_type(dp)),
gko::stop::ResidualNorm<ValueType>::build()
                            .with_reduction_factor(reduction_factor))
         .with_preconditioner(bj::build())
         .on(exec);
auto solver = solver_gen->generate(gko::give(matrix));
Solve system
    solver->apply(b, x);
int main(int argc, char* argv[])
    using ValueType = double:
    using IndexType = int;
Print version information
std::exit(-1);
const auto executor_string = argc >= 2 ? argv[1] : "reference";
const IndexType discretization_points =
    argc >= 3 ? std::atoi(argv[2]) : 100;
problem:
auto correct_u = [](ValueType x) { return x * x * x; };
auto f = [](ValueType x) { return ValueType(6) * x; };
auto u0 = correct_u(0);
auto u1 = correct_u(1);
std::vector<IndexType> row_ptrs(discretization_points + 1);
std::vector<IndexType> col_idxs(3 * discretization_points - 2);
std::vector<ValueType> values(3 * discretization_points - 2);
right hand side
std::vector<ValueType> rhs(discretization_points);
solution
std::vector<ValueType> u(discretization_points, 0.0);
const gko::remove_complex<ValueType> reduction_factor = 1e-7;
generate_stencil_matrix(discretization_points, row_ptrs.data(),
                          col_idxs.data(), values.data());
looking for solution u = x^3: f = 6x, u(0) = 0, u(1) = 1
generate_rhs(discretization_points, f, u0, u1, rhs.data());
solve_system(executor_string, discretization_points, row_ptrs.data(),
              col_idxs.data(), values.data(), rhs.data(), u.data(),
              reduction_factor);
Uncomment to print the solution print_solution<ValueType, IndexType>(discretization_points, 0, 1, u.data());
    std::cout « "The average relative error is "
              « calculate_error(discretization_points, u.data(), correct_u) /
                      discretization_points
               « std::endl;
```

## **Results**

#### This is the expected output:

The average relative error is 2.52236e-11

#### Comments about programming and debugging

# The plain program

```
This example solves a 1D Poisson equation:
u : [0, 1] \rightarrow R
u'' = f
u(0) = u0
u(1) = u1
using a finite difference method on an equidistant grid with \ discretization
points ('K' can be controlled with a command line parameter). The discretization
is done via the second order Taylor polynomial:
u(x + h) = u(x) - u'(x)h + 1/2 u''(x)h^2 + O(h^3)
u(x - h) = u(x) + u'(x)h + 1/2 u''(x)h^2 + O(h^3) / +
-u(x - h) + 2u(x) + -u(x + h) = -f(x)h^2 + O(h^3)
For an equidistant grid with K "inner" discretization points x1, \dots, xk, and
step size h = 1 / (K + 1), the formula produces a system of linear equations
2u_1 - u_2
               = -f_1 h^2 + u0
-u_{(k-1)} + 2u_{k} - u_{(k+1)} = -f_{k} h^{2}
                                              k = 2, ..., K - 1
-u_(K-1) + 2u_K
                           = -f K h^2 + u1
which is then solved using {\tt Ginkgo's} implementation of the CG method
\label{eq:preconditioned} \mbox{ with block-Jacobi. It is also possible to specify on which}
executor Ginkgo will solve the system via the command line. The function 'f' is set to 'f(x) = 6x' (making the solution 'u(x) = x^3'), but
that can be changed in the 'main' function.
The intention of the example is to show how Ginkgo can be integrated into
existing software - the 'generate_stencil_matrix', 'generate_rhs', 'print_solution', 'compute_error' and 'main' function do not reference Ginkgo at
all (i.e. they could have been there before the application developer decided to
use Ginkgo, and the only part where Ginkgo is introduced is inside the
'solve_system' function.
#include <iostream>
#include <map>
#include <string>
#include <vector>
#include <ginkgo/ginkgo.hpp>
template <typename ValueType, typename IndexType>
void generate_stencil_matrix(IndexType discretization_points,
                               IndexType* row_ptrs, IndexType* col_idxs,
                               ValueType* values)
    IndexType pos = 0;
    const ValueType coefs[] = \{-1, 2, -1\};
    row_ptrs[0] = pos;
    for (IndexType i = 0; i < discretization_points; ++i) {</pre>
        for (auto ofs: {-1, 0, 1}) {
    if (0 <= i + ofs && i + ofs < discretization_points) {</pre>
                 values[pos] = coefs[ofs + 1];
                 col_idxs[pos] = i + ofs;
                 ++pos;
            }
        row_ptrs[i + 1] = pos;
template <typename Closure, typename ValueType, typename IndexType>
void generate_rhs(IndexType discretization_points, Closure f, ValueType u0,
                   ValueType u1, ValueType* rhs)
    const ValueType h = 1.0 / (discretization_points + 1);
for (IndexType i = 0; i < discretization_points; ++i) {</pre>
        const ValueType xi = ValueType(i + 1) \star h;
        rhs[i] = -f(xi) * h * h;
    rhs[0] += u0;
    rhs[discretization_points - 1] += u1;
template <typename ValueType, typename IndexType>
void print_solution(IndexType discretization_points, ValueType u0, ValueType u1,
                     const ValueType* u)
    std::cout « u0 « '\n';
    for (IndexType i = 0; i < discretization_points; ++i) {</pre>
```

```
std::cout « u[i] « '\n';
    std::cout « u1 « std::end]:
template <typename Closure, typename ValueType, typename IndexType>
gko::remove_complex<ValueType> calculate_error(IndexType discretization_points,
                                                  const ValueType* u,
                                                  Closure correct_u)
    const ValueType h = 1.0 / (discretization_points + 1);
gko::remove_complex<ValueType> error = 0.0;
    for (IndexType i = 0; i < discretization_points; ++i) {
        using std::abs;
        const ValueType xi = ValueType(i + 1) * h;
error += abs(u[i] - correct_u(xi)) / abs(correct_u(xi));
    return error:
template <typename ValueType, typename IndexType>
void solve_system(const std::string& executor_string,
                   IndexType discretization_points, IndexType* row_ptrs,
                   IndexType* col_idxs, ValueType* values, ValueType* rhs,
ValueType* u, gko::remove_complex<ValueType> reduction_factor)
    using vec = gko::matrix::Dense<ValueType>;
    using mtx = gko::matrix::Csr<ValueType, IndexType>;
    using cg = gko::solver::Cg<ValueType>;
    using bj = gko::preconditioner::Jacobi<ValueType, IndexType>;
    using val_array = gko::array<ValueType>;
using idx_array = gko::array<IndexType>;
const auto& dp = discretization_points;
    std::map<std::string, std::function<std::shared_ptr<gko::Executor>()»
        exec_map{
             {"omp", [] { return gko::OmpExecutor::create(); }},
             {"cuda",
              [] {
                  return gko::CudaExecutor::create(0,
                                                      gko::OmpExecutor::create());
              }},
             {"hip",
              [] {
                  return gko::HipExecutor::create(0, gko::OmpExecutor::create());
             { "dpcpp",
              [] {
                  return gko::DpcppExecutor::create(0,
                                                       gko::OmpExecutor::create());
             {"reference", [] { return gko::ReferenceExecutor::create(); }}};
    const auto exec = exec_map.at(executor_string)(); // throws if not valid
    const auto app_exec = exec->get_master();
    auto matrix = mtx::create(exec, gko::dim<2>(dp),
                                val_array::view(app_exec, 3 * dp - 2, values),
                                idx_array::view(app_exec, 3 * dp - 2, col_idxs),
                                idx_array::view(app_exec, dp + 1, row_ptrs));
    auto b = vec::create(exec, gko::dim<2>(dp, 1),
                           val_array::view(app_exec, dp, rhs), 1);
    auto x = vec::create(app_exec, gko::dim<2>(dp, 1),
                           val_array::view(app_exec, dp, u), 1);
    auto solver_gen =
        ca::build()
             .with_criteria(gko::stop::Iteration::build().with_max_iters(
                                gko::size_type(dp)),
                             gko::stop::ResidualNorm<ValueType>::build()
                                  .with_reduction_factor(reduction_factor))
             .with_preconditioner(bj::build())
             .on(exec);
    auto solver = solver_gen->generate(gko::give(matrix));
    solver->apply(b, x);
int main(int argc, char* argv[])
    using ValueType = double;
    using IndexType = int;
    if (argc == 2 && std::string(argv[1]) == "--help") {
        std::exit(-1);
    const auto executor_string = argc >= 2 ? argv[1] : "reference";
    const IndexType discretization_points =
    argc >= 3 ? std::atoi(argv[2]) : 100;
auto correct_u = [](ValueType x) { return x * x * x; };
    auto f = [](ValueType x) { return ValueType(6) * x; };
    auto u0 = correct_u(0);
    auto u1 = correct_u(1);
```

# Chapter 44

# **Module Documentation**

# 44.1 CUDA Executor

A module dedicated to the implementation and usage of the CUDA executor in Ginkgo.

## Classes

• class gko::CudaExecutor

This is the Executor subclass which represents the CUDA device.

# 44.1.1 Detailed Description

A module dedicated to the implementation and usage of the CUDA executor in Ginkgo.

# 44.2 DPC++ Executor

A module dedicated to the implementation and usage of the DPC++ executor in Ginkgo.

## **Classes**

• class gko::DpcppExecutor

This is the Executor subclass which represents a DPC++ enhanced device.

# 44.2.1 Detailed Description

A module dedicated to the implementation and usage of the DPC++ executor in Ginkgo.

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## 44.3 Executors

A module dedicated to the implementation and usage of the executors in Ginkgo.

## **Modules**

CUDA Executor

A module dedicated to the implementation and usage of the CUDA executor in Ginkgo.

DPC++ Executor

A module dedicated to the implementation and usage of the DPC++ executor in Ginkgo.

HIP Executor

A module dedicated to the implementation and usage of the HIP executor in Ginkgo.

OpenMP Executor

A module dedicated to the implementation and usage of the OpenMP executor in Ginkgo.

• Reference Executor

A module dedicated to the implementation and usage of the Reference executor in Ginkgo.

#### **Classes**

· class gko::Operation

Operations can be used to define functionalities whose implementations differ among devices.

· class gko::Executor

The first step in using the Ginkgo library consists of creating an executor.

class gko::executor\_deleter< T >

This is a deleter that uses an executor's free method to deallocate the data.

class gko::OmpExecutor

This is the Executor subclass which represents the OpenMP device (typically CPU).

class gko::ReferenceExecutor

This is a specialization of the OmpExecutor, which runs the reference implementations of the kernels used for debugging purposes.

· class gko::CudaExecutor

This is the Executor subclass which represents the CUDA device.

· class gko::HipExecutor

This is the Executor subclass which represents the HIP enhanced device.

· class gko::DpcppExecutor

This is the Executor subclass which represents a DPC++ enhanced device.

#### **Macros**

• #define GKO\_REGISTER\_OPERATION(\_name, \_kernel)

Binds a set of device-specific kernels to an Operation.

#define GKO\_REGISTER\_HOST\_OPERATION(\_name, \_kernel)

Binds a host-side kernel (independent of executor type) to an Operation.

# 44.3.1 Detailed Description

A module dedicated to the implementation and usage of the executors in Ginkgo.

Below, we provide a brief introduction to executors in Ginkgo, how they have been implemented, how to best make use of them and how to add new executors.

## 44.3.2 Executors in Ginkgo.

The first step in using the Ginkgo library consists of creating an executor. Executors are used to specify the location for the data of linear algebra objects, and to determine where the operations will be executed. Ginkgo currently supports three different executor types:

- OpenMP Executor specifies that the data should be stored and the associated operations executed on an OpenMP-supporting device (e.g. host CPU);
- CUDA Executor specifies that the data should be stored and the operations executed on the NVIDIA GPU accelerator;
- HIP Executor uses the HIP library to compile code for either NVIDIA or AMD GPU accelerator;
- DPC++ Executor uses the DPC++ compiler for any DPC++ supported hardware (e.g. Intel CPUs, GPU, FPGAs, ...);
- Reference Executor executes a non-optimized reference implementation, which can be used to debug the library.

#### 44.3.3 Macro Definition Documentation

#### 44.3.3.1 GKO REGISTER HOST OPERATION

#### Value:

Binds a host-side kernel (independent of executor type) to an Operation.

It also defines a helper function which creates the associated operation. Any input arguments passed to the helper function are forwarded to the kernel when the operation is executed. The kernel name is searched for in the namespace where this macro is called. Host operations are used to make computations that are not part of the device kernels visible to profiling loggers and benchmarks.

#### **Parameters**

_name	operation name
_kernel	kernel which will be bound to the operation

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#### 44.3.3.2 Example

```
{c++}
void host_kernel(int) {
    // do some expensive computations
}
// Bind the kernels to the operation
GKO_REGISTER_HOST_OPERATION(my_op, host_kernel);
int main() {
    // create executor
    auto ref = ReferenceExecutor::create();
    // create the operation
    auto op = make_my_op(5); // x = 5
    ref->run(op); // run host kernel
}
```

## 44.3.3.3 GKO\_REGISTER\_OPERATION

Binds a set of device-specific kernels to an Operation.

It also defines a helper function which creates the associated operation. Any input arguments passed to the helper function are forwarded to the kernel when the operation is executed.

The kernels used to bind the operation are searched in kernels::DEV\_TYPE namespace, where DEV\_TYPE is replaced by omp, cuda, hip, dpcpp and reference.

#### **Parameters**

_name	operation name
_kernel	kernel which will be bound to the operation

## 44.3.3.4 Example

```
{ c++ }
// define the omp, cuda, hip and reference kernels which will be bound to the
// operation
namespace kernels {
namespace omp {
void my_kernel(int x) {
     // omp code
namespace cuda {
void my_kernel(int x) {
      // cuda code
namespace hip {
void my_kernel(int x) {
    // hip code
namespace dpcpp {
void my_kernel(int x) {
     // dpcpp code
namespace reference {
void my_kernel(int x) {
    // reference code
```

```
// Bind the kernels to the operation
GKO_REGISTER_OPERATION(my_op, my_kernel);
int main() {
    // create executors
    auto omp = OmpExecutor::create();
    auto cuda = CudaExecutor::create(0, omp);
    auto hip = HipExecutor::create(0, omp);
    auto dpcpp = DpcppExecutor::create(0, omp);
    auto ref = ReferenceExecutor::create();
    // create the operation
    auto op = make_my_op(5); // x = 5
    omp->run(op); // run omp kernel
    cuda->run(op); // run hip kernel
    dpcpp->run(op); // run bPC++ kernel
    ref->run(op); // run reference kernel
}
```

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## 44.4 Factorizations

A module dedicated to the implementation and usage of the Factorizations in Ginkgo.

## **Namespaces**

· gko::factorization

The Factorization namespace.

#### Classes

class gko::factorization::lc
 ValueType, IndexType >

Represents an incomplete Cholesky factorization (IC(0)) of a sparse matrix.

class gko::factorization::llu
 ValueType, IndexType

Represents an incomplete LU factorization – ILU(0) – of a sparse matrix.

class gko::factorization::ParIc< ValueType, IndexType >

ParIC is an incomplete Cholesky factorization which is computed in parallel.

class gko::factorization::ParIct< ValueType, IndexType >

ParICT is an incomplete threshold-based Cholesky factorization which is computed in parallel.

- class gko::factorization::Parllu< ValueType, IndexType >

ParILU is an incomplete LU factorization which is computed in parallel.

class gko::factorization::Parllut< ValueType, IndexType >

ParILUT is an incomplete threshold-based LU factorization which is computed in parallel.

## 44.4.1 Detailed Description

A module dedicated to the implementation and usage of the Factorizations in Ginkgo.

# 44.5 HIP Executor

A module dedicated to the implementation and usage of the HIP executor in Ginkgo.

## **Classes**

• class gko::HipExecutor

This is the Executor subclass which represents the HIP enhanced device.

# 44.5.1 Detailed Description

A module dedicated to the implementation and usage of the HIP executor in Ginkgo.

44.6 Jacobi Preconditioner 287

## 44.6 Jacobi Preconditioner

A module dedicated to the implementation and usage of the Jacobi Preconditioner in Ginkgo.

#### **Classes**

- class gko::batch::preconditioner::Jacobi< ValueType, IndexType >
  - A block-Jacobi preconditioner is a block-diagonal linear operator, obtained by inverting the diagonal blocks (stored in a dense row major fashion) of the source operator.
- struct gko::preconditioner::block\_interleaved\_storage\_scheme < IndexType >
  - Defines the parameters of the interleaved block storage scheme used by block-Jacobi blocks.
- class gko::preconditioner::Jacobi < ValueType, IndexType >
  - A block-Jacobi preconditioner is a block-diagonal linear operator, obtained by inverting the diagonal blocks of the source operator.

## 44.6.1 Detailed Description

A module dedicated to the implementation and usage of the Jacobi Preconditioner in Ginkgo.

# 44.7 Linear Operators

A module dedicated to the implementation and usage of the Linear operators in Ginkgo.

## **Modules**

Factorizations

A module dedicated to the implementation and usage of the Factorizations in Ginkgo.

· SpMV employing different Matrix formats

A module dedicated to the implementation and usage of the various Matrix Formats in Ginkgo.

Preconditioners

A module dedicated to the implementation and usage of the Preconditioners in Ginkgo.

Solvers

A module dedicated to the implementation and usage of the Solvers in Ginkgo.

#### **Classes**

class gko::Combination
 ValueType >

The Combination class can be used to construct a linear combination of multiple linear operators  $c1 * op1 + c2 * op2 + \dots$ 

class gko::Composition < ValueType >

The Composition class can be used to compose linear operators op1, op2, ..., opn and obtain the operator op1 \* op2 \* ...

class gko::LinOpFactory

A LinOpFactory represents a higher order mapping which transforms one linear operator into another.

class gko::ReadableFromMatrixData< ValueType, IndexType >

A LinOp implementing this interface can read its data from a matrix\_data structure.

 $\bullet \ \ {\it class gko::} Writable {\it ToMatrixData} < \ {\it ValueType, IndexType} >$ 

A LinOp implementing this interface can write its data to a matrix\_data structure.

· class gko::Preconditionable

A LinOp implementing this interface can be preconditioned.

· class gko::DiagonalLinOpExtractable

The diagonal of a LinOp can be extracted.

class gko::DiagonalExtractable< ValueType >

The diagonal of a LinOp implementing this interface can be extracted.

class gko::EnableAbsoluteComputation< AbsoluteLinOp >

The EnableAbsoluteComputation mixin provides the default implementations of compute\_absolute\_linop and the absolute interface.

class gko::EnableLinOp
 ConcreteLinOp
 PolymorphicBase

The EnableLinOp mixin can be used to provide sensible default implementations of the majority of the LinOp and PolymorphicObject interface.

 $\bullet \ \ {\it class gko::} Perturbation < \ \ {\it ValueType} >$ 

The Perturbation class can be used to construct a LinOp to represent the operation (identity + scalar \* basis \* projector).

 $\bullet \ \, {\it class gko::experimental::Enable Distributed Lin Op < Concrete Lin Op, Polymorphic Base > } \\$ 

This mixin does the same as EnableLinOp, but for concrete types that are derived from distributed::DistributedBase.

• class gko::experimental::distributed::preconditioner::Schwarz< ValueType, LocalIndexType, GlobalIndexType >

A Schwarz preconditioner is a simple domain decomposition preconditioner that generalizes the Block Jacobi preconditioner, incorporating options for different local subdomain solvers and overlaps between the subdomains.

class gko::experimental::distributed::Vector< ValueType >

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Vector is a format which explicitly stores (multiple) distributed column vectors in a dense storage format.

class gko::factorization::lc
 ValueType, IndexType >

Represents an incomplete Cholesky factorization (IC(0)) of a sparse matrix.

class gko::factorization::llu
 ValueType, IndexType

Represents an incomplete LU factorization – ILU(0) – of a sparse matrix.

class gko::factorization::ParIc< ValueType, IndexType >

ParIC is an incomplete Cholesky factorization which is computed in parallel.

class gko::factorization::ParIct< ValueType, IndexType >

ParICT is an incomplete threshold-based Cholesky factorization which is computed in parallel.

class gko::factorization::Parllu
 ValueType, IndexType

ParILU is an incomplete LU factorization which is computed in parallel.

class gko::factorization::Parllut< ValueType, IndexType >

ParILUT is an incomplete threshold-based LU factorization which is computed in parallel.

class gko::matrix::Coo< ValueType, IndexType >

COO stores a matrix in the coordinate matrix format.

class gko::matrix::Csr< ValueType, IndexType >

CSR is a matrix format which stores only the nonzero coefficients by compressing each row of the matrix (compressed sparse row format).

class gko::matrix::Dense< ValueType >

Dense is a matrix format which explicitly stores all values of the matrix.

class gko::matrix::Diagonal
 ValueType >

This class is a utility which efficiently implements the diagonal matrix (a linear operator which scales a vector row wise).

class gko::matrix::Ell< ValueType, IndexType >

ELL is a matrix format where stride with explicit zeros is used such that all rows have the same number of stored elements.

class gko::matrix::Fbcsr< ValueType, IndexType >

Fixed-block compressed sparse row storage matrix format.

· class gko::matrix::Fft

This LinOp implements a 1D Fourier matrix using the FFT algorithm.

class gko::matrix::Fft2

This LinOp implements a 2D Fourier matrix using the FFT algorithm.

class gko::matrix::Fft3

This LinOp implements a 3D Fourier matrix using the FFT algorithm.

class gko::matrix::Hybrid< ValueType, IndexType >

HYBRID is a matrix format which splits the matrix into ELLPACK and COO format.

class gko::matrix::Identity< ValueType >

This class is a utility which efficiently implements the identity matrix (a linear operator which maps each vector to itself).

class gko::matrix::IdentityFactory< ValueType >

This factory is a utility which can be used to generate Identity operators.

class gko::matrix::Permutation< IndexType >

Permutation is a matrix format that represents a permutation matrix, i.e.

class gko::matrix::RowGatherer< IndexType >

RowGatherer is a matrix "format" which stores the gather indices arrays which can be used to gather rows to another matrix

class gko::matrix::ScaledPermutation
 ValueType, IndexType >

ScaledPermutation is a matrix combining a permutation with scaling factors.

class gko::matrix::Sellp< ValueType, IndexType >

SELL-P is a matrix format similar to ELL format.

- class gko::matrix::SparsityCsr< ValueType, IndexType >

SparsityCsr is a matrix format which stores only the sparsity pattern of a sparse matrix by compressing each row of the matrix (compressed sparse row format).

class gko::multigrid::FixedCoarsening
 ValueType, IndexType >

FixedCoarsening is a very simple coarse grid generation algorithm.

class gko::multigrid::Pgm< ValueType, IndexType >

Parallel graph match (Pgm) is the aggregate method introduced in the paper M.

class gko::preconditioner::lc< LSolverType, IndexType >

The Incomplete Cholesky (IC) preconditioner solves the equation  $LL^H*x=b$  for a given lower triangular matrix L and the right hand side b (can contain multiple right hand sides).

class gko::preconditioner::llu< LSolverType, USolverType, ReverseApply, IndexType >

The Incomplete LU (ILU) preconditioner solves the equation LUx = b for a given lower triangular matrix L, an upper triangular matrix U and the right hand side b (can contain multiple right hand sides).

class gko::preconditioner::lsai< lsaiType, ValueType, IndexType >

The Incomplete Sparse Approximate Inverse (ISAI) Preconditioner generates an approximate inverse matrix for a given square matrix A, lower triangular matrix L, upper triangular matrix U or symmetric positive (spd) matrix B.

class gko::preconditioner::Jacobi< ValueType, IndexType >

A block-Jacobi preconditioner is a block-diagonal linear operator, obtained by inverting the diagonal blocks of the source operator.

class gko::solver::Bicg< ValueType >

BICG or the Biconjugate gradient method is a Krylov subspace solver.

class gko::solver::Bicgstab
 ValueType >

BiCGSTAB or the Bi-Conjugate Gradient-Stabilized is a Krylov subspace solver.

class gko::solver::CbGmres
 ValueType >

CB-GMRES or the compressed basis generalized minimal residual method is an iterative type Krylov subspace method which is suitable for nonsymmetric linear systems.

class gko::solver::Cg< ValueType >

CG or the conjugate gradient method is an iterative type Krylov subspace method which is suitable for symmetric positive definite methods.

class gko::solver::Cgs< ValueType >

CGS or the conjugate gradient square method is an iterative type Krylov subspace method which is suitable for general systems.

class gko::solver::Fcg< ValueType >

FCG or the flexible conjugate gradient method is an iterative type Krylov subspace method which is suitable for symmetric positive definite methods.

class gko::solver::Gcr< ValueType >

GCR or the generalized conjugate residual method is an iterative type Krylov subspace method similar to GMRES which is suitable for nonsymmetric linear systems.

class gko::solver::Gmres < ValueType >

GMRES or the generalized minimal residual method is an iterative type Krylov subspace method which is suitable for nonsymmetric linear systems.

class gko::solver::ldr< ValueType >

IDR(s) is an efficient method for solving large nonsymmetric systems of linear equations.

class gko::solver::Ir< ValueType >

Iterative refinement (IR) is an iterative method that uses another coarse method to approximate the error of the current solution via the current residual.

· class gko::solver::Multigrid

Multigrid methods have a hierarchy of many levels, whose corase level is a subset of the fine level, of the problem.

class gko::solver::EnableSolverBase< DerivedType, MatrixType >

A LinOp deriving from this CRTP class stores a system matrix.

class gko::solver::IterativeBase

A LinOp implementing this interface stores a stopping criterion factory.

class gko::solver::EnableIterativeBase
 DerivedType >

A LinOp deriving from this CRTP class stores a stopping criterion factory and allows applying with a guess.

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class gko::solver::EnablePreconditionedIterativeSolver< ValueType, DerivedType >

A LinOp implementing this interface stores a system matrix and stopping criterion factory.

class gko::solver::LowerTrs< ValueType, IndexType >

Lower Trs is the triangular solver which solves the system L x = b, when L is a lower triangular matrix.

class gko::solver::UpperTrs< ValueType, IndexType >

UpperTrs is the triangular solver which solves the system U x = b, when U is an upper triangular matrix.

### **Macros**

#define GKO\_CREATE\_FACTORY\_PARAMETERS(\_parameters\_name, \_factory\_name)

This Macro will generate a new type containing the parameters for the factory\_factory\_name.

#define GKO\_ENABLE\_BUILD\_METHOD(\_factory\_name)

Defines a build method for the factory, simplifying its construction by removing the repetitive typing of factory's name.

#define GKO\_FACTORY\_PARAMETER(\_name, ...)

Creates a factory parameter in the factory parameters structure.

 #define GKO\_FACTORY\_PARAMETER\_SCALAR(\_name, \_default) GKO\_FACTORY\_PARAMETER(\_← name, default)

Creates a scalar factory parameter in the factory parameters structure.

Creates a vector factory parameter in the factory parameters structure.

• #define GKO\_ENABLE\_LIN\_OP\_FACTORY(\_lin\_op, \_parameters\_name, \_factory\_name)

This macro will generate a default implementation of a LinOpFactory for the LinOp subclass it is defined in.

## **Typedefs**

template < typename ConcreteFactory , typename ConcreteLinOp , typename ParametersType , typename PolymorphicBase = Lin←OpFactory>

using gko::EnableDefaultLinOpFactory = EnableDefaultFactory< ConcreteFactory, ConcreteLinOpFactory = EnableDefaultFactory< ConcreteFactory, ConcreteLinOpFactory = EnableDefaultFactory< ConcreteFactory, ConcreteLinOpFactory = EnableDefaultFactory< ConcreteFactory, ConcreteFactor

This is an alias for the EnableDefaultFactory mixin, which correctly sets the template parameters to enable a subclass of LinOpFactory.

## **Functions**

template<typename Matrix , typename... TArgs>
 std::unique\_ptr< Matrix > gko::initialize (size\_type stride, std::initializer\_list< typename Matrix::value\_type
 > vals, std::shared\_ptr< const Executor > exec, TArgs &&... create\_args)

Creates and initializes a column-vector.

template < typename Matrix , typename... TArgs > std::unique\_ptr < Matrix > gko::initialize (std::initializer\_list < typename Matrix::value\_type > vals, std ← ::shared\_ptr < const Executor > exec, TArgs &&... create\_args)

Creates and initializes a column-vector.

template<typename Matrix , typename... TArgs>
 std::unique\_ptr< Matrix > gko::initialize (size\_type stride, std::initializer\_list< std::initializer\_list< typename
 Matrix::value\_type >> vals, std::shared\_ptr< const Executor > exec, TArgs &&... create\_args)

Creates and initializes a matrix.

template<typename Matrix , typename... TArgs>
 std::unique\_ptr< Matrix > gko::initialize (std::initializer\_list< std::initializer\_list< typename Matrix::value\_
 type >> vals, std::shared\_ptr< const Executor > exec, TArgs &&... create\_args)

Creates and initializes a matrix.

## 44.7.1 Detailed Description

A module dedicated to the implementation and usage of the Linear operators in Ginkgo.

Below we elaborate on one of the most important concepts of Ginkgo, the linear operator. The linear operator (LinOp) is a base class for all linear algebra objects in Ginkgo. The main benefit of having a single base class for the entire collection of linear algebra objects (as opposed to having separate hierarchies for matrices, solvers and preconditioners) is the generality it provides.

## 44.7.2 Advantages of this approach and usage

A common interface often allows for writing more generic code. If a user's routine requires only operations provided by the LinOp interface, the same code can be used for any kind of linear operators, independent of whether these are matrices, solvers or preconditioners. This feature is also extensively used in Ginkgo itself. For example, a preconditioner used inside a Krylov solver is a LinOp. This allows the user to supply a wide variety of preconditioners: either the ones which were designed to be used in this scenario (like ILU or block-Jacobi), a user-supplied matrix which is known to be a good preconditioner for the specific problem, or even another solver (e.g., if constructing a flexible GMRES solver).

For example, a matrix free implementation would require the user to provide an apply implementation and instead of passing the generated matrix to the solver, they would have to provide their apply implementation for all the executors needed and no other code needs to be changed. See The custom-matrix-format program example for more details.

## 44.7.3 Linear operator as a concept

The linear operator (LinOp) is a base class for all linear algebra objects in Ginkgo. The main benefit of having a single base class for the entire collection of linear algebra objects (as opposed to having separate hierarchies for matrices, solvers and preconditioners) is the generality it provides.

First, since all subclasses provide a common interface, the library users are exposed to a smaller set of routines. For example, a matrix-vector product, a preconditioner application, or even a system solve are just different terms given to the operation of applying a certain linear operator to a vector. As such, Ginkgo uses the same routine name, LinOp::apply() for each of these operations, where the actual operation performed depends on the type of linear operator involved in the operation.

Second, a common interface often allows for writing more generic code. If a user's routine requires only operations provided by the LinOp interface, the same code can be used for any kind of linear operators, independent of whether these are matrices, solvers or preconditioners. This feature is also extensively used in Ginkgo itself. For example, a preconditioner used inside a Krylov solver is a LinOp. This allows the user to supply a wide variety of preconditioners: either the ones which were designed to be used in this scenario (like ILU or block-Jacobi), a user-supplied matrix which is known to be a good preconditioner for the specific problem, or even another solver (e.g., if constructing a flexible GMRES solver).

A key observation for providing a unified interface for matrices, solvers, and preconditioners is that the most common operation performed on all of them can be expressed as an application of a linear operator to a vector:

- the sparse matrix-vector product with a matrix A is a linear operator application y = Ax;
- the application of a preconditioner is a linear operator application  $y = M^{-1}x$ , where M is an approximation of the original system matrix A (thus a preconditioner represents an "approximate inverse" operator  $M^{-1}$ ).
- the system solve Ax = b can be viewed as linear operator application  $x = A^{-1}b$  (it goes without saying that the implementation of linear system solves does not follow this conceptual idea), so a linear system solver can be viewed as a representation of the operator  $A^{-1}$ .

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Finally, direct manipulation of LinOp objects is rarely required in simple scenarios. As an illustrative example, one could construct a fixed-point iteration routine  $x_{k+1} = Lx_k + b$  as follows:

```
std::unique_ptr<matrix::Dense<» calculate_fixed_point(
    int iters, const LinOp *L, const matrix::Dense<> *x0
    const matrix::Dense<> *b)
{
    auto x = gko::clone(x0);
    auto tmp = gko::clone(x0);
    auto one = Dense<>::create(L->get_executor(), {1.0,});
    for (int i = 0; i < iters; ++i) {
        L->apply(tmp, x);
        x->add_scaled(one, b);
        tmp->copy_from(x);
    }
    return x;
}
```

Here, if L is a matrix, LinOp::apply() refers to the matrix vector product, and L->apply(a, b) computes  $b = L \cdot a$ . x->add\_scaled(one, b) is the axpy vector update x := x + b.

The interesting part of this example is the apply() routine at line 4 of the function body. Since this routine is part of the LinOp base class, the fixed-point iteration routine can calculate a fixed point not only for matrices, but for any type of linear operator.

**Linear Operators** 

#### 44.7.4 Macro Definition Documentation

## 44.7.4.1 GKO\_CREATE\_FACTORY\_PARAMETERS

This Macro will generate a new type containing the parameters for the factory \_factory\_name.

For more details, see GKO\_ENABLE\_LIN\_OP\_FACTORY(). It is required to use this macro before calling the macro GKO\_ENABLE\_LIN\_OP\_FACTORY(). It is also required to use the same names for all parameters between both macros.

#### **Parameters**

_parameters_name	name of the parameters member in the class
_factory_name	name of the generated factory type

## 44.7.4.2 GKO\_ENABLE\_BUILD\_METHOD

Defines a build method for the factory, simplifying its construction by removing the repetitive typing of factory's name.

#### **Parameters**

#### 44.7.4.3 GKO ENABLE LIN OP FACTORY

This macro will generate a default implementation of a LinOpFactory for the LinOp subclass it is defined in.

It is required to first call the macro GKO\_CREATE\_FACTORY\_PARAMETERS() before this one in order to instantiate the parameters type first.

The list of parameters for the factory should be defined in a code block after the macro definition, and should contain a list of GKO\_FACTORY\_PARAMETER\_\* declarations. The class should provide a constructor with signature  $\leftarrow$  \_lin\_op(const \_factory\_name \*, std::shared\_ptr<const LinOp>) which the factory will use a callback to construct the object.

A minimal example of a linear operator is the following:

auto my\_op = fact->generate(gko::matrix::Identity::create(exec, 2));
std::cout « my\_op->get\_my\_parameters().my\_value; // prints 0

""c++ struct MyLinOp: public EnableLinOp<MyLinOp> { GKO\_ENABLE\_LIN\_OP\_FACTORY(MyLinOp, my\_parameters, Factory) { // a factory parameter named "my\_value", of type int and default // value of 5 int GKO\_FACTORY\_PARAMETER\_SCALAR(my\_value, // a factory parameter named my\_pair of type std::pair<int,int>// and default value {5, 5} std::pair<int, int> GKO\_FACTORY\_PARAMETER\_VECTOR(my\_pair, 5, 5); }; // constructor needed by EnableLinOp explicit MyLinOp(std::shared\_ptr<const Executor> exec) { : EnableLinOp<MyLinOp>(exec) {} // constructor needed by the factory explicit MyLinOp(const Factory \*factory, std::shared\_ptr<const LinOp> matrix) : EnableLinOp<← MyLinOp>(factory->get\_executor()), matrix->get\_size()), // store factory's parameters locally my\_parameters\_← {factory->get\_parameters()}, { int value = my\_parameters\_.my\_value; // do something with value } MyLinOp can then be created as follows: `c++ auto exec = gko::ReferenceExecutor::create(); // create a factory with default 'my\_value' parameter auto fact = MyLinOp::build().on(exec); // create a operator using the factory: auto my\_op = fact->generate(gko::matrix::Identity::create(exec, 2)); std::cout « my\_op->get\_my\_parameters().my\_value; // prints 5
// create a factory with custom 'my\_value' parameter auto fact = MyLinOp::build().with\_my\_value(0).on(exec); // create a operator using the factory:

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#### Note

It is possible to combine both the #GKO\_CREATE\_FACTORY\_PARAMETER\_\*() macros with this one in a unique macro for class **templates** (not with regular classes). Splitting this into two distinct macros allows to use them in all contexts. See <a href="https://stackoverflow.com/q/50202718/9385966">https://stackoverflow.com/q/50202718/9385966</a> for more details.

#### **Parameters**

_lin_op	concrete operator for which the factory is to be created [CRTP parameter]
_parameters_name	name of the parameters member in the class (its type is
	<pre>&lt;_parameters_name&gt;_type, the protected member's name is</pre>
	<_parameters_name>_, and the public getter's name is
	<pre>get_&lt;_parameters_name&gt;())</pre>
_factory_name	name of the generated factory type

#### 44.7.4.4 GKO\_FACTORY\_PARAMETER

Creates a factory parameter in the factory parameters structure.

#### **Parameters**

_name	name of the parameter
<strong>VA_ARGS</strong>	default value of the parameter

#### See also

GKO\_ENABLE\_LIN\_OP\_FACTORY for more details, and usage example

## 44.7.4.5 GKO\_FACTORY\_PARAMETER\_SCALAR

Creates a scalar factory parameter in the factory parameters structure.

Scalar in this context means that the constructor for this type only takes a single parameter.

#### **Parameters**

_name	name of the parameter
_default	default value of the parameter

#### See also

GKO\_ENABLE\_LIN\_OP\_FACTORY for more details, and usage example

## 44.7.4.6 GKO\_FACTORY\_PARAMETER\_VECTOR

Creates a vector factory parameter in the factory parameters structure.

Vector in this context means that the constructor for this type takes multiple parameters.

#### **Parameters**

_n	ame	name of the parameter
_a	lefault	default value of the parameter

## See also

GKO\_ENABLE\_LIN\_OP\_FACTORY for more details, and usage example

## 44.7.5 Typedef Documentation

## 44.7.5.1 EnableDefaultLinOpFactory

```
template<typename ConcreteFactory , typename ConcreteLinOp , typename ParametersType , typename PolymorphicBase = LinOpFactory> using gko::EnableDefaultLinOpFactory = typedef EnableDefaultFactory<ConcreteFactory, Concrete← LinOp, ParametersType, PolymorphicBase>
```

This is an alias for the EnableDefaultFactory mixin, which correctly sets the template parameters to enable a subclass of LinOpFactory.

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#### **Template Parameters**

ConcreteFactory	the concrete factory which is being implemented [CRTP parameter]
ConcreteLinOp	the concrete LinOp type which this factory produces, needs to have a constructor which takes a const ConcreteFactory *, and an std::shared_ptr <const linop=""> as parameters.</const>
	takes a const concrete actory *, and an statishated_pti \const cinop \rangle as parameters.
ParametersType	a subclass of enable_parameters_type template which defines all of the parameters of the factory
PolymorphicBase	parent of ConcreteFactory in the polymorphic hierarchy, has to be a subclass of LinOpFactory

## 44.7.6 Function Documentation

# 44.7.6.1 initialize() [1/4]

Creates and initializes a matrix.

This function first creates a temporary Dense matrix, fills it with passed in values, and then converts the matrix to the requested type.

## **Template Parameters**

Ма	trix	matrix type to initialize (Dense has to implement the ConvertibleTo <matrix> interface)</matrix>
TA	rgs	argument types for Matrix::create method (not including the implied Executor as the first argument)

## Parameters

stride	row stride for the temporary Dense matrix
vals	values used to initialize the matrix
exec	Executor associated to the matrix
create_args	additional arguments passed to Matrix::create, not including the Executor, which is passed as
	the first argument

```
1612 {
            using dense = matrix::Dense<typename Matrix::value_type>;
1613
            size_type num_rows = vals.size();
size_type num_cols = num_rows > 0 ? begin(vals) -> size() : 1;
1614
1615
1616
           auto tmp =
1617
                 dense::create(exec->get_master(), dim<2>{num_rows, num_cols}, stride);
1618
            size_type ridx = 0;
          size_type ridx - o;
for (const auto& row : vals) {
    size_type cidx = 0;
    for (const auto& elem : row) {
        tmp->at(ridx, cidx) = elem;
}
1619
1620
1621
1622
1623
                        ++cidx;
```

References gko::matrix::Dense< ValueType >::at().

#### 44.7.6.2 initialize() [2/4]

Creates and initializes a column-vector.

This function first creates a temporary Dense matrix, fills it with passed in values, and then converts the matrix to the requested type.

#### **Template Parameters**

Matrix	matrix type to initialize (Dense has to implement the ConvertibleTo <matrix> interface)</matrix>
TArgs	argument types for Matrix::create method (not including the implied Executor as the first argument)

#### Parameters

stride	row stride for the temporary Dense matrix
vals	values used to initialize the vector
exec	Executor associated to the vector
create_args	additional arguments passed to Matrix::create, not including the Executor, which is passed as the first argument

References gko::matrix::Dense< ValueType >::at().

## 44.7.6.3 initialize() [3/4]

Creates and initializes a matrix.

This function first creates a temporary Dense matrix, fills it with passed in values, and then converts the matrix to the requested type. The stride of the intermediate Dense matrix is set to the number of columns of the initializer list.

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# **Template Parameters**

Matrix	matrix type to initialize (Dense has to implement the ConvertibleTo <matrix> interface)</matrix>
TArgs	argument types for Matrix::create method (not including the implied Executor as the first argument)

#### **Parameters**

vals	values used to initialize the matrix
exec	Executor associated to the matrix
create_args	additional arguments passed to Matrix::create, not including the Executor, which is passed as the first argument

# 44.7.6.4 initialize() [4/4]

Creates and initializes a column-vector.

This function first creates a temporary Dense matrix, fills it with passed in values, and then converts the matrix to the requested type. The stride of the intermediate Dense matrix is set to 1.

## **Template Parameters**

Matrix	matrix type to initialize (Dense has to implement the ConvertibleTo <matrix> interface)</matrix>
TArgs	argument types for Matrix::create method (not including the implied Executor as the first argument)

# **Parameters**

vals	values used to initialize the vector
exec	Executor associated to the vector
create_args	additional arguments passed to Matrix::create, not including the Executor, which is passed as the first argument

# 44.8 Logging

A module dedicated to the implementation and usage of the Logging in Ginkgo.

# **Namespaces**

• gko::batch::log

The logger namespace.

• gko::log

The logger namespace.

#### Classes

class gko::batch::log::BatchConvergence
 ValueType >

Logs the final residuals and iteration counts for a batch solver.

class gko::log::Convergence < ValueType >

Convergence is a Logger which logs data strictly from the criterion\_check\_completed event.

class gko::log::Papi< ValueType >

Papi is a Logger which logs every event to the PAPI software.

• class gko::log::PerformanceHint

PerformanceHint is a Logger which analyzes the performance of the application and outputs hints for unnecessary copies and allocations.

class gko::log::Stream
 ValueType >

Stream is a Logger which logs every event to a stream.

# 44.8.1 Detailed Description

A module dedicated to the implementation and usage of the Logging in Ginkgo.

The Logger class represents a simple Logger object. It comprises all masks and events internally. Every new logging event addition should be done here. The Logger class also provides a default implementation for most events which do nothing, therefore it is not an obligation to change all classes which derive from Logger, although it is good practice. The logger class is built using event masks to control which events should be logged, and which should not.

# 44.9 SpMV employing different Matrix formats

A module dedicated to the implementation and usage of the various Matrix Formats in Ginkgo.

#### **Classes**

class gko::experimental::distributed::Vector< ValueType >

Vector is a format which explicitly stores (multiple) distributed column vectors in a dense storage format.

class gko::batch::matrix::Csr< ValueType, IndexType >

Csr is a general sparse matrix format that stores the column indices for each nonzero entry and a cumulative sum of the number of nonzeros in each row.

class gko::batch::matrix::Dense< ValueType >

Dense is a batch matrix format which explicitly stores all values of the matrix in each of the batches.

class gko::batch::matrix::Ell< ValueType, IndexType >

Ell is a sparse matrix format that stores the same number of nonzeros in each row, enabling coalesced accesses.

class gko::batch::matrix::Identity< ValueType >

The batch Identity matrix, which represents a batch of Identity matrices.

class gko::matrix::Coo< ValueType, IndexType >

COO stores a matrix in the coordinate matrix format.

class gko::matrix::Csr< ValueType, IndexType >

CSR is a matrix format which stores only the nonzero coefficients by compressing each row of the matrix (compressed sparse row format).

class gko::matrix::Dense
 ValueType >

Dense is a matrix format which explicitly stores all values of the matrix.

class gko::matrix::Diagonal
 ValueType >

This class is a utility which efficiently implements the diagonal matrix (a linear operator which scales a vector row wise).

class gko::matrix::Ell< ValueType, IndexType >

ELL is a matrix format where stride with explicit zeros is used such that all rows have the same number of stored elements.

class gko::matrix::Fbcsr< ValueType, IndexType >

Fixed-block compressed sparse row storage matrix format.

class gko::matrix::Fft

This LinOp implements a 1D Fourier matrix using the FFT algorithm.

class gko::matrix::Fft2

This LinOp implements a 2D Fourier matrix using the FFT algorithm.

class gko::matrix::Fft3

This LinOp implements a 3D Fourier matrix using the FFT algorithm.

- class gko::matrix::Hybrid< ValueType, IndexType >

HYBRID is a matrix format which splits the matrix into ELLPACK and COO format.

class gko::matrix::Identity < ValueType >

This class is a utility which efficiently implements the identity matrix (a linear operator which maps each vector to itself)

class gko::matrix::IdentityFactory
 ValueType >

This factory is a utility which can be used to generate Identity operators.

class gko::matrix::Permutation< IndexType >

Permutation is a matrix format that represents a permutation matrix, i.e.

class gko::matrix::ScaledPermutation< ValueType, IndexType >

ScaledPermutation is a matrix combining a permutation with scaling factors.

class gko::matrix::Sellp< ValueType, IndexType >

SELL-P is a matrix format similar to ELL format.

class gko::matrix::SparsityCsr< ValueType, IndexType >

SparsityCsr is a matrix format which stores only the sparsity pattern of a sparse matrix by compressing each row of the matrix (compressed sparse row format).

# 44.9.1 Detailed Description

A module dedicated to the implementation and usage of the various Matrix Formats in Ginkgo.

# 44.10 OpenMP Executor

A module dedicated to the implementation and usage of the OpenMP executor in Ginkgo.

# **Classes**

• class gko::OmpExecutor

This is the Executor subclass which represents the OpenMP device (typically CPU).

# 44.10.1 Detailed Description

A module dedicated to the implementation and usage of the OpenMP executor in Ginkgo.

# 44.11 Preconditioners

A module dedicated to the implementation and usage of the Preconditioners in Ginkgo.

#### **Modules**

· Jacobi Preconditioner

A module dedicated to the implementation and usage of the Jacobi Preconditioner in Ginkgo.

# **Namespaces**

· gko::experimental::distributed::preconditioner

The Preconditioner namespace.

· gko::preconditioner

The Preconditioner namespace.

#### Classes

· class gko::Preconditionable

A LinOp implementing this interface can be preconditioned.

class gko::experimental::distributed::preconditioner::Schwarz< ValueType, LocalIndexType, GlobalIndexType >

A Schwarz preconditioner is a simple domain decomposition preconditioner that generalizes the Block Jacobi preconditioner, incorporating options for different local subdomain solvers and overlaps between the subdomains.

class gko::batch::preconditioner::Jacobi< ValueType, IndexType >

A block-Jacobi preconditioner is a block-diagonal linear operator, obtained by inverting the diagonal blocks (stored in a dense row major fashion) of the source operator.

class gko::preconditioner::lc< LSolverType, IndexType >

The Incomplete Cholesky (IC) preconditioner solves the equation  $LL^H * x = b$  for a given lower triangular matrix L and the right hand side b (can contain multiple right hand sides).

class gko::preconditioner::Ilu< LSolverType, USolverType, ReverseApply, IndexType >

The Incomplete LU (ILU) preconditioner solves the equation LUx = b for a given lower triangular matrix L, an upper triangular matrix U and the right hand side b (can contain multiple right hand sides).

class gko::preconditioner::lsai< lsaiType, ValueType, IndexType >

The Incomplete Sparse Approximate Inverse (ISAI) Preconditioner generates an approximate inverse matrix for a given square matrix A, lower triangular matrix L, upper triangular matrix U or symmetric positive (spd) matrix B.

class gko::preconditioner::Jacobi < ValueType, IndexType >

A block-Jacobi preconditioner is a block-diagonal linear operator, obtained by inverting the diagonal blocks of the source operator.

# 44.11.1 Detailed Description

A module dedicated to the implementation and usage of the Preconditioners in Ginkgo.

44.12 Reference Executor 305

# 44.12 Reference Executor

A module dedicated to the implementation and usage of the Reference executor in Ginkgo.

# **Classes**

• class gko::ReferenceExecutor

This is a specialization of the OmpExecutor, which runs the reference implementations of the kernels used for debugging purposes.

# 44.12.1 Detailed Description

A module dedicated to the implementation and usage of the Reference executor in Ginkgo.

#### 44.13 Solvers

A module dedicated to the implementation and usage of the Solvers in Ginkgo.

# **Namespaces**

· gko::solver

The ginkgo Solve namespace.

#### Classes

class gko::batch::solver::Bicgstab < ValueType >

BiCGSTAB or the Bi-Conjugate Gradient-Stabilized is a Krylov subspace solver.

class gko::batch::solver::Cg< ValueType >

Cg or the Conjugate Gradient is a Krylov subspace solver.

class gko::batch::solver::BatchSolver

The BatchSolver is a base class for all batched solvers and provides the common getters and setter for these batched solver classes.

class gko::solver::Bicg< ValueType >

BICG or the Biconjugate gradient method is a Krylov subspace solver.

class gko::solver::Bicgstab < ValueType >

BiCGSTAB or the Bi-Conjugate Gradient-Stabilized is a Krylov subspace solver.

class gko::solver::CbGmres< ValueType >

CB-GMRES or the compressed basis generalized minimal residual method is an iterative type Krylov subspace method which is suitable for nonsymmetric linear systems.

class gko::solver::Cg< ValueType >

CG or the conjugate gradient method is an iterative type Krylov subspace method which is suitable for symmetric positive definite methods.

class gko::solver::Cgs< ValueType >

CGS or the conjugate gradient square method is an iterative type Krylov subspace method which is suitable for general systems.

class gko::solver::Fcg< ValueType >

FCG or the flexible conjugate gradient method is an iterative type Krylov subspace method which is suitable for symmetric positive definite methods.

class gko::solver::Gcr< ValueType >

GCR or the generalized conjugate residual method is an iterative type Krylov subspace method similar to GMRES which is suitable for nonsymmetric linear systems.

class gko::solver::Gmres < ValueType >

GMRES or the generalized minimal residual method is an iterative type Krylov subspace method which is suitable for nonsymmetric linear systems.

class gko::solver::ldr< ValueType >

IDR(s) is an efficient method for solving large nonsymmetric systems of linear equations.

class gko::solver::Ir< ValueType >

Iterative refinement (IR) is an iterative method that uses another coarse method to approximate the error of the current solution via the current residual.

· class gko::solver::Multigrid

Multigrid methods have a hierarchy of many levels, whose corase level is a subset of the fine level, of the problem.

class gko::solver::LowerTrs< ValueType, IndexType >

LowerTrs is the triangular solver which solves the system L x = b, when L is a lower triangular matrix.

class gko::solver::UpperTrs< ValueType, IndexType >

UpperTrs is the triangular solver which solves the system U x = b, when U is an upper triangular matrix.

#### 44.13.1 Detailed Description

A module dedicated to the implementation and usage of the Solvers in Ginkgo.

44.14 Stopping criteria 307

# 44.14 Stopping criteria

A module dedicated to the implementation and usage of the Stopping Criteria in Ginkgo.

#### **Namespaces**

gko::stop

The Stopping criterion namespace.

# Classes

class gko::stop::Combined

The Combined class is used to combine multiple criterions together through an OR operation.

class gko::stop::Iteration

The Iteration class is a stopping criterion which stops the iteration process after a preset number of iterations.

class gko::stop::ResidualNormBase
 ValueType >

The ResidualNormBase class provides a framework for stopping criteria related to the residual norm.

class gko::stop::ResidualNorm< ValueType >

The ResidualNorm class is a stopping criterion which stops the iteration process when the actual residual norm is below a certain threshold relative to.

class gko::stop::ImplicitResidualNorm< ValueType >

The ImplicitResidualNorm class is a stopping criterion which stops the iteration process when the implicit residual norm is below a certain threshold relative to.

class gko::stop::ResidualNormReduction< ValueType >

The ResidualNormReduction class is a stopping criterion which stops the iteration process when the residual norm is below a certain threshold relative to the norm of the initial residual, i.e.

class gko::stop::RelativeResidualNorm< ValueType >

The RelativeResidualNorm class is a stopping criterion which stops the iteration process when the residual norm is below a certain threshold relative to the norm of the right-hand side, i.e.

class gko::stop::AbsoluteResidualNorm< ValueType >

The AbsoluteResidualNorm class is a stopping criterion which stops the iteration process when the residual norm is below a certain threshold, i.e.

· class gko::stopping status

This class is used to keep track of the stopping status of one vector.

class gko::stop::Time

The Time class is a stopping criterion which stops the iteration process after a certain amount of time has passed.

# **Enumerations**

· enum gko::stop::mode

The mode for the residual norm criterion.

#### **Functions**

template<typename FactoryContainer >
 std::shared\_ptr< const CriterionFactory > gko::stop::combine (FactoryContainer &&factories)

Combines multiple criterion factories into a single combined criterion factory.

# 44.14.1 Detailed Description

A module dedicated to the implementation and usage of the Stopping Criteria in Ginkgo.

# 44.14.2 Enumeration Type Documentation

#### 44.14.2.1 mode

```
enum gko::stop::mode [strong]
```

The mode for the residual norm criterion.

- absolute: Check for tolerance against residual norm.  $||r|| \leq \tau$
- initial\_resnorm: Check for tolerance relative to the initial residual norm.  $||r|| \le \tau \times ||r_0||$
- rhs\_norm: Check for tolerance relative to the rhs norm.  $||r|| \leq \tau \times ||b||$

```
36 { absolute, initial_resnorm, rhs_norm };
```

# 44.14.3 Function Documentation

# 44.14.3.1 combine()

Combines multiple criterion factories into a single combined criterion factory.

This function treats a singleton container as a special case and avoids creating an additional object and just returns the input factory.

# **Template Parameters**

FactoryContainer a random access container type	е
---	---

#### **Parameters**

factories	a list of factories to combined

#### Returns

a combined criterion factory if the input contains multiple factories or the input factory if the input contains only one factory

```
110 {
111
112
        switch (factories.size()) {
        case 0:
113
            GKO_NOT_SUPPORTED (nullptr);
114
        case 1:
            if (factories[0] == nullptr) {
                 GKO_NOT_SUPPORTED (nullptr);
116
117
118
119
             return factories[0];
        default:
120
            if (factories[0] == nullptr) {
                 // first factory must be valid to capture executor
121
                 GKO_NOT_SUPPORTED(nullptr);
            } else {
123
                auto exec = factories[0]->get_executor();
124
                return Combined::build()
   .with_criteria(std::forward<FactoryContainer>(factories))
125
126
127
                     .on(exec);
128
            }
        }
129
130 }
```

# 44.15 BatchLinOp

#### **Classes**

· class gko::batch::BatchLinOpFactory

A BatchLinOpFactory represents a higher order mapping which transforms one batch linear operator into another.

class gko::batch::EnableBatchLinOp
 ConcreteBatchLinOp
 PolymorphicBase

The EnableBatchLinOp mixin can be used to provide sensible default implementations of the majority of the Batch← LinOp and PolymorphicObject interface.

class gko::batch::matrix::Csr< ValueType, IndexType >

Csr is a general sparse matrix format that stores the column indices for each nonzero entry and a cumulative sum of the number of nonzeros in each row.

class gko::batch::matrix::Dense< ValueType >

Dense is a batch matrix format which explicitly stores all values of the matrix in each of the batches.

class gko::batch::matrix::Ell< ValueType, IndexType >

Ell is a sparse matrix format that stores the same number of nonzeros in each row, enabling coalesced accesses.

class gko::batch::matrix::Identity< ValueType >

The batch Identity matrix, which represents a batch of Identity matrices.

class gko::batch::preconditioner::Jacobi< ValueType, IndexType >

A block-Jacobi preconditioner is a block-diagonal linear operator, obtained by inverting the diagonal blocks (stored in a dense row major fashion) of the source operator.

class gko::batch::solver::Bicgstab < ValueType >

BiCGSTAB or the Bi-Conjugate Gradient-Stabilized is a Krylov subspace solver.

class gko::batch::solver::Cg< ValueType >

Cg or the Conjugate Gradient is a Krylov subspace solver.

# **Macros**

• #define GKO\_ENABLE\_BATCH\_LIN\_OP\_FACTORY(\_batch\_lin\_op, \_parameters\_name, \_factory\_name)

This macro will generate a default implementation of a BatchLinOpFactory for the BatchLinOp subclass it is defined in.

# **Typedefs**

• template<typename ConcreteFactory , typename ConcreteBatchLinOp , typename ParametersType , typename PolymorphicBase = BatchLinOpFactory>

using gko::batch::EnableDefaultBatchLinOpFactory = EnableDefaultFactory< ConcreteFactory, Concrete ← BatchLinOp, ParametersType, PolymorphicBase >

This is an alias for the EnableDefaultFactory mixin, which correctly sets the template parameters to enable a subclass of BatchLinOpFactory.

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# 44.15.1 Detailed Description

# 44.15.2 Batched Linear operator as a concept

A batch linear operator (BatchLinOp) forms the base class for all batched linear algebra objects. In general, it follows the same structure as the LinOp class, but has some crucial differences which make it not strictly representable through or with the LinOp class.

A batched operator is defined as a set of independent linear operators which have no communication/information exchange between them. Therefore, any collective operations between the batches is not possible and not implemented. This allows for each batch to be computed and operated on in an embarrassingly parallel fashion.

A key difference between the LinOp and the BatchLinOp class is that the apply between BatchLinOps is no longer supported. The user can apply a BatchLinOp to a batch::MultiVector but not to any general BatchLinOp.

Therefore, the BatchLinOp serves only as a base class providing necessary core functionality from Polymorphic object and store the dimensions of the batched object.

Note

Apply to batch::MultiVector objects are handled by the concrete LinOp and may be moved to the base Batch 
LinOp class in the future.

BatchLinOp

#### 44.15.3 Macro Definition Documentation

#### 44.15.3.1 GKO\_ENABLE\_BATCH\_LIN\_OP\_FACTORY

This macro will generate a default implementation of a BatchLinOpFactory for the BatchLinOp subclass it is defined in.

It is required to first call the macro GKO\_CREATE\_FACTORY\_PARAMETERS() before this one in order to instantiate the parameters type first.

The list of parameters for the factory should be defined in a code block after the macro definition, and should contain a list of GKO\_FACTORY\_PARAMETER\_\* declarations. The class should provide a constructor with signature \_ batch\_lin\_op(const \_factory\_name \*, std::shared\_ptr<const BatchLinOp>) which the factory will use a callback to construct the object.

A minimal example of a batch linear operator is the following:

""c++ struct MyBatchLinOp: public EnableBatchLinOp<MyBatchLinOp>{GKO\_ENABLE\_BATCH\_LIN\_OP\_FACTORY(MyBatchLinCy { // a factory parameter named "my\_value", of type int and default // value of 5 int GKO\_FACTORY\_PARAMETER\_SCALAR(my\_value, // a factory parameter named my\_pair of type std::pair<int,int> // and default value {5, 5} std::pair<int, int> GKO\_FACTORY\_PARAMETER\_VECTOR(my\_pair, 5, 5); }; // constructor needed by EnableBatchLinOp

explicit MyBatchLinOp(std::shared\_ptr<const Executor> exec) { : EnableBatchLinOp<MyBatchLinOp>(exec) {} // constructor needed by the factory explicit MyBatchLinOp(const Factory \*factory, std::shared\_ptr<const Batch LinOp> matrix) : EnableBatchLinOp<MyBatchLinOp>(factory->get\_executor()), matrix->get\_size()), // store factory's parameters locally my\_parameters\_{factory->get\_parameters()} { int value = my\_parameters\_.my\_value; // do something with value }

```
MyBatchLinOp can then be created as follows:
"`c++
auto exec = gko::ReferenceExecutor::create();
// create a factory with default 'my_value' parameter
auto fact = MyBatchLinOp::build().on(exec);
// create a operator using the factory:
auto my_op = fact->generate(gko::batch::matrix::Identity::create(exec, 2));
std::cout « my_op->get_my_parameters().my_value; // prints 5
// create a factory with custom 'my_value' parameter
auto fact = MyLinOp::build().with_my_value(0).on(exec);
// create a operator using the factory:
auto my_op = fact->generate(gko::batch::matrix::Identity::create(exec, 2));
std::cout « my_op->get_my_parameters().my_value; // prints 0
```

#### Note

It is possible to combine both the #GKO\_CREATE\_FACTORY\_PARAMETER\_\*() macros with this one in a unique macro for class **templates** (not with regular classes). Splitting this into two distinct macros allows to use them in all contexts. See <a href="https://stackoverflow.com/q/50202718/9385966">https://stackoverflow.com/q/50202718/9385966</a> for more details.

#### **Parameters**

_batch_lin_op	concrete operator for which the factory is to be created [CRTP parameter]
_parameters_name	name of the parameters member in the class (its type is
	<pre>&lt;_parameters_name&gt;_type, the protected member's name is</pre>
	<_parameters_name>_, and the public getter's name is
	<pre>get_&lt;_parameters_name&gt;())</pre>
_factory_name	name of the generated factory type

## 44.15.4 Typedef Documentation

#### 44.15.4.1 EnableDefaultBatchLinOpFactory

```
template<typename ConcreteFactory , typename ConcreteBatchLinOp , typename ParametersType , typename PolymorphicBase = BatchLinOpFactory> using gko::batch::EnableDefaultBatchLinOpFactory = typedef EnableDefaultFactory<Concrete↔ Factory, ConcreteBatchLinOp, ParametersType, PolymorphicBase>
```

This is an alias for the EnableDefaultFactory mixin, which correctly sets the template parameters to enable a subclass of BatchLinOpFactory.

#### **Template Parameters**

ConcreteFactory	the concrete factory which is being implemented [CRTP parameter]
ConcreteBatchLinOp	the concrete BatchLinOp type which this factory produces, needs to have a constructor which takes a const ConcreteFactory *, and an std::shared_ptr <const batchlinop=""> as parameters.</const>
ParametersType	a subclass of enable_parameters_type template which defines all of the parameters of the factory
	the factory
PolymorphicBase	parent of ConcreteFactory in the polymorphic hierarchy, has to be a subclass of by Doxygen BatchLinOpFactory

# **Chapter 45**

# **Namespace Documentation**

# 45.1 gko Namespace Reference

The Ginkgo namespace.

# **Namespaces**

accessor

The accessor namespace.

factorization

The Factorization namespace.

log

The logger namespace .

matrix

The matrix namespace.

• multigrid

The multigrid components namespace.

name\_demangling

The name demangling namespace.

• preconditioner

The Preconditioner namespace.

reorder

The Reorder namespace.

solver

The ginkgo Solve namespace.

• stop

The Stopping criterion namespace.

syn

The Synthesizer namespace.

xstd

The namespace for functionalities after C++14 standard.

#### **Classes**

· class AbsoluteComputable

The AbsoluteComputable is an interface that allows to get the component wise absolute of a LinOp.

class AbstractFactory

The AbstractFactory is a generic interface template that enables easy implementation of the abstract factory design pattern.

class AllocationError

AllocationError is thrown if a memory allocation fails.

· class Allocator

Provides generic allocation and deallocation functionality to be used by an Executor.

· class amd device

amd\_device handles the number of executor on Amd devices and have the corresponding recursive\_mutex.

· struct are all integral

Evaluates if all template arguments Args fulfill std::is\_integral.

· class array

An array is a container which encapsulates fixed-sized arrays, stored on the Executor tied to the array.

class BadDimension

BadDimension is thrown if an operation is being applied to a LinOp with bad dimensions.

· struct batch\_dim

A type representing the dimensions of a multidimensional batch object.

class BlockOperator

A BlockOperator represents a linear operator that is partitioned into multiple blocks.

· class BlockSizeError

Error that denotes issues between block sizes and matrix dimensions.

class Combination

The Combination class can be used to construct a linear combination of multiple linear operators  $c1 * op1 + c2 * op2 + \dots$ 

· class Composition

The Composition class can be used to compose linear operators op1, op2, ..., opn and obtain the operator op1 \* op2 \* ...

class ConvertibleTo

ConvertibleTo interface is used to mark that the implementer can be converted to the object of ResultType.

· class CpuAllocator

Allocator using new/delete.

class CpuAllocatorBase

Implement this interface to provide an allocator for OmpExecutor or ReferenceExecutor.

class CpuTimer

A timer using std::chrono::steady\_clock for timing.

struct cpx\_real\_type

Access the underlying real type of a complex number.

class CublasError

CublasError is thrown when a cuBLAS routine throws a non-zero error code.

class cuda\_stream

An RAII wrapper for a custom CUDA stream.

· class CudaAllocator

Allocator using cudaMalloc.

class CudaAllocatorBase

Implement this interface to provide an allocator for CudaExecutor.

class CudaError

CudaError is thrown when a CUDA routine throws a non-zero error code.

class CudaExecutor

This is the Executor subclass which represents the CUDA device.

class CudaTimer

A timer using events for timing on a CudaExecutor.

class CufftError

CufftError is thrown when a cuFFT routine throws a non-zero error code.

class CurandError

CurandError is thrown when a cuRAND routine throws a non-zero error code.

class CusparseError

CusparseError is thrown when a cuSPARSE routine throws a non-zero error code.

· struct default converter

Used to convert objects of type S to objects of type R using static\_cast.

· class deferred factory parameter

Represents a factory parameter of factory type that can either initialized by a pre-existing factory or by passing in a factory\_parameters object whose .on (exec) will be called to instantiate a factory.

class device\_matrix\_data

This type is a device-side equivalent to matrix\_data.

· class DiagonalExtractable

The diagonal of a LinOp implementing this interface can be extracted.

class DiagonalLinOpExtractable

The diagonal of a LinOp can be extracted.

struct dim

A type representing the dimensions of a multidimensional object.

· class DimensionMismatch

DimensionMismatch is thrown if an operation is being applied to LinOps of incompatible size.

class DpcppExecutor

This is the Executor subclass which represents a DPC++ enhanced device.

class DpcppTimer

A timer using kernels for timing on a DpcppExecutor in profiling mode.

· class enable\_parameters\_type

The enable\_parameters\_type mixin is used to create a base implementation of the factory parameters structure.

· class EnableAbsoluteComputation

The EnableAbsoluteComputation mixin provides the default implementations of compute\_absolute\_linop and the absolute interface.

class EnableAbstractPolymorphicObject

This mixin inherits from (a subclass of) PolymorphicObject and provides a base implementation of a new abstract object.

class EnableCreateMethod

This mixin implements a static create() method on ConcreteType that dynamically allocates the memory, uses the passed-in arguments to construct the object, and returns an std::unique\_ptr to such an object.

class EnableDefaultFactory

This mixin provides a default implementation of a concrete factory.

class EnableLinOp

The EnableLinOp mixin can be used to provide sensible default implementations of the majority of the LinOp and PolymorphicObject interface.

· class EnablePolymorphicAssignment

This mixin is used to enable a default PolymorphicObject::copy\_from() implementation for objects that have implemented conversions between them.

class EnablePolymorphicObject

This mixin inherits from (a subclass of) PolymorphicObject and provides a base implementation of a new concrete polymorphic object.

class Error

The Error class is used to report exceptional behaviour in library functions.

· class Executor

The first step in using the Ginkgo library consists of creating an executor.

· class executor deleter

This is a deleter that uses an executor's free method to deallocate the data.

class hip\_stream

An RAII wrapper for a custom HIP stream.

class HipAllocatorBase

Implement this interface to provide an allocator for HipExecutor.

class HipblasError

HipblasError is thrown when a hipBLAS routine throws a non-zero error code.

class HipError

HipError is thrown when a HIP routine throws a non-zero error code.

class HipExecutor

This is the Executor subclass which represents the HIP enhanced device.

class HipfftError

HipfftError is thrown when a hipFFT routine throws a non-zero error code.

· class HiprandError

HiprandError is thrown when a hipRAND routine throws a non-zero error code.

· class HipsparseError

HipsparseError is thrown when a hipSPARSE routine throws a non-zero error code.

· class HipTimer

A timer using events for timing on a HipExecutor.

· class index set

An index set class represents an ordered set of intervals.

class InvalidStateError

Exception thrown if an object is in an invalid state.

class KernelNotFound

KernelNotFound is thrown if Ginkgo cannot find a kernel which satisfies the criteria imposed by the input arguments.

class LinOpFactory

A LinOpFactory represents a higher order mapping which transforms one linear operator into another.

class machine\_topology

The machine topology class represents the hierarchical topology of a machine, including NUMA nodes, cores and PCI Devices.

· class matrix assembly data

This structure is used as an intermediate type to assemble a sparse matrix.

• struct matrix\_data

This structure is used as an intermediate data type to store a sparse matrix.

struct matrix\_data\_entry

Type used to store nonzeros.

class MetisError

MetisError is thrown when METIS routine throws an error code.

class MpiError

MpiError is thrown when a MPI routine throws a non-zero error code.

class NotCompiled

NotCompiled is thrown when attempting to call an operation which is a part of a module that was not compiled on the system.

class NotImplemented

NotImplemented is thrown in case an operation has not yet been implemented (but will be implemented in the future).

class NotSupported

NotSupported is thrown in case it is not possible to perform the requested operation on the given object type.

class null\_deleter

This is a deleter that does not delete the object.

· class nvidia\_device

nvidia\_device handles the number of executor on Nvidia devices and have the corresponding recursive\_mutex.

class OmpExecutor

This is the Executor subclass which represents the OpenMP device (typically CPU).

class Operation

Operations can be used to define functionalities whose implementations differ among devices.

· class OutOfBoundsError

OutOfBoundsError is thrown if a memory access is detected to be out-of-bounds.

class OverflowError

OverflowError is thrown when an index calculation for storage requirements overflows.

class Permutable

Linear operators which support permutation should implement the Permutable interface.

· class Perturbation

The Perturbation class can be used to construct a LinOp to represent the operation (identity + scalar \* basis \* projector).

class PolymorphicObject

A PolymorphicObject is the abstract base for all "heavy" objects in Ginkgo that behave polymorphically.

· class precision reduction

This class is used to encode storage precisions of low precision algorithms.

· class Preconditionable

A LinOp implementing this interface can be preconditioned.

· class ptr param

This class is used for function parameters in the place of raw pointers.

· class range

A range is a multidimensional view of the memory.

class ReadableFromMatrixData

A LinOp implementing this interface can read its data from a matrix\_data structure.

• class ReferenceExecutor

This is a specialization of the OmpExecutor, which runs the reference implementations of the kernels used for debugging purposes.

· class ScaledIdentityAddable

Adds the operation M < -a I + b M for matrix M, identity operator I and scalars a and b, where M is the calling object.

· class scoped device id guard

This move-only class uses RAII to set the device id within a scoped block, if necessary.

struct segmented\_array

A minimal interface for a segmented array.

· struct span

A span is a lightweight structure used to create sub-ranges from other ranges.

· class stopping\_status

This class is used to keep track of the stopping status of one vector.

class StreamError

StreamError is thrown if accessing a stream failed.

class time\_point

An opaque wrapper for a time point generated by a timer.

· class Timer

Represents a generic timer that can be used to record time points and measure time differences on host or device streams.

· class Transposable

Linear operators which support transposition should implement the Transposable interface.

class UnsupportedMatrixProperty

Exception throws if a matrix does not have a property required by a numerical method.

class UseComposition

The UseComposition class can be used to store the composition information in LinOp.

class ValueMismatch

ValueMismatch is thrown if two values are not equal.

struct version

This structure is used to represent versions of various Ginkgo modules.

· class version info

Ginkgo uses version numbers to label new features and to communicate backward compatibility guarantees:

· class WritableToMatrixData

A LinOp implementing this interface can write its data to a matrix\_data structure.

# **Typedefs**

template < typename ConcreteFactory, typename ConcreteLinOp, typename ParametersType, typename PolymorphicBase = LinOp←</li>
 Factory>

```
using EnableDefaultLinOpFactory = EnableDefaultFactory < ConcreteFactory, ConcreteLinOp, Parameters ← Type, PolymorphicBase >
```

This is an alias for the EnableDefaultFactory mixin, which correctly sets the template parameters to enable a subclass of LinOpFactory.

template<typename T >

```
using is complex s = detail::is complex impl< T >
```

Allows to check if T is a complex value during compile time by accessing the value attribute of this struct.

• template<typename T >

```
using is_complex_or_scalar_s = detail::is_complex_or_scalar_impl< T >
```

Allows to check if T is a complex or scalar value during compile time by accessing the value attribute of this struct.

template<typename T >

```
using remove_complex = typename detail::remove_complex_s < T >::type
```

Obtain the type which removed the complex of complex/scalar type or the template parameter of class by accessing the type attribute of this struct.

• template<typename T >

```
using to complex = typename detail::to complex s< T >::type
```

Obtain the type which adds the complex of complex/scalar type or the template parameter of class by accessing the type attribute of this struct.

• template<typename T >

```
using to_real = remove_complex< T >
```

to\_real is alias of remove\_complex

 $\bullet \quad \text{template}{<} \text{typename T} >$ 

```
using next_precision = typename detail::next_precision_impl< T >::type
```

Obtains the next type in the singly-linked precision list.

 $\bullet \ \ \text{template}{<} \text{typename T} >$ 

```
using previous_precision = next_precision < T >
```

Obtains the previous type in the singly-linked precision list.

template<typename T >

```
using reduce_precision = typename detail::reduce_precision_impl< T >::type
```

Obtains the next type in the hierarchy with lower precision than T.

• template<typename T >

```
using increase_precision = typename detail::increase_precision_impl< T >::type
```

Obtains the next type in the hierarchy with higher precision than T.

• template<typename... Ts>

```
using highest_precision = typename detail::highest_precision_variadic< Ts... >::type
```

Obtains the smallest arithmetic type that is able to store elements of all template parameter types exactly.

template<typename T, size\_type Limit = sizeof(uint16) \* byte\_size>
 using truncate\_type = std::conditional\_t< detail::type\_size\_impl< T >::value >=2 \*Limit, typename detail
 ::truncate\_type\_impl< T >::type, T >

Truncates the type by half (by dropping bits), but ensures that it is at least Limit bits wide.

using size\_type = std::size\_t

Integral type used for allocation quantities.

• using int8 = std::int8\_t

8-bit signed integral type.

• using int16 = std::int16\_t

16-bit signed integral type.

using int32 = std::int32\_t

32-bit signed integral type.

• using int64 = std::int64\_t

64-bit signed integral type.

using uint8 = std::uint8\_t

8-bit unsigned integral type.

• using uint16 = std::uint16 t

16-bit unsigned integral type.

• using uint32 = std::uint32\_t

32-bit unsigned integral type.

• using uint64 = std::uint64 t

64-bit unsigned integral type.

• using uintptr = std::uintptr\_t

Unsigned integer type capable of holding a pointer to void.

• using float16 = half

Half precision floating point type.

using float32 = float

Single precision floating point type.

• using float64 = double

Double precision floating point type.

using full\_precision = double

The most precise floating-point type.

• using default\_precision = double

Precision used if no precision is explicitly specified.

#### **Enumerations**

• enum log\_propagation\_mode { log\_propagation\_mode::never, log\_propagation\_mode::automatic }

How Logger events are propagated to their Executor.

enum allocation\_mode

Specify the mode of allocation for CUDA/HIP GPUs.

enum layout\_type { layout\_type::array, layout\_type::coordinate }

Specifies the layout type when writing data in matrix market format.

#### **Functions**

```
• template<typename ValueType >
  ValueType reduce add (const array < ValueType > &input arr, const ValueType init val=0)
     Reduce (sum) the values in the array.

    template<typename ValueType >

  void reduce_add (const array< ValueType > &input_arr, array< ValueType > &result)
     Reduce (sum) the values in the array.

    template<typename ValueType >

  array < ValueType > make array view (std::shared ptr < const Executor > exec, size type size, ValueType
  *data)
     Helper function to create an array view deducing the value type.

    template<typename ValueType >

  detail::const array view < ValueType > make const array view (std::shared ptr < const Executor > exec,
  size type size, const ValueType *data)
     Helper function to create a const array view deducing the value type.
• template<typename DimensionType >
  batch_dim< 2, DimensionType > transpose (const batch_dim< 2, DimensionType > &input)
      Returns a batch dim object with its dimensions swapped for batched operators.

    template<typename DimensionType >

  constexpr dim < 2, DimensionType > transpose (const dim < 2, DimensionType > & dimensions) noexcept
     Returns a dim<2> object with its dimensions swapped.

    template<typename T >

  constexpr bool is complex ()
     Checks if T is a complex type.
template<typename T >
  constexpr bool is_complex_or_scalar ()
      Checks if T is a complex/scalar type.
• template<typename T >
  constexpr reduce_precision < T > round_down (T val)
     Reduces the precision of the input parameter.
• template<typename T >
  constexpr increase precision < T > round up (T val)
     Increases the precision of the input parameter.
· constexpr int64 ceildiv (int64 num, int64 den)
     Performs integer division with rounding up.

    template<typename T >

  constexpr T zero ()
      Returns the additive identity for T.
• template<typename T >
  constexpr T zero (const T &)
     Returns the additive identity for T.
• template<typename T >
  constexpr T one ()
     Returns the multiplicative identity for T.
• template<typename T >
  constexpr T one (const T &)
     Returns the multiplicative identity for T.

    template<typename T >

  constexpr bool is_zero (T value)
     Returns true if and only if the given value is zero.
template<typename T >
  constexpr bool is_nonzero (T value)
```

```
Returns true if and only if the given value is not zero.
• template<typename T >
  constexpr T max (const T &x, const T &y)
      Returns the larger of the arguments.

    template<typename T >

  constexpr T min (const T &x, const T &y)
      Returns the smaller of the arguments.

    template<typename T >

  constexpr auto real (const T &x)
      Returns the real part of the object.

    template<typename T >

  constexpr auto imag (const T &x)
      Returns the imaginary part of the object.

    template<typename T >

  constexpr auto conj (const T &x)
      Returns the conjugate of an object.
template<typename T >
  constexpr auto squared norm (const T &x) -> decltype(real(conj(x) *x))
      Returns the squared norm of the object.
template<typename T >
  constexpr std::enable if t<!is complex s<T>::value, T > abs (const T &x)
      Returns the absolute value of the object.
template<typename T >
  constexpr T pi ()
     Returns the value of pi.

    template<typename T >

  constexpr std::complex < remove complex < T >> unit root (int64 n, int64 k=1)
      Returns the value of exp(2 * pi * i * k / n), i.e.
• template<typename T >
  constexpr uint32 get significant bit (const T &n, uint32 hint=0u) noexcept
      Returns the position of the most significant bit of the number.
• template<typename T >
  constexpr T get_superior_power (const T &base, const T &limit, const T &hint=T{1}) noexcept
      Returns the smallest power of base not smaller than limit.

    template<typename T >

  std::enable_if_t<!is_complex_s< T>::value, bool > is_finite (const T &value)
      Checks if a floating point number is finite, meaning it is neither +/- infinity nor NaN.

    template<typename T >

  std::enable if t< is complex s< T>::value, bool > is finite (const T &value)
      Checks if all components of a complex value are finite, meaning they are neither +/- infinity nor NaN.
 template<typename T >
  T safe divide (T a, T b)
      Computes the quotient of the given parameters, guarding against division by zero.
template<typename T >
  std::enable_if_t<!is_complex_s< T>::value, bool > is_nan (const T &value)
      Checks if a floating point number is NaN.

    template<typename T >

  std::enable_if_t< is_complex_s< T >::value, bool > is_nan (const T &value)
      Checks if any component of a complex value is NaN.

    template<typename T >

  constexpr std::enable if t < lis complex s < T > ::value, T > nan()
      Returns a quiet NaN of the given type.
```

```
• template<typename T >
  constexpr std::enable_if_t< is_complex_s< T >::value, T > nan ()
     Returns a complex with both components quiet NaN.
• template<typename ValueType = default precision, typename IndexType = int32>
  matrix_data< ValueType, IndexType > read_raw (std::istream &is)
     Reads a matrix stored in matrix market format from an input stream.
• template<typename ValueType = default_precision, typename IndexType = int32>
  matrix_data< ValueType, IndexType > read_binary_raw (std::istream &is)
      Reads a matrix stored in Ginkgo's binary matrix format from an input stream.
• template<typename ValueType = default_precision, typename IndexType = int32>
  matrix_data< ValueType, IndexType > read_generic_raw (std::istream &is)
      Reads a matrix stored in either binary or matrix market format from an input stream.

    template<typename ValueType , typename IndexType >

  void write raw (std::ostream &os, const matrix data < ValueType, IndexType > &data, layout type
  layout=layout type::coordinate)
      Writes a matrix_data structure to a stream in matrix market format.

    template<typename ValueType , typename IndexType >

  void write_binary_raw (std::ostream &os, const matrix_data< ValueType, IndexType > &data)
      Writes a matrix_data structure to a stream in binary format.

    template<typename MatrixType , typename StreamType , typename... MatrixArgs>

  std::unique_ptr< MatrixType > read (StreamType &&is, MatrixArgs &&... args)
      Reads a matrix stored in matrix market format from an input stream.
• template<typename MatrixType , typename StreamType , typename... MatrixArgs>
  std::unique ptr< MatrixType > read binary (StreamType &&is, MatrixArgs &&... args)
      Reads a matrix stored in binary format from an input stream.
• template<typename MatrixType , typename StreamType , typename... MatrixArgs>
  std::unique_ptr< MatrixType > read_generic (StreamType &&is, MatrixArgs &&... args)
     Reads a matrix stored either in binary or matrix market format from an input stream.

    template<typename MatrixPtrType , typename StreamType >

  void write (StreamType &&os, MatrixPtrType &&matrix, layout_type layout=detail::mtx_io_traits< std↔
  ::remove_cv_t< detail::pointee< MatrixPtrType >>>::default_layout)
      Writes a matrix into an output stream in matrix market format.

    template<typename MatrixPtrType , typename StreamType >

  void write_binary (StreamType &&os, MatrixPtrType &&matrix)
      Writes a matrix into an output stream in binary format.
• template<typename R , typename T >
  std::unique_otr< R, std::function< void(R *)> > copy_and_convert_to (std::shared_ptr< const Executor >
  exec, T *obj)
     Converts the object to R and places it on Executor exec.

    template<typename R , typename T >

  std::unique ptr< const R, std::function< void(const R *)> > copy and convert to (std::shared ptr< const
  Executor > exec, const T *obj)
     Converts the object to R and places it on Executor exec.

    template<typename R , typename T >

  std::shared_ptr< R > copy_and_convert_to (std::shared_ptr< const Executor > exec, std::shared_ptr< T >
  obj)
     Converts the object to R and places it on Executor exec.

    template<typename R, typename T >

  std::shared_ptr< const R > copy_and_convert_to (std::shared_ptr< const Executor > exec, std::shared_
  ptr < const T > obj)
```

 $\label{lem:conversion} $$ \det \exists :: ext(s) = 1.5 \text{ } \\ \det \exists :: ext(s) = 1.5$ 

template<typename ValueType , typename Ptr >

trix)

Convert the given LinOp from matrix::Dense<...> to matrix::Dense<ValueType>.

template < typename ValueType , typename Function , typename... Args > void precision\_dispatch (Function fn, Args \*... linops)

Calls the given function with each given argument LinOp temporarily converted into matrix::Dense< ValueType> as parameters.

template < typename ValueType, typename Function >
 void precision\_dispatch\_real\_complex (Function fn, const LinOp \*in, LinOp \*out)

Calls the given function with the given LinOps temporarily converted to matrix::Dense< ValueType>\* as parameters.

• template<typename ValueType , typename Function >

void precision\_dispatch\_real\_complex (Function fn, const LinOp \*alpha, const LinOp \*in, LinOp \*out)

Calls the given function with the given LinOps temporarily converted to matrix::Dense< ValueType>\* as parameters.

template<typename ValueType, typename Function >
 void precision\_dispatch\_real\_complex (Function fn, const LinOp \*alpha, const LinOp \*in, const LinOp \*beta,
 LinOp \*out)

Calls the given function with the given LinOps temporarily converted to matrix::Dense< ValueType>\* as parameters.

template < typename ValueType , typename Function >
void mixed\_precision\_dispatch (Function fn, const LinOp \*in, LinOp \*out)

Calls the given function with each given argument LinOp converted into matrix::Dense< ValueType> as parameters.

template<typename ValueType , typename Function , std::enable\_if\_t< is\_complex< ValueType >()> \* = nullptr> void mixed\_precision\_dispatch\_real\_complex (Function fn, const LinOp \*in, LinOp \*out)

Calls the given function with the given LinOps cast to their dynamic type matrix::Dense< ValueType>\* as parameters.

template<typename Ptr >

detail::temporary\_clone < detail::pointee < Ptr > > make\_temporary\_clone (std::shared\_ptr < const Executor > exec, Ptr &&ptr)

Creates a temporary\_clone.

• template<typename Ptr >

 $\label{lem:const} \mbox{detail::temporary\_clone} < \mbox{detail::pointee} < \mbox{Ptr} >> \mbox{make\_temporary\_output\_clone} \ \mbox{(std::shared\_ptr} < \mbox{const} \\ \mbox{Executor} > \mbox{exec}, \mbox{Ptr} \& \mbox{ptr})$ 

Creates a uninitialized temporary\_clone that will be copied back to the input afterwards.

• constexpr bool operator== (precision\_reduction x, precision\_reduction y) noexcept

Checks if two precision\_reduction encodings are equal.

constexpr bool operator!= (precision reduction x, precision reduction y) noexcept

Checks if two precision\_reduction encodings are different.

• template<typename IndexType >

constexpr IndexType invalid\_index ()

Value for an invalid signed index type.

• template<typename Pointer >

detail::cloned\_type< Pointer > clone (const Pointer &p)

Creates a unique clone of the object pointed to by p.

template<typename Pointer >

detail::cloned\_type< Pointer > clone (std::shared\_ptr< const Executor > exec, const Pointer &p)

Creates a unique clone of the object pointed to by p on Executor exec.

 $\bullet \ \ \text{template}{<} \text{typename OwningPointer}{>}$ 

detail::shared\_type< OwningPointer > share (OwningPointer &&p)

Marks the object pointed to by p as shared.

 $\bullet \ \ \text{template}{<} \text{typename OwningPointer} >$ 

std::remove\_reference< OwningPointer >::type && give (OwningPointer &&p)

Marks that the object pointed to by p can be given to the callee.

template<typename Pointer >

 $std::enable\_if < detail::have\_ownership\_s < Pointer > ::value, detail::pointee < Pointer > * > ::type \ lend \ (const Pointer &p)$ 

Returns a non-owning (plain) pointer to the object pointed to by p.

template<typename Pointer >
 std::enable\_if<!detail::have\_ownership\_s< Pointer >::value, detail::pointee< Pointer > \* >::type lend (const Pointer &p)

Returns a non-owning (plain) pointer to the object pointed to by p.

```
    template<typename T, typename U >
std::decay t< T > * as (U *obj)
```

Performs polymorphic type conversion.

template<typename T , typename U >
 const std::decay\_t< T > \* as (const U \*obj)

Performs polymorphic type conversion.

template < typename T , typename U >
 std::decay\_t < T > \* as (ptr\_param < U > obj)

Performs polymorphic type conversion on a ptr\_param.

template<typename T, typename U >
 const std::decay\_t< T > \* as (ptr\_param< const U > obj)

Performs polymorphic type conversion.

template < typename T , typename U >
 std::unique\_ptr < std::decay\_t < T > > as (std::unique\_ptr < U > &&obj)

Performs polymorphic type conversion of a unique\_ptr.

• template<typename T , typename U > std::shared\_ptr< std::decay\_t< T > > as (std::shared\_ptr< U > obj)

Performs polymorphic type conversion of a shared\_ptr.

template<typename T , typename U >
 std::shared\_ptr< const std::decay\_t< T >> as (std::shared\_ptr< const U > obj)

Performs polymorphic type conversion of a shared\_ptr.

std::ostream & operator<< (std::ostream &os, const version &ver)</li>

Prints version information to a stream.

std::ostream & operator<< (std::ostream &os, const version\_info &ver\_info)</li>

Prints library version information in human-readable format to a stream.

template < template < typename, typename > class MatrixType, typename... Args > auto with matrix type (Args &&... create args)

This function returns a type that delays a call to MatrixType::create.

template<typename VecPtr >

std::unique\_ptr< matrix::Dense< typename detail::pointee< VecPtr >::value\_type > > make\_dense\_view (VecPtr &&vector)

Creates a view of a given Dense vector.

template<typename VecPtr >

std::unique\_ptr< const matrix::Dense< typename detail::pointee< VecPtr >::value\_type >> make\_const\_dense\_view (VecPtr &vector)

Creates a view of a given Dense vector.

template<typename Matrix , typename... TArgs>
 std::unique\_ptr< Matrix > initialize (size\_type stride, std::initializer\_list< typename Matrix::value\_type > vals, std::shared\_ptr< const Executor > exec, TArgs &&... create\_args)

Creates and initializes a column-vector.

template < typename Matrix , typename... TArgs > std::unique\_ptr < Matrix > initialize (std::initializer\_list < typename Matrix::value\_type > vals, std::shared\_← ptr < const Executor > exec, TArgs &&... create\_args)

Creates and initializes a column-vector.

template<typename Matrix , typename... TArgs>
 std::unique\_ptr< Matrix > initialize (size\_type stride, std::initializer\_list< std::initializer\_list< typename
 Matrix::value\_type >> vals, std::shared\_ptr< const Executor > exec, TArgs &&... create\_args)

Creates and initializes a matrix.

template<typename Matrix , typename... TArgs>
 std::unique\_ptr< Matrix > initialize (std::initializer\_list< std::initializer\_list< typename Matrix::value\_type >>
 vals, std::shared\_ptr< const Executor > exec, TArgs &&... create\_args)

Creates and initializes a matrix.

- bool operator== (const stopping\_status &x, const stopping\_status &y) noexcept Checks if two stopping statuses are equivalent.
- bool operator!= (const stopping\_status &x, const stopping\_status &y) noexcept Checks if two stopping statuses are different.

#### **Variables**

constexpr size\_type byte\_size = CHAR\_BIT
 Number of bits in a byte.

# 45.1.1 Detailed Description

The Ginkgo namespace.

# 45.1.2 Typedef Documentation

# 45.1.2.1 highest\_precision

```
template<typename... Ts>
using gko::highest_precision = typedef typename detail::highest_precision_variadic<Ts...>←
::type
```

Obtains the smallest arithmetic type that is able to store elements of all template parameter types exactly.

All template type parameters need to be either real or complex types, mixing them is not possible.

Formally, it computes a right-fold over the type list, with the highest precision of a pair of real arithmetic types T1, T2 computed as  $decltype(T1\{\} + T2\{\})$ , or  $std::complex<highest_precision<remove\_{} complex<T1>$ ,  $remove\_complex<T2>>> for complex types$ .

# 45.1.2.2 is\_complex\_or\_scalar\_s

```
template<typename T >
using gko::is_complex_or_scalar_s = typedef detail::is_complex_or_scalar_impl<T>
```

Allows to check if T is a complex or scalar value during compile time by accessing the value attribute of this struct.

If value is true, T is a complex/scalar type, if it is false, T is not a complex/scalar type.

#### **Template Parameters**

```
T | type to check
```

## 45.1.2.3 is\_complex\_s

```
template<typename T >
using gko::is_complex_s = typedef detail::is_complex_impl<T>
```

Allows to check if T is a complex value during compile time by accessing the value attribute of this struct.

If value is true, T is a complex type, if it is false, T is not a complex type.

## **Template Parameters**

T type to check

# 45.1.2.4 previous\_precision

```
template<typename T >
using gko::previous_precision = typedef next_precision<T>
```

Obtains the previous type in the singly-linked precision list.

Note

Currently our lists contains only two elements, so this is the same as next\_precision.

# 45.1.2.5 remove\_complex

```
template<typename T >
using gko::remove_complex = typedef typename detail::remove_complex_s<T>::type
```

Obtain the type which removed the complex of complex/scalar type or the template parameter of class by accessing the type attribute of this struct.

## **Template Parameters**

T type to remove complex

## Note

remove\_complex<class> can not be used in friend class declaration.

#### 45.1.2.6 to\_complex

```
template<typename T >
using gko::to_complex = typedef typename detail::to_complex_s<T>::type
```

Obtain the type which adds the complex of complex/scalar type or the template parameter of class by accessing the type attribute of this struct.

#### **Template Parameters**

```
T type to complex_type
```

#### Note

to\_complex < class > can not be used in friend class declaration. the followings are the error message from different combination. friend to\_complex < Csr >; error: can not recognize it is class correctly. friend class to\_complex < Csr >; error: using alias template specialization friend class to\_complex\_s < Csr < ValueType, \leftarrow IndexType >>::type; error: can not recognize it is class correctly.

# 45.1.2.7 to\_real

```
template<typename T >
using gko::to_real = typedef remove_complex<T>
```

to\_real is alias of remove\_complex

#### **Template Parameters**

```
T type to real
```

## 45.1.3 Enumeration Type Documentation

#### 45.1.3.1 allocation\_mode

```
enum gko::allocation_mode [strong]
```

Specify the mode of allocation for CUDA/HIP GPUs.

device allocates memory on the device and Unified Memory model is not used.

unified\_global allocates memory on the device, but is accessible by the host through the Unified memory model.

unified\_host allocates memory on the host and it is not available on devices which do not have concurrent accesses switched on, but this access can be explicitly switched on, when necessary.

```
62 { device, unified_global, unified_host };
```

# 45.1.3.2 layout\_type

```
enum gko::layout_type [strong]
```

Specifies the layout type when writing data in matrix market format.

#### Enumerator

array	The matrix should be written as dense matrix in column-major order.
coordinate	The matrix should be written as a sparse matrix in coordinate format.

```
92
96 array,
100 coordinate
101 };
```

# 45.1.3.3 log\_propagation\_mode

```
enum gko::log_propagation_mode [strong]
```

How Logger events are propagated to their Executor.

#### Enumerator

never	Events only get reported at loggers attached to the triggering object. (Except for allocation/free, copy and Operations, since they happen at the Executor).
automatic	Events get reported to loggers attached to the triggering object and propagating loggers (Logger::needs_propagation() return true) attached to its Executor.

# 45.1.4 Function Documentation

## 45.1.4.1 abs()

Returns the absolute value of the object.

# **Template Parameters**

```
T the type of the object
```

# **Parameters**

```
x the object
```

Returns

```
x >= zero<T>() ? x:-x;
947 {
948     return x >= zero<T>() ? x : -x;
949 }
```

Referenced by is finite().

#### 45.1.4.2 as() [1/7]

Performs polymorphic type conversion.

This is the constant version of the function.

#### **Template Parameters**

T	requested result type
U	static type of the passed object

#### **Parameters**

```
obj the object which should be converted
```

#### Returns

If successful, returns a pointer to the subtype, otherwise throws NotSupported.

```
334 {
       if (auto p = dynamic_cast<const std::decay_t<T>*>(obj)) {
335
336
       return p;
} else {
337
338
           throw NotSupported(__FILE__, __LINE__,
339
                        std::string{"gko::as<"} +
340
                                  name_demangling::get_type_name(typeid(T)) + ">",
341
                              name_demangling::get_type_name(typeid(*obj)));
342
       }
343 }
```

# 45.1.4.3 as() [2/7]

```
template<typename T , typename U > const std::decay_t<T>* gko::as ( ptr\_param< const \ U > obj ) \quad [inline]
```

Performs polymorphic type conversion.

This is the constant version of the function.

# **Template Parameters**

T	requested result type
U	static type of the passed object

#### **Parameters**

#### Returns

If successful, returns a pointer to the subtype, otherwise throws NotSupported.

References gko::ptr\_param< T >::get().

# **45.1.4.4** as() [3/7]

```
template<typename T , typename U > std::decay_t<T>* gko::as ( ptr\_param < U > obj ) \quad [inline]
```

Performs polymorphic type conversion on a ptr\_param.

# **Template Parameters**

T	requested result type
U	static type of the passed object

# **Parameters**

obj the object which should	be converted
-----------------------------	--------------

# Returns

If successful, returns a pointer to the subtype, otherwise throws NotSupported.

References gko::ptr\_param< T >::get().

# 45.1.4.5 as() [4/7]

Performs polymorphic type conversion of a shared ptr.

This is the constant version of the function.

## **Template Parameters**

T	requested result type
U	static type of the passed object

#### **Parameters**

```
obj the shared_ptr to the object which should be converted.
```

#### Returns

If successful, returns a shared\_ptr to the subtype, otherwise throws NotSupported. This pointer shares ownership with the input pointer.

#### 45.1.4.6 as() [5/7]

```
template<typename T , typename U > std::shared_ptr<std::decay_t<T> > gko::as ( std::shared_ptr< U > obj ) \quad [inline]
```

Performs polymorphic type conversion of a shared\_ptr.

#### **Template Parameters**

T	requested result type
U	static type of the passed object

# **Parameters**

```
obj the shared_ptr to the object which should be converted.
```

#### Returns

If successful, returns a shared\_ptr to the subtype, otherwise throws NotSupported. This pointer shares ownership with the input pointer.

#### 45.1.4.7 as() [6/7]

```
template<typename T , typename U > std::unique_ptr<std::decay_t<T> > gko::as (  std::unique\_ptr< U > \&\& obj ) \quad [inline]
```

Performs polymorphic type conversion of a unique\_ptr.

# **Template Parameters**

Τ	requested result type	
U	static type of the passed object	

#### **Parameters**

obj the unique\_ptr to the object which should be converted. If successful, it will be reset to a nullptr.

#### Returns

If successful, returns a unique\_ptr to the subtype, otherwise throws NotSupported.

## 45.1.4.8 as() [7/7]

Performs polymorphic type conversion.

## **Template Parameters**

T	requested result type
U	static type of the passed object

#### **Parameters**

<i>obj</i> t	the object which should be converted
--------------	--------------------------------------

#### Returns

If successful, returns a pointer to the subtype, otherwise throws NotSupported.

Referenced by gko::preconditioner::lsai< lsaiType, ValueType, IndexType >::get\_approximate\_inverse().

# 45.1.4.9 ceildiv()

Performs integer division with rounding up.

#### **Parameters**

num	numerator
den	denominator

#### Returns

returns the ceiled quotient.

Referenced by gko::matrix::Csr< ValueType, IndexType >::load\_balance::clac\_size(), gko::preconditioner::block = \_interleaved\_storage\_scheme< index\_type >::compute\_storage\_space(), and gko::matrix::Csr< ValueType, IndexType >::load\_balance::process().

#### 45.1.4.10 clone() [1/2]

Creates a unique clone of the object pointed to by p.

The pointee (i.e. \*p) needs to have a clone method that returns a std::unique\_ptr in order for this method to work.

#### **Template Parameters**

#### **Parameters**

p a pointer to the object

#### Note

The difference between this function and directly calling LinOp::clone() is that this one preserves the static type of the object.

Referenced by gko::preconditioner::lc< LSolverType, IndexType >::operator=(), gko::preconditioner::llu< L  $\leftarrow$  SolverType, USolverType, ReverseApply, IndexType >::operator=(), gko::solver::EnablePreconditionable< Bicg< ValueType > >::set\_preconditioner(), and gko::solver::EnableIterativeBase< Bicg< ValueType > >::set\_stop\_ $\leftarrow$  criterion\_factory().

# 45.1.4.11 clone() [2/2]

```
template<typename Pointer >
detail::cloned_type<Pointer> gko::clone (
```

```
std::shared_ptr< const Executor > exec,
const Pointer & p ) [inline]
```

Creates a unique clone of the object pointed to by p on Executor exec.

The pointee (i.e. \*p) needs to have a clone method that takes an executor and returns a std::unique\_ptr in order for this method to work.

# **Template Parameters**

Pointer	type of pointer to the object (plain or smart pointer)
---------	--

#### **Parameters**

е	exec	the executor where the cloned object should be stored	
p	•	a pointer to the object	

#### Note

The difference between this function and directly calling LinOp::clone() is that this one preserves the static type of the object.

# 45.1.4.12 conj()

Returns the conjugate of an object.

#### **Parameters**

```
x the number to conjugate
```

#### Returns

conjugate of the object (by default, the object itself)

Referenced by squared\_norm().

## 45.1.4.13 copy\_and\_convert\_to() [1/4]

```
\label{template} $$ template < typename R , typename T > std::unique_ptr < const R, std::function < void(const R*) > > gko::copy_and_convert_to (
```

```
std::shared_ptr< const Executor > exec,
const T * obj )
```

Converts the object to R and places it on Executor exec.

If the object is already of the requested type and on the requested executor, the copy and conversion is avoided and a reference to the original object is returned instead.

#### **Template Parameters**

R	the type to which the object should be converted
T	the type of the input object

#### **Parameters**

exec	the executor where the result should be placed
obj	the object that should be converted

#### Returns

a unique pointer (with dynamically bound deleter) to the converted object

#### Note

This is a version of the function which adds the const qualifier to the result if the input had the same qualifier.

```
578 {
579     return detail::copy_and_convert_to_impl<const R>(std::move(exec), obj);
580 }
```

### 45.1.4.14 copy\_and\_convert\_to() [2/4]

This is the version that takes in the std::shared\_ptr and returns a std::shared\_ptr

If the object is already of the requested type and on the requested executor, the copy and conversion is avoided and a reference to the original object is returned instead.

#### **Template Parameters**

R	the type to which the object should be converted
T	the type of the input object

#### **Parameters**

exec	the executor where the result should be placed
------	--

obj the object that should be converted	
---	--

#### Returns

a shared pointer to the converted object

#### Note

This is a version of the function which adds the const qualifier to the result if the input had the same qualifier.

### 45.1.4.15 copy\_and\_convert\_to() [3/4]

Converts the object to R and places it on Executor exec.

This is the version that takes in the std::shared\_ptr and returns a std::shared\_ptr

If the object is already of the requested type and on the requested executor, the copy and conversion is avoided and a reference to the original object is returned instead.

### **Template Parameters**

R	the type to which the object should be converted
T	the type of the input object

#### **Parameters**

exec	the executor where the result should be placed
obj	the object that should be converted

### Returns

a shared pointer to the converted object

## 45.1.4.16 copy\_and\_convert\_to() [4/4]

```
template<typename R , typename T > std::unique_ptr<R, std::function<void(R*)> > gko::copy_and_convert_to (
```

```
std::shared_ptr< const Executor > exec,
T * obj )
```

Converts the object to R and places it on Executor exec.

If the object is already of the requested type and on the requested executor, the copy and conversion is avoided and a reference to the original object is returned instead.

### **Template Parameters**

R	the type to which the object should be converted
T	the type of the input object

#### **Parameters**

exec	the executor where the result should be placed
obj	the object that should be converted

#### Returns

a unique pointer (with dynamically bound deleter) to the converted object

## 45.1.4.17 get\_significant\_bit()

Returns the position of the most significant bit of the number.

This is the same as the rounded down base-2 logarithm of the number.

## **Template Parameters**

T	a numeric type supporting bit shift and comparison

#### **Parameters**

n	a number
hint	a lower bound for the position o the significant bit

## Returns

maximum of  $\mbox{hint}$  and the significant bit position of  $\mbox{n}$ 

## 45.1.4.18 get\_superior\_power()

Returns the smallest power of base not smaller than limit.

### **Template Parameters**

T	a numeric type supporting multiplication and comparison
---	---

#### **Parameters**

base	the base of the power to be returned
limit	the lower limit on the size of the power returned
hint	a lower bound on the result, has to be a power of base

### Returns

the smallest power of base not smaller than limit

## 45.1.4.19 give()

Marks that the object pointed to by p can be given to the callee.

Effectively calls std::move(p).

## **Template Parameters**

OwningPointer	type of pointer with ownership to the object (has to be a smart pointer)
- 3	

## **Parameters**

p	a pointer to the object

#### Note

The original pointer p becomes invalid after this call.

### 45.1.4.20 imag()

Returns the imaginary part of the object.

### **Template Parameters**

```
T type of the object
```

#### **Parameters**

```
x the object
```

### Returns

imaginary part of the object (by default, zero<T>())

### 45.1.4.21 is\_complex()

```
template<typename T >
constexpr bool gko::is_complex ( ) [inline], [constexpr]
```

Checks if T is a complex type.

### **Template Parameters**



#### Returns

true if T is a complex type, false otherwise

## 45.1.4.22 is\_complex\_or\_scalar()

```
template<typename T >
constexpr bool gko::is_complex_or_scalar ( ) [inline], [constexpr]
```

Checks if T is a complex/scalar type.

### **Template Parameters**

```
T type to check
```

#### Returns

true if T is a complex/scalar type, false otherwise

## 45.1.4.23 is\_finite() [1/2]

Checks if a floating point number is finite, meaning it is neither +/- infinity nor NaN.

### **Template Parameters**

```
T \mid \text{type of the value to check}
```

#### **Parameters**

```
value | value to check
```

## Returns

true if the value is finite, meaning it are neither +/- infinity nor NaN.

References abs().

Referenced by is\_finite().

### 45.1.4.24 is\_finite() [2/2]

Checks if all components of a complex value are finite, meaning they are neither +/- infinity nor NaN.

### **Template Parameters**

T | complex type of the value to check

value	complex value to check
-------	------------------------

### Returns

true if both components of the given value are finite, meaning they are neither +/- infinity nor NaN.

References is\_finite().

### 45.1.4.25 is\_nan() [1/2]

Checks if a floating point number is NaN.

### **Template Parameters**

T type of the value to check

#### **Parameters**

```
value value to check
```

### Returns

true if the value is NaN.

Referenced by is nan().

## 45.1.4.26 is\_nan() [2/2]

Checks if any component of a complex value is NaN.

#### **Template Parameters**

T complex type of the value to check

value	complex value to check
-------	------------------------

## Returns

true if any component of the given value is NaN.

References is\_nan().

### 45.1.4.27 is\_nonzero()

Returns true if and only if the given value is not zero.

## **Template Parameters**

```
T the type of the value
```

### **Parameters**

```
value the given value
```

### Returns

true iff the given value is not zero, i.e. value != zero < T > ()

Referenced by gko::matrix\_data< ValueType, IndexType >::diag().

## 45.1.4.28 is\_zero()

Returns true if and only if the given value is zero.

## **Template Parameters**

T the type of the value

value	the given value
-------	-----------------

#### Returns

```
true iff the given value is zero, i.e. value == zero<T>()
```

Referenced by gko::matrix\_data< ValueType, IndexType >::remove\_zeros().

#### 45.1.4.29 lend() [1/2]

Returns a non-owning (plain) pointer to the object pointed to by p.

#### **Template Parameters**

Pointer	type of pointer to the object (plain or smart pointer)
---------	--

#### **Parameters**

```
p a pointer to the object
```

#### Note

This is the overload for owning (smart) pointers, that behaves the same as calling .get() on the smart pointer.

#### 45.1.4.30 lend() [2/2]

Returns a non-owning (plain) pointer to the object pointed to by p.

## **Template Parameters**

Pointer	type of pointer to the object (plain or smart pointer)
1 0111101	type of pointer to the object (plant of email pointer)

```
p a pointer to the object
```

#### Note

This is the overload for non-owning (plain) pointers, that just returns p.

### 45.1.4.31 make\_array\_view()

Helper function to create an array view deducing the value type.

#### **Parameters**

exec	the executor on which the array resides
size	the number of elements for the array
data	the pointer to the array we create a view on.

### **Template Parameters**

ValueType	the type of the array elements
-----------	--------------------------------

#### Returns

```
array<ValueType>::view(exec, size, data)
789 {
790     return array<ValueType>::view(exec, size, data);
791 }
```

References make\_array\_view().

Referenced by make array view().

### 45.1.4.32 make\_const\_array\_view()

Helper function to create a const array view deducing the value type.

exec	the executor on which the array resides
size	the number of elements for the array
data	the pointer to the array we create a view on.

#### **Template Parameters**

ValueType	the type of the array elements
-----------	--------------------------------

#### Returns

```
array<ValueType>::const_view(exec, size, data)
```

References make\_const\_array\_view().

Referenced by make\_const\_array\_view().

### 45.1.4.33 make\_const\_dense\_view()

Creates a view of a given Dense vector.

### **Template Parameters**

### **Parameters**

vecto	the vec	tor on whicl	n to create t	he view
-------	---------	--------------	---------------	---------

References gko::matrix::Dense< ValueType >::create\_const\_view\_of().

### 45.1.4.34 make\_dense\_view()

Creates a view of a given Dense vector.

### **Template Parameters**

<i>VecPtr</i>	a (smart or raw) pointer to the vector.
---------------	---

#### **Parameters**

vector	the vector on which to create the view
--------	--

References gko::matrix::Dense< ValueType >::create view of().

#### 45.1.4.35 make\_temporary\_clone()

Creates a temporary\_clone.

This is a helper function which avoids the need to explicitly specify the type of the object, as would be the case if using the constructor of temporary\_clone.

#### **Parameters**

exec	the executor where the clone will be created
ptr	a pointer to the object of which the clone will be created

### **Template Parameters**

```
Ptr the (raw or smart) pointer type to be temporarily cloned
```

```
210 {
211    using T = detail::pointee<Ptr>
212    return detail::temporary_clone<T>(std::move(exec), std::forward<Ptr>
(ptr));
213 }
```

Referenced by gko::ScaledIdentityAddable::add\_scaled\_identity(), gko::matrix::Csr< ValueType, IndexType  $> \leftarrow$  ::inv\_scale(), and gko::matrix::Csr< ValueType, IndexType > ::scale().

#### 45.1.4.36 make\_temporary\_conversion()

 $\label{lem:convert} \mbox{Convert the given LinOp from matrix::Dense} < ... > \mbox{to matrix::Dense} < \mbox{ValueType} >.$ 

The conversion tries to convert the input LinOp to all Dense types with value type recursively reachable by next← \_precision<...> starting from the ValueType template parameter. This means that all real-to-real and complex-to-complex conversions for default precisions are being considered. If the input matrix is non-const, the contents of the modified converted object will be converted back to the input matrix when the returned object is destroyed. This may lead to a loss of precision!

#### **Parameters**

matrix

the input matrix which is supposed to be converted. It is wrapped unchanged if it is already of type matrix::Dense<ValueType>, otherwise it will be converted to this type if possible.

#### Returns

a detail::temporary conversion pointing to the (potentially converted) object.

#### **Exceptions**

**NotSupported** 

if the input matrix cannot be converted to matrix::Dense<ValueType>

#### **Template Parameters**

ValueType | the value type into whose associated matrix::Dense type to convert the input LinOp.

```
48 {
49
       using Pointee = detail::pointee<Ptr>;
       using Dense = matrix::Dense<ValueType>;
50
       using NextDense = matrix::Dense<next_precision<ValueType»;</pre>
51
       using MaybeConstDense =
52
           std::conditional_t<std::is_const<Pointee>::value, const Dense, Dense>;
54
       auto result = detail::temporary_conversion
55
           MaybeConstDense>::template create<NextDense>(matrix);
       if (!result) {
   GKO_NOT_SUPPORTED(*matrix);
56
57
58
59
       return result;
60 }
```

### 45.1.4.37 make\_temporary\_output\_clone()

Creates a uninitialized temporary\_clone that will be copied back to the input afterwards.

It can be used for output parameters to avoid an unnecessary copy in make\_temporary\_clone.

This is a helper function which avoids the need to explicitly specify the type of the object, as would be the case if using the constructor of temporary\_clone.

#### **Parameters**

exec	the executor where the uninitialized clone will be created
ptr	a pointer to the object of which the clone will be created

## **Template Parameters**

Ptr the (raw or smart) pointer type to be temporarily cloned

## 45.1.4.38 max()

Returns the larger of the arguments.

## **Template Parameters**

```
T type of the arguments
```

#### **Parameters**

X	first argument
У	second argument

### Returns

$$x >= y ? x : y$$

## 45.1.4.39 min()

Returns the smaller of the arguments.

## **Template Parameters**

T	type of the arguments
---	-----------------------

#### **Parameters**

X	first argument
у	second argument

#### Returns

```
x \le y ? x : y
```

Referenced by gko::matrix::Csr< ValueType, IndexType >::load\_balance::clac\_size().

### 45.1.4.40 mixed\_precision\_dispatch()

Calls the given function with each given argument LinOp converted into matrix::Dense<ValueType> as parameters.

If GINKGO\_MIXED\_PRECISION is defined, this means that the function will be called with its dynamic type as a static type, so the (templated/generic) function will be instantiated with all pairs of Dense<ValueType> and Dense<next\_precision<ValueType>> parameter types, and the appropriate overload will be called based on the dynamic type of the parameter.

If GINKGO MIXED PRECISION is not defined, it will behave exactly like precision dispatch.

#### **Parameters**

fn	the given function. It will be called with one const and one non-const matrix::Dense<> parameter based on the dynamic type of the inputs (GINKGO_MIXED_PRECISION) or of type matrix::Dense <valuetype> (no GINKGO_MIXED_PRECISION).</valuetype>
in	The first parameter to be cast (GINKGO_MIXED_PRECISION) or converted (no GINKGO_MIXED_PRECISION) and used to call fn.
out	The second parameter to be cast (GINKGO_MIXED_PRECISION) or converted (no GINKGO_MIXED_PRECISION) and used to call fn.

#### **Template Parameters**

ValueType	the value type to use for the parameters of fn (no GINKGO_MIXED_PRECISION). With GINKGO_MIXED_PRECISION enabled, it only matters whether this type is complex or real.
Function	the function pointer, lambda or other functor type to call with the converted arguments.

#### 45.1.4.41 mixed\_precision\_dispatch\_real\_complex()

Calls the given function with the given LinOps cast to their dynamic type matrix::Dense<ValueType>\* as parameters

If ValueType is real and both in and out are complex, uses matrix::Dense::get\_real\_view() to convert them into real matrices after precision conversion.

See also

mixed\_precision\_dispatch()

### 45.1.4.42 nan() [1/2]

```
template<typename T >
constexpr std::enable_if_t<!is_complex_s<T>::value, T> gko::nan ( ) [inline], [constexpr]
```

Returns a quiet NaN of the given type.

**Template Parameters** 

```
T the type of the object
```

Returns

NaN.

Referenced by nan().

### 45.1.4.43 nan() [2/2]

```
template<typename T >
constexpr std::enable_if_t<is_complex_s<T>::value, T> gko::nan ( ) [inline], [constexpr]
```

Returns a complex with both components quiet NaN.

#### **Template Parameters**

```
T the type of the object
```

### Returns

complex{NaN, NaN}.

References nan().

#### 45.1.4.44 one() [1/2]

```
template<typename T >
constexpr T gko::one ( ) [inline], [constexpr]
```

Returns the multiplicative identity for T.

### Returns

the multiplicative identity for T

Referenced by unit\_root().

## 45.1.4.45 one() [2/2]

Returns the multiplicative identity for T.

### Returns

the multiplicative identity for T

#### Note

This version takes an unused reference argument to avoid complicated calls like one < decltype(x) > (). Instead, it allows one(x).

### 45.1.4.46 operator"!=() [1/2]

Checks if two stopping statuses are different.

### **Parameters**

X	a stopping status
У	a stopping status

#### Returns

```
true if and only if ! (x == y)

151 {
    return x.data_ != y.data_;
153 }
```

## 45.1.4.47 operator"!=() [2/2]

Checks if two precision reduction encodings are different.

#### **Parameters**

X	an encoding
У	an encoding

#### Returns

true if and only if x and y are different encodings.

```
378 {
379     using st = precision_reduction::storage_type;
380     return static_cast<st>(x) != static_cast<st>(y);
381 }
```

### 45.1.4.48 operator << () [1/2]

Prints version information to a stream.

#### **Parameters**

os	output stream	
ver	version structure	

#### Returns

os

```
108 }
```

References gko::version::major, gko::version::minor, gko::version::patch, and gko::version::tag.

#### 45.1.4.49 operator <<() [2/2]

Prints library version information in human-readable format to a stream.

#### **Parameters**

os	output stream
ver_info	version information

### Returns

os

### 45.1.4.50 operator==() [1/2]

Checks if two stopping statuses are equivalent.

## **Parameters**

Х	a stopping status
У	a stopping status

## Returns

true if and only if both  $\boldsymbol{x}$  and  $\boldsymbol{y}$  have the same mask and converged and finalized state

### 45.1.4.51 operator==() [2/2]

Checks if two precision\_reduction encodings are equal.

Х	an encoding
у	an encoding

#### Returns

true if and only if  $\boldsymbol{x}$  and  $\boldsymbol{y}$  are the same encodings

## 45.1.4.52 pi()

```
template<typename T >
constexpr T gko::pi ( ) [inline], [constexpr]
```

Returns the value of pi.

## **Template Parameters**

```
T the value type to return
```

### 45.1.4.53 precision\_dispatch()

Calls the given function with each given argument LinOp temporarily converted into matrix::Dense<ValueType> as parameters.

### **Parameters**

fn	the given function. It will be passed one (potentially const) matrix::Dense <valuetype>* parameter per parameter in the parameter pack linops.</valuetype>
linops	the given arguments to be converted and passed on to fn.

### **Template Parameters**

ValueType	the value type to use for the parameters of fn.
Function	the function pointer, lambda or other functor type to call with the converted arguments.
Args	the argument type list.

#### 45.1.4.54 precision\_dispatch\_real\_complex() [1/3]

Calls the given function with the given LinOps temporarily converted to matrix::Dense<ValueType>\* as parameters.

If ValueType is real and both in and out are complex, uses matrix::Dense::get\_real\_view() to convert them into real matrices after precision conversion.

See also

precision dispatch()

#### 45.1.4.55 precision\_dispatch\_real\_complex() [2/3]

Calls the given function with the given LinOps temporarily converted to matrix::Dense<ValueType>\* as parameters.

If ValueType is real and both in and out are complex, uses matrix::Dense::get\_real\_view() to convert them into real matrices after precision conversion.

See also

precision\_dispatch()

#### 45.1.4.56 precision\_dispatch\_real\_complex() [3/3]

```
template<typename ValueType , typename Function > void gko::precision_dispatch_real_complex (  Function \ fn, \\ const \ LinOp * in, \\ LinOp * out )
```

Calls the given function with the given LinOps temporarily converted to matrix::Dense<ValueType>\* as parameters.

If ValueType is real and both input vectors are complex, uses matrix::Dense::get\_real\_view() to convert them into real matrices after precision conversion.

See also

precision\_dispatch()

### 45.1.4.57 read()

Reads a matrix stored in matrix market format from an input stream.

#### **Template Parameters**

MatrixType	a ReadableFromMatrixData LinOp type used to store the matrix once it's been read from disk.
StreamType	type of stream used to write the data to
MatrixArgs	additional argument types passed to MatrixType constructor

#### **Parameters**

is	input stream from which to read the data
args	additional arguments passed to MatrixType constructor

#### Returns

A MatrixType LinOp filled with data from filename

References read\_raw().

Referenced by gko::ReadableFromMatrixData< ValueType, int32 >::read().

## 45.1.4.58 read\_binary()

Reads a matrix stored in binary format from an input stream.

## **Template Parameters**

MatrixType	a ReadableFromMatrixData LinOp type used to store the matrix once it's been read from disk.
StreamType	type of stream used to write the data to
MatrixArgs	additional argument types passed to MatrixType constructor

#### **Parameters**

is	input stream from which to read the data
args	additional arguments passed to MatrixType constructor

#### Returns

A MatrixType LinOp filled with data from filename

References read\_binary\_raw().

#### 45.1.4.59 read\_binary\_raw()

Reads a matrix stored in Ginkgo's binary matrix format from an input stream.

Note that this format depends on the processor's endianness, so files from a big endian processor can't be read from a little endian processor and vice-versa.

The binary format has the following structure (in system endianness):

- A 32 byte header consisting of 4 uint64\_t values: magic = GINKGO\_\_: The highest two bytes stand for value and index type. value type: S (float), D (double), C (complex<float>), Z(complex<double>) index type: I (int32), L (int64) num\_rows: Number of rows num\_cols: Number of columns num\_entries: Number of (row, column, value) tuples to follow
- 2. Following are num\_entries blocks of size sizeof(IndexType) \* 2 + sizeof(ValueType). Each consists of a row index stored as IndexType, followed by a column index stored as IndexType and a value stored as ValueType.

### **Template Parameters**

ValueType	type of matrix values
IndexType	type of matrix indexes

#### **Parameters**

is input stream from which to read the data

#### Returns

A matrix\_data structure containing the matrix. The nonzero elements are sorted in lexicographic order of their (row, column) indexes.

#### Note

This is an advanced routine that will return the raw matrix data structure. Consider using gko::read\_binary instead.

Referenced by read\_binary().

#### 45.1.4.60 read\_generic()

Reads a matrix stored either in binary or matrix market format from an input stream.

#### **Template Parameters**

MatrixType	a ReadableFromMatrixData LinOp type used to store the matrix once it's been read from disk.	
StreamType	type of stream used to write the data to	
MatrixArgs	ixArgs additional argument types passed to MatrixType constructor	

#### **Parameters**

is	input stream from which to read the data
args	additional arguments passed to MatrixType constructor

#### Returns

A MatrixType LinOp filled with data from filename

References read\_generic\_raw().

### 45.1.4.61 read\_generic\_raw()

Reads a matrix stored in either binary or matrix market format from an input stream.

### **Template Parameters**

ValueType	type of matrix values
IndexType	type of matrix indexes

#### **Parameters**

is input stream from which to read the data

### Returns

A matrix\_data structure containing the matrix. The nonzero elements are sorted in lexicographic order of their (row, column) indexes.

#### Note

This is an advanced routine that will return the raw matrix data structure. Consider using gko::read\_generic instead.

Referenced by read\_generic().

#### 45.1.4.62 read\_raw()

Reads a matrix stored in matrix market format from an input stream.

#### **Template Parameters**

ValueType	type of matrix values
IndexType	type of matrix indexes

#### **Parameters**

is input stream from which to read the data

#### Returns

A matrix\_data structure containing the matrix. The nonzero elements are sorted in lexicographic order of their (row, column) indexes.

#### Note

This is an advanced routine that will return the raw matrix data structure. Consider using gko::read instead.

Referenced by read().

## 45.1.4.63 real()

Returns the real part of the object.

### **Template Parameters**

T type of the object

```
x the object
```

## Returns

real part of the object (by default, the object itself)

Referenced by squared\_norm().

### 45.1.4.64 reduce\_add() [1/2]

Reduce (sum) the values in the array.

### **Template Parameters**

The	type of the input data
-----	------------------------

#### **Parameters**

in	input_arr	the input array to be reduced	
in,out	result	the reduced value. The result is written into the first entry and the value in the first	
		entry is used as the initial value for the reduce.	

## 45.1.4.65 reduce\_add() [2/2]

Reduce (sum) the values in the array.

### **Template Parameters**

The	type of the input data
1110	type of the hipat data

in	input_arr	the input array to be reduced
in	init_val	the initial value

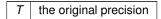
### Returns

the reduced value

### 45.1.4.66 round\_down()

Reduces the precision of the input parameter.

### **Template Parameters**



#### **Parameters**

val the value to round down
-----------------------------

#### Returns

the rounded down value

## 45.1.4.67 round\_up()

Increases the precision of the input parameter.

#### **Template Parameters**

```
T the original precision
```

#### **Parameters**

val	the value to round up
-----	-----------------------

#### Returns

the rounded up value

## 45.1.4.68 safe\_divide()

Computes the quotient of the given parameters, guarding against division by zero.

## **Template Parameters**

```
T value type of the parameters
```

#### **Parameters**

а	the dividend
b	the divisor

#### Returns

the value of a / b if b is non-zero, zero otherwise.

### 45.1.4.69 share()

Marks the object pointed to by p as shared.

Effectively converts a pointer with ownership to std::shared\_ptr.

### **Template Parameters**

OwningPointer	type of pointer with ownership to the object (has to be a smart pointer)
---------------	--

#### **Parameters**

p a pointer to the object. It must be a temporary or explicitly marked movable (rvalue reference).

Note

The original pointer p becomes invalid after this call.

Referenced by gko::preconditioner::lc< LSolverType, IndexType >::conj\_transpose(), gko::preconditioner::llu< L  $\leftarrow$  SolverType, USolverType, ReverseApply, IndexType >::conj\_transpose(), gko::preconditioner::lc< LSolverType, IndexType >::transpose(), and gko::preconditioner::llu< LSolverType, USolverType, ReverseApply, IndexType > $\leftarrow$  ::transpose().

### 45.1.4.70 squared\_norm()

Returns the squared norm of the object.

#### **Template Parameters**

```
T type of the object.
```

#### Returns

The squared norm of the object.

References conj(), and real().

## 45.1.4.71 transpose() [1/2]

Returns a batch\_dim object with its dimensions swapped for batched operators.

#### **Template Parameters**

DimensionType	datatype used to represent each dimension
---------------	---

#### **Parameters**

dimensions	original object

#### Returns

a batch\_dim object with dimensions swapped

References gko::batch\_dim< Dimensionality, DimensionType >::get\_common\_size(), and gko::batch\_dim< Dimensionality, DimensionType >::get num batch items().

Referenced by gko::preconditioner::lc< LSolverType, IndexType >::conj\_transpose(), gko::preconditioner::llu< L  $\leftarrow$  SolverType, USolverType, ReverseApply, IndexType >::conj\_transpose(), gko::preconditioner::lc< LSolverType, IndexType >::transpose(), and gko::preconditioner::llu< LSolverType, USolverType, ReverseApply, IndexType > $\leftarrow$  ::transpose().

#### 45.1.4.72 transpose() [2/2]

Returns a dim<2> object with its dimensions swapped.

#### **Template Parameters**

DimensionType	datatype used to represent each dimension
---------------	---

#### **Parameters**

```
dimensions original object
```

#### Returns

a dim<2> object with its dimensions swapped

```
253 {
254    return {dimensions[1], dimensions[0]};
255 }
```

#### 45.1.4.73 unit\_root()

```
template<typename T >
constexpr std::complex<remove_complex<T> > gko::unit_root (
    int64 n,
    int64 k = 1) [inline], [constexpr]
```

Returns the value of exp(2 \* pi \* i \* k / n), i.e.

an nth root of unity.

n	the denominator of the argument
k	the numerator of the argument. Defaults to 1.

#### **Template Parameters**

```
T the corresponding real value type.
```

References one().

#### 45.1.4.74 with\_matrix\_type()

This function returns a type that delays a call to MatrixType::create.

It can be used to set the used value and index type, as well as the executor at a later stage.

For example, the following code creates first a temporary object, which is then used later to construct an operator of the previously defined base type:

```
auto type = gko::with_matrix_type<gko::matrix::Csr>();
...
std::unique_ptr<LinOp> concrete_op
if(flag1) {
   concrete_op = type.template create<double, int>(exec);
} else {
   concrete_op = type.template create<float, int>(exec);
}
```

#### Note

This is mainly a helper function to specify the local matrix type for a gko::experimental::distributed::Matrix more easily.

#### **Template Parameters**

MatrixType	A template type that accepts two types, the first one will be set to the value type, the second one to the index type.
Args	Types of the arguments passed to MatrixType::create.

#### **Parameters**

create_args	arguments that will be forwarded to MatrixType::create
-------------	--

#### Returns

A type with a function create < value\_type, index\_type > (executor).

```
126 {
127     return detail::MatrixTypeBuilderFromValueAndIndex<MatrixType, Args...>{
128     std::forward_as_tuple(create_args...)};
129 }
```

### 45.1.4.75 write()

Writes a matrix into an output stream in matrix market format.

#### **Template Parameters**

MatrixPtrType	a (smart or raw) pointer to a WritableToMatrixData object providing data to be written.
StreamType	type of stream used to write the data to

#### **Parameters**

os	output stream where the data is to be written
matrix	the matrix to write
layout	the layout used in the output

References write\_raw().

## 45.1.4.76 write\_binary()

Writes a matrix into an output stream in binary format.

Note that this format depends on the processor's endianness, so files from a big endian processor can't be read from a little endian processor and vice-versa.

### **Template Parameters**

MatrixPtrType	a (smart or raw) pointer to a WritableToMatrixData object providing data to be written.
StreamType	type of stream used to write the data to

os	output stream where the data is to be written
matrix	the matrix to write

References write\_binary\_raw().

#### 45.1.4.77 write\_binary\_raw()

Writes a matrix\_data structure to a stream in binary format.

Note that this format depends on the processor's endianness, so files from a big endian processor can't be read from a little endian processor and vice-versa.

#### **Template Parameters**

ValueType	type of matrix values
IndexType	type of matrix indexes

#### **Parameters**

os	output stream where the data is to be written
data	the matrix data to write

## Note

This is an advanced routine that writes the raw matrix data structure. If you are trying to write an existing matrix, consider using gko::write\_binary instead.

Referenced by write\_binary().

### 45.1.4.78 write\_raw()

Writes a matrix\_data structure to a stream in matrix market format.

## **Template Parameters**

ValueType	type of matrix values
IndexType	type of matrix indexes

#### **Parameters**

os	output stream where the data is to be written
data	the matrix data to write
layout	the layout used in the output

#### Note

This is an advanced routine that writes the raw matrix data structure. If you are trying to write an existing matrix, consider using gko::write instead.

Referenced by write().

#### 45.1.4.79 zero() [1/2]

```
template<typename T >
constexpr T gko::zero ( ) [inline], [constexpr]
```

Returns the additive identity for T.

### Returns

additive identity for T

Referenced by gko::matrix::Hybrid< ValueType, IndexType >::strategy\_type::strategy\_type().

### 45.1.4.80 zero() [2/2]

Returns the additive identity for T.

#### Returns

additive identity for T

#### Note

This version takes an unused reference argument to avoid complicated calls like zero < decltype(x) > (). Instead, it allows zero(x).

## 45.2 gko::accessor Namespace Reference

The accessor namespace.

### **Classes**

· class row\_major

A row\_major accessor is a bridge between a range and the row-major memory layout.

## 45.2.1 Detailed Description

The accessor namespace.

# 45.3 gko::batch::log Namespace Reference

The logger namespace.

#### **Classes**

· class BatchConvergence

Logs the final residuals and iteration counts for a batch solver.

## 45.3.1 Detailed Description

The logger namespace.

Logging

# 45.4 gko::experimental::distributed Namespace Reference

The distributed namespace.

## **Namespaces**

· preconditioner

The Preconditioner namespace.

#### **Classes**

· class DistributedBase

A base class for distributed objects.

struct index\_map

This class defines mappings between global and local indices.

· class Matrix

The Matrix class defines a (MPI-)distributed matrix.

class Partition

Represents a partition of a range of indices [0, size) into a disjoint set of parts.

· class Vector

Vector is a format which explicitly stores (multiple) distributed column vectors in a dense storage format.

### **Typedefs**

using comm\_index\_type = int

Index type for enumerating processes in a distributed application.

#### **Enumerations**

enum index\_space { index\_space::local, index\_space::non\_local, index\_space::combined }
 Index space classification for the locally stored indices.

#### **Functions**

template<typename ValueType >
 detail::temporary\_conversion< experimental::distributed::Vector< ValueType > > make\_temporary\_conversion
 (LinOp \*matrix)

Convert the given LinOp from experimental::distributed::Vector<...> to experimental::distributed::Vector< Value ← Type>.

• template<typename ValueType >

detail::temporary\_conversion < const experimental::distributed::Vector < ValueType > > make\_temporary\_conversion (const LinOp \*matrix)

Convert the given LinOp from experimental::distributed::Vector<...> to experimental::distributed::Vector< Value ← Type>.

template < typename ValueType , typename Function , typename... Args > void precision\_dispatch (Function fn, Args \*... linops)

Calls the given function with each given argument LinOp temporarily converted into experimental::distributed:: Vector< Value Type> as parameters.

template < typename ValueType, typename Function >
 void precision dispatch real complex (Function fn, const LinOp \*in, LinOp \*out)

Calls the given function with the given LinOps temporarily converted to experimental::distributed::Vector< Value ← Type>\* as parameters.

template<typename ValueType, typename Function >
 void precision\_dispatch\_real\_complex (Function fn, const LinOp \*alpha, const LinOp \*in, LinOp \*out)

Calls the given function with the given LinOps temporarily converted to experimental::distributed::Vector< Value ← Type>\* as parameters.

template<typename ValueType, typename Function >
 void precision\_dispatch\_real\_complex (Function fn, const LinOp \*alpha, const LinOp \*in, const LinOp \*beta,
 LinOp \*out)

Calls the given function with the given LinOps temporarily converted to experimental::distributed::Vector< Value ← Type>\* as parameters.

template < typename LocalIndexType, typename GlobalIndexType >
 std::unique\_ptr < Partition < LocalIndexType, GlobalIndexType > build\_partition\_from\_local\_range (std
 ::shared\_ptr < const Executor > exec, mpi::communicator comm, span local\_range)

Builds a partition from a local range.

template<typename LocalIndexType, typename GlobalIndexType >
 std::unique\_ptr< Partition< LocalIndexType, GlobalIndexType > build\_partition\_from\_local\_size (std
 ::shared\_ptr< const Executor > exec, mpi::communicator comm, size\_type local\_size)

Builds a partition from a local size.

# 45.4.1 Detailed Description

The distributed namespace.

# 45.4.2 Typedef Documentation

#### 45.4.2.1 comm\_index\_type

```
using gko::experimental::distributed::comm_index_type = typedef int
```

Index type for enumerating processes in a distributed application.

Conforms to the MPI C interface of e.g. MPI rank or size

# 45.4.3 Enumeration Type Documentation

# 45.4.3.1 index\_space

```
enum gko::experimental::distributed::index_space [strong]
```

Index space classification for the locally stored indices.

The definitions of the enum values is clarified in index\_map.

# Enumerator

local	indices that are locally owned
non_local	indices that are owned by other processes
combined	both local and non_local indices

```
23 {
24 local,
```

#### 45.4.4 Function Documentation

#### 45.4.4.1 build\_partition\_from\_local\_range()

Builds a partition from a local range.

#### **Parameters**

exec	the Executor on which the partition should be built.
comm	the communicator used to determine the global partition.
local_range	the start and end indices of the local range.

#### Warning

```
This throws, if the resulting partition would contain gaps. That means that for a partition of size n every local range r_i = [s_i, e_i) either s_i != 0 and another local range r_j = [s_j, e_j = s_i) exists, or e_i != n and another local range r_j = [s_j = e_i, e_j) exists.
```

#### Returns

a Partition where each range has the individual local\_start and local\_ends.

# 45.4.4.2 build\_partition\_from\_local\_size()

Builds a partition from a local size.

#### **Parameters**

exec	the Executor on which the partition should be built.
comm	the communicator used to determine the global partition.
local_range	the number of the locally owned indices

#### Returns

```
a Partition where each range has the specified local size. More specifically, if this is called on process i with local_size s_i, then the range i has size s_i, and range r_i = [start, start + s_i), where start = sum_j^{(i-1)} s_j.
```

#### 45.4.4.3 make\_temporary\_conversion() [1/2]

Convert the given LinOp from experimental::distributed::Vector<...> to experimental::distributed::Vector<Value $\leftarrow$  Type>.

The conversion tries to convert the input LinOp to all Dense types with value type recursively reachable by next⇔ \_precision<...> starting from the ValueType template parameter. This means that all real-to-real and complex-to-complex conversions for default precisions are being considered. If the input matrix is non-const, the contents of the modified converted object will be converted back to the input matrix when the returned object is destroyed. This may lead to a loss of precision!

#### **Parameters**

matrix	the input matrix which is supposed to be converted. It is wrapped unchanged if it is already of type
	experimental::distributed::Vector <valuetype>, otherwise it will be converted to this type if possible.</valuetype>

#### Returns

a detail::temporary\_conversion pointing to the (potentially converted) object.

## **Exceptions**

NotSupported	if the input matrix cannot be converted to experimental::distributed::Vector <valuetype></valuetype>
--------------	--

# **Template Parameters**

ValueType	the value type into whose associated experimental::distributed::Vector type to convert the input
	LinOp.

#### 45.4.4.4 make\_temporary\_conversion() [2/2]

Convert the given LinOp from experimental::distributed::Vector<...> to experimental::distributed::Vector<Value $\leftarrow$  Type>.

The conversion tries to convert the input LinOp to all Dense types with value type recursively reachable by next← \_precision<...> starting from the ValueType template parameter. This means that all real-to-real and complex-to-complex conversions for default precisions are being considered. If the input matrix is non-const, the contents of the modified converted object will be converted back to the input matrix when the returned object is destroyed. This may lead to a loss of precision!

#### **Parameters**

matrix	the input matrix which is supposed to be converted. It is wrapped unchanged if it is already of type
	experimental::distributed::Vector <valuetype>, otherwise it will be converted to this type if possible.</valuetype>

#### Returns

a detail::temporary\_conversion pointing to the (potentially converted) object.

#### **Exceptions**

	NotSupported	if the input matrix cannot be converted to experimental::distributed::Vector <valuetype></valuetype>	
--	--------------	--	--

# **Template Parameters**

ValueType	the value type into whose associated experimental::distributed::Vector type to convert the input
	LinOp.

## 45.4.4.5 precision\_dispatch()

Calls the given function with each given argument LinOp temporarily converted into experimental::distributed::

Vector<ValueType> as parameters.

#### **Parameters**

fn	the given function. It will be passed one (potentially const) experimental::distributed::Vector <valuetype>* parameter per parameter in the parameter pack linops.</valuetype>
linops	the given arguments to be converted and passed on to fn.

#### **Template Parameters**

ſ	ValueType	the value type to use for the parameters of fn.
	Function	the function pointer, lambda or other functor type to call with the converted arguments.
Ī	Args	the argument type list.

## 45.4.4.6 precision\_dispatch\_real\_complex() [1/3]

Calls the given function with the given LinOps temporarily converted to experimental::distributed::Vector<Value←
Type>∗ as parameters.

If ValueType is real and both input vectors are complex, uses experimental::distributed::Vector::get\_real\_view() to convert them into real matrices after precision conversion.

#### See also

precision\_dispatch()

#### 45.4.4.7 precision\_dispatch\_real\_complex() [2/3]

Calls the given function with the given LinOps temporarily converted to experimental::distributed::Vector<Value $\leftarrow$ Type>\* as parameters.

If ValueType is real and both input vectors are complex, uses experimental::distributed::Vector::get\_real\_view() to convert them into real matrices after precision conversion.

#### See also

precision\_dispatch()

#### 45.4.4.8 precision\_dispatch\_real\_complex() [3/3]

Calls the given function with the given LinOps temporarily converted to experimental::distributed::Vector<Value 
Type>\* as parameters.

If ValueType is real and both input vectors are complex, uses experimental::distributed::Vector::get\_real\_view() to convert them into real matrices after precision conversion.

See also

precision dispatch()

# 45.5 gko::experimental::distributed::preconditioner Namespace Reference

The Preconditioner namespace.

#### Classes

· class Schwarz

A Schwarz preconditioner is a simple domain decomposition preconditioner that generalizes the Block Jacobi preconditioner, incorporating options for different local subdomain solvers and overlaps between the subdomains.

# 45.5.1 Detailed Description

The Preconditioner namespace.

# 45.6 gko::experimental::mpi Namespace Reference

The mpi namespace, contains wrapper for many MPI functions.

#### Classes

· class communicator

A thin wrapper of MPI\_Comm that supports most MPI calls.

· class contiguous\_type

A move-only wrapper for a contiguous MPI\_Datatype.

· class environment

Class that sets up and finalizes the MPI environment.

· class request

The request class is a light, move-only wrapper around the MPI\_Request handle.

· struct status

The status struct is a light wrapper around the MPI\_Status struct.

struct type\_impl

A struct that is used to determine the MPI\_Datatype of a specified type.

· class window

This class wraps the MPI\_Window class with RAII functionality.

#### **Enumerations**

· enum thread\_type

This enum specifies the threading type to be used when creating an MPI environment.

# **Functions**

• constexpr bool is\_gpu\_aware ()

Return if GPU aware functionality is available.

• int map\_rank\_to\_device\_id (MPI\_Comm comm, int num\_devices)

Maps each MPI rank to a single device id in a round robin manner.

std::vector< status > wait\_all (std::vector< request > &req)

Allows a rank to wait on multiple request handles.

• bool requires\_host\_buffer (const std::shared\_ptr< const Executor > &exec, const communicator &comm)

Checks if the combination of Executor and communicator requires passing MPI buffers from the host memory.

• double get\_walltime ()

Get the rank in the communicator of the calling process.

# 45.6.1 Detailed Description

The mpi namespace, contains wrapper for many MPI functions.

# 45.6.2 Function Documentation

# 45.6.2.1 get\_walltime()

```
double gko::experimental::mpi::get_walltime () [inline]
```

Get the rank in the communicator of the calling process.

#### **Parameters**

```
comm the communicator

1494 { return MPI_Wtime(); }
```

# 45.6.2.2 map\_rank\_to\_device\_id()

Maps each MPI rank to a single device id in a round robin manner.

#### **Parameters**

comm	used to determine the node-local rank, if no suitable environment variable is available.
num_devices	the number of devices per node.

#### Returns

device id that this rank should use.

#### 45.6.2.3 wait\_all()

Allows a rank to wait on multiple request handles.

#### **Parameters**

req	The vector of request handles to be waited on.
-----	--

#### Returns

status The vector of status objects that can be queried.

# 45.7 gko::experimental::reorder Namespace Reference

The Reorder namespace.

# **Classes**

class Amd

Computes a Approximate Minimum Degree (AMD) reordering of an input matrix.

class Mc64

MC64 is an algorithm for permuting large entries to the diagonal of a sparse matrix.

class Rcm

Rcm (Reverse Cuthill-McKee) is a reordering algorithm minimizing the bandwidth of a matrix.

· class ScaledReordered

Provides an interface to wrap reorderings like Rcm and diagonal scaling like equilibration around a LinOp like e.g.

# **Enumerations**

enum mc64\_strategy

Strategy defining the goal of the MC64 reordering.

# 45.7.1 Detailed Description

The Reorder namespace.

# 45.7.2 Enumeration Type Documentation

#### 45.7.2.1 mc64 strategy

```
enum gko::experimental::reorder::mc64_strategy [strong]
```

Strategy defining the goal of the MC64 reordering.

max\_diagonal\_product aims at maximizing the product of absolute diagonal entries. max\_diag\_sum aims at maximizing the sum of absolute values for the diagonal entries.

43 { max\_diagonal\_product, max\_diagonal\_sum };

# 45.8 gko::factorization Namespace Reference

The Factorization namespace.

#### **Classes**

• class Ic

Represents an incomplete Cholesky factorization (IC(0)) of a sparse matrix.

class Ilu

Represents an incomplete LU factorization – ILU(0) – of a sparse matrix.

• class Parlc

ParlC is an incomplete Cholesky factorization which is computed in parallel.

· class Parlct

ParICT is an incomplete threshold-based Cholesky factorization which is computed in parallel.

· class Parllu

ParILU is an incomplete LU factorization which is computed in parallel.

class Parllut

ParILUT is an incomplete threshold-based LU factorization which is computed in parallel.

# 45.8.1 Detailed Description

The Factorization namespace.

# 45.9 gko::log Namespace Reference

The logger namespace.

#### **Classes**

· class Convergence

Convergence is a Logger which logs data strictly from the criterion\_check\_completed event.

· struct criterion\_data

Struct representing Criterion related data.

· class EnableLogging

EnableLogging is a mixin which should be inherited by any class which wants to enable logging.

· struct executor data

Struct representing Executor related data.

· struct iteration complete data

Struct representing iteration complete related data.

· struct linop\_data

Struct representing LinOp related data.

struct linop\_factory\_data

Struct representing LinOp factory related data.

class Loggable

Loggable class is an interface which should be implemented by classes wanting to support logging.

· struct operation data

Struct representing Operator related data.

· class Papi

Papi is a Logger which logs every event to the PAPI software.

class PerformanceHint

PerformanceHint is a Logger which analyzes the performance of the application and outputs hints for unnecessary copies and allocations.

· struct polymorphic object data

Struct representing PolymorphicObject related data.

class ProfilerHook

This Logger can be used to annotate the execution of Ginkgo functionality with profiler-specific ranges.

· class profiling\_scope\_guard

Scope guard that annotates its scope with the provided profiler hooks.

class Record

Record is a Logger which logs every event to an object.

class SolverProgress

This Logger outputs the value of all scalar values (and potentially vectors) stored internally by the solver after each iteration.

· class Stream

Stream is a Logger which logs every event to a stream.

# **Enumerations**

enum profile\_event\_category {
 profile\_event\_category::memory, profile\_event\_category::operation, profile\_event\_category::object,
 profile\_event\_category::linop,
 profile\_event\_category::factory, profile\_event\_category::solver, profile\_event\_category::criterion, profile\_event\_category::user,
 profile\_event\_category::internal }

Categorization of logger events.

# 45.9.1 Detailed Description

The logger namespace .

The Logging namespace.

Logging

# 45.9.2 Enumeration Type Documentation

# 45.9.2.1 profile\_event\_category

```
enum gko::log::profile_event_category [strong]
```

Categorization of logger events.

#### Enumerator

memory	Memory allocation.
operation	Kernel execution and data movement.
object	PolymorphicObject events.
linop	LinOp events.
factory	LinOpFactory events.
solver	Solver events.
criterion	Stopping criterion events.
user	User-defined events.
internal	For development use.

```
22
24 memory,
26 operation,
28 object,
30 linop,
32 factory,
34 solver,
36 criterion,
38 user,
40 internal,
41 };
```

# 45.10 gko::matrix Namespace Reference

The matrix namespace.

# **Classes**

• class Coo

COO stores a matrix in the coordinate matrix format.

• class Csr

CSR is a matrix format which stores only the nonzero coefficients by compressing each row of the matrix (compressed sparse row format).

· class Dense

Dense is a matrix format which explicitly stores all values of the matrix.

class Diagonal

This class is a utility which efficiently implements the diagonal matrix (a linear operator which scales a vector row wise).

class Ell

ELL is a matrix format where stride with explicit zeros is used such that all rows have the same number of stored elements.

· class Fbcsr

Fixed-block compressed sparse row storage matrix format.

class Fft

This LinOp implements a 1D Fourier matrix using the FFT algorithm.

• class Fft2

This LinOp implements a 2D Fourier matrix using the FFT algorithm.

class Fft3

This LinOp implements a 3D Fourier matrix using the FFT algorithm.

· class Hybrid

HYBRID is a matrix format which splits the matrix into ELLPACK and COO format.

· class Identity

This class is a utility which efficiently implements the identity matrix (a linear operator which maps each vector to itself).

· class IdentityFactory

This factory is a utility which can be used to generate Identity operators.

· class Permutation

Permutation is a matrix format that represents a permutation matrix, i.e.

class RowGatherer

RowGatherer is a matrix "format" which stores the gather indices arrays which can be used to gather rows to another matrix.

· class ScaledPermutation

ScaledPermutation is a matrix combining a permutation with scaling factors.

· class Sellp

SELL-P is a matrix format similar to ELL format.

class SparsityCsr

SparsityCsr is a matrix format which stores only the sparsity pattern of a sparse matrix by compressing each row of the matrix (compressed sparse row format).

# **Enumerations**

```
    enum permute_mode: unsigned {
        permute_mode::none = 0b000u, permute_mode::rows = 0b001u, permute_mode::columns = 0b010u,
        permute_mode::symmetric = 0b011u,
        permute_mode::inverse = 0b100u, permute_mode::inverse_rows = 0b101u, permute_mode::inverse_columns
        = 0b110u, permute_mode::inverse_symmetric = 0b111u }
```

Specifies how a permutation will be applied to a matrix.

# **Functions**

permute\_mode operator (permute\_mode a, permute\_mode b)

Combines two permutation modes.

• permute\_mode operator& (permute\_mode a, permute\_mode b)

Computes the intersection of two permutation modes.

permute\_mode operator<sup>^</sup> (permute\_mode a, permute\_mode b)

Computes the symmetric difference of two permutation modes.

• std::ostream & operator<< (std::ostream &stream, permute\_mode mode)

Prints a permutation mode.

# 45.10.1 Detailed Description

The matrix namespace.

# 45.10.2 Enumeration Type Documentation

#### 45.10.2.1 permute\_mode

```
enum gko::matrix::permute_mode : unsigned [strong]
```

Specifies how a permutation will be applied to a matrix.

For the effect of the different permutation modes, see the following table.

mode	entry mapping	matrix representation
none	A'(i,j) = A(i,j)	A' = A
rows	A'(i,j) = A(p[i],j)	A' = PA
columns	A'(i,j) = A(i,p[j])	$A' = AP^T$
inverse_rows	A'(p[i],j) = A(i,j)	$A' = P^{-1}A$
inverse_columns	A'(i, p[j]) = A(i, j)	$A' = AP^{-T}$
symmetric	A'(i,j) = A(p[i], p[j])	$A' = PAP^T$
inverse_symmetric	A'(p[i],p[j]) = A(i,j)	$A' = P^{-1}AP^{-T}$

#### Enumerator

none	Neither rows nor columns will be permuted.
rows	The rows will be permuted.
columns	The columns will be permuted.
symmetric	The rows and columns will be permuted. This is equivalent to
	permute_mode::rows   permute_mode::columns.
inverse	The permutation will be inverted before being applied.
inverse_rows	The rows will be permuted using the inverse permutation. This is equivalent to
	<pre>permute_mode::rows   permute_mode::inverse.</pre>

#### Enumerator

inverse_columns	The columns will be permuted using the inverse permutation. This is equivalent to	
	permute_mode::columns   permute_mode::inverse.	
inverse_symmetric	The rows and columns will be permuted using the inverse permutation. This is equivalent	
	<pre>to permute_mode::symmetric   permute_mode::inverse.</pre>	

```
42 : unsigned {
44     none = 0b000u,
46     rows = 0b001u,
48     columns = 0b010u,
53     symmetric = 0b011u,
55     inverse = 0b10u,
60     inverse_rows = 0b101u,
65     inverse_columns = 0b110u,
67     inverse_symmetric = 0b111u
68     rows = 0b110u,
69     rows = 0b110u,
60     rows = 0b110u,
61     rows = 0b110u,
62     rows = 0b110u,
63     rows = 0b110u,
64     rows = 0b110u,
65     rows = 0b110u,
66     rows = 0b111u
```

# 45.11 gko::multigrid Namespace Reference

The multigrid components namespace.

## **Classes**

· class EnableMultigridLevel

The EnableMultigridLevel gives the default implementation of MultigridLevel with composition and provides  $set\_ \leftarrow multigrid\_level$  function.

class FixedCoarsening

FixedCoarsening is a very simple coarse grid generation algorithm.

class MultigridLevel

This class represents two levels in a multigrid hierarchy.

class Pgm

Parallel graph match (Pgm) is the aggregate method introduced in the paper M.

# 45.11.1 Detailed Description

The multigrid components namespace.

# 45.12 gko::name\_demangling Namespace Reference

The name demangling namespace.

## **Functions**

template<typename T >
 std::string get\_static\_type (const T &)

This function uses name demangling facilities to get the name of the static type (T) of the object passed in arguments.

template<typename T >
 std::string get\_dynamic\_type (const T &t)

This function uses name demangling facilities to get the name of the dynamic type of the object passed in arguments.

# 45.12.1 Detailed Description

The name demangling namespace.

## 45.12.2 Function Documentation

## 45.12.2.1 get\_dynamic\_type()

```
template<typename T > std::string gko::name_demangling::get_dynamic_type ( const T & t )
```

This function uses name demangling facilities to get the name of the dynamic type of the object passed in arguments.

## **Template Parameters**

T the type of the object to demangle

#### **Parameters**

t the object we get the dynamic type of

```
73 {
74     return get_type_name(typeid(t));
75 }
```

## 45.12.2.2 get\_static\_type()

This function uses name demangling facilities to get the name of the static type (T) of the object passed in arguments.

#### **Template Parameters**

T the type of the object to demangle

#### **Parameters**

unused

# 45.13 gko::preconditioner Namespace Reference

The Preconditioner namespace.

#### Classes

· struct block interleaved storage scheme

Defines the parameters of the interleaved block storage scheme used by block-Jacobi blocks.

• class Ic

The Incomplete Cholesky (IC) preconditioner solves the equation  $LL^H * x = b$  for a given lower triangular matrix L and the right hand side b (can contain multiple right hand sides).

class IIu

The Incomplete LU (ILU) preconditioner solves the equation LUx = b for a given lower triangular matrix L, an upper triangular matrix U and the right hand side b (can contain multiple right hand sides).

· class Isai

The Incomplete Sparse Approximate Inverse (ISAI) Preconditioner generates an approximate inverse matrix for a given square matrix A, lower triangular matrix L, upper triangular matrix U or symmetric positive (spd) matrix B.

class Jacobi

A block-Jacobi preconditioner is a block-diagonal linear operator, obtained by inverting the diagonal blocks of the source operator.

## **Enumerations**

· enum isai\_type

This enum lists the types of the ISAI preconditioner.

# 45.13.1 Detailed Description

The Preconditioner namespace.

# 45.13.2 Enumeration Type Documentation

## 45.13.2.1 isai\_type

```
enum gko::preconditioner::isai_type [strong]
```

This enum lists the types of the ISAI preconditioner.

ISAI can either be generated for a general square matrix, a lower triangular matrix, an upper triangular matrix or an spd matrix.

```
36 { lower, upper, general, spd };
```

# 45.14 gko::reorder Namespace Reference

The Reorder namespace.

#### **Classes**

· class Rcm

Rcm (Reverse Cuthill-McKee) is a reordering algorithm minimizing the bandwidth of a matrix.

· class ReorderingBase

The ReorderingBase class is a base class for all the reordering algorithms.

• struct ReorderingBaseArgs

This struct is used to pass parameters to the EnableDefaultReorderingBaseFactory::generate() method.

# **Typedefs**

- template<typename IndexType = int32>
   using ReorderingBaseFactory = AbstractFactory< ReorderingBase< IndexType >, ReorderingBaseArgs >
   Declares an Abstract Factory specialized for ReorderingBases.
- template<typename ConcreteFactory , typename ConcreteReorderingBase , typename ParametersType , typename IndexType = int32, typename PolymorphicBase = ReorderingBaseFactory<IndexType>> using EnableDefaultReorderingBaseFactory = EnableDefaultFactory< ConcreteFactory, Concrete← ReorderingBase, ParametersType, PolymorphicBase >

This is an alias for the EnableDefaultFactory mixin, which correctly sets the template parameters to enable a subclass of ReorderingBaseFactory.

# 45.14.1 Detailed Description

The Reorder namespace.

The reordering namespace.

# 45.14.2 Typedef Documentation

# 45.14.2.1 EnableDefaultReorderingBaseFactory

template<typename ConcreteFactory , typename ConcreteReorderingBase , typename ParametersType , typename IndexType = int32, typename PolymorphicBase = ReorderingBaseFactory<IndexType>> using gko::reorder::EnableDefaultReorderingBaseFactory = typedef EnableDefaultFactory<Concrete↔Factory, ConcreteReorderingBase, ParametersType, PolymorphicBase>

This is an alias for the EnableDefaultFactory mixin, which correctly sets the template parameters to enable a subclass of ReorderingBaseFactory.

# **Template Parameters**

ConcreteFactory	the concrete factory which is being implemented [CRTP parameter]
ConcreteReorderingBase	the concrete ReorderingBase type which this factory produces, needs to have a constructor which takes a const ConcreteFactory *, and a const ReorderingBaseArgs * as parameters.
ParametersType	a subclass of enable_parameters_type template which defines all of the parameters of the factory
PolymorphicBase Generated by Doxygen	parent of ConcreteFactory in the polymorphic hierarchy, has to be a subclass of ReorderingBaseFactory

# 45.15 gko::solver Namespace Reference

The ginkgo Solve namespace.

# **Namespaces**

· multigrid

The solver multigrid namespace.

#### **Classes**

· class ApplyWithInitialGuess

ApplyWithInitialGuess provides a way to give the input guess for apply function.

class Bicg

BICG or the Biconjugate gradient method is a Krylov subspace solver.

· class Bicgstab

BiCGSTAB or the Bi-Conjugate Gradient-Stabilized is a Krylov subspace solver.

class CbGmres

CB-GMRES or the compressed basis generalized minimal residual method is an iterative type Krylov subspace method which is suitable for nonsymmetric linear systems.

class Cg

CG or the conjugate gradient method is an iterative type Krylov subspace method which is suitable for symmetric positive definite methods.

• class Cgs

CGS or the conjugate gradient square method is an iterative type Krylov subspace method which is suitable for general systems.

· class EnableApplyWithInitialGuess

EnableApplyWithInitialGuess providing default operation for ApplyWithInitialGuess with correct validation and log.

• class EnableIterativeBase

A LinOp deriving from this CRTP class stores a stopping criterion factory and allows applying with a guess.

class EnablePreconditionable

Mixin providing default operation for Preconditionable with correct value semantics.

· class EnablePreconditionedIterativeSolver

A LinOp implementing this interface stores a system matrix and stopping criterion factory.

class EnableSolverBase

A LinOp deriving from this CRTP class stores a system matrix.

class Fcg

FCG or the flexible conjugate gradient method is an iterative type Krylov subspace method which is suitable for symmetric positive definite methods.

· class Gcr

GCR or the generalized conjugate residual method is an iterative type Krylov subspace method similar to GMRES which is suitable for nonsymmetric linear systems.

· class Gmres

GMRES or the generalized minimal residual method is an iterative type Krylov subspace method which is suitable for nonsymmetric linear systems.

struct has\_with\_criteria

Helper structure to test if the Factory of SolverType has a function with\_criteria.

· class Idi

IDR(s) is an efficient method for solving large nonsymmetric systems of linear equations.

class Ir

Iterative refinement (IR) is an iterative method that uses another coarse method to approximate the error of the current solution via the current residual.

· class IterativeBase

A LinOp implementing this interface stores a stopping criterion factory.

class LowerTrs

LowerTrs is the triangular solver which solves the system L x = b, when L is a lower triangular matrix.

class Multigrid

Multigrid methods have a hierarchy of many levels, whose corase level is a subset of the fine level, of the problem.

class UpperTrs

UpperTrs is the triangular solver which solves the system Ux = b, when U is an upper triangular matrix.

· struct workspace traits

Traits class providing information on the type and location of workspace vectors inside a solver.

#### **Enumerations**

enum initial\_guess\_mode { initial\_guess\_mode::zero, initial\_guess\_mode::rhs, initial\_guess\_mode::provided }

Give a initial guess mode about the input of the apply method.

• enum trisolve\_algorithm

A helper for algorithm selection in the triangular solvers.

## **Functions**

template<typename ValueType >
 auto build\_smoother (std::shared\_ptr< const LinOpFactory > factory, size\_type iteration=1, ValueType
 relaxation factor=0.9)

build\_smoother gives a shortcut to build a smoother by IR(Richardson) with limited stop criterion(iterations and relacation\_factor).

template < typename ValueType >
 auto build\_smoother (std::shared\_ptr < const LinOp > solver, size\_type iteration=1, ValueType relaxation\_
 factor=0.9)

build\_smoother gives a shortcut to build a smoother by IR(Richardson) with limited stop criterion(iterations and relacation\_factor).

#### 45.15.1 Detailed Description

The ginkgo Solve namespace.

The ginkgo Solver namespace.

# 45.15.2 Enumeration Type Documentation

#### 45.15.2.1 initial\_guess\_mode

```
enum gko::solver::initial_guess_mode [strong]
```

Give a initial guess mode about the input of the apply method.

#### Enumerator

zero	the input is zero
rhs	the input is right hand side
provided	the input is provided

```
33 {
37 zero,
41 rhs,
45 provided
6 }
```

## 45.15.2.2 trisolve\_algorithm

```
enum gko::solver::trisolve_algorithm [strong]
```

A helper for algorithm selection in the triangular solvers.

It currently only matters for the Cuda executor as there, we have a choice between the Ginkgo syncfree and cuS← PARSE implementations.

```
40 { sparselib, syncfree };
```

# 45.15.3 Function Documentation

## 45.15.3.1 build\_smoother() [1/2]

build\_smoother gives a shortcut to build a smoother by IR(Richardson) with limited stop criterion(iterations and relacation\_factor).

#### **Parameters**

solver	the shared pointer of solver
iteration	the maximum number of iteration, which default is 1
relaxation_factor	the relaxation factor for Richardson

# Returns

the pointer of Ir(Richardson)

Note

this is the overload function for LinOp.

```
328 {
329     auto exec = solver->get_executor();
330     return Ir<ValueType>::build()
331     .with_generated_solver(solver)
332     .with_relaxation_factor(relaxation_factor)
333     .with_criteria(gko::stop::Iteration::build().with_max_iters(iteration))
334     .on(exec);
335 }
```

## 45.15.3.2 build\_smoother() [2/2]

build\_smoother gives a shortcut to build a smoother by IR(Richardson) with limited stop criterion(iterations and relacation\_factor).

#### **Parameters**

factory	the shared pointer of factory
iteration	the maximum number of iteration, which default is 1
relaxation_factor	the relaxation factor for Richardson

#### Returns

the pointer of Ir(Richardson)

# 45.16 gko::solver::multigrid Namespace Reference

The solver multigrid namespace.

#### **Enumerations**

• enum cycle

cycle defines which kind of multigrid cycle can be used.

• enum mid\_smooth\_type

mid\_smooth\_type gives the options to handle the middle smoother behavior between the two cycles in the same level.

# 45.16.1 Detailed Description

The solver multigrid namespace.

# 45.16.2 Enumeration Type Documentation

#### 45.16.2.1 cycle

```
enum gko::solver::multigrid::cycle [strong]
```

cycle defines which kind of multigrid cycle can be used.

It contains V, W, and F cycle.

- V, W cycle uses the algorithm according to Briggs, Henson, and McCormick: A multigrid tutorial 2nd Edition.
- F cycle uses the algorithm according to Trottenberg, Oosterlee, and Schuller: Multigrid 1st Edition. F cycle first uses the recursive call but second uses the V-cycle call such that F-cycle is between V and W cycle.

#### 45.16.2.2 mid\_smooth\_type

```
enum gko::solver::multigrid::mid_smooth_type [strong]
```

mid\_smooth\_type gives the options to handle the middle smoother behavior between the two cycles in the same level.

It only affects the behavior when there's no operation between the post smoother of previous cycle and the pre smoother of next cycle. Thus, it only affects W cycle and F cycle.

- both: gives the same behavior as the original algorithm, which use posts smoother from previous cycle and pre smoother from next cycle.
- · post\_smoother: only uses the post smoother of previous cycle in the mid smoother
- · pre\_smoother: only uses the pre smoother of next cycle in the mid smoother
- standalone: uses the defined smoother in the mid smoother

# 45.17 gko::stop Namespace Reference

The Stopping criterion namespace.

#### **Classes**

· class AbsoluteResidualNorm

The AbsoluteResidualNorm class is a stopping criterion which stops the iteration process when the residual norm is below a certain threshold, i.e.

· class Combined

The Combined class is used to combine multiple criterions together through an OR operation.

class Criterion

The Criterion class is a base class for all stopping criteria.

struct CriterionArgs

This struct is used to pass parameters to the EnableDefaultCriterionFactoryCriterionFactory::generate() method.

· class ImplicitResidualNorm

The ImplicitResidualNorm class is a stopping criterion which stops the iteration process when the implicit residual norm is below a certain threshold relative to.

· class Iteration

The Iteration class is a stopping criterion which stops the iteration process after a preset number of iterations.

· class RelativeResidualNorm

The RelativeResidualNorm class is a stopping criterion which stops the iteration process when the residual norm is below a certain threshold relative to the norm of the right-hand side, i.e.

class ResidualNorm

The ResidualNorm class is a stopping criterion which stops the iteration process when the actual residual norm is below a certain threshold relative to.

· class ResidualNormBase

The ResidualNormBase class provides a framework for stopping criteria related to the residual norm.

· class ResidualNormReduction

The ResidualNormReduction class is a stopping criterion which stops the iteration process when the residual norm is below a certain threshold relative to the norm of the initial residual, i.e.

· class Time

The Time class is a stopping criterion which stops the iteration process after a certain amount of time has passed.

# **Typedefs**

using CriterionFactory = AbstractFactory < Criterion, CriterionArgs >

Declares an Abstract Factory specialized for Criterions.

 template<typename ConcreteFactory , typename ConcreteCriterion , typename ParametersType , typename PolymorphicBase = CriterionFactory>

using EnableDefaultCriterionFactory = EnableDefaultFactory< ConcreteFactory, ConcreteCriterion, ParametersType, PolymorphicBase >

This is an alias for the EnableDefaultFactory mixin, which correctly sets the template parameters to enable a subclass of CriterionFactory.

## **Enumerations**

enum mode

The mode for the residual norm criterion.

# **Functions**

template<typename FactoryContainer >
 std::shared\_ptr< const CriterionFactory > combine (FactoryContainer &&factories)

Combines multiple criterion factories into a single combined criterion factory.

# 45.17.1 Detailed Description

The Stopping criterion namespace.

Stopping criteria

# 45.17.2 Typedef Documentation

# 45.17.2.1 EnableDefaultCriterionFactory

```
template<typename ConcreteFactory , typename ConcreteCriterion , typename ParametersType ,
typename PolymorphicBase = CriterionFactory>
using gko::stop::EnableDefaultCriterionFactory = typedef EnableDefaultFactory<ConcreteFactory,
ConcreteCriterion, ParametersType, PolymorphicBase>
```

This is an alias for the EnableDefaultFactory mixin, which correctly sets the template parameters to enable a subclass of CriterionFactory.

## **Template Parameters**

ConcreteFactory	the concrete factory which is being implemented [CRTP parameter]
ConcreteCriterion	the concrete Criterion type which this factory produces, needs to have a constructor which takes a const ConcreteFactory *, and a const CriterionArgs * as parameters.
ParametersType	a subclass of enable_parameters_type template which defines all of the parameters of the factory
PolymorphicBase	parent of ConcreteFactory in the polymorphic hierarchy, has to be a subclass of CriterionFactory

# 45.18 gko::syn Namespace Reference

The Synthesizer namespace.

## **Classes**

struct range

range records start, end, step in template

struct type\_list

type\_list records several types in template

struct value\_list

value\_list records several values with the same type in template.

# **Typedefs**

```
    template < typename List1 , typename List2 > using concatenate = typename detail::concatenate_impl < List1, List2 >::type concatenate combines two value_list into one value_list.
    template < typename T > using as_list = typename detail::as_list_impl < T >::type as_list < T> gives the alias type of as_list_impl < T>::type.
```

#### **Functions**

```
    template<typename T, T... Value>
    constexpr std::array< T, sizeof...(Value)> as_array (value_list< T, Value... > vI)
    as_array<T> returns the array from value_list.
```

# 45.18.1 Detailed Description

The Synthesizer namespace.

# 45.18.2 Typedef Documentation

#### 45.18.2.1 as\_list

```
template<typename T >
using gko::syn::as_list = typedef typename detail::as_list_impl<T>::type
as_list<T> gives the alias type of as_list_impl<T>::type.
```

It gives a list (itself) if input is already a list, or generates list type from range input.

# **Template Parameters**

```
T list or range
```

#### 45.18.2.2 concatenate

```
template<typename List1 , typename List2 >
using gko::syn::concatenate = typedef typename detail::concatenate_impl<List1, List2>::type
concatenate combines two value list into one value list.
```

# **Template Parameters**

List1	the first list
List2	the second list

## 45.18.3 Function Documentation

# 45.18.3.1 as\_array()

as\_array<T> returns the array from value\_list.

It will be helpful if using for in runtime on the array.

#### **Template Parameters**

T	the type of value_list
Value	the values of value_list

#### **Parameters**

```
value_list the input value_list
```

#### Returns

std::array the std::array contains the values of value\_list

```
176 {
177     return std::array<T, sizeof...(Value)>{Value...};
178 }
```

References gko::array.

# 45.19 gko::xstd Namespace Reference

The namespace for functionalities after C++14 standard.

# **Typedefs**

template<typename... Ts>
 using void\_t = typename detail::make\_void< Ts... >::type

Use the custom implementation, since the std::void\_t used in is\_matrix\_type\_builder seems to trigger a compiler bug in GCC 7.5.

# 45.19.1 Detailed Description

The namespace for functionalities after C++14 standard.

# **Chapter 46**

# **Class Documentation**

# 46.1 gko::AbsoluteComputable Class Reference

The AbsoluteComputable is an interface that allows to get the component wise absolute of a LinOp.

```
#include <ginkgo/core/base/lin_op.hpp>
```

#### **Public Member Functions**

- virtual std::unique\_ptr< LinOp > compute\_absolute\_linop () const =0
   Gets the absolute LinOp.
- virtual void compute\_absolute\_inplace ()=0

  Compute absolute inplace on each element.

# 46.1.1 Detailed Description

The AbsoluteComputable is an interface that allows to get the component wise absolute of a LinOp.

Use EnableAbsoluteComputation<AbsoluteLinOp> to implement this interface.

#### 46.1.2 Member Function Documentation

# 46.1.2.1 compute\_absolute\_linop()

```
virtual std::unique_ptr<LinOp> gko::AbsoluteComputable::compute_absolute_linop ( ) const
[pure virtual]
```

Gets the absolute LinOp.

#### Returns

a pointer to the new absolute LinOp

Implemented in gko::EnableAbsoluteComputation < AbsoluteLinOp >, gko::EnableAbsoluteComputation < remove\_complex < Hybrid gko::EnableAbsoluteComputation < remove\_complex < Sellp < ValueType, IndexType > > , gko::EnableAbsoluteComputation < regko::EnableAbsoluteComputation < remove\_complex < Coo < ValueType, IndexType > > , gko::EnableAbsoluteComputation < remove\_complex < Vector < ValueType > > , gko::EnableAbsoluteComputation < remove\_complex < Vector < ValueType > > , gko::EnableAbsoluteComputation < remove\_complex < Vector < ValueType, IndexType > > , and gko::EnableAbsoluteComputation < remove\_complex < Csr < ValueType, IndexType > > , and gko::EnableAbsoluteComputation < remove\_complex < Csr < ValueType, IndexType > > , and gko::EnableAbsoluteComputation < remove\_complex < Csr < ValueType, IndexType > > , and gko::EnableAbsoluteComputation < remove\_complex < Csr < ValueType, IndexType > > , and gko::EnableAbsoluteComputation < remove\_complex < Csr < ValueType, IndexType > > , and gko::EnableAbsoluteComputation < remove\_complex < Csr < ValueType, IndexType > > , and gko::EnableAbsoluteComputation < remove\_complex < Csr < ValueType, IndexType > > , and gko::EnableAbsoluteComputation < remove\_complex < Csr < ValueType, IndexType > > , and gko::EnableAbsoluteComputation < remove\_complex < Csr < ValueType, IndexType > > , and gko::EnableAbsoluteComputation < remove\_complex < Csr < ValueType, IndexType > > , and gko::EnableAbsoluteComputation < remove\_complex < Csr < ValueType, IndexType > > , and gko::EnableAbsoluteComputation < remove\_complex < Csr < ValueType, IndexType > > , and gko::EnableAbsoluteComputation < remove\_complex < Csr < ValueType, IndexType > > , and gko::EnableAbsoluteComputation < remove\_complex < Csr < ValueType > > , and gko::EnableAbsoluteComputation < remove\_complex < Csr < ValueType > > , and gko::EnableAbsoluteComputation < remove\_complex < Csr < ValueType > > , and gko::EnableAbsoluteComputation < remove\_complex < Csr < ValueType > > , and gko::EnableAbsoluteComputation < remove\_comple

The documentation for this class was generated from the following file:

• ginkgo/core/base/lin\_op.hpp

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# 46.2 gko::stop::AbsoluteResidualNorm< ValueType > Class Template Reference

The AbsoluteResidualNorm class is a stopping criterion which stops the iteration process when the residual norm is below a certain threshold, i.e.

```
#include <ginkgo/core/stop/residual_norm.hpp>
```

# 46.2.1 Detailed Description

```
template < typename ValueType = default_precision > class gko::stop::AbsoluteResidualNorm < ValueType >
```

The AbsoluteResidualNorm class is a stopping criterion which stops the iteration process when the residual norm is below a certain threshold, i.e.

when norm(residual) < threshold. For better performance, the checks are run thanks to kernels on the executor where the algorithm is executed.

Note

To use this stopping criterion there are some dependencies. The constructor depends on b in order to get the number of right-hand sides. If this is not correctly provided, an exception ::gko::NotSupported() is thrown.

The documentation for this class was generated from the following file:

ginkgo/core/stop/residual\_norm.hpp

# 46.3 gko::AbstractFactory< AbstractProductType, ComponentsType > Class Template Reference

The AbstractFactory is a generic interface template that enables easy implementation of the abstract factory design pattern.

```
#include <ginkgo/core/base/abstract_factory.hpp>
```

# **Public Member Functions**

```
    template<typename... Args>
    std::unique_ptr< abstract_product_type > generate (Args &&... args) const
        Creates a new product from the given components.
```

# 46.3.1 Detailed Description

```
template < typename\ AbstractProductType,\ typename\ ComponentsType > \\ class\ gko:: AbstractFactory < AbstractProductType,\ ComponentsType > \\
```

The AbstractFactory is a generic interface template that enables easy implementation of the abstract factory design pattern.

The interface provides the AbstractFactory::generate() method that can produce products of type Abstract ProductType using an object of ComponentsType (which can be constructed on the fly from parameters to its constructors). The generate() method is not declared as virtual, as this allows subclasses to hide the method with a variant that preserves the compile-time type of the objects. Instead, implementers should override the generate impl() method, which is declared virtual.

Implementers of concrete factories should consider using the EnableDefaultFactory mixin to obtain default implementations of utility methods of PolymorphicObject and AbstractFactory.

#### **Template Parameters**

AbstractProductType	the type of products the factory produces
ComponentsType	the type of components the factory needs to produce the product

## 46.3.2 Member Function Documentation

#### 46.3.2.1 generate()

Creates a new product from the given components.

The method will create an ComponentsType object from the arguments of this method, and pass it to the generate ← \_impl() function which will create a new AbstractProductType.

#### **Template Parameters**

# **Parameters**

```
args arguments passed to the constructor of ComponentsType
```

## Returns

#### an instance of AbstractProductType

The documentation for this class was generated from the following file:

ginkgo/core/base/abstract\_factory.hpp

# 46.4 gko::AllocationError Class Reference

AllocationError is thrown if a memory allocation fails.

```
#include <ginkgo/core/base/exception.hpp>
```

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## **Public Member Functions**

AllocationError (const std::string &file, int line, const std::string &device, size\_type bytes)
 Initializes an allocation error.

# 46.4.1 Detailed Description

AllocationError is thrown if a memory allocation fails.

#### 46.4.2 Constructor & Destructor Documentation

#### 46.4.2.1 AllocationError()

Initializes an allocation error.

#### **Parameters**

file	The name of the offending source file
line	The source code line number where the error occurred
device	The device on which the error occurred
bytes	The size of the memory block whose allocation failed.

```
547 : Error(file, line,
548 device + ": failed to allocate memory block of " +
549 std::to_string(bytes) + "B")
550 {}
```

The documentation for this class was generated from the following file:

• ginkgo/core/base/exception.hpp

# 46.5 gko::Allocator Class Reference

Provides generic allocation and deallocation functionality to be used by an Executor.

```
#include <ginkgo/core/base/memory.hpp>
```

# 46.5.1 Detailed Description

Provides generic allocation and deallocation functionality to be used by an Executor.

The documentation for this class was generated from the following file:

• ginkgo/core/base/memory.hpp

# 46.6 gko::experimental::reorder::Amd< IndexType > Class Template Reference

Computes a Approximate Minimum Degree (AMD) reordering of an input matrix.

```
#include <ginkgo/core/reorder/amd.hpp>
```

#### **Public Member Functions**

- const parameters\_type & get\_parameters ()
   Returns the parameters used to construct the factory.
- std::unique\_ptr< permutation\_type > generate (std::shared\_ptr< const LinOp > system\_matrix) const

#### Static Public Member Functions

static parameters\_type build ()
 Creates a new parameter\_type to set up the factory.

# 46.6.1 Detailed Description

```
template < typename IndexType = int32 > class gko::experimental::reorder::Amd < IndexType >
```

Computes a Approximate Minimum Degree (AMD) reordering of an input matrix.

**Template Parameters** 

IndexType the type used to store sparsity pattern indices of the system matrix

# 46.6.2 Member Function Documentation

# 46.6.2.1 generate()

# Note

This function overrides the default LinOpFactory::generate to return a Permutation instead of a generic LinOp, which would need to be cast to Permutation again to access its indices. It is only necessary because smart pointers aren't covariant.

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#### 46.6.2.2 get\_parameters()

```
template<typename IndexType = int32>
const parameters_type& gko::experimental::reorder::Amd< IndexType >::get_parameters ( ) [inline]
```

Returns the parameters used to construct the factory.

#### Returns

the parameters used to construct the factory.

```
67 { return parameters_; }
```

The documentation for this class was generated from the following file:

• ginkgo/core/reorder/amd.hpp

# 46.7 gko::amd\_device Class Reference

amd\_device handles the number of executor on Amd devices and have the corresponding recursive\_mutex.

```
#include <ginkgo/core/base/device.hpp>
```

## 46.7.1 Detailed Description

amd\_device handles the number of executor on Amd devices and have the corresponding recursive\_mutex.

The documentation for this class was generated from the following file:

• ginkgo/core/base/device.hpp

# 46.8 gko::solver::ApplyWithInitialGuess Class Reference

ApplyWithInitialGuess provides a way to give the input guess for apply function.

```
#include <ginkgo/core/solver/solver_base.hpp>
```

# 46.8.1 Detailed Description

ApplyWithInitialGuess provides a way to give the input guess for apply function.

All functionalities have the protected access specifier. It should only be used internally.

The documentation for this class was generated from the following file:

• ginkgo/core/solver/solver\_base.hpp

# 46.9 gko::are\_all\_integral < Args > Struct Template Reference

Evaluates if all template arguments Args fulfill std::is\_integral.

#include <ginkgo/core/base/types.hpp>

# 46.9.1 Detailed Description

```
template<typename... Args>
struct gko::are_all_integral< Args>
```

Evaluates if all template arguments Args fulfill std::is\_integral.

If that is the case, this class inherits from std::true\_type, otherwise, it inherits from std::false\_type. If no values are passed in, std::true\_type is inherited from.

#### **Template Parameters**

```
Args... Arguments to test for std::is_integral
```

The documentation for this struct was generated from the following file:

• ginkgo/core/base/types.hpp

# 46.10 gko::array< ValueType > Class Template Reference

An array is a container which encapsulates fixed-sized arrays, stored on the Executor tied to the array.

```
#include <ginkgo/core/base/array.hpp>
```

# **Public Types**

• using value\_type = ValueType

The type of elements stored in the array.

using default\_deleter = executor\_deleter< value\_type[]>

The default deleter type used by array.

• using view\_deleter = null\_deleter < value\_type[]>

The deleter type used for views.

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#### **Public Member Functions**

array () noexcept

Creates an empty array not tied to any executor.

array (std::shared ptr< const Executor > exec) noexcept

Creates an empty array tied to the specified Executor.

array (std::shared\_ptr< const Executor > exec, size\_type size)

Creates an array on the specified Executor.

template<typename DeleterType >

array (std::shared ptr< const Executor > exec, size type size, value type \*data, DeleterType deleter)

Creates an array from existing memory.

array (std::shared\_ptr< const Executor > exec, size\_type size, value\_type \*data)

Creates an array from existing memory.

• template<typename RandomAccessIterator >

array (std::shared\_ptr< const Executor > exec, RandomAccessIterator begin, RandomAccessIterator end)

Creates an array on the specified Executor and initializes it with values.

template<typename T >

```
array (std::shared ptr< const Executor > exec, std::initializer list< T > init list)
```

Creates an array on the specified Executor and initializes it with values.

array (std::shared\_ptr< const Executor > exec, const array &other)

Creates a copy of another array on a different executor.

array (const array &other)

Creates a copy of another array.

array (std::shared\_ptr< const Executor > exec, array &&other)

Moves another array to a different executor.

• array (array &&other)

Moves another array.

array< ValueType > as\_view ()

Returns a non-owning view of the memory owned by this array.

detail::const array view< ValueType > as const view () const

Returns a non-owning constant view of the memory owned by this array.

array & operator= (const array & other)

Copies data from another array or view.

array & operator= (array &&other)

Moves data from another array or view.

 $\bullet \ \ {\it template}{<} {\it typename OtherValueType}>$ 

std::enable\_if\_t<!std::is\_same< ValueType, OtherValueType >::value, array > & operator= (const array< OtherValueType > &other)

Copies and converts data from another array with another data type.

array & operator= (const detail::const\_array\_view < ValueType > &other)

Copies data from a const\_array\_view.

• void clear () noexcept

Deallocates all data used by the array.

void resize\_and\_reset (size\_type size)

Resizes the array so it is able to hold the specified number of elements.

• void fill (const value\_type value)

Fill the array with the given value.

size\_type get\_size () const noexcept

Returns the number of elements in the array.

· size type get num elems () const noexcept

Returns the number of elements in the array.

value\_type \* get\_data () noexcept

Returns a pointer to the block of memory used to store the elements of the array.

const value\_type \* get\_const\_data () const noexcept

Returns a constant pointer to the block of memory used to store the elements of the array.

std::shared\_ptr< const Executor > get\_executor () const noexcept

Returns the Executor associated with the array.

void set\_executor (std::shared\_ptr< const Executor > exec)

Changes the Executor of the array, moving the allocated data to the new Executor.

· bool is owning ()

Tells whether this array owns its data or not.

#### Static Public Member Functions

• static array view (std::shared\_ptr< const Executor > exec, size\_type size, value\_type \*data)

Creates an array from existing memory.

static detail::const\_array\_view
 ValueType > const\_view (std::shared\_ptr< const Executor > exec, size\_type size, const value\_type \*data)

Creates a constant (immutable) array from existing memory.

# 46.10.1 Detailed Description

```
template<typename ValueType> class gko::array< ValueType>
```

An array is a container which encapsulates fixed-sized arrays, stored on the Executor tied to the array.

The array stores and transfers its data as **raw** memory, which means that the constructors of its elements are not called when constructing, copying or moving the array. Thus, the array class is most suitable for storing POD types.

**Template Parameters** 

```
ValueType the type of elements stored in the array
```

# 46.10.2 Constructor & Destructor Documentation

# 46.10.2.1 array() [1/11]

```
template<typename ValueType>
gko::array< ValueType >::array ( ) [inline], [noexcept]
```

Creates an empty array not tied to any executor.

An array without an assigned executor can only be empty. Attempts to change its size (e.g. via the resize\_and\_\circ} reset method) will result in an exception. If such an array is used as the right hand side of an assignment or move assignment expression, the data of the target array will be cleared, but its executor will not be modified.

The executor can later be set by using the set\_executor method. If an array with no assigned executor is assigned or moved to, it will inherit the executor of the source array.

# 46.10.2.2 array() [2/11]

Creates an empty array tied to the specified Executor.

#### **Parameters**

```
exec the Executor where the array data is allocated
```

# 46.10.2.3 array() [3/11]

Creates an array on the specified Executor.

#### **Parameters**

exec	the Executor where the array data will be allocated
size	the amount of memory (expressed as the number of value_type elements) allocated on the Executor

# 46.10.2.4 array() [4/11]

Creates an array from existing memory.

The memory will be managed by the array, and deallocated using the specified deleter (e.g. use std::default\_delete for data allocated with new).

# **Template Parameters**

DeleterType	type of the deleter
-------------	---------------------

#### **Parameters**

exec	executor where data is located
size	number of elements in data
data	chunk of memory used to create the array
deleter	the deleter used to free the memory

#### See also

```
array::view() to create an array that does not deallocate memory
array(std::shared_ptr<cont Executor>, size_type, value_type*) to deallocate the memory using Executor::free()
method
```

# 46.10.2.5 array() [5/11]

Creates an array from existing memory.

The memory will be managed by the array, and deallocated using the Executor::free method.

# **Parameters**

exec	executor where data is located	
size	number of elements in data	
data	chunk of memory used to create the array	

# **46.10.2.6** array() [6/11]

Creates an array on the specified Executor and initializes it with values.

# **Template Parameters**

RandomAccessIterator	type of the iterators

#### **Parameters**

exec	the Executor where the array data will be allocate	
begin	start of range of values	
end	end of range of values	

# 46.10.2.7 array() [7/11]

Creates an array on the specified Executor and initializes it with values.

# **Template Parameters**

T | type of values used to initialize the array (T has to be implicitly convertible to value\_type)

# **Parameters**

exec	the Executor where the array data will be allocated
init_list	list of values used to initialize the array

# 46.10.2.8 array() [8/11]

Creates a copy of another array on a different executor.

This does not invoke the constructors of the elements, instead they are copied as POD types.

# **Parameters**

exec	the executor where the new array will be created
other	the array to copy from

### 46.10.2.9 array() [9/11]

Creates a copy of another array.

This does not invoke the constructors of the elements, instead they are copied as POD types.

#### **Parameters**

other	the array to copy from
-------	------------------------

# 46.10.2.10 array() [10/11]

Moves another array to a different executor.

This does not invoke the constructors of the elements, instead they are copied as POD types.

#### **Parameters**

exec	the executor where the new array will be moved
other	the array to move

# 46.10.2.11 array() [11/11]

Moves another array.

This does not invoke the constructors of the elements, instead they are copied as POD types.

#### **Parameters**

#### 46.10.3 Member Function Documentation

# 46.10.3.1 as\_const\_view()

```
template<typename ValueType>
detail::const_array_view<ValueType> gko::array< ValueType >::as_const_view ( ) const [inline]
```

Returns a non-owning constant view of the memory owned by this array.

It can only be used until this array gets deleted, cleared or resized.

#### 46.10.3.2 as\_view()

```
template<typename ValueType>
array<ValueType> gko::array< ValueType >::as_view ( ) [inline]
```

Returns a non-owning view of the memory owned by this array.

It can only be used until this array gets deleted, cleared or resized.

#### 46.10.3.3 clear()

```
template<typename ValueType>
void gko::array< ValueType >::clear ( ) [inline], [noexcept]
```

Deallocates all data used by the array.

The array is left in a valid, but empty state, so the same array can be used to allocate new memory. Calls to array::get\_data() will return a nullptr.

Referenced by gko::index\_set< IndexType >::clear(), and gko::array< index\_type >::operator=().

#### 46.10.3.4 const\_view()

Creates a constant (immutable) array from existing memory.

The array does not take ownership of the memory, and will not deallocate it once it goes out of scope. This array type cannot use the function resize\_and\_reset since it does not own the data it should resize.

#### **Parameters**

exec	executor where data is located	
size	number of elements in data	
data	chunk of memory used to create the array	

#### Returns

an array constructed from data

Referenced by gko::array< index\_type >::as\_const\_view().

#### 46.10.3.5 fill()

Fill the array with the given value.

#### **Parameters**

value the value to be filled	
------------------------------	--

## 46.10.3.6 get\_const\_data()

```
template<typename ValueType>
const value_type* gko::array< ValueType >::get_const_data ( ) const [inline], [noexcept]
```

Returns a constant pointer to the block of memory used to store the elements of the array.

#### Returns

a constant pointer to the block of memory used to store the elements of the array

IndexType >::get\_const\_col\_idxs\_for\_item(), gko::batch::preconditioner::Jacobi< ValueType, IndexType >::get\_← const\_map\_block\_to\_row(), gko::matrix::ScaledPermutation< ValueType, IndexType >::get\_const\_permutation(), gko::matrix::Permutation< IndexType >::get\_const\_permutation(), gko::matrix::RowGatherer< IndexType >← ::get\_const\_row\_idxs(), gko::matrix::Coo< ValueType, IndexType >::get\_const\_row\_idxs(), gko::device\_matrix\_ data< ValueType, IndexType >::get\_const\_row\_idxs(), gko::batch::matrix::Csr< ValueType, IndexType >::get\_← const row ptrs(), gko::matrix::SparsityCsr< ValueType, IndexType >::get const row ptrs(), gko::matrix::Fbcsr< ValueType, IndexType >::get const row ptrs(), gko::matrix::Csr< ValueType, IndexType >::get const row ← ptrs(), gko::matrix::ScaledPermutation < ValueType, IndexType >::get const scaling factors(), gko::matrix::Sellp < ValueType, IndexType >::get const slice lengths(), gko::matrix::Sellp< ValueType, IndexType >::get const ← slice sets(), gko::matrix::Csr< ValueType, IndexType >::get const srow(), gko::matrix::SparsityCsr< ValueType, IndexType >::get\_const\_value(), gko::batch::matrix::Csr< ValueType, IndexType >::get\_const\_values(), gko⇔ ::batch::matrix::Ell< ValueType, IndexType >::get\_const\_values(), gko::matrix::Diagonal< ValueType >::get← \_const\_values(), gko::batch::matrix::Dense< ValueType >::get\_const\_values(), gko::matrix::Sellp< ValueType, IndexType >::get\_const\_values(), gko::matrix::Coo< ValueType, IndexType >::get\_const\_values(), gko::matrix← ::Ell< ValueType, IndexType >::get\_const\_values(), gko::batch::MultiVector< ValueType >::get\_const\_values(), gko::device\_matrix\_data< ValueType, IndexType >::get\_const\_values(), gko::matrix::Fbcsr< ValueType, Index Type >::get const values(), gko::matrix::Dense < value type >::get const values(), gko::matrix::Csr < ValueType, IndexType >::get\_const\_values(), gko::batch::MultiVector< ValueType >::get\_const\_values\_for\_item(), gko⇔ ::batch::matrix::Csr< ValueType, IndexType >::get\_const\_values\_for\_item(), gko::batch::matrix::Dense< Value← Type >::get\_const\_values\_for\_item(), gko::batch::matrix::Ell< ValueType, IndexType >::get\_const\_values\_← for item(), gko::experimental::distributed::Partition< LocalIndexType, GlobalIndexType >::get part ids(), gko↔ ::experimental::distributed::Partition< LocalIndexType, GlobalIndexType >::get part sizes(), gko::experimental ::distributed::Partition< LocalIndexType, GlobalIndexType >::get\_range\_bounds(), gko::experimental::distributed ← ::Partition< LocalIndexType, GlobalIndexType >::get\_range\_starting\_indices(), gko::index\_set< IndexType > \leftrightarrow ::get\_subsets\_begin(), gko::index\_set< IndexType >::get\_subsets\_end(), gko::index\_set< IndexType >::get\_← superset\_indices(), gko::matrix::Csr< ValueType, IndexType >::classical::process(), gko::matrix::Csr< ValueType, IndexType >::load\_balance::process(), gko::matrix::Ell < ValueType, IndexType >::val\_at(), and gko::matrix::Sellp < ValueType, IndexType >::val at().

# 46.10.3.7 get\_data()

```
template<typename ValueType>
value_type* gko::array< ValueType >::get_data ( ) [inline], [noexcept]
```

Returns a pointer to the block of memory used to store the elements of the array.

# Returns

a pointer to the block of memory used to store the elements of the array

Referenced by gko::array< index\_type >::as\_view(), gko::batch::matrix::Dense< ValueType >::at(), gko::batch::

MultiVector< ValueType >::at(), gko::matrix::Dense< value\_type >::at(), gko::matrix::Hybrid< ValueType, Index

Type >::imbalance\_limit::compute\_ell\_num\_stored\_elements\_per\_row(), gko::multigrid::Pgm< ValueType, Index

Type >::get\_agg(), gko::batch::matrix::Csr< ValueType, IndexType >::get\_col\_idxs(), gko::batch::matrix::Ell<

ValueType, IndexType >::get\_col\_idxs(), gko::matrix::SparsityCsr< ValueType, IndexType >::get\_col\_idxs(), gko::matrix::Sellp< ValueType, IndexType >::get\_col\_idxs(), gko::matrix::Coo< ValueType, IndexType >::get\_col\_idxs(), gko::matrix::Ell< ValueType, IndexType >::get\_col\_idxs(), gko::matrix::Csr< ValueType, IndexType >::get\_col\_idxs(), gko::matrix::Csr< ValueType, IndexType >::get\_col\_idxs(), gko::matrix::Csr< ValueType, IndexType >::get\_col\_idxs(), gko::matrix::Coo< ValueType, IndexType >::get\_permutation</ri>
| Sko::matrix::Coo< ValueType, IndexType >::get\_row\_idxs(), gko::matrix::Coo< ValueType, IndexType >::get\_row\_idxs(), gko::batch::matrix::Csr< ValueType, IndexType >::get\_row\_idxs(), gko::batch::matrix::Csr< ValueType, IndexType >::get\_row\_ptrs(), gko::matrix::SparsityCsr< ValueType, IndexType >::get\_row\_ptrs(), gko::matrix::Csr< ValueType, IndexType >::get\_row\_ptrs(), gko::matrix::Csr< ValueType, IndexType >::get\_row\_ptrs(), gko::matrix::Csr< ValueType, IndexType, IndexType >::get\_row\_ptrs(), gko::matrix::Csr< ValueType, IndexType >::get\_row\_ptrs(), gko::matrix::Csr< Value

IndexType >::get\_row\_ptrs(), gko::matrix::ScaledPermutation< ValueType, IndexType >::get\_scaling\_factors(), gko::matrix::Sellp< ValueType, IndexType >::get\_slice\_lengths(), gko::matrix::Sellp< ValueType, IndexType >::get\_slice\_sets(), gko::matrix::Csr< ValueType, IndexType >::get\_srow(), gko::matrix::SparsityCsr< ValueType, IndexType >::get\_values(), gko::batch::matrix::Csr< ValueType, IndexType >::get\_values(), gko::batch::matrix::Ell< ValueType, IndexType >::get\_values(), gko::batch::matrix::Ell< ValueType, IndexType >::get\_values(), gko::matrix::Sellp< ValueType, IndexType >::get\_values(), gko::batch::matrix::Coo< ValueType, IndexType >::get\_values(), gko::batch::matrix::Ell< ValueType, IndexType >::get\_values(), gko::batch::matrix::Ell< ValueType, IndexType >::get\_values(), gko::matrix::Dense< ValueType, IndexType >::get\_values(), gko::matrix::Csr< ValueType, IndexType >::get\_values(), gko::batch::MultiVector< ValueType, IndexType >::get\_values(), gko::batch::MultiVector< ValueType, IndexType >::get\_values(), gko::batch::matrix::Csr< ValueType, IndexType >::get\_values\_for\_item(), gko::batch::matrix::Dense< ValueType, IndexType >::get\_values\_for\_item(), gko::batch::matrix::Ell< ValueType, IndexType >::get\_values\_for\_item(), gko::matrix::Ell< ValueType, IndexType >::get\_values\_for\_item(), gko::matrix::Ell< ValueType, IndexType >::load\_balance::process(), gko::matrix::Ell< ValueType, IndexType >::val\_at().

# 46.10.3.8 get\_executor()

```
template<typename ValueType>
std::shared_ptr<const Executor> gko::array< ValueType >::get_executor ( ) const [inline],
[noexcept]
```

Returns the Executor associated with the array.

#### Returns

the Executor associated with the array

Referenced by gko::array< index\_type >::as\_const\_view(), gko::array< index\_type >::as\_view(), gko::matrix::

Hybrid< ValueType, IndexType >::strategy\_type::compute\_hybrid\_config(), gko::device\_matrix\_data< ValueType, IndexType >::get\_executor(), gko::matrix::Csr< ValueType, IndexType >::classical::process(), and gko::matrix::

Csr< ValueType, IndexType >::load\_balance::process().

## 46.10.3.9 get\_num\_elems()

```
template<typename ValueType>
size_type gko::array< ValueType >::get_num_elems ( ) const [inline], [noexcept]
```

Returns the number of elements in the array.

#### Returns

the number of elements in the array

#### 46.10.3.10 get\_size()

```
template<typename ValueType>
size_type gko::array< ValueType >::get_size ( ) const [inline], [noexcept]
```

Returns the number of elements in the array.

#### Returns

the number of elements in the array

Referenced by gko::array< index\_type >::as\_const\_view(), gko::array< index\_type >::as\_view(), gko::matrix::← Hybrid< ValueType, IndexType >::imbalance limit::compute ell num stored elements per row(), gko::matrix← ::Hybrid< ValueType, IndexType >::imbalance bounded limit::compute ell num stored elements per row(), gko::matrix::Hybrid< ValueType, IndexType >::strategy\_type::compute\_hybrid\_config(), gko::batch::matrix::↔ Csr< ValueType, IndexType >::get\_const\_values\_for\_item(), gko::matrix::SparsityCsr< ValueType, IndexType >::get num nonzeros(), gko::experimental::distributed::Partition< LocalIndexType, GlobalIndexType >::get ← num ranges(), gko::matrix::Csr< ValueType, IndexType >::get num srow elements(), gko::matrix::Fbcsr< ValueType, IndexType >::get\_num\_stored\_blocks(), gko::batch::preconditioner::Jacobi< ValueType, IndexType >::get num stored elements(), gko::batch::matrix::Ell< ValueType, IndexType >::get num stored elements(), gko::batch::matrix::Csr< ValueType, IndexType >::get\_num\_stored\_elements(), gko::device\_matrix\_data< ValueType, IndexType >::get\_num\_stored\_elements(), gko::matrix::Ell< ValueType, IndexType >::get\_num\_← stored\_elements(), gko::matrix::Coo< ValueType, IndexType >::get\_num\_stored\_elements(), gko::batch::Multi← Vector< ValueType >::get\_num\_stored\_elements(), gko::batch::matrix::Dense< ValueType >::get\_num\_stored ← elements(), gko::matrix::Sellp< ValueType, IndexType >::get num stored elements(), gko::preconditioner::⇔ Jacobi< ValueType, IndexType >::get\_num\_stored\_elements(), gko::matrix::Fbcsr< ValueType, IndexType >↔ ::get\_num\_stored\_elements(), gko::matrix::Dense< value\_type >::get\_num\_stored\_elements(), gko::matrix::← Csr< ValueType, IndexType >::get\_num\_stored\_elements(), gko::index\_set< IndexType >::get\_num\_subsets(), gko::matrix::Sellp< ValueType, IndexType >::get total cols(), gko::batch::matrix::Csr< ValueType, IndexType >::get\_values\_for\_item(), gko::index\_set< IndexType >::index\_set(), gko::array< index\_type >::operator=(), gko::matrix::Csr< ValueType, IndexType >::classical::process(), and gko::matrix::Csr< ValueType, IndexType >::load balance::process().

# 46.10.3.11 is\_owning()

```
template<typename ValueType>
bool gko::array< ValueType >::is_owning ( ) [inline]
```

Tells whether this array owns its data or not.

Views do not own their data and this has multiple implications. They cannot be resized since the data is not owned by the array which stores a view. It is also unclear whether custom deleter types are owning types as they could be a user-created view-type, therefore only proper array which use the default\_deleter are considered owning types.

#### Returns

whether this array can be resized or not.

Referenced by gko::array< index type >::operator=().

#### 46.10.3.12 operator=() [1/4]

Moves data from another array or view.

Only the pointer and deleter type change, a copy only happens when targeting another executor's data. This means that in the following situation:

```
gko::array<int> a; // an existing array or view
gko::array<int> b; // an existing array or view
b = std::move(a);
```

Depending on whether a and b are array or view, this happens:

- a and b are views, b becomes the only valid view of a;
- a and  ${\tt b}$  are arrays,  ${\tt b}$  becomes the only valid array of a;
- a is a view and b is an array, b frees its data and becomes the only valid view of a ();
- a is an array and b is a view, b becomes the only valid array of a.

In all the previous cases, a becomes empty (e.g., a nullptr).

This does not invoke the constructors of the elements, instead they are copied as POD types.

The executor of this is preserved. In case this does not have an assigned executor, it will inherit the executor of other.

#### **Parameters**

other	the array to move data from
-------	-----------------------------

# Returns

this

## 46.10.3.13 operator=() [2/4]

Copies data from another array or view.

In the case of an array target, the array is resized to match the source's size. In the case of a view target, if the dimensions are not compatible a gko::OutOfBoundsError is thrown.

This does not invoke the constructors of the elements, instead they are copied as POD types.

The executor of this is preserved. In case this does not have an assigned executor, it will inherit the executor of other.

#### **Parameters**

other the array to copy from
------------------------------

#### Returns

this

## 46.10.3.14 operator=() [3/4]

Copies and converts data from another array with another data type.

In the case of an array target, the array is resized to match the source's size. In the case of a view target, if the dimensions are not compatible a gko::OutOfBoundsError is thrown.

This does not invoke the constructors of the elements, instead they are copied as POD types.

The executor of this is preserved. In case this does not have an assigned executor, it will inherit the executor of other.

# **Parameters**

other	the array to copy from
-------	------------------------

# **Template Parameters**

|--|

# Returns

this

# 46.10.3.15 operator=() [4/4]

Copies data from a const\_array\_view.

In the case of an array target, the array is resized to match the source's size. In the case of a view target, if the dimensions are not compatible a gko::OutOfBoundsError is thrown.

This does not invoke the constructors of the elements, instead they are copied as POD types.

The executor of this is preserved. In case this does not have an assigned executor, it will inherit the executor of other.

#### **Parameters**

```
other the const_array_view to copy from
```

# Returns

this

# 46.10.3.16 resize and reset()

Resizes the array so it is able to hold the specified number of elements.

For a view and other non-owning array types, this throws an exception since these types cannot be resized.

All data stored in the array will be lost.

If the array is not assigned an executor, an exception will be thrown.

#### **Parameters**

size the amount of memory (expressed as the number of value\_type elements) allocated on the Executor

Referenced by gko::array< index\_type >::operator=().

# 46.10.3.17 set\_executor()

Changes the Executor of the array, moving the allocated data to the new Executor.

# **Parameters**

exec the Executor where the data will be moved to

## 46.10.3.18 view()

Creates an array from existing memory.

The array does not take ownership of the memory, and will not deallocate it once it goes out of scope. This array type cannot use the function resize\_and\_reset since it does not own the data it should resize.

#### **Parameters**

exec	executor where data is located
size	number of elements in data
data	chunk of memory used to create the array

#### Returns

an array constructed from data

Referenced by gko::array< index\_type >::as\_view().

The documentation for this class was generated from the following file:

• ginkgo/core/base/array.hpp

# 46.11 gko::device\_matrix\_data< ValueType, IndexType >::arrays Struct Reference

Stores the internal arrays of a device\_matrix\_data object.

```
#include <ginkgo/core/base/device_matrix_data.hpp>
```

# 46.11.1 Detailed Description

```
template<typename ValueType, typename IndexType>
struct gko::device_matrix_data< ValueType, IndexType >::arrays
```

Stores the internal arrays of a device\_matrix\_data object.

The documentation for this struct was generated from the following file:

• ginkgo/core/base/device\_matrix\_data.hpp

# 46.12 gko::matrix::Hybrid< ValueType, IndexType >::automatic Class Reference

automatic is a strategy\_type which decides the number of stored elements per row of the ell part automatically.

```
#include <ginkgo/core/matrix/hybrid.hpp>
```

# **Public Member Functions**

• automatic ()

Creates an automatic strategy.

size\_type compute\_ell\_num\_stored\_elements\_per\_row (array < size\_type > \*row\_nnz) const override
 Computes the number of stored elements per row of the ell part.

# 46.12.1 Detailed Description

```
template<typename ValueType = default_precision, typename IndexType = int32> class gko::matrix::Hybrid< ValueType, IndexType >::automatic
```

automatic is a strategy\_type which decides the number of stored elements per row of the ell part automatically.

#### 46.12.2 Member Function Documentation

# 46.12.2.1 compute\_ell\_num\_stored\_elements\_per\_row()

Computes the number of stored elements per row of the ell part.

#### **Parameters**

	row_nnz	the number of nonzeros of each row	
--	---------	------------------------------------	--

# Returns

the number of stored elements per row of the ell part

Implements gko::matrix::Hybrid< ValueType, IndexType >::strategy type.

References gko::matrix::Hybrid< ValueType, IndexType >::imbalance\_bounded\_limit::compute\_ell\_num\_stored ← \_\_elements\_per\_row().

The documentation for this class was generated from the following file:

· ginkgo/core/matrix/hybrid.hpp

# 46.13 gko::BadDimension Class Reference

BadDimension is thrown if an operation is being applied to a LinOp with bad dimensions.

```
#include <ginkgo/core/base/exception.hpp>
```

# **Public Member Functions**

• BadDimension (const std::string &file, int line, const std::string &func, const std::string &op\_name, size\_type op\_num\_rows, size\_type op\_num\_cols, const std::string &clarification)

Initializes a bad dimension error.

# 46.13.1 Detailed Description

BadDimension is thrown if an operation is being applied to a LinOp with bad dimensions.

# 46.13.2 Constructor & Destructor Documentation

# 46.13.2.1 BadDimension()

Initializes a bad dimension error.

#### **Parameters**

file	The name of the offending source file
line	The source code line number where the error occurred
func	The function name where the error occurred
op_name	The name of the operator
op_num_rows	The row dimension of the operator
op_num_cols	The column dimension of the operator
clarification	An additional message further describing the error

The documentation for this class was generated from the following file:

· ginkgo/core/base/exception.hpp

# 46.14 gko::batch\_dim< Dimensionality, DimensionType > Struct Template Reference

A type representing the dimensions of a multidimensional batch object.

#include <ginkgo/core/base/batch\_dim.hpp>

#### **Public Member Functions**

• size\_type get\_num\_batch\_items () const

Get the number of batch items stored.

dim< dimensionality, dimension\_type > get\_common\_size () const

Get the common size of the batch items.

• batch dim ()

The default constructor.

Creates a batch\_dim object which stores a uniform size for all batch entries.

# **Friends**

bool operator== (const batch\_dim &x, const batch\_dim &y)

Checks if two batch\_dim objects are equal.

 bool operator!= (const batch\_dim< Dimensionality, DimensionType > &x, const batch\_dim< Dimensionality, DimensionType > &y)

Checks if two batch\_dim objects are different.

# 46.14.1 Detailed Description

template < size\_type Dimensionality = 2, typename DimensionType = size\_type > struct gko::batch\_dim < Dimensionality, DimensionType >

A type representing the dimensions of a multidimensional batch object.

# **Template Parameters**

Dimensionality	number of dimensions of the object
DimensionType	datatype used to represent each dimension

# 46.14.2 Constructor & Destructor Documentation

# 46.14.2.1 batch\_dim()

Creates a batch\_dim object which stores a uniform size for all batch entries.

#### **Parameters**

num_batch_items	the number of batch items to be stored
common_size	the common size of all the batch items stored

#### Note

Use this constructor when uniform batches need to be stored.

#### 46.14.3 Member Function Documentation

# 46.14.3.1 get\_common\_size()

```
template<size_type Dimensionality = 2, typename DimensionType = size_type>
dim<dimensionality, dimension_type> gko::batch_dim< Dimensionality, DimensionType >::get_←
common_size ( ) const [inline]
```

Get the common size of the batch items.

#### Returns

common\_size

Referenced by gko::batch::MultiVector< ValueType >::get common size(), and gko::transpose().

## 46.14.3.2 get\_num\_batch\_items()

```
template<size_type Dimensionality = 2, typename DimensionType = size_type>
size_type gko::batch_dim< Dimensionality, DimensionType >::get_num_batch_items ( ) const
[inline]
```

Get the number of batch items stored.

#### Returns

num\_batch\_items

Referenced by gko::batch::MultiVector< ValueType >::get\_num\_batch\_items(), and gko::transpose().

# 46.14.4 Friends And Related Function Documentation

# 46.14.4.1 operator"!=

Checks if two batch\_dim objects are different.

#### **Template Parameters**

Dimensionality	number of dimensions of the dim objects
DimensionType	datatype used to represent each dimension

#### **Parameters**

Х	first object
у	second object

#### Returns

```
!(x == y)
```

# 46.14.4.2 operator==

Checks if two batch\_dim objects are equal.

# **Parameters**

X	first object
У	second object

# Returns

true if and only if all dimensions of both objects are equal.

The documentation for this struct was generated from the following file:

• ginkgo/core/base/batch\_dim.hpp

# 46.15 gko::batch::log::BatchConvergence < ValueType > Class Template Reference

Logs the final residuals and iteration counts for a batch solver.

```
#include <ginkgo/core/log/batch_logger.hpp>
```

#### **Public Member Functions**

- const array< index\_type > & get\_num\_iterations () const noexcept
- const array< real\_type > & get\_residual\_norm () const noexcept

#### **Static Public Member Functions**

Creates a convergence logger.

# 46.15.1 Detailed Description

```
template<typename ValueType = default_precision> class gko::batch::log::BatchConvergence< ValueType >
```

Logs the final residuals and iteration counts for a batch solver.

The purpose of this logger is to give simple access to standard data generated by the solver once it has converged.

Note

The final logged residuals are the implicit residuals that have been computed within the solver process. Depending on the solver algorithm, this may be significantly different from the true residual (||b - Ax||).

#### 46.15.2 Member Function Documentation

#### 46.15.2.1 create()

Creates a convergence logger.

This dynamically allocates the memory, constructs the object and returns an std::unique\_ptr to this object. TODO: See if the objects can be pre-allocated beforehand instead of being copied in the  $on_<$  event

#### **Parameters**

exec	the executor
enabled_events	the events enabled for this logger. By default all events.

#### Returns

an std::unique ptr to the the constructed object

```
95 {
96     return std::unique_ptr<BatchConvergence>(
97     new BatchConvergence(enabled_events));
98 }
```

#### 46.15.2.2 get num iterations()

```
template<typename ValueType = default_precision>
const array<index_type>& gko::batch::log::BatchConvergence< ValueType >::get_num_iterations (
) const [inline], [noexcept]
```

#### Returns

The number of iterations for entire batch

# 46.15.2.3 get\_residual\_norm()

```
template<typename ValueType = default_precision>
const array<real_type>& gko::batch::log::BatchConvergence< ValueType >::get_residual_norm ( )
const [inline], [noexcept]
```

#### Returns

The residual norms for the entire batch.

The documentation for this class was generated from the following file:

ginkgo/core/log/batch\_logger.hpp

# 46.16 gko::batch::BatchLinOpFactory Class Reference

A BatchLinOpFactory represents a higher order mapping which transforms one batch linear operator into another.

```
#include <ginkgo/core/base/batch_lin_op.hpp>
```

#### **Additional Inherited Members**

# 46.16.1 Detailed Description

A BatchLinOpFactory represents a higher order mapping which transforms one batch linear operator into another.

In a similar fashion to LinOps, BatchLinOps are also "generated" from the BatchLinOpFactory. A function of this class is to provide a generate method, which internally cals the generate\_impl(), which the concrete BatchLinOps have to implement.

## 46.16.1.1 Example: using BatchCG in Ginkgo

The documentation for this class was generated from the following file:

ginkgo/core/base/batch\_lin\_op.hpp

# 46.17 gko::batch::solver::BatchSolver Class Reference

The BatchSolver is a base class for all batched solvers and provides the common getters and setter for these batched solver classes.

```
#include <ginkgo/core/solver/batch_solver_base.hpp>
```

# **Public Member Functions**

std::shared\_ptr< const BatchLinOp > get\_system\_matrix () const

Returns the system operator (matrix) of the linear system.

std::shared ptr< const BatchLinOp > get preconditioner () const

Returns the generated preconditioner.

• double get\_tolerance () const

Get the residual tolerance used by the solver.

void reset\_tolerance (double res\_tol)

Update the residual tolerance to be used by the solver.

• int get\_max\_iterations () const

Get the maximum number of iterations set on the solver.

void reset max iterations (int max iterations)

Set the maximum number of iterations for the solver to use, independent of the factory that created it.

::gko::batch::stop::tolerance\_type get\_tolerance\_type () const

Get the tolerance type.

void reset\_tolerance\_type (::gko::batch::stop::tolerance\_type tol\_type)

Set the type of tolerance check to use inside the solver.

# 46.17.1 Detailed Description

The BatchSolver is a base class for all batched solvers and provides the common getters and setter for these batched solver classes.

# 46.17.2 Member Function Documentation

# 46.17.2.1 get\_max\_iterations()

```
int gko::batch::solver::BatchSolver::get_max_iterations ( ) const [inline]
```

Get the maximum number of iterations set on the solver.

#### Returns

Maximum number of iterations.

```
77 { return this->max_iterations_; }
```

# 46.17.2.2 get\_preconditioner()

```
std::shared_ptr<const BatchLinOp> gko::batch::solver::BatchSolver::get_preconditioner ( )
const [inline]
```

Returns the generated preconditioner.

# Returns

the generated preconditioner.

# 46.17.2.3 get\_system\_matrix()

std::shared\_ptr<const BatchLinOp> gko::batch::solver::BatchSolver::get\_system\_matrix ( ) const
[inline]

Returns the system operator (matrix) of the linear system.

# Returns

the system operator (matrix)

# 46.17.2.4 get\_tolerance()

```
double gko::batch::solver::BatchSolver::get_tolerance ( ) const [inline]
```

Get the residual tolerance used by the solver.

#### Returns

The residual tolerance.

# 46.17.2.5 get\_tolerance\_type()

```
::gko::batch::stop::tolerance_type gko::batch::solver::BatchSolver::get_tolerance_type ( )
const [inline]
```

Get the tolerance type.

#### Returns

The tolerance type.

# 46.17.2.6 reset\_max\_iterations()

Set the maximum number of iterations for the solver to use, independent of the factory that created it.

### **Parameters**

	max iterations	The maximum number of iterations for the solver.	
--	----------------	--	--

# 46.17.2.7 reset\_tolerance()

Update the residual tolerance to be used by the solver.

#### **Parameters**

res_tol	The residual tolerance to be used for subsequent invocations of the solver.
---------	---

# 46.17.2.8 reset\_tolerance\_type()

Set the type of tolerance check to use inside the solver.

#### **Parameters**

The documentation for this class was generated from the following file:

ginkgo/core/solver/batch solver base.hpp

# 46.18 gko::solver::Bicg < ValueType > Class Template Reference

BICG or the Biconjugate gradient method is a Krylov subspace solver.

```
#include <ginkgo/core/solver/bicg.hpp>
```

#### **Public Member Functions**

- std::unique\_ptr< LinOp > transpose () const override
  - Returns a LinOp representing the transpose of the Transposable object.
- std::unique\_ptr< LinOp > conj\_transpose () const override
  - Returns a LinOp representing the conjugate transpose of the Transposable object.
- bool apply\_uses\_initial\_guess () const override

Return true as iterative solvers use the data in x as an initial guess.

# **Static Public Member Functions**

• static parameters\_type parse (const config::pnode &config, const config::registry &context, const config::type descriptor &td for child=config::make type descriptor < ValueType >())

Create the parameters from the property\_tree.

# 46.18.1 Detailed Description

```
template<typename ValueType = default_precision> class gko::solver::Bicg< ValueType >
```

BICG or the Biconjugate gradient method is a Krylov subspace solver.

Being a generic solver, it is capable of solving general matrices, including non-s.p.d matrices. Though, the memory and the computational requirement of the BiCG solver are higher than of its s.p.d solver counterpart, it has the capability to solve generic systems.

BiCG is based on the bi-Lanczos tridiagonalization method and in exact arithmetic should terminate in at most N iterations (2N MV's, with A and  $A^{\wedge}H$ ). It forms the basis of many of the cheaper methods such as BiCGSTAB and CGS.

Reference: R.Fletcher, Conjugate gradient methods for indefinite systems, doi: 10.1007/BFb0080116

# **Template Parameters**

ValueType	precision of matrix elements
-----------	------------------------------

#### 46.18.2 Member Function Documentation

#### 46.18.2.1 apply\_uses\_initial\_guess()

```
template<typename ValueType = default_precision>
bool gko::solver::Bicg< ValueType >::apply_uses_initial_guess ( ) const [inline], [override]
```

Return true as iterative solvers use the data in x as an initial guess.

#### Returns

true as iterative solvers use the data in x as an initial guess.

```
73 { return true; }
```

#### 46.18.2.2 conj transpose()

```
template<typename ValueType = default_precision>
std::unique_ptr<LinOp> gko::solver::Bicg< ValueType >::conj_transpose ( ) const [override],
[virtual]
```

Returns a LinOp representing the conjugate transpose of the Transposable object.

# Returns

a pointer to the new conjugate transposed object

Implements gko::Transposable.

#### 46.18.2.3 parse()

Create the parameters from the property\_tree.

Because this is directly tied to the specific type, the value/index type settings within config are ignored and type\_ descriptor is only used for children configs.

#### **Parameters**

config	the property tree for setting	
context	the registry	
td_for_child	the type descriptor for children configs. The default uses the value type of this class.	

#### Returns

parameters

# 46.18.2.4 transpose()

```
template<typename ValueType = default_precision>
std::unique_ptr<LinOp> gko::solver::Bicg< ValueType >::transpose ( ) const [override], [virtual]
```

Returns a LinOp representing the transpose of the Transposable object.

#### Returns

a pointer to the new transposed object

Implements gko::Transposable.

The documentation for this class was generated from the following file:

ginkgo/core/solver/bicg.hpp

# 46.19 gko::batch::solver::Bicgstab< ValueType > Class Template Reference

BiCGSTAB or the Bi-Conjugate Gradient-Stabilized is a Krylov subspace solver.

#include <ginkgo/core/solver/batch\_bicgstab.hpp>

#### **Additional Inherited Members**

# 46.19.1 Detailed Description

```
template<typename ValueType = default_precision> class gko::batch::solver::Bicgstab< ValueType >
```

BiCGSTAB or the Bi-Conjugate Gradient-Stabilized is a Krylov subspace solver.

Being a generic solver, it is capable of solving general matrices, including non-s.p.d matrices.

This solver solves a batch of linear systems using the Bicgstab algorithm. Each linear system in the batch can converge independently.

Unless otherwise specified via the preconditioner factory parameter, this implementation does not use any preconditioner by default. The type of tolerance (absolute or relative) and the maximum number of iterations to be used in the stopping criterion can be set via the factory parameters.

Note

The tolerance check is against the internal residual computed within the solver process. This implicit (internal) residual, can diverge from the true residual (||b - Ax||). A posterori checks (by computing the true residual, ||b - Ax||) are recommended to ensure that the solution has converged to the desired tolerance.

# **Template Parameters**

ValueType	precision of matrix elements
-----------	------------------------------

The documentation for this class was generated from the following file:

• ginkgo/core/solver/batch\_bicgstab.hpp

# 46.20 gko::solver::Bicgstab < ValueType > Class Template Reference

BiCGSTAB or the Bi-Conjugate Gradient-Stabilized is a Krylov subspace solver.

#include <ginkgo/core/solver/bicgstab.hpp>

# **Public Member Functions**

- std::unique\_ptr< LinOp > transpose () const override
   Returns a LinOp representing the transpose of the Transposable object.
- $std::unique\_ptr < LinOp > conj\_transpose$  () const override

Returns a LinOp representing the conjugate transpose of the Transposable object.

· bool apply\_uses\_initial\_guess () const override

Return true as iterative solvers use the data in x as an initial guess.

# **Static Public Member Functions**

• static parameters\_type parse (const config::pnode &config, const config::registry &context, const config::type\_descriptor &td\_for\_child=config::make\_type\_descriptor < ValueType >())

Create the parameters from the property\_tree.

# 46.20.1 Detailed Description

template<typename ValueType = default\_precision> class gko::solver::Bicgstab< ValueType >

BiCGSTAB or the Bi-Conjugate Gradient-Stabilized is a Krylov subspace solver.

Being a generic solver, it is capable of solving general matrices, including non-s.p.d matrices. Though, the memory and the computational requirement of the BiCGSTAB solver are higher than of its s.p.d solver counterpart, it has the capability to solve generic systems. It was developed by stabilizing the BiCG method.

# **Template Parameters**

ValueType precision of the elements of the system matrix.

# 46.20.2 Member Function Documentation

# 46.20.2.1 apply\_uses\_initial\_guess()

```
template<typename ValueType = default_precision>
bool gko::solver::Bicgstab< ValueType >::apply_uses_initial_guess ( ) const [inline], [override]
```

Return true as iterative solvers use the data in x as an initial guess.

#### Returns

true as iterative solvers use the data in x as an initial guess.

```
72 { return true; }
```

# 46.20.2.2 conj\_transpose()

```
template<typename ValueType = default_precision>
std::unique_ptr<LinOp> gko::solver::Bicgstab< ValueType >::conj_transpose ( ) const [override],
[virtual]
```

Returns a LinOp representing the conjugate transpose of the Transposable object.

# Returns

a pointer to the new conjugate transposed object

Implements gko::Transposable.

## 46.20.2.3 parse()

Create the parameters from the property tree.

Because this is directly tied to the specific type, the value/index type settings within config are ignored and type\_ descriptor is only used for children configs.

#### **Parameters**

config	the property tree for setting	
context	the registry	
td_for_child	the type descriptor for children configs. The default uses the value type of this class.	

#### Returns

parameters

#### 46.20.2.4 transpose()

```
template<typename ValueType = default_precision>
std::unique_ptr<LinOp> gko::solver::Bicgstab< ValueType >::transpose ( ) const [override],
[virtual]
```

Returns a LinOp representing the transpose of the Transposable object.

#### Returns

a pointer to the new transposed object

Implements gko::Transposable.

The documentation for this class was generated from the following file:

• ginkgo/core/solver/bicgstab.hpp

# 46.21 gko::preconditioner::block\_interleaved\_storage\_scheme < IndexType > Struct Template Reference

Defines the parameters of the interleaved block storage scheme used by block-Jacobi blocks.

#include <ginkgo/core/preconditioner/jacobi.hpp>

# **Public Member Functions**

- IndexType get\_group\_size () const noexcept
  - Returns the number of elements in the group.
- size\_type compute\_storage\_space (size\_type num\_blocks) const noexcept

Computes the storage space required for the requested number of blocks.

- IndexType get\_group\_offset (IndexType block\_id) const noexcept
  - Returns the offset of the group belonging to the block with the given ID.
- IndexType get\_block\_offset (IndexType block\_id) const noexcept
  - Returns the offset of the block with the given ID within its group.
- IndexType get\_global\_block\_offset (IndexType block\_id) const noexcept

Returns the offset of the block with the given ID.

IndexType get\_stride () const noexcept

Returns the stride between columns of the block.

# **Public Attributes**

IndexType block\_offset

The offset between consecutive blocks within the group.

IndexType group\_offset

The offset between two block groups.

• uint32 group\_power

Then base 2 power of the group.

# 46.21.1 Detailed Description

```
template<typename IndexType> struct gko::preconditioner::block_interleaved_storage_scheme< IndexType >
```

Defines the parameters of the interleaved block storage scheme used by block-Jacobi blocks.

**Template Parameters** 

IndexType type used for storing indices of the matrix

#### 46.21.2 Member Function Documentation

#### 46.21.2.1 compute\_storage\_space()

Computes the storage space required for the requested number of blocks.

#### **Parameters**

num blocks	the total number of blocks that needs to be stored
num biocks	ine loial number of blocks that needs to be st

#### Returns

the total memory (as the number of elements) that need to be allocated for the scheme

#### Note

To simplify using the method in situations where the number of blocks is not known, for a special input  $size \leftarrow \_type\{\} - 1$  the method returns 0 to avoid overallocation of memory.

# 46.21.2.2 get\_block\_offset()

Returns the offset of the block with the given ID within its group.

#### **Parameters**

block←	the ID of the block
id	

#### Returns

the offset of the block with ID block\_id within its group

Referenced by gko::preconditioner::block\_interleaved\_storage\_scheme < index\_type >::get\_global\_block\_offset().

# 46.21.2.3 get\_global\_block\_offset()

Returns the offset of the block with the given ID.

#### **Parameters**

block⊷	the ID of the block
_id	

# Returns

the offset of the block with ID block\_id

# 46.21.2.4 get\_group\_offset()

Returns the offset of the group belonging to the block with the given ID.

#### **Parameters**

block⊷	the ID of the block
id	

#### Returns

the offset of the group belonging to block with ID block\_id

Referenced by gko::preconditioner::block\_interleaved\_storage\_scheme < index\_type >::get\_global\_block\_offset().

#### 46.21.2.5 get\_group\_size()

```
template<typename IndexType>
IndexType gko::preconditioner::block_interleaved_storage_scheme< IndexType >::get_group_size (
) const [inline], [noexcept]
```

Returns the number of elements in the group.

## Returns

the number of elements in the group

Referenced by  $gko::preconditioner::block_interleaved_storage_scheme < index_type >::compute_storage_ \leftrightarrow space(), and <math>gko::preconditioner::block_interleaved_storage_scheme < index_type >::get_block_offset().$ 

# 46.21.2.6 get\_stride()

```
template<typename IndexType>
IndexType gko::preconditioner::block_interleaved_storage_scheme< IndexType >::get_stride ( )
const [inline], [noexcept]
```

Returns the stride between columns of the block.

#### Returns

stride between columns of the block

#### 46.21.3 Member Data Documentation

#### 46.21.3.1 group power

```
template<typename IndexType>
uint32 gko::preconditioner::block_interleaved_storage_scheme< IndexType >::group_power
```

Then base 2 power of the group.

I.e. the group contains 1 << group\_power elements.

Referenced by gko::preconditioner::block\_interleaved\_storage\_scheme< index\_type >::get\_group\_offset(), gko ::preconditioner::block\_interleaved\_storage\_scheme< index\_type >::get\_group\_size(), and gko::preconditioner ::block interleaved storage scheme< index type >::get stride().

The documentation for this struct was generated from the following file:

• ginkgo/core/preconditioner/jacobi.hpp

# 46.22 gko::BlockOperator Class Reference

A BlockOperator represents a linear operator that is partitioned into multiple blocks.

```
#include <ginkgo/core/base/block_operator.hpp>
```

#### **Public Member Functions**

dim< 2 > get\_block\_size () const

Get the block dimension of this, i.e.

const LinOp \* block\_at (size\_type i, size\_type j) const

Const access to a specific block.

BlockOperator (const BlockOperator & other)

Copy constructs a BlockOperator.

BlockOperator (BlockOperator &&other) noexcept

Move constructs a BlockOperator.

BlockOperator & operator= (const BlockOperator & other)

Copy assigns a BlockOperator.

• BlockOperator & operator= (BlockOperator &&other)

Move assigns a BlockOperator.

# **Static Public Member Functions**

- static std::unique\_ptr< BlockOperator > create (std::shared\_ptr< const Executor > exec)
   Create empty BlockOperator.
- static std::unique\_ptr< BlockOperator > create (std::shared\_ptr< const Executor > exec, std::vector< std → ::vector< std::shared\_ptr< const LinOp >>> blocks)

Create BlockOperator from the given blocks.

# 46.22.1 Detailed Description

A BlockOperator represents a linear operator that is partitioned into multiple blocks.

For example, a BlockOperator can be used to define the operator:

```
| A B |
| C D |
```

where A, B, C, D itself are matrices of compatible size. This can be created with:

```
std::shared_ptr<LinOp> A = ...;
std::shared_ptr<LinOp> B = ...;
std::shared_ptr<LinOp> C = ...;
std::shared_ptr<LinOp> D = ...;
auto bop = BlockOperator::create(exec, {{A, B}, {C, D}});
```

The requirements on the individual blocks passed to the create method are:

- · In each block-row, all blocks have the same number of rows
- · In each block-column, all blocks have the same number of columns
- Each block-row must have the same number of blocks It is possible to set blocks to zero, by passing in a nullptr. But every block-row and block-column must contain at least one non-nullptr block.

The constructor will store all passed in blocks on the same executor as the BlockOperator, which will requires copying any block that is associated with a different executor.

#### 46.22.2 Constructor & Destructor Documentation

# 46.22.2.1 BlockOperator() [1/2]

Copy constructs a BlockOperator.

The executor of other is used for this. The blocks of other are deep-copied into this, using clone.

# 46.22.2.2 BlockOperator() [2/2]

Move constructs a BlockOperator.

The executor of other is used for this. All remaining data of other is moved into this. After this operation, other will be empty.

# 46.22.3 Member Function Documentation

# 46.22.3.1 block\_at()

Const access to a specific block.

#### **Parameters**

i	block row.
j	block column.

# Returns

the block stored at (i, j).

# 46.22.3.2 create() [1/2]

Create empty BlockOperator.

#### **Parameters**

exec	the executor of this.
------	-----------------------

#### Returns

empty BlockOperator.

# 46.22.3.3 create() [2/2]

Create BlockOperator from the given blocks.

# **Parameters**

exec	the executor of this.	
blocks	the blocks of this operator. The blocks will be used in a row-major form.	

#### Returns

BlockOperator with the given blocks.

#### 46.22.3.4 get\_block\_size()

```
dim<2> gko::BlockOperator::get_block_size ( ) const [inline]
```

Get the block dimension of this, i.e.

the number of blocks per row and column.

Returns

The block dimension of this.

#### 46.22.3.5 operator=() [1/2]

Move assigns a BlockOperator.

The executor of this is not modified. All data of other (except its executor) is moved into this. If the executor of this and other differ, the blocks will be copied to the executor of this. After this operation, other will be empty.

#### 46.22.3.6 operator=() [2/2]

Copy assigns a BlockOperator.

The executor of this is not modified. The blocks of other are deep-copied into this, using clone.

The documentation for this class was generated from the following file:

· ginkgo/core/base/block\_operator.hpp

# 46.23 gko::BlockSizeError< IndexType > Class Template Reference

Error that denotes issues between block sizes and matrix dimensions.

```
#include <ginkgo/core/base/exception.hpp>
```

## **Public Member Functions**

BlockSizeError (const std::string &file, const int line, const int block\_size, const IndexType size)

# 46.23.1 Detailed Description

```
template<typename IndexType>
class gko::BlockSizeError< IndexType >
```

Error that denotes issues between block sizes and matrix dimensions.

# **Template Parameters**

#### 46.23.2 Constructor & Destructor Documentation

# 46.23.2.1 BlockSizeError()

#### **Parameters**

file	The name of the offending source file	
line	The source code line number where the error occurred	
block_size	Size of small dense blocks in a matrix	
size	The size that is not exactly divided by the block size	

The documentation for this class was generated from the following file:

· ginkgo/core/base/exception.hpp

# 46.24 gko::solver::CbGmres < ValueType > Class Template Reference

CB-GMRES or the compressed basis generalized minimal residual method is an iterative type Krylov subspace method which is suitable for nonsymmetric linear systems.

```
#include <ginkgo/core/solver/cb_gmres.hpp>
```

# **Public Member Functions**

• size\_type get\_krylov\_dim () const

Returns the Krylov dimension.

void set\_krylov\_dim (size\_type other)

Sets the Krylov dimension.

• cb\_gmres::storage\_precision get\_storage\_precision () const

Returns the storage precision used internally.

#### **Static Public Member Functions**

• static parameters\_type parse (const config::pnode &config, const config::registry &context, const config::type\_descriptor &td\_for\_child=config::make\_type\_descriptor < ValueType >())

Create the parameters from the property\_tree.

# 46.24.1 Detailed Description

```
template<typename ValueType = default_precision> class gko::solver::CbGmres< ValueType >
```

CB-GMRES or the compressed basis generalized minimal residual method is an iterative type Krylov subspace method which is suitable for nonsymmetric linear systems.

The implementation in Ginkgo makes use of the merged kernel to make the best use of data locality. The inner operations in one iteration of CB-GMRES are merged into 2 separate steps. Classical Gram-Schmidt with reorthogonalization is used.

The Krylov basis can be stored in reduced precision (compressed) to reduce memory accesses, while all computations (including Krylov basis operations) are performed in the same arithmetic precision ValueType. By default, the Krylov basis are stored in one precision lower than ValueType.

#### **Template Parameters**

#### 46.24.2 Member Function Documentation

# 46.24.2.1 get\_krylov\_dim()

```
template<typename ValueType = default_precision>
size_type gko::solver::CbGmres< ValueType >::get_krylov_dim ( ) const [inline]
```

Returns the Krylov dimension.

# Returns

the Krylov dimension

```
110 { return parameters_.krylov_dim; }
```

#### 46.24.2.2 get\_storage\_precision()

```
template<typename ValueType = default_precision>
cb_gmres::storage_precision gko::solver::CbGmres< ValueType >::get_storage_precision ( ) const
[inline]
```

Returns the storage precision used internally.

#### Returns

the storage precision used internally

#### 46.24.2.3 parse()

Create the parameters from the property\_tree.

Because this is directly tied to the specific type, the value/index type settings within config are ignored and type\_ descriptor is only used for children configs.

#### **Parameters**

config	the property tree for setting	
context	the registry	
td_for_child	the type descriptor for children configs. The default uses the value type of this class.	

#### Returns

parameters

# 46.24.2.4 set\_krylov\_dim()

Sets the Krylov dimension.

#### **Parameters**

other	the new Krylov dimension
-------	--------------------------

The documentation for this class was generated from the following file:

ginkgo/core/solver/cb\_gmres.hpp

# 46.25 gko::batch::solver::Cg< ValueType > Class Template Reference

Cg or the Conjugate Gradient is a Krylov subspace solver.

#include <ginkgo/core/solver/batch\_cg.hpp>

#### **Additional Inherited Members**

# 46.25.1 Detailed Description

template<typename ValueType = default\_precision> class gko::batch::solver::Cg< ValueType >

Cg or the Conjugate Gradient is a Krylov subspace solver.

It is a short recurrence solver that is generally used to solve linear systems with SPD matrices.

This solver solves a batch of linear systems using the Cg algorithm. Each linear system in the batch can converge independently.

Unless otherwise specified via the preconditioner factory parameter, this implementation does not use any preconditioner by default. The type of tolerance (absolute or relative) and the maximum number of iterations to be used in the stopping criterion can be set via the factory parameters.

#### Note

The tolerance check is against the internal residual computed within the solver process. This implicit (internal) residual can diverge from the true residual (||b - Ax||). A posterori checks (by computing the true residual, ||b - Ax||) are recommended to ensure that the solution has converged to the desired tolerance.

#### **Template Parameters**

ValueType	precision of matrix elements

The documentation for this class was generated from the following file:

ginkgo/core/solver/batch\_cg.hpp

# 46.26 gko::solver::Cg< ValueType > Class Template Reference

CG or the conjugate gradient method is an iterative type Krylov subspace method which is suitable for symmetric positive definite methods.

```
#include <ginkgo/core/solver/cg.hpp>
```

#### **Public Member Functions**

- std::unique\_ptr< LinOp > transpose () const override
   Returns a LinOp representing the transpose of the Transposable object.
- std::unique\_ptr< LinOp > conj\_transpose () const override

Returns a LinOp representing the conjugate transpose of the Transposable object.

· bool apply\_uses\_initial\_guess () const override

Return true as iterative solvers use the data in x as an initial guess.

#### **Static Public Member Functions**

• static parameters\_type parse (const config::pnode &config, const config::registry &context, const config::type\_descriptor &td\_for\_child=config::make\_type\_descriptor < ValueType >())

Create the parameters from the property tree.

# 46.26.1 Detailed Description

```
template<typename ValueType = default_precision>
class gko::solver::Cg< ValueType >
```

CG or the conjugate gradient method is an iterative type Krylov subspace method which is suitable for symmetric positive definite methods.

Though this method performs very well for symmetric positive definite matrices, it is in general not suitable for general matrices.

The implementation in Ginkgo makes use of the merged kernel to make the best use of data locality. The inner operations in one iteration of CG are merged into 2 separate steps.

#### **Template Parameters**

```
ValueType precision of matrix elements
```

# 46.26.2 Member Function Documentation

#### 46.26.2.1 apply\_uses\_initial\_guess()

```
template<typename ValueType = default_precision>
bool gko::solver::Cg< ValueType >::apply_uses_initial_guess ( ) const [inline], [override]
```

Return true as iterative solvers use the data in x as an initial guess.

#### Returns

true as iterative solvers use the data in x as an initial guess.

```
67 { return true; }
```

# 46.26.2.2 conj\_transpose()

```
template<typename ValueType = default_precision>
std::unique_ptr<LinOp> gko::solver::Cg< ValueType >::conj_transpose ( ) const [override],
[virtual]
```

Returns a LinOp representing the conjugate transpose of the Transposable object.

#### Returns

a pointer to the new conjugate transposed object

Implements gko::Transposable.

#### 46.26.2.3 parse()

Create the parameters from the property\_tree.

Because this is directly tied to the specific type, the value/index type settings within config are ignored and type\_ descriptor is only used for children configs.

# **Parameters**

config	the property tree for setting
context	the registry
td_for_child	the type descriptor for children configs. The default uses the value type of this class.

# Returns

parameters

#### 46.26.2.4 transpose()

```
template<typename ValueType = default_precision>
std::unique_ptr<LinOp> gko::solver::Cg< ValueType >::transpose ( ) const [override], [virtual]
```

Returns a LinOp representing the transpose of the Transposable object.

Returns

a pointer to the new transposed object

Implements gko::Transposable.

The documentation for this class was generated from the following file:

• ginkgo/core/solver/cg.hpp

# 46.27 gko::solver::Cgs< ValueType > Class Template Reference

CGS or the conjugate gradient square method is an iterative type Krylov subspace method which is suitable for general systems.

#include <ginkgo/core/solver/cgs.hpp>

# **Public Member Functions**

- std::unique\_ptr< LinOp > transpose () const override
  - Returns a LinOp representing the transpose of the Transposable object.
- std::unique\_ptr< LinOp > conj\_transpose () const override

Returns a LinOp representing the conjugate transpose of the Transposable object.

· bool apply\_uses\_initial\_guess () const override

Return true as iterative solvers use the data in x as an initial guess.

#### **Static Public Member Functions**

• static parameters\_type parse (const config::pnode &config, const config::registry &context, const config::type\_descriptor &td\_for\_child=config::make\_type\_descriptor < ValueType >())

Create the parameters from the property\_tree.

# 46.27.1 Detailed Description

```
template<typename ValueType = default_precision> class gko::solver::Cgs< ValueType >
```

CGS or the conjugate gradient square method is an iterative type Krylov subspace method which is suitable for general systems.

The implementation in Ginkgo makes use of the merged kernel to make the best use of data locality. The inner operations in one iteration of CGS are merged into 3 separate steps.

#### **Template Parameters**

ValueType | precision of matrix elements

#### 46.27.2 Member Function Documentation

#### 46.27.2.1 apply\_uses\_initial\_guess()

```
template<typename ValueType = default_precision>
bool gko::solver::Cgs< ValueType >::apply_uses_initial_guess ( ) const [inline], [override]
```

Return true as iterative solvers use the data in x as an initial guess.

#### Returns

true as iterative solvers use the data in x as an initial guess.

```
64 { return true; }
```

#### 46.27.2.2 conj transpose()

```
template<typename ValueType = default_precision>
std::unique_ptr<LinOp> gko::solver::Cgs< ValueType >::conj_transpose ( ) const [override],
[virtual]
```

Returns a LinOp representing the conjugate transpose of the Transposable object.

# Returns

a pointer to the new conjugate transposed object

Implements gko::Transposable.

#### 46.27.2.3 parse()

Create the parameters from the property\_tree.

Because this is directly tied to the specific type, the value/index type settings within config are ignored and type\_ descriptor is only used for children configs.

#### **Parameters**

config	the property tree for setting	
context	the registry	
td_for_child	the type descriptor for children configs. The default uses the value type of this class.	

#### Returns

parameters

#### 46.27.2.4 transpose()

```
template<typename ValueType = default_precision>
std::unique_ptr<LinOp> gko::solver::Cgs< ValueType >::transpose ( ) const [override], [virtual]
```

Returns a LinOp representing the transpose of the Transposable object.

#### Returns

a pointer to the new transposed object

Implements gko::Transposable.

The documentation for this class was generated from the following file:

• ginkgo/core/solver/cgs.hpp

# 46.28 gko::experimental::factorization::Cholesky< ValueType, IndexType > Class Template Reference

Computes a Cholesky factorization of a symmetric, positive-definite sparse matrix.

#include <ginkgo/core/factorization/cholesky.hpp>

# **Public Member Functions**

- const parameters\_type & get\_parameters ()
   Returns the parameters used to construct the factory.
- const parameters\_type & get\_parameters () const

Returns the parameters used to construct the factory.

• std::unique\_ptr< factorization\_type > generate (std::shared\_ptr< const LinOp > system\_matrix) const

#### Static Public Member Functions

- static parameters\_type build ()
  - Creates a new parameter\_type to set up the factory.
- static parameters\_type parse (const config::pnode &config, const config::registry &context, const config::type\_descriptor &td\_for\_child=config::make\_type\_descriptor < ValueType, IndexType >())

Create the parameters from the property\_tree.

# 46.28.1 Detailed Description

```
template < typename\ ValueType,\ typename\ IndexType > \\ class\ gko::experimental::factorization::Cholesky < ValueType,\ IndexType > \\
```

Computes a Cholesky factorization of a symmetric, positive-definite sparse matrix.

This LinOpFactory returns a Factorization storing the L and  $L^{\wedge}H$  factors for the provided system matrix in matrix::Csr format. If no symbolic factorization is provided, it will be computed first.

#### **Template Parameters**

ValueType	the type used to store values of the system matrix
IndexType	the type used to store sparsity pattern indices of the system matrix

# 46.28.2 Member Function Documentation

#### 46.28.2.1 generate()

### Note

This function overrides the default LinOpFactory::generate to return a Factorization instead of a generic LinOp, which would need to be cast to Factorization again to access its factors. It is only necessary because smart pointers aren't covariant.

#### 46.28.2.2 get\_parameters() [1/2]

```
\label{template} $$ \ensuremath{\sf template}$ \ensuremath{\sf type}$ , typename IndexType > $$ const parameters_type& gko::experimental::factorization::Cholesky< ValueType, IndexType > $$ ::get_parameters ( ) [inline] $$
```

Returns the parameters used to construct the factory.

#### Returns

the parameters used to construct the factory.

```
77 { return parameters_; }
```

#### 46.28.2.3 get parameters() [2/2]

```
template<typename ValueType , typename IndexType >
const parameters_type& gko::experimental::factorization::Cholesky< ValueType, IndexType >←
::get_parameters ( ) const [inline]
```

Returns the parameters used to construct the factory.

#### Returns

the parameters used to construct the factory.

# 46.28.2.4 parse()

Create the parameters from the property\_tree.

Because this is directly tied to the specific type, the value/index type settings within config are ignored and type\_ descriptor is only used for children configs.

#### **Parameters**

config	the property tree for setting	
context	the registry	
td_for_child	the type descriptor for children configs. The default uses the value/index type of this class.	

Returns

parameters

The documentation for this class was generated from the following file:

· ginkgo/core/factorization/cholesky.hpp

# 46.29 gko::matrix::Csr< ValueType, IndexType >::classical Class Reference

classical is a strategy\_type which uses the same number of threads on each row.

```
#include <ginkgo/core/matrix/csr.hpp>
```

#### **Public Member Functions**

· classical ()

Creates a classical strategy.

- void process (const array < index\_type > &mtx\_row\_ptrs, array < index\_type > \*mtx\_srow) override
   Computes srow according to row pointers.
- int64\_t clac\_size (const int64\_t nnz) override

Computes the srow size according to the number of nonzeros.

 std::shared\_ptr< strategy\_type > copy () override Copy a strategy.

# 46.29.1 Detailed Description

```
template < typename ValueType = default_precision, typename IndexType = int32 > class gko::matrix::Csr < ValueType, IndexType > ::classical
```

classical is a strategy\_type which uses the same number of threads on each row.

Classical strategy uses multithreads to calculate on parts of rows and then do a reduction of these threads results. The number of threads per row depends on the max number of stored elements per row.

#### 46.29.2 Member Function Documentation

# 46.29.2.1 clac\_size()

Computes the srow size according to the number of nonzeros.

#### **Parameters**

```
nnz the number of nonzeros
```

#### Returns

the size of srow

Implements gko::matrix::Csr< ValueType, IndexType >::strategy\_type.

#### 46.29.2.2 copy()

```
template<typename ValueType = default_precision, typename IndexType = int32>
std::shared_ptr<strategy_type> gko::matrix::Csr< ValueType, IndexType >::classical::copy ( )
[inline], [override], [virtual]
```

Copy a strategy.

This is a workaround until strategies are revamped, since strategies like automatical do not work when actually shared.

Implements gko::matrix::Csr< ValueType, IndexType >::strategy\_type.

# 46.29.2.3 process()

Computes srow according to row pointers.

#### **Parameters**

mtx_row_ptrs	the row pointers of the matrix
mtx_srow	the srow of the matrix

 $Implements\ gko::matrix::Csr< ValueType,\ IndexType>::strategy\_type.$ 

References gko::array< ValueType >::get\_const\_data(), gko::array< ValueType >::get\_executor(), and gko ::array< ValueType >::get size().

The documentation for this class was generated from the following file:

ginkgo/core/matrix/csr.hpp

# 46.30 gko::matrix::Hybrid< ValueType, IndexType >::column\_limit Class Reference

column\_limit is a strategy\_type which decides the number of stored elements per row of the ell part by specifying the number of columns.

#include <ginkgo/core/matrix/hybrid.hpp>

# **Public Member Functions**

- column\_limit (size\_type num\_column=0)
  - Creates a column\_limit strategy.
- size\_type compute\_ell\_num\_stored\_elements\_per\_row (array< size\_type > \*row\_nnz) const override

  Computes the number of stored elements per row of the ell part.
- auto get\_num\_columns () const

Get the number of columns limit.

# 46.30.1 Detailed Description

template<typename ValueType = default\_precision, typename IndexType = int32> class gko::matrix::Hybrid< ValueType, IndexType >::column\_limit

column\_limit is a strategy\_type which decides the number of stored elements per row of the ell part by specifying the number of columns.

# 46.30.2 Constructor & Destructor Documentation

#### 46.30.2.1 column\_limit()

Creates a column\_limit strategy.

#### **Parameters**

num\_column the specified number of columns of the ell part

## 46.30.3 Member Function Documentation

#### 46.30.3.1 compute\_ell\_num\_stored\_elements\_per\_row()

Computes the number of stored elements per row of the ell part.

#### **Parameters**

row_nnz	the number of nonzeros of each row
---------	------------------------------------

#### Returns

the number of stored elements per row of the ell part

Implements gko::matrix::Hybrid< ValueType, IndexType >::strategy\_type.

# 46.30.3.2 get\_num\_columns()

```
template<typename ValueType = default_precision, typename IndexType = int32>
auto gko::matrix::Hybrid< ValueType, IndexType >::column_limit::get_num_columns ( ) const
[inline]
```

Get the number of columns limit.

#### Returns

the number of columns limit

The documentation for this class was generated from the following file:

· ginkgo/core/matrix/hybrid.hpp

# 46.31 gko::Combination < ValueType > Class Template Reference

The Combination class can be used to construct a linear combination of multiple linear operators c1 \* op1 + c2 \* op2 + ...

#include <ginkgo/core/base/combination.hpp>

#### **Public Member Functions**

- const std::vector< std::shared\_ptr< const LinOp > > & get\_coefficients () const noexcept
   Returns a list of coefficients of the combination.
- const std::vector< std::shared\_ptr< const LinOp > > & get\_operators () const noexcept Returns a list of operators of the combination.
- std::unique\_ptr< LinOp > transpose () const override

Returns a LinOp representing the transpose of the Transposable object.

std::unique\_ptr< LinOp > conj\_transpose () const override

Returns a LinOp representing the conjugate transpose of the Transposable object.

Combination & operator= (const Combination &)

Copy-assigns a Combination.

• Combination & operator= (Combination &&)

Move-assigns a Combination.

• Combination (const Combination &)

Copy-constructs a Combination.

Combination (Combination &&)

Move-constructs a Combination.

# 46.31.1 Detailed Description

```
template<typename ValueType = default_precision> class gko::Combination< ValueType >
```

The Combination class can be used to construct a linear combination of multiple linear operators c1 \* op1 + c2 \* op2 + ...

• ck \* opk.

Combination ensures that all LinOps passed to its constructor use the same executor, and if not, copies the operators to the executor of the first operator.

**Template Parameters** 

ValueType precision of input and result vectors

# 46.31.2 Constructor & Destructor Documentation

#### 46.31.2.1 Combination() [1/2]

Copy-constructs a Combination.

This inherits the executor of the input Combination and all of its operators with shared ownership.

# 46.31.2.2 Combination() [2/2]

Move-constructs a Combination.

This inherits the executor of the input Combination and all of its operators. The moved-from object is empty (0x0 LinOp without operators) afterwards.

# 46.31.3 Member Function Documentation

# 46.31.3.1 conj\_transpose()

```
template<typename ValueType = default_precision>
std::unique_ptr<LinOp> gko::Combination< ValueType >::conj_transpose ( ) const [override],
[virtual]
```

Returns a LinOp representing the conjugate transpose of the Transposable object.

#### Returns

a pointer to the new conjugate transposed object

Implements gko::Transposable.

# 46.31.3.2 get\_coefficients()

```
template<typename ValueType = default_precision> const std::vector<std::shared_ptr<const LinOp> >& gko::Combination< ValueType >::get_ \leftarrow coefficients ( ) const [inline], [noexcept]
```

Returns a list of coefficients of the combination.

#### Returns

# a list of coefficients

```
48 {
49 return coefficients_;
50 }
```

#### 46.31.3.3 get\_operators()

```
template<typename ValueType = default_precision> const std::vector<std::shared_ptr<const LinOp> >& gko::Combination< ValueType >::get_ \leftarrow operators ( ) const [inline], [noexcept]
```

Returns a list of operators of the combination.

Returns

a list of operators

#### 46.31.3.4 operator=() [1/2]

Move-assigns a Combination.

The executor is not modified, and the wrapped LinOps are only being cloned if they are on a different executor, otherwise they share ownership. The moved-from object is empty (0x0 LinOp without operators) afterwards.

#### 46.31.3.5 operator=() [2/2]

Copy-assigns a Combination.

The executor is not modified, and the wrapped LinOps are only being cloned if they are on a different executor.

#### 46.31.3.6 transpose()

```
template<typename ValueType = default_precision>
std::unique_ptr<LinOp> gko::Combination< ValueType >::transpose ( ) const [override], [virtual]
```

Returns a LinOp representing the transpose of the Transposable object.

Returns

a pointer to the new transposed object

Implements gko::Transposable.

The documentation for this class was generated from the following file:

• ginkgo/core/base/combination.hpp

# 46.32 gko::stop::Combined Class Reference

The Combined class is used to combine multiple criterions together through an OR operation.

#include <ginkgo/core/stop/combined.hpp>

# 46.32.1 Detailed Description

The Combined class is used to combine multiple criterions together through an OR operation.

The typical use case is to stop the iteration process if any of the criteria is fulfilled, e.g. a number of iterations, the relative residual norm has reached a threshold, etc.

The documentation for this class was generated from the following file:

· ginkgo/core/stop/combined.hpp

# 46.33 gko::experimental::mpi::communicator Class Reference

A thin wrapper of MPI Comm that supports most MPI calls.

#include <ginkgo/core/base/mpi.hpp>

# **Public Member Functions**

communicator (const MPI Comm &comm, bool force host buffer=false)

Non-owning constructor for an existing communicator of type MPI\_Comm.

communicator (const MPI\_Comm &comm, int color, int key)

Create a communicator object from an existing MPI\_Comm object using color and key.

communicator (const communicator &comm, int color, int key)

Create a communicator object from an existing MPI\_Comm object using color and key.

• const MPI\_Comm & get () const

Return the underlying MPI\_Comm object.

· int size () const

Return the size of the communicator (number of ranks).

• int rank () const

Return the rank of the calling process in the communicator.

int node\_local\_rank () const

Return the node local rank of the calling process in the communicator.

bool operator== (const communicator &rhs) const

Compare two communicator objects for equality.

bool operator!= (const communicator &rhs) const

Compare two communicator objects for non-equality.

• void synchronize () const

This function is used to synchronize the ranks in the communicator.

template<typename SendType >
 void send (std::shared\_ptr< const Executor > exec, const SendType \*send\_buffer, const int send\_count,
 const int destination\_rank, const int send\_tag) const

Send (Blocking) data from calling process to destination rank.

template<typename SendType >

request i\_send (std::shared\_ptr< const Executor > exec, const SendType \*send\_buffer, const int send\_← count, const int destination\_rank, const int send\_tag) const

Send (Non-blocking, Immediate return) data from calling process to destination rank.

template<typename RecvType >

status recv (std::shared\_ptr< const Executor > exec, RecvType \*recv\_buffer, const int recv\_count, const int source rank, const int recv\_tag) const

Receive data from source rank.

template<typename RecvType >

request i\_recv (std::shared\_ptr< const Executor > exec, RecvType \*recv\_buffer, const int recv\_count, const int source\_rank, const int recv\_tag) const

Receive (Non-blocking, Immediate return) data from source rank.

 $\bullet \ \ \text{template}{<} \text{typename BroadcastType} >$ 

void broadcast (std::shared\_ptr< const Executor > exec, BroadcastType \*buffer, int count, int root\_rank) const

Broadcast data from calling process to all ranks in the communicator.

template < typename BroadcastType >

request i\_broadcast (std::shared\_ptr< const Executor > exec, BroadcastType \*buffer, int count, int root\_rank) const

(Non-blocking) Broadcast data from calling process to all ranks in the communicator

template<typename ReduceType >

void reduce (std::shared\_ptr< const Executor > exec, const ReduceType \*send\_buffer, ReduceType \*recv← \_buffer, int count, MPI\_Op operation, int root\_rank) const

Reduce data into root from all calling processes on the same communicator.

• template<typename ReduceType >

request i\_reduce (std::shared\_ptr< const Executor > exec, const ReduceType \*send\_buffer, ReduceType \*recv\_buffer, int count, MPI\_Op operation, int root\_rank) const

(Non-blocking) Reduce data into root from all calling processes on the same communicator.

 $\bullet \ \ \text{template}{<} \text{typename ReduceType} >$ 

void all\_reduce (std::shared\_ptr< const Executor > exec, ReduceType \*recv\_buffer, int count, MPI\_Op operation) const

(In-place) Reduce data from all calling processes from all calling processes on same communicator.

• template<typename ReduceType>

request i\_all\_reduce (std::shared\_ptr< const Executor > exec, ReduceType \*recv\_buffer, int count, MPI\_Op operation) const

(In-place, non-blocking) Reduce data from all calling processes from all calling processes on same communicator.

 $\bullet \ \ \text{template}{<} \text{typename ReduceType}>$ 

void all\_reduce (std::shared\_ptr< const Executor > exec, const ReduceType \*send\_buffer, ReduceType \*recv\_buffer, int count, MPI\_Op operation) const

Reduce data from all calling processes from all calling processes on same communicator.

• template<typename ReduceType >

request i\_all\_reduce (std::shared\_ptr< const Executor > exec, const ReduceType \*send\_buffer, ReduceType \*recv\_buffer, int count, MPI\_Op operation) const

Reduce data from all calling processes from all calling processes on same communicator.

template<typename SendType , typename RecvType >

void gather (std::shared\_ptr< const Executor > exec, const SendType \*send\_buffer, const int send\_count, RecvType \*recv buffer, const int recv count, int root rank) const

Gather data onto the root rank from all ranks in the communicator.

template<typename SendType , typename RecvType >

request i\_gather (std::shared\_ptr< const Executor > exec, const SendType \*send\_buffer, const int send\_← count, RecvType \*recv buffer, const int recv count, int root rank) const

(Non-blocking) Gather data onto the root rank from all ranks in the communicator.

template<typename SendType, typename RecvType >
 void gather\_v (std::shared\_ptr< const Executor > exec, const SendType \*send\_buffer, const int send\_count,
 RecvType \*recv buffer, const int \*recv counts, const int \*displacements, int root rank) const

Gather data onto the root rank from all ranks in the communicator with offsets.

template < typename SendType , typename RecvType >
 request i\_gather\_v (std::shared\_ptr < const Executor > exec, const SendType \*send\_buffer, const int send ←
 \_count, RecvType \*recv\_buffer, const int \*recv\_counts, const int \*displacements, int root\_rank) const
 (Non-blocking) Gather data onto the root rank from all ranks in the communicator with offsets.

template<typename SendType , typename RecvType >
 void all\_gather (std::shared\_ptr< const Executor > exec, const SendType \*send\_buffer, const int send\_
 count, RecvType \*recv buffer, const int recv count) const

Gather data onto all ranks from all ranks in the communicator.

template<typename SendType, typename RecvType >
 request i\_all\_gather (std::shared\_ptr< const Executor > exec, const SendType \*send\_buffer, const int send\_count, RecvType \*recv\_buffer, const int recv\_count) const

(Non-blocking) Gather data onto all ranks from all ranks in the communicator.

template<typename SendType, typename RecvType >
 void scatter (std::shared\_ptr< const Executor > exec, const SendType \*send\_buffer, const int send\_count,
 RecvType \*recv\_buffer, const int recv\_count, int root\_rank) const

Scatter data from root rank to all ranks in the communicator.

template<typename SendType, typename RecvType >
 request i\_scatter (std::shared\_ptr< const Executor > exec, const SendType \*send\_buffer, const int send\_
 count, RecvType \*recv\_buffer, const int recv\_count, int root\_rank) const

(Non-blocking) Scatter data from root rank to all ranks in the communicator.

template<typename SendType, typename RecvType >
 void scatter\_v (std::shared\_ptr< const Executor > exec, const SendType \*send\_buffer, const int \*send\_
 counts, const int \*displacements, RecvType \*recv\_buffer, const int recv\_count, int root\_rank) const

Scatter data from root rank to all ranks in the communicator with offsets.

template<typename SendType, typename RecvType >
 request i\_scatter\_v (std::shared\_ptr< const Executor > exec, const SendType \*send\_buffer, const int
 \*send\_counts, const int \*displacements, RecvType \*recv\_buffer, const int recv\_count, int root\_rank) const
 (Non-blocking) Scatter data from root rank to all ranks in the communicator with offsets.

template<typename RecvType >
 void all\_to\_all (std::shared\_ptr< const Executor > exec, RecvType \*recv\_buffer, const int recv\_count) const
 (In-place) Communicate data from all ranks to all other ranks in place (MPI\_Alltoall).

template<typename RecvType >
 request i\_all\_to\_all (std::shared\_ptr< const Executor > exec, RecvType \*recv\_buffer, const int recv\_count)
 const

(In-place, Non-blocking) Communicate data from all ranks to all other ranks in place (MPI\_lalltoall).

template<typename SendType, typename RecvType >
 void all\_to\_all (std::shared\_ptr< const Executor > exec, const SendType \*send\_buffer, const int send\_count,
 RecvType \*recv\_buffer, const int recv\_count) const

Communicate data from all ranks to all other ranks (MPI\_Alltoall).

template<typename SendType, typename RecvType >
 request i\_all\_to\_all (std::shared\_ptr< const Executor > exec, const SendType \*send\_buffer, const int send
 count, RecvType \*recv buffer, const int recv count) const

(Non-blocking) Communicate data from all ranks to all other ranks (MPI\_lalltoall).

template<typename SendType, typename RecvType >
 void all\_to\_all\_v (std::shared\_ptr< const Executor > exec, const SendType \*send\_buffer, const int \*send
 \_counts, const int \*send\_offsets, RecvType \*recv\_buffer, const int \*recv\_counts, const int \*recv\_offsets)
 const

Communicate data from all ranks to all other ranks with offsets (MPI\_Alltoallv).

void all\_to\_all\_v (std::shared\_ptr< const Executor > exec, const void \*send\_buffer, const int \*send\_←
 counts, const int \*send\_offsets, MPI\_Datatype send\_type, void \*recv\_buffer, const int \*recv\_counts, const
 int \*recv\_offsets, MPI\_Datatype recv\_type) const

Communicate data from all ranks to all other ranks with offsets (MPI\_Alltoallv).

request i\_all\_to\_all\_v (std::shared\_ptr< const Executor > exec, const void \*send\_buffer, const int \*send
 \_counts, const int \*send\_offsets, MPI\_Datatype send\_type, void \*recv\_buffer, const int \*recv\_counts, const
 int \*recv\_offsets, MPI\_Datatype recv\_type) const

Communicate data from all ranks to all other ranks with offsets (MPI\_Ialltoallv).

template<typename SendType, typename RecvType >
 request i\_all\_to\_all\_v (std::shared\_ptr< const Executor > exec, const SendType \*send\_buffer, const int
 \*send\_counts, const int \*send\_offsets, RecvType \*recv\_buffer, const int \*recv\_counts, const int \*recv\_counts, const int \*recv\_counts

Communicate data from all ranks to all other ranks with offsets (MPI lalltoallv).

template<typename ScanType >
 void scan (std::shared\_ptr< const Executor > exec, const ScanType \*send\_buffer, ScanType \*recv\_buffer,
 int count, MPI Op operation) const

Does a scan operation with the given operator.

template<typename ScanType >
 request i\_scan (std::shared\_ptr< const Executor > exec, const ScanType \*send\_buffer, ScanType \*recv\_
 buffer, int count, MPI\_Op operation) const

Does a scan operation with the given operator.

# 46.33.1 Detailed Description

A thin wrapper of MPI\_Comm that supports most MPI calls.

A wrapper class that takes in the given MPI communicator. If a bare MPI\_Comm is provided, the wrapper takes no ownership of the MPI\_Comm. Thus the MPI\_Comm must remain valid throughout the lifetime of the communicator. If the communicator was created through splitting, the wrapper takes ownership of the MPI\_Comm. In this case, as the class or object goes out of scope, the underlying MPI\_Comm is freed.

Note

All MPI calls that work on a buffer take in an Executor as an additional argument. This argument specifies the memory space the buffer lives in.

# 46.33.2 Constructor & Destructor Documentation

#### 46.33.2.1 communicator() [1/3]

Non-owning constructor for an existing communicator of type MPI\_Comm.

The MPI\_Comm object will not be deleted after the communicator object has been freed and an explicit MPI\_← Comm\_free needs to be called on the original MPI\_Comm object.

#### **Parameters**

comm	The input MPI_Comm object.	
force host buffer	If set to true, always communicates through host memory	
_	, ,	Т

# 46.33.2.2 communicator() [2/3]

Create a communicator object from an existing MPI\_Comm object using color and key.

#### **Parameters**

comm	The input MPI_Comm object.
color	The color to split the original comm object
key	The key to split the comm object

# 46.33.2.3 communicator() [3/3]

Create a communicator object from an existing MPI\_Comm object using color and key.

#### **Parameters**

comm	The input communicator object.
color	The color to split the original comm object
key	The key to split the comm object

References get().

# 46.33.3 Member Function Documentation

# 46.33.3.1 all\_gather()

```
RecvType * recv_buffer,
const int recv_count ) const [inline]
```

Gather data onto all ranks from all ranks in the communicator.

#### **Parameters**

exec	The executor, on which the message buffers are located.
send_buffer	the buffer to gather from
send_count	the number of elements to send
recv_buffer	the buffer to gather into
recv_count	the number of elements to receive

# **Template Parameters**

SendType	the type of the data to send. Has to be a type which has a specialization of type_impl that defines its MPI_Datatype.
RecvType	the type of the data to receive. The same restrictions as for SendType apply.

References get().

# 46.33.3.2 all\_reduce() [1/2]

```
template<typename ReduceType >
void gko::experimental::mpi::communicator::all_reduce (
    std::shared_ptr< const Executor > exec,
    const ReduceType * send_buffer,
    ReduceType * recv_buffer,
    int count,
    MPI_Op operation ) const [inline]
```

Reduce data from all calling processes from all calling processes on same communicator.

# **Parameters**

exec	The executor, on which the message buffers are located.
send_buffer	the data to reduce
recv_buffer	the reduced result
count	the number of elements to reduce
operation	the reduce operation. See @MPI_Op

# **Template Parameters**

ReduceType	the type of the data to send. Has to be a type which has a specialization of type_impl that	
	defines its MPI_Datatype.	

References get().

# 46.33.3.3 all\_reduce() [2/2]

 ${\tt template}{<}{\tt typename} \ {\tt ReduceType} \ >$ 

(In-place) Reduce data from all calling processes from all calling processes on same communicator.

#### **Parameters**

exec	The executor, on which the message buffer is located.
recv_buffer	the data to reduce and the reduced result
count	the number of elements to reduce
operation	the MPI_Op type reduce operation.

# **Template Parameters**

ReduceType	the type of the data to send. Has to be a type which has a specialization of type_impl that	1
	defines its MPI_Datatype.	

References get().

# 46.33.3.4 all\_to\_all() [1/2]

Communicate data from all ranks to all other ranks (MPI\_Alltoall).

See MPI documentation for more details.

# **Parameters**

exec	The executor, on which the message buffers are located.
send_buffer	the buffer to send
send_count	the number of elements to send
recv_buffer	the buffer to receive
recv_count	the number of elements to receive

#### **Template Parameters**

SendType	the type of the data to send. Has to be a type which has a specialization of type_impl that defines its MPI_Datatype.
RecvType	the type of the data to receive. The same restrictions as for SendType apply.

References get().

# 46.33.3.5 all\_to\_all() [2/2]

(In-place) Communicate data from all ranks to all other ranks in place (MPI Alltoall).

See MPI documentation for more details.

#### **Parameters**

exec	The executor, on which the message buffer is located.
buffer	the buffer to send and the buffer receive
recv_count	the number of elements to receive
comm	the communicator

#### **Template Parameters**

RecvType	the type of the data to send. Has to be a type which has a specialization of type_impl that defines	
	its MPI_Datatype.	

# Note

This overload uses MPI\_IN\_PLACE and the source and destination buffers are the same.

References get().

# 46.33.3.6 all\_to\_all\_v() [1/2]

```
template<typename SendType , typename RecvType >
void gko::experimental::mpi::communicator::all_to_all_v (
    std::shared_ptr< const Executor > exec,
    const SendType * send_buffer,
    const int * send_counts,
    const int * send_offsets,
    RecvType * recv_buffer,
    const int * recv_counts,
    const int * recv_counts,
    const int * recv_offsets ) const [inline]
```

Communicate data from all ranks to all other ranks with offsets (MPI\_Alltoallv).

See MPI documentation for more details.

#### **Parameters**

exec	The executor, on which the message buffers are located.
send_buffer	the buffer to send
send_count	the number of elements to send
send_offsets	the offsets for the send buffer
recv_buffer	the buffer to gather into
recv_count	the number of elements to receive
recv_offsets	the offsets for the recv buffer
comm	the communicator

# **Template Parameters**

SendType	the type of the data to send. Has to be a type which has a specialization of type_impl that defines its MPI_Datatype.
RecvType	the type of the data to receive. The same restrictions as for SendType apply.

# 46.33.3.7 all\_to\_all\_v() [2/2]

```
void gko::experimental::mpi::communicator::all_to_all_v (
    std::shared_ptr< const Executor > exec,
    const void * send_buffer,
    const int * send_counts,
    const int * send_offsets,
    MPI_Datatype send_type,
    void * recv_buffer,
    const int * recv_counts,
    const int * recv_counts,
    const int * recv_offsets,
    MPI_Datatype recv_type ) const [inline]
```

Communicate data from all ranks to all other ranks with offsets (MPI\_Alltoallv).

See MPI documentation for more details.

# **Parameters**

exec	The executor, on which the message buffers are located.
send_buffer	the buffer to send
send_count	the number of elements to send
send_offsets	the offsets for the send buffer
send_type	the MPI_Datatype for the send buffer
recv_buffer	the buffer to gather into
recv_count	the number of elements to receive
recv_offsets	the offsets for the recv buffer
recv_type	the MPI_Datatype for the recv buffer
comm	the communicator

# References get().

#### 46.33.3.8 broadcast()

Broadcast data from calling process to all ranks in the communicator.

#### **Parameters**

exec	The executor, on which the message buffer is located.
buffer	the buffer to broadcsat
count	the number of elements to broadcast
root_rank	the rank to broadcast from

# **Template Parameters**

BroadcastType	the type of the data to broadcast. Has to be a type which has a specialization of type_impl
	that defines its MPI_Datatype.

References get().

# 46.33.3.9 gather()

Gather data onto the root rank from all ranks in the communicator.

# **Parameters**

exec	The executor, on which the message buffers are located.
send_buffer	the buffer to gather from
send_count	the number of elements to send
recv_buffer	the buffer to gather into
recv_count	the number of elements to receive
root_rank	the rank to gather into

# **Template Parameters**

SendType	the type of the data to send. Has to be a type which has a specialization of type_impl that defines its MPI_Datatype.	]
RecvType	the type of the data to receive. The same restrictions as for SendType apply.	1

References get().

# 46.33.3.10 gather\_v()

Gather data onto the root rank from all ranks in the communicator with offsets.

#### **Parameters**

exec	The executor, on which the message buffers are located.
send_buffer	the buffer to gather from
send_count	the number of elements to send
recv_buffer	the buffer to gather into
recv_count	the number of elements to receive
displacements	the offsets for the buffer
root_rank	the rank to gather into

# **Template Parameters**

SendType	the type of the data to send. Has to be a type which has a specialization of type_impl that defines its MPI_Datatype.
RecvType	the type of the data to receive. The same restrictions as for SendType apply.

References get().

# 46.33.3.11 get()

```
const MPI_Comm& gko::experimental::mpi::communicator::get ( ) const [inline]
```

Return the underlying MPI\_Comm object.

#### Returns

the MPI\_Comm object

Referenced by all\_gather(), all\_reduce(), all\_to\_all(), all\_to\_all\_v(), broadcast(), communicator(), gather(), gather(), i\_all\_gather(), i\_all\_reduce(), i\_all\_to\_all(), i\_all\_to\_all\_v(), i\_broadcast(), i\_gather(), i\_gather\_v(), i\_recv(), i\_reduce(), i\_scan(), i\_scanter\_v(), i\_send(), recv(), reduce(), scan(), scatter(), scatter\_v(), send(), synchronize(), and gko::experimental::mpi::window<br/>
ValueType >::window().

# 46.33.3.12 i\_all\_gather()

(Non-blocking) Gather data onto all ranks from all ranks in the communicator.

#### **Parameters**

exec	The executor, on which the message buffers are located.
send_buffer	the buffer to gather from
send_count	the number of elements to send
recv_buffer	the buffer to gather into
recv_count	the number of elements to receive

# **Template Parameters**

SendType	the type of the data to send. Has to be a type which has a specialization of type_impl that defines its MPI_Datatype.
RecvType	the type of the data to receive. The same restrictions as for SendType apply.

# Returns

the request handle for the call

References gko::experimental::mpi::request::get(), and get().

# 46.33.3.13 i\_all\_reduce() [1/2]

```
const ReduceType * send_buffer,
ReduceType * recv_buffer,
int count,
MPI_Op operation ) const [inline]
```

Reduce data from all calling processes from all calling processes on same communicator.

#### **Parameters**

exec	The executor, on which the message buffers are located.
send_buffer	the data to reduce
recv_buffer	the reduced result
count	the number of elements to reduce
operation	the reduce operation. See @MPI_Op

# **Template Parameters**

ReduceType	the type of the data to reduce. Has to be a type which has a specialization of type_impl that	1
	defines its MPI_Datatype.	

#### Returns

the request handle for the call

References gko::experimental::mpi::request::get(), and get().

# 46.33.3.14 i\_all\_reduce() [2/2]

(In-place, non-blocking) Reduce data from all calling processes from all calling processes on same communicator.

# **Parameters**

exec	The executor, on which the message buffer is located.
recv_buffer	the data to reduce and the reduced result
count	the number of elements to reduce
operation	the reduce operation. See @MPI_Op

# **Template Parameters**

ReduceType	the type of the data to reduce. Has to be a type which has a specialization of type_impl that
	defines its MPI_Datatype.

#### Returns

the request handle for the call

References gko::experimental::mpi::request::get(), and get().

# 46.33.3.15 i\_all\_to\_all() [1/2]

(Non-blocking) Communicate data from all ranks to all other ranks (MPI\_lalltoall).

See MPI documentation for more details.

#### **Parameters**

exec	The executor, on which the message buffers are located.
send_buffer	the buffer to send
send_count	the number of elements to send
recv_buffer	the buffer to receive
recv_count	the number of elements to receive

# **Template Parameters**

SendType	the type of the data to send. Has to be a type which has a specialization of type_impl that defines its MPI_Datatype.
RecvType	the type of the data to receive. The same restrictions as for SendType apply.

#### Returns

the request handle for the call

References gko::experimental::mpi::request::get(), and get().

# 46.33.3.16 i\_all\_to\_all() [2/2]

(In-place, Non-blocking) Communicate data from all ranks to all other ranks in place (MPI\_Ialltoall).

See MPI documentation for more details.

#### **Parameters**

exec	The executor, on which the message buffer is located.
buffer	the buffer to send and the buffer receive
recv_count	the number of elements to receive
comm	the communicator

# **Template Parameters**

RecvType	the type of the data to receive. Has to be a type which has a specialization of type_impl that	1
	defines its MPI_Datatype.	

#### Returns

the request handle for the call

#### Note

This overload uses MPI\_IN\_PLACE and the source and destination buffers are the same.

References gko::experimental::mpi::request::get(), and get().

# 46.33.3.17 i\_all\_to\_all\_v() [1/2]

Communicate data from all ranks to all other ranks with offsets (MPI\_lalltoallv).

See MPI documentation for more details.

# Parameters

exec	The executor, on which the message buffers are located.
send_buffer	the buffer to send
send_count	the number of elements to send
send_offsets	the offsets for the send buffer
recv_buffer	the buffer to gather into
recv_count	the number of elements to receive
recv_offsets	the offsets for the recv buffer

# **Template Parameters**

SendType	the type of the data to send. Has to be a type which has a specialization of type_impl that defines its MPI_Datatype.	
RecvType	the type of the data to receive. The same restrictions as for SendType apply.	

# Returns

the request handle for the call

References i\_all\_to\_all\_v().

# 46.33.3.18 i\_all\_to\_all\_v() [2/2]

Communicate data from all ranks to all other ranks with offsets (MPI\_lalltoallv).

See MPI documentation for more details.

#### **Parameters**

exec	The executor, on which the message buffers are located.
send_buffer	the buffer to send
send_count	the number of elements to send
send_offsets	the offsets for the send buffer
send_type	the MPI_Datatype for the send buffer
recv_buffer	the buffer to gather into
recv_count	the number of elements to receive
recv_offsets	the offsets for the recv buffer
recv_type	the MPI_Datatype for the recv buffer

# Returns

the request handle for the call

Note

This overload allows specifying the MPI\_Datatype for both the send and received data.

References gko::experimental::mpi::request::get(), and get().

Referenced by i\_all\_to\_all\_v().

### 46.33.3.19 i broadcast()

(Non-blocking) Broadcast data from calling process to all ranks in the communicator

### **Parameters**

exec	The executor, on which the message buffer is located.
buffer	the buffer to broadcsat
count	the number of elements to broadcast
root_rank	the rank to broadcast from

# **Template Parameters**

BroadcastType	the type of the data to broadcast. Has to be a type which has a specialization of type_impl
	that defines its MPI_Datatype.

### Returns

the request handle for the call

References gko::experimental::mpi::request::get(), and get().

### 46.33.3.20 i\_gather()

(Non-blocking) Gather data onto the root rank from all ranks in the communicator.

### **Parameters**

exec	The executor, on which the message buffers are located.
send_buffer	the buffer to gather from
send_count	the number of elements to send
recv_buffer	the buffer to gather into
recv_count	the number of elements to receive
root_rank	the rank to gather into

# **Template Parameters**

SendType	the type of the data to send. Has to be a type which has a specialization of type_impl that defines its MPI_Datatype.
RecvType	the type of the data to receive. The same restrictions as for SendType apply.

### Returns

the request handle for the call

References gko::experimental::mpi::request::get(), and get().

# 46.33.3.21 i\_gather\_v()

(Non-blocking) Gather data onto the root rank from all ranks in the communicator with offsets.

### **Parameters**

exec	The executor, on which the message buffers are located.
send_buffer	the buffer to gather from
send_count	the number of elements to send
recv_buffer	the buffer to gather into
recv_count	the number of elements to receive
displacements	the offsets for the buffer
root_rank	the rank to gather into

# **Template Parameters**

SendType	the type of the data to send. Has to be a type which has a specialization of type_impl that defines its MPI_Datatype.	]
RecvType	the type of the data to receive. The same restrictions as for SendType apply.	1

# Returns

the request handle for the call

References gko::experimental::mpi::request::get(), and get().

# 46.33.3.22 i\_recv()

Receive (Non-blocking, Immediate return) data from source rank.

### **Parameters**

exec	The executor, on which the message buffer is located.
recv_buffer	the buffer to send
recv_count	the number of elements to receive
source_rank	the rank to receive the data from
recv_tag	the tag for the recv call

# **Template Parameters**

RecvType	the type of the data to receive. Has to be a type which has a specialization of type_impl that
	defines its MPI_Datatype.

# Returns

the request handle for the recv call

References gko::experimental::mpi::request::get(), and get().

### 46.33.3.23 i\_reduce()

```
template<typename ReduceType >
request gko::experimental::mpi::communicator::i_reduce (
    std::shared_ptr< const Executor > exec,
    const ReduceType * send_buffer,
    ReduceType * recv_buffer,
    int count,
    MPI_Op operation,
    int root_rank ) const [inline]
```

(Non-blocking) Reduce data into root from all calling processes on the same communicator.

### **Parameters**

exec	The executor, on which the message buffer is located.
send_buffer	the buffer to reduce
recv_buffer	the reduced result
count	the number of elements to reduce
operation	the MPI_Op type reduce operation.

# **Template Parameters**

ReduceType	the type of the data to reduce. Has to be a type which has a specialization of type_impl that
	defines its MPI_Datatype.

# Returns

the request handle for the call

References gko::experimental::mpi::request::get(), and get().

# 46.33.3.24 i\_scan()

Does a scan operation with the given operator.

(MPI\_Iscan). See MPI documentation for more details.

# **Parameters**

exec	The executor, on which the message buffers are located.
send_buffer	the buffer to scan from
recv_buffer	the result buffer
recv_count	the number of elements to scan
operation	the operation type to be used for the scan. See @MPI_Op

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# **Template Parameters**

ScanType	the type of the data to scan. Has to be a type which has a specialization of type_impl that defines	
	its MPI_Datatype.	

# Returns

the request handle for the call

References gko::experimental::mpi::request::get(), and get().

# 46.33.3.25 i\_scatter()

(Non-blocking) Scatter data from root rank to all ranks in the communicator.

# **Parameters**

exec	The executor, on which the message buffers are located.
send_buffer	the buffer to gather from
send_count	the number of elements to send
recv_buffer	the buffer to gather into
recv count	the number of elements to receive

# **Template Parameters**

SendType	the type of the data to send. Has to be a type which has a specialization of type_impl that defines its MPI_Datatype.
RecvType	the type of the data to receive. The same restrictions as for SendType apply.

# Returns

the request handle for the call

References gko::experimental::mpi::request::get(), and get().

# 46.33.3.26 i\_scatter\_v()

(Non-blocking) Scatter data from root rank to all ranks in the communicator with offsets.

### **Parameters**

exec	The executor, on which the message buffers are located.
send_buffer	the buffer to gather from
send_count	the number of elements to send
recv_buffer	the buffer to gather into
recv_count	the number of elements to receive
displacements	the offsets for the buffer
comm	the communicator

# **Template Parameters**

SendType	the type of the data to send. Has to be a type which has a specialization of type_impl that defines its MPI_Datatype.	
RecvType	the type of the data to receive. The same restrictions as for SendType apply.	

# Returns

the request handle for the call

References gko::experimental::mpi::request::get(), and get().

# 46.33.3.27 i\_send()

Send (Non-blocking, Immediate return) data from calling process to destination rank.

### **Parameters**

exec	The executor, on which the message buffer is located.
send_buffer	the buffer to send
send_count	the number of elements to send
destination_rank	the rank to send the data to
send_tag	the tag for the send call

# **Template Parameters**

SendType	the type of the data to send. Has to be a type which has a specialization of type_impl that defines	]
	its MPI_Datatype.	

### Returns

the request handle for the send call

References gko::experimental::mpi::request::get(), and get().

# 46.33.3.28 node\_local\_rank()

```
int gko::experimental::mpi::communicator::node_local_rank ( ) const [inline]
```

Return the node local rank of the calling process in the communicator.

# Returns

the node local rank

# 46.33.3.29 operator"!=()

Compare two communicator objects for non-equality.

# Returns

if the two comm objects are not equal

### 46.33.3.30 operator==()

Compare two communicator objects for equality.

# Returns

if the two comm objects are equal

# 46.33.3.31 rank()

```
int gko::experimental::mpi::communicator::rank ( ) const [inline]
```

Return the rank of the calling process in the communicator.

### Returns

the rank

# 46.33.3.32 recv()

Receive data from source rank.

### **Parameters**

exec	The executor, on which the message buffer is located.
recv_buffer	the buffer to receive
recv_count	the number of elements to receive
source_rank	the rank to receive the data from
recv_tag	the tag for the recv call

# **Template Parameters**

RecvType	the type of the data to receive. Has to be a type which has a specialization of type_impl that
	defines its MPI_Datatype.

### Returns

the status of completion of this call

References gko::experimental::mpi::status::get(), and get().

# 46.33.3.33 reduce()

```
template<typename ReduceType >
void gko::experimental::mpi::communicator::reduce (
    std::shared_ptr< const Executor > exec,
    const ReduceType * send_buffer,
    ReduceType * recv_buffer,
    int count,
    MPI_Op operation,
    int root_rank ) const [inline]
```

Reduce data into root from all calling processes on the same communicator.

### **Parameters**

exec	The executor, on which the message buffer is located.
send_buffer	the buffer to reduce
recv_buffer	the reduced result
count	the number of elements to reduce
operation	the MPI_Op type reduce operation.

### **Template Parameters**

ReduceType	the type of the data to reduce. Has to be a type which has a specialization of type_impl that
	defines its MPI_Datatype.

References get().

### 46.33.3.34 scan()

```
template<typename ScanType >
void gko::experimental::mpi::communicator::scan (
    std::shared_ptr< const Executor > exec,
    const ScanType * send_buffer,
    ScanType * recv_buffer,
    int count,
    MPI_Op operation ) const [inline]
```

Does a scan operation with the given operator.

(MPI\_Scan). See MPI documentation for more details.

### **Parameters**

exec	The executor, on which the message buffers are located.
send_buffer	the buffer to scan from
recv_buffer	the result buffer
recv_count	the number of elements to scan
operation	the operation type to be used for the scan. See @MPI_Op

# **Template Parameters**

ScanType	the type of the data to scan. Has to be a type which has a specialization of type_impl that defines	1
	its MPI_Datatype.	

References get().

# 46.33.3.35 scatter()

Scatter data from root rank to all ranks in the communicator.

# **Parameters**

exec	The executor, on which the message buffers are located.
send_buffer	the buffer to gather from
send_count	the number of elements to send
recv_buffer	the buffer to gather into
recv_count	the number of elements to receive

# **Template Parameters**

SendType	the type of the data to send. Has to be a type which has a specialization of type_impl that defines its MPI_Datatype.
RecvType	the type of the data to receive. The same restrictions as for SendType apply.

References get().

# 46.33.3.36 scatter\_v()

Scatter data from root rank to all ranks in the communicator with offsets.

### **Parameters**

exec	The executor, on which the message buffers are located.
send_buffer	the buffer to gather from
send_count	the number of elements to send
recv_buffer	the buffer to gather into
recv_count	the number of elements to receive
displacements	the offsets for the buffer
comm	the communicator

# **Template Parameters**

SendType	the type of the data to send. Has to be a type which has a specialization of type_impl that defines its MPI_Datatype.	
RecvType	the type of the data to receive. The same restrictions as for SendType apply.	

References get().

# 46.33.3.37 send()

```
template<typename SendType >
void gko::experimental::mpi::communicator::send (
    std::shared_ptr< const Executor > exec,
    const SendType * send_buffer,
    const int send_count,
    const int destination_rank,
    const int send_tag ) const [inline]
```

Send (Blocking) data from calling process to destination rank.

### **Parameters**

exec	The executor, on which the message buffer is located.
send_buffer	the buffer to send
send_count	the number of elements to send
destination_rank	the rank to send the data to
_send_tag	the tag for the send call

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# **Template Parameters**

SendType

the type of the data to send. Has to be a type which has a specialization of type\_impl that defines its MPI\_Datatype.

References get().

# 46.33.3.38 size()

```
int gko::experimental::mpi::communicator::size ( ) const [inline]
```

Return the size of the communicator (number of ranks).

Returns

the size

# 46.33.3.39 synchronize()

```
void gko::experimental::mpi::communicator::synchronize ( ) const [inline]
```

This function is used to synchronize the ranks in the communicator.

Calls MPI\_Barrier

References get().

The documentation for this class was generated from the following file:

· ginkgo/core/base/mpi.hpp

# 46.34 gko::Composition < ValueType > Class Template Reference

The Composition class can be used to compose linear operators op1, op2, ..., opn and obtain the operator op1 \* op2 \* ...

#include <ginkgo/core/base/composition.hpp>

### **Public Member Functions**

- const std::vector< std::shared\_ptr< const LinOp > > & get\_operators () const noexcept Returns a list of operators of the composition.
- std::unique\_ptr< LinOp > transpose () const override

Returns a LinOp representing the transpose of the Transposable object.

• std::unique\_ptr< LinOp > conj\_transpose () const override

Returns a LinOp representing the conjugate transpose of the Transposable object.

• Composition & operator= (const Composition &)

Copy-assigns a Composition.

• Composition & operator= (Composition &&)

Move-assigns a Composition.

• Composition (const Composition &)

Copy-constructs a Composition.

Composition (Composition &&)

Move-constructs a Composition.

# 46.34.1 Detailed Description

```
template<typename ValueType = default_precision> class gko::Composition< ValueType >
```

The Composition class can be used to compose linear operators op1, op2, ..., opn and obtain the operator op1 \* op2 \* ...

• opn.

All LinOps of the Composition must operate on Dense inputs. For an operator  $op_k$  that require an initial guess for their apply, Composition provides either

- the output of the previous op\_{k+1}->apply if op\_k has square dimension
- zero if op\_k is rectangular as an initial guess.

Composition ensures that all LinOps passed to its constructor use the same executor, and if not, copies the operators to the executor of the first operator.

# **Template Parameters**

ValueType	precision of input and result vectors

# 46.34.2 Constructor & Destructor Documentation

### 46.34.2.1 Composition() [1/2]

Copy-constructs a Composition.

This inherits the executor of the input Composition and all of its operators with shared ownership.

### 46.34.2.2 Composition() [2/2]

Move-constructs a Composition.

This inherits the executor of the input Composition and all of its operators. The moved-from object is empty (0x0 LinOp without operators) afterwards.

### 46.34.3 Member Function Documentation

### 46.34.3.1 conj\_transpose()

```
template<typename ValueType = default_precision>
std::unique_ptr<LinOp> gko::Composition< ValueType >::conj_transpose ( ) const [override],
[virtual]
```

Returns a LinOp representing the conjugate transpose of the Transposable object.

Returns

a pointer to the new conjugate transposed object

Implements gko::Transposable.

### 46.34.3.2 get\_operators()

```
template<typename ValueType = default_precision>
const std::vector<std::shared_ptr<const LinOp> >& gko::Composition< ValueType >::get_
operators ( ) const [inline], [noexcept]
```

Returns a list of operators of the composition.

Returns

```
a list of operators
```

### 46.34.3.3 operator=() [1/2]

Move-assigns a Composition.

The executor is not modified, and the wrapped LinOps are only being cloned if they are on a different executor, otherwise they share ownership. The moved-from object is empty (0x0 LinOp without operators) afterwards.

### 46.34.3.4 operator=() [2/2]

Copy-assigns a Composition.

The executor is not modified, and the wrapped LinOps are only being cloned if they are on a different executor.

### 46.34.3.5 transpose()

```
template<typename ValueType = default_precision>
std::unique_ptr<LinOp> gko::Composition< ValueType >::transpose ( ) const [override], [virtual]
```

Returns a LinOp representing the transpose of the Transposable object.

### Returns

a pointer to the new transposed object

Implements gko::Transposable.

The documentation for this class was generated from the following file:

ginkgo/core/base/composition.hpp

# 46.35 gko::experimental::mpi::contiguous type Class Reference

A move-only wrapper for a contiguous MPI\_Datatype.

```
#include <ginkgo/core/base/mpi.hpp>
```

# **Public Member Functions**

• contiguous\_type (int count, MPI\_Datatype old\_type)

Constructs a wrapper for a contiguous MPI\_Datatype.

contiguous\_type ()

Constructs empty wrapper with MPI\_DATATYPE\_NULL.

• contiguous\_type (const contiguous\_type &)=delete

Disallow copying of wrapper type.

contiguous\_type & operator= (const contiguous\_type &)=delete

Disallow copying of wrapper type.

• contiguous\_type (contiguous\_type &&other) noexcept

Move constructor, leaves other with MPI\_DATATYPE\_NULL.

contiguous\_type & operator= (contiguous\_type &&other) noexcept

Move assignment, leaves other with MPI\_DATATYPE\_NULL.

 ~contiguous\_type ()

Destructs object by freeing wrapped MPI\_Datatype.

• MPI\_Datatype get () const

Access the underlying MPI\_Datatype.

# 46.35.1 Detailed Description

A move-only wrapper for a contiguous MPI\_Datatype.

The underlying MPI\_Datatype is automatically created and committed when an object of this type is constructed, and freed when it is destructed.

# 46.35.2 Constructor & Destructor Documentation

# 46.35.2.1 contiguous\_type() [1/2]

Constructs a wrapper for a contiguous MPI\_Datatype.

# Parameters

count	the number of old_type elements the new datatype contains.
old_type	the MPI_Datatype that is contained.

### 46.35.2.2 contiguous\_type() [2/2]

```
\verb"gko::experimental::mpi::contiguous_type::contiguous_type" (
```

```
contiguous_type && other ) [inline], [noexcept]
```

Move constructor, leaves other with MPI\_DATATYPE\_NULL.

### **Parameters**

```
other to be moved from object.
```

### 46.35.3 Member Function Documentation

### 46.35.3.1 get()

```
MPI_Datatype gko::experimental::mpi::contiguous_type::get ( ) const [inline]
```

Access the underlying MPI Datatype.

### Returns

the underlying MPI\_Datatype.

# 46.35.3.2 operator=()

Move assignment, leaves other with MPI\_DATATYPE\_NULL.

### **Parameters**

other	to be moved from object.
-------	--------------------------

### Returns

this object.

The documentation for this class was generated from the following file:

• ginkgo/core/base/mpi.hpp

# 46.36 gko::log::Convergence < ValueType > Class Template Reference

Convergence is a Logger which logs data strictly from the criterion\_check\_completed event.

#include <ginkgo/core/log/convergence.hpp>

### **Public Member Functions**

• bool has\_converged () const noexcept

Returns true if the solver has converged.

• void reset\_convergence\_status ()

Resets the convergence status to false.

• const size\_type & get\_num\_iterations () const noexcept

Returns the number of iterations.

const LinOp \* get\_residual () const noexcept

Returns the residual.

const LinOp \* get residual norm () const noexcept

Returns the residual norm.

• const LinOp \* get\_implicit\_sq\_resnorm () const noexcept

Returns the implicit squared residual norm.

### Static Public Member Functions

 static std::unique\_ptr< Convergence > create (std::shared\_ptr< const Executor >, const mask\_type &enabled\_events=Logger::criterion\_events\_mask|Logger::iteration\_complete\_mask)

Creates a convergence logger.

static std::unique\_ptr< Convergence > create (const mask\_type &enabled\_events=Logger::criterion\_
 events\_mask|Logger::iteration\_complete\_mask)

Creates a convergence logger.

# 46.36.1 Detailed Description

```
template < typename ValueType = default_precision > class gko::log::Convergence < ValueType >
```

Convergence is a Logger which logs data strictly from the criterion\_check\_completed event.

The purpose of this logger is to give a simple access to standard data generated by the solver once it has stopped with minimal overhead.

This logger also computes the residual norm from the residual when the residual norm was not available. This can add some slight overhead.

### 46.36.2 Member Function Documentation

### 46.36.2.1 create() [1/2]

Creates a convergence logger.

This dynamically allocates the memory, constructs the object and returns an std::unique\_ptr to this object.

### **Parameters**

enabled events	the events enabled for this logger. By default all events.

### Returns

an std::unique\_ptr to the the constructed object

# 46.36.2.2 create() [2/2]

Creates a convergence logger.

This dynamically allocates the memory, constructs the object and returns an std::unique\_ptr to this object.

### **Parameters**

exec	the executor
enabled_events	the events enabled for this logger. By default all events.

### Returns

an std::unique\_ptr to the the constructed object

# 46.36.2.3 get\_implicit\_sq\_resnorm()

```
template<typename ValueType = default_precision>
const LinOp* gko::log::Convergence< ValueType >::get_implicit_sq_resnorm ( ) const [inline],
[noexcept]
```

Returns the implicit squared residual norm.

### Returns

the implicit squared residual norm

# 46.36.2.4 get\_num\_iterations()

```
template<typename ValueType = default_precision>
const size_type& gko::log::Convergence< ValueType >::get_num_iterations ( ) const [inline],
[noexcept]
```

Returns the number of iterations.

Returns

the number of iterations

### 46.36.2.5 get\_residual()

```
template<typename ValueType = default_precision>
const LinOp* gko::log::Convergence< ValueType >::get_residual ( ) const [inline], [noexcept]
```

Returns the residual.

Returns

the residual

# 46.36.2.6 get\_residual\_norm()

```
template<typename ValueType = default_precision>
const LinOp* gko::log::Convergence< ValueType >::get_residual_norm ( ) const [inline], [noexcept]
```

Returns the residual norm.

Returns

the residual norm

# 46.36.2.7 has\_converged()

```
template<typename ValueType = default_precision>
bool gko::log::Convergence< ValueType >::has_converged ( ) const [inline], [noexcept]
```

Returns true if the solver has converged.

Returns

the bool flag for convergence status

The documentation for this class was generated from the following file:

• ginkgo/core/log/convergence.hpp

# 46.37 gko::ConvertibleTo< ResultType > Class Template Reference

ConvertibleTo interface is used to mark that the implementer can be converted to the object of ResultType.

```
#include <ginkgo/core/base/polymorphic_object.hpp>
```

### **Public Member Functions**

- virtual void convert\_to (result\_type \*result) const =0
   Converts the implementer to an object of type result\_type.
- virtual void move\_to (result\_type \*result)=0

Converts the implementer to an object of type result\_type by moving data from this object.

# 46.37.1 Detailed Description

```
template<typename ResultType> class gko::ConvertibleTo< ResultType >
```

ConvertibleTo interface is used to mark that the implementer can be converted to the object of ResultType.

This interface is used to enable conversions between polymorphic objects. To mark that an object of type U can be converted to an object of type V, U should implement Convertible To < V>. Then, the implementation of PolymorphicObject::copy\_from automatically generated by EnablePolymorphicObject mixin will use RTTI to figure out that U implements the interface and convert it using the convert\_to / move\_to methods of the interface.

### As an example, the following function:

```
{c++}
void my_function(const U *u, V *v) {
  v->copy_from(u);
}
```

will convert object u to object v by checking that u can be dynamically casted to ConvertibleTo<V>: convert\_to(V\*)` to do the actual conversion.

In case u is passed as a unique\_ptr, call to <code>convert\_to</code> will be replaced by a call to <code>move\_to</code> and trigger move semantics.

### **Template Parameters**

ResultType the type to which the implementer can be converted to, has to be a subclass of PolymorphicObject

### 46.37.2 Member Function Documentation

### 46.37.2.1 convert\_to()

Converts the implementer to an object of type result\_type.

#### **Parameters**

```
result the object used to store the result of the conversion
```

Implemented in gko::EnablePolymorphicAssignment < ConcreteType, ResultType >, gko::EnablePolymorphicAssignment < Factoriza gko::EnablePolymorphicAssignment< Lu< ValueType, IndexType > >, gko::EnablePolymorphicAssignment< Isai< IsaiType, Value gko::EnablePolymorphicAssignment< SparsityCsr< ValueType, IndexType > >, gko::EnablePolymorphicAssignment< Vector< ValueType gko::EnablePolymorphicAssignment< Mc64< ValueType, IndexType > >, gko::EnablePolymorphicAssignment< Diagonal< ValueType gko::EnablePolymorphicAssignment< Pgm< ValueType, IndexType > >, gko::EnablePolymorphicAssignment< Dense< ValueType gko::EnablePolymorphicAssignment< UpperTrs< ValueType, IndexType > >, gko::EnablePolymorphicAssignment< Amd< IndexType gko::EnablePolymorphicAssignment< Matrix< ValueType, LocalIndexType, GlobalIndexType > , gko::EnablePolymorphicAssignment gko::EnablePolymorphicAssignment< Identity< ValueType > >, gko::EnablePolymorphicAssignment< ConcreteLinOp >, gko::EnablePolymorphicAssignment< Rcm< IndexType >>, gko::EnablePolymorphicAssignment< Fft3 >, gko::EnablePolymorphicAssignment< Partition< LocalIndexType, GlobalIndexType > >, gko::EnablePolymorphicAssignment< Com gko::EnablePolymorphicAssignment< ConcreteBatchLinOp >, gko::EnablePolymorphicAssignment< RowGatherer< IndexType > 3 gko::EnablePolymorphicAssignment< Cholesky< ValueType, IndexType > >, gko::EnablePolymorphicAssignment< Fft2 >, gko::EnablePolymorphicAssignment< FixedCoarsening< ValueType, IndexType > >, gko::EnablePolymorphicAssignment< Fbcsr< gko::EnablePolymorphicAssignment< LowerTrs< ValueType, IndexType > >, gko::EnablePolymorphicAssignment< Combination< gko::EnablePolymorphicAssignment< Bicgstab< ValueType > >, gko::EnablePolymorphicAssignment< MultiVector< ValueType > gko::EnablePolymorphicAssignment< Multigrid >, gko::EnablePolymorphicAssignment< Gmres< ValueType >>, gko::EnablePolymorphicAssignment< CbGmres< ValueType > >, gko::EnablePolymorphicAssignment< Csr< ValueType, IndexType gko::EnablePolymorphicAssignment< ConcreteSolver >, gko::EnablePolymorphicAssignment< Ir< ValueType > >, gko::EnablePolymorphicAssignment< Coo< ValueType, IndexType > >, gko::EnablePolymorphicAssignment< Fcg< ValueType > gko::EnablePolymorphicAssignment< Rcm< ValueType, IndexType > >, gko::EnablePolymorphicAssignment< Fft >, gko::EnablePolymorphicAssignment< BlockOperator >, gko::EnablePolymorphicAssignment< Direct< ValueType, IndexType >>, gko::EnablePolymorphicAssignment< Idr< ValueType > >, gko::EnablePolymorphicAssignment< ConcreteFactory >, gko::EnablePolymorphicAssignment< Cgs< ValueType > >, gko::EnablePolymorphicAssignment< Ell< ValueType, IndexType > > gko::EnablePolymorphicAssignment< Ilu< LSolverType, USolverType, ReverseApply, IndexType >>, gko::EnablePolymorphicAssignment gko::EnablePolymorphicAssignment< Permutation< IndexType > >, gko::EnablePolymorphicAssignment< ScaledPermutation< Va gko::EnablePolymorphicAssignment< Jacobi< ValueType, IndexType > >, gko::EnablePolymorphicAssignment< Gcr< ValueType gko::EnablePolymorphicAssignment< Schwarz< ValueType, LocalIndexType, GlobalIndexType > >, gko::EnablePolymorphicAssign gko::EnablePolymorphicAssignment< ScaledReordered< ValueType, IndexType > >, gko::EnablePolymorphicAssignment< Sellp< gko::EnablePolymorphicAssignment< Bicg< ValueType > >, gko::EnablePolymorphicAssignment< Perturbation< ValueType > >, and gko::preconditioner::Jacobi < ValueType, IndexType >.

### 46.37.2.2 move\_to()

Converts the implementer to an object of type result\_type by moving data from this object.

This method is used when the implementer is a temporary object, and move semantics can be used.

# Parameters

result	the object used to emplace the result of the conversion

Note

ConvertibleTo::move\_to can be implemented by simply calling ConvertibleTo::convert\_to. However, this operation can often be optimized by exploiting the fact that implementer's data can be moved to the result.

Implemented in gko::EnablePolymorphicAssignment < ConcreteType, ResultType >, gko::EnablePolymorphicAssignment < Factoriza gko::EnablePolymorphicAssignment< Lu< ValueType, IndexType > , gko::EnablePolymorphicAssignment< Isai< IsaiType, Value  ${\tt gko::} Enable {\tt PolymorphicAssignment} < {\tt SparsityCsr} < {\tt ValueType}, {\tt IndexType} >>, {\tt gko::} Enable {\tt PolymorphicAssignment} < {\tt Vector} < {\tt ValueType}, {\tt IndexType} >>, {\tt gko::} {\tt EnablePolymorphicAssignment} < {\tt Vector} < {\tt ValueType}, {\tt IndexType} >>, {\tt gko::} {\tt EnablePolymorphicAssignment} < {\tt Vector} < {\tt ValueType}, {\tt IndexType} >>, {\tt gko::} {\tt EnablePolymorphicAssignment} < {\tt Vector} < {\tt ValueType}, {\tt IndexType} >>, {\tt gko::} {\tt EnablePolymorphicAssignment} < {\tt Vector} < {\tt ValueType}, {\tt IndexType} >>, {\tt gko::} {\tt EnablePolymorphicAssignment} < {\tt Vector} < {\tt ValueType}, {\tt IndexType} >>, {\tt gko::} {\tt EnablePolymorphicAssignment} < {\tt Vector} < {\tt ValueType}, {\tt IndexType} >>, {\tt gko::} {\tt EnablePolymorphicAssignment} < {\tt Vector} < {\tt ValueType}, {\tt IndexType} >>, {\tt gko::} {\tt EnablePolymorphicAssignment} < {\tt Vector} < {\tt ValueType}, {\tt IndexType} >>, {\tt gko::} {\tt EnablePolymorphicAssignment} < {\tt Vector} < {\tt ValueType}, {\tt IndexType} >>, {\tt gko::} {\tt EnablePolymorphicAssignment} < {\tt Vector} < {\tt ValueType}, {\tt IndexType} >>, {\tt gko::} {\tt EnablePolymorphicAssignment} < {\tt Vector} < {\tt ValueType}, {\tt IndexType} >>, {\tt gko::} {\tt EnablePolymorphicAssignment} < {\tt Vector} < {\tt ValueType}, {\tt IndexType} >>, {\tt gko::} {\tt EnablePolymorphicAssignment} < {\tt Vector} < {\tt ValueType}, {\tt ValueType}, {\tt IndexType} >>, {\tt gko::} {\tt EnablePolymorphicAssignment} < {\tt Vector} < {\tt ValueType}, {\tt ValueType},$ gko::EnablePolymorphicAssignment< Mc64< ValueType, IndexType > >, gko::EnablePolymorphicAssignment< Diagonal< ValueType gko::EnablePolymorphicAssignment< Pgm< ValueType, IndexType > >, gko::EnablePolymorphicAssignment< Dense< ValueType gko::EnablePolymorphicAssignment< UpperTrs< ValueType, IndexType > >, gko::EnablePolymorphicAssignment< Amd< IndexType gko::EnablePolymorphicAssignment< Matrix< ValueType, LocalIndexType, GlobalIndexType > >, gko::EnablePolymorphicAssignment gko::EnablePolymorphicAssignment< Identity< ValueType > >, gko::EnablePolymorphicAssignment< ConcreteLinOp >, gko::EnablePolymorphicAssignment< Rcm< IndexType >>, gko::EnablePolymorphicAssignment< Fft3 >, gko::EnablePolymorphicAssignment< Partition< LocalIndexType, GlobalIndexType > >, gko::EnablePolymorphicAssignment< Con gko::EnablePolymorphicAssignment< ConcreteBatchLinOp >, gko::EnablePolymorphicAssignment< RowGatherer< IndexType > 3 gko::EnablePolymorphicAssignment< Cholesky< ValueType, IndexType > >, gko::EnablePolymorphicAssignment< Fft2 >, gko::EnablePolymorphicAssignment< FixedCoarsening< ValueType, IndexType > >, gko::EnablePolymorphicAssignment< Fbcsr< gko::EnablePolymorphicAssignment< LowerTrs< ValueType, IndexType > >, gko::EnablePolymorphicAssignment< Combination< gko::EnablePolymorphicAssignment< Bicgstab< ValueType > >, gko::EnablePolymorphicAssignment< MultiVector< ValueType > gko::EnablePolymorphicAssignment< Multigrid >, gko::EnablePolymorphicAssignment< Gmres< ValueType > >, gko::EnablePolymorphicAssignment< CbGmres< ValueType > >, gko::EnablePolymorphicAssignment< Csr< ValueType, IndexType gko::EnablePolymorphicAssignment< ConcreteSolver >, gko::EnablePolymorphicAssignment< Ir< ValueType > >, gko::EnablePolymorphicAssignment< Coo< ValueType, IndexType > >, gko::EnablePolymorphicAssignment< Fcg< ValueType > gko::EnablePolymorphicAssignment< Rcm< ValueType, IndexType > >, gko::EnablePolymorphicAssignment< Fft >, gko::EnablePolymorphicAssignment< BlockOperator >, gko::EnablePolymorphicAssignment< Direct< ValueType, IndexType >>,  ${\tt gko::} Enable {\tt PolymorphicAssignment} < {\tt Idr} < {\tt ValueType} >>, {\tt gko::} Enable {\tt PolymorphicAssignment} < {\tt ConcreteFactory} >, {\tt gko::} Enable {\tt PolymorphicAssignment} < {\tt ConcreteFactory} >, {\tt gko::} Enable {\tt PolymorphicAssignment} < {\tt ConcreteFactory} >, {\tt gko::} Enable {\tt PolymorphicAssignment} < {\tt ConcreteFactory} >, {\tt gko::} Enable {\tt PolymorphicAssignment} < {\tt ConcreteFactory} >, {\tt gko::} Enable {\tt PolymorphicAssignment} < {\tt ConcreteFactory} >, {\tt gko::} Enable {\tt PolymorphicAssignment} < {\tt ConcreteFactory} >, {\tt gko::} Enable {\tt PolymorphicAssignment} < {\tt ConcreteFactory} >, {\tt gko::} Enable {\tt PolymorphicAssignment} < {\tt ConcreteFactory} >, {\tt gko::} Enable {\tt PolymorphicAssignment} < {\tt ConcreteFactory} >, {\tt gko::} Enable {\tt PolymorphicAssignment} < {\tt ConcreteFactory} >, {\tt gko::} Enable {\tt PolymorphicAssignment} < {\tt ConcreteFactory} >, {\tt gko::} Enable {\tt PolymorphicAssignment} < {\tt ConcreteFactory} >, {\tt gko::} Enable {\tt PolymorphicAssignment} < {\tt ConcreteFactory} >, {\tt gko::} Enable {\tt gko::} Enable {\tt ConcreteFactory} >, {\tt gko::} Enable {\tt gko::} E$ gko::EnablePolymorphicAssignment< Cgs< ValueType > >, gko::EnablePolymorphicAssignment< Ell< ValueType, IndexType > > gko::EnablePolymorphicAssignment< Ilu< LSolverType, USolverType, ReverseApply, IndexType >>, gko::EnablePolymorphicAssignment gko::EnablePolymorphicAssignment< Permutation< IndexType > >, gko::EnablePolymorphicAssignment< ScaledPermutation< Va gko::EnablePolymorphicAssignment< Jacobi< ValueType, IndexType > >, gko::EnablePolymorphicAssignment< Gcr< ValueType  ${\sf gko::} Enable {\sf PolymorphicAssignment} {\sf < Schwarz} {\sf < Value Type, Local Index Type, Global Index Type} >>, {\sf gko::} Enable {\sf PolymorphicAssignment} {\sf < Schwarz} {\sf < Value Type, Local Index Type, Global Index Type} >>, {\sf gko::} {\sf Enable PolymorphicAssignment} {\sf < Schwarz} {\sf < Value Type, Local Index Type, Global Index Type} >>, {\sf gko::} {\sf Enable PolymorphicAssignment} {\sf < Schwarz} {\sf < Value Type, Local Index Type, Global Index Type} >>, {\sf gko::} {\sf Enable PolymorphicAssignment} {\sf < Schwarz} {\sf < Value Type, Global Index Type, Global Index Type} >>, {\sf gko::} {\sf Enable PolymorphicAssignment} {\sf < Schwarz} {\sf < Value Type, Global Index Type, Global Index Type} >>, {\sf gko::} {\sf Enable PolymorphicAssignment} {\sf < Schwarz} {\sf < Value Type, Global Index Type, Global Index Type} >>, {\sf gko::} {\sf Enable PolymorphicAssignment} {\sf < Schwarz} {\sf < Value Type, Global Index Type, Global Index Type} >>, {\sf gko::} {\sf < Color Fyremant} {\sf < Color Fyreman$ gko::EnablePolymorphicAssignment< ScaledReordered< ValueType, IndexType > >, gko::EnablePolymorphicAssignment< Sellp< gko::EnablePolymorphicAssignment< Bicg< ValueType > >, gko::EnablePolymorphicAssignment< Perturbation< ValueType > >, and gko::preconditioner::Jacobi < ValueType, IndexType >.

The documentation for this class was generated from the following file:

ginkgo/core/base/polymorphic\_object.hpp

# 46.38 gko::matrix::Coo< ValueType, IndexType > Class Template Reference

COO stores a matrix in the coordinate matrix format.

#include <ginkgo/core/matrix/coo.hpp>

# **Public Member Functions**

· void read (const mat data &data) override

Reads a matrix from a matrix\_data structure.

void read (const device\_mat\_data &data) override

Reads a matrix from a device\_matrix\_data structure.

void read (device\_mat\_data &&data) override

Reads a matrix from a device\_matrix\_data structure.

• void write (mat\_data &data) const override

Writes a matrix to a matrix\_data structure.

std::unique\_ptr< Diagonal</li>
 ValueType > > extract\_diagonal () const override

Extracts the diagonal entries of the matrix into a vector.

std::unique\_ptr< absolute\_type > compute\_absolute () const override

Gets the AbsoluteLinOp.

· void compute absolute inplace () override

Compute absolute inplace on each element.

value\_type \* get\_values () noexcept

Returns the values of the matrix.

• const value\_type \* get\_const\_values () const noexcept

Returns the values of the matrix.

index\_type \* get\_col\_idxs () noexcept

Returns the column indexes of the matrix.

const index\_type \* get\_const\_col\_idxs () const noexcept

Returns the column indexes of the matrix.

• index\_type \* get\_row\_idxs () noexcept

Returns the row indexes of the matrix.

- const index\_type \* get\_const\_row\_idxs () const noexcept
- size\_type get\_num\_stored\_elements () const noexcept

Returns the number of elements explicitly stored in the matrix.

LinOp \* apply2 (ptr\_param < const LinOp > b, ptr\_param < LinOp > x)

Applies Coo matrix axpy to a vector (or a sequence of vectors).

- const LinOp \* apply2 (ptr\_param < const LinOp > b, ptr\_param < LinOp > x) const
- LinOp \* apply2 (ptr\_param < const LinOp > alpha, ptr\_param < const LinOp > b, ptr\_param < LinOp > x)
   Performs the operation x = alpha \* Coo \* b + x.
- const LinOp \* apply2 (ptr\_param< const LinOp > alpha, ptr\_param< const LinOp > b, ptr\_param< LinOp > x) const

### **Static Public Member Functions**

static std::unique\_ptr< Coo > create (std::shared\_ptr< const Executor > exec, const dim< 2 > &size=dim< 2 > {}, size\_type num\_nonzeros={})

Creates an uninitialized COO matrix of the specified size.

 static std::unique\_ptr< Coo > create (std::shared\_ptr< const Executor > exec, const dim< 2 > &size, array< value\_type > values, array< index\_type > col\_idxs, array< index\_type > row\_idxs)

Creates a COO matrix from already allocated (and initialized) row index, column index and value arrays.

template<typename InputValueType , typename InputRowIndexType , typename InputRowIndexType >
 static std::unique\_ptr< Coo > create (std::shared\_ptr< const Executor > exec, const dim< 2 > &size,
 std::initializer\_list< InputValueType > values, std::initializer\_list< InputColumnIndexType > col\_idxs, std
 ::initializer list< InputRowIndexType > row idxs)

create(std::shared\_ptr<const Executor>,

static std::unique\_ptr< const Coo > create\_const (std::shared\_ptr< const Executor > exec, const dim< 2
 <ul>
 &size, gko::detail::const\_array\_view< ValueType > &&values, gko::detail::const\_array\_view< IndexType</li>
 &&col idxs, gko::detail::const\_array\_view< IndexType > &&row idxs)

Creates a constant (immutable) Coo matrix from a set of constant arrays.

# 46.38.1 Detailed Description

template<typename ValueType = default\_precision, typename IndexType = int32> class gko::matrix::Coo< ValueType, IndexType >

COO stores a matrix in the coordinate matrix format.

The nonzero elements are stored in an array row-wise (but not necessarily sorted by column index within a row). Two extra arrays contain the row and column indexes of each nonzero element of the matrix.

### **Template Parameters**

ValueType	precision of matrix elements
IndexType	precision of matrix indexes

### 46.38.2 Member Function Documentation

### 46.38.2.1 apply2() [1/4]

Performs the operation x = alpha \* Coo \* b + x.

### **Parameters**

alpha	scaling of the result of Coo * b
b	vector(s) on which the operator is applied
Х	output vector(s)

### Returns

this

# 46.38.2.2 apply2() [2/4]

### 46.38.2.3 apply2() [3/4]

Applies Coo matrix axpy to a vector (or a sequence of vectors).

Performs the operation x = Coo \* b + x

### **Parameters**

	the input vector(s) on which the operator is applied
X	the output vector(s) where the result is stored

### Returns

this

### 46.38.2.4 apply2() [4/4]

# 46.38.2.5 compute\_absolute()

```
template<typename ValueType = default_precision, typename IndexType = int32>
std::unique_ptr<absolute_type> gko::matrix::Coo< ValueType, IndexType >::compute_absolute ( )
const [override], [virtual]
```

Gets the AbsoluteLinOp.

### Returns

a pointer to the new absolute object

Implements gko::EnableAbsoluteComputation< remove\_complex< Coo< ValueType, IndexType >> >.

### 46.38.2.6 create() [1/3]

Creates a COO matrix from already allocated (and initialized) row index, column index and value arrays.

#### **Parameters**

exec	Executor associated to the matrix
size	size of the matrix
values	array of matrix values
col_idxs	array of column indexes
row_idxs	array of row pointers

### Note

If one of row\_idxs, col\_idxs or values is not an rvalue, not an array of IndexType, IndexType and ValueType, respectively, or is on the wrong executor, an internal copy of that array will be created, and the original array data will not be used in the matrix.

### Returns

A smart pointer to the matrix wrapping the input arrays (if they reside on the same executor as the matrix) or a copy of these arrays on the correct executor.

### 46.38.2.7 create() [2/3]

create(std::shared\_ptr<const Executor>,

References gko::matrix::Coo< ValueType, IndexType >::create().

### 46.38.2.8 create() [3/3]

Creates an uninitialized COO matrix of the specified size.

### **Parameters**

exec	Executor associated to the matrix
size	size of the matrix
num_nonzeros	number of nonzeros

### Returns

A smart pointer to the newly created matrix.

Referenced by gko::matrix::Coo < ValueType, IndexType >::create().

### 46.38.2.9 create const()

Creates a constant (immutable) Coo matrix from a set of constant arrays.

# **Parameters**

exec	the executor to create the matrix on
size	the dimensions of the matrix
values	the value array of the matrix
col_idxs	the column index array of the matrix
row_ptrs	the row index array of the matrix

### Returns

A smart pointer to the constant matrix wrapping the input arrays (if they reside on the same executor as the matrix) or a copy of these arrays on the correct executor.

# 46.38.2.10 extract\_diagonal()

```
template<typename ValueType = default_precision, typename IndexType = int32> std::unique_ptr<Diagonal<ValueType> > gko::matrix::Coo< ValueType, IndexType >::extract_← diagonal () const [override], [virtual]
```

Extracts the diagonal entries of the matrix into a vector.

### **Parameters**

diag the vector into which the diagonal will be written

Implements gko::DiagonalExtractable< ValueType >.

# 46.38.2.11 get\_col\_idxs()

```
template<typename ValueType = default_precision, typename IndexType = int32>
index_type* gko::matrix::Coo< ValueType, IndexType >::get_col_idxs ( ) [inline], [noexcept]
```

Returns the column indexes of the matrix.

### Returns

the column indexes of the matrix.

References gko::array< ValueType >::get\_data().

# 46.38.2.12 get\_const\_col\_idxs()

```
template<typename ValueType = default_precision, typename IndexType = int32>
const index_type* gko::matrix::Coo< ValueType, IndexType >::get_const_col_idxs ( ) const [inline],
[noexcept]
```

Returns the column indexes of the matrix.

### Returns

the column indexes of the matrix.

### Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

References gko::array< ValueType >::get\_const\_data().

# 46.38.2.13 get\_const\_row\_idxs()

```
template<typename ValueType = default_precision, typename IndexType = int32>
const index_type* gko::matrix::Coo< ValueType, IndexType >::get_const_row_idxs ( ) const [inline],
[noexcept]
```

### Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

References gko::array< ValueType >::get\_const\_data().

# 46.38.2.14 get\_const\_values()

```
template<typename ValueType = default_precision, typename IndexType = int32>
const value_type* gko::matrix::Coo< ValueType, IndexType >::get_const_values ( ) const [inline],
[noexcept]
```

Returns the values of the matrix.

### Returns

the values of the matrix.

### Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

References gko::array< ValueType >::get\_const\_data().

### 46.38.2.15 get\_num\_stored\_elements()

```
template<typename ValueType = default_precision, typename IndexType = int32>
size_type gko::matrix::Coo< ValueType, IndexType >::get_num_stored_elements ( ) const [inline],
[noexcept]
```

Returns the number of elements explicitly stored in the matrix.

### Returns

the number of elements explicitly stored in the matrix

References gko::array< ValueType >::get size().

### 46.38.2.16 get\_row\_idxs()

```
template<typename ValueType = default_precision, typename IndexType = int32>
index_type* gko::matrix::Coo< ValueType, IndexType >::get_row_idxs () [inline], [noexcept]
```

Returns the row indexes of the matrix.

#### Returns

the row indexes of the matrix.

References gko::array< ValueType >::get\_data().

### 46.38.2.17 get\_values()

```
template<typename ValueType = default_precision, typename IndexType = int32>
value_type* gko::matrix::Coo< ValueType, IndexType >::get_values () [inline], [noexcept]
```

Returns the values of the matrix.

### Returns

the values of the matrix.

References gko::array< ValueType >::get\_data().

### 46.38.2.18 read() [1/3]

Reads a matrix from a device\_matrix\_data structure.

# **Parameters**

```
data the device_matrix_data structure.
```

Reimplemented from gko::ReadableFromMatrixData< ValueType, IndexType >.

# 46.38.2.19 read() [2/3]

Reads a matrix from a matrix\_data structure.

### **Parameters**

```
data the matrix_data structure
```

Implements gko::ReadableFromMatrixData< ValueType, IndexType >.

### 46.38.2.20 read() [3/3]

Reads a matrix from a device\_matrix\_data structure.

The structure may be emptied by this function.

#### **Parameters**

```
data the device_matrix_data structure.
```

 $Reimplemented\ from\ gko:: Readable From Matrix Data < Value Type,\ Index Type >.$ 

# 46.38.2.21 write()

Writes a matrix to a matrix\_data structure.

# **Parameters**

```
data the matrix_data structure
```

Implements gko::WritableToMatrixData< ValueType, IndexType >.

The documentation for this class was generated from the following file:

• ginkgo/core/matrix/coo.hpp

# 46.39 gko::CpuAllocator Class Reference

Allocator using new/delete.

#include <ginkgo/core/base/memory.hpp>

# 46.39.1 Detailed Description

Allocator using new/delete.

The documentation for this class was generated from the following file:

• ginkgo/core/base/memory.hpp

# 46.40 gko::CpuAllocatorBase Class Reference

Implement this interface to provide an allocator for OmpExecutor or ReferenceExecutor.

#include <ginkgo/core/base/memory.hpp>

# 46.40.1 Detailed Description

Implement this interface to provide an allocator for OmpExecutor or ReferenceExecutor.

The documentation for this class was generated from the following file:

• ginkgo/core/base/memory.hpp

# 46.41 gko::CpuTimer Class Reference

A timer using std::chrono::steady\_clock for timing.

#include <ginkgo/core/base/timer.hpp>

# **Public Member Functions**

- void record (time\_point &time) override
   Records a time point at the current time.
- void wait (time\_point &time) override

Waits until all kernels in-process when recording the time point are finished.

std::chrono::nanoseconds difference\_async (const time\_point &start, const time\_point &stop) override
 Computes the difference between the two time points in nanoseconds.

# **Additional Inherited Members**

# 46.41.1 Detailed Description

A timer using std::chrono::steady\_clock for timing.

# 46.41.2 Member Function Documentation

### 46.41.2.1 difference async()

Computes the difference between the two time points in nanoseconds.

This asynchronous version does not synchronize itself, so the time points need to have been synchronized with, i.e. timer->wait(stop) needs to have been called. The version is intended for more advanced users who want to measure the overhead of timing functionality separately.

### **Parameters**

start	the first time point (earlier)
end	the second time point (later)

#### Returns

the difference between the time points in nanoseconds.

Implements gko::Timer.

The documentation for this class was generated from the following file:

• ginkgo/core/base/timer.hpp

# 46.42 gko::cpx\_real\_type< T > Struct Template Reference

Access the underlying real type of a complex number.

```
#include <ginkgo/core/base/math.hpp>
```

# **Public Types**

```
• using type = T

The type.
```

# 46.42.1 Detailed Description

```
template < typename T> struct gko::cpx_real_type < T>
```

Access the underlying real type of a complex number.

**Template Parameters** 

```
T | the type being checked.
```

# 46.42.2 Member Typedef Documentation

### 46.42.2.1 type

```
template<typename T >
using gko::cpx_real_type< T >::type = T
```

The type.

When the type is not complex, return the type itself.

The documentation for this struct was generated from the following file:

· ginkgo/core/base/math.hpp

# 46.43 gko::stop::Criterion Class Reference

The Criterion class is a base class for all stopping criteria.

```
#include <ginkgo/core/stop/criterion.hpp>
```

### **Classes**

· class Updater

The Updater class serves for convenient argument passing to the Criterion's check function.

# **Public Member Functions**

• Updater update ()

Returns the updater object.

bool check (uint8 stopping\_id, bool set\_finalized, array< stopping\_status > \*stop\_status, bool \*one\_←
changed, const Updater &updater)

This checks whether convergence was reached for a certain criterion.

# 46.43.1 Detailed Description

The Criterion class is a base class for all stopping criteria.

It contains a factory to instantiate criteria. It is up to each specific stopping criterion to decide what to do with the data that is passed to it.

Note that depending on the criterion, convergence may not have happened after stopping.

### 46.43.2 Member Function Documentation

### 46.43.2.1 check()

```
bool gko::stop::Criterion::check (
          uint8 stopping_id,
          bool set_finalized,
          array< stopping_status > * stop_status,
          bool * one_changed,
          const Updater & updater ) [inline]
```

This checks whether convergence was reached for a certain criterion.

The actual implantation of the criterion goes here.

#### **Parameters**

stopping_id	id of the stopping criterion
set_finalized	Controls if the current version should count as finalized or not
stop_status	status of the stopping criterion
one_changed	indicates if the status of a vector has changed
updater	the Updater object containing all the information

# Returns

### whether convergence was completely reached

```
140
             this->template log<log::Logger::criterion_check_started>(
142
                 this, updater.num_iterations_, updater.residual_,
143
                  updater.residual_norm_, updater.solution_, stopping_id,
144
            set_finalized);
auto all_converged = this->check_impl(
145
146
                 stopping_id, set_finalized, stop_status, one_changed, updater);
147
            this->template log<log::Logger::criterion_check_completed>(
148
                 this, updater.num_iterations_, updater.residual_,
149
                  updater.residual_norm_, updater.implicit_sq_residual_norm_,
             updater.solution_, stopping_id, set_finalized, stop_status,
    *one_changed, all_converged);
return all_converged;
150
151
152
```

Referenced by gko::stop::Criterion::Updater::check().

# 46.43.2.2 update()

```
Updater gko::stop::Criterion::update ( ) [inline]
```

Returns the updater object.

### Returns

the updater object

The documentation for this class was generated from the following file:

• ginkgo/core/stop/criterion.hpp

# 46.44 gko::log::criterion data Struct Reference

Struct representing Criterion related data.

#include <ginkgo/core/log/record.hpp>

# 46.44.1 Detailed Description

Struct representing Criterion related data.

The documentation for this struct was generated from the following file:

· ginkgo/core/log/record.hpp

# 46.45 gko::stop::CriterionArgs Struct Reference

This struct is used to pass parameters to the EnableDefaultCriterionFactoryCriterionFactory::generate() method.

#include <ginkgo/core/stop/criterion.hpp>

# 46.45.1 Detailed Description

This struct is used to pass parameters to the EnableDefaultCriterionFactoryCriterionFactory::generate() method.

It is the ComponentsType of CriterionFactory.

Note

Dependly on the use case, some of these parameters can be nullptr as only some stopping criterion require them to be set. An example is the ResidualNormReduction which really requires the initial  $\leftarrow$  \_residual to be set.

The documentation for this struct was generated from the following file:

• ginkgo/core/stop/criterion.hpp

# 46.46 gko::batch::matrix::Csr< ValueType, IndexType > Class Template Reference

Csr is a general sparse matrix format that stores the column indices for each nonzero entry and a cumulative sum of the number of nonzeros in each row.

#include <ginkgo/core/matrix/batch\_csr.hpp>

#### **Public Member Functions**

• std::unique\_ptr< unbatch\_type > create\_view\_for\_item (size\_type item\_id)

Creates a mutable view (of matrix::Csr type) of one item of the batch::matrix::Csr<value\_type> object.

std::unique\_ptr< const unbatch\_type > create\_const\_view\_for\_item (size\_type item\_id) const

Creates a mutable view (of matrix::Csr type) of one item of the batch::matrix::Csr <value\_type> object.

value\_type \* get\_values () noexcept

Returns a pointer to the array of values of the matrix.

const value\_type \* get\_const\_values () const noexcept

Returns a pointer to the array of values of the matrix.

index\_type \* get\_col\_idxs () noexcept

Returns a pointer to the array of column indices of the matrix.

const index\_type \* get\_const\_col\_idxs () const noexcept

Returns a pointer to the array of column indices of the matrix.

index\_type \* get\_row\_ptrs () noexcept

Returns a pointer to the array of row pointers of the matrix.

const index\_type \* get\_const\_row\_ptrs () const noexcept

Returns a pointer to the array of row pointers of the matrix.

• size type get num stored elements () const noexcept

Returns the number of elements explicitly stored in the batch matrix, cumulative across all the batch items.

• size type get num elements per item () const noexcept

Returns the number of stored elements in each batch item.

value type \* get values for item (size type batch id) noexcept

Returns a pointer to the array of values of the matrix for a specific batch item.

• const value\_type \* get\_const\_values\_for\_item (size\_type batch\_id) const noexcept

Returns a pointer to the array of values of the matrix for a specific batch item.

- Csr \* apply (ptr\_param < const MultiVector < value\_type >> b, ptr\_param < MultiVector < value\_type >> x)
   Apply the matrix to a multi-vector.
- Csr \* apply (ptr\_param< const MultiVector< value\_type >> alpha, ptr\_param< const MultiVector< value 
   \_type >> b, ptr\_param< const MultiVector< value\_type >> beta, ptr\_param< MultiVector< value\_type
   <p>>> x)

Apply the matrix to a multi-vector with a linear combination of the given input vector.

- const Csr \* apply (ptr\_param< const MultiVector< value\_type >> b, ptr\_param< MultiVector< value\_type >> x) const
- const Csr \* apply (ptr\_param< const MultiVector< value\_type >> alpha, ptr\_param< const MultiVector< value\_type >> beta, ptr\_param< MultiVector< value\_type >> beta, ptr\_param< MultiVector< value\_type >> x) const
- void scale (const array < value\_type > &row\_scale, const array < value\_type > &col\_scale)

Performs in-place row and column scaling for this matrix.

 void add\_scaled\_identity (ptr\_param< const MultiVector< value\_type >> alpha, ptr\_param< const MultiVector< value\_type >> beta)

Performs the operation this = alpha\*I + beta\*this.

# **Static Public Member Functions**

static std::unique\_ptr< Csr > create (std::shared\_ptr< const Executor > exec, const batch\_dim< 2 > &size=batch\_dim< 2 >{}, size\_type num\_nonzeros\_per\_item={})

Creates an uninitialized Csr matrix of the specified size.

 static std::unique\_ptr< Csr > create (std::shared\_ptr< const Executor > exec, const batch\_dim< 2 > &size, array< value\_type > values, array< index\_type > col\_idxs, array< index\_type > row\_ptrs)

Creates a Csr matrix from an already allocated (and initialized) array.

template<typename InputValueType, typename ColIndexType, typename RowPtrType >
 static std::unique\_ptr< Csr > create (std::shared\_ptr< const Executor > exec, const batch\_dim< 2 > &size,
 std::initializer\_list< InputValueType > values, std::initializer\_list< ColIndexType > col\_idxs, std::initializer\_
 list< RowPtrType > row\_ptrs)

create(std::shared\_ptr<const Executor>,

static std::unique\_ptr< const Csr > create\_const (std::shared\_ptr< const Executor > exec, const batch\_dim< 2 > &sizes, gko::detail::const\_array\_view< value\_type > &&values, gko::detail::const\_← array\_view< index\_type > &&row\_ptrs)

Creates a constant (immutable) batch csr matrix from a constant array.

# 46.46.1 Detailed Description

```
template<typename ValueType = default_precision, typename IndexType = int32> class gko::batch::matrix::Csr< ValueType, IndexType >
```

Csr is a general sparse matrix format that stores the column indices for each nonzero entry and a cumulative sum of the number of nonzeros in each row.

It is one of the most popular sparse matrix formats due to its versatility and ability to store a wide range of sparsity patterns in an efficient fashion.

#### Note

It is assumed that the sparsity pattern of all the items in the batch is the same and therefore only a single copy of the sparsity pattern is stored.

Currently only IndexType of int32 is supported.

#### **Template Parameters**

ValueType	value precision of matrix elements
IndexType	index precision of matrix elements

## 46.46.2 Member Function Documentation

#### 46.46.2.1 add scaled identity()

Performs the operation this = alpha\*I + beta\*this.

alpha	the scalar for identity	
beta	the scalar to multiply this matrix	

Note

Performs the operation in-place for this batch matrix

This operation fails in case this matrix does not have all its diagonal entries.

# 46.46.2.2 apply() [1/4]

Apply the matrix to a multi-vector with a linear combination of the given input vector.

Represents the matrix vector multiplication, x = alpha \* A

• b + beta \* x, where x and b are both multi-vectors.

#### **Parameters**

alpha	the scalar to scale the matrix-vector product with
b	the multi-vector to be applied to
beta	the scalar to scale the x vector with
X	the output multi-vector

# 46.46.2.3 apply() [2/4]

# 46.46.2.4 apply() [3/4]

Apply the matrix to a multi-vector.

Represents the matrix vector multiplication, x = A \* b, where x and b are both multi-vectors.

#### **Parameters**

	the multi-vector to be applied to
Х	the output multi-vector

# 46.46.2.5 apply() [4/4]

# 46.46.2.6 create() [1/3]

```
template<typename ValueType = default_precision, typename IndexType = int32>
static std::unique_ptr<Csr> gko::batch::matrix::Csr< ValueType, IndexType >::create (
    std::shared_ptr< const Executor > exec,
    const batch_dim< 2 > & size,
    array< value_type > values,
    array< index_type > col_idxs,
    array< index_type > row_ptrs ) [static]
```

Creates a Csr matrix from an already allocated (and initialized) array.

The column indices array needs to be the same for all batch items.

# **Parameters**

exec	Executor associated to the matrix
size	size of the matrix
values	array of matrix values
col_idxs the col_idxs array of a single batch item of the matrix	
row_ptrs	the row_ptrs array of a single batch item of the matrix.

# Note

If values is not an rvalue, not an array of ValueType, or is on the wrong executor, an internal copy will be created, and the original array data will not be used in the matrix.

# Returns

A smart pointer to the newly created matrix.

#### 46.46.2.7 create() [2/3]

```
template<typename ValueType = default_precision, typename IndexType = int32>
\verb|template| < typename InputValueType , typename ColIndexType , typename RowPtrType >
static std::unique_ptr<Csr> gko::batch::matrix::Csr< ValueType, IndexType >::create (
             std::shared_ptr< const Executor > exec,
             const batch_dim< 2 > & size,
             std::initializer_list< InputValueType > values,
             std::initializer_list< ColIndexType > col_idxs,
             std::initializer_list< RowPtrType > row_ptrs ) [inline], [static]
create(std::shared_ptr<const Executor>,
create(std::shared_ptr<const Executor>, const batch_dim<2>&, array<value_type>, array<index_type>,
array<index_type>)
260
           return create(exec, size, array<value_type>{exec, std::move(values)},
261
                        array<index_type>{exec, std::move(col_idxs)}
2.62
                        array<index_type>{exec, std::move(row_ptrs)});
```

References gko::batch::matrix::Csr< ValueType, IndexType >::create().

#### 46.46.2.8 create() [3/3]

```
template<typename ValueType = default_precision, typename IndexType = int32>
static std::unique_ptr<Csr> gko::batch::matrix::Csr< ValueType, IndexType >::create (
    std::shared_ptr< const Executor > exec,
    const batch_dim< 2 > & size = batch_dim< 2 > {},
    size_type num_nonzeros_per_item = {}) [static]
```

Creates an uninitialized Csr matrix of the specified size.

#### **Parameters**

2.63

exec	Executor associated to the matrix
size	size of the matrix
num_nonzeros_per_item	number of nonzeros in each item of the batch matrix

Referenced by gko::batch::matrix::Csr< ValueType, IndexType >::create().

#### 46.46.2.9 create const()

```
\label{eq:gko::detail::const_array_view< index_type > \&\& col_idxs,} $$gko::detail::const_array_view< index_type > \&\& row_ptrs ) [static]
```

Creates a constant (immutable) batch csr matrix from a constant array.

Only a single sparsity pattern (column indices and row pointers) is stored and hence the user needs to ensure that each batch item has the same sparsity pattern.

#### **Parameters**

exec	the executor to create the matrix on
size	the dimensions of the matrix
values	the value array of the matrix
col_idxs	the col_idxs array of a single batch item of the matrix.
row_ptrs	the row_ptrs array of a single batch item of the matrix.

#### Returns

A smart pointer to the constant matrix wrapping the input array (if it resides on the same executor as the matrix) or a copy of the array on the correct executor.

A smart pointer to the newly created matrix.

# 46.46.2.10 create\_const\_view\_for\_item()

Creates a mutable view (of matrix::Csr type) of one item of the batch::matrix::Csr<value\_type> object.

Does not perform any deep copies, but only returns a view of the data.

#### **Parameters**

item←	The index of the batch item
_id	

#### Returns

a batch::matrix::Csr object with the data from the batch item at the given index.

#### 46.46.2.11 create\_view\_for\_item()

Creates a mutable view (of matrix::Csr type) of one item of the batch::matrix::Csr < value\_type > object.

Does not perform any deep copies, but only returns a view of the data.

#### **Parameters**

item⊷	The index of the batch item
_id	

#### Returns

a batch::matrix::Csr object with the data from the batch item at the given index.

# 46.46.2.12 get\_col\_idxs()

```
template<typename ValueType = default_precision, typename IndexType = int32>
index_type* gko::batch::matrix::Csr< ValueType, IndexType >::get_col_idxs ( ) [inline], [noexcept]
```

Returns a pointer to the array of column indices of the matrix.

#### Returns

the pointer to the array of column indices

References gko::array< ValueType >::get\_data().

# 46.46.2.13 get\_const\_col\_idxs()

```
template<typename ValueType = default_precision, typename IndexType = int32>
const index_type* gko::batch::matrix::Csr< ValueType, IndexType >::get_const_col_idxs ( )
const [inline], [noexcept]
```

Returns a pointer to the array of column indices of the matrix.

# Returns

the pointer to the array of column indices

# Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

References gko::array< ValueType >::get\_const\_data().

# 46.46.2.14 get\_const\_row\_ptrs()

```
template<typename ValueType = default_precision, typename IndexType = int32>
const index_type* gko::batch::matrix::Csr< ValueType, IndexType >::get_const_row_ptrs ( )
const [inline], [noexcept]
```

Returns a pointer to the array of row pointers of the matrix.

#### Returns

the pointer to the array of row pointers

#### Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

References gko::array< ValueType >::get\_const\_data().

# 46.46.2.15 get\_const\_values()

```
template<typename ValueType = default_precision, typename IndexType = int32>
const value_type* gko::batch::matrix::Csr< ValueType, IndexType >::get_const_values ( ) const
[inline], [noexcept]
```

Returns a pointer to the array of values of the matrix.

#### Returns

the pointer to the array of values

#### Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

References gko::array< ValueType >::get\_const\_data().

#### 46.46.2.16 get\_const\_values\_for\_item()

Returns a pointer to the array of values of the matrix for a specific batch item.

#### **Parameters**

batch←	the id of the batch item.
_id	

#### Returns

the pointer to the array of values

#### Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

References gko::array< ValueType >::get\_const\_data(), gko::batch::matrix::Csr< ValueType, IndexType >::get\_const\_data(), gko::batch::get\_const\_data(), gko::batch::get\_const\_data(), gko::batch::get\_const\_data(), gko::batch::get\_const\_data(), gko::batch::get\_const\_data(), gko::batch::get\_const\_data(), gko

#### 46.46.2.17 get num elements per item()

```
template<typename ValueType = default_precision, typename IndexType = int32>
size_type gko::batch::matrix::Csr< ValueType, IndexType >::get_num_elements_per_item ( ) const
[inline], [noexcept]
```

Returns the number of stored elements in each batch item.

#### Returns

the number of stored elements per batch item.

References gko::batch::matrix::Csr< ValueType, IndexType >::get\_num\_stored\_elements().

Referenced by gko::batch::matrix::Csr< ValueType, IndexType >::get\_const\_values\_for\_item(), and gko::batch ::matrix::Csr< ValueType, IndexType >::get\_values\_for\_item().

## 46.46.2.18 get\_num\_stored\_elements()

```
template<typename ValueType = default_precision, typename IndexType = int32>
size_type gko::batch::matrix::Csr< ValueType, IndexType >::get_num_stored_elements ( ) const
[inline], [noexcept]
```

Returns the number of elements explicitly stored in the batch matrix, cumulative across all the batch items.

## Returns

the number of elements explicitly stored in the vector, cumulative across all the batch items

References gko::array< ValueType >::get\_size().

Referenced by gko::batch::matrix::Csr< ValueType, IndexType >::get\_num\_elements\_per\_item().

## 46.46.2.19 get\_row\_ptrs()

```
template<typename ValueType = default_precision, typename IndexType = int32>
index_type* gko::batch::matrix::Csr< ValueType, IndexType >::get_row_ptrs () [inline], [noexcept]
```

Returns a pointer to the array of row pointers of the matrix.

#### Returns

the pointer to the array of row pointers

References gko::array< ValueType >::get\_data().

#### 46.46.2.20 get\_values()

```
template<typename ValueType = default_precision, typename IndexType = int32>
value_type* gko::batch::matrix::Csr< ValueType, IndexType >::get_values () [inline], [noexcept]
```

Returns a pointer to the array of values of the matrix.

#### Returns

the pointer to the array of values

References gko::array< ValueType >::get\_data().

# 46.46.2.21 get\_values\_for\_item()

Returns a pointer to the array of values of the matrix for a specific batch item.

## **Parameters**

batch⊷	the id of the batch item.
_id	

#### Returns

the pointer to the array of values

References gko::array< ValueType >::get\_data(), gko::batch::matrix::Csr< ValueType, IndexType >::get\_num\_ $\leftarrow$  elements\_per\_item(), and gko::array< ValueType >::get\_size().

## 46.46.2.22 scale()

Performs in-place row and column scaling for this matrix.

#### **Parameters**

row_scale	the row scalars
col_scale	the column scalars

The documentation for this class was generated from the following file:

• ginkgo/core/matrix/batch\_csr.hpp

# 46.47 gko::matrix::Csr< ValueType, IndexType > Class Template Reference

CSR is a matrix format which stores only the nonzero coefficients by compressing each row of the matrix (compressed sparse row format).

```
#include <ginkgo/core/matrix/csr.hpp>
```

# **Classes**

· class classical

classical is a strategy\_type which uses the same number of threads on each row.

· class cusparse

cusparse is a strategy\_type which uses the sparselib csr.

· class load balance

load\_balance is a strategy\_type which uses the load balance algorithm.

· class merge\_path

merge\_path is a strategy\_type which uses the merge\_path algorithm.

class sparselib

sparselib is a strategy\_type which uses the sparselib csr.

· class strategy\_type

strategy\_type is to decide how to set the csr algorithm.

#### **Public Member Functions**

void read (const mat\_data &data) override

Reads a matrix from a matrix\_data structure.

void read (const device mat data &data) override

Reads a matrix from a device\_matrix\_data structure.

void read (device\_mat\_data &&data) override

Reads a matrix from a device\_matrix\_data structure.

void write (mat\_data &data) const override

Writes a matrix to a matrix\_data structure.

• std::unique\_ptr< LinOp > transpose () const override

Returns a LinOp representing the transpose of the Transposable object.

std::unique\_ptr< LinOp > conj\_transpose () const override

Returns a LinOp representing the conjugate transpose of the Transposable object.

• std::unique\_ptr< Csr > permute (ptr\_param< const Permutation< index\_type >> permutation, permute mode mode=permute mode::symmetric) const

Creates a permuted copy A' of this matrix A with the given permutation P.

• std::unique\_ptr< Csr > permute (ptr\_param< const Permutation< index\_type >> row\_permutation, ptr\_param< const Permutation< index\_type >> column\_permutation, bool invert=false) const

Creates a non-symmetrically permuted copy A' of this matrix A with the given row and column permutations P and Q.

std::unique\_ptr< Csr > scale\_permute (ptr\_param< const ScaledPermutation< value\_type, index\_type >> permutation, permute mode=permute mode::symmetric) const

Creates a scaled and permuted copy of this matrix.

std::unique\_ptr< Csr > scale\_permute (ptr\_param< const ScaledPermutation< value\_type, index\_type >> row\_permutation, ptr\_param< const ScaledPermutation< value\_type, index\_type >> column\_permutation, bool invert=false) const

Creates a scaled and permuted copy of this matrix.

• std::unique\_ptr< LinOp > permute (const array< IndexType > \*permutation\_indices) const override

Returns a LinOp representing the symmetric row and column permutation of the Permutable object.

std::unique\_ptr< LinOp > inverse\_permute (const array< IndexType > \*inverse\_permutation\_indices) const override

Returns a LinOp representing the symmetric inverse row and column permutation of the Permutable object.

- std::unique\_ptr< LinOp > row\_permute (const array< IndexType > \*permutation\_indices) const override

  Returns a LinOp representing the row permutation of the Permutable object.
- std::unique\_ptr< LinOp > column\_permute (const array< IndexType > \*permutation\_indices) const override

  Returns a LinOp representing the column permutation of the Permutable object.
- std::unique\_ptr< LinOp > inverse\_row\_permute (const array< IndexType > \*inverse\_permutation\_indices) const override

Returns a LinOp representing the row permutation of the inverse permuted object.

std::unique\_ptr< LinOp > inverse\_column\_permute (const array< IndexType > \*inverse\_permutation\_← indices) const override

Returns a LinOp representing the row permutation of the inverse permuted object.

std::unique\_ptr< Diagonal</li>
 ValueType > > extract\_diagonal () const override

Extracts the diagonal entries of the matrix into a vector.

std::unique ptr< absolute type > compute absolute () const override

Gets the AbsoluteLinOp.

void compute\_absolute\_inplace () override

Compute absolute inplace on each element.

void sort\_by\_column\_index ()

Sorts all (value, col idx) pairs in each row by column index.

value\_type \* get\_values () noexcept

Returns the values of the matrix.

const value\_type \* get\_const\_values () const noexcept

Returns the values of the matrix.

index\_type \* get\_col\_idxs () noexcept

Returns the column indexes of the matrix.

const index\_type \* get\_const\_col\_idxs () const noexcept

Returns the column indexes of the matrix.

index\_type \* get\_row\_ptrs () noexcept

Returns the row pointers of the matrix.

const index\_type \* get\_const\_row\_ptrs () const noexcept

Returns the row pointers of the matrix.

index type \* get srow () noexcept

Returns the starting rows.

const index type \* get const srow () const noexcept

Returns the starting rows.

size\_type get\_num\_srow\_elements () const noexcept

Returns the number of the srow stored elements (involved warps)

size\_type get\_num\_stored\_elements () const noexcept

Returns the number of elements explicitly stored in the matrix.

std::shared\_ptr< strategy\_type > get\_strategy () const noexcept

Returns the strategy.

void set\_strategy (std::shared\_ptr< strategy\_type > strategy)

Set the strategy.

void scale (ptr\_param< const LinOp > alpha)

Scales the matrix with a scalar.

void inv\_scale (ptr\_param< const LinOp > alpha)

Scales the matrix with the inverse of a scalar.

std::unique\_ptr< Csr< ValueType, IndexType > > create\_submatrix (const index\_set< IndexType > &row
 \_index\_set, const index\_set< IndexType > &column\_index\_set) const

Creates a submatrix from this Csr matrix given row and column index\_set objects.

• std::unique\_ptr< Csr< ValueType, IndexType > > create\_submatrix (const span &row\_span, const span &column\_span) const

Creates a submatrix from this Csr matrix given row and column spans.

• Csr & operator= (const Csr &)

Copy-assigns a Csr matrix.

Csr & operator= (Csr &&)

Move-assigns a Csr matrix.

Csr (const Csr &)

Copy-constructs a Csr matrix.

• Csr (Csr &&)

Move-constructs a Csr matrix.

# **Static Public Member Functions**

static std::unique\_ptr< Csr > create (std::shared\_ptr< const Executor > exec, std::shared\_ptr< strategy\_type > strategy)

Creates an uninitialized CSR matrix of the specified size.

• static std::unique\_ptr< Csr > create (std::shared\_ptr< const Executor > exec, const dim< 2 > &size={}, size\_type num\_nonzeros={}, std::shared\_ptr< strategy\_type > strategy=nullptr)

Creates an uninitialized CSR matrix of the specified size.

static std::unique\_ptr< Csr > create (std::shared\_ptr< const Executor > exec, const dim< 2 > &size, array< value\_type > values, array< index\_type > col\_idxs, array< index\_type > row\_ptrs, std::shared
 \_\_ptr< strategy\_type > strategy=nullptr)

Creates a CSR matrix from already allocated (and initialized) row pointer, column index and value arrays.

template<typename InputValueType, typename InputColumnIndexType, typename InputRowPtrType>
 static std::unique\_ptr< Csr > create (std::shared\_ptr< const Executor > exec, const dim< 2 > &size, std::initializer\_list< InputValueType > values, std::initializer\_list< InputColumnIndexType > col\_idxs, std
 ::initializer\_list< InputRowPtrType > row\_ptrs)

```
create(std::shared_ptr<const Executor>,
```

static std::unique\_ptr< const Csr > create\_const (std::shared\_ptr< const Executor > exec, const dim< 2
 <p>> &size, gko::detail::const\_array\_view< ValueType > &&values, gko::detail::const\_array\_view< IndexType
 <p>> &&col\_idxs, gko::detail::const\_array\_view< IndexType > &&row\_ptrs, std::shared\_ptr< strategy\_type > strategy=nullptr)

Creates a constant (immutable) Csr matrix from a set of constant arrays.

# 46.47.1 Detailed Description

```
template<typename ValueType = default_precision, typename IndexType = int32> class gko::matrix::Csr< ValueType, IndexType >
```

CSR is a matrix format which stores only the nonzero coefficients by compressing each row of the matrix (compressed sparse row format).

The nonzero elements are stored in a 1D array row-wise, and accompanied with a row pointer array which stores the starting index of each row. An additional column index array is used to identify the column of each nonzero element.

#### The Csr LinOp supports different operations:

Both the SpGEMM and SpGEAM operation require the input matrices to be sorted by column index, otherwise the algorithms will produce incorrect results.

#### **Template Parameters**

ValueType	precision of matrix elements
IndexType	precision of matrix indexes

# 46.47.2 Constructor & Destructor Documentation

# 46.47.2.1 Csr() [1/2]

Copy-constructs a Csr matrix.

Inherits executor, strategy and data.

# 46.47.2.2 Csr() [2/2]

Move-constructs a Csr matrix.

Inherits executor and strategy, moves the data and leaves the moved-from object in an empty state (0x0 LinOp with unchanged executor and strategy, no nonzeros and valid row pointers).

## 46.47.3 Member Function Documentation

#### 46.47.3.1 column\_permute()

Returns a LinOp representing the column permutation of the Permutable object.

In the resulting LinOp, the column i contains the input column perm[i].

From the linear algebra perspective, with  $P_{ij} = \delta_{i\pi(i)}$ , this represents the operation  $AP^T$ .

#### **Parameters**

permutation_indices	the array of indices containing the permutation order perm.
---------------------	---

#### Returns

a pointer to the new column permuted object

Implements gko::Permutable < IndexType >.

## 46.47.3.2 compute\_absolute()

```
template<typename ValueType = default_precision, typename IndexType = int32>
std::unique_ptr<absolute_type> gko::matrix::Csr< ValueType, IndexType >::compute_absolute ()
const [override], [virtual]
```

Gets the AbsoluteLinOp.

#### Returns

a pointer to the new absolute object

Implements gko::EnableAbsoluteComputation< remove\_complex< Csr< ValueType, IndexType >> >.

#### 46.47.3.3 conj\_transpose()

```
template<typename ValueType = default_precision, typename IndexType = int32>
std::unique_ptr<LinOp> gko::matrix::Csr< ValueType, IndexType >::conj_transpose ( ) const
[override], [virtual]
```

Returns a LinOp representing the conjugate transpose of the Transposable object.

## Returns

a pointer to the new conjugate transposed object

Implements gko::Transposable.

## 46.47.3.4 create() [1/4]

```
template<typename ValueType = default_precision, typename IndexType = int32>
static std::unique_ptr<Csr> gko::matrix::Csr< ValueType, IndexType >::create (
    std::shared_ptr< const Executor > exec,
    const dim< 2 > & size,
    array< value_type > values,
    array< index_type > col_idxs,
    array< index_type > row_ptrs,
    std::shared_ptr< strategy_type > strategy = nullptr ) [static]
```

Creates a CSR matrix from already allocated (and initialized) row pointer, column index and value arrays.

exec	Executor associated to the matrix
size	size of the matrix
values	array of matrix values
col_idxs	array of column indexes
row_ptrs	array of row pointers
Generateow D	the strategy the matrix uses for SpMV operations

#### Note

If one of row\_ptrs, col\_idxs or values is not an rvalue, not an array of IndexType, IndexType and ValueType, respectively, or is on the wrong executor, an internal copy of that array will be created, and the original array data will not be used in the matrix.

#### Returns

A smart pointer to the newly created matrix.

# 46.47.3.5 create() [2/4]

create(std::shared\_ptr<const Executor>,

References gko::matrix::Csr< ValueType, IndexType >::create().

#### 46.47.3.6 create() [3/4]

Creates an uninitialized CSR matrix of the specified size.

exec	Executor associated to the matrix		
size	size of the matrix		
num_nonzeros	number of nonzeros		
strategy	the strategy of CSR, or the default strategy if set to nullptr		

#### Returns

A smart pointer to the newly created matrix.

# 46.47.3.7 create() [4/4]

Creates an uninitialized CSR matrix of the specified size.

#### **Parameters**

exec	Executor associated to the matrix
strategy	the strategy of CSR

#### Returns

A smart pointer to the newly created matrix.

Referenced by gko::matrix::Csr< ValueType, IndexType >::create().

# 46.47.3.8 create\_const()

Creates a constant (immutable) Csr matrix from a set of constant arrays.

exec	the executor to create the matrix on
size	the dimensions of the matrix
values	the value array of the matrix
col_idxs	the column index array of the matrix
row_ptrs	the row pointer array of the matrix
strategy	the strategy the matrix uses for SpMV operations

#### Returns

A smart pointer to the constant matrix wrapping the input arrays (if they reside on the same executor as the matrix) or a copy of these arrays on the correct executor.

A smart pointer to the newly created matrix.

# 46.47.3.9 create\_submatrix() [1/2]

Creates a submatrix from this Csr matrix given row and column index\_set objects.

#### **Parameters**

row_index_set	the row index set containing the set of rows to be in the submatrix.
column_index_set	the col index set containing the set of columns to be in the submatrix.

#### Returns

A new CSR matrix with the elements that belong to the row and columns of this matrix as specified by the index sets.

#### Note

This is not a view but creates a new, separate CSR matrix.

### 46.47.3.10 create\_submatrix() [2/2]

Creates a submatrix from this Csr matrix given row and column spans.

row_span	the row span containing the contiguous set of rows to be in the submatrix.
column_span	the column span containing the contiguous set of columns to be in the submatrix.

#### Returns

A new CSR matrix with the elements that belong to the row and columns of this matrix as specified by the index sets.

#### Note

This is not a view but creates a new, separate CSR matrix.

#### 46.47.3.11 extract diagonal()

```
template<typename ValueType = default_precision, typename IndexType = int32>
std::unique_ptr<Diagonal<ValueType> > gko::matrix::Csr< ValueType, IndexType >::extract_
diagonal ( ) const [override], [virtual]
```

Extracts the diagonal entries of the matrix into a vector.

#### **Parameters**

diag the vector into which the diagonal will be written

Implements gko::DiagonalExtractable < ValueType >.

## 46.47.3.12 get\_col\_idxs()

```
template<typename ValueType = default_precision, typename IndexType = int32>
index_type* gko::matrix::Csr< ValueType, IndexType >::get_col_idxs ( ) [inline], [noexcept]
```

Returns the column indexes of the matrix.

#### Returns

the column indexes of the matrix.

References gko::array< ValueType >::get\_data().

#### 46.47.3.13 get\_const\_col\_idxs()

```
template<typename ValueType = default_precision, typename IndexType = int32>
const index_type* gko::matrix::Csr< ValueType, IndexType >::get_const_col_idxs ( ) const [inline],
[noexcept]
```

Returns the column indexes of the matrix.

#### Returns

the column indexes of the matrix.

#### Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

References gko::array< ValueType >::get\_const\_data().

# 46.47.3.14 get\_const\_row\_ptrs()

```
template<typename ValueType = default_precision, typename IndexType = int32>
const index_type* gko::matrix::Csr< ValueType, IndexType >::get_const_row_ptrs ( ) const [inline],
[noexcept]
```

Returns the row pointers of the matrix.

#### Returns

the row pointers of the matrix.

#### Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

References gko::array< ValueType >::get\_const\_data().

#### 46.47.3.15 get\_const\_srow()

```
template<typename ValueType = default_precision, typename IndexType = int32>
const index_type* gko::matrix::Csr< ValueType, IndexType >::get_const_srow ( ) const [inline],
[noexcept]
```

Returns the starting rows.

#### Returns

the starting rows.

#### Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

References gko::array< ValueType >::get\_const\_data().

#### 46.47.3.16 get\_const\_values()

```
template<typename ValueType = default_precision, typename IndexType = int32>
const value_type* gko::matrix::Csr< ValueType, IndexType >::get_const_values ( ) const [inline],
[noexcept]
```

Returns the values of the matrix.

#### Returns

the values of the matrix.

#### Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

References gko::array < ValueType >::get\_const\_data().

#### 46.47.3.17 get num srow elements()

```
template<typename ValueType = default_precision, typename IndexType = int32>
size_type gko::matrix::Csr< ValueType, IndexType >::get_num_srow_elements ( ) const [inline],
[noexcept]
```

Returns the number of the srow stored elements (involved warps)

## Returns

the number of the srow stored elements (involved warps)

References gko::array< ValueType >::get\_size().

#### 46.47.3.18 get\_num\_stored\_elements()

```
template<typename ValueType = default_precision, typename IndexType = int32>
size_type gko::matrix::Csr< ValueType, IndexType >::get_num_stored_elements ( ) const [inline],
[noexcept]
```

Returns the number of elements explicitly stored in the matrix.

# Returns

the number of elements explicitly stored in the matrix

References gko::array< ValueType >::get\_size().

#### 46.47.3.19 get\_row\_ptrs()

```
template<typename ValueType = default_precision, typename IndexType = int32>
index_type* gko::matrix::Csr< ValueType, IndexType >::get_row_ptrs ( ) [inline], [noexcept]
```

Returns the row pointers of the matrix.

Returns

the row pointers of the matrix.

References gko::array< ValueType >::get\_data().

# 46.47.3.20 get\_srow()

```
template<typename ValueType = default_precision, typename IndexType = int32>
index_type* gko::matrix::Csr< ValueType, IndexType >::get_srow () [inline], [noexcept]
```

Returns the starting rows.

Returns

the starting rows.

References gko::array< ValueType >::get\_data().

#### 46.47.3.21 get strategy()

```
template<typename ValueType = default_precision, typename IndexType = int32>
std::shared_ptr<strategy_type> gko::matrix::Csr< ValueType, IndexType >::get_strategy ( )
const [inline], [noexcept]
```

Returns the strategy.

Returns

the strategy

# 46.47.3.22 get\_values()

```
template<typename ValueType = default_precision, typename IndexType = int32>
value_type* gko::matrix::Csr< ValueType, IndexType >::get_values () [inline], [noexcept]
```

Returns the values of the matrix.

Returns

the values of the matrix.

References gko::array< ValueType >::get\_data().

# 46.47.3.23 inv\_scale()

Scales the matrix with the inverse of a scalar.

#### **Parameters**

alpha The entire matrix is scaled by 1 / alpha. alpha has to be a 1x1 Dense matrix.

References gko::PolymorphicObject::get\_executor(), and gko::make\_temporary\_clone().

#### 46.47.3.24 inverse column permute()

Returns a LinOp representing the row permutation of the inverse permuted object.

In the resulting LinOp, the column perm[i] contains the input column i.

From the linear algebra perspective, with  $P_{ij} = \delta_{i\pi(i)}$ , this represents the operation  $AP^{-T}$ .

#### **Parameters**

permutation indices	the array of indices containing the permutation order perm.
---------------------	---

#### Returns

a pointer to the new inverse permuted object

Implements gko::Permutable < IndexType >.

#### 46.47.3.25 inverse\_permute()

Returns a LinOp representing the symmetric inverse row and column permutation of the Permutable object.

In the resulting LinOp, the entry at location (perm[i], perm[j]) contains the input value (i, j).

From the linear algebra perspective, with  $P_{ij} = \delta_{i\pi(i)}$ , this represents the operation  $P^{-1}AP^{-T}$ .

p	permutation indices	the array of indice	s containing the	permutation order.
---	---------------------	---------------------	------------------	--------------------

#### Returns

a pointer to the new permuted object

Reimplemented from gko::Permutable < IndexType >.

## 46.47.3.26 inverse\_row\_permute()

Returns a LinOp representing the row permutation of the inverse permuted object.

In the resulting LinOp, the row perm[i] contains the input row i.

From the linear algebra perspective, with  $P_{ij} = \delta_{i\pi(i)}$ , this represents the operation  $P^{-1}A$ .

#### **Parameters**

	permutation_indices	the array of indices containing the permutation order perm.	
--	---------------------	---	--

#### Returns

a pointer to the new inverse permuted object

Implements gko::Permutable < IndexType >.

# 46.47.3.27 operator=() [1/2]

Copy-assigns a Csr matrix.

Preserves executor, copies everything else.

#### 46.47.3.28 operator=() [2/2]

Move-assigns a Csr matrix.

Preserves executor, moves the data and leaves the moved-from object in an empty state (0x0 LinOp with unchanged executor and strategy, no nonzeros and valid row pointers).

#### 46.47.3.29 permute() [1/3]

Returns a LinOp representing the symmetric row and column permutation of the Permutable object.

In the resulting LinOp, the entry at location (i, j) contains the input value (perm[i], perm[j]).

From the linear algebra perspective, with  $P_{ij} = \delta_{i\pi(i)}$ , this represents the operation  $PAP^T$ .

#### **Parameters**

permutation_indices	the array of indices containing the permutation order.	
---------------------	--	--

#### Returns

a pointer to the new permuted object

Reimplemented from gko::Permutable < IndexType >.

# 46.47.3.30 permute() [2/3]

Creates a permuted copy A' of this matrix A with the given permutation P.

By default, this computes a symmetric permutation (permute\_mode::symmetric). For the effect of the different permutation modes, see permute\_mode

#### **Parameters**

permutation	The input permutation.
mode	The permutation mode. If permute_mode::inverse is set, we use the inverse permutation $P^{-1}$ instead of $P$ . If permute_mode::rows is set, the rows will be permuted. If permute_mode::columns is set, the columns will be permuted.

#### Returns

The permuted matrix.

#### 46.47.3.31 permute() [3/3]

Creates a non-symmetrically permuted copy A' of this matrix A with the given row and column permutations P and Q.

The operation will compute A'(i,j) = A(p[i],q[j]), or  $A' = PAQ^T$  if invert is false, and A'(p[i],q[j]) = A(i,j), or  $A' = P^{-1}AQ^{-T}$  if invert is true.

#### **Parameters**

row_permutation	The permutation $P$ to apply to the rows
column_permutation	The permutation ${\cal Q}$ to apply to the columns
invert	If set to false, uses the input permutations, otherwise uses their inverses ${\cal P}^{-1}, {\cal Q}^{-1}$

#### Returns

The permuted matrix.

# 46.47.3.32 read() [1/3]

Reads a matrix from a device\_matrix\_data structure.

#### **Parameters**

```
data the device_matrix_data structure.
```

 $\label{lem:lemented_rom_gko::ReadableFromMatrixData} Reimplemented from gko:: ReadableFromMatrixData < ValueType, IndexType >.$ 

# 46.47.3.33 read() [2/3]

Reads a matrix from a matrix\_data structure.

#### **Parameters**

```
data the matrix_data structure
```

Implements gko::ReadableFromMatrixData< ValueType, IndexType >.

#### 46.47.3.34 read() [3/3]

Reads a matrix from a device\_matrix\_data structure.

The structure may be emptied by this function.

#### **Parameters**

```
data the device_matrix_data structure.
```

Reimplemented from gko::ReadableFromMatrixData< ValueType, IndexType >.

# 46.47.3.35 row\_permute()

Returns a LinOp representing the row permutation of the Permutable object.

In the resulting LinOp, the row i contains the input row perm[i].

From the linear algebra perspective, with  $P_{ij} = \delta_{i\pi(i)}$ , this represents the operation PA.

#### **Parameters**

```
permutation_indices the array of indices containing the permutation order.
```

#### Returns

a pointer to the new permuted object

Implements gko::Permutable < IndexType >.

#### 46.47.3.36 scale()

Scales the matrix with a scalar.

#### **Parameters**

alpha	The entire matrix is scaled by alpha. alpha has to be a 1x1 Dense matrix.
-------	---

References gko::PolymorphicObject::get\_executor(), and gko::make\_temporary\_clone().

# 46.47.3.37 scale\_permute() [1/2]

Creates a scaled and permuted copy of this matrix.

For an explanation of the permutation modes, see permute(ptr\_param<const Permutation<index\_type>>, permute\_mode)

# **Parameters**

permutation	The scaled permutation.
mode	The permutation mode.

## Returns

The permuted matrix.

#### 46.47.3.38 scale\_permute() [2/2]

Creates a scaled and permuted copy of this matrix.

For an explanation of the parameters, see permute(ptr\_param<const Permutation<index\_type>>, ptr\_param<const Permutation<index\_type>>, permute\_mode)

#### **Parameters**

row_permutation	The scaled row permutation.
column_permutation	The scaled column permutation.
invert	If set to false, uses the input permutations, otherwise uses their inverses ${\cal P}^{-1}, {\cal Q}^{-1}$

#### Returns

The permuted matrix.

# 46.47.3.39 set\_strategy()

# Set the strategy.

#### **Parameters**

strategy	the csr strategy
----------	------------------

#### 46.47.3.40 transpose()

```
template<typename ValueType = default_precision, typename IndexType = int32>
std::unique_ptr<LinOp> gko::matrix::Csr< ValueType, IndexType >::transpose ( ) const [override],
[virtual]
```

Returns a LinOp representing the transpose of the Transposable object.

## Returns

a pointer to the new transposed object

Implements gko::Transposable.

#### 46.47.3.41 write()

Writes a matrix to a matrix\_data structure.

#### **Parameters**

data	the matrix_data structure
------	---------------------------

Implements gko::WritableToMatrixData< ValueType, IndexType >.

The documentation for this class was generated from the following files:

- ginkgo/core/distributed/matrix.hpp
- · ginkgo/core/matrix/csr.hpp

# 46.48 gko::CublasError Class Reference

CublasError is thrown when a cuBLAS routine throws a non-zero error code.

```
#include <ginkgo/core/base/exception.hpp>
```

# **Public Member Functions**

CublasError (const std::string &file, int line, const std::string &func, int64 error\_code)
 Initializes a cuBLAS error.

# 46.48.1 Detailed Description

CublasError is thrown when a cuBLAS routine throws a non-zero error code.

#### 46.48.2 Constructor & Destructor Documentation

# 46.48.2.1 CublasError()

Initializes a cuBLAS error.

file	The name of the offending source file
line	The source code line number where the error occurred
func	The name of the cuBLAS routine that failed
error_code	The resulting cuBLAS error code

The documentation for this class was generated from the following file:

• ginkgo/core/base/exception.hpp

# 46.49 gko::cuda\_stream Class Reference

An RAII wrapper for a custom CUDA stream.

```
#include <ginkgo/core/base/stream.hpp>
```

# **Public Member Functions**

• cuda\_stream ()

Creates an empty stream wrapper, representing the default stream.

cuda\_stream (int device\_id)

Creates a new custom CUDA stream on the given device.

~cuda\_stream ()

Destroys the custom CUDA stream, if it isn't empty.

cuda\_stream (cuda\_stream &&)

Move-constructs from an existing stream, which will be emptied.

cuda\_stream & operator= (cuda\_stream &&)=delete

Move-assigns from an existing stream, which will be emptied.

• CUstream\_st \* get () const

Returns the native CUDA stream handle.

# 46.49.1 Detailed Description

An RAII wrapper for a custom CUDA stream.

The stream will be created on construction and destroyed when the lifetime of the wrapper ends.

## 46.49.2 Constructor & Destructor Documentation

# 46.49.2.1 cuda\_stream()

Creates a new custom CUDA stream on the given device.

device⊷	the device ID to create the stream on.
_id	

# 46.49.3 Member Function Documentation

# 46.49.3.1 get()

```
CUstream_st* gko::cuda_stream::get ( ) const
```

Returns the native CUDA stream handle.

In an empty cuda\_stream, this will return nullptr.

The documentation for this class was generated from the following file:

• ginkgo/core/base/stream.hpp

# 46.50 gko::CudaAllocator Class Reference

Allocator using cudaMalloc.

```
#include <ginkgo/core/base/memory.hpp>
```

# 46.50.1 Detailed Description

Allocator using cudaMalloc.

The documentation for this class was generated from the following file:

• ginkgo/core/base/memory.hpp

# 46.51 gko::CudaAllocatorBase Class Reference

Implement this interface to provide an allocator for CudaExecutor.

```
#include <ginkgo/core/base/memory.hpp>
```

# 46.51.1 Detailed Description

Implement this interface to provide an allocator for CudaExecutor.

The documentation for this class was generated from the following file:

• ginkgo/core/base/memory.hpp

# 46.52 gko::CudaError Class Reference

CudaError is thrown when a CUDA routine throws a non-zero error code.

```
#include <ginkgo/core/base/exception.hpp>
```

#### **Public Member Functions**

CudaError (const std::string &file, int line, const std::string &func, int64 error\_code)
 Initializes a CUDA error.

# 46.52.1 Detailed Description

CudaError is thrown when a CUDA routine throws a non-zero error code.

# 46.52.2 Constructor & Destructor Documentation

#### 46.52.2.1 CudaError()

Initializes a CUDA error.

#### **Parameters**

file	The name of the offending source file
line	The source code line number where the error occurred
func	The name of the CUDA routine that failed
error_code	The resulting CUDA error code

The documentation for this class was generated from the following file:

· ginkgo/core/base/exception.hpp

# 46.53 gko::CudaExecutor Class Reference

This is the Executor subclass which represents the CUDA device.

```
#include <ginkgo/core/base/executor.hpp>
```

#### **Public Member Functions**

std::shared\_ptr< Executor > get\_master () noexcept override

Returns the master OmpExecutor of this Executor.

std::shared\_ptr< const Executor > get\_master () const noexcept override

Returns the master OmpExecutor of this Executor.

· void synchronize () const override

Synchronize the operations launched on the executor with its master.

- std::string get\_description () const override
- int get\_device\_id () const noexcept

Get the CUDA device id of the device associated to this executor.

• int get\_num\_warps\_per\_sm () const noexcept

Get the number of warps per SM of this executor.

int get\_num\_multiprocessor () const noexcept

Get the number of multiprocessor of this executor.

int get\_num\_warps () const noexcept

Get the number of warps of this executor.

• int get\_warp\_size () const noexcept

Get the warp size of this executor.

int get major version () const noexcept

Get the major version of compute capability.

int get\_minor\_version () const noexcept

Get the minor version of compute capability.

cublasContext \* get cublas handle () const

Get the cubias handle for this executor.

• cublasContext \* get\_blas\_handle () const

Get the cubias handle for this executor.

cusparseContext \* get\_cusparse\_handle () const

Get the cusparse handle for this executor.

cusparseContext \* get\_sparselib\_handle () const

Get the cusparse handle for this executor.

std::vector< int > get\_closest\_pus () const

Get the closest PUs.

int get\_closest\_numa () const

Get the closest NUMA node.

CUstream\_st \* get\_stream () const

Returns the CUDA stream used by this executor.

virtual void run (const Operation &op) const=0

Runs the specified Operation using this Executor.

• template<typename ClosureOmp , typename ClosureCuda , typename ClosureHip , typename ClosureDpcpp > void run (const ClosureOmp &op\_omp, const ClosureCuda &op\_cuda, const ClosureHip &op\_hip, const ClosureDpcpp &op\_dpcpp) const

Runs one of the passed in functors, depending on the Executor type.

template < typename ClosureReference , typename ClosureOmp , typename ClosureCuda , typename ClosureHip , typename Closure ← Dpcpp >

void run (std::string name, const ClosureReference &op\_ref, const ClosureOmp &op\_omp, const Closure ← Cuda &op\_cuda, const ClosureHip &op\_hip, const ClosureDpcpp &op\_dpcpp) const

Runs one of the passed in functors, depending on the Executor type.

### Static Public Member Functions

- static std::shared\_ptr< CudaExecutor > create (int device\_id, std::shared\_ptr< Executor > master, bool device\_reset, allocation\_mode alloc\_mode=default\_cuda\_alloc\_mode, CUstream\_st \*stream=nullptr)
  - Creates a new CudaExecutor.
- static std::shared\_ptr< CudaExecutor > create (int device\_id, std::shared\_ptr< Executor > master, std::shared\_ptr< CudaAllocatorBase > alloc=std::make\_shared< CudaAllocator >(), CUstream\_st \*stream=nullptr)

Creates a new CudaExecutor with a custom allocator and device stream.

• static int get\_num\_devices ()

Get the number of devices present on the system.

## 46.53.1 Detailed Description

This is the Executor subclass which represents the CUDA device.

## 46.53.2 Member Function Documentation

### 46.53.2.1 create() [1/2]

```
static std::shared_ptr<CudaExecutor> gko::CudaExecutor::create (
    int device_id,
    std::shared_ptr< Executor > master,
    bool device_reset,
    allocation_mode alloc_mode = default_cuda_alloc_mode,
    CUstream_st * stream = nullptr ) [static]
```

Creates a new CudaExecutor.

#### **Parameters**

device_id	the CUDA device id of this device
master	an executor on the host that is used to invoke the device kernels
device_reset	this option no longer has any effect.
alloc_mode the allocation mode that the executor should operate on. See @allocation_mode for more details	
stream	the stream to execute operations on.

### 46.53.2.2 create() [2/2]

Creates a new CudaExecutor with a custom allocator and device stream.

#### **Parameters**

device⊷	the CUDA device id of this device
_id	
master	an executor on the host that is used to invoke the device kernels.
alloc	the allocator to use for device memory allocations.
stream	the stream to execute operations on.

## 46.53.2.3 get\_blas\_handle()

```
cublasContext* gko::CudaExecutor::get_blas_handle ( ) const [inline]
```

Get the cubias handle for this executor.

## Returns

the cublas handle (cublasContext\*) for this executor

## 46.53.2.4 get\_closest\_numa()

```
int gko::CudaExecutor::get_closest_numa ( ) const [inline]
```

Get the closest NUMA node.

## Returns

the closest NUMA node closest to this device

## 46.53.2.5 get\_closest\_pus()

```
std::vector<int> gko::CudaExecutor::get_closest_pus ( ) const [inline]
```

Get the closest PUs.

## Returns

the array of PUs closest to this device

## 46.53.2.6 get\_cublas\_handle()

```
cublasContext* gko::CudaExecutor::get_cublas_handle ( ) const [inline]
```

Get the cubias handle for this executor.

#### Returns

the cublas handle (cublasContext\*) for this executor

## 46.53.2.7 get\_cusparse\_handle()

```
cusparseContext* gko::CudaExecutor::get_cusparse_handle ( ) const [inline]
```

Get the cusparse handle for this executor.

### Returns

the cusparse handle (cusparseContext\*) for this executor

## 46.53.2.8 get\_description()

```
std::string gko::CudaExecutor::get_description ( ) const [override], [virtual]
```

#### Returns

a textual representation of the executor and its device.

Implements gko::Executor.

## 46.53.2.9 get\_master() [1/2]

```
std::shared_ptr<const Executor> gko::CudaExecutor::get_master ( ) const [override], [virtual],
[noexcept]
```

Returns the master OmpExecutor of this Executor.

## Returns

the master OmpExecutor of this Executor.

Implements gko::Executor.

## 46.53.2.10 get\_master() [2/2]

```
std::shared_ptr<Executor> gko::CudaExecutor::get_master ( ) [override], [virtual], [noexcept]
```

Returns the master OmpExecutor of this Executor.

### Returns

the master OmpExecutor of this Executor.

Implements gko::Executor.

## 46.53.2.11 get\_sparselib\_handle()

```
cusparseContext* gko::CudaExecutor::get_sparselib_handle ( ) const [inline]
```

Get the cusparse handle for this executor.

#### Returns

the cusparse handle (cusparseContext\*) for this executor

## 46.53.2.12 get\_stream()

```
CUstream_st* gko::CudaExecutor::get_stream ( ) const [inline]
```

Returns the CUDA stream used by this executor.

Can be nullptr for the default stream.

## Returns

the stream used to execute kernels and memory operations.

## 46.53.2.13 run() [1/3]

Runs one of the passed in functors, depending on the Executor type.

## **Template Parameters**

ClosureOmp	type of op_omp
ClosureCuda	type of op_cuda
ClosureHip	type of op_hip
ClosureDpcpp	type of op_dpcpp

### **Parameters**

op_omp	functor to run in case of a OmpExecutor or ReferenceExecutor
op_cuda	functor to run in case of a CudaExecutor
op_hip	functor to run in case of a HipExecutor
op_dpcpp	functor to run in case of a DpcppExecutor

## 46.53.2.14 run() [2/3]

virtual void gko::Executor::run

Runs the specified Operation using this Executor.

### **Parameters**

op the operation to run

## 46.53.2.15 run() [3/3]

Runs one of the passed in functors, depending on the Executor type.

## **Template Parameters**

ClosureReference	type of op_ref
ClosureOmp	type of op_omp
ClosureCuda	type of op_cuda
ClosureHip	type of op_hip
ClosureDpcpp	type of op_dpcpp

#### **Parameters**

name	the name of the operation
op_ref	functor to run in case of a ReferenceExecutor
op_omp	functor to run in case of a OmpExecutor
op_cuda	functor to run in case of a CudaExecutor
op_hip	functor to run in case of a HipExecutor
op_dpcpp	functor to run in case of a DpcppExecutor

The documentation for this class was generated from the following file:

• ginkgo/core/base/executor.hpp

## 46.54 gko::CudaTimer Class Reference

A timer using events for timing on a CudaExecutor.

```
#include <ginkgo/core/base/timer.hpp>
```

#### **Public Member Functions**

- void record (time\_point &time) override
- Records a time point at the current time.

   void wait (time\_point &time) override
  - Waits until all kernels in-process when recording the time point are finished.
- std::chrono::nanoseconds difference\_async (const time\_point &start, const time\_point &stop) override Computes the difference between the two time points in nanoseconds.

## **Additional Inherited Members**

## 46.54.1 Detailed Description

A timer using events for timing on a CudaExecutor.

Note

When using a CudaExecutor with a custom stream, make sure that the stream's lifetime is longer than the lifetime of this timer.

## 46.54.2 Member Function Documentation

## 46.54.2.1 difference\_async()

Computes the difference between the two time points in nanoseconds.

This asynchronous version does not synchronize itself, so the time points need to have been synchronized with, i.e. timer->wait(stop) needs to have been called. The version is intended for more advanced users who want to measure the overhead of timing functionality separately.

#### **Parameters**

start	the first time point (earlier)
end	the second time point (later)

## Returns

the difference between the time points in nanoseconds.

Implements gko::Timer.

The documentation for this class was generated from the following file:

• ginkgo/core/base/timer.hpp

## 46.55 gko::CufftError Class Reference

CufftError is thrown when a cuFFT routine throws a non-zero error code.

```
#include <ginkgo/core/base/exception.hpp>
```

## **Public Member Functions**

CufftError (const std::string &file, int line, const std::string &func, int64 error\_code)
 Initializes a cuFFT error.

## 46.55.1 Detailed Description

CufftError is thrown when a cuFFT routine throws a non-zero error code.

## 46.55.2 Constructor & Destructor Documentation

## 46.55.2.1 CufftError()

Initializes a cuFFT error.

#### **Parameters**

file	The name of the offending source file
line	The source code line number where the error occurred
func	The name of the cuFFT routine that failed
error_code	The resulting cuFFT error code

The documentation for this class was generated from the following file:

• ginkgo/core/base/exception.hpp

# 46.56 gko::CurandError Class Reference

CurandError is thrown when a cuRAND routine throws a non-zero error code.

```
#include <ginkgo/core/base/exception.hpp>
```

## **Public Member Functions**

• CurandError (const std::string &file, int line, const std::string &func, int64 error\_code)

Initializes a cuRAND error.

## 46.56.1 Detailed Description

CurandError is thrown when a cuRAND routine throws a non-zero error code.

## 46.56.2 Constructor & Destructor Documentation

## 46.56.2.1 CurandError()

Initializes a cuRAND error.

## **Parameters**

file	The name of the offending source file
line	The source code line number where the error occurred
func	The name of the cuRAND routine that failed
error_code	The resulting cuRAND error code

The documentation for this class was generated from the following file:

· ginkgo/core/base/exception.hpp

# 46.57 gko::matrix::Csr< ValueType, IndexType >::cusparse Class Reference

cusparse is a strategy\_type which uses the sparselib csr.

```
#include <ginkgo/core/matrix/csr.hpp>
```

## **Public Member Functions**

· cusparse ()

Creates a cusparse strategy.

- void process (const array < index\_type > &mtx\_row\_ptrs, array < index\_type > \*mtx\_srow) override
   Computes srow according to row pointers.
- int64\_t clac\_size (const int64\_t nnz) override

Computes the srow size according to the number of nonzeros.

 std::shared\_ptr< strategy\_type > copy () override Copy a strategy.

## 46.57.1 Detailed Description

```
template < typename ValueType = default_precision, typename IndexType = int32 > class gko::matrix::Csr < ValueType, IndexType > ::cusparse
```

cusparse is a strategy\_type which uses the sparselib csr.

Note

cusparse is also known to the hip executor which converts between cuda and hip.

## 46.57.2 Member Function Documentation

## 46.57.2.1 clac\_size()

Computes the srow size according to the number of nonzeros.

#### **Parameters**

```
nnz the number of nonzeros
```

### Returns

the size of srow

Implements gko::matrix::Csr< ValueType, IndexType >::strategy\_type.

## 46.57.2.2 copy()

```
template<typename ValueType = default_precision, typename IndexType = int32>
std::shared_ptr<strategy_type> gko::matrix::Csr< ValueType, IndexType >::cusparse::copy ( )
[inline], [override], [virtual]
```

Copy a strategy.

This is a workaround until strategies are revamped, since strategies like automatical do not work when actually shared.

Implements gko::matrix::Csr< ValueType, IndexType >::strategy\_type.

## 46.57.2.3 process()

Computes srow according to row pointers.

#### **Parameters**

mtx_row_ptrs	the row pointers of the matrix
mtx_srow	the srow of the matrix

Implements gko::matrix::Csr< ValueType, IndexType >::strategy\_type.

The documentation for this class was generated from the following file:

ginkgo/core/matrix/csr.hpp

## 46.58 gko::CusparseError Class Reference

CusparseError is thrown when a cuSPARSE routine throws a non-zero error code.

```
#include <ginkgo/core/base/exception.hpp>
```

### **Public Member Functions**

CusparseError (const std::string &file, int line, const std::string &func, int64 error\_code)
 Initializes a cuSPARSE error.

## 46.58.1 Detailed Description

CusparseError is thrown when a cuSPARSE routine throws a non-zero error code.

## 46.58.2 Constructor & Destructor Documentation

### 46.58.2.1 CusparseError()

Initializes a cuSPARSE error.

#### **Parameters**

file	The name of the offending source file
line	The source code line number where the error occurred
func	The name of the cuSPARSE routine that failed
error_code	The resulting cuSPARSE error code

The documentation for this class was generated from the following file:

· ginkgo/core/base/exception.hpp

# 46.59 gko::default\_converter < S, R > Struct Template Reference

Used to convert objects of type S to objects of type R using static\_cast.

```
#include <ginkgo/core/base/math.hpp>
```

### **Public Member Functions**

R operator() (S val)

Converts the object to result type.

## 46.59.1 Detailed Description

```
template < typename S, typename R> struct gko::default_converter < S, R >
```

Used to convert objects of type S to objects of type R using static\_cast.

### **Template Parameters**

S	source type
R	result type

## 46.59.2 Member Function Documentation

## 46.59.2.1 operator()()

Converts the object to result type.

## Parameters

val	the object to convert

#### Returns

the converted object

The documentation for this struct was generated from the following file:

• ginkgo/core/base/math.hpp

# 46.60 gko::deferred\_factory\_parameter< FactoryType > Class Template Reference

Represents a factory parameter of factory type that can either initialized by a pre-existing factory or by passing in a factory\_parameters object whose .on (exec) will be called to instantiate a factory.

```
#include <ginkgo/core/base/abstract_factory.hpp>
```

### **Public Member Functions**

• deferred\_factory\_parameter ()=default

Creates an empty deferred factory parameter.

deferred\_factory\_parameter (std::nullptr\_t)

Creates a deferred factory parameter returning a nullptr.

• template<typename ConcreteFactoryType , std::enable\_if\_t< detail::is\_pointer\_convertible< ConcreteFactoryType, FactoryType > ← ::value > \* = nullptr>

```
deferred factory parameter (std::shared ptr< ConcreteFactoryType > factory)
```

Creates a deferred factory parameter from a preexisting factory with shared ownership.

• template<typename ConcreteFactoryType , typename Deleter , std::enable\_if\_t< detail::is\_pointer\_convertible< ConcreteFactory←

Type, FactoryType >::value > \* = nullptr>

```
deferred_factory_parameter (std::unique_ptr< ConcreteFactoryType, Deleter > factory)
```

Creates a deferred factory parameter by taking ownership of a preexisting factory with unique ownership.

• template<typename ParametersType , typename U = decltype(std::declval<ParametersType>().on( std::shared\_ptr<const Executor>{})), std::enable\_if\_t< detail::is\_pointer\_convertible< typename U::element\_type, FactoryType >::value > \* = nullptr> deferred\_factory\_parameter (ParametersType parameters)

Creates a deferred factory parameter object from a factory\_parameters-like object.

 $\bullet \ \ \mathsf{std} :: \mathsf{shared\_ptr} < \mathsf{FactoryType} > \mathsf{on} \ (\mathsf{std} :: \mathsf{shared\_ptr} < \mathsf{const} \ \mathsf{Executor} > \mathsf{exec}) \ \mathsf{const} \\$ 

Instantiates the deferred parameter into an actual factory.

bool is\_empty () const

Returns true iff the parameter is empty.

## 46.60.1 Detailed Description

```
template<typename FactoryType> class gko::deferred_factory_parameter< FactoryType >
```

Represents a factory parameter of factory type that can either initialized by a pre-existing factory or by passing in a factory\_parameters object whose .on(exec) will be called to instantiate a factory.

**Template Parameters** 

```
FactoryType | the type of factory that can be instantiated from this object.
```

## 46.60.2 Constructor & Destructor Documentation

#### 46.60.2.1 deferred\_factory\_parameter()

Creates a deferred factory parameter object from a factory\_parameters-like object.

To instantiate the actual factory, the parameter's <code>.on(exec)</code> function will be called.

#### 46.60.3 Member Function Documentation

#### 46.60.3.1 on()

Instantiates the deferred parameter into an actual factory.

This will throw if the deferred factory parameter is empty.

The documentation for this class was generated from the following file:

ginkgo/core/base/abstract factory.hpp

# 46.61 gko::batch::matrix::Dense< ValueType > Class Template Reference

Dense is a batch matrix format which explicitly stores all values of the matrix in each of the batches.

```
#include <ginkgo/core/matrix/batch_dense.hpp>
```

## **Public Member Functions**

std::unique\_ptr< unbatch\_type > create\_view\_for\_item (size\_type item\_id)

Creates a mutable view (of gko::matrix::Dense type) of one item of the batch::matrix::Dense<value\_type> object.

• std::unique\_ptr< const unbatch\_type > create\_const\_view\_for\_item (size\_type item\_id) const

Creates a mutable view (of gko::matrix::Dense type) of one item of the batch::matrix::Dense<value\_type> object.

size\_type get\_cumulative\_offset (size\_type batch\_id) const

Get the cumulative storage size offset.

value\_type \* get\_values () noexcept

Returns a pointer to the array of values of the multi-vector.

const value\_type \* get\_const\_values () const noexcept

Returns a pointer to the array of values of the multi-vector.

value\_type & at (size\_type batch\_id, size\_type row, size\_type col)

Returns a single element for a particular batch item.

value\_type at (size\_type batch\_id, size\_type row, size\_type col) const

Returns a single element for a particular batch item.

• ValueType & at (size\_type batch\_id, size\_type idx) noexcept

Returns a single element for a particular batch item.

• ValueType at (size\_type batch\_id, size\_type idx) const noexcept

Returns a single element for a particular batch item.

value type \* get values for item (size type batch id) noexcept

Returns a pointer to the array of values of the matrix for a specific batch item.

const value\_type \* get\_const\_values\_for\_item (size\_type batch\_id) const noexcept

Returns a pointer to the array of values of the matrix for a specific batch item.

size\_type get\_num\_stored\_elements () const noexcept

Returns the number of elements explicitly stored in the batch matrix, cumulative across all the batch items.

• size\_type get\_num\_elements\_per\_item () const noexcept

Returns the number of stored elements in each batch item.

Dense \* apply (ptr\_param < const MultiVector < value\_type >> b, ptr\_param < MultiVector < value\_type >> x)

Apply the matrix to a multi-vector.

Dense \* apply (ptr\_param< const MultiVector< value\_type >> alpha, ptr\_param< const MultiVector< value\_type >> b, ptr\_param< const MultiVector< value\_type >> beta, ptr\_param< MultiVector< value\_
 type >> x)

Apply the matrix to a multi-vector with a linear combination of the given input vector.

- const Dense \* apply (ptr\_param< const MultiVector< value\_type >> b, ptr\_param< MultiVector< value\_
   type >> x) const
- const Dense \* apply (ptr\_param< const MultiVector< value\_type >> alpha, ptr\_param< const MultiVector< value\_type >> beta, ptr\_param< MultiVector< value\_type >> beta, ptr\_param< MultiVector< value\_type >> x) const
- void scale (const array< value\_type > &row\_scale, const array< value\_type > &col\_scale)

Performs in-place row and column scaling for this matrix.

void scale\_add (ptr\_param< const MultiVector< value\_type >> alpha, ptr\_param< const batch::matrix::Dense</li>
 value\_type >> b)

Performs the operation this = alpha\*this + b.

 void add\_scaled\_identity (ptr\_param< const MultiVector< value\_type >> alpha, ptr\_param< const MultiVector< value type >> beta)

Performs the operation this = alpha\*I + beta\*this.

## **Static Public Member Functions**

static std::unique\_ptr< Dense > create (std::shared\_ptr< const Executor > exec, const batch\_dim< 2 > &size=batch\_dim< 2 >{})

Creates an uninitialized Dense matrix of the specified size.

static std::unique\_ptr< Dense > create (std::shared\_ptr< const Executor > exec, const batch\_dim< 2 > &size, array< value type > values)

Creates a Dense matrix from an already allocated (and initialized) array.

template<typename InputValueType >

static std::unique\_ptr< Dense > create (std::shared\_ptr< const Executor > exec, const batch\_dim< 2 > &size, std::initializer\_list< InputValueType > values)

create(std::shared\_ptr<const Executor>,

• static std::unique\_ptr< const Dense > create\_const (std::shared\_ptr< const Executor > exec, const batch\_dim< 2 > &sizes, gko::detail::const\_array\_view< ValueType > &&values)

Creates a constant (immutable) batch dense matrix from a constant array.

## 46.61.1 Detailed Description

```
template<typename ValueType = default_precision> class gko::batch::matrix::Dense< ValueType >
```

Dense is a batch matrix format which explicitly stores all values of the matrix in each of the batches.

The values in each of the batches are stored in row-major format (values belonging to the same row appear consecutive in the memory and the values of each batch item are also stored consecutively in memory).

Note

Though the storage layout is the same as the multi-vector object, the class semantics and the operations it aims to provide are different. Hence it is recommended to create multi-vector objects if the user means to view the data as a set of vectors.

## **Template Parameters**

ValueType precision of matrix elements	
--	--

## 46.61.2 Member Function Documentation

## 46.61.2.1 add\_scaled\_identity()

Performs the operation this = alpha\*I + beta\*this.

#### **Parameters**

alpha	the scalar for identity
beta	the scalar to multiply this matrix

## Note

Performs the operation in-place for this batch matrix

## 46.61.2.2 apply() [1/4]

Apply the matrix to a multi-vector with a linear combination of the given input vector.

Represents the matrix vector multiplication, x = alpha \* A

• b + beta \* x, where x and b are both multi-vectors.

## **Parameters**

alpha	the scalar to scale the matrix-vector product with
b	the multi-vector to be applied to
beta	the scalar to scale the x vector with
Х	the output multi-vector

### 46.61.2.3 apply() [2/4]

## 46.61.2.4 apply() [3/4]

Apply the matrix to a multi-vector.

Represents the matrix vector multiplication, x = A \* b, where x and b are both multi-vectors.

### **Parameters**

	the multi-vector to be applied to
X	the output multi-vector

#### 46.61.2.5 apply() [4/4]

```
template<typename ValueType = default_precision>
const Dense* gko::batch::matrix::Dense< ValueType >::apply (
    ptr_param< const MultiVector< value_type >> b,
    ptr_param< MultiVector< value_type >> x ) const
```

## 46.61.2.6 at() [1/4]

Returns a single element for a particular batch item.

#### **Parameters**

batch⊷ _id	the batch item index to be queried
row	the row of the requested element
col	the column of the requested element

#### Note

the method has to be called on the same Executor the matrix is stored at (e.g. trying to call this method on a GPU Dense object from the OMP may result in incorrect behaviour)

References gko::array< ValueType >::get\_const\_data().

## 46.61.2.7 at() [2/4]

Returns a single element for a particular batch item.

Useful for iterating across all elements of the matrix. However, it is less efficient than the two-parameter variant of this method.

## **Parameters**

batch←	the batch item index to be queried
_id	
idx	a linear index of the requested element

## Note

the method has to be called on the same Executor the matrix is stored at (e.g. trying to call this method on a GPU Dense object from the OMP may result in incorrect behaviour)

References gko::array< ValueType >::get\_data().

## 46.61.2.8 at() [3/4]

```
template<typename ValueType = default_precision>
value_type& gko::batch::matrix::Dense< ValueType >::at (
```

```
size_type batch_id,
size_type row,
size_type col ) [inline]
```

Returns a single element for a particular batch item.

#### **Parameters**

batch⊷ _id	the batch item index to be queried
row	the row of the requested element
col	the column of the requested element

#### Note

the method has to be called on the same Executor the matrix is stored at (e.g. trying to call this method on a GPU Dense object from the OMP may result in incorrect behaviour)

References gko::array< ValueType >::get\_data().

## 46.61.2.9 at() [4/4]

Returns a single element for a particular batch item.

#### **Parameters**

batch⊷	the batch item index to be queried
_id	
row	the row of the requested element
col	the column of the requested element

#### Note

the method has to be called on the same Executor the matrix is stored at (e.g. trying to call this method on a GPU Dense object from the OMP may result in incorrect behaviour)

References gko::array< ValueType >::get\_const\_data().

## 46.61.2.10 create() [1/3]

Creates a Dense matrix from an already allocated (and initialized) array.

#### **Parameters**

exec	Executor associated to the matrix
size	sizes of the batch matrices in a batch_dim object
values	array of matrix values

#### Note

If values is not an rvalue, not an array of ValueType, or is on the wrong executor, an internal copy will be created, and the original array data will not be used in the matrix.

#### Returns

A smart pointer to the newly created matrix.

### 46.61.2.11 create() [2/3]

#### 46.61.2.12 create() [3/3]

Creates an uninitialized Dense matrix of the specified size.

References gko::batch::matrix::Dense< ValueType >::create().

#### **Parameters**

exec	Executor associated to the matrix
size	size of the matrix

#### Returns

A smart pointer to the newly created matrix.

Referenced by gko::batch::matrix::Dense< ValueType >::create().

## 46.61.2.13 create\_const()

Creates a constant (immutable) batch dense matrix from a constant array.

#### **Parameters**

exec	the executor to create the matrix on
size	the dimensions of the matrix
values	the value array of the matrix

#### Returns

A smart pointer to the constant matrix wrapping the input array (if it resides on the same executor as the matrix) or a copy of the array on the correct executor.

A smart pointer to the newly created matrix.

## 46.61.2.14 create\_const\_view\_for\_item()

Creates a mutable view (of gko::matrix::Dense type) of one item of the batch::matrix::Dense < value\_type > object.

Does not perform any deep copies, but only returns a view of the data.

#### **Parameters**

item⊷	The index of the batch item
_id	

#### Returns

a gko::matrix::Dense object with the data from the batch item at the given index.

## 46.61.2.15 create\_view\_for\_item()

Creates a mutable view (of gko::matrix::Dense type) of one item of the batch::matrix::Dense<value\_type> object.

Does not perform any deep copies, but only returns a view of the data.

#### **Parameters**

item←	The index of the batch item
_id	

#### Returns

a gko::matrix::Dense object with the data from the batch item at the given index.

## 46.61.2.16 get\_const\_values()

```
template<typename ValueType = default_precision>
const value_type* gko::batch::matrix::Dense< ValueType >::get_const_values ( ) const [inline],
[noexcept]
```

Returns a pointer to the array of values of the multi-vector.

#### Returns

the pointer to the array of values

### Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

References gko::array< ValueType >::get\_const\_data().

## 46.61.2.17 get\_const\_values\_for\_item()

Returns a pointer to the array of values of the matrix for a specific batch item.

#### **Parameters**

batch←	the id of the batch item.
_id	

#### Returns

the pointer to the array of values

#### Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

## 46.61.2.18 get\_cumulative\_offset()

Get the cumulative storage size offset.

#### **Parameters**

batch⊷	the batch id
_id	

### Returns

the cumulative offset

Referenced by gko::batch::matrix::Dense < ValueType >::get\_const\_values\_for\_item(), and gko::batch::matrix:: $\leftarrow$  Dense < ValueType >::get\_values\_for\_item().

## 46.61.2.19 get\_num\_elements\_per\_item()

```
template<typename ValueType = default_precision>
size_type gko::batch::matrix::Dense< ValueType >::get_num_elements_per_item ( ) const [inline],
[noexcept]
```

Returns the number of stored elements in each batch item.

#### Returns

the number of stored elements per batch item.

 $References\ gko::batch::matrix::Dense<\ Value\ Type>::get\_num\_stored\_elements().$ 

### 46.61.2.20 get\_num\_stored\_elements()

```
template<typename ValueType = default_precision>
size_type gko::batch::matrix::Dense< ValueType >::get_num_stored_elements ( ) const [inline],
[noexcept]
```

Returns the number of elements explicitly stored in the batch matrix, cumulative across all the batch items.

### Returns

the number of elements explicitly stored in the vector, cumulative across all the batch items

References gko::array< ValueType >::get\_size().

Referenced by gko::batch::matrix::Dense< ValueType >::get\_num\_elements\_per\_item().

## 46.61.2.21 get\_values()

```
template<typename ValueType = default_precision>
value_type* gko::batch::matrix::Dense< ValueType >::get_values ( ) [inline], [noexcept]
```

Returns a pointer to the array of values of the multi-vector.

## Returns

the pointer to the array of values

References gko::array< ValueType >::get\_data().

## 46.61.2.22 get\_values\_for\_item()

Returns a pointer to the array of values of the matrix for a specific batch item.

### **Parameters**

batch⊷	the id of the batch item.
_id	

## Returns

the pointer to the array of values

References gko::batch::matrix::Dense< ValueType >::get\_cumulative\_offset(), and gko::array< ValueType >
::get\_data().

## 46.61.2.23 scale()

Performs in-place row and column scaling for this matrix.

#### **Parameters**

row_scale	the row scalars
col_scale	the column scalars

## 46.61.2.24 scale\_add()

Performs the operation this = alpha\*this + b.

#### **Parameters**

alpha	the scalar to multiply this matrix
b	the matrix to add

## Note

Performs the operation in-place for this batch matrix

The documentation for this class was generated from the following file:

• ginkgo/core/matrix/batch\_dense.hpp

# 46.62 gko::matrix::Dense< ValueType > Class Template Reference

Dense is a matrix format which explicitly stores all values of the matrix.

```
#include <ginkgo/core/matrix/dense.hpp>
```

### **Public Member Functions**

• std::unique ptr< LinOp > transpose () const override

Returns a LinOp representing the transpose of the Transposable object.

std::unique\_ptr< LinOp > conj\_transpose () const override

Returns a LinOp representing the conjugate transpose of the Transposable object.

void transpose (ptr param < Dense > output) const

Writes the transposed matrix into the given output matrix.

void conj\_transpose (ptr\_param< Dense > output) const

Writes the conjugate-transposed matrix into the given output matrix.

void fill (const ValueType value)

Fill the dense matrix with a given value.

std::unique\_ptr< Dense > permute (ptr\_param< const Permutation< int32 >> permutation, permute\_mode mode=permute\_mode::symmetric) const

Creates a permuted copy A' of this matrix A with the given permutation P.

- std::unique\_ptr< Dense > permute (ptr\_param< const Permutation< int64 >> permutation, permute\_mode mode=permute mode::symmetric) const
- void permute (ptr\_param< const Permutation< int32 >> permutation, ptr\_param< Dense > output, permute\_mode mode) const

Overload of permute(ptr\_param<const Permutation<int32>>, permute\_mode) that writes the permuted copy into an existing Dense matrix.

- void permute (ptr\_param< const Permutation< int64 >> permutation, ptr\_param< Dense > output, permute mode mode) const
- std::unique\_ptr< Dense > permute (ptr\_param< const Permutation< int32 >> row\_permutation, ptr\_param< const Permutation< int32 >> column\_permutation, bool invert=false) const

Creates a non-symmetrically permuted copy A' of this matrix A with the given row and column permutations P and Q.

- std::unique\_ptr< Dense > permute (ptr\_param< const Permutation< int64 >> row\_permutation, ptr param< const Permutation< int64 >> column permutation, bool invert=false) const
- void permute (ptr\_param < const Permutation < int32 >> row\_permutation, ptr\_param < const Permutation < int32 >> column\_permutation, ptr\_param < Dense > output, bool invert=false) const

 $\label{eq:const_permute} Overload \quad of \quad permute(\textit{ptr\_param} < \textit{const} \quad Permutation < \textit{int32} >>, \quad \textit{ptr\_param} < \textit{const} \quad Permutation < \textit{int32} >>, \\ permute\_mode) \ that \ \textit{writes} \ the \ permuted \ \textit{copy} \ \textit{into} \ \textit{an existing Dense matrix}.$ 

- void permute (ptr\_param < const Permutation < int64 >> row\_permutation, ptr\_param < const Permutation < int64 >> column\_permutation, ptr\_param < Dense > output, bool invert=false) const
- std::unique\_ptr< Dense > scale\_permute (ptr\_param< const ScaledPermutation< value\_type, int32 >> permutation, permute\_mode mode=permute\_mode::symmetric) const

Creates a scaled and permuted copy of this matrix.

- std::unique\_ptr< Dense > scale\_permute (ptr\_param< const ScaledPermutation< value\_type, int64 >> permutation, permute\_mode mode=permute\_mode::symmetric) const
- void scale\_permute (ptr\_param< const ScaledPermutation< value\_type, int32 >> permutation, ptr\_param
   Dense > output, permute mode mode) const

Overload of scale\_permute(ptr\_param<const ScaledPermutation<value\_type, int32>>, permute\_mode) that writes the permuted copy into an existing Dense matrix.

- void scale\_permute (ptr\_param< const ScaledPermutation< value\_type, int64 >> permutation, ptr\_param
   Dense > output, permute\_mode mode) const
- std::unique\_ptr< Dense > scale\_permute (ptr\_param< const ScaledPermutation< value\_type, int32 >> row\_permutation, ptr\_param< const ScaledPermutation< value\_type, int32 >> column\_permutation, bool invert=false) const

Creates a scaled and permuted copy of this matrix.

• std::unique\_ptr< Dense > scale\_permute (ptr\_param< const ScaledPermutation< value\_type, int64 >> row\_permutation, ptr\_param< const ScaledPermutation< value\_type, int64 >> column\_permutation, bool invert=false) const

void scale\_permute (ptr\_param< const ScaledPermutation< value\_type, int32 >> row\_permutation, ptr\_param< const ScaledPermutation< value\_type, int32 >> column\_permutation, ptr\_param< Dense > output, bool invert=false) const

Overload of scale\_permute(ptr\_param<const ScaledPermutation<value\_type, int32>>, ptr\_param<const ScaledPermutation<value\_type, int32>>, bool) that writes the permuted copy into an existing Dense matrix.

- void scale\_permute (ptr\_param< const ScaledPermutation< value\_type, int64 >> row\_permutation, ptr\_param< const ScaledPermutation< value\_type, int64 >> column\_permutation, ptr\_param< Dense > output, bool invert=false) const
- std::unique\_ptr< LinOp > permute (const array< int32 > \*permutation\_indices) const override

  Returns a LinOp representing the symmetric row and column permutation of the Permutable object.
- std::unique\_ptr< LinOp > permute (const array< int64 > \*permutation\_indices) const override

  Returns a LinOp representing the symmetric row and column permutation of the Permutable object.
- void permute (const array< int32 > \*permutation\_indices, ptr\_param< Dense > output) const

  Writes the symmetrically permuted matrix into the given output matrix.
- void permute (const array< int64 > \*permutation indices, ptr param< Dense > output) const
- std::unique\_ptr< LinOp > inverse\_permute (const array< int32 > \*permutation\_indices) const override

  Returns a LinOp representing the symmetric inverse row and column permutation of the Permutable object.
- std::unique\_ptr< LinOp > inverse\_permute (const array< int64 > \*permutation\_indices) const override

  Returns a LinOp representing the symmetric inverse row and column permutation of the Permutable object.
- void inverse\_permute (const array< int32 > \*permutation\_indices, ptr\_param< Dense > output) const Writes the inverse symmetrically permuted matrix into the given output matrix.
- void inverse permute (const array< int64 > \*permutation indices, ptr param< Dense > output) const
- std::unique\_ptr< LinOp > row\_permute (const array< int32 > \*permutation\_indices) const override

  Returns a LinOp representing the row permutation of the Permutable object.
- std::unique\_ptr< LinOp > row\_permute (const array< int64 > \*permutation\_indices) const override
   Returns a LinOp representing the row permutation of the Permutable object.
- void row\_permute (const array< int32 > \*permutation\_indices, ptr\_param< Dense > output) const Writes the row-permuted matrix into the given output matrix.
- void row\_permute (const array < int64 > \*permutation\_indices, ptr\_param < Dense > output) const
- std::unique\_ptr< Dense > row\_gather (const array< int32 > \*gather\_indices) const

• std::unique ptr< Dense > row gather (const array< int64 > \*gather indices) const

- Create a Dense matrix consisting of the given rows from this matrix.
- Create a Dense matrix consisting of the given rows from this matrix.
- void row\_gather (const array< int32 > \*gather\_indices, ptr\_param< LinOp > row\_collection) const
   Copies the given rows from this matrix into row\_collection
- void row\_gather (const array< int64 > \*gather\_indices, ptr\_param< LinOp > row\_collection) const
- void row\_gather (ptr\_param < const LinOp > alpha, const array < int32 > \*gather\_indices, ptr\_param < const LinOp > beta, ptr\_param < LinOp > row\_collection) const
  - Copies the given rows from this matrix into row\_collection with scaling.
- void row\_gather (ptr\_param < const LinOp > alpha, const array < int64 > \*gather\_indices, ptr\_param < const LinOp > beta, ptr\_param < LinOp > row\_collection) const
- std::unique\_ptr< LinOp > column\_permute (const array< int32 > \*permutation\_indices) const override
   Returns a LinOp representing the column permutation of the Permutable object.
- std::unique\_ptr< LinOp > column\_permute (const array< int64 > \*permutation\_indices) const override

  Returns a LinOp representing the column permutation of the Permutable object.
- void column\_permute (const array< int32 > \*permutation\_indices, ptr\_param< Dense > output) const Writes the column-permuted matrix into the given output matrix.
- void column\_permute (const array< int64 > \*permutation\_indices, ptr\_param< Dense > output) const
- std::unique\_ptr< LinOp > inverse\_row\_permute (const array< int32 > \*permutation\_indices) const override

  Returns a LinOp representing the row permutation of the inverse permuted object.
- std::unique\_ptr< LinOp > inverse\_row\_permute (const array< int64 > \*permutation\_indices) const override

  Returns a LinOp representing the row permutation of the inverse permuted object.

- void inverse\_row\_permute (const array< int32 > \*permutation\_indices, ptr\_param< Dense > output) const Writes the inverse row-permuted matrix into the given output matrix.
- void inverse\_row\_permute (const array< int64 > \*permutation\_indices, ptr\_param< Dense > output) const
- std::unique\_ptr< LinOp > inverse\_column\_permute (const array< int32 > \*permutation\_indices) const over-ride

Returns a LinOp representing the row permutation of the inverse permuted object.

 std::unique\_ptr< LinOp > inverse\_column\_permute (const array< int64 > \*permutation\_indices) const override

Returns a LinOp representing the row permutation of the inverse permuted object.

void inverse\_column\_permute (const array< int32 > \*permutation\_indices, ptr\_param< Dense > output)
 const

Writes the inverse column-permuted matrix into the given output matrix.

- void inverse\_column\_permute (const array< int64 > \*permutation\_indices, ptr\_param< Dense > output)
- std::unique ptr< Diagonal< ValueType > > extract diagonal () const override

Extracts the diagonal entries of the matrix into a vector.

void extract diagonal (ptr param< Diagonal< ValueType >> output) const

Writes the diagonal of this matrix into an existing diagonal matrix.

• std::unique ptr< absolute type > compute absolute () const override

Gets the AbsoluteLinOp.

void compute absolute (ptr param< absolute type > output) const

Writes the absolute values of this matrix into an existing matrix.

· void compute absolute inplace () override

Compute absolute inplace on each element.

std::unique ptr< complex type > make complex () const

Creates a complex copy of the original matrix.

void make\_complex (ptr\_param< complex\_type > result) const

Writes a complex copy of the original matrix to a given complex matrix.

std::unique\_ptr< real\_type > get\_real () const

Creates a new real matrix and extracts the real part of the original matrix into that.

void get\_real (ptr\_param < real\_type > result) const

Extracts the real part of the original matrix into a given real matrix.

std::unique\_ptr< real\_type > get\_imag () const

Creates a new real matrix and extracts the imaginary part of the original matrix into that.

void get\_imag (ptr\_param< real\_type > result) const

Extracts the imaginary part of the original matrix into a given real matrix.

value\_type \* get\_values () noexcept

Returns a pointer to the array of values of the matrix.

• const value\_type \* get\_const\_values () const noexcept

Returns a pointer to the array of values of the matrix.

size\_type get\_stride () const noexcept

Returns the stride of the matrix.

• size\_type get\_num\_stored\_elements () const noexcept

Returns the number of elements explicitly stored in the matrix.

value type & at (size type row, size type col) noexcept

Returns a single element of the matrix.

value\_type at (size\_type row, size\_type col) const noexcept

Returns a single element of the matrix.

ValueType & at (size\_type idx) noexcept

Returns a single element of the matrix.

ValueType at (size\_type idx) const noexcept

Returns a single element of the matrix.

void scale (ptr\_param< const LinOp > alpha)

Scales the matrix with a scalar (aka: BLAS scal).

void inv\_scale (ptr\_param< const LinOp > alpha)

Scales the matrix with the inverse of a scalar.

void add\_scaled (ptr\_param< const LinOp > alpha, ptr\_param< const LinOp > b)

Adds b scaled by alpha to the matrix (aka: BLAS axpy).

void sub\_scaled (ptr\_param< const LinOp > alpha, ptr\_param< const LinOp > b)

Subtracts b scaled by alpha from the matrix (aka: BLAS axpy).

void compute\_dot (ptr\_param < const LinOp > b, ptr\_param < LinOp > result) const

Computes the column-wise dot product of this matrix and b.

• void compute\_dot (ptr\_param< const LinOp > b, ptr\_param< LinOp > result, array< char > &tmp) const Computes the column-wise dot product of this matrix and b.

void compute\_conj\_dot (ptr\_param< const LinOp > b, ptr\_param< LinOp > result) const

Computes the column-wise dot product of conj (this matrix) and b.

void compute\_conj\_dot (ptr\_param< const LinOp > b, ptr\_param< LinOp > result, array< char > &tmp)
 const

Computes the column-wise dot product of conj(this matrix) and b.

void compute\_norm2 (ptr\_param< LinOp > result) const

Computes the column-wise Euclidean ( $L^2$ ) norm of this matrix.

void compute\_norm2 (ptr\_param < LinOp > result, array < char > &tmp) const

Computes the column-wise Euclidean ( $L^{\wedge}$ 2) norm of this matrix.

void compute norm1 (ptr param< LinOp > result) const

Computes the column-wise ( $L^{\wedge}$ 1) norm of this matrix.

void compute\_norm1 (ptr\_param < LinOp > result, array < char > &tmp) const

Computes the column-wise ( $L^{\wedge}$ 1) norm of this matrix.

void compute\_squared\_norm2 (ptr\_param< LinOp > result) const

Computes the square of the column-wise Euclidean ( $L^2$ ) norm of this matrix.

• void compute\_squared\_norm2 (ptr\_param< LinOp > result, array< char > &tmp) const

Computes the square of the column-wise Euclidean ( $L^{\wedge}2$ ) norm of this matrix.

void compute\_mean (ptr\_param< LinOp > result) const

Computes the column-wise arithmetic mean of this matrix.

void compute\_mean (ptr\_param< LinOp > result, array< char > &tmp) const

Computes the column-wise arithmetic mean of this matrix.

std::unique\_ptr< Dense > create\_submatrix (const span &rows, const span &columns, const size\_type stride)

Create a submatrix from the original matrix.

• std::unique\_ptr< Dense > create\_submatrix (const span &rows, const span &columns)

Create a submatrix from the original matrix.

std::unique\_ptr< real\_type > create\_real\_view ()

Create a real view of the (potentially) complex original matrix.

• std::unique ptr< const real type > create real view () const

Create a real view of the (potentially) complex original matrix.

Dense & operator= (const Dense &)

Copy-assigns a Dense matrix.

Dense & operator= (Dense &&)

Move-assigns a Dense matrix.

• Dense (const Dense &)

Copy-constructs a Dense matrix.

Dense (Dense &&)

Move-constructs a Dense matrix.

### Static Public Member Functions

static std::unique\_ptr< Dense > create\_with\_config\_of (ptr\_param< const Dense > other)

Creates a Dense matrix with the same size and stride as another Dense matrix.

static std::unique\_ptr< Dense > create\_with\_type\_of (ptr\_param< const Dense > other, std::shared\_ptr< const Executor > exec, const dim< 2 > &size=dim< 2 > {})

Creates a Dense matrix with the same type as another Dense matrix but on a different executor and with a different size.

- static std::unique\_ptr< Dense > create\_with\_type\_of (ptr\_param< const Dense > other, std::shared\_ptr< const Executor > exec, const dim< 2 > &size, size type stride)
- static std::unique\_ptr< Dense > create\_with\_type\_of (ptr\_param< const Dense > other, std::shared\_ptr< const Executor > exec, const dim< 2 > &size, const dim< 2 > &local\_size, size\_type stride)
- static std::unique\_ptr< Dense > create\_view\_of (ptr\_param< Dense > other)

Creates a Dense matrix, where the underlying array is a view of another Dense matrix' array.

static std::unique\_ptr< const Dense > create\_const\_view\_of (ptr\_param< const Dense > other)

Creates a immutable Dense matrix, where the underlying array is a view of another Dense matrix' array.

 static std::unique\_ptr< Dense > create (std::shared\_ptr< const Executor > exec, const dim< 2 > &size={}, size\_type stride=0)

Creates an uninitialized Dense matrix of the specified size.

 static std::unique\_ptr< Dense > create (std::shared\_ptr< const Executor > exec, const dim< 2 > &size, array< value\_type > values, size\_type stride)

Creates a Dense matrix from an already allocated (and initialized) array.

• template<typename InputValueType >

static std::unique\_ptr< Dense > create (std::shared\_ptr< const Executor > exec, const dim< 2 > &size, std::initializer list< InputValueType > values, size type stride)

create(std::shared\_ptr<const Executor>,

static std::unique\_ptr< const Dense > create\_const (std::shared\_ptr< const Executor > exec, const dim
 2 > &size, gko::detail::const\_array\_view< ValueType > &&values, size\_type stride)

Creates a constant (immutable) Dense matrix from a constant array.

## 46.62.1 Detailed Description

 $\label{template} \mbox{typename ValueType = default\_precision} > \\ \mbox{class gko::matrix::Dense} < \mbox{ValueType} > \\$ 

Dense is a matrix format which explicitly stores all values of the matrix.

The values are stored in row-major format (values belonging to the same row appear consecutive in the memory). Optionally, rows can be padded for better memory access.

#### **Template Parameters**

ValueType precision of matrix elements

Note

While this format is not very useful for storing sparse matrices, it is often suitable to store vectors, and sets of vectors.

## 46.62.2 Constructor & Destructor Documentation

### 46.62.2.1 Dense() [1/2]

Copy-constructs a Dense matrix.

Inherits executor and dimensions, but copies data without padding.

## 46.62.2.2 Dense() [2/2]

Move-constructs a Dense matrix.

Inherits executor, dimensions and data with padding. The moved-from object is empty (0x0 with empty Array).

## 46.62.3 Member Function Documentation

## 46.62.3.1 add\_scaled()

Adds b scaled by alpha to the matrix (aka: BLAS axpy).

## **Parameters**

alpha	alpha If alpha is 1x1 Dense matrix, the entire matrix is scaled by alpha. If it is a Dense row vector of value	
	then i-th column of the matrix is scaled with the i-th element of alpha (the number of columns of alpha	
	has to match the number of columns of the matrix).	
b	a matrix of the same dimension as this	

## 46.62.3.2 at() [1/4]

Returns a single element of the matrix.

Useful for iterating across all elements of the matrix. However, it is less efficient than the two-parameter variant of this method.

#### **Parameters**

```
idx a linear index of the requested element (ignoring the stride)
```

#### Note

the method has to be called on the same Executor the matrix is stored at (e.g. trying to call this method on a GPU matrix from the OMP results in a runtime error)

## 46.62.3.3 at() [2/4]

Returns a single element of the matrix.

Useful for iterating across all elements of the matrix. However, it is less efficient than the two-parameter variant of this method.

### **Parameters**

```
idx a linear index of the requested element (ignoring the stride)
```

## Note

the method has to be called on the same Executor the matrix is stored at (e.g. trying to call this method on a GPU matrix from the OMP results in a runtime error)

## 46.62.3.4 at() [3/4]

Returns a single element of the matrix.

### Parameters

row	the row of the requested element
col	the column of the requested element

#### Note

the method has to be called on the same Executor the matrix is stored at (e.g. trying to call this method on a GPU matrix from the OMP results in a runtime error)

### 46.62.3.5 at() [4/4]

Returns a single element of the matrix.

#### **Parameters**

row the row of the requested element	
col	the column of the requested element

#### Note

the method has to be called on the same Executor the matrix is stored at (e.g. trying to call this method on a GPU matrix from the OMP results in a runtime error)

Referenced by gko::initialize().

#### 46.62.3.6 column\_permute() [1/4]

Returns a LinOp representing the column permutation of the Permutable object.

In the resulting LinOp, the column  $\mathtt{i}$  contains the input column  $\mathtt{perm}[\mathtt{i}]$ .

From the linear algebra perspective, with  $P_{ij} = \delta_{i\pi(i)}$ , this represents the operation  $AP^T$ .

#### **Parameters**

_		
	permutation_indices	the array of indices containing the permutation order perm.

## Returns

a pointer to the new column permuted object

Implements gko::Permutable < int32 >.

# 46.62.3.7 column\_permute() [2/4]

Writes the column-permuted matrix into the given output matrix.

# **Parameters**

permutation_indices	The array containing permutation indices. It must have this->get_size() [1] elements.
output	The output matrix. It must have the dimensions this->get_size()

#### See also

Dense::column\_permute(const array<int32>\*)

# 46.62.3.8 column\_permute() [3/4]

Returns a LinOp representing the column permutation of the Permutable object.

In the resulting LinOp, the column i contains the input column perm[i].

From the linear algebra perspective, with  $P_{ij} = \delta_{i\pi(i)}$ , this represents the operation  $AP^T$ .

## **Parameters**

permutation_indices	the array of indices containing the permutation order perm.

# Returns

a pointer to the new column permuted object

Implements gko::Permutable < int64 >.

# 46.62.3.9 column\_permute() [4/4]

# 46.62.3.10 compute\_absolute() [1/2]

```
template<typename ValueType = default_precision>
std::unique_ptr<absolute_type> gko::matrix::Dense< ValueType >::compute_absolute ( ) const
[override], [virtual]
```

Gets the AbsoluteLinOp.

Returns

a pointer to the new absolute object

Implements gko::EnableAbsoluteComputation< remove\_complex< Dense< ValueType >> >.

# 46.62.3.11 compute\_absolute() [2/2]

Writes the absolute values of this matrix into an existing matrix.

# **Parameters**

output	The output matrix. Its size must match the size of this matrix.
--------	---

See also

Dense::compute\_absolute()

# 46.62.3.12 compute\_conj\_dot() [1/2]

Computes the column-wise dot product of conj (this matrix) and b.

#### **Parameters**

	b	a Dense matrix of same dimension as this
ſ	result	a Dense row vector, used to store the dot product (the number of column in the vector must match the
		number of columns of this)

# 46.62.3.13 compute\_conj\_dot() [2/2]

Computes the column-wise dot product of conj (this matrix) and b.

#### **Parameters**

b	a Dense matrix of same dimension as this
result	a Dense row vector, used to store the dot product (the number of column in the vector must match the
	number of columns of this)
tmp	the temporary storage to use for partial sums during the reduction computation. It may be resized
	and/or reset to the correct executor.

# 46.62.3.14 compute\_dot() [1/2]

Computes the column-wise dot product of this matrix and  ${\tt b.}$ 

# **Parameters**

b	a Dense matrix of same dimension as this
result	a Dense row vector, used to store the dot product (the number of column in the vector must match the
	number of columns of this)

# 46.62.3.15 compute\_dot() [2/2]

```
template<typename ValueType = default_precision>
void gko::matrix::Dense< ValueType >::compute_dot (
```

```
ptr_param< const LinOp > b,
ptr_param< LinOp > result,
array< char > & tmp ) const
```

Computes the column-wise dot product of this matrix and b.

# **Parameters**

b	a Dense matrix of same dimension as this
result	a Dense row vector, used to store the dot product (the number of column in the vector must match the number of columns of this)
tmp	the temporary storage to use for partial sums during the reduction computation. It may be resized and/or reset to the correct executor.

# 46.62.3.16 compute\_mean() [1/2]

Computes the column-wise arithmetic mean of this matrix.

# **Parameters**

result	a Dense row vector, used to store the mean (the number of columns in the vector must match the
	number of columns of this)

# 46.62.3.17 compute\_mean() [2/2]

Computes the column-wise arithmetic mean of this matrix.

result	a Dense row vector, used to store the mean (the number of columns in the vector must match the number of columns of this)
tmp	the temporary storage to use for partial sums during the reduction computation. It may be resized and/or reset to the correct executor.

# 46.62.3.18 compute\_norm1() [1/2]

Computes the column-wise ( $L^{\wedge}1$ ) norm of this matrix.

# **Parameters**

result

a Dense row vector, used to store the norm (the number of columns in the vector must match the number of columns of this)

# 46.62.3.19 compute\_norm1() [2/2]

Computes the column-wise ( $L^{\wedge}1$ ) norm of this matrix.

# **Parameters**

result	a Dense row vector, used to store the norm (the number of columns in the vector must match the number of columns of this)
tmp	the temporary storage to use for partial sums during the reduction computation. It may be resized
	and/or reset to the correct executor.

# 46.62.3.20 compute\_norm2() [1/2]

Computes the column-wise Euclidean ( $L^2$ ) norm of this matrix.

# **Parameters**

result

a Dense row vector, used to store the norm (the number of columns in the vector must match the number of columns of this)

# 46.62.3.21 compute\_norm2() [2/2]

Computes the column-wise Euclidean ( $L^2$ ) norm of this matrix.

#### **Parameters**

result	a Dense row vector, used to store the norm (the number of columns in the vector must match the number of columns of this)
tmp	the temporary storage to use for partial sums during the reduction computation. It may be resized and/or reset to the correct executor.

# 46.62.3.22 compute squared norm2() [1/2]

Computes the square of the column-wise Euclidean ( $L^2$ ) norm of this matrix.

# **Parameters**

result	a Dense row vector, used to store the norm (the number of columns in the vector must match the
	number of columns of this)

# 46.62.3.23 compute\_squared\_norm2() [2/2]

Computes the square of the column-wise Euclidean ( $L^{\wedge}2$ ) norm of this matrix.

result	a Dense row vector, used to store the norm (the number of columns in the vector must match the number of columns of this)	
tmp	the temporary storage to use for partial sums during the reduction computation. It may be resized and/or reset to the correct executor.	

# 46.62.3.24 conj\_transpose() [1/2]

```
template<typename ValueType = default_precision>
std::unique_ptr<LinOp> gko::matrix::Dense< ValueType >::conj_transpose ( ) const [override],
[virtual]
```

Returns a LinOp representing the conjugate transpose of the Transposable object.

# Returns

a pointer to the new conjugate transposed object

Implements gko::Transposable.

# 46.62.3.25 conj\_transpose() [2/2]

Writes the conjugate-transposed matrix into the given output matrix.

#### **Parameters**

```
        output
        The output matrix. It must have the dimensions gko::transpose(this->get_size())
```

# 46.62.3.26 create() [1/3]

Creates a Dense matrix from an already allocated (and initialized) array.

exec	Executor associated to the matrix	
size	size of the matrix	
values	array of matrix values	
stride	stride of the rows (i.e. offset between the first elements of two consecutive rows, expressed as the number of matrix elements)	

#### Note

If values is not an rvalue, not an array of ValueType, or is on the wrong executor, an internal copy will be created, and the original array data will not be used in the matrix.

#### Returns

A smart pointer to the newly created matrix.

# 46.62.3.27 create() [2/3]

create(std::shared\_ptr<const Executor>,

create(std::shared\_ptr<const Executor>, const dim<2>&, array<value\_type>, size\_type)

# 46.62.3.28 create() [3/3]

Creates an uninitialized Dense matrix of the specified size.

## **Parameters**

exec	Executor associated to the matrix	
size	size of the matrix	
stride	stride of the rows (i.e. offset between the first elements of two consecutive rows, expressed as the number of matrix elements). If it is set to 0, size[1] will be used instead.	
	Harrison of matrix dismonto). If it is set to 0, 0.25[1] will be asset motoda.	

# Returns

A smart pointer to the newly created matrix.

Referenced by gko::matrix::Dense< value\_type >::create().

#### 46.62.3.29 create\_const()

Creates a constant (immutable) Dense matrix from a constant array.

#### **Parameters**

exec	the executor to create the matrix on
size	the dimensions of the matrix
values	the value array of the matrix
stride	the row-stride of the matrix

#### Returns

A smart pointer to the constant matrix wrapping the input array (if it resides on the same executor as the matrix) or a copy of the array on the correct executor.

# 46.62.3.30 create\_const\_view\_of()

Creates a immutable Dense matrix, where the underlying array is a view of another Dense matrix' array.

#### **Parameters**

other	The other matrix on which to create the view
-------	--

## Returns

A immutable Dense matrix that is a view of other

Referenced by gko::make\_const\_dense\_view().

#### 46.62.3.31 create real view() [1/2]

```
template<typename ValueType = default_precision>
std::unique_ptr<real_type> gko::matrix::Dense< ValueType >::create_real_view ( )
```

Create a real view of the (potentially) complex original matrix.

If the original matrix is real, nothing changes. If the original matrix is complex, the result is created by viewing the complex matrix with as real with a reinterpret\_cast with twice the number of columns and double the stride.

# 46.62.3.32 create\_real\_view() [2/2]

```
template<typename ValueType = default_precision>
std::unique_ptr<const real_type> gko::matrix::Dense< ValueType >::create_real_view ( ) const
```

Create a real view of the (potentially) complex original matrix.

If the original matrix is real, nothing changes. If the original matrix is complex, the result is created by viewing the complex matrix with as real with a reinterpret\_cast with twice the number of columns and double the stride.

# 46.62.3.33 create\_submatrix() [1/2]

Create a submatrix from the original matrix.

#### **Parameters**

rows	row span	
columns	column span	

# 46.62.3.34 create\_submatrix() [2/2]

Create a submatrix from the original matrix.

Warning: defining stride for this create\_submatrix method might cause wrong memory access. Better use the create\_submatrix(rows, columns) method instead.

#### **Parameters**

rows	row span
columns	column span
stride	stride of the new submatrix.

Referenced by gko::matrix::Dense< value\_type >::create\_submatrix().

# 46.62.3.35 create\_view\_of()

Creates a Dense matrix, where the underlying array is a view of another Dense matrix' array.

#### **Parameters**

other	The other matrix on which to create the view
-------	--

#### Returns

A Dense matrix that is a view of other

Referenced by gko::make\_dense\_view().

# 46.62.3.36 create\_with\_config\_of()

Creates a Dense matrix with the same size and stride as another Dense matrix.

## **Parameters**

```
other The other matrix whose configuration needs to copied.
```

# 46.62.3.37 create\_with\_type\_of() [1/3]

```
template<typename ValueType = default_precision>
static std::unique_ptr<Dense> gko::matrix::Dense< ValueType >::create_with_type_of (
    ptr_param< const Dense< ValueType > other,
    std::shared_ptr< const Executor > exec,
    const dim< 2 > & size,
    const dim< 2 > & local_size,
    size_type stride ) [inline], [static]
```

local_size	Unused
stride	The stride of the new matrix.

#### Note

This is an overload to stay consistent with gko::experimental::distributed::Vector

# 46.62.3.38 create\_with\_type\_of() [2/3]

```
template<typename ValueType = default_precision>
static std::unique_ptr<Dense> gko::matrix::Dense< ValueType >::create_with_type_of (
    ptr_param< const Dense< ValueType > > other,
    std::shared_ptr< const Executor > exec,
    const dim< 2 > & size,
    size_type stride ) [inline], [static]
```

#### **Parameters**

stride	The stride of the new matrix.
--------	-------------------------------

#### Note

This is an overload which allows full parameter specification.

# 46.62.3.39 create\_with\_type\_of() [3/3]

Creates a Dense matrix with the same type as another Dense matrix but on a different executor and with a different size.

# Parameters

other	The other matrix whose type we target.	
exec	The executor of the new matrix.	
size	The size of the new matrix.	
stride	The stride of the new matrix.	

# Returns

a Dense matrix with the type of other.

# 46.62.3.40 extract\_diagonal() [1/2]

```
template<typename ValueType = default_precision>
std::unique_ptr<Diagonal<ValueType> > gko::matrix::Dense< ValueType >::extract_diagonal ( )
const [override], [virtual]
```

Extracts the diagonal entries of the matrix into a vector.

#### **Parameters**

diag the vector into which the diagonal will be written

Implements gko::DiagonalExtractable < ValueType >.

# 46.62.3.41 extract\_diagonal() [2/2]

Writes the diagonal of this matrix into an existing diagonal matrix.

# **Parameters**

output The output matrix. Its size must match the size of this matrix's diagonal.

See also

Dense::extract\_diagonal()

# 46.62.3.42 fill()

Fill the dense matrix with a given value.

# **Parameters**

value the value to be filled

# 46.62.3.43 get\_const\_values()

```
template<typename ValueType = default_precision>
const value_type* gko::matrix::Dense< ValueType >::get_const_values ( ) const [inline], [noexcept]
```

Returns a pointer to the array of values of the matrix.

#### Returns

the pointer to the array of values

#### Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

# 46.62.3.44 get\_num\_stored\_elements()

```
template<typename ValueType = default_precision>
size_type gko::matrix::Dense< ValueType >::get_num_stored_elements ( ) const [inline], [noexcept]
```

Returns the number of elements explicitly stored in the matrix.

#### Returns

the number of elements explicitly stored in the matrix

# 46.62.3.45 get\_stride()

```
template<typename ValueType = default_precision>
size_type gko::matrix::Dense< ValueType >::get_stride ( ) const [inline], [noexcept]
```

Returns the stride of the matrix.

# Returns

the stride of the matrix.

Referenced by gko::matrix::Dense< value\_type >::create\_submatrix().

# 46.62.3.46 get\_values()

```
template<typename ValueType = default_precision>
value_type* gko::matrix::Dense< ValueType >::get_values ( ) [inline], [noexcept]
```

Returns a pointer to the array of values of the matrix.

#### Returns

the pointer to the array of values

# 46.62.3.47 inv\_scale()

Scales the matrix with the inverse of a scalar.

#### **Parameters**

alpha

If alpha is 1x1 Dense matrix, the entire matrix is scaled by 1 / alpha. If it is a Dense row vector of values, then i-th column of the matrix is scaled with the inverse of the i-th element of alpha (the number of columns of alpha has to match the number of columns of the matrix).

# 46.62.3.48 inverse\_column\_permute() [1/4]

Returns a LinOp representing the row permutation of the inverse permuted object.

In the resulting LinOp, the column perm[i] contains the input column i.

From the linear algebra perspective, with  $P_{ij} = \delta_{i\pi(i)}$ , this represents the operation  $AP^{-T}$ .

# **Parameters**

permutation_indices	the array of indices containing the permutation order perm.
---------------------	---

# Returns

a pointer to the new inverse permuted object

Implements gko::Permutable < int32 >.

# 46.62.3.49 inverse\_column\_permute() [2/4]

Writes the inverse column-permuted matrix into the given output matrix.

#### **Parameters**

permutation_indices	The array containing permutation indices. It must have this->get_size()[1]	
	elements.	
output	The output matrix. It must have the dimensions this->get_size()	

# See also

Dense::inverse\_column\_permute(const array<int32>\*)

# 46.62.3.50 inverse\_column\_permute() [3/4]

Returns a LinOp representing the row permutation of the inverse permuted object.

In the resulting LinOp, the column perm[i] contains the input column i.

From the linear algebra perspective, with  $P_{ij} = \delta_{i\pi(i)}$ , this represents the operation  $AP^{-T}$ .

#### **Parameters**

permutation_indices	the array of indices containing the permutation order perm.
---------------------	---

# Returns

a pointer to the new inverse permuted object

Implements gko::Permutable < int64 >.

# 46.62.3.51 inverse\_column\_permute() [4/4]

# 46.62.3.52 inverse\_permute() [1/4]

Returns a LinOp representing the symmetric inverse row and column permutation of the Permutable object.

In the resulting LinOp, the entry at location (perm[i], perm[j]) contains the input value (i, j).

From the linear algebra perspective, with  $P_{ij} = \delta_{i\pi(i)}$ , this represents the operation  $P^{-1}AP^{-T}$ .

#### **Parameters**

permutation_indices	the array of indices containing the permutation order.
---------------------	--

#### Returns

a pointer to the new permuted object

Reimplemented from gko::Permutable < int32 >.

# 46.62.3.53 inverse\_permute() [2/4]

Writes the inverse symmetrically permuted matrix into the given output matrix.

#### **Parameters**

permutation_indices	The array containing permutation indices. It must have this->get_size()[0]
	elements.
output	The output matrix. It must have the dimensions this->get_size()

# See also

Dense::inverse\_permute(const array<int32>\*)

# 46.62.3.54 inverse\_permute() [3/4]

Returns a LinOp representing the symmetric inverse row and column permutation of the Permutable object.

In the resulting LinOp, the entry at location (perm[i], perm[j]) contains the input value (i, j).

From the linear algebra perspective, with  $P_{ij} = \delta_{i\pi(i)}$ , this represents the operation  $P^{-1}AP^{-T}$ .

#### **Parameters**

```
permutation_indices the array of indices containing the permutation order.
```

# Returns

a pointer to the new permuted object

Reimplemented from gko::Permutable < int64 >.

# 46.62.3.55 inverse\_permute() [4/4]

#### 46.62.3.56 inverse\_row\_permute() [1/4]

Returns a LinOp representing the row permutation of the inverse permuted object.

In the resulting LinOp, the row perm[i] contains the input row i.

From the linear algebra perspective, with  $P_{ij} = \delta_{i\pi(i)}$ , this represents the operation  $P^{-1}A$ .

# **Parameters**

indices the array of ind	es containing the permutation order perm.
--------------------------	---

# Returns

a pointer to the new inverse permuted object

Implements gko::Permutable < int32 >.

# 46.62.3.57 inverse\_row\_permute() [2/4]

Writes the inverse row-permuted matrix into the given output matrix.

#### **Parameters**

permutation_indices	The array containing permutation indices. It must have this->get_size()[0] elements.
output	The output matrix. It must have the dimensions this->get_size()

# See also

Dense::inverse\_row\_permute(const array<int32>\*)

# 46.62.3.58 inverse\_row\_permute() [3/4]

Returns a LinOp representing the row permutation of the inverse permuted object.

In the resulting LinOp, the row perm[i] contains the input row i.

From the linear algebra perspective, with  $P_{ij} = \delta_{i\pi(i)}$ , this represents the operation  $P^{-1}A$ .

#### **Parameters**

permutation_indices	the array of indices containing the permutation order perm.
---------------------	---

# Returns

a pointer to the new inverse permuted object

Implements gko::Permutable < int64 >.

# 46.62.3.59 inverse\_row\_permute() [4/4]

#### 46.62.3.60 make\_complex() [1/2]

```
template<typename ValueType = default_precision>
std::unique_ptr<complex_type> gko::matrix::Dense< ValueType >::make_complex ( ) const
```

Creates a complex copy of the original matrix.

If the original matrix was real, the imaginary part of the result will be zero.

# 46.62.3.61 make\_complex() [2/2]

Writes a complex copy of the original matrix to a given complex matrix.

If the original matrix was real, the imaginary part of the result will be zero.

## 46.62.3.62 operator=() [1/2]

Copy-assigns a Dense matrix.

Preserves the executor, reallocates the matrix with minimal stride if the dimensions don't match, then copies the data over, ignoring padding.

# 46.62.3.63 operator=() [2/2]

Move-assigns a Dense matrix.

Preserves the executor, moves the data over preserving size and stride. Leaves the moved-from object in an empty state (0x0 with empty Array).

# 46.62.3.64 permute() [1/12]

Returns a LinOp representing the symmetric row and column permutation of the Permutable object.

In the resulting LinOp, the entry at location (i, j) contains the input value (perm[i], perm[j]).

From the linear algebra perspective, with  $P_{ij} = \delta_{i\pi(i)}$ , this represents the operation  $PAP^T$ .

#### **Parameters**

permutation indices	the array of indices containing the permutation order.

# Returns

a pointer to the new permuted object

Reimplemented from gko::Permutable < int32 >.

# 46.62.3.65 permute() [2/12]

Writes the symmetrically permuted matrix into the given output matrix.

#### **Parameters**

permutation_indices	The array containing permutation indices. It must have this->get_size()[0]	
	elements.	
output	The output matrix. It must have the dimensions this->get_size()	

# See also

Dense::permute(const array<int32>\*)

# 46.62.3.66 permute() [3/12]

Returns a LinOp representing the symmetric row and column permutation of the Permutable object.

In the resulting LinOp, the entry at location (i,j) contains the input value (perm[i], perm[j]).

From the linear algebra perspective, with  $P_{ij} = \delta_{i\pi(i)}$ , this represents the operation  $PAP^T$ .

permutation_indices	the array of indices containing the permutation order.
---------------------	--

#### Returns

a pointer to the new permuted object

Reimplemented from gko::Permutable < int64 >.

# 46.62.3.67 permute() [4/12]

# 46.62.3.68 permute() [5/12]

```
template<typename ValueType = default_precision>
std::unique_ptr<Dense> gko::matrix::Dense< ValueType >::permute (
    ptr_param< const Permutation< int32 >> permutation,
    permute_mode mode = permute_mode::symmetric ) const
```

Creates a permuted copy A' of this matrix A with the given permutation P.

By default, this computes a symmetric permutation (permute\_mode::symmetric). For the effect of the different permutation modes, see permute\_mode.

# Parameters

permutation	The input permutation.
mode	The permutation mode. If permute_mode::inverse is set, we use the inverse permutation $P^{-1}$ instead of $P$ . If permute_mode::rows is set, the rows will be permuted. If permute_mode::columns is set, the columns will be permuted.

# Returns

The permuted matrix.

# 46.62.3.69 permute() [6/12]

Overload of permute(ptr\_param<const Permutation<int32>>, permute\_mode) that writes the permuted copy into an existing Dense matrix.

#### **Parameters**

# 46.62.3.70 permute() [7/12]

```
template<typename ValueType = default_precision>
std::unique_ptr<Dense> gko::matrix::Dense< ValueType >::permute (
    ptr_param< const Permutation< int32 >> row_permutation,
    ptr_param< const Permutation< int32 >> column_permutation,
    bool invert = false ) const
```

Creates a non-symmetrically permuted copy A' of this matrix A with the given row and column permutations P and Q.

The operation will compute A'(i,j) = A(p[i],q[j]), or  $A' = PAQ^T$  if invert is false, and A'(p[i],q[j]) = A(i,j), or  $A' = P^{-1}AQ^{-T}$  if invert is true.

#### **Parameters**

row_permutation	The permutation $P$ to apply to the rows
column_permutation	The permutation ${\cal Q}$ to apply to the columns
invert	If set to false, uses the input permutations, otherwise uses their inverses ${\cal P}^{-1}, {\cal Q}^{-1}$

# Returns

The permuted matrix.

# 46.62.3.71 permute() [8/12]

Overload of permute(ptr\_param < const Permutation < int32>>, ptr\_param < const Permutation < int32>>, permute\_mode) that writes the permuted copy into an existing Dense matrix.

```
output the output matrix.
```

# 46.62.3.72 permute() [9/12]

```
template<typename ValueType = default_precision>
std::unique_ptr<Dense> gko::matrix::Dense< ValueType >::permute (
    ptr_param< const Permutation< int64 >> permutation,
    permute_mode mode = permute_mode::symmetric ) const
```

#### 46.62.3.73 permute() [10/12]

# 46.62.3.74 permute() [11/12]

```
template<typename ValueType = default_precision>
std::unique_ptr<Dense> gko::matrix::Dense< ValueType >::permute (
    ptr_param< const Permutation< int64 >> row_permutation,
    ptr_param< const Permutation< int64 >> column_permutation,
    bool invert = false ) const
```

# 46.62.3.75 permute() [12/12]

# 46.62.3.76 row\_gather() [1/6]

Create a Dense matrix consisting of the given rows from this matrix.

#### **Parameters**

gather_indices pointer to an array containing row indices from this matrix. It may contain duplicates	.
---	---

#### Returns

Dense matrix on the same executor with the same number of columns and  $gather\_indices->get \leftarrow \_size()$  rows containing the gathered rows from this matrix:  $output(i,j) = input(gather\_ \leftarrow indices(i), j)$ 

# 46.62.3.77 row\_gather() [2/6]

Copies the given rows from this matrix into row\_collection

#### **Parameters**

gather_indices	pointer to an array containing row indices from this matrix. It may contain duplicates.
row_collection	pointer to a LinOp that will store the gathered rows: row_collection(i, j) =
	input (gather_indices(i), j) It must have the same number of columns as this
	matrix and gather_indices->get_size() rows.

# 46.62.3.78 row\_gather() [3/6]

Create a Dense matrix consisting of the given rows from this matrix.

# **Parameters**

9	gather_indices	pointer to an array containing row indices from this matrix. It may contain duplicates.	
---	----------------	---	--

# Returns

Dense matrix on the same executor with the same number of columns and  $gather\_indices->get \leftarrow \_size()$  rows containing the gathered rows from this matrix:  $output(i,j) = input(gather\_ \leftarrow indices(i), j)$ 

# 46.62.3.79 row\_gather() [4/6]

# 46.62.3.80 row\_gather() [5/6]

Copies the given rows from this matrix into row\_collection with scaling.

#### **Parameters**

alpha	scaling the result of row gathering
gather_indices	pointer to an array containing row indices from this matrix. It may contain duplicates.
beta	scaling the input row_collection
row_collection	<pre>pointer to a LinOp that will store the gathered rows: row_collection(i, j) = input(gather_indices(i), j) It must have the same number of columns as this matrix and gather_indices-&gt;get_size() rows.</pre>

# 46.62.3.81 row\_gather() [6/6]

```
template<typename ValueType = default_precision>
void gko::matrix::Dense< ValueType >::row_gather (
    ptr_param< const LinOp > alpha,
    const array< int64 > * gather_indices,
    ptr_param< const LinOp > beta,
    ptr_param< LinOp > row_collection ) const
```

#### 46.62.3.82 row\_permute() [1/4]

Returns a LinOp representing the row permutation of the Permutable object.

In the resulting LinOp, the row i contains the input row perm[i].

From the linear algebra perspective, with  $P_{ij} = \delta_{i\pi(i)}$ , this represents the operation PA.

#### **Parameters**

permutation indices	the array of indices containing the permutation order.

# Returns

a pointer to the new permuted object

Implements gko::Permutable < int32 >.

# 46.62.3.83 row\_permute() [2/4]

Writes the row-permuted matrix into the given output matrix.

#### **Parameters**

permutation_indices	The array containing permutation indices. It must have this->get_size()[0]
	elements.
output	The output matrix. It must have the dimensions this->get_size()

# See also

Dense::row\_permute(const array<int32>\*)

# 46.62.3.84 row\_permute() [3/4]

Returns a LinOp representing the row permutation of the Permutable object.

In the resulting LinOp, the row  $\mathtt{i}$  contains the input row  $\mathtt{perm}[\mathtt{i}]$ .

From the linear algebra perspective, with  $P_{ij} = \delta_{i\pi(i)}$ , this represents the operation PA.

permutation_indices	the array of indices containing the permutation order.
---------------------	--

#### Returns

a pointer to the new permuted object

Implements gko::Permutable < int64 >.

# 46.62.3.85 row\_permute() [4/4]

# 46.62.3.86 scale()

Scales the matrix with a scalar (aka: BLAS scal).

#### **Parameters**

alpha

If alpha is 1x1 Dense matrix, the entire matrix is scaled by alpha. If it is a Dense row vector of values, then i-th column of the matrix is scaled with the i-th element of alpha (the number of columns of alpha has to match the number of columns of the matrix).

# 46.62.3.87 scale\_permute() [1/8]

Creates a scaled and permuted copy of this matrix.

For an explanation of the permutation modes, see permute(ptr\_param<const Permutation<index\_type>>, permute\_mode)

permutation	The scaled permutation.
mode	The permutation mode.

#### Returns

The permuted matrix.

# 46.62.3.88 scale\_permute() [2/8]

Overload of scale\_permute(ptr\_param < const ScaledPermutation < value\_type, int32>>, permute\_mode) that writes the permuted copy into an existing Dense matrix.

#### **Parameters**

output	the output matrix.
--------	--------------------

# 46.62.3.89 scale permute() [3/8]

```
template<typename ValueType = default_precision>
std::unique_ptr<Dense> gko::matrix::Dense< ValueType >::scale_permute (
    ptr_param< const ScaledPermutation< value_type, int32 >> row_permutation,
    ptr_param< const ScaledPermutation</pre>
value_type, int32 >> column_permutation,
bool invert = false ) const
```

Creates a scaled and permuted copy of this matrix.

For an explanation of the parameters, see  $permute(ptr\_param < const Permutation < index\_type>>, ptr\_param < const Permutation < index\_type>>, permute\_mode)$ 

## **Parameters**

row_permutation	The scaled row permutation.
column_permutation	The scaled column permutation.
invert	If set to false, uses the input permutations, otherwise uses their inverses ${\cal P}^{-1}, {\cal Q}^{-1}$

# Returns

The permuted matrix.

# 46.62.3.90 scale\_permute() [4/8]

Overload of scale\_permute(ptr\_param<const ScaledPermutation<value\_type, int32>>, ptr\_param<const ScaledPermutation<value\_type, int32>>, bool) that writes the permuted copy into an existing Dense matrix.

#### **Parameters**

```
output the output matrix.
```

#### 46.62.3.91 scale permute() [5/8]

# 46.62.3.92 scale\_permute() [6/8]

# 46.62.3.93 scale\_permute() [7/8]

```
template<typename ValueType = default_precision>
std::unique_ptr<Dense> gko::matrix::Dense< ValueType >::scale_permute (
    ptr_param< const ScaledPermutation< value_type, int64 >> row_permutation,
    ptr_param< const ScaledPermutation< value_type, int64 >> column_permutation,
    bool invert = false) const
```

# 46.62.3.94 scale\_permute() [8/8]

# 46.62.3.95 sub\_scaled()

Subtracts b scaled by alpha from the matrix (aka: BLAS axpy).

#### **Parameters**

alpha	If alpha is 1x1 Dense matrix, b is scaled by alpha. If it is a Dense row vector of values, then i-th column
	of b is scaled with the i-th element of alpha (the number of columns of alpha has to match the number
	of columns of the matrix).
b	a matrix of the same dimension as this

# 46.62.3.96 transpose() [1/2]

```
template<typename ValueType = default_precision>
std::unique_ptr<LinOp> gko::matrix::Dense< ValueType >::transpose ( ) const [override],
[virtual]
```

Returns a LinOp representing the transpose of the Transposable object.

# Returns

a pointer to the new transposed object

Implements gko::Transposable.

# 46.62.3.97 transpose() [2/2]

Writes the transposed matrix into the given output matrix.

#### **Parameters**

output The output matrix. It must have the dimensions gko::transpose(this->get\_size())

The documentation for this class was generated from the following files:

- · ginkgo/core/base/dense cache.hpp
- · ginkgo/core/matrix/dense.hpp

# 46.63 gko::device\_matrix\_data< ValueType, IndexType > Class Template Reference

This type is a device-side equivalent to matrix data.

#include <ginkgo/core/base/device\_matrix\_data.hpp>

# **Classes**

· struct arrays

Stores the internal arrays of a device\_matrix\_data object.

# **Public Member Functions**

- device\_matrix\_data (std::shared\_ptr< const Executor > exec, dim< 2 > size={}, size\_type num\_entries=0)
   Initializes a new device\_matrix\_data object.
- device\_matrix\_data (std::shared\_ptr< const Executor > exec, const device\_matrix\_data &data)

Initializes a device\_matrix\_data object by copying an existing object on another executor.

device\_matrix\_data (std::shared\_ptr< const Executor > exec, dim< 2 > size, array< index\_type > row\_idxs, array< index\_type > col\_idxs, array< value\_type > values)

Initializes a new device\_matrix\_data object from existing data.

- template<typename InputValueType, typename RowIndexType, typename ColIndexType >
   device\_matrix\_data (std::shared\_ptr< const Executor > exec, dim< 2 > size, std::initializer\_list< Row IndexType > row\_idxs, std::initializer\_list< ColIndexType > col\_idxs, std::initializer\_list< InputValueType >
   values)
- host\_type copy\_to\_host () const

Copies the device\_matrix\_data entries to the host to return a regular matrix\_data object with the same dimensions and entries.

void sort row major ()

Sorts the matrix entries in row-major order This means that they will be sorted by row index first, and then by column index inside each row.

void remove\_zeros ()

Removes all zero entries from the storage.

· void sum\_duplicates ()

Sums up all duplicate entries pointing to the same non-zero location.

std::shared\_ptr< const Executor > get\_executor () const

Returns the executor used to store the device\_matrix\_data entries.

dim< 2 > get\_size () const

Returns the dimensions of the matrix.

size\_type get\_num\_elems () const

Returns the number of stored elements of the matrix.

• size\_type get\_num\_stored\_elements () const

Returns the number of stored elements of the matrix.

index\_type \* get\_row\_idxs ()

Returns a pointer to the row index array.

const index\_type \* get\_const\_row\_idxs () const

Returns a pointer to the constant row index array.

index\_type \* get\_col\_idxs ()

Returns a pointer to the column index array.

const index\_type \* get\_const\_col\_idxs () const

Returns a pointer to the constant column index array.

value\_type \* get\_values ()

Returns a pointer to the value array.

const value\_type \* get\_const\_values () const

Returns a pointer to the constant value array.

void resize\_and\_reset (size\_type new\_num\_entries)

Resizes the internal storage to the given number of stored matrix entries.

void resize\_and\_reset (dim< 2 > new\_size, size\_type new\_num\_entries)

Resizes the matrix and internal storage to the given dimensions.

• arrays empty out ()

Moves out the internal arrays of the device\_matrix\_data object and resets it to an empty 0x0 matrix.

#### **Static Public Member Functions**

 static device\_matrix\_data create\_from\_host (std::shared\_ptr< const Executor > exec, const host\_type &data)

Creates a device\_matrix\_data object from the given host data on the given executor.

# 46.63.1 Detailed Description

```
template < typename ValueType, typename IndexType > class gko::device_matrix_data < ValueType, IndexType >
```

This type is a device-side equivalent to matrix\_data.

It stores the data necessary to initialize any matrix format in Ginkgo in individual value, column and row index arrays together with associated matrix dimensions. <a href="matrix\_data">matrix\_data</a> uses array-of-Structs storage (AoS), while device\_matrix\_data uses Struct-of-Arrays (SoA).

# Note

To be used with a Ginkgo matrix type, the entry array must be sorted in row-major order, i.e. by row index, then by column index within rows. This can be achieved by calling the sort\_row\_major function.

The data must not contain any duplicate (row, column) pairs.

#### **Template Parameters**

ValueType	the type used to store matrix values
IndexType	the type used to store matrix row and column indices

# 46.63.2 Constructor & Destructor Documentation

# 46.63.2.1 device\_matrix\_data() [1/4]

Initializes a new device\_matrix\_data object.

It uses the given executor to allocate storage for the given number of entries and matrix dimensions.

# **Parameters**

exec	the executor to be used to store the matrix entries
size	the matrix dimensions
num_entries	the number of entries to be stored

# 46.63.2.2 device\_matrix\_data() [2/4]

Initializes a device\_matrix\_data object by copying an existing object on another executor.

## **Parameters**

ехес	the executor to be used to store the matrix entries
data	the device_matrix data object to copy, potentially stored on another executor.

# 46.63.2.3 device\_matrix\_data() [3/4]

Initializes a new device\_matrix\_data object from existing data.

#### **Parameters**

size	the matrix dimensions
values	the array containing the matrix values
col_idxs	the array containing the matrix column indices
row_idxs	the array containing the matrix row indices

# 46.63.2.4 device\_matrix\_data() [4/4]

#### **Parameters**

size	the matrix dimensions
values	the array containing the matrix values
col_idxs	the array containing the matrix column indices
row_idxs	the array containing the matrix row indices

# 46.63.3 Member Function Documentation

# 46.63.3.1 copy\_to\_host()

```
template<typename ValueType, typename IndexType>
host_type gko::device_matrix_data< ValueType, IndexType >::copy_to_host ( ) const
```

Copies the device\_matrix\_data entries to the host to return a regular matrix\_data object with the same dimensions and entries.

# Returns

a matrix\_data object with the same dimensions and entries.

Referenced by gko::ReadableFromMatrixData< ValueType, int32 >::read().

# 46.63.3.2 create\_from\_host()

Creates a device matrix data object from the given host data on the given executor.

#### **Parameters**

exec	the executor to create the device_matrix_data on.
data	the data to be wrapped or copied into a device_matrix_data.

#### Returns

a device\_matrix\_data object with the same size and entries as data copied to the device executor.

# 46.63.3.3 empty\_out()

```
template<typename ValueType, typename IndexType>
arrays gko::device_matrix_data< ValueType, IndexType >::empty_out ( )
```

Moves out the internal arrays of the device\_matrix\_data object and resets it to an empty 0x0 matrix.

# Returns

a struct containing the internal arrays.

# 46.63.3.4 get\_col\_idxs()

```
template<typename ValueType, typename IndexType>
index_type* gko::device_matrix_data< ValueType, IndexType >::get_col_idxs ( ) [inline]
```

Returns a pointer to the column index array.

# Returns

a pointer to the column index array

References gko::array< ValueType >::get\_data().

# 46.63.3.5 get\_const\_col\_idxs()

```
template<typename ValueType, typename IndexType>
const index_type* gko::device_matrix_data< ValueType, IndexType >::get_const_col_idxs ( )
const [inline]
```

Returns a pointer to the constant column index array.

## Returns

a pointer to the constant column index array

References gko::array< ValueType >::get\_const\_data().

## 46.63.3.6 get\_const\_row\_idxs()

```
template<typename ValueType, typename IndexType>
const index_type* gko::device_matrix_data< ValueType, IndexType >::get_const_row_idxs ( )
const [inline]
```

Returns a pointer to the constant row index array.

## Returns

a pointer to the constant row index array

References gko::array< ValueType >::get\_const\_data().

## 46.63.3.7 get const values()

```
template<typename ValueType, typename IndexType>
const value_type* gko::device_matrix_data< ValueType, IndexType >::get_const_values ( ) const
[inline]
```

Returns a pointer to the constant value array.

## Returns

a pointer to the constant value array

References gko::array< ValueType >::get\_const\_data().

## 46.63.3.8 get\_executor()

```
template<typename ValueType, typename IndexType>
std::shared_ptr<const Executor> gko::device_matrix_data< ValueType, IndexType >::get_executor
( ) const [inline]
```

Returns the executor used to store the device matrix data entries.

## Returns

the executor used to store the device\_matrix\_data entries.

References gko::array< ValueType >::get executor().

## 46.63.3.9 get\_num\_elems()

```
template<typename ValueType, typename IndexType>
size_type gko::device_matrix_data< ValueType, IndexType >::get_num_elems ( ) const [inline]
```

Returns the number of stored elements of the matrix.

## Returns

the number of stored elements of the matrix.

References gko::device\_matrix\_data< ValueType, IndexType >::get\_num\_stored\_elements().

# 46.63.3.10 get\_num\_stored\_elements()

```
template<typename ValueType, typename IndexType>
size_type gko::device_matrix_data< ValueType, IndexType >::get_num_stored_elements ( ) const
[inline]
```

Returns the number of stored elements of the matrix.

# Returns

the number of stored elements of the matrix.

References gko::array< ValueType >::get\_size().

Referenced by gko::device\_matrix\_data< ValueType, IndexType >::get\_num\_elems().

## 46.63.3.11 get\_row\_idxs()

```
template<typename ValueType, typename IndexType>
index_type* gko::device_matrix_data< ValueType, IndexType >::get_row_idxs ( ) [inline]
```

Returns a pointer to the row index array.

Returns

a pointer to the row index array

References gko::array< ValueType >::get\_data().

## 46.63.3.12 get\_size()

```
template<typename ValueType, typename IndexType>
dim<2> gko::device_matrix_data< ValueType, IndexType >::get_size ( ) const [inline]
```

Returns the dimensions of the matrix.

Returns

the dimensions of the matrix.

## 46.63.3.13 get\_values()

```
template<typename ValueType, typename IndexType>
value_type* gko::device_matrix_data< ValueType, IndexType >::get_values ( ) [inline]
```

Returns a pointer to the value array.

Returns

a pointer to the value array

References gko::array< ValueType >::get\_data().

## 46.63.3.14 remove\_zeros()

```
template<typename ValueType, typename IndexType>
void gko::device_matrix_data< ValueType, IndexType >::remove_zeros ( )
```

Removes all zero entries from the storage.

This does not modify the storage if there are no zero entries, and keeps the relative order of nonzero entries otherwise.

# 46.63.3.15 resize and reset() [1/2]

Resizes the matrix and internal storage to the given dimensions.

The resulting storage should be assumed uninitialized.

## **Parameters**

new_size	the new matrix dimensions.
new_num_entries	the new number of stored matrix entries.

## 46.63.3.16 resize\_and\_reset() [2/2]

Resizes the internal storage to the given number of stored matrix entries.

The resulting storage should be assumed uninitialized.

## **Parameters**

new_num_entries	the new number of stored matrix entries.
-----------------	--

# 46.63.3.17 sum\_duplicates()

```
template<typename ValueType, typename IndexType>
void gko::device_matrix_data< ValueType, IndexType >::sum_duplicates ( )
```

Sums up all duplicate entries pointing to the same non-zero location.

The output will be sorted in row-major order, and it will only reallocate if duplicates exist.

The documentation for this class was generated from the following file:

• ginkgo/core/base/device\_matrix\_data.hpp

# 46.64 gko::matrix::Diagonal < ValueType > Class Template Reference

This class is a utility which efficiently implements the diagonal matrix (a linear operator which scales a vector row wise).

#include <ginkgo/core/matrix/diagonal.hpp>

## **Public Member Functions**

std::unique\_ptr< LinOp > transpose () const override

Returns a LinOp representing the transpose of the Transposable object.

std::unique\_ptr< LinOp > conj\_transpose () const override

Returns a LinOp representing the conjugate transpose of the Transposable object.

• std::unique\_ptr< absolute\_type > compute\_absolute () const override

Gets the AbsoluteLinOp.

void compute\_absolute\_inplace () override

Compute absolute inplace on each element.

value\_type \* get\_values () noexcept

Returns a pointer to the array of values of the matrix.

const value\_type \* get\_const\_values () const noexcept

Returns a pointer to the array of values of the matrix.

void rapply (ptr\_param < const LinOp > b, ptr\_param < LinOp > x) const

Applies the diagonal matrix from the right side to a matrix b, which means scales the columns of b with the according diagonal entries.

void inverse\_apply (ptr\_param < const LinOp > b, ptr\_param < LinOp > x) const

Applies the inverse of the diagonal matrix to a matrix b, which means scales the columns of b with the inverse of the according diagonal entries.

## **Static Public Member Functions**

- static std::unique\_ptr< Diagonal > create (std::shared\_ptr< const Executor > exec, size\_type size=0)

  Creates an Diagonal matrix of the specified size.
- static std::unique\_ptr< Diagonal > create (std::shared\_ptr< const Executor > exec, const size\_type size, array< value\_type > values)

Creates a Diagonal matrix from an already allocated (and initialized) array.

 $\bullet \ \ {\it template}{<} {\it typename InputValueType}>$ 

static std::unique\_ptr< Diagonal > create (std::shared\_ptr< const Executor > exec, const size\_type size, std::initializer\_list< InputValueType > values)

create(std::shared\_ptr<const

static std::unique\_ptr< const Diagonal > create\_const (std::shared\_ptr< const Executor > exec, size\_type size, gko::detail::const array view< ValueType > &&values)

Creates a constant (immutable) Diagonal matrix from a constant array.

## 46.64.1 Detailed Description

```
template<typename ValueType = default_precision> class gko::matrix::Diagonal< ValueType >
```

This class is a utility which efficiently implements the diagonal matrix (a linear operator which scales a vector row wise).

Objects of the Diagonal class always represent a square matrix, and require one array to store their values.

# **Template Parameters**

ValueType	precision of matrix elements
IndexType	precision of matrix indexes of a CSR matrix the diagonal is applied or converted to.

# 46.64.2 Member Function Documentation

# 46.64.2.1 compute\_absolute()

```
template<typename ValueType = default_precision>
std::unique_ptr<absolute_type> gko::matrix::Diagonal< ValueType >::compute_absolute ( ) const
[override], [virtual]
```

Gets the AbsoluteLinOp.

## Returns

a pointer to the new absolute object

Implements gko::EnableAbsoluteComputation< remove\_complex< Diagonal< ValueType >>>.

# 46.64.2.2 conj\_transpose()

```
template<typename ValueType = default_precision>
std::unique_ptr<LinOp> gko::matrix::Diagonal< ValueType >::conj_transpose ( ) const [override],
[virtual]
```

Returns a LinOp representing the conjugate transpose of the Transposable object.

## Returns

a pointer to the new conjugate transposed object

Implements gko::Transposable.

# 46.64.2.3 create() [1/3]

Creates a Diagonal matrix from an already allocated (and initialized) array.

## **Parameters**

exec	Executor associated to the matrix
size	size of the matrix
values	array of matrix values

#### Note

If values is not an rvalue, not an array of ValueType, or is on the wrong executor, an internal copy will be created, and the original array data will not be used in the matrix.

## Returns

A smart pointer to the newly created matrix.

## 46.64.2.4 create() [2/3]

References gko::matrix::Diagonal < ValueType >::create().

## 46.64.2.5 create() [3/3]

Creates an Diagonal matrix of the specified size.

## **Parameters**

exec	Executor associated to the matrix
size	size of the matrix

## Returns

A smart pointer to the newly created matrix.

Referenced by gko::matrix::Diagonal < ValueType >::create().

## 46.64.2.6 create\_const()

Creates a constant (immutable) Diagonal matrix from a constant array.

## **Parameters**

exec	the executor to create the matrix on
size	the size of the square matrix
values	the value array of the matrix

## Returns

A smart pointer to the constant matrix wrapping the input array (if it resides on the same executor as the matrix) or a copy of the array on the correct executor.

## 46.64.2.7 get\_const\_values()

```
template<typename ValueType = default_precision>
const value_type* gko::matrix::Diagonal< ValueType >::get_const_values ( ) const [inline],
[noexcept]
```

Returns a pointer to the array of values of the matrix.

## Returns

the pointer to the array of values

# Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

References gko::array< ValueType >::get\_const\_data().

# 46.64.2.8 get\_values()

```
template<typename ValueType = default_precision>
value_type* gko::matrix::Diagonal< ValueType >::get_values ( ) [inline], [noexcept]
```

Returns a pointer to the array of values of the matrix.

## Returns

the pointer to the array of values

References gko::array< ValueType >::get\_data().

## 46.64.2.9 inverse\_apply()

Applies the inverse of the diagonal matrix to a matrix b, which means scales the columns of b with the inverse of the according diagonal entries.

## **Parameters**

b	the input vector(s) on which the inverse of the diagonal matrix is applied
X	the output vector(s) where the result is stored

References gko::ptr\_param< T >::get().

## 46.64.2.10 rapply()

Applies the diagonal matrix from the right side to a matrix b, which means scales the columns of b with the according diagonal entries.

# **Parameters**

	the input vector(s) on which the diagonal matrix is applied
Χ	the output vector(s) where the result is stored

References gko::ptr\_param< T >::get().

# 46.64.2.11 transpose()

```
template<typename ValueType = default_precision>
std::unique_ptr<LinOp> gko::matrix::Diagonal< ValueType >::transpose ( ) const [override],
[virtual]
```

Returns a LinOp representing the transpose of the Transposable object.

## Returns

a pointer to the new transposed object

Implements gko::Transposable.

The documentation for this class was generated from the following files:

- ginkgo/core/base/lin\_op.hpp
- ginkgo/core/matrix/diagonal.hpp

# 46.65 gko::DiagonalExtractable < ValueType > Class Template Reference

The diagonal of a LinOp implementing this interface can be extracted.

```
#include <ginkgo/core/base/lin_op.hpp>
```

# **Public Member Functions**

- std::unique\_ptr< LinOp > extract\_diagonal\_linop () const override

  Extracts the diagonal entries of the matrix into a vector.
- virtual std::unique\_ptr< matrix::Diagonal< ValueType >> extract\_diagonal () const =0
   Extracts the diagonal entries of the matrix into a vector.

# 46.65.1 Detailed Description

```
template<typename ValueType>
class gko::DiagonalExtractable< ValueType >
```

The diagonal of a LinOp implementing this interface can be extracted.

extract\_diagonal extracts the elements whose col and row index are the same and stores the result in a min(nrows, ncols) x 1 dense matrix.

## 46.65.2 Member Function Documentation

# 46.65.2.1 extract\_diagonal()

```
template<typename ValueType >
virtual std::unique_ptr<matrix::Diagonal<ValueType> > gko::DiagonalExtractable< ValueType
>::extract_diagonal ( ) const [pure virtual]
```

Extracts the diagonal entries of the matrix into a vector.

## **Parameters**

```
diag the vector into which the diagonal will be written
```

Implemented in gko::matrix::Csr< ValueType, IndexType >, gko::matrix::Dense< ValueType >, gko::matrix::Dense< ValueType >, gko::matrix::Dense< ValueType, IndexType >, gko::matrix::Hybrid< ValueType, IndexType >, gko::matrix::Fbcsr< ValueType, IndexType, IndexType, IndexType, IndexType, IndexType, IndexType, IndexType, IndexType >, and gko::matrix::Sellp< ValueType, IndexType, IndexType >.

## 46.65.2.2 extract\_diagonal\_linop()

```
template<typename ValueType >
std::unique_ptr<LinOp> gko::DiagonalExtractable< ValueType >::extract_diagonal_linop ( )
const [override], [virtual]
```

Extracts the diagonal entries of the matrix into a vector.

Returns

linop the linop of diagonal format

Implements gko::DiagonalLinOpExtractable.

The documentation for this class was generated from the following file:

• ginkgo/core/base/lin\_op.hpp

# 46.66 gko::DiagonalLinOpExtractable Class Reference

The diagonal of a LinOp can be extracted.

```
#include <ginkgo/core/base/lin_op.hpp>
```

# **Public Member Functions**

virtual std::unique\_ptr< LinOp > extract\_diagonal\_linop () const =0
 Extracts the diagonal entries of the matrix into a vector.

# 46.66.1 Detailed Description

The diagonal of a LinOp can be extracted.

It will be implemented by DiagonalExtractable<ValueType>, so the class does not need to implement it. extract — \_diagonal\_linop returns a linop which extracts the elements whose col and row index are the same and stores the result in a min(nrows, ncols) x 1 dense matrix.

## 46.66.2 Member Function Documentation

## 46.66.2.1 extract\_diagonal\_linop()

virtual std::unique\_ptr<LinOp> gko::DiagonalLinOpExtractable::extract\_diagonal\_linop ( ) const
[pure virtual]

Extracts the diagonal entries of the matrix into a vector.

## Returns

linop the linop of diagonal format

Implemented in gko::DiagonalExtractable < ValueType >.

The documentation for this class was generated from the following file:

· ginkgo/core/base/lin\_op.hpp

# 46.67 gko::dim< Dimensionality, DimensionType > Struct Template Reference

A type representing the dimensions of a multidimensional object.

#include <ginkgo/core/base/dim.hpp>

## **Public Member Functions**

constexpr dim ()

Creates a dimension object with all dimensions set to zero.

constexpr dim (const dimension\_type &size)

Creates a dimension object with all dimensions set to the same value.

template<typename... Rest, std::enable\_if\_t< sizeof...(Rest)==Dimensionality - 1 > \* = nullptr>
constexpr dim (const dimension\_type &first, const Rest &... rest)

Creates a dimension object with the specified dimensions.

constexpr const dimension\_type & operator[] (const size\_type & dimension) const noexcept

Returns the requested dimension.

- dimension\_type & operator[] (const size\_type &dimension) noexcept
- · constexpr operator bool () const

Checks if all dimensions evaluate to true.

# **Friends**

constexpr friend bool operator== (const dim &x, const dim &y)

Checks if two dim objects are equal.

constexpr friend bool operator!= (const dim &x, const dim &y)

Checks if two dim objects are not equal.

constexpr friend dim operator\* (const dim &x, const dim &y)

Multiplies two dim objects.

std::ostream & operator<< (std::ostream &os, const dim &x)</li>

A stream operator overload for dim.

# 46.67.1 Detailed Description

template < size\_type Dimensionality, typename DimensionType = size\_type > struct gko::dim < Dimensionality, DimensionType >

A type representing the dimensions of a multidimensional object.

# **Template Parameters**

Dimensionality	number of dimensions of the object
DimensionType	datatype used to represent each dimension

# 46.67.2 Constructor & Destructor Documentation

# 46.67.2.1 dim() [1/2]

Creates a dimension object with all dimensions set to the same value.

#### **Parameters**

size the size of each dimensio	n
--------------------------------	---

# 46.67.2.2 dim() [2/2]

Creates a dimension object with the specified dimensions.

If the number of dimensions given is less than the dimensionality of the object, the remaining dimensions are set to the same value as the last value given.

For example, in the context of matrices  $dim<2>\{2, 3\}$  creates the dimensions for a 2-by-3 matrix.

## **Parameters**

first	first dimension
rest	other dimensions

# 46.67.3 Member Function Documentation

# 46.67.3.1 operator bool()

```
template<size_type Dimensionality, typename DimensionType = size_type>
constexpr gko::dim< Dimensionality, DimensionType >::operator bool ( ) const [inline], [explicit],
[constexpr]
```

Checks if all dimensions evaluate to true.

For standard arithmetic types, this is equivalent to all dimensions being different than zero.

## Returns

true if and only if all dimensions evaluate to true

## Note

This operator is explicit to avoid implicit dim-to-int casts. It will still be used in contextual conversions (if, &&, ||, ||)

# 46.67.3.2 operator[]() [1/2]

Returns the requested dimension.

For example, if d is a dim<2> object representing matrix dimensions, d [0] returns the number of rows, and d [1] returns the number of columns.

# **Parameters**

dimension	the requested dimension
-----------	-------------------------

## Returns

the  ${\tt dimension}$ -th  ${\tt dimension}$ 

# 46.67.3.3 operator[]() [2/2]

# 46.67.4 Friends And Related Function Documentation

## 46.67.4.1 operator"!=

Checks if two dim objects are not equal.

## **Parameters**

X	first object	
У	second object	

## Returns

false if and only if all dimensions of both objects are equal.

# 46.67.4.2 operator\*

Multiplies two dim objects.

# Parameters

Х	first object	
У	second object	

# Returns

a dim object representing the size of the tensor product x \* y

## 46.67.4.3 operator <<

```
template<size_type Dimensionality, typename DimensionType = size_type>
std::ostream& operator<< (</pre>
```

```
std::ostream & os, const dim< Dimensionality, DimensionType > & x ) [friend]
```

A stream operator overload for dim.

## **Parameters**

os	stream object
Х	dim object

## Returns

a stream object appended with the dim output

## 46.67.4.4 operator==

Checks if two dim objects are equal.

## **Parameters**

X	first object
У	second object

## Returns

true if and only if all dimensions of both objects are equal.

The documentation for this struct was generated from the following file:

· ginkgo/core/base/dim.hpp

# 46.68 gko::DimensionMismatch Class Reference

DimensionMismatch is thrown if an operation is being applied to LinOps of incompatible size.

```
#include <ginkgo/core/base/exception.hpp>
```

# **Public Member Functions**

• DimensionMismatch (const std::string &file, int line, const std::string &func, const std::string &first\_name, size\_type first\_rows, size\_type first\_cols, const std::string &second\_name, size\_type second\_rows, size\_type second\_cols, const std::string &clarification)

Initializes a dimension mismatch error.

# 46.68.1 Detailed Description

DimensionMismatch is thrown if an operation is being applied to LinOps of incompatible size.

# 46.68.2 Constructor & Destructor Documentation

# 46.68.2.1 DimensionMismatch()

Initializes a dimension mismatch error.

## **Parameters**

file	The name of the offending source file
line	The source code line number where the error occurred
func	The function name where the error occurred
first_name	The name of the first operator
first_rows	The output dimension of the first operator
first_cols	The input dimension of the first operator
second_name	The name of the second operator
second_rows	The output dimension of the second operator
second_cols	The input dimension of the second operator
clarification	An additional message describing the error further

The documentation for this class was generated from the following file:

· ginkgo/core/base/exception.hpp

# 46.69 gko::experimental::solver::Direct< ValueType, IndexType > Class Template Reference

A direct solver based on a factorization into lower and upper triangular factors (with an optional diagonal scaling).

#include <ginkgo/core/solver/direct.hpp>

# **Public Member Functions**

• std::unique\_ptr< LinOp > transpose () const override

Returns a LinOp representing the transpose of the Transposable object.

• std::unique\_ptr< LinOp > conj\_transpose () const override

Returns a LinOp representing the conjugate transpose of the Transposable object.

• Direct (const Direct &)

Creates a copy of the solver.

Direct (Direct &&)

Moves from the given solver, leaving it empty.

## **Static Public Member Functions**

• static parameters\_type parse (const config::pnode &config, const config::registry &context, const config::type\_descriptor &td\_for\_child=config::make\_type\_descriptor < ValueType, IndexType >())

Create the parameters from the property\_tree.

# 46.69.1 Detailed Description

```
template<typename ValueType, typename IndexType>
class gko::experimental::solver::Direct< ValueType, IndexType>
```

A direct solver based on a factorization into lower and upper triangular factors (with an optional diagonal scaling).

The solver is built from the Factorization returned by the provided LinOpFactory.

## **Template Parameters**

ValueType	the type used to store values of the system matrix
IndexType	the type used to store sparsity pattern indices of the system matrix

## 46.69.2 Member Function Documentation

## 46.69.2.1 conj\_transpose()

```
template<typename ValueType , typename IndexType >
std::unique_ptr<LinOp> gko::experimental::solver::Direct< ValueType, IndexType >::conj_←
transpose ( ) const [override], [virtual]
```

Returns a LinOp representing the conjugate transpose of the Transposable object.

## Returns

a pointer to the new conjugate transposed object

Implements gko::Transposable.

## 46.69.2.2 parse()

Create the parameters from the property\_tree.

Because this is directly tied to the specific type, the value/index type settings within config are ignored and type\_ descriptor is only used for children configs.

#### **Parameters**

config	the property tree for setting	
context	the registry	
td_for_child	the type descriptor for children configs. The default uses the value/index type of this class.	

## Returns

parameters

# 46.69.2.3 transpose()

```
template<typename ValueType , typename IndexType >
std::unique_ptr<LinOp> gko::experimental::solver::Direct< ValueType, IndexType >::transpose (
) const [override], [virtual]
```

Returns a LinOp representing the transpose of the Transposable object.

## Returns

a pointer to the new transposed object

Implements gko::Transposable.

The documentation for this class was generated from the following file:

• ginkgo/core/solver/direct.hpp

# 46.70 gko::experimental::distributed::DistributedBase Class Reference

A base class for distributed objects.

#include <ginkgo/core/distributed/base.hpp>

# **Public Member Functions**

• DistributedBase & operator= (const DistributedBase &)

Copy assignment that doesn't change the used mpi::communicator.

• DistributedBase & operator= (DistributedBase &&) noexcept

Move assignment that doesn't change the used mpi::communicator.

mpi::communicator get\_communicator () const

Access the used mpi::communicator.

# 46.70.1 Detailed Description

A base class for distributed objects.

This class stores and gives access to the used mpi::communicator object.

Note

The communicator is not changed on assignment.

# 46.70.2 Member Function Documentation

# 46.70.2.1 get\_communicator()

```
mpi::communicator gko::experimental::distributed::DistributedBase::get_communicator ( ) const
[inline]
```

Access the used mpi::communicator.

# Returns

```
used mpi::communicator
```

```
56 { return comm_; }
```

# 46.70.2.2 operator=() [1/2]

Copy assignment that doesn't change the used mpi::communicator.

## Returns

unmodified \*this

## 46.70.2.3 operator=() [2/2]

Move assignment that doesn't change the used mpi::communicator.

Returns

unmodified \*this

The documentation for this class was generated from the following file:

ginkgo/core/distributed/base.hpp

# 46.71 gko::DpcppExecutor Class Reference

This is the Executor subclass which represents a DPC++ enhanced device.

```
#include <ginkgo/core/base/executor.hpp>
```

## **Public Member Functions**

std::shared\_ptr< Executor > get\_master () noexcept override

Returns the master OmpExecutor of this Executor.

std::shared ptr< const Executor > get master () const noexcept override

Returns the master OmpExecutor of this Executor.

void synchronize () const override

Synchronize the operations launched on the executor with its master.

- std::string get\_description () const override
- int get\_device\_id () const noexcept

Get the DPCPP device id of the device associated to this executor.

const std::vector< int > & get\_subgroup\_sizes () const noexcept

Get the available subgroup sizes for this device.

• int get\_num\_computing\_units () const noexcept

Get the number of Computing Units of this executor.

int get\_num\_subgroups () const noexcept

Get the number of subgroups of this executor.

const std::vector< int > & get\_max\_workitem\_sizes () const noexcept

Get the maximum work item sizes.

int get\_max\_workgroup\_size () const noexcept

Get the maximum workgroup size.

int get\_max\_subgroup\_size () const noexcept

Get the maximum subgroup size.

std::string get\_device\_type () const noexcept

Get a string representing the device type.

virtual void run (const Operation &op) const=0

Runs the specified Operation using this Executor.

template < typename ClosureOmp, typename ClosureCuda, typename ClosureHip, typename ClosureDpcpp > void run (const ClosureOmp & op\_omp, const ClosureCuda & op\_cuda, const ClosureHip & op\_hip, const ClosureDpcpp & op\_dpcpp) const

Runs one of the passed in functors, depending on the Executor type.

• template<typename ClosureReference , typename ClosureOmp , typename ClosureCuda , typename ClosureHip , typename Closure

DDCDD >

void run (std::string name, const ClosureReference &op\_ref, const ClosureOmp &op\_omp, const Closure ← Cuda &op\_cuda, const ClosureHip &op\_hip, const ClosureDpcpp &op\_dpcpp) const

Runs one of the passed in functors, depending on the Executor type.

# **Static Public Member Functions**

Creates a new DpcppExecutor.

static int get\_num\_devices (std::string device\_type)

Get the number of devices present on the system.

# 46.71.1 Detailed Description

This is the Executor subclass which represents a DPC++ enhanced device.

## 46.71.2 Member Function Documentation

# 46.71.2.1 create()

```
static std::shared_ptr<DpcppExecutor> gko::DpcppExecutor::create (
    int device_id,
    std::shared_ptr< Executor > master,
    std::string device_type = "all",
    dpcpp_queue_property property = dpcpp_queue_property::in_order ) [static]
```

Creates a new DpcppExecutor.

## **Parameters**

device_id	the DPCPP device id of this device	
master	an executor on the host that is used to invoke the device kernels	
device_type	a string representing the type of device to consider (accelerator, cpu, gpu or all).	

# 46.71.2.2 get\_description()

```
std::string gko::DpcppExecutor::get_description ( ) const [override], [virtual]
```

## Returns

a textual representation of the executor and its device.

Implements gko::Executor.

# 46.71.2.3 get\_device\_id()

```
int gko::DpcppExecutor::get_device_id ( ) const [inline], [noexcept]
```

Get the DPCPP device id of the device associated to this executor.

## Returns

the DPCPP device id of the device associated to this executor

## 46.71.2.4 get\_device\_type()

```
std::string gko::DpcppExecutor::get_device_type ( ) const [inline], [noexcept]
```

Get a string representing the device type.

## Returns

a string representing the device type

# 46.71.2.5 get\_master() [1/2]

```
std::shared_ptr<const Executor> gko::DpcppExecutor::get_master ( ) const [override], [virtual],
[noexcept]
```

Returns the master OmpExecutor of this Executor.

# Returns

the master OmpExecutor of this Executor.

Implements gko::Executor.

# 46.71.2.6 get\_master() [2/2]

```
std::shared_ptr<Executor> gko::DpcppExecutor::get_master ( ) [override], [virtual], [noexcept]
```

Returns the master OmpExecutor of this Executor.

## Returns

the master OmpExecutor of this Executor.

Implements gko::Executor.

## 46.71.2.7 get\_max\_subgroup\_size()

```
int gko::DpcppExecutor::get_max_subgroup_size ( ) const [inline], [noexcept]
```

Get the maximum subgroup size.

Returns

the maximum subgroup size

# 46.71.2.8 get\_max\_workgroup\_size()

```
int gko::DpcppExecutor::get_max_workgroup_size ( ) const [inline], [noexcept]
```

Get the maximum workgroup size.

Returns

the maximum workgroup size

# 46.71.2.9 get\_max\_workitem\_sizes()

```
const std::vector<int>& gko::DpcppExecutor::get_max_workitem_sizes ( ) const [inline], [noexcept]
```

Get the maximum work item sizes.

Returns

the maximum work item sizes

# 46.71.2.10 get\_num\_computing\_units()

```
int gko::DpcppExecutor::get_num_computing_units ( ) const [inline], [noexcept]
```

Get the number of Computing Units of this executor.

Returns

the number of Computing Units of this executor

# 46.71.2.11 get\_num\_devices()

Get the number of devices present on the system.

## **Parameters**

device_type	a string representing the device type
-------------	---------------------------------------

# Returns

the number of devices present on the system

# 46.71.2.12 get\_subgroup\_sizes()

```
const std::vector<int>& gko::DpcppExecutor::get_subgroup_sizes ( ) const [inline], [noexcept]
```

Get the available subgroup sizes for this device.

## Returns

the available subgroup sizes for this device

# 46.71.2.13 run() [1/3]

Runs one of the passed in functors, depending on the Executor type.

# **Template Parameters**

ClosureOmp	type of op_omp
ClosureCuda	type of op_cuda
ClosureHip	type of op_hip
ClosureDpcpp	type of op_dpcpp

## **Parameters**

op omp	functor to run in case of a OmpExecutor or ReferenceExecutor	
op cuda	functor to run in case of a CudaExecutor	
op hip	functor to run in case of a HipExecutor	
'-'		
op_dpcpp	functor to run in case of a DpcppExecutor	

# 46.71.2.14 run() [2/3]

```
virtual void gko::Executor::run
```

Runs the specified Operation using this Executor.

## **Parameters**

```
op the operation to run
```

# 46.71.2.15 run() [3/3]

Runs one of the passed in functors, depending on the Executor type.

# **Template Parameters**

ClosureReference	type of op_ref
ClosureOmp	type of op_omp
ClosureCuda	type of op_cuda
ClosureHip	type of op_hip
ClosureDpcpp	type of op_dpcpp

# Parameters

name	the name of the operation
op_ref	functor to run in case of a ReferenceExecutor
op_omp	functor to run in case of a OmpExecutor
op_cuda	functor to run in case of a CudaExecutor
op_hip	functor to run in case of a HipExecutor
op_dpcpp	functor to run in case of a DpcppExecutor

The documentation for this class was generated from the following file:

• ginkgo/core/base/executor.hpp

# 46.72 gko::DpcppTimer Class Reference

A timer using kernels for timing on a DpcppExecutor in profiling mode.

```
#include <ginkgo/core/base/timer.hpp>
```

## **Public Member Functions**

• void record (time\_point &time) override

Records a time point at the current time.

· void wait (time\_point &time) override

Waits until all kernels in-process when recording the time point are finished.

std::chrono::nanoseconds difference\_async (const time\_point &start, const time\_point &stop) override
 Computes the difference between the two time points in nanoseconds.

## **Additional Inherited Members**

# 46.72.1 Detailed Description

A timer using kernels for timing on a DpcppExecutor in profiling mode.

## 46.72.2 Member Function Documentation

# 46.72.2.1 difference\_async()

Computes the difference between the two time points in nanoseconds.

This asynchronous version does not synchronize itself, so the time points need to have been synchronized with, i.e. timer->wait(stop) needs to have been called. The version is intended for more advanced users who want to measure the overhead of timing functionality separately.

## **Parameters**

start	the first time point (earlier)
end	the second time point (later)

## Returns

the difference between the time points in nanoseconds.

Implements gko::Timer.

The documentation for this class was generated from the following file:

· ginkgo/core/base/timer.hpp

# 46.73 gko::batch::matrix::Ell< ValueType, IndexType > Class Template Reference

Ell is a sparse matrix format that stores the same number of nonzeros in each row, enabling coalesced accesses.

#include <ginkgo/core/matrix/batch\_ell.hpp>

## **Public Member Functions**

• std::unique\_ptr< unbatch\_type > create\_view\_for\_item (size\_type item\_id)

Creates a mutable view (of matrix::Ell type) of one item of the batch::matrix::Ell<value\_type> object.

std::unique\_ptr< const unbatch\_type > create\_const\_view\_for\_item (size\_type item\_id) const

Creates a mutable view (of matrix::Ell type) of one item of the batch::matrix::Ell<value\_type> object.

value\_type \* get\_values () noexcept

Returns a pointer to the array of values of the matrix.

const value type \* get const values () const noexcept

Returns a pointer to the array of values of the matrix.

index\_type \* get\_col\_idxs () noexcept

Returns a pointer to the array of column indices of the matrix.

const index\_type \* get\_const\_col\_idxs () const noexcept

Returns a pointer to the array of column indices of the matrix.

• index\_type get\_num\_stored\_elements\_per\_row () const noexcept

Returns the number of elements per row explicitly stored.

• size\_type get\_num\_stored\_elements () const noexcept

Returns the number of elements explicitly stored in the batch matrix, cumulative across all the batch items.

size\_type get\_num\_elements\_per\_item () const noexcept

Returns the number of stored elements in each batch item.

• index type \* get col idxs for item (size type batch id) noexcept

Returns a pointer to the array of col\_idxs of the matrix.

const index\_type \* get\_const\_col\_idxs\_for\_item (size\_type batch\_id) const noexcept

Returns a pointer to the array of col idxs of the matrix.

value\_type \* get\_values\_for\_item (size\_type batch\_id) noexcept

Returns a pointer to the array of values of the matrix for a specific batch item.

• const value\_type \* get\_const\_values\_for\_item (size\_type batch\_id) const noexcept

Returns a pointer to the array of values of the matrix for a specific batch item.

- Ell \* apply (ptr\_param < const MultiVector < value\_type >> b, ptr\_param < MultiVector < value\_type >> x)
   Apply the matrix to a multi-vector.
- Ell \* apply (ptr\_param < const MultiVector < value\_type >> alpha, ptr\_param < const MultiVector < value\_
   type >> b, ptr\_param < const MultiVector < value\_type >> beta, ptr\_param < MultiVector < value\_type >> x)

Apply the matrix to a multi-vector with a linear combination of the given input vector.

const Ell \* apply (ptr\_param< const MultiVector< value\_type >> b, ptr\_param< MultiVector< value\_type</li>
 >> x) const

- const Ell \* apply (ptr\_param< const MultiVector< value\_type >> alpha, ptr\_param< const MultiVector< value\_type >> b, ptr\_param< const MultiVector< value\_type >> beta, ptr\_param< MultiVector< value\_
   type >> x) const
- $\bullet \ \ \mathsf{void} \ \mathsf{scale} \ (\mathsf{const} \ \mathsf{array} < \mathsf{value\_type} > \& \mathsf{row\_scale}, \ \mathsf{const} \ \mathsf{array} < \mathsf{value\_type} > \& \mathsf{col\_scale})$

Performs in-place row and column scaling for this matrix.

 void add\_scaled\_identity (ptr\_param< const MultiVector< value\_type >> alpha, ptr\_param< const MultiVector< value\_type >> beta)

Performs the operation this = alpha\*I + beta\*this.

## **Static Public Member Functions**

static std::unique\_ptr< Ell > create (std::shared\_ptr< const Executor > exec, const batch\_dim< 2 > &size=batch\_dim< 2 >{}, const IndexType num\_elems\_per\_row=0)

Creates an uninitialized Ell matrix of the specified size.

static std::unique\_ptr< Ell > create (std::shared\_ptr< const Executor > exec, const batch\_dim< 2 > &size, const IndexType num\_elems\_per\_row, array< value\_type > values, array< index\_type > col\_idxs)

Creates a Ell matrix from an already allocated (and initialized) array.

template<typename InputValueType, typename ColIndexType >
 static std::unique\_ptr< Ell > create (std::shared\_ptr< const Executor > exec, const batch\_dim< 2 >
 &size, const IndexType num\_elems\_per\_row, std::initializer\_list< InputValueType > values, std::initializer\_
 list< ColIndexType > col\_idxs)

create(std::shared\_ptr<const Executor>,

static std::unique\_ptr< const Ell > create\_const (std::shared\_ptr< const Executor > exec, const batch\_dim
 2 > &sizes, const index\_type num\_elems\_per\_row, gko::detail::const\_array\_view< value\_type > &&values, gko::detail::const\_array\_view< index\_type > &&col\_idxs)

Creates a constant (immutable) batch ell matrix from a constant array.

## 46.73.1 Detailed Description

template<typename ValueType = default\_precision, typename IndexType = int32> class gko::batch::matrix::Ell< ValueType, IndexType >

Ell is a sparse matrix format that stores the same number of nonzeros in each row, enabling coalesced accesses.

It is suitable for sparsity patterns that have a similar number of nonzeros in every row. The values are stored in a column-major fashion similar to the monolithic gko::matrix::Ell class.

Similar to the monolithic gko::matrix::Ell class, invalid\_index<IndexType> is used as the column index for padded zero entries.

## Note

It is also assumed that the sparsity pattern of all the items in the batch is the same and therefore only a single copy of the sparsity pattern is stored.

Currently only IndexType of int32 is supported.

# **Template Parameters**

ValueType	value precision of matrix elements
IndexType	index precision of matrix elements

# 46.73.2 Member Function Documentation

# 46.73.2.1 add\_scaled\_identity()

Performs the operation this = alpha\*I + beta\*this.

#### **Parameters**

alpha	the scalar for identity
beta	the scalar to multiply this matrix

## Note

Performs the operation in-place for this batch matrix.

This operation fails in case this matrix does not have all its diagonal entries.

## 46.73.2.2 apply() [1/4]

Apply the matrix to a multi-vector with a linear combination of the given input vector.

Represents the matrix vector multiplication, x = alpha \* A

• b + beta \* x, where x and b are both multi-vectors.

# **Parameters**

alpha	the scalar to scale the matrix-vector product with	
b	the multi-vector to be applied to	
beta	the scalar to scale the x vector with	
X	the output multi-vector	

## 46.73.2.3 apply() [2/4]

# 46.73.2.4 apply() [3/4]

Apply the matrix to a multi-vector.

Represents the matrix vector multiplication, x = A \* b, where x and b are both multi-vectors.

#### **Parameters**

b	the multi-vector to be applied to
Х	the output multi-vector

# 46.73.2.5 apply() [4/4]

# 46.73.2.6 create() [1/3]

Creates a Ell matrix from an already allocated (and initialized) array.

The column indices array needs to be the same for all batch items.

#### **Parameters**

exec	Executor associated to the matrix
size	size of the matrix
num_elems_per_row	the number of elements to be stored in each row
values	array of matrix values
col_idxs	the col_idxs array of a single batch item of the matrix.

#### Note

If values is not an rvalue, not an array of ValueType, or is on the wrong executor, an internal copy will be created, and the original array data will not be used in the matrix.

## Returns

A smart pointer to the newly created matrix.

# 46.73.2.7 create() [2/3]

create(std::shared\_ptr<const Executor>,

References gko::batch::matrix::Ell< ValueType, IndexType >::create().

# 46.73.2.8 create() [3/3]

Creates an uninitialized Ell matrix of the specified size.

## **Parameters**

exec	Executor associated to the matrix
size	size of the matrix
num_elems_per_row	the number of elements to be stored in each row

## Returns

A smart pointer to the newly created matrix.

Referenced by gko::batch::matrix::Ell< ValueType, IndexType >::create().

## 46.73.2.9 create const()

Creates a constant (immutable) batch ell matrix from a constant array.

The column indices array needs to be the same for all batch items.

## **Parameters**

exec	the executor to create the matrix on
size	the dimensions of the matrix
num_elems_per_row	the number of elements to be stored in each row
values	the value array of the matrix
col_idxs	the col_idxs array of a single batch item of the matrix.

# Returns

A smart pointer to the constant matrix wrapping the input array (if it resides on the same executor as the matrix) or a copy of the array on the correct executor.

A smart pointer to the newly created matrix.

# 46.73.2.10 create\_const\_view\_for\_item()

Creates a mutable view (of matrix::Ell type) of one item of the batch::matrix::Ell<value\_type> object.

Does not perform any deep copies, but only returns a view of the data.

# **Parameters**

item←	The index of the batch item
_id	

## Returns

a batch::matrix::Ell object with the data from the batch item at the given index.

# 46.73.2.11 create\_view\_for\_item()

Creates a mutable view (of matrix::Ell type) of one item of the batch::matrix::Ell<value\_type> object.

Does not perform any deep copies, but only returns a view of the data.

## **Parameters**

item←	The index of the batch item
_id	

# Returns

a batch::matrix::Ell object with the data from the batch item at the given index.

# 46.73.2.12 get\_col\_idxs()

```
template<typename ValueType = default_precision, typename IndexType = int32>
index_type* gko::batch::matrix::Ell< ValueType, IndexType >::get_col_idxs () [inline], [noexcept]
```

Returns a pointer to the array of column indices of the matrix.

# Returns

the pointer to the array of column indices

References gko::array< ValueType >::get\_data().

# 46.73.2.13 get\_col\_idxs\_for\_item()

Returns a pointer to the array of col\_idxs of the matrix.

This is shared across all batch items.

#### **Parameters**

batch←	the id of the batch item.
_id	

## Returns

the pointer to the array of col\_idxs

References gko::array< ValueType >::get\_data().

## 46.73.2.14 get\_const\_col\_idxs()

```
template<typename ValueType = default_precision, typename IndexType = int32>
const index_type* gko::batch::matrix::Ell< ValueType, IndexType >::get_const_col_idxs ( )
const [inline], [noexcept]
```

Returns a pointer to the array of column indices of the matrix.

# Returns

the pointer to the array of column indices

## Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

References gko::array< ValueType >::get\_const\_data().

# 46.73.2.15 get\_const\_col\_idxs\_for\_item()

Returns a pointer to the array of col\_idxs of the matrix.

This is shared across all batch items.

## **Parameters**

batch⊷	the id of the batch item.
_id	

## Returns

the pointer to the array of col\_idxs

## Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

References gko::array< ValueType >::get\_const\_data().

# 46.73.2.16 get\_const\_values()

```
template<typename ValueType = default_precision, typename IndexType = int32>
const value_type* gko::batch::matrix::Ell< ValueType, IndexType >::get_const_values ( ) const
[inline], [noexcept]
```

Returns a pointer to the array of values of the matrix.

## Returns

the pointer to the array of values

# Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

References gko::array< ValueType >::get const data().

# 46.73.2.17 get\_const\_values\_for\_item()

Returns a pointer to the array of values of the matrix for a specific batch item.

### **Parameters**

batch←	the id of the batch item.
_id	

### Returns

the pointer to the array of values

#### Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

References gko::array< ValueType >::get\_const\_data(), and gko::batch::matrix::Ell< ValueType, IndexType ><-- ::get\_num\_elements\_per\_item().

### 46.73.2.18 get num elements per item()

```
template<typename ValueType = default_precision, typename IndexType = int32>
size_type gko::batch::matrix::Ell< ValueType, IndexType >::get_num_elements_per_item ( ) const
[inline], [noexcept]
```

Returns the number of stored elements in each batch item.

### Returns

the number of stored elements per batch item.

References gko::batch::matrix::Ell< ValueType, IndexType >::get\_num\_stored\_elements().

Referenced by gko::batch::matrix::Ell< ValueType, IndexType >::get\_const\_values\_for\_item(), and gko::batch ::matrix::Ell< ValueType, IndexType >::get\_values\_for\_item().

## 46.73.2.19 get\_num\_stored\_elements()

```
template<typename ValueType = default_precision, typename IndexType = int32>
size_type gko::batch::matrix::Ell< ValueType, IndexType >::get_num_stored_elements ( ) const
[inline], [noexcept]
```

Returns the number of elements explicitly stored in the batch matrix, cumulative across all the batch items.

### Returns

the number of elements explicitly stored in the vector, cumulative across all the batch items

References gko::array< ValueType >::get\_size().

Referenced by gko::batch::matrix::Ell< ValueType, IndexType >::get\_num\_elements\_per\_item().

### 46.73.2.20 get\_num\_stored\_elements\_per\_row()

```
template<typename ValueType = default_precision, typename IndexType = int32>
index_type gko::batch::matrix::Ell< ValueType, IndexType >::get_num_stored_elements_per_row (
) const [inline], [noexcept]
```

Returns the number of elements per row explicitly stored.

### Returns

the number of elements stored in each row of the ELL matrix. Same for each batch item

### 46.73.2.21 get\_values()

```
template<typename ValueType = default_precision, typename IndexType = int32>
value_type* gko::batch::matrix::Ell< ValueType, IndexType >::get_values ( ) [inline], [noexcept]
```

Returns a pointer to the array of values of the matrix.

### Returns

the pointer to the array of values

References gko::array< ValueType >::get\_data().

## 46.73.2.22 get\_values\_for\_item()

Returns a pointer to the array of values of the matrix for a specific batch item.

### **Parameters**

batch←	the id of the batch item.
_id	

## Returns

the pointer to the array of values

### 46.73.2.23 scale()

Performs in-place row and column scaling for this matrix.

#### **Parameters**

row_scale	the row scalars
col_scale	the column scalars

The documentation for this class was generated from the following file:

· ginkgo/core/matrix/batch ell.hpp

## 46.74 gko::matrix::Ell< ValueType, IndexType > Class Template Reference

ELL is a matrix format where stride with explicit zeros is used such that all rows have the same number of stored elements.

```
#include <ginkgo/core/matrix/ell.hpp>
```

### **Public Member Functions**

• void read (const mat\_data &data) override

Reads a matrix from a matrix\_data structure.

void read (const device\_mat\_data &data) override

Reads a matrix from a device matrix data structure.

void read (device\_mat\_data &&data) override

Reads a matrix from a device\_matrix\_data structure.

void write (mat\_data &data) const override

Writes a matrix to a matrix\_data structure.

std::unique\_ptr< Diagonal</li>
 ValueType > > extract\_diagonal () const override

Extracts the diagonal entries of the matrix into a vector.

• std::unique ptr< absolute type > compute absolute () const override

Gets the AbsoluteLinOp.

void compute\_absolute\_inplace () override

Compute absolute inplace on each element.

value\_type \* get\_values () noexcept

Returns the values of the matrix.

const value\_type \* get\_const\_values () const noexcept

Returns the values of the matrix.

index\_type \* get\_col\_idxs () noexcept

Returns the column indexes of the matrix.

const index\_type \* get\_const\_col\_idxs () const noexcept

Returns the column indexes of the matrix.

• size\_type get\_num\_stored\_elements\_per\_row () const noexcept

Returns the number of stored elements per row.

• size\_type get\_stride () const noexcept

Returns the stride of the matrix.

size\_type get\_num\_stored\_elements () const noexcept

Returns the number of elements explicitly stored in the matrix.

value\_type & val\_at (size\_type row, size\_type idx) noexcept

Returns the idx-th non-zero element of the row-th row.

value\_type val\_at (size\_type row, size\_type idx) const noexcept

Returns the idx-th non-zero element of the row-th row.

index\_type & col\_at (size\_type row, size\_type idx) noexcept

Returns the idx-th column index of the row-th row.

• index\_type col\_at (size\_type row, size\_type idx) const noexcept

Returns the idx-th column index of the row-th row.

Ell & operator= (const Ell &)

Copy-assigns an Ell matrix.

• Ell & operator= (Ell &&)

Move-assigns an Ell matrix.

• Ell (const Ell &)

Copy-constructs an Ell matrix.

• Ell (Ell &&)

Move-constructs an Ell matrix.

## **Static Public Member Functions**

 static std::unique\_ptr< Ell > create (std::shared\_ptr< const Executor > exec, const dim< 2 > &size={}, size\_type num\_stored\_elements\_per\_row=0, size\_type stride=0)

Creates an uninitialized Ell matrix of the specified size.

static std::unique\_ptr< Ell > create (std::shared\_ptr< const Executor > exec, const dim< 2 > &size, array<</li>
 value\_type > values, array< index\_type > col\_idxs, size\_type num\_stored\_elements\_per\_row, size\_type stride)

Creates an ELL matrix from already allocated (and initialized) column index and value arrays.

template<typename InputValueType, typename InputColumnIndexType>
 static std::unique\_ptr< Ell > create (std::shared\_ptr< const Executor > exec, const dim< 2 > &size, std
 ::initializer\_list< InputValueType > values, std::initializer\_list< InputColumnIndexType > col\_idxs, size\_type num\_stored\_elements\_per\_row, size\_type stride)

create(std::shared\_ptr<const Executor>,

static std::unique\_ptr< const Ell > create\_const (std::shared\_ptr< const Executor > exec, const dim< 2 > &size, gko::detail::const\_array\_view< ValueType > &&values, gko::detail::const\_array\_view< IndexType > &&col\_idxs, size\_type num\_stored\_elements\_per\_row, size\_type stride)

Creates a constant (immutable) Ell matrix from a set of constant arrays.

## 46.74.1 Detailed Description

template < typename ValueType = default\_precision, typename IndexType = int32 > class gko::matrix::EII < ValueType, IndexType >

ELL is a matrix format where stride with explicit zeros is used such that all rows have the same number of stored elements.

The number of elements stored in each row is the largest number of nonzero elements in any of the rows (obtainable through <a href="mailto:get\_num\_stored\_elements\_per\_row">get\_num\_stored\_elements\_per\_row</a>() method). This removes the need of a row pointer like in the CSR format, and allows for SIMD processing of the distinct rows. For efficient processing, the nonzero elements and the corresponding column indices are stored in column-major fashion. The columns are padded to the length by user-defined stride parameter whose default value is the number of rows of the matrix.

This implementation uses the column index value invalid\_index<IndexType>() to mark padding entries that are not part of the sparsity pattern.

### **Template Parameters**

ValueType	precision of matrix elements
IndexType	precision of matrix indexes

### 46.74.2 Constructor & Destructor Documentation

## 46.74.2.1 EII() [1/2]

Copy-constructs an Ell matrix.

Inherits executor and dimensions, but copies data without padding.

### 46.74.2.2 EII() [2/2]

Move-constructs an Ell matrix.

Inherits executor, dimensions and data with padding. The moved-from object is empty (0x0 with empty Array).

## 46.74.3 Member Function Documentation

### 46.74.3.1 col\_at() [1/2]

Returns the idx-th column index of the row-th row .

### **Parameters**

row	the row of the requested element
idx	the idx-th stored element of the row

### Note

the method has to be called on the same Executor the matrix is stored at (e.g. trying to call this method on a GPU matrix from the OMP results in a runtime error)

```
220 {
221         return this->get_const_col_idxs()[this->linearize_index(row, idx)];
222 }
```

References gko::matrix::Ell< ValueType, IndexType >::get\_const\_col\_idxs().

## 46.74.3.2 col\_at() [2/2]

Returns the  ${\tt idx}\text{-th}$  column index of the  ${\tt row}\text{-th}$  row .

### **Parameters**

row	the row of the requested element
idx	the idx-th stored element of the row

## Note

the method has to be called on the same Executor the matrix is stored at (e.g. trying to call this method on a GPU matrix from the OMP results in a runtime error)

References gko::matrix::Ell< ValueType, IndexType >::get\_col\_idxs().

### 46.74.3.3 compute\_absolute()

```
template<typename ValueType = default_precision, typename IndexType = int32>
std::unique_ptr<absolute_type> gko::matrix::Ell< ValueType, IndexType >::compute_absolute ()
const [override], [virtual]
```

Gets the AbsoluteLinOp.

### Returns

a pointer to the new absolute object

Implements gko::EnableAbsoluteComputation< remove\_complex< Ell< ValueType, IndexType >> >.

### 46.74.3.4 create() [1/3]

Creates an ELL matrix from already allocated (and initialized) column index and value arrays.

### **Parameters**

exec	Executor associated to the matrix
size	size of the matrix
values	array of matrix values
col_idxs	array of column indexes
num_stored_elements_per_row	the number of stored elements per row
stride	stride of the rows

### Note

If one of col\_idxs or values is not an rvalue, not an array of IndexType and ValueType, respectively, or is on the wrong executor, an internal copy of that array will be created, and the original array data will not be used in the matrix.

## Returns

A smart pointer to the newly created matrix.

### 46.74.3.5 create() [2/3]

create(std::shared\_ptr<const Executor>,

create(std::shared\_ptr<const Executor>, const dim<2>&, array<value\_type>, array<index\_type>, size\_type, size\_type)

References gko::matrix::Ell< ValueType, IndexType >::create().

### 46.74.3.6 create() [3/3]

Creates an uninitialized Ell matrix of the specified size.

## Parameters

exec	Executor associated to the matrix
size	size of the matrix
num_stored_elements_per_row	the number of stored elements per row
stride	stride of the columns. If it is set to 0, size[0] will be used instead.

## Returns

A smart pointer to the newly created matrix.

Referenced by gko::matrix::Ell< ValueType, IndexType >::create().

## 46.74.3.7 create\_const()

```
template<trypename ValueType = default_precision, typename IndexType = int32>
static std::unique_ptr<const Ell> gko::matrix::Ell< ValueType, IndexType >::create_const (
```

```
std::shared_ptr< const Executor > exec,
const dim< 2 > & size,
gko::detail::const_array_view< ValueType > && values,
gko::detail::const_array_view< IndexType > && col_idxs,
size_type num_stored_elements_per_row,
size_type stride ) [static]
```

Creates a constant (immutable) Ell matrix from a set of constant arrays.

### **Parameters**

exec	the executor to create the matrix on
size	the dimensions of the matrix
values	the value array of the matrix
col_idxs	the column index array of the matrix
num_stored_elements_per_row	the number of stored nonzeros per row
stride	the column-stride of the value and column index array

### Returns

A smart pointer to the constant matrix wrapping the input arrays (if they reside on the same executor as the matrix) or a copy of the arrays on the correct executor.

### 46.74.3.8 extract\_diagonal()

```
template<typename ValueType = default_precision, typename IndexType = int32>
std::unique_ptr<Diagonal<ValueType> > gko::matrix::Ell< ValueType, IndexType >::extract_
diagonal () const [override], [virtual]
```

Extracts the diagonal entries of the matrix into a vector.

## Parameters

```
diag the vector into which the diagonal will be written
```

Implements gko::DiagonalExtractable < ValueType >.

### 46.74.3.9 get\_col\_idxs()

```
template<typename ValueType = default_precision, typename IndexType = int32>
index_type* gko::matrix::Ell< ValueType, IndexType >::get_col_idxs () [inline], [noexcept]
```

Returns the column indexes of the matrix.

#### Returns

the column indexes of the matrix.

References gko::array< ValueType >::get\_data().

Referenced by gko::matrix::Ell< ValueType, IndexType >::col\_at().

### 46.74.3.10 get\_const\_col\_idxs()

```
template<typename ValueType = default_precision, typename IndexType = int32>
const index_type* gko::matrix::Ell< ValueType, IndexType >::get_const_col_idxs ( ) const [inline],
[noexcept]
```

Returns the column indexes of the matrix.

#### Returns

the column indexes of the matrix.

#### Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

References gko::array< ValueType >::get\_const\_data().

Referenced by gko::matrix::Ell< ValueType, IndexType >::col\_at().

## 46.74.3.11 get\_const\_values()

```
template<typename ValueType = default_precision, typename IndexType = int32>
const value_type* gko::matrix::Ell< ValueType, IndexType >::get_const_values ( ) const [inline],
[noexcept]
```

Returns the values of the matrix.

### Returns

the values of the matrix.

### Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

References gko::array< ValueType >::get\_const\_data().

### 46.74.3.12 get\_num\_stored\_elements()

```
template<typename ValueType = default_precision, typename IndexType = int32>
size_type gko::matrix::Ell< ValueType, IndexType >::get_num_stored_elements ( ) const [inline],
[noexcept]
```

Returns the number of elements explicitly stored in the matrix.

#### Returns

the number of elements explicitly stored in the matrix

References gko::array< ValueType >::get\_size().

### 46.74.3.13 get\_num\_stored\_elements\_per\_row()

```
template<typename ValueType = default_precision, typename IndexType = int32>
size_type gko::matrix::Ell< ValueType, IndexType >::get_num_stored_elements_per_row ( ) const
[inline], [noexcept]
```

Returns the number of stored elements per row.

### Returns

the number of stored elements per row.

### 46.74.3.14 get\_stride()

```
template<typename ValueType = default_precision, typename IndexType = int32>
size_type gko::matrix::Ell< ValueType, IndexType >::get_stride ( ) const [inline], [noexcept]
```

Returns the stride of the matrix.

### Returns

the stride of the matrix.

## 46.74.3.15 get\_values()

```
template<typename ValueType = default_precision, typename IndexType = int32>
value_type* gko::matrix::Ell< ValueType, IndexType >::get_values () [inline], [noexcept]
```

Returns the values of the matrix.

### Returns

the values of the matrix.

References gko::array< ValueType >::get\_data().

### 46.74.3.16 operator=() [1/2]

Copy-assigns an Ell matrix.

Preserves the executor, reallocates the matrix with minimal stride if the dimensions don't match, then copies the data over, ignoring padding.

## 46.74.3.17 operator=() [2/2]

Move-assigns an Ell matrix.

Preserves the executor, moves the data over preserving size and stride. Leaves the moved-from object in an empty state (0x0 with empty Array).

### 46.74.3.18 read() [1/3]

Reads a matrix from a device\_matrix\_data structure.

### **Parameters**

```
data the device_matrix_data structure.
```

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## **46.74.3.19** read() [2/3]

Reads a matrix from a matrix data structure.

### **Parameters**

data	the matrix	data structure

Implements gko::ReadableFromMatrixData< ValueType, IndexType >.

### 46.74.3.20 read() [3/3]

Reads a matrix from a device\_matrix\_data structure.

The structure may be emptied by this function.

#### **Parameters**

```
data the device_matrix_data structure.
```

Reimplemented from gko::ReadableFromMatrixData< ValueType, IndexType >.

### 46.74.3.21 val at() [1/2]

Returns the idx-th non-zero element of the row-th row .

### **Parameters**

row	the row of the requested element
idx	the idx-th stored element of the row

### Note

the method has to be called on the same Executor the matrix is stored at (e.g. trying to call this method on a GPU matrix from the OMP results in a runtime error)

References gko::array< ValueType >::get\_const\_data().

## 46.74.3.22 val\_at() [2/2]

Returns the idx-th non-zero element of the row-th row.

### **Parameters**

row	the row of the requested element
idx	the idx-th stored element of the row

#### Note

the method has to be called on the same Executor the matrix is stored at (e.g. trying to call this method on a GPU matrix from the OMP results in a runtime error)

References gko::array< ValueType >::get\_data().

### 46.74.3.23 write()

Writes a matrix to a matrix\_data structure.

### **Parameters**

```
data the matrix_data structure
```

Implements gko::WritableToMatrixData< ValueType, IndexType >.

The documentation for this class was generated from the following files:

- · ginkgo/core/matrix/csr.hpp
- · ginkgo/core/matrix/ell.hpp

## 46.75 gko::enable\_parameters\_type< ConcreteParametersType, Factory > Class Template Reference

The enable\_parameters\_type mixin is used to create a base implementation of the factory parameters structure.

```
#include <ginkgo/core/base/abstract_factory.hpp>
```

## **Public Member Functions**

template<typename... Args>
 ConcreteParametersType & with\_loggers (Args &&... \_value)

Provides the loggers to be added to the factory and its generated objects in a fluent interface.

• std::unique\_ptr< Factory > on (std::shared\_ptr< const Executor > exec) const

Creates a new factory on the specified executor.

## 46.75.1 Detailed Description

template<typename ConcreteParametersType, typename Factory> class gko::enable\_parameters\_type< ConcreteParametersType, Factory >

The enable\_parameters\_type mixin is used to create a base implementation of the factory parameters structure.

It provides only the on() method which can be used to instantiate the factory give the parameters stored in the structure.

### **Template Parameters**

ConcreteParametersType	the concrete parameters type which is being implemented [CRTP parameter]
Factory	the concrete factory for which these parameters are being used

## 46.75.2 Member Function Documentation

## 46.75.2.1 on()

Creates a new factory on the specified executor.

## **Parameters**

exec	the executor where the factory will be created
------	--

### Returns

a new factory instance

The documentation for this class was generated from the following file:

• ginkgo/core/base/abstract\_factory.hpp

## 46.76 gko::EnableAbsoluteComputation< AbsoluteLinOp > Class Template Reference

The EnableAbsoluteComputation mixin provides the default implementations of  $compute\_absolute\_linop$  and the absolute interface.

#include <ginkgo/core/base/lin\_op.hpp>

### **Public Member Functions**

- std::unique\_ptr< LinOp > compute\_absolute\_linop () const override
   Gets the absolute LinOp.
- virtual std::unique\_ptr< absolute\_type > compute\_absolute () const =0
   Gets the AbsoluteLinOp.

## 46.76.1 Detailed Description

```
\label{lem:continuous} \ensuremath{\mathsf{template}}{<} \mathsf{typename} \ \mathsf{AbsoluteLinOp}{>} \\ \ensuremath{\mathsf{class}} \ \mathsf{gko}{::} \mathsf{EnableAbsoluteComputation}{<} \ \mathsf{AbsoluteLinOp}{>} \\
```

The EnableAbsoluteComputation mixin provides the default implementations of compute\_absolute\_linop and the absolute interface.

compute\_absolute gets a new AbsoluteLinOp. compute\_absolute\_inplace applies absolute inplace, so it still keeps the value\_type of the class.

## **Template Parameters**

AbsoluteLinOn	the absolute LinOp which is being returned [CRTP parameter]
, iboolato_iiiop	the about to Emop which is being retarned [orthoparameter]

### 46.76.2 Member Function Documentation

### 46.76.2.1 compute\_absolute()

```
template<typename AbsoluteLinOp>
virtual std::unique_ptr<absolute_type> gko::EnableAbsoluteComputation< AbsoluteLinOp >
::compute_absolute ( ) const [pure virtual]
```

Gets the AbsoluteLinOp.

### Returns

a pointer to the new absolute object

Implemented in gko::matrix::Csr< ValueType, IndexType >, gko::matrix::Dense< ValueType >, gko::matrix::Dense< value\_type >, gko::matrix::Dense< ValueType, IndexType >, gko::matrix::Hybrid< ValueType, IndexType >, gko::matrix::Fbcsr< ValueType, IndexType >, gko::experimental::distributed::Vector< gko::matrix::Ell< ValueType, IndexType >, gko::matrix::Sellp< ValueType, IndexType >, gko::matrix::Dense< ValueType, IndexType >, gko::matrix::Sellp< ValueType, IndexType >, and gko::matrix::Diagonal< ValueType >.

Referenced by gko::EnableAbsoluteComputation< remove\_complex< Ell< ValueType, IndexType  $> > \leftarrow$  ::compute\_absolute\_linop().

## 46.76.2.2 compute\_absolute\_linop()

```
template<typename AbsoluteLinOp>
std::unique_ptr<LinOp> gko::EnableAbsoluteComputation< AbsoluteLinOp >::compute_absolute_
linop ( ) const [inline], [override], [virtual]
```

Gets the absolute LinOp.

### Returns

a pointer to the new absolute LinOp

### Implements gko::AbsoluteComputable.

```
801 {
802     return this->compute_absolute();
803 }
```

The documentation for this class was generated from the following file:

· ginkgo/core/base/lin\_op.hpp

## 46.77 gko::EnableAbstractPolymorphicObject< AbstractObject, PolymorphicBase > Class Template Reference

This mixin inherits from (a subclass of) PolymorphicObject and provides a base implementation of a new abstract object.

#include <ginkgo/core/base/polymorphic\_object.hpp>

## 46.77.1 Detailed Description

template<typename AbstractObject, typename PolymorphicBase = PolymorphicObject> class gko::EnableAbstractPolymorphicObject< AbstractObject, PolymorphicBase >

This mixin inherits from (a subclass of) PolymorphicObject and provides a base implementation of a new abstract object.

It uses method hiding to update the parameter and return types from PolymorphicObject toAbstractObject` wherever it makes sense. As opposed to EnablePolymorphicObject, it does not implement PolymorphicObject's virtual methods.

## **Template Parameters**

AbstractObject	the abstract class which is being implemented [CRTP parameter]
PolymorphicBase	parent of AbstractObject in the polymorphic hierarchy, has to be a subclass of polymorphic object

See also

EnablePolymorphicObject for creating a concrete subclass of PolymorphicObject.

The documentation for this class was generated from the following file:

· ginkgo/core/base/polymorphic object.hpp

## 46.78 gko::solver::EnableApplyWithInitialGuess< DerivedType > Class Template Reference

EnableApplyWithInitialGuess providing default operation for ApplyWithInitialGuess with correct validation and log.

#include <ginkgo/core/solver/solver\_base.hpp>

## 46.78.1 Detailed Description

template<typename DerivedType> class gko::solver::EnableApplyWithInitialGuess< DerivedType >

EnableApplyWithInitialGuess providing default operation for ApplyWithInitialGuess with correct validation and log.

It ensures that vectors of apply\_with\_initial\_guess will always have the same executor as the object this mixin is used in, creating a clone on the correct executor if necessary.

### **Template Parameters**

DerivedType	The type that this Mixin is used in. It must provide get_size() and get_executor() functions that
	return correctly initialized values and the logger functionality.

The documentation for this class was generated from the following file:

• ginkgo/core/solver/solver base.hpp

## 46.79 gko::batch::EnableBatchLinOp< ConcreteBatchLinOp, PolymorphicBase > Class Template Reference

The EnableBatchLinOp mixin can be used to provide sensible default implementations of the majority of the Batch← LinOp and PolymorphicObject interface.

#include <ginkgo/core/base/batch\_lin\_op.hpp>

### **Additional Inherited Members**

## 46.79.1 Detailed Description

template<typename ConcreteBatchLinOp, typename PolymorphicBase = BatchLinOp> class gko::batch::EnableBatchLinOp< ConcreteBatchLinOp, PolymorphicBase >

The EnableBatchLinOp mixin can be used to provide sensible default implementations of the majority of the Batch 
LinOp and PolymorphicObject interface.

The goal of the mixin is to facilitate the development of new BatchLinOp, by enabling the implementers to focus on the important parts of their operator, while the library takes care of generating the trivial utility functions. The mixin will provide default implementations for the entire PolymorphicObject interface, including a default implementation of copy\_from between objects of the new BatchLinOp type.

Implementers of new BatchLinOps are required to specify only the following aspects:

1. Creation of the BatchLinOp: This can be facilitated via either <a href="EnableCreateMethod">EnableCreateMethod</a> mixin (used mostly for matrix formats), or <a href="GKO\_ENABLE\_BATCH\_LIN\_OP\_FACTORY">GKO\_ENABLE\_BATCH\_LIN\_OP\_FACTORY</a> macro (used for operators created from other operators, like preconditioners and solvers).

### **Template Parameters**

ConcreteBatchLinOp	the concrete BatchLinOp which is being implemented [CRTP parameter]
PolymorphicBase	parent of ConcreteBatchLinOp in the polymorphic hierarchy, has to be a subclass of BatchLinOp

The documentation for this class was generated from the following file:

ginkgo/core/base/batch\_lin\_op.hpp

## 46.80 gko::batch::solver::EnableBatchSolver< ConcreteSolver, ValueType, PolymorphicBase > Class Template Reference

This mixin provides apply and common iterative solver functionality to all the batched solvers.

#include <ginkgo/core/solver/batch\_solver\_base.hpp>

## **Additional Inherited Members**

## 46.80.1 Detailed Description

template<typename ConcreteSolver, typename ValueType, typename PolymorphicBase = BatchLinOp> class gko::batch::solver::EnableBatchSolver< ConcreteSolver, ValueType, PolymorphicBase >

This mixin provides apply and common iterative solver functionality to all the batched solvers.

### **Template Parameters**

ConcreteSolver	The concrete solver class.
ValueType	The value type of the multivectors.
PolymorphicBase	The base class; must be a subclass of BatchLinOp.

The documentation for this class was generated from the following file:

· ginkgo/core/solver/batch solver base.hpp

## 46.81 gko::EnableCreateMethod< ConcreteType > Class Template Reference

This mixin implements a static create() method on ConcreteType that dynamically allocates the memory, uses the passed-in arguments to construct the object, and returns an std::unique ptr to such an object.

#include <ginkgo/core/base/polymorphic\_object.hpp>

## 46.81.1 Detailed Description

template<typename ConcreteType> class gko::EnableCreateMethod< ConcreteType >

This mixin implements a static create() method on ConcreteType that dynamically allocates the memory, uses the passed-in arguments to construct the object, and returns an std::unique ptr to such an object.

## **Template Parameters**

ConcreteObject	the concrete type for which create() is being implemented [CRTP parameter]

The documentation for this class was generated from the following file:

• ginkgo/core/base/polymorphic\_object.hpp

# 46.82 gko::EnableDefaultFactory< ConcreteFactory, ProductType, ParametersType, PolymorphicBase > Class Template Reference

This mixin provides a default implementation of a concrete factory.

#include <ginkgo/core/base/abstract\_factory.hpp>

## **Public Member Functions**

const parameters\_type & get\_parameters () const noexcept
 Returns the parameters of the factory.

## **Static Public Member Functions**

• static parameters\_type create ()

Creates a new ParametersType object which can be used to instantiate a new ConcreteFactory.

## 46.82.1 Detailed Description

template<typename ConcreteFactory, typename ProductType, typename ParametersType, typename PolymorphicBase> class gko::EnableDefaultFactory< ConcreteFactory, ProductType, ParametersType, PolymorphicBase >

This mixin provides a default implementation of a concrete factory.

It implements all the methods of AbstractFactory and PolymorphicObject. Its implementation of the generate — impl() method delegates the creation of the product by calling the ProductType::ProductType(const ConcreteFactory \*, const components\_type &) constructor. The factory also supports parameters by using the ParametersType structure, which is defined by the user.

For a simple example, see IntFactory in core/test/base/abstract\_factory.cpp.

## **Template Parameters**

ConcreteFactory	the concrete factory which is being implemented [CRTP parameter]
ProductType	the concrete type of products which this factory produces, has to be a subclass of PolymorphicBase::abstract_product_type
ParametersType	a type representing the parameters of the factory, has to inherit from the enable_parameters_type mixin
PolymorphicBase	parent of ConcreteFactory in the polymorphic hierarchy, has to be a subclass of AbstractFactory

## 46.82.2 Member Function Documentation

### 46.82.2.1 create()

```
template<typename ConcreteFactory , typename ProductType , typename ParametersType , typename PolymorphicBase > static parameters_type gko::EnableDefaultFactory< ConcreteFactory, ProductType, Parameters← Type, PolymorphicBase >::create ( ) [inline], [static]
```

Creates a new ParametersType object which can be used to instantiate a new ConcreteFactory.

This method does not construct the factory directly, but returns a new parameters\_type object, which can be used to set the parameters of the factory. Once the parameters have been set, the parameters\_type::on() method can be used to obtain an instance of the factory with those parameters.

### Returns

a default parameters\_type object

### 46.82.2.2 get\_parameters()

```
template<typename ConcreteFactory , typename ProductType , typename ParametersType , typename PolymorphicBase > const parameters_type& gko::EnableDefaultFactory< ConcreteFactory, ProductType, Parameters← Type, PolymorphicBase >::get_parameters ( ) const [inline], [noexcept]
```

Returns the parameters of the factory.

### Returns

the parameters of the factory

The documentation for this class was generated from the following file:

• ginkgo/core/base/abstract\_factory.hpp

# 46.83 gko::experimental::EnableDistributedLinOp< ConcreteLinOp, PolymorphicBase > Class Template Reference

This mixin does the same as EnableLinOp, but for concrete types that are derived from distributed::DistributedBase.

```
#include <ginkgo/core/distributed/lin_op.hpp>
```

## **Additional Inherited Members**

## 46.83.1 Detailed Description

template<typename ConcreteLinOp, typename PolymorphicBase = LinOp> class gko::experimental::EnableDistributedLinOp< ConcreteLinOp, PolymorphicBase >

This mixin does the same as EnableLinOp, but for concrete types that are derived from distributed::DistributedBase.

## See also

EnableLinOp.

### **Template Parameters**

ConcreteLinOp	the concrete LinOp which is being implemented that is derived from	
	distributed::DistributedBase [CRTP parameter]	
PolymorphicBase	parent of ConcreteLinOp in the polymorphic hierarchy, has to be a subclass of LinOp	

The documentation for this class was generated from the following file:

ginkgo/core/distributed/lin\_op.hpp

## 46.84 gko::experimental::EnableDistributedPolymorphicObject < ConcreteObject, PolymorphicBase > Class Template Reference

This mixin does the same as EnablePolymorphicObject, but for concrete types that are derived from distributed::DistributedBase.

#include <ginkgo/core/distributed/polymorphic\_object.hpp>

## 46.84.1 Detailed Description

template < typename ConcreteObject, typename PolymorphicBase = PolymorphicObject > class gko::experimental::EnableDistributedPolymorphicObject < ConcreteObject, PolymorphicBase >

This mixin does the same as EnablePolymorphicObject, but for concrete types that are derived from distributed::DistributedBase.

### See also

EnablePolymporphicObject.

### The following is a minimal example of a distributed PolymorphicObject:

## **Template Parameters**

ConcreteObject	the concrete type which is being implemented that is derived from distributed::DistributedBase [CRTP parameter]
PolymorphicBase	parent of ConcreteObject in the polymorphic hierarchy, has to be a subclass of polymorphic object

The documentation for this class was generated from the following file:

• ginkgo/core/distributed/polymorphic\_object.hpp

## 46.85 gko::solver::EnableIterativeBase< DerivedType > Class Template Reference

A LinOp deriving from this CRTP class stores a stopping criterion factory and allows applying with a guess.

#include <ginkgo/core/solver/solver\_base.hpp>

## **Public Member Functions**

• EnableIterativeBase & operator= (const EnableIterativeBase &other)

Creates a shallow copy of the provided stopping criterion, clones it onto this executor if executors don't match.

• EnableIterativeBase & operator= (EnableIterativeBase &&other)

Moves the provided stopping criterion, clones it onto this executor if executors don't match.

• EnableIterativeBase (const EnableIterativeBase &other)

Creates a shallow copy of the provided stopping criterion.

• EnableIterativeBase (EnableIterativeBase &&other)

Moves the provided stopping criterion.

• void set\_stop\_criterion\_factory (std::shared\_ptr< const stop::CriterionFactory > new\_stop\_factory) override Sets the stopping criterion of the solver.

## 46.85.1 Detailed Description

```
template<typename DerivedType>
class gko::solver::EnableIterativeBase< DerivedType >
```

A LinOp deriving from this CRTP class stores a stopping criterion factory and allows applying with a guess.

**Template Parameters** 

```
DerivedType the CRTP type that derives from this
```

## 46.85.2 Constructor & Destructor Documentation

## 46.85.2.1 EnableIterativeBase()

Moves the provided stopping criterion.

The moved-from object has a nullptr stopping criterion.

## 46.85.3 Member Function Documentation

### 46.85.3.1 operator=()

Moves the provided stopping criterion, clones it onto this executor if executors don't match.

The moved-from object has a nullptr stopping criterion.

## 46.85.3.2 set\_stop\_criterion\_factory()

Sets the stopping criterion of the solver.

#### **Parameters**

other the	new stopping criterion factory
-----------	--------------------------------

Reimplemented from gko::solver::IterativeBase.

 $\label{lem:base} Referenced \ by \ gko::solver::EnableIterativeBase < Bicg < ValueType > > ::operator = ().$ 

The documentation for this class was generated from the following file:

• ginkgo/core/solver/solver\_base.hpp

# 46.86 gko::EnableLinOp< ConcreteLinOp, PolymorphicBase > Class Template Reference

The EnableLinOp mixin can be used to provide sensible default implementations of the majority of the LinOp and PolymorphicObject interface.

```
#include <ginkgo/core/base/lin_op.hpp>
```

## **Additional Inherited Members**

## 46.86.1 Detailed Description

```
template<typename ConcreteLinOp, typename PolymorphicBase = LinOp> class gko::EnableLinOp< ConcreteLinOp, PolymorphicBase >
```

The EnableLinOp mixin can be used to provide sensible default implementations of the majority of the LinOp and PolymorphicObject interface.

The goal of the mixin is to facilitate the development of new LinOp, by enabling the implementers to focus on the important parts of their operator, while the library takes care of generating the trivial utility functions. The mixin will provide default implementations for the entire PolymorphicObject interface, including a default implementation of copy\_from between objects of the new LinOp type. It will also hide the default LinOp::apply() methods with versions that preserve the static type of the object.

Implementers of new LinOps are required to specify only the following aspects:

- Creation of the LinOp: This can be facilitated via either EnableCreateMethod mixin (used mostly for matrix formats), or GKO\_ENABLE\_LIN\_OP\_FACTORY macro (used for operators created from other operators, like preconditioners and solvers).
- 2. Application of the LinOp: Implementers have to override the two overloads of the LinOp::apply\_impl() virtual methods.

### Note

This mixin can't be used with concrete types that derive from experimental::distributed::DistributedBase. In that case use experimental::EnableDistributedLinOp instead.

### **Template Parameters**

ConcreteLinOp	the concrete LinOp which is being implemented [CRTP parameter]
PolymorphicBase	parent of ConcreteLinOp in the polymorphic hierarchy, has to be a subclass of LinOp

The documentation for this class was generated from the following file:

· ginkgo/core/base/lin\_op.hpp

## 46.87 gko::log::EnableLogging< ConcreteLoggable, PolymorphicBase > Class Template Reference

EnableLogging is a mixin which should be inherited by any class which wants to enable logging.

```
#include <ginkgo/core/log/logger.hpp>
```

### 46.87.1 Detailed Description

template < typename ConcreteLoggable, typename PolymorphicBase = Loggable > class gko::log::EnableLogging < ConcreteLoggable, PolymorphicBase >

EnableLogging is a mixin which should be inherited by any class which wants to enable logging.

All the received events are passed to the loggers this class contains.

### **Template Parameters**

ConcreteLoggable	the object being logged [CRTP parameter]
PolymorphicBase	the polymorphic base of this class. By default it is Loggable. Change it if you want to use
	a new superclass of Loggable as polymorphic base of this class.  Generated by Doxygen

The documentation for this class was generated from the following file:

· ginkgo/core/log/logger.hpp

## 46.88 gko::multigrid::EnableMultigridLevel < ValueType > Class Template Reference

The EnableMultigridLevel gives the default implementation of MultigridLevel with composition and provides set ← \_multigrid\_level function.

#include <ginkgo/core/multigrid/multigrid\_level.hpp>

### **Public Member Functions**

- std::shared\_ptr< const LinOp > get\_fine\_op () const override
   Returns the operator on fine level.
- std::shared\_ptr< const LinOp > get\_restrict\_op () const override
   Returns the restrict operator.
- std::shared\_ptr< const LinOp > get\_coarse\_op () const override
   Returns the operator on coarse level.
- std::shared\_ptr< const LinOp > get\_prolong\_op () const override
   Returns the prolong operator.

## 46.88.1 Detailed Description

template<typename ValueType>
class gko::multigrid::EnableMultigridLevel< ValueType >

The EnableMultigridLevel gives the default implementation of MultigridLevel with composition and provides set ← \_multigrid\_level function.

A class inherit from EnableMultigridLevel should use the this->get\_compositions()->apply(...) as its own apply, which represents op(b) = prolong(coarse(restrict(b))).

## 46.88.2 Member Function Documentation

### 46.88.2.1 get\_coarse\_op()

```
template<typename ValueType >
std::shared_ptr<const LinOp> gko::multigrid::EnableMultigridLevel< ValueType >::get_coarse_op
( ) const [inline], [override], [virtual]
```

Returns the operator on coarse level.

#### Returns

the operator on coarse level.

Implements gko::multigrid::MultigridLevel.

References gko::UseComposition < ValueType >::get\_operator\_at().

## 46.88.2.2 get\_fine\_op()

```
template<typename ValueType >
std::shared_ptr<const LinOp> gko::multigrid::EnableMultigridLevel< ValueType >::get_fine_op (
) const [inline], [override], [virtual]
```

Returns the operator on fine level.

### Returns

the operator on fine level.

Implements gko::multigrid::MultigridLevel.

## 46.88.2.3 get\_prolong\_op()

```
template<typename ValueType >
std::shared_ptr<const LinOp> gko::multigrid::EnableMultigridLevel< ValueType >::get_prolong←
_op ( ) const [inline], [override], [virtual]
```

Returns the prolong operator.

### Returns

the prolong operator.

Implements gko::multigrid::MultigridLevel.

 $References\ gko:: Use Composition < Value Type >:: get\_operator\_at().$ 

## 46.88.2.4 get\_restrict\_op()

```
template<typename ValueType >
std::shared_ptr<const LinOp> gko::multigrid::EnableMultigridLevel< ValueType >::get_restrict

_op ( ) const [inline], [override], [virtual]
```

Returns the restrict operator.

### Returns

the restrict operator.

Implements gko::multigrid::MultigridLevel.

References gko::UseComposition < ValueType >::get\_operator\_at().

The documentation for this class was generated from the following file:

• ginkgo/core/multigrid/multigrid level.hpp

## 46.89 gko::EnablePolymorphicAssignment< ConcreteType, ResultType > Class Template Reference

This mixin is used to enable a default PolymorphicObject::copy\_from() implementation for objects that have implemented conversions between them.

#include <ginkgo/core/base/polymorphic\_object.hpp>

### **Public Member Functions**

- void convert\_to (result\_type \*result) const override
   Converts the implementer to an object of type result\_type.
- void move\_to (result\_type \*result) override

Converts the implementer to an object of type result\_type by moving data from this object.

## 46.89.1 Detailed Description

```
\label{template} \textbf{typename ConcreteType}, \textbf{typename ResultType = ConcreteType} \\ \textbf{class gko::EnablePolymorphicAssignment} \\ \textbf{< ConcreteType}, \textbf{ResultType} \\ \textbf{>} \\ \\ \textbf{< ConcreteType}, \textbf{< ResultType} \\ \textbf{>} \\ \textbf{< ConcreteType}, \textbf{< C
```

This mixin is used to enable a default PolymorphicObject::copy\_from() implementation for objects that have implemented conversions between them.

The requirement is that there is either a conversion constructor from ConcreteType in ResultType, or a conversion operator to ResultType in ConcreteType.

## **Template Parameters**

ConcreteTy	ре	the concrete type from which the copy_from is being enabled [CRTP parameter]
ResultTy	ре	the type to which copy_from is being enabled

## 46.89.2 Member Function Documentation

## 46.89.2.1 convert\_to()

Converts the implementer to an object of type result\_type.

#### **Parameters**

result	the object used to store the result of the conversion
--------	---

Implements gko::ConvertibleTo < ResultType >.

## 46.89.2.2 move to()

Converts the implementer to an object of type result\_type by moving data from this object.

This method is used when the implementer is a temporary object, and move semantics can be used.

## **Parameters**

result	the object used to emplace the result of the conversion

## Note

ConvertibleTo::move\_to can be implemented by simply calling ConvertibleTo::convert\_to. However, this operation can often be optimized by exploiting the fact that implementer's data can be moved to the result.

Implements gko::ConvertibleTo < ResultType >.

The documentation for this class was generated from the following file:

• ginkgo/core/base/polymorphic\_object.hpp

## 46.90 gko::EnablePolymorphicObject< ConcreteObject, PolymorphicBase > Class Template Reference

This mixin inherits from (a subclass of) PolymorphicObject and provides a base implementation of a new concrete polymorphic object.

```
#include <ginkgo/core/base/polymorphic_object.hpp>
```

## 46.90.1 Detailed Description

```
template<typename ConcreteObject, typename PolymorphicBase = PolymorphicObject> class gko::EnablePolymorphicObject< ConcreteObject, PolymorphicBase >
```

This mixin inherits from (a subclass of) PolymorphicObject and provides a base implementation of a new concrete polymorphic object.

The mixin changes parameter and return types of appropriate public methods of PolymorphicObject in the same way EnableAbstractPolymorphicObject does. In addition, it also provides default implementations of PolymorphicObject's virtual methods by using the *executor default constructor* and the assignment operator of ConcreteObject. Consequently, the following is a minimal example of PolymorphicObject:

```
struct MyObject : EnablePolymorphicObject<MyObject> {
   MyObject(std::shared_ptr<const Executor> exec)
            : EnablePolymorphicObject<MyObject>(std::move(exec))
            {}
};
```

In a way, this mixin can be viewed as an extension of default constructor/destructor/assignment operators.

## Note

This mixin does not enable copying the polymorphic object to the object of the same type (i.e. it does not implement the ConvertibleTo<ConcreteObject> interface). To enable a default implementation of this interface see the EnablePolymorphicAssignment mixin.

This mixin can't be used with concrete types that derive from experimental::distributed::DistributedBase. In that case use experimental::EnableDistributedPolymorphicObject instead.

### **Template Parameters**

ConcreteObject	the concrete type which is being implemented [CRTP parameter]
PolymorphicBase	parent of ConcreteObject in the polymorphic hierarchy, has to be a subclass of polymorphic object

The documentation for this class was generated from the following file:

• ginkgo/core/base/polymorphic object.hpp

## 46.91 gko::solver::EnablePreconditionable< DerivedType > Class Template Reference

Mixin providing default operation for Preconditionable with correct value semantics.

```
#include <ginkgo/core/solver/solver_base.hpp>
```

## **Public Member Functions**

• void set\_preconditioner (std::shared\_ptr< const LinOp > new\_precond) override

Sets the preconditioner operator used by the Preconditionable.

EnablePreconditionable & operator= (const EnablePreconditionable & other)

Creates a shallow copy of the provided preconditioner, clones it onto this executor if executors don't match.

• EnablePreconditionable & operator= (EnablePreconditionable &&other)

Moves the provided preconditioner, clones it onto this executor if executors don't match.

• EnablePreconditionable (const EnablePreconditionable &other)

Creates a shallow copy of the provided preconditioner.

• EnablePreconditionable (EnablePreconditionable &&other)

Moves the provided preconditioner.

## 46.91.1 Detailed Description

```
template<typename DerivedType> class gko::solver::EnablePreconditionable< DerivedType >
```

Mixin providing default operation for Preconditionable with correct value semantics.

It ensures that the preconditioner stored in this class will always have the same executor as the object this mixin is used in, creating a clone on the correct executor if necessary.

### **Template Parameters**

DerivedType	The type that this Mixin is used in. It must provide get_size() and get_executor() functions that
	return correctly initialized values when the EnablePreconditionable constructor is called, i.e. the
	constructor must be provided by a base class added before EnablePreconditionable, since the
	member initialization order also applying to multiple inheritance.

## 46.91.2 Constructor & Destructor Documentation

## 46.91.2.1 EnablePreconditionable()

Moves the provided preconditioner.

The moved-from object has a nullptr preconditioner.

### 46.91.3 Member Function Documentation

## 46.91.3.1 operator=()

Moves the provided preconditioner, clones it onto this executor if executors don't match.

The moved-from object has a nullptr preconditioner.

## 46.91.3.2 set\_preconditioner()

Sets the preconditioner operator used by the Preconditionable.

### **Parameters**

new\_precond the new preconditioner operator used by the Preconditionable

Reimplemented from gko::Preconditionable.

Referenced by gko::solver::EnablePreconditionable 
Sicg 
ValueType 
> ::operator=().

The documentation for this class was generated from the following file:

• ginkgo/core/solver/solver\_base.hpp

## 46.92 gko::solver::EnablePreconditionedIterativeSolver< ValueType, DerivedType > Class Template Reference

A LinOp implementing this interface stores a system matrix and stopping criterion factory.

```
#include <ginkgo/core/solver/solver_base.hpp>
```

### **Additional Inherited Members**

## 46.92.1 Detailed Description

```
template<typename ValueType, typename DerivedType> class gko::solver::EnablePreconditionedIterativeSolver< ValueType, DerivedType>
```

A LinOp implementing this interface stores a system matrix and stopping criterion factory.

## **Template Parameters**

ValueType	the value type that iterative solver uses for its vectors
DerivedType	the CRTP type that derives from this

The documentation for this class was generated from the following file:

• ginkgo/core/solver/solver\_base.hpp

## 46.93 gko::solver::EnableSolverBase< DerivedType, MatrixType > Class Template Reference

A LinOp deriving from this CRTP class stores a system matrix.

#include <ginkgo/core/solver/solver\_base.hpp>

### **Public Member Functions**

EnableSolverBase & operator= (const EnableSolverBase & other)

Creates a shallow copy of the provided system matrix, clones it onto this executor if executors don't match.

EnableSolverBase & operator= (EnableSolverBase &&other)

Moves the provided system matrix, clones it onto this executor if executors don't match.

EnableSolverBase (const EnableSolverBase & other)

Creates a shallow copy of the provided system matrix.

EnableSolverBase (EnableSolverBase &&other)

Moves the provided system matrix.

std::vector< int > get\_workspace\_scalars () const override

Returns the IDs of all scalars (workspace vectors with system dimension-independent size, usually 1 x num rhs).

std::vector< int > get\_workspace\_vectors () const override

Returns the IDs of all vectors (workspace vectors with system dimension-dependent size, usually system\_matrix\_size x num\_rhs).

## 46.93.1 Detailed Description

template<typename DerivedType, typename MatrixType = LinOp> class gko::solver::EnableSolverBase< DerivedType, MatrixType >

A LinOp deriving from this CRTP class stores a system matrix.

### **Template Parameters**

DerivedType	the CRTP type that derives from this
MatrixType	the concrete matrix type to be stored as system_matrix

### 46.93.2 Constructor & Destructor Documentation

### 46.93.2.1 EnableSolverBase()

Moves the provided system matrix.

The moved-from object has a nullptr system matrix.

### 46.93.3 Member Function Documentation

## 46.93.3.1 operator=()

Moves the provided system matrix, clones it onto this executor if executors don't match.

The moved-from object has a nullptr system matrix.

The documentation for this class was generated from the following file:

• ginkgo/core/solver/solver\_base.hpp

## 46.94 gko::experimental::mpi::environment Class Reference

Class that sets up and finalizes the MPI environment.

```
#include <ginkgo/core/base/mpi.hpp>
```

## **Public Member Functions**

• int get\_provided\_thread\_support () const

Return the provided thread support.

- environment (int &argc, char \*\*&argv, const thread\_type thread\_t=thread\_type::serialized)
  - Call MPI\_Init\_thread and initialize the MPI environment.
- ∼environment ()

Call MPI\_Finalize at the end of the scope of this class.

## 46.94.1 Detailed Description

Class that sets up and finalizes the MPI environment.

This class is a simple RAII wrapper to MPI\_Init and MPI\_Finalize.

MPI Init must have been called before calling any MPI functions.

Note

If MPI\_Init has already been called, then this class should not be used.

## 46.94.2 Constructor & Destructor Documentation

### 46.94.2.1 environment()

Call MPI\_Init\_thread and initialize the MPI environment.

### **Parameters**

argc	the number of arguments to the main function.
argv	the arguments provided to the main function.
thread←	the type of threading for initialization. See @thread_type
t	

## 46.94.3 Member Function Documentation

### 46.94.3.1 get provided thread support()

```
int gko::experimental::mpi::environment::get_provided_thread_support ( ) const [inline]
```

Return the provided thread support.

## Returns

the provided thread support

The documentation for this class was generated from the following file:

• ginkgo/core/base/mpi.hpp

# 46.95 gko::Error Class Reference

The Error class is used to report exceptional behaviour in library functions.

```
#include <ginkgo/core/base/exception.hpp>
```

#### **Public Member Functions**

- Error (const std::string &file, int line, const std::string &what)

  Initializes an error.
- virtual const char \* what () const noexcept override
   Returns a human-readable string with a more detailed description of the error.

## 46.95.1 Detailed Description

The Error class is used to report exceptional behaviour in library functions.

Ginkgo uses C++ exception mechanism to this end, and the Error class represents a base class for all types of errors. The exact list of errors which could occur during the execution of a certain library routine is provided in the documentation of that routine, along with a short description of the situation when that error can occur. During runtime, these errors can be detected by using standard C++ try-catch blocks, and a human-readable error description can be obtained by calling the Error::what() method.

As an example, trying to compute a matrix-vector product with arguments of incompatible size will result in a DimensionMismatch error, which is demonstrated in the following program.

```
#include <ginkgo.h>
#include <iostream>
using namespace gko;
int main()
{
    auto omp = create<OmpExecutor>();
    auto A = randn_fill<matrix::Csr<float>(5, 5, 0f, 1f, omp);
    auto x = fill<matrix::Dense<float>(6, 1, 1f, omp);
    try {
        auto y = apply(A, x);
    } catch(Error e) {
        // an error occurred, write the message to screen and exit std::cout « e.what() « std::endl;
        return -1;
    }
    return 0;
```

## 46.95.2 Constructor & Destructor Documentation

## 46.95.2.1 Error()

Initializes an error.

#### **Parameters**

file	The name of the offending source file
line	The source code line number where the error occurred
what	The error message

The documentation for this class was generated from the following file:

• ginkgo/core/base/exception.hpp

# 46.96 gko::Executor Class Reference

The first step in using the Ginkgo library consists of creating an executor.

#include <ginkgo/core/base/executor.hpp>

#### **Public Member Functions**

virtual void run (const Operation &op) const =0

Runs the specified Operation using this Executor.

template < typename ClosureOmp, typename ClosureCuda, typename ClosureHip, typename ClosureDpcpp > void run (const ClosureOmp & op\_omp, const ClosureCuda & op\_cuda, const ClosureHip & op\_hip, const ClosureDpcpp & op dpcpp) const

Runs one of the passed in functors, depending on the Executor type.

template < typename ClosureReference , typename ClosureOmp , typename ClosureCuda , typename ClosureHip , typename Closure ← Dpcpp >

void run (std::string name, const ClosureReference &op\_ref, const ClosureOmp &op\_omp, const Closure ← Cuda &op\_cuda, const ClosureHip &op\_hip, const ClosureDpcpp &op\_dpcpp) const

Runs one of the passed in functors, depending on the Executor type.

• template<typename T >

T \* alloc (size\_type num\_elems) const

Allocates memory in this Executor.

void free (void \*ptr) const noexcept

Frees memory previously allocated with Executor::alloc().

template<typename T >

void copy\_from (ptr\_param< const Executor > src\_exec, size\_type num\_elems, const T \*src\_ptr, T \*dest⇔\_ptr) const

Copies data from another Executor.

 $\bullet \ \ template {<} typename \ T >$ 

void copy (size\_type num\_elems, const T \*src\_ptr, T \*dest\_ptr) const

Copies data within this Executor.

• template<typename T >

T copy val to host (const T \*ptr) const

Retrieves a single element at the given location from executor memory.

virtual std::shared\_ptr< Executor > get\_master () noexcept=0

Returns the master OmpExecutor of this Executor.

virtual std::shared\_ptr< const Executor > get\_master () const noexcept=0

Returns the master OmpExecutor of this Executor.

virtual void synchronize () const =0

Synchronize the operations launched on the executor with its master.

- void add\_logger (std::shared\_ptr< const log::Logger > logger) override
- void remove\_logger (const log::Logger \*logger) override
- void set log propagation mode (log propagation mode mode)

Sets the logger event propagation mode for the executor.

bool should\_propagate\_log () const

Returns true iff events occurring at an object created on this executor should be logged at propagating loggers attached to this executor, and there is at least one such propagating logger.

bool memory\_accessible (const std::shared\_ptr< const Executor > &other) const

Verifies whether the executors share the same memory.

virtual std::string get\_description () const =0

## 46.96.1 Detailed Description

The first step in using the Ginkgo library consists of creating an executor.

Executors are used to specify the location for the data of linear algebra objects, and to determine where the operations will be executed. Ginkgo currently supports five different executor types:

- OmpExecutor specifies that the data should be stored and the associated operations executed on an Open
   — MP-supporting device (e.g. host CPU);
- CudaExecutor specifies that the data should be stored and the operations executed on the NVIDIA GPU accelerator;
- HipExecutor specifies that the data should be stored and the operations executed on either an NVIDIA or AMD GPU accelerator;
- DpcppExecutor specifies that the data should be stored and the operations executed on an hardware supporting DPC++;
- ReferenceExecutor executes a non-optimized reference implementation, which can be used to debug the library.

The following code snippet demonstrates the simplest possible use of the Ginkgo library:

```
auto omp = gko::create<gko::OmpExecutor>();
auto A = gko::read_from_mtx<gko::matrix::Csr<float»("A.mtx", omp);</pre>
```

First, we create a OMP executor, which will be used in the next line to specify where we want the data for the matrix A to be stored. The second line will read a matrix from the matrix market file 'A.mtx', and store the data on the CPU in CSR format (gko::matrix::Csr is a Ginkgo matrix class which stores its data in CSR format). At this point, matrix A is bound to the CPU, and any routines called on it will be performed on the CPU. This approach is usually desired in sparse linear algebra, as the cost of individual operations is several orders of magnitude lower than the cost of copying the matrix to the GPU.

If matrix A is going to be reused multiple times, it could be beneficial to copy it over to the accelerator, and perform the operations there, as demonstrated by the next code snippet:

```
auto cuda = gko::create<gko::CudaExecutor>(0, omp);
auto dA = gko::copy_to<gko::matrix::Csr<float»(A.get(), cuda);</pre>
```

The first line of the snippet creates a new CUDA executor. Since there may be multiple NVIDIA GPUs present on the system, the first parameter instructs the library to use the first device (i.e. the one with device ID zero, as in cudaSetDevice() routine from the CUDA runtime API). In addition, since GPUs are not stand-alone processors, it is required to pass a "master" OmpExecutor which will be used to schedule the requested CUDA kernels on the accelerator.

The second command creates a copy of the matrix A on the GPU. Notice the use of the get() method. As Ginkgo aims to provide automatic memory management of its objects, the result of calling gko::read\_from\_mtx() is a smart pointer (std::unique\_ptr) to the created object. On the other hand, as the library will not hold a reference to A once the copy is completed, the input parameter for gko::copy\_to() is a plain pointer. Thus, the get() method is used to convert from a std::unique\_ptr to a plain pointer, as expected by gko::copy\_to().

As a side note, the gko::copy\_to routine is far more powerful than just copying data between different devices. It can also be used to convert data between different formats. For example, if the above code used gko::matrix::Ell as the template parameter, dA would be stored on the GPU, in ELLPACK format.

Finally, if all the processing of the matrix is supposed to be done on the GPU, and a CPU copy of the matrix is not required, we could have read the matrix to the GPU directly:

```
auto omp = gko::create<gko::OmpExecutor>();
auto cuda = gko::create<gko::CudaExecutor>(0, omp);
auto dA = gko::read_from_mtx<gko::matrix::Csr<float>("A.mtx", cuda);
```

Notice that even though reading the matrix directly from a file to the accelerator is not supported, the library is designed to abstract away the intermediate step of reading the matrix to the CPU memory. This is a general design approach taken by the library: in case an operation is not supported by the device, the data will be copied to the CPU, the operation performed there, and finally the results copied back to the device. This approach makes using the library more concise, as explicit copies are not required by the user. Nevertheless, this feature should be taken into account when considering performance implications of using such operations.

#### 46.96.2 Member Function Documentation

## 46.96.2.1 add\_logger()

Note

This specialization keeps track of whether any propagating loggers were attached to the executor.

See also

Logger::needs\_propagation()

Implements gko::log::Loggable.

# 46.96.2.2 alloc()

Allocates memory in this Executor.

## **Template Parameters**

```
T datatype to allocate
```

#### **Parameters**

num_elems	number of elements of type T to allocate
-----------	--

## **Exceptions**

## Returns

pointer to allocated memory

## 46.96.2.3 copy()

Copies data within this Executor.

## **Template Parameters**

```
T datatype to copy
```

## **Parameters**

num_elems	number of elements of type T to copy	
src_ptr pointer to a block of memory containing the data to be copied		
dest_ptr	pointer to an allocated block of memory where the data will be copied to	

References copy\_from().

## 46.96.2.4 copy\_from()

```
size_type num_elems,
const T * src_ptr,
T * dest_ptr ) const [inline]
```

Copies data from another Executor.

## **Template Parameters**

```
T datatype to copy
```

#### **Parameters**

src_exec	Executor from which the memory will be copied
num_elems   number of elements of type T to copy	
src_ptr	pointer to a block of memory containing the data to be copied
dest_ptr	pointer to an allocated block of memory where the data will be copied to

References gko::ptr\_param< T >::get().

Referenced by copy().

## 46.96.2.5 copy\_val\_to\_host()

Retrieves a single element at the given location from executor memory.

#### **Template Parameters**

```
T datatype to copy
```

## **Parameters**

ptr the pointer to the element to be copied

#### Returns

the value stored at ptr

References get\_master().

#### 46.96.2.6 free()

Frees memory previously allocated with Executor::alloc().

If ptr is a nullptr, the function has no effect.

#### **Parameters**

ptr | pointer to the allocated memory block

## 46.96.2.7 get\_description()

```
virtual std::string gko::Executor::get_description ( ) const [pure virtual]
```

#### Returns

a textual representation of the executor and its device.

Implemented in gko::DpcppExecutor, gko::HipExecutor, gko::CudaExecutor, gko::ReferenceExecutor, and gko::OmpExecutor.

# 46.96.2.8 get\_master() [1/2]

```
virtual std::shared_ptr<const Executor> gko::Executor::get_master ( ) const [pure virtual],
[noexcept]
```

Returns the master OmpExecutor of this Executor.

#### Returns

the master OmpExecutor of this Executor.

Implemented in gko::DpcppExecutor, gko::HipExecutor, gko::CudaExecutor, and gko::OmpExecutor.

## 46.96.2.9 get\_master() [2/2]

```
virtual std::shared_ptr<Executor> gko::Executor::get_master ( ) [pure virtual], [noexcept]
```

Returns the master OmpExecutor of this Executor.

#### Returns

the master OmpExecutor of this Executor.

Implemented in gko::DpcppExecutor, gko::HipExecutor, gko::CudaExecutor, and gko::OmpExecutor.

Referenced by copy\_val\_to\_host().

#### 46.96.2.10 memory\_accessible()

Verifies whether the executors share the same memory.

#### **Parameters**

```
other the other Executor to compare against
```

#### Returns

whether the executors this and other share the same memory.

## 46.96.2.11 remove\_logger()

#### Note

This specialization keeps track of whether any propagating loggers were attached to the executor.

#### See also

Logger::needs\_propagation()

Implements gko::log::Loggable.

# 46.96.2.12 run() [1/3]

```
template<typename ClosureOmp , typename ClosureCuda , typename ClosureHip , typename Closure←Dpcpp >

void gko::Executor::run (

const ClosureOmp & op_omp,

const ClosureCuda & op_cuda,

const ClosureHip & op_hip,

const ClosureDpcpp & op_dpcpp ) const [inline]
```

Runs one of the passed in functors, depending on the Executor type.

# **Template Parameters**

ClosureOmp	type of op_omp
ClosureCuda	type of op_cuda
ClosureHip	type of op_hip
ClosureDpcpp	type of op_dpcpp

#### **Parameters**

op_omp	functor to run in case of a OmpExecutor or ReferenceExecutor		
op_cuda	functor to run in case of a CudaExecutor		
op_hip	functor to run in case of a HipExecutor		
op_dpcpp	functor to run in case of a DpcppExecutor		

References run().

## 46.96.2.13 run() [2/3]

Runs the specified Operation using this Executor.

#### **Parameters**

ор	the operation to run
----	----------------------

Implemented in gko::ReferenceExecutor.

Referenced by run().

## 46.96.2.14 run() [3/3]

Runs one of the passed in functors, depending on the Executor type.

## **Template Parameters**

ClosureReference	type of op_ref	
ClosureOmp	type of op_omp	
ClosureCuda	type of op_cuda	
ClosureHip	type of op_hip	
ClosureDpcpp	type of op_dpcpp	

#### **Parameters**

name	the name of the operation		
op_ref	functor to run in case of a ReferenceExecutor		
op_omp	functor to run in case of a OmpExecutor		
op_cuda	functor to run in case of a CudaExecutor		
op_hip	functor to run in case of a HipExecutor		
op_dpcpp	functor to run in case of a DpcppExecutor		

References run().

## 46.96.2.15 set\_log\_propagation\_mode()

Sets the logger event propagation mode for the executor.

This controls whether events that happen at objects created on this executor will also be logged at propagating loggers attached to the executor.

#### See also

Logger::needs\_propagation()

## 46.96.2.16 should\_propagate\_log()

```
bool gko::Executor::should_propagate_log ( ) const [inline]
```

Returns true iff events occurring at an object created on this executor should be logged at propagating loggers attached to this executor, and there is at least one such propagating logger.

#### See also

Logger::needs\_propagation()

Executor::set\_log\_propagation\_mode(log\_propagation\_mode)

References gko::automatic.

The documentation for this class was generated from the following file:

• ginkgo/core/base/executor.hpp

# 46.97 gko::log::executor\_data Struct Reference

Struct representing Executor related data.

#include <ginkgo/core/log/record.hpp>

## 46.97.1 Detailed Description

Struct representing Executor related data.

The documentation for this struct was generated from the following file:

• ginkgo/core/log/record.hpp

# 46.98 gko::executor deleter < T > Class Template Reference

This is a deleter that uses an executor's free method to deallocate the data.

#include <ginkgo/core/base/executor.hpp>

#### **Public Member Functions**

- executor\_deleter (std::shared\_ptr< const Executor > exec)
  - Creates a new deleter.
- void operator() (pointer ptr) const

Deletes the object.

## 46.98.1 Detailed Description

```
\label{template} \mbox{template} < \mbox{typename T} > \\ \mbox{class gko::executor\_deleter} < \mbox{T} > \\
```

This is a deleter that uses an executor's free method to deallocate the data.

**Template Parameters** 

T the type of object being deleted

## 46.98.2 Constructor & Destructor Documentation

#### 46.98.2.1 executor\_deleter()

Creates a new deleter.

**Parameters** 

```
exec the executor used to free the data
```

#### 46.98.3 Member Function Documentation

#### 46.98.3.1 operator()()

Deletes the object.

**Parameters** 

ptr pointer to the object being deleted

The documentation for this class was generated from the following file:

• ginkgo/core/base/executor.hpp

# 46.99 gko::experimental::factorization::Factorization < ValueType, IndexType > Class Template Reference

Represents a generic factorization consisting of two triangular factors (upper and lower) and an optional diagonal scaling matrix.

```
#include <ginkgo/core/factorization/factorization.hpp>
```

## **Public Member Functions**

std::unique\_ptr< Factorization > unpack () const

Transforms the factorization from a compact representation suitable only for triangular solves to a composition representation that can also be used to access individual factors and multiply with the factorization.

storage\_type get\_storage\_type () const

Returns the storage type used by this factorization.

std::shared\_ptr< const matrix\_type > get\_lower\_factor () const

Returns the lower triangular factor of the factorization, if available, nullptr otherwise.

• std::shared\_ptr< const diag\_type > get\_diagonal () const

Returns the diagonal scaling matrix of the factorization, if available, nullptr otherwise.

std::shared\_ptr< const matrix\_type > get\_upper\_factor () const

Returns the upper triangular factor of the factorization, if available, nullptr otherwise.

std::shared ptr< const matrix type > get combined () const

Returns the matrix storing a compact representation of the factorization, if available, nullptr otherwise.

Factorization (const Factorization &)

Creates a deep copy of the factorization.

Factorization (Factorization &&)

Moves from the given factorization, leaving it empty.

#### Static Public Member Functions

static std::unique\_ptr< Factorization > create\_from\_composition (std::unique\_ptr< composition\_type > composition)

Creates a Factorization from an existing composition.

• static std::unique\_ptr< Factorization > create\_from\_symm\_composition (std::unique\_ptr< composition\_type > composition)

Creates a Factorization from an existing symmetric composition.

• static std::unique\_ptr< Factorization > create\_from\_combined\_lu (std::unique\_ptr< matrix\_type > matrix)

Creates a Factorization from an existing combined representation of an LU factorization.

## 46.99.1 Detailed Description

```
template<typename ValueType, typename IndexType>
class gko::experimental::factorization::Factorization< ValueType, IndexType>
```

Represents a generic factorization consisting of two triangular factors (upper and lower) and an optional diagonal scaling matrix.

This class is used to represent a wide range of different factorizations to be passed on to direct solvers and other similar operations. The storage\_type represents how the individual factors are stored internally: They may be stored as separate matrices or in a single matrix, and be symmetric or unsymmetric, with the diagonal belonging to both factory, a single factor or being a separate scaling factor (Cholesky vs. LDL^H vs. LU vs. LDU).

## **Template Parameters**

ValueType	the value type used to store the factorization entries
IndexType	the index type used to represent the sparsity pattern

## 46.99.2 Member Function Documentation

## 46.99.2.1 create\_from\_combined\_lu()

Creates a Factorization from an existing combined representation of an LU factorization.

#### **Parameters**

n	าล	tt	Ίλ

the composition consisting of 2 or 3 elements. We expect the first entry to be a lower triangular matrix, and the last entry to be the transpose of the first entry. If the composition has 3 elements, we expect the middle entry to be a diagonal matrix.

#### Returns

a symmetric Factorization storing the elements from the Composition.

#### 46.99.2.2 create from composition()

Creates a Factorization from an existing composition.

#### **Parameters**

	sitior

the composition consisting of 2 or 3 elements. We expect the first entry to be a lower triangular matrix, and the last entry to be an upper triangular matrix. If the composition has 3 elements, we expect the middle entry to be a diagonal matrix.

#### Returns

a Factorization storing the elements from the Composition.

# 46.99.2.3 create\_from\_symm\_composition()

Creates a Factorization from an existing symmetric composition.

#### **Parameters**

composition	the composition consisting of 2 or 3 elements. We expect the first entry to be a lower triangular
	matrix, and the last entry to be the transpose of the first entry. If the composition has 3
	elements, we expect the middle entry to be a diagonal matrix.

#### Returns

a symmetric Factorization storing the elements from the Composition.

#### 46.99.2.4 unpack()

```
template<typename ValueType , typename IndexType >
std::unique_ptr<Factorization> gko::experimental::factorization::Factorization
ValueType,
IndexType >::unpack ( ) const
```

Transforms the factorization from a compact representation suitable only for triangular solves to a composition representation that can also be used to access individual factors and multiply with the factorization.

#### Returns

a new Factorization object containing this factorization represented as storage\_type::composition.

The documentation for this class was generated from the following file:

• ginkgo/core/factorization/factorization.hpp

# 46.100 gko::matrix::Fbcsr< ValueType, IndexType > Class Template Reference

Fixed-block compressed sparse row storage matrix format.

#include <ginkgo/core/matrix/fbcsr.hpp>

#### **Public Member Functions**

void convert\_to (Csr< ValueType, IndexType > \*result) const override

Converts the matrix to CSR format.

void convert\_to (SparsityCsr< ValueType, IndexType > \*result) const override

Get the block sparsity pattern in CSR-like format.

• void read (const mat\_data &data) override

Reads a matrix data into Fbcsr format.

· void read (const device\_mat\_data &data) override

Reads a matrix from a device\_matrix\_data structure.

· void read (device mat data &&data) override

Reads a matrix from a device\_matrix\_data structure.

· void write (mat data &data) const override

Writes a matrix to a matrix\_data structure.

• std::unique\_ptr< LinOp > transpose () const override

Returns a LinOp representing the transpose of the Transposable object.

• std::unique\_ptr< LinOp > conj\_transpose () const override

Returns a LinOp representing the conjugate transpose of the Transposable object.

std::unique\_ptr< Diagonal</li>
 ValueType > > extract\_diagonal () const override

Extracts the diagonal entries of the matrix into a vector.

• std::unique\_ptr< absolute\_type > compute\_absolute () const override

Gets the AbsoluteLinOp.

· void compute absolute inplace () override

Compute absolute inplace on each element.

void sort\_by\_column\_index ()

Sorts the values blocks and block-column indices in each row by column index.

bool is\_sorted\_by\_column\_index () const

Tests if all row entry pairs (value, col\_idx) are sorted by column index.

- value\_type \* get\_values () noexcept
- const value\_type \* get\_const\_values () const noexcept
- index\_type \* get\_col\_idxs () noexcept
- const index\_type \* get\_const\_col\_idxs () const noexcept
- index\_type \* get\_row\_ptrs () noexcept
- const index\_type \* get\_const\_row\_ptrs () const noexcept
- size type get num stored elements () const noexcept
- size\_type get\_num\_stored\_blocks () const noexcept
- int get\_block\_size () const noexcept
- index\_type get\_num\_block\_rows () const noexcept
- index\_type get\_num\_block\_cols () const noexcept
- Fbcsr & operator= (const Fbcsr &)

Copy-assigns an Fbcsr matrix.

Fbcsr & operator= (Fbcsr &&)

Move-assigns an Fbcsr matrix.

• Fbcsr (const Fbcsr &)

Copy-constructs an Ell matrix.

• Fbcsr (Fbcsr &&)

Move-constructs an Fbcsr matrix.

#### Static Public Member Functions

- static std::unique\_ptr< Fbcsr > create (std::shared\_ptr< const Executor > exec, int block\_size=1)

  Creates an uninitialized FBCSR matrix with the given block size.
- static std::unique\_ptr< Fbcsr > create (std::shared\_ptr< const Executor > exec, const dim< 2 > &size, size\_type num\_nonzeros, int block\_size)

Creates an uninitialized FBCSR matrix of the specified size.

• static std::unique\_ptr< Fbcsr > create (std::shared\_ptr< const Executor > exec, const dim< 2 > &size, int block size, array< value type > values, array< index type > col idxs, array< index type > row ptrs)

Creates a FBCSR matrix from already allocated (and initialized) row pointer, column index and value arrays.

template<typename InputValueType, typename InputColumnIndexType, typename InputRowPtrType>
 static std::unique\_ptr< Fbcsr > create (std::shared\_ptr< const Executor > exec, const dim< 2 > &size, int block\_size, std::initializer\_list< InputValueType > values, std::initializer\_list< InputColumnIndexType > col\_idxs, std::initializer\_list< InputRowPtrType > row\_ptrs)

create(std::shared\_ptr<const Executor>,

static std::unique\_ptr< const Fbcsr > create\_const (std::shared\_ptr< const Executor > exec, const dim
 2 > &size, int blocksize, gko::detail::const\_array\_view< ValueType > &&values, gko::detail::const\_array\_view< IndexType > &&row\_ptrs)

Creates a constant (immutable) Fbcsr matrix from a constant array.

## 46.100.1 Detailed Description

template<typename ValueType = default\_precision, typename IndexType = int32> class gko::matrix::Fbcsr< ValueType, IndexType >

Fixed-block compressed sparse row storage matrix format.

FBCSR is a matrix format meant for matrices having a natural block structure made up of small, dense, disjoint blocks. It is similar to CSR

See also

Csr. However, unlike Csr, each non-zero location stores a small dense block of entries having a constant size. This reduces the number of integers that need to be stored in order to refer to a given non-zero entry, and enables efficient implementation of certain block methods.

The block size is expected to be known in advance and passed to the constructor.

Note

The total number of rows and the number of columns are expected to be divisible by the block size.

The nonzero elements are stored in a 1D array row-wise, and accompanied with a row pointer array which stores the starting index of each block-row. An additional block-column index array is used to identify the block-column of each nonzero block.

#### The Fbcsr LinOp supports different operations:

## **Template Parameters**

ValueType	precision of matrix elements
IndexType	precision of matrix indexes

## 46.100.2 Constructor & Destructor Documentation

#### 46.100.2.1 Fbcsr() [1/2]

Copy-constructs an Ell matrix.

Inherits executor and data.

## 46.100.2.2 Fbcsr() [2/2]

Move-constructs an Fbcsr matrix.

Inherits executor and data. The moved-from object is empty (0x0 with no nonzeros, but valid row pointers).

## 46.100.3 Member Function Documentation

#### 46.100.3.1 compute\_absolute()

```
template<typename ValueType = default_precision, typename IndexType = int32>
std::unique_ptr<absolute_type> gko::matrix::Fbcsr< ValueType, IndexType >::compute_absolute (
) const [override], [virtual]
```

Gets the AbsoluteLinOp.

#### Returns

a pointer to the new absolute object

 $Implements\ gko:: Enable Absolute Computation < remove\_complex < Fbcsr < Value Type,\ Index Type >>>.$ 

#### 46.100.3.2 conj\_transpose()

```
template<typename ValueType = default_precision, typename IndexType = int32>
std::unique_ptr<LinOp> gko::matrix::Fbcsr< ValueType, IndexType >::conj_transpose ( ) const
[override], [virtual]
```

Returns a LinOp representing the conjugate transpose of the Transposable object.

Returns

a pointer to the new conjugate transposed object

Implements gko::Transposable.

#### 46.100.3.3 convert\_to() [1/2]

Converts the matrix to CSR format.

Note

Any explicit zeros in the original matrix are retained in the converted result.

#### 46.100.3.4 convert to() [2/2]

Get the block sparsity pattern in CSR-like format.

Note

The actual non-zero values are never copied; the result always has a value array of size 1 with the value 1.

#### 46.100.3.5 create() [1/4]

```
template<typename ValueType = default_precision, typename IndexType = int32>
static std::unique_ptr<Fbcsr> gko::matrix::Fbcsr< ValueType, IndexType >::create (
    std::shared_ptr< const Executor > exec,
    const dim< 2 > & size,
    int block_size,
    array< value_type > values,
    array< index_type > col_idxs,
    array< index_type > row_ptrs ) [static]
```

Creates a FBCSR matrix from already allocated (and initialized) row pointer, column index and value arrays.

#### **Parameters**

exec	Executor associated to the matrix
size	size of the matrix
block_size	Size of the small square dense nonzero blocks
values	the value array of the matrix, stored in column-major order for each block
col_idxs	the block column index array of the matrix
row_ptrs	the block row pointer array of the matrix

#### Note

If one of row\_ptrs, col\_idxs or values is not an rvalue, not an array of IndexType, IndexType and ValueType, respectively, or is on the wrong executor, an internal copy of that array will be created, and the original array data will not be used in the matrix.

#### Returns

A smart pointer to the newly created matrix.

#### 46.100.3.6 create() [2/4]

create(std::shared\_ptr<const Executor>,

create(std::shared\_ptr<const Executor>, const dim<2>&, int, array<value\_type>, array<index\_type>,
array<index\_type>)

References gko::matrix::Fbcsr< ValueType, IndexType >::create().

## 46.100.3.7 create() [3/4]

Creates an uninitialized FBCSR matrix of the specified size.

#### **Parameters**

exec	Executor associated to the matrix
size	size of the matrix
num_nonzeros	number of stored nonzeros. It needs to be a multiple of block_size * block_size.
block_size	size of the small dense square blocks

#### Returns

A smart pointer to the newly created matrix.

## 46.100.3.8 create() [4/4]

Creates an uninitialized FBCSR matrix with the given block size.

#### **Parameters**

exec	Executor associated to the matrix
block_size	The desired size of the dense square nonzero blocks; defaults to 1.

## Returns

A smart pointer to the newly created matrix.

Referenced by gko::matrix::Fbcsr< ValueType, IndexType >::create().

## 46.100.3.9 create\_const()

Creates a constant (immutable) Fbcsr matrix from a constant array.

#### **Parameters**

exec	the executor to create the matrix on
size	the dimensions of the matrix
blocksize	the block size of the matrix
values	the value array of the matrix, stored in column-major order for each block
col_idxs	the block column index array of the matrix
row_ptrs	the block row pointer array of the matrix

#### Returns

A smart pointer to the constant matrix wrapping the input arrays (if they reside on the same executor as the matrix) or a copy of the arrays on the correct executor.

## 46.100.3.10 extract\_diagonal()

```
template<typename ValueType = default_precision, typename IndexType = int32>
std::unique_ptr<Diagonal<ValueType> > gko::matrix::Fbcsr< ValueType, IndexType >::extract_
diagonal ( ) const [override], [virtual]
```

Extracts the diagonal entries of the matrix into a vector.

#### **Parameters**

diag	the vector into which the diagonal will be written
------	--

Implements gko::DiagonalExtractable < ValueType >.

## 46.100.3.11 get\_block\_size()

```
template<typename ValueType = default_precision, typename IndexType = int32>
int gko::matrix::Fbcsr< ValueType, IndexType >::get_block_size ( ) const [inline], [noexcept]
```

#### Returns

The fixed block size for this matrix

## 46.100.3.12 get\_col\_idxs()

```
template<typename ValueType = default_precision, typename IndexType = int32>
index_type* gko::matrix::Fbcsr< ValueType, IndexType >::get_col_idxs () [inline], [noexcept]
```

#### Returns

The column indexes of the matrix.

 $References\ gko::array < ValueType > ::get\_data().$ 

#### 46.100.3.13 get\_const\_col\_idxs()

```
template<typename ValueType = default_precision, typename IndexType = int32>
const index_type* gko::matrix::Fbcsr< ValueType, IndexType >::get_const_col_idxs ( ) const
[inline], [noexcept]
```

#### Returns

The column indexes of the matrix.

#### Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

References gko::array< ValueType >::get\_const\_data().

#### 46.100.3.14 get\_const\_row\_ptrs()

```
template<typename ValueType = default_precision, typename IndexType = int32>
const index_type* gko::matrix::Fbcsr< ValueType, IndexType >::get_const_row_ptrs ( ) const
[inline], [noexcept]
```

#### Returns

The row pointers of the matrix.

#### Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

References gko::array< ValueType >::get\_const\_data().

## 46.100.3.15 get\_const\_values()

```
template<typename ValueType = default_precision, typename IndexType = int32>
const value_type* gko::matrix::Fbcsr< ValueType, IndexType >::get_const_values ( ) const [inline],
[noexcept]
```

#### Returns

The values of the matrix.

#### Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

References gko::array< ValueType >::get\_const\_data().

## 46.100.3.16 get\_num\_block\_cols()

```
template<typename ValueType = default_precision, typename IndexType = int32>
index_type gko::matrix::Fbcsr< ValueType, IndexType >::get_num_block_cols ( ) const [inline],
[noexcept]
```

#### Returns

The number of block-columns in the matrix

## 46.100.3.17 get\_num\_block\_rows()

```
template<typename ValueType = default_precision, typename IndexType = int32>
index_type gko::matrix::Fbcsr< ValueType, IndexType >::get_num_block_rows ( ) const [inline],
[noexcept]
```

#### Returns

The number of block-rows in the matrix

## 46.100.3.18 get\_num\_stored\_blocks()

```
template<typename ValueType = default_precision, typename IndexType = int32>
size_type gko::matrix::Fbcsr< ValueType, IndexType >::get_num_stored_blocks ( ) const [inline],
[noexcept]
```

#### Returns

The number of non-zero blocks explicitly stored in the matrix

References gko::array< ValueType >::get\_size().

#### 46.100.3.19 get\_num\_stored\_elements()

```
template<typename ValueType = default_precision, typename IndexType = int32>
size_type gko::matrix::Fbcsr< ValueType, IndexType >::get_num_stored_elements ( ) const [inline],
[noexcept]
```

#### Returns

The number of elements explicitly stored in the matrix

References gko::array< ValueType >::get\_size().

#### 46.100.3.20 get\_row\_ptrs()

```
template<typename ValueType = default_precision, typename IndexType = int32>
index_type* gko::matrix::Fbcsr< ValueType, IndexType >::get_row_ptrs () [inline], [noexcept]
```

#### Returns

The row pointers of the matrix.

References gko::array< ValueType >::get\_data().

#### 46.100.3.21 get\_values()

```
template<typename ValueType = default_precision, typename IndexType = int32>
value_type* gko::matrix::Fbcsr< ValueType, IndexType >::get_values ( ) [inline], [noexcept]
```

#### Returns

The values of the matrix.

References gko::array< ValueType >::get data().

## 46.100.3.22 is\_sorted\_by\_column\_index()

```
template<typename ValueType = default_precision, typename IndexType = int32>
bool gko::matrix::Fbcsr< ValueType, IndexType >::is_sorted_by_column_index ( ) const
```

Tests if all row entry pairs (value, col\_idx) are sorted by column index.

## Returns

True if all row entry pairs (value, col idx) are sorted by column index

# 46.100.3.23 operator=() [1/2]

Copy-assigns an Fbcsr matrix.

Preserves the executor, copies data and block size from the input.

#### 46.100.3.24 operator=() [2/2]

Move-assigns an Fbcsr matrix.

Preserves the executor, moves the data over preserving size and stride. Leaves the moved-from object in an empty state (0x0 with no nonzeros, but valid row pointers).

#### 46.100.3.25 read() [1/3]

Reads a matrix from a device matrix data structure.

#### **Parameters**

```
data the device_matrix_data structure.
```

Reimplemented from gko::ReadableFromMatrixData< ValueType, IndexType >.

#### 46.100.3.26 read() [2/3]

Reads a matrix\_data into Fbcsr format.

Requires the block size to be set beforehand

See also

set\_block\_size.

Warning

Unlike Csr::read, here explicit non-zeros are NOT dropped.

Implements gko::ReadableFromMatrixData< ValueType, IndexType >.

## 46.100.3.27 read() [3/3]

Reads a matrix from a device matrix data structure.

The structure may be emptied by this function.

#### **Parameters**

```
data the device_matrix_data structure.
```

Reimplemented from gko::ReadableFromMatrixData< ValueType, IndexType >.

#### 46.100.3.28 transpose()

```
template<typename ValueType = default_precision, typename IndexType = int32>
std::unique_ptr<LinOp> gko::matrix::Fbcsr< ValueType, IndexType >::transpose ( ) const [override],
[virtual]
```

Returns a LinOp representing the transpose of the Transposable object.

#### Returns

a pointer to the new transposed object

Implements gko::Transposable.

#### 46.100.3.29 write()

Writes a matrix to a matrix\_data structure.

#### **Parameters**

```
data the matrix_data structure
```

Implements gko::WritableToMatrixData< ValueType, IndexType >.

The documentation for this class was generated from the following files:

- ginkgo/core/matrix/csr.hpp
- · ginkgo/core/matrix/fbcsr.hpp

# 46.101 gko::solver::Fcg< ValueType > Class Template Reference

FCG or the flexible conjugate gradient method is an iterative type Krylov subspace method which is suitable for symmetric positive definite methods.

#include <ginkgo/core/solver/fcg.hpp>

#### **Public Member Functions**

• std::unique\_ptr< LinOp > transpose () const override

Returns a LinOp representing the transpose of the Transposable object.

• std::unique\_ptr< LinOp > conj\_transpose () const override

Returns a LinOp representing the conjugate transpose of the Transposable object.

bool apply\_uses\_initial\_guess () const override

Return true as iterative solvers use the data in x as an initial guess.

#### **Static Public Member Functions**

• static parameters\_type parse (const config::pnode &config, const config::registry &context, const config::type\_descriptor &td\_for\_child=config::make\_type\_descriptor < ValueType >())

Create the parameters from the property\_tree.

## 46.101.1 Detailed Description

```
template<typename ValueType = default_precision> class gko::solver::Fcg< ValueType >
```

FCG or the flexible conjugate gradient method is an iterative type Krylov subspace method which is suitable for symmetric positive definite methods.

Though this method performs very well for symmetric positive definite matrices, it is in general not suitable for general matrices.

In contrast to the standard CG based on the Polack-Ribiere formula, the flexible CG uses the Fletcher-Reeves formula for creating the orthonormal vectors spanning the Krylov subspace. This increases the computational cost of every Krylov solver iteration but allows for non-constant preconditioners.

The implementation in Ginkgo makes use of the merged kernel to make the best use of data locality. The inner operations in one iteration of FCG are merged into 2 separate steps.

#### **Template Parameters**

ValueType	precision of matrix elements
-----------	------------------------------

#### 46.101.2 Member Function Documentation

#### 46.101.2.1 apply\_uses\_initial\_guess()

```
template<typename ValueType = default_precision>
bool gko::solver::Fcg< ValueType >::apply_uses_initial_guess ( ) const [inline], [override]
```

Return true as iterative solvers use the data in x as an initial guess.

#### Returns

true as iterative solvers use the data in x as an initial guess.

```
72 { return true; }
```

## 46.101.2.2 conj\_transpose()

```
template<typename ValueType = default_precision>
std::unique_ptr<LinOp> gko::solver::Fcg< ValueType >::conj_transpose ( ) const [override],
[virtual]
```

Returns a LinOp representing the conjugate transpose of the Transposable object.

#### Returns

a pointer to the new conjugate transposed object

Implements gko::Transposable.

## 46.101.2.3 parse()

Create the parameters from the property\_tree.

Because this is directly tied to the specific type, the value/index type settings within config are ignored and type\_ descriptor is only used for children configs.

## **Parameters**

config	the property tree for setting
context	the registry
td_for_child	the type descriptor for children configs. The default uses the value type of this class.

#### Returns

parameters

## 46.101.2.4 transpose()

```
template<typename ValueType = default_precision>
std::unique_ptr<LinOp> gko::solver::Fcg< ValueType >::transpose ( ) const [override], [virtual]
```

Returns a LinOp representing the transpose of the Transposable object.

#### Returns

a pointer to the new transposed object

Implements gko::Transposable.

The documentation for this class was generated from the following file:

· ginkgo/core/solver/fcg.hpp

# 46.102 gko::matrix::Fft Class Reference

This LinOp implements a 1D Fourier matrix using the FFT algorithm.

```
#include <ginkgo/core/matrix/fft.hpp>
```

# **Public Member Functions**

- std::unique\_ptr< LinOp > transpose () const override
   Returns a LinOp representing the transpose of the Transposable object.
- std::unique\_ptr< LinOp > conj\_transpose () const override

Returns a LinOp representing the conjugate transpose of the Transposable object.

- void write (matrix\_data < std::complex < float >, int32 > &data) const override
   Writes a matrix to a matrix\_data structure.
- void write (matrix\_data < std::complex < float >, int64 > &data) const override
   Writes a matrix to a matrix\_data structure.
- void write (matrix\_data < std::complex < double >, int32 > &data) const override
   Writes a matrix to a matrix\_data structure.
- void write (matrix\_data < std::complex < double >, int64 > &data) const override
   Writes a matrix to a matrix\_data structure.

#### **Static Public Member Functions**

- static std::unique\_ptr< Fft > create (std::shared\_ptr< const Executor > exec)
   Creates an empty Fourier matrix.
- static std::unique\_ptr< Fft > create (std::shared\_ptr< const Executor > exec, size\_type size=0, bool inverse=false)

Creates an Fourier matrix with the given dimensions.

## 46.102.1 Detailed Description

This LinOp implements a 1D Fourier matrix using the FFT algorithm.

It implements forward and inverse DFT.

For a power-of-two size n with corresponding root of unity  $\omega=e^{-2\pi i/n}$  for forward DFT and  $\omega=e^{2\pi i/n}$  for inverse DFT it computes

$$x_k = \sum_{j=0}^{n-1} \omega^{jk} b_j$$

without normalization factors.

The Reference and OpenMP implementations support only power-of-two input sizes, as they use the Radix-2 algorithm by J. W. Cooley and J. W. Tukey, "An Algorithm for the Machine Calculation of Complex Fourier Series," Mathematics of Computation, vol. 19, no. 90, pp. 297–301, 1965, doi: 10.2307/2003354. The CUDA and HIP implementations use cuSPARSE/hipSPARSE with full support for non-power-of-two input sizes and special optimizations for products of small prime powers.

#### 46.102.2 Member Function Documentation

## 46.102.2.1 conj\_transpose()

```
std::unique_ptr<LinOp> gko::matrix::Fft::conj_transpose ( ) const [override], [virtual]
```

Returns a LinOp representing the conjugate transpose of the Transposable object.

Returns

a pointer to the new conjugate transposed object

Implements gko::Transposable.

# 46.102.2.2 create() [1/2]

Creates an empty Fourier matrix.

#### **Parameters**

exec Executor associated to the matrix

#### Returns

A smart pointer to the newly created matrix.

## 46.102.2.3 create() [2/2]

Creates an Fourier matrix with the given dimensions.

#### **Parameters**

size	size of the matrix
inverse	true to compute an inverse DFT instead of a normal DFT

#### Returns

A smart pointer to the newly created matrix.

## 46.102.2.4 transpose()

```
std::unique_ptr<LinOp> gko::matrix::Fft::transpose ( ) const [override], [virtual]
```

Returns a LinOp representing the transpose of the Transposable object.

#### Returns

a pointer to the new transposed object

Implements gko::Transposable.

## 46.102.2.5 write() [1/4]

Writes a matrix to a matrix\_data structure.

#### **Parameters**

```
data the matrix_data structure
```

Implements gko::WritableToMatrixData< std::complex< double >, int32 >.

#### 46.102.2.6 write() [2/4]

Writes a matrix to a matrix\_data structure.

#### **Parameters**

```
data the matrix_data structure
```

Implements gko::WritableToMatrixData< std::complex< double >, int64 >.

## 46.102.2.7 write() [3/4]

Writes a matrix to a matrix\_data structure.

## **Parameters**

```
data the matrix_data structure
```

 $Implements\ gko::Writable To Matrix Data < std::complex < float >, int 32 >.$ 

#### 46.102.2.8 write() [4/4]

Writes a matrix to a matrix\_data structure.

#### **Parameters**

```
data the matrix_data structure
```

Implements gko::WritableToMatrixData< std::complex< float >, int64 >.

The documentation for this class was generated from the following file:

· ginkgo/core/matrix/fft.hpp

# 46.103 gko::matrix::Fft2 Class Reference

This LinOp implements a 2D Fourier matrix using the FFT algorithm.

#include <ginkgo/core/matrix/fft.hpp>

#### **Public Member Functions**

std::unique\_ptr< LinOp > transpose () const override
 Returns a LinOp representing the transpose of the Transposable object.

• std::unique\_ptr< LinOp > conj\_transpose () const override

Returns a LinOp representing the conjugate transpose of the Transposable object.

- void write (matrix\_data < std::complex < float >, int32 > &data) const override
   Writes a matrix to a matrix\_data structure.
- void write (matrix\_data < std::complex < float >, int64 > &data) const override
   Writes a matrix to a matrix data structure.
- void write (matrix\_data < std::complex < double >, int32 > &data) const override
   Writes a matrix to a matrix\_data structure.
- void write (matrix\_data < std::complex < double >, int64 > &data) const override
   Writes a matrix to a matrix\_data structure.

## **Static Public Member Functions**

- static std::unique\_ptr< Fft2 > create (std::shared\_ptr< const Executor > exec)
   Creates an empty Fourier matrix.
- static std::unique\_ptr< Fft2 > create (std::shared\_ptr< const Executor > exec, size\_type size)
   Creates an Fourier matrix with the given dimensions.
- static std::unique\_ptr< Fft2 > create (std::shared\_ptr< const Executor > exec, size\_type size1, size\_type size2, bool inverse=false)

Creates an Fourier matrix with the given dimensions.

## 46.103.1 Detailed Description

This LinOp implements a 2D Fourier matrix using the FFT algorithm.

For indexing purposes, the first dimension is the major axis.

It implements complex-to-complex forward and inverse FFT.

For a power-of-two sizes  $n_1,n_2$  with corresponding root of unity  $\omega=e^{-2\pi i/(n_1n_2)}$  for forward DFT and  $\omega=e^{2\pi i/(n_1n_2)}$  for inverse DFT it computes

$$x_{k_1 n_2 + k_2} = \sum_{i_1 = 0}^{n_1 - 1} \sum_{i_2 = 0}^{n_2 - 1} \omega^{i_1 k_1 + i_2 k_2} b_{i_1 n_2 + i_2}$$

without normalization factors.

The Reference and OpenMP implementations support only power-of-two input sizes, as they use the Radix-2 algorithm by J. W. Cooley and J. W. Tukey, "An Algorithm for the Machine Calculation of Complex Fourier Series," Mathematics of Computation, vol. 19, no. 90, pp. 297–301, 1965, doi: 10.2307/2003354. The CUDA and HIP implementations use cuSPARSE/hipSPARSE with full support for non-power-of-two input sizes and special optimizations for products of small prime powers.

# 46.103.2 Member Function Documentation

## 46.103.2.1 conj\_transpose()

```
std::unique_ptr<LinOp> gko::matrix::Fft2::conj_transpose ( ) const [override], [virtual]
```

Returns a LinOp representing the conjugate transpose of the Transposable object.

#### Returns

a pointer to the new conjugate transposed object

Implements gko::Transposable.

#### 46.103.2.2 create() [1/3]

Creates an empty Fourier matrix.

#### **Parameters**

```
exec Executor associated to the matrix
```

#### Returns

A smart pointer to the newly created matrix.

## 46.103.2.3 create() [2/3]

Creates an Fourier matrix with the given dimensions.

#### **Parameters**

size | size of both FFT dimensions

#### Returns

A smart pointer to the newly created matrix.

## 46.103.2.4 create() [3/3]

```
static std::unique_ptr<Fft2> gko::matrix::Fft2::create (
    std::shared_ptr< const Executor > exec,
    size_type size1,
    size_type size2,
    bool inverse = false ) [static]
```

Creates an Fourier matrix with the given dimensions.

#### **Parameters**

size1	size of the first FFT dimension
size2	size of the second FFT dimension
inverse	true to compute an inverse DFT instead of a normal DFT

## Returns

A smart pointer to the newly created matrix.

## 46.103.2.5 transpose()

```
std::unique_ptr<LinOp> gko::matrix::Fft2::transpose ( ) const [override], [virtual]
```

Returns a LinOp representing the transpose of the Transposable object.

## Returns

a pointer to the new transposed object

Implements gko::Transposable.

#### 46.103.2.6 write() [1/4]

Writes a matrix to a matrix\_data structure.

#### **Parameters**

```
data the matrix_data structure
```

Implements gko::WritableToMatrixData< std::complex< double >, int32 >.

## 46.103.2.7 write() [2/4]

Writes a matrix to a matrix\_data structure.

#### **Parameters**

```
data the matrix_data structure
```

Implements gko::WritableToMatrixData< std::complex< double >, int64 >.

## 46.103.2.8 write() [3/4]

Writes a matrix to a matrix\_data structure.

## **Parameters**

```
data the matrix_data structure
```

 $Implements\ gko::Writable To Matrix Data < std::complex < float >, int 32 >.$ 

### 46.103.2.9 write() [4/4]

Writes a matrix to a matrix\_data structure.

## **Parameters**

```
data the matrix_data structure
```

Implements gko::WritableToMatrixData< std::complex< float >, int64 >.

The documentation for this class was generated from the following file:

· ginkgo/core/matrix/fft.hpp

# 46.104 gko::matrix::Fft3 Class Reference

This LinOp implements a 3D Fourier matrix using the FFT algorithm.

#include <ginkgo/core/matrix/fft.hpp>

#### **Public Member Functions**

std::unique\_ptr< LinOp > transpose () const override
 Returns a LinOp representing the transpose of the Transposable object.

std::unique\_ptr< LinOp > conj\_transpose () const override

Returns a LinOp representing the conjugate transpose of the Transposable object.

- void write (matrix\_data < std::complex < float >, int32 > &data) const override
   Writes a matrix to a matrix\_data structure.
- void write (matrix\_data < std::complex < float >, int64 > &data) const override
   Writes a matrix to a matrix data structure.
- void write (matrix\_data < std::complex < double >, int32 > &data) const override
   Writes a matrix to a matrix\_data structure.
- void write (matrix\_data < std::complex < double >, int64 > &data) const override
   Writes a matrix to a matrix\_data structure.

## **Static Public Member Functions**

- static std::unique\_ptr< Fft3 > create (std::shared\_ptr< const Executor > exec)
   Creates an empty Fourier matrix.
- static std::unique\_ptr< Fft3 > create (std::shared\_ptr< const Executor > exec, size\_type size)
   Creates an Fourier matrix with the given dimensions.
- static std::unique\_ptr< Fft3 > create (std::shared\_ptr< const Executor > exec, size\_type size1, size\_type size2, size\_type size3, bool inverse=false)

Creates an Fourier matrix with the given dimensions.

## 46.104.1 Detailed Description

This LinOp implements a 3D Fourier matrix using the FFT algorithm.

For indexing purposes, the first dimension is the major axis.

It implements complex-to-complex forward and inverse FFT.

For a power-of-two sizes  $n_1,n_2,n_3$  with corresponding root of unity  $\omega=e^{-2\pi i/(n_1n_2n_3)}$  for forward DFT and  $\omega=e^{2\pi i/(n_1n_2n_3)}$  for inverse DFT it computes

$$x_{k_1 n_2 n_3 + k_2 n_3 + k_3} = \sum_{i_1 = 0}^{n_1 - 1} \sum_{i_2 = 0}^{n_2 - 1} \sum_{i_3 = 0}^{n_3 - 1} \omega^{i_1 k_1 + i_2 k_2 + i_3 k_3} b_{i_1 n_2 n_3 + i_2 n_3 + i_3}$$

without normalization factors.

The Reference and OpenMP implementations support only power-of-two input sizes, as they use the Radix-2 algorithm by J. W. Cooley and J. W. Tukey, "An Algorithm for the Machine Calculation of Complex Fourier Series," Mathematics of Computation, vol. 19, no. 90, pp. 297–301, 1965, doi: 10.2307/2003354. The CUDA and HIP implementations use cuSPARSE/hipSPARSE with full support for non-power-of-two input sizes and special optimizations for products of small prime powers.

## 46.104.2 Member Function Documentation

## 46.104.2.1 conj\_transpose()

```
std::unique_ptr<LinOp> gko::matrix::Fft3::conj_transpose ( ) const [override], [virtual]
```

Returns a LinOp representing the conjugate transpose of the Transposable object.

#### Returns

a pointer to the new conjugate transposed object

Implements gko::Transposable.

## 46.104.2.2 create() [1/3]

Creates an empty Fourier matrix.

### **Parameters**

```
exec Executor associated to the matrix
```

## Returns

A smart pointer to the newly created matrix.

## 46.104.2.3 create() [2/3]

Creates an Fourier matrix with the given dimensions.

#### **Parameters**

size size of all FFT dimensions

#### Returns

A smart pointer to the newly created matrix.

## 46.104.2.4 create() [3/3]

Creates an Fourier matrix with the given dimensions.

#### **Parameters**

size1	size of the first FFT dimension	
size2	size of the second FFT dimension	
size3 size of the third FFT dimension		
inverse	true to compute an inverse DFT instead of a normal DFT	

### Returns

A smart pointer to the newly created matrix.

## 46.104.2.5 transpose()

```
std::unique_ptr<LinOp> gko::matrix::Fft3::transpose ( ) const [override], [virtual]
```

Returns a LinOp representing the transpose of the Transposable object.

## Returns

a pointer to the new transposed object

Implements gko::Transposable.

## 46.104.2.6 write() [1/4]

Writes a matrix to a matrix\_data structure.

#### **Parameters**

```
data the matrix_data structure
```

Implements gko::WritableToMatrixData< std::complex< double >, int32 >.

## 46.104.2.7 write() [2/4]

Writes a matrix to a matrix\_data structure.

#### **Parameters**

```
data the matrix_data structure
```

Implements gko::WritableToMatrixData< std::complex< double >, int64 >.

## 46.104.2.8 write() [3/4]

Writes a matrix to a matrix\_data structure.

## **Parameters**

```
data the matrix_data structure
```

 $Implements\ gko::Writable To Matrix Data < std::complex < float >, int 32 >.$ 

### 46.104.2.9 write() [4/4]

Writes a matrix to a matrix\_data structure.

## **Parameters**

```
data the matrix_data structure
```

Implements gko::WritableToMatrixData< std::complex< float >, int64 >.

The documentation for this class was generated from the following file:

ginkgo/core/matrix/fft.hpp

# 46.105 gko::multigrid::FixedCoarsening< ValueType, IndexType > Class Template Reference

FixedCoarsening is a very simple coarse grid generation algorithm.

```
#include <ginkgo/core/multigrid/fixed_coarsening.hpp>
```

### **Public Member Functions**

 std::shared\_ptr< const LinOp > get\_system\_matrix () const Returns the system operator (matrix) of the linear system.

## 46.105.1 Detailed Description

template<typename ValueType = default\_precision, typename IndexType = int32> class gko::multigrid::FixedCoarsening< ValueType, IndexType >

FixedCoarsening is a very simple coarse grid generation algorithm.

It selects the coarse matrix from the fine matrix by with user-specified indices.

The user needs to specify the indices (with global numbering) of the fine matrix, they wish to be in the coarse matrix. The restriction and prolongation matrices will map to and from the coarse space without any interpolation or weighting.

## **Template Parameters**

	ValueType	precision of matrix elements
ſ	IndexType	precision of matrix indexes

## 46.105.2 Member Function Documentation

### 46.105.2.1 get\_system\_matrix()

```
template<typename ValueType = default_precision, typename IndexType = int32> std::shared_ptr<const LinOp> gko::multigrid::FixedCoarsening< ValueType, IndexType >::get_← system_matrix ( ) const [inline]
```

Returns the system operator (matrix) of the linear system.

#### Returns

the system operator (matrix)

```
58 {
59     return system_matrix_;
60 }
```

The documentation for this class was generated from the following file:

· ginkgo/core/multigrid/fixed coarsening.hpp

# 46.106 gko::solver::Gcr< ValueType > Class Template Reference

GCR or the generalized conjugate residual method is an iterative type Krylov subspace method similar to GMRES which is suitable for nonsymmetric linear systems.

```
#include <ginkgo/core/solver/gcr.hpp>
```

#### **Public Member Functions**

- std::unique\_ptr< LinOp > transpose () const override
  - Returns a LinOp representing the transpose of the Transposable object.
- std::unique\_ptr< LinOp > conj\_transpose () const override
  - Returns a LinOp representing the conjugate transpose of the Transposable object.
- · bool apply\_uses\_initial\_guess () const override
  - Return true as iterative solvers use the data in x as an initial guess.
- size\_type get\_krylov\_dim () const
  - Gets the Krylov dimension of the solver.
- void set\_krylov\_dim (size\_type other)

Sets the Krylov dimension.

### Static Public Member Functions

• static parameters\_type parse (const config::pnode &config, const config::registry &context, const config::type\_descriptor &td\_for\_child=config::make\_type\_descriptor < ValueType >())

Create the parameters from the property\_tree.

## 46.106.1 Detailed Description

```
template<typename ValueType = default_precision> class gko::solver::Gcr< ValueType >
```

GCR or the generalized conjugate residual method is an iterative type Krylov subspace method similar to GMRES which is suitable for nonsymmetric linear systems.

The implementation in Ginkgo makes use of the merged kernel to make the best use of data locality. The inner operations in one iteration of GCR are merged into one step. Modified Gram-Schmidt is used.

## **Template Parameters**

ValueType	precision of matrix elements
-----------	------------------------------

## 46.106.2 Member Function Documentation

## 46.106.2.1 apply\_uses\_initial\_guess()

```
template<typename ValueType = default_precision>
bool gko::solver::Gcr< ValueType >::apply_uses_initial_guess ( ) const [inline], [override]
```

Return true as iterative solvers use the data in x as an initial guess.

#### Returns

true as iterative solvers use the data in x as an initial guess.

```
68 { return true; }
```

## 46.106.2.2 conj\_transpose()

```
template<typename ValueType = default_precision>
std::unique_ptr<LinOp> gko::solver::Gcr< ValueType >::conj_transpose ( ) const [override],
[virtual]
```

Returns a LinOp representing the conjugate transpose of the Transposable object.

#### Returns

a pointer to the new conjugate transposed object

Implements gko::Transposable.

## 46.106.2.3 get\_krylov\_dim()

```
template<typename ValueType = default_precision>
size_type gko::solver::Gcr< ValueType >::get_krylov_dim ( ) const [inline]
```

Gets the Krylov dimension of the solver.

#### Returns

the Krylov dimension

### 46.106.2.4 parse()

Create the parameters from the property\_tree.

Because this is directly tied to the specific type, the value/index type settings within config are ignored and type\_ descriptor is only used for children configs.

#### **Parameters**

config	the property tree for setting	
context	the registry	
td_for_child	the type descriptor for children configs. The default uses the value type of this class.	

### Returns

parameters

## 46.106.2.5 set\_krylov\_dim()

Sets the Krylov dimension.

## **Parameters**

```
other the new Krylov dimension
```

### 46.106.2.6 transpose()

```
template<typename ValueType = default_precision>
std::unique_ptr<LinOp> gko::solver::Gcr< ValueType >::transpose ( ) const [override], [virtual]
```

Returns a LinOp representing the transpose of the Transposable object.

#### Returns

a pointer to the new transposed object

Implements gko::Transposable.

The documentation for this class was generated from the following file:

· ginkgo/core/solver/gcr.hpp

# 46.107 gko::solver::Gmres < ValueType > Class Template Reference

GMRES or the generalized minimal residual method is an iterative type Krylov subspace method which is suitable for nonsymmetric linear systems.

#include <ginkgo/core/solver/gmres.hpp>

### **Public Member Functions**

- std::unique ptr< LinOp > transpose () const override
  - Returns a LinOp representing the transpose of the Transposable object.
- std::unique\_ptr< LinOp > conj\_transpose () const override

Returns a LinOp representing the conjugate transpose of the Transposable object.

· bool apply\_uses\_initial\_guess () const override

Return true as iterative solvers use the data in x as an initial guess.

• size\_type get\_krylov\_dim () const

Gets the Krylov dimension of the solver.

void set\_krylov\_dim (size\_type other)

Sets the Krylov dimension.

### **Static Public Member Functions**

• static parameters\_type parse (const config::pnode &config, const config::registry &context, const config::type\_descriptor &td\_for\_child=config::make\_type\_descriptor < ValueType >())

Create the parameters from the property\_tree.

## 46.107.1 Detailed Description

```
template < typename ValueType = default_precision > class gko::solver::Gmres < ValueType >
```

GMRES or the generalized minimal residual method is an iterative type Krylov subspace method which is suitable for nonsymmetric linear systems.

The implementation in Ginkgo makes use of the merged kernel to make the best use of data locality. The inner operations in one iteration of GMRES are merged into 2 separate steps. Modified Gram-Schmidt is used.

## **Template Parameters**

ValueType	precision of matrix elements
-----------	------------------------------

### 46.107.2 Member Function Documentation

## 46.107.2.1 apply\_uses\_initial\_guess()

```
template<typename ValueType = default_precision>
bool gko::solver::Gmres< ValueType >::apply_uses_initial_guess ( ) const [inline], [override]
```

Return true as iterative solvers use the data in x as an initial guess.

#### Returns

true as iterative solvers use the data in x as an initial guess.

```
92 { return true; }
```

## 46.107.2.2 conj\_transpose()

```
template<typename ValueType = default_precision>
std::unique_ptr<LinOp> gko::solver::Gmres< ValueType >::conj_transpose ( ) const [override],
[virtual]
```

Returns a LinOp representing the conjugate transpose of the Transposable object.

#### Returns

a pointer to the new conjugate transposed object

Implements gko::Transposable.

## 46.107.2.3 get\_krylov\_dim()

```
template<typename ValueType = default_precision>
size_type gko::solver::Gmres< ValueType >::get_krylov_dim ( ) const [inline]
```

Gets the Krylov dimension of the solver.

#### Returns

the Krylov dimension

### 46.107.2.4 parse()

Create the parameters from the property\_tree.

Because this is directly tied to the specific type, the value/index type settings within config are ignored and type\_ descriptor is only used for children configs.

#### **Parameters**

config	the property tree for setting	
context	the registry	
td_for_child	the type descriptor for children configs. The default uses the value type of this class.	

#### Returns

parameters

## 46.107.2.5 set\_krylov\_dim()

Sets the Krylov dimension.

## **Parameters**

```
other the new Krylov dimension
```

### 46.107.2.6 transpose()

```
template<typename ValueType = default_precision>
std::unique_ptr<LinOp> gko::solver::Gmres< ValueType >::transpose ( ) const [override],
[virtual]
```

Returns a LinOp representing the transpose of the Transposable object.

Returns

a pointer to the new transposed object

Implements gko::Transposable.

The documentation for this class was generated from the following file:

• ginkgo/core/solver/gmres.hpp

# 46.108 gko::solver::has\_with\_criteria< SolverType, typename > Struct Template Reference

Helper structure to test if the Factory of SolverType has a function with\_criteria.

#include <ginkgo/core/solver/solver\_traits.hpp>

## 46.108.1 Detailed Description

template < typename SolverType, typename = void > struct gko::solver::has\_with\_criteria < SolverType, typename >

Helper structure to test if the Factory of SolverType has a function with\_criteria.

Contains a constexpr boolean value, which is true if the Factory class of SolverType has a with\_criteria, and false otherwise.

**Template Parameters** 

SolverType | Solver to test if its factory has a with\_criteria function.

The documentation for this struct was generated from the following file:

• ginkgo/core/solver/solver\_traits.hpp

# 46.109 gko::hip\_stream Class Reference

An RAII wrapper for a custom HIP stream.

#include <ginkgo/core/base/stream.hpp>

## **Public Member Functions**

hip\_stream ()

Creates an empty stream wrapper, representing the default stream.

hip\_stream (int device\_id)

Creates a new custom HIP stream on the given device.

∼hip\_stream ()

Destroys the custom HIP stream, if it isn't empty.

hip\_stream (hip\_stream &&)

Move-constructs from an existing stream, which will be emptied.

• hip\_stream & operator= (hip\_stream &&)=delete

Move-assigns from an existing stream, which will be emptied.

• CUstream\_st \* get () const

Returns the native HIP stream handle.

## 46.109.1 Detailed Description

An RAII wrapper for a custom HIP stream.

The stream will be created on construction and destroyed when the lifetime of the wrapper ends.

## 46.109.2 Constructor & Destructor Documentation

## 46.109.2.1 hip\_stream()

Creates a new custom HIP stream on the given device.

## **Parameters**

device←	the device ID to create the stream on.
id	

## 46.109.3 Member Function Documentation

## 46.109.3.1 get()

```
CUstream_st* gko::hip_stream::get ( ) const
```

Returns the native HIP stream handle.

In an empty hip\_stream, this will return nullptr.

The documentation for this class was generated from the following file:

• ginkgo/core/base/stream.hpp

# 46.110 gko::HipAllocatorBase Class Reference

Implement this interface to provide an allocator for HipExecutor.

```
#include <ginkgo/core/base/memory.hpp>
```

## 46.110.1 Detailed Description

Implement this interface to provide an allocator for HipExecutor.

The documentation for this class was generated from the following file:

• ginkgo/core/base/memory.hpp

# 46.111 gko::HipblasError Class Reference

HipblasError is thrown when a hipBLAS routine throws a non-zero error code.

```
#include <ginkgo/core/base/exception.hpp>
```

### **Public Member Functions**

• HipblasError (const std::string &file, int line, const std::string &func, int64 error\_code)

Initializes a hipBLAS error.

## 46.111.1 Detailed Description

HipblasError is thrown when a hipBLAS routine throws a non-zero error code.

## 46.111.2 Constructor & Destructor Documentation

## 46.111.2.1 HipblasError()

Initializes a hipBLAS error.

#### **Parameters**

file	The name of the offending source file	
line	The source code line number where the error occurred	
func	The name of the hipBLAS routine that failed	
error_code	The resulting hipBLAS error code	

The documentation for this class was generated from the following file:

• ginkgo/core/base/exception.hpp

# 46.112 gko::HipError Class Reference

HipError is thrown when a HIP routine throws a non-zero error code.

```
#include <ginkgo/core/base/exception.hpp>
```

## **Public Member Functions**

HipError (const std::string &file, int line, const std::string &func, int64 error\_code)
 Initializes a HIP error.

## 46.112.1 Detailed Description

HipError is thrown when a HIP routine throws a non-zero error code.

## 46.112.2 Constructor & Destructor Documentation

## 46.112.2.1 HipError()

Initializes a HIP error.

#### **Parameters**

file	The name of the offending source file	
line	The source code line number where the error occurred	
func The name of the HIP routine that failed		
error_code	The resulting HIP error code	

The documentation for this class was generated from the following file:

· ginkgo/core/base/exception.hpp

## 46.113 gko::HipExecutor Class Reference

This is the Executor subclass which represents the HIP enhanced device.

#include <ginkgo/core/base/executor.hpp>

### **Public Member Functions**

• std::shared\_ptr< Executor > get\_master () noexcept override

Returns the master OmpExecutor of this Executor.

std::shared\_ptr< const Executor > get\_master () const noexcept override

Returns the master OmpExecutor of this Executor.

· void synchronize () const override

Synchronize the operations launched on the executor with its master.

- std::string get\_description () const override
- int get\_device\_id () const noexcept

Get the HIP device id of the device associated to this executor.

• int get\_num\_warps\_per\_sm () const noexcept

Get the number of warps per SM of this executor.

int get\_num\_multiprocessor () const noexcept

Get the number of multiprocessor of this executor.

int get\_major\_version () const noexcept

Get the major version of compute capability.

int get\_minor\_version () const noexcept

Get the minor version of compute capability.

int get\_num\_warps () const noexcept

Get the number of warps of this executor.

int get\_warp\_size () const noexcept

Get the warp size of this executor.

hipblasContext \* get\_hipblas\_handle () const

Get the hipblas handle for this executor.

hipblasContext \* get\_blas\_handle () const

Get the hipblas handle for this executor.

• hipsparseContext \* get\_hipsparse\_handle () const

Get the hipsparse handle for this executor.

hipsparseContext \* get\_sparselib\_handle () const

Get the hipsparse handle for this executor.

• int get\_closest\_numa () const

Get the closest NUMA node.

std::vector< int > get\_closest\_pus () const

Get the closest PUs.

• virtual void run (const Operation &op) const=0

Runs the specified Operation using this Executor.

template < typename ClosureOmp, typename ClosureCuda, typename ClosureHip, typename ClosureDpcpp >
 void run (const ClosureOmp & op\_omp, const ClosureCuda & op\_cuda, const ClosureHip & op\_hip, const ClosureDpcpp & op\_dpcpp) const

Runs one of the passed in functors, depending on the Executor type.

• template < typename ClosureReference , typename ClosureOmp , typename ClosureCuda , typename ClosureHip , typename Closure ← Dpcpp >

void run (std::string name, const ClosureReference &op\_ref, const ClosureOmp &op\_omp, const Closure ← Cuda &op\_cuda, const ClosureHip &op\_hip, const ClosureDpcpp &op\_dpcpp) const

Runs one of the passed in functors, depending on the Executor type.

#### **Static Public Member Functions**

• static std::shared\_ptr< HipExecutor > create (int device\_id, std::shared\_ptr< Executor > master, bool device\_reset, allocation\_mode alloc\_mode=default\_hip\_alloc\_mode, CUstream\_st \*stream=nullptr)

Creates a new HipExecutor.

• static int get\_num\_devices ()

Get the number of devices present on the system.

## 46.113.1 Detailed Description

This is the Executor subclass which represents the HIP enhanced device.

## 46.113.2 Member Function Documentation

## 46.113.2.1 create()

```
static std::shared_ptr<HipExecutor> gko::HipExecutor::create (
    int device_id,
    std::shared_ptr< Executor > master,
    bool device_reset,
    allocation_mode alloc_mode = default_hip_alloc_mode,
    CUstream_st * stream = nullptr ) [static]
```

Creates a new HipExecutor.

#### **Parameters**

device_id the HIP device id of this device	
master	an executor on the host that is used to invoke the device kernels
device_reset whether to reset the device after the object exits the scope.	
alloc_mode	the allocation mode that the executor should operate on. See @allocation_mode for more details

## 46.113.2.2 get\_blas\_handle()

```
hipblasContext* gko::HipExecutor::get_blas_handle ( ) const [inline]
```

Get the hipblas handle for this executor.

Returns

the hipblas handle (hipblasContext\*) for this executor

Referenced by get\_hipblas\_handle().

## 46.113.2.3 get\_closest\_numa()

```
int gko::HipExecutor::get_closest_numa ( ) const [inline]
```

Get the closest NUMA node.

Returns

the closest NUMA node closest to this device

## 46.113.2.4 get\_closest\_pus()

```
std::vector<int> gko::HipExecutor::get_closest_pus ( ) const [inline]
```

Get the closest PUs.

Returns

the array of PUs closest to this device

## 46.113.2.5 get\_description()

```
std::string gko::HipExecutor::get_description ( ) const [override], [virtual]
```

Returns

a textual representation of the executor and its device.

Implements gko::Executor.

## 46.113.2.6 get\_hipblas\_handle()

```
hipblasContext* gko::HipExecutor::get_hipblas_handle ( ) const [inline]
```

Get the hipblas handle for this executor.

Returns

the hipblas handle (hipblasContext\*) for this executor

References get\_blas\_handle().

## 46.113.2.7 get\_hipsparse\_handle()

```
hipsparseContext* gko::HipExecutor::get_hipsparse_handle ( ) const [inline]
```

Get the hipsparse handle for this executor.

Returns

the hipsparse handle (hipsparseContext\*) for this executor

References get\_sparselib\_handle().

### 46.113.2.8 get\_master() [1/2]

```
std::shared_ptr<const Executor> gko::HipExecutor::get_master ( ) const [override], [virtual],
[noexcept]
```

Returns the master OmpExecutor of this Executor.

Returns

the master OmpExecutor of this Executor.

Implements gko::Executor.

### 46.113.2.9 get\_master() [2/2]

```
std::shared_ptr<Executor> gko::HipExecutor::get_master ( ) [override], [virtual], [noexcept]
```

Returns the master OmpExecutor of this Executor.

Returns

the master OmpExecutor of this Executor.

Implements gko::Executor.

## 46.113.2.10 get\_sparselib\_handle()

```
hipsparseContext* gko::HipExecutor::get_sparselib_handle ( ) const [inline]
```

Get the hipsparse handle for this executor.

### Returns

the hipsparse handle (hipsparseContext\*) for this executor

Referenced by get\_hipsparse\_handle().

## 46.113.2.11 run() [1/3]

Runs one of the passed in functors, depending on the Executor type.

## **Template Parameters**

ClosureOmp	type of op_omp
ClosureCuda	type of op_cuda
ClosureHip	type of op_hip
ClosureDpcpp	type of op_dpcpp

## **Parameters**

op_omp	functor to run in case of a OmpExecutor or ReferenceExecutor	
op_cuda	functor to run in case of a CudaExecutor	
op_hip functor to run in case of a HipExecutor		
op_dpcpp	functor to run in case of a DpcppExecutor	

## 46.113.2.12 run() [2/3]

```
virtual void gko::Executor::run
```

Runs the specified Operation using this Executor.

#### **Parameters**

```
op the operation to run
```

## 46.113.2.13 run() [3/3]

Runs one of the passed in functors, depending on the Executor type.

## **Template Parameters**

ClosureReference	type of op_ref
ClosureOmp	type of op_omp
ClosureCuda	type of op_cuda
ClosureHip	type of op_hip
ClosureDpcpp	type of op_dpcpp

### **Parameters**

name	the name of the operation
op_ref	functor to run in case of a ReferenceExecutor
op_omp	functor to run in case of a OmpExecutor
op_cuda	functor to run in case of a CudaExecutor
op_hip	functor to run in case of a HipExecutor
op_dpcpp	functor to run in case of a DpcppExecutor

The documentation for this class was generated from the following file:

• ginkgo/core/base/executor.hpp

# 46.114 gko::HipfftError Class Reference

HipfftError is thrown when a hipFFT routine throws a non-zero error code.

#include <ginkgo/core/base/exception.hpp>

## **Public Member Functions**

HipfftError (const std::string &file, int line, const std::string &func, int64 error\_code)
 Initializes a hipFFT error.

## 46.114.1 Detailed Description

HipfftError is thrown when a hipFFT routine throws a non-zero error code.

## 46.114.2 Constructor & Destructor Documentation

## 46.114.2.1 HipfftError()

Initializes a hipFFT error.

## **Parameters**

file	The name of the offending source file
line	The source code line number where the error occurred
func	The name of the hipFFT routine that failed
error_code	The resulting hipFFT error code

The documentation for this class was generated from the following file:

· ginkgo/core/base/exception.hpp

# 46.115 gko::HiprandError Class Reference

HiprandError is thrown when a hipRAND routine throws a non-zero error code.

```
#include <ginkgo/core/base/exception.hpp>
```

## **Public Member Functions**

HiprandError (const std::string &file, int line, const std::string &func, int64 error\_code)
 Initializes a hipRAND error.

## 46.115.1 Detailed Description

HiprandError is thrown when a hipRAND routine throws a non-zero error code.

## 46.115.2 Constructor & Destructor Documentation

## 46.115.2.1 HiprandError()

Initializes a hipRAND error.

#### **Parameters**

file	The name of the offending source file
line	The source code line number where the error occurred
func	The name of the hipRAND routine that failed
error_code	The resulting hipRAND error code

The documentation for this class was generated from the following file:

• ginkgo/core/base/exception.hpp

# 46.116 gko::HipsparseError Class Reference

HipsparseError is thrown when a hipSPARSE routine throws a non-zero error code.

```
#include <ginkgo/core/base/exception.hpp>
```

## **Public Member Functions**

HipsparseError (const std::string &file, int line, const std::string &func, int64 error\_code)
 Initializes a hipSPARSE error.

## 46.116.1 Detailed Description

HipsparseError is thrown when a hipSPARSE routine throws a non-zero error code.

## 46.116.2 Constructor & Destructor Documentation

## 46.116.2.1 HipsparseError()

Initializes a hipSPARSE error.

#### **Parameters**

file	The name of the offending source file
line	The source code line number where the error occurred
func	The name of the hipSPARSE routine that failed
error_code	The resulting hipSPARSE error code

The documentation for this class was generated from the following file:

· ginkgo/core/base/exception.hpp

# 46.117 gko::HipTimer Class Reference

A timer using events for timing on a HipExecutor.

```
#include <ginkgo/core/base/timer.hpp>
```

## **Public Member Functions**

- · void record (time point &time) override
  - Records a time point at the current time.
- void wait (time\_point &time) override
  - Waits until all kernels in-process when recording the time point are finished.
- std::chrono::nanoseconds difference\_async (const time\_point &start, const time\_point &stop) override Computes the difference between the two time points in nanoseconds.

## **Additional Inherited Members**

## 46.117.1 Detailed Description

A timer using events for timing on a HipExecutor.

Note

When using a HipExecutor with a custom stream, make sure that the stream's lifetime is longer than the lifetime of this timer.

#### 46.117.2 Member Function Documentation

## 46.117.2.1 difference async()

Computes the difference between the two time points in nanoseconds.

This asynchronous version does not synchronize itself, so the time points need to have been synchronized with, i.e. timer->wait(stop) needs to have been called. The version is intended for more advanced users who want to measure the overhead of timing functionality separately.

#### **Parameters**

start	the first time point (earlier)
end	the second time point (later)

#### Returns

the difference between the time points in nanoseconds.

Implements gko::Timer.

The documentation for this class was generated from the following file:

• ginkgo/core/base/timer.hpp

# 46.118 gko::matrix::Hybrid< ValueType, IndexType > Class Template Reference

HYBRID is a matrix format which splits the matrix into ELLPACK and COO format.

```
#include <ginkgo/core/matrix/hybrid.hpp>
```

## **Classes**

· class automatic

automatic is a strategy\_type which decides the number of stored elements per row of the ell part automatically.

· class column\_limit

column\_limit is a strategy\_type which decides the number of stored elements per row of the ell part by specifying the number of columns.

· class imbalance bounded limit

imbalance\_bounded\_limit is a strategy\_type which decides the number of stored elements per row of the ell part.

class imbalance limit

imbalance\_limit is a strategy\_type which decides the number of stored elements per row of the ell part according to the percent.

· class minimal\_storage\_limit

minimal\_storage\_limit is a strategy\_type which decides the number of stored elements per row of the ell part.

· class strategy\_type

strategy\_type is to decide how to set the hybrid config.

### **Public Member Functions**

void read (const mat\_data &data) override

Reads a matrix from a matrix\_data structure.

· void read (const device mat data &data) override

Reads a matrix from a device\_matrix\_data structure.

• void read (device\_mat\_data &&data) override

Reads a matrix from a device\_matrix\_data structure.

· void write (mat data &data) const override

Writes a matrix to a matrix\_data structure.

std::unique\_ptr< Diagonal</li>
 ValueType > > extract\_diagonal () const override

Extracts the diagonal entries of the matrix into a vector.

std::unique\_ptr< absolute\_type > compute\_absolute () const override

Gets the AbsoluteLinOp.

void compute\_absolute\_inplace () override

Compute absolute inplace on each element.

value\_type \* get\_ell\_values () noexcept

Returns the values of the ell part.

const value\_type \* get\_const\_ell\_values () const noexcept

Returns the values of the ell part.

• index\_type \* get\_ell\_col\_idxs () noexcept

Returns the column indexes of the ell part.

const index\_type \* get\_const\_ell\_col\_idxs () const noexcept

Returns the column indexes of the ell part.

• size\_type get\_ell\_num\_stored\_elements\_per\_row () const noexcept

Returns the number of stored elements per row of ell part.

• size\_type get\_ell\_stride () const noexcept

Returns the stride of the ell part.

size\_type get\_ell\_num\_stored\_elements () const noexcept

Returns the number of elements explicitly stored in the ell part.

• value type & ell val at (size type row, size type idx) noexcept

Returns the idx-th non-zero element of the row-th row in the ell part.

value\_type ell\_val\_at (size\_type row, size\_type idx) const noexcept

Returns the idx-th non-zero element of the row-th row in the ell part.

index\_type & ell\_col\_at (size\_type row, size\_type idx) noexcept

Returns the idx-th column index of the row-th row in the ell part.

• index\_type ell\_col\_at (size\_type row, size\_type idx) const noexcept

Returns the idx-th column index of the row-th row in the ell part.

const ell\_type \* get\_ell () const noexcept

Returns the matrix of the ell part.

• value\_type \* get\_coo\_values () noexcept

Returns the values of the coo part.

const value\_type \* get\_const\_coo\_values () const noexcept

Returns the values of the coo part.

• index type \* get coo col idxs () noexcept

Returns the column indexes of the coo part.

• const index\_type \* get\_const\_coo\_col\_idxs () const noexcept

Returns the column indexes of the coo part.

• index type \* get coo row idxs () noexcept

Returns the row indexes of the coo part.

• const index\_type \* get\_const\_coo\_row\_idxs () const noexcept

Returns the row indexes of the coo part.

• size\_type get\_coo\_num\_stored\_elements () const noexcept

Returns the number of elements explicitly stored in the coo part.

const coo\_type \* get\_coo () const noexcept

Returns the matrix of the coo part.

size\_type get\_num\_stored\_elements () const noexcept

Returns the number of elements explicitly stored in the matrix.

std::shared\_ptr< strategy\_type > get\_strategy () const noexcept

Returns the strategy.

• template<typename HybType >

 ${\tt std::shared\_ptr} < {\tt typename\ HybType::strategy\_type} > {\tt get\_strategy\ ()\ const}$ 

Returns the current strategy allowed in given hybrid format.

Hybrid & operator= (const Hybrid &)

Copy-assigns a Hybrid matrix.

Hybrid & operator= (Hybrid &&)

Move-assigns a Hybrid matrix.

• Hybrid (const Hybrid &)

Copy-assigns a Hybrid matrix.

• Hybrid (Hybrid &&)

Move-assigns a Hybrid matrix.

#### Static Public Member Functions

static std::unique\_ptr< Hybrid > create (std::shared\_ptr< const Executor > exec, std::shared\_ptr<</li>
 strategy\_type > strategy=std::make\_shared< automatic >())

Creates an uninitialized Hybrid matrix of specified method.

• static std::unique\_ptr< Hybrid > create (std::shared\_ptr< const Executor > exec, const dim< 2 > &size, std::shared\_ptr< strategy\_type > strategy=std::make\_shared< automatic >())

Creates an uninitialized Hybrid matrix of the specified size and method.

static std::unique\_ptr< Hybrid > create (std::shared\_ptr< const Executor > exec, const dim< 2 > &size, size\_type num\_stored\_elements\_per\_row, std::shared\_ptr< strategy\_type > strategy=std::make\_shared< automatic >())

Creates an uninitialized Hybrid matrix of the specified size and method.

static std::unique\_ptr< Hybrid > create (std::shared\_ptr< const Executor > exec, const dim< 2 > &size, size\_type num\_stored\_elements\_per\_row, size\_type stride, std::shared\_ptr< strategy\_type > strategy)

Creates an uninitialized Hybrid matrix of the specified size and method.

static std::unique\_ptr< Hybrid > create (std::shared\_ptr< const Executor > exec, const dim< 2 > &size, size\_type num\_stored\_elements\_per\_row, size\_type stride, size\_type num\_nonzeros={}, std::shared\_ptr< strategy\_type > strategy=std::make\_shared< automatic >())

Creates an uninitialized Hybrid matrix of the specified size and method.

### 46.118.1 Detailed Description

template < typename ValueType = default\_precision, typename IndexType = int32 > class gko::matrix::Hybrid < ValueType, IndexType >

HYBRID is a matrix format which splits the matrix into ELLPACK and COO format.

Achieve the excellent performance with a proper partition of ELLPACK and COO.

### **Template Parameters**

ValueType	precision of matrix elements
IndexType	precision of matrix indexes

## 46.118.2 Constructor & Destructor Documentation

## 46.118.2.1 Hybrid() [1/2]

Copy-assigns a Hybrid matrix.

Inherits the executor, copies the Ell and Coo matrices.

### 46.118.2.2 Hybrid() [2/2]

Move-assigns a Hybrid matrix.

Inherits the executor, moves the Ell and Coo matrices. The moved-from matrix is empty (0x0 with empty Ell/Coo matrices).

## 46.118.3 Member Function Documentation

#### 46.118.3.1 compute\_absolute()

```
template<typename ValueType = default_precision, typename IndexType = int32>
std::unique_ptr<absolute_type> gko::matrix::Hybrid< ValueType, IndexType >::compute_absolute
( ) const [override], [virtual]
```

Gets the AbsoluteLinOp.

## Returns

a pointer to the new absolute object

 $Implements\ gko:: Enable Absolute Computation < remove\_complex < \ Hybrid < Value Type,\ Index Type >>>.$ 

### 46.118.3.2 create() [1/5]

Creates an uninitialized Hybrid matrix of the specified size and method.

#### **Parameters**

exec	Executor associated to the matrix
size	size of the matrix
num_stored_elements_per_row	the number of stored elements per row
stride	stride of the rows
num_nonzeros	number of nonzeros
strategy	strategy of deciding the Hybrid config

#### Returns

A smart pointer to the newly created matrix.

## 46.118.3.3 create() [2/5]

```
template<typename ValueType = default_precision, typename IndexType = int32>
static std::unique_ptr<Hybrid> gko::matrix::Hybrid< ValueType, IndexType >::create (
    std::shared_ptr< const Executor > exec,
    const dim< 2 > & size,
    size_type num_stored_elements_per_row,
    size_type stride,
    std::shared_ptr< strategy_type > strategy ) [static]
```

Creates an uninitialized Hybrid matrix of the specified size and method.

## **Parameters**

exec	Executor associated to the matrix
size	size of the matrix
num_stored_elements_per_row	the number of stored elements per row
stride	stride of the rows
strategy	strategy of deciding the Hybrid config

#### Returns

A smart pointer to the newly created matrix.

## 46.118.3.4 create() [3/5]

Creates an uninitialized Hybrid matrix of the specified size and method.

(ell\_stride is set to the number of rows of the matrix.)

#### **Parameters**

exec	Executor associated to the matrix
size	size of the matrix
num_stored_elements_per_row	the number of stroed elements per row
strategy	strategy of deciding the Hybrid config

#### Returns

A smart pointer to the newly created matrix.

## 46.118.3.5 create() [4/5]

Creates an uninitialized Hybrid matrix of the specified size and method.

(ell\_num\_stored\_elements\_per\_row is set to the number of cols of the matrix. ell\_stride is set to the number of rows of the matrix.)

#### **Parameters**

exec	Executor associated to the matrix
size	size of the matrix
strategy	strategy of deciding the Hybrid config

#### Returns

A smart pointer to the newly created matrix.

## 46.118.3.6 create() [5/5]

Creates an uninitialized Hybrid matrix of specified method.

(ell\_num\_stored\_elements\_per\_row is set to the number of cols of the matrix. ell\_stride is set to the number of rows of the matrix.)

#### **Parameters**

exec	Executor associated to the matrix
strategy	strategy of deciding the Hybrid config

## Returns

A smart pointer to the newly created matrix.

## 46.118.3.7 ell\_col\_at() [1/2]

Returns the idx-th column index of the row-th row in the ell part.

#### **Parameters**

row	the row of the requested element
idx	the idx-th stored element of the row

## Note

the method has to be called on the same Executor the matrix is stored at (e.g. trying to call this method on a GPU matrix from the OMP results in a runtime error)

```
495 {
496          return ell_->col_at(row, idx);
497    }
```

### 46.118.3.8 ell\_col\_at() [2/2]

Returns the idx-th column index of the row-th row in the ell part.

#### **Parameters**

row	the row of the requested element
idx	the idx-th stored element of the row

### Note

the method has to be called on the same Executor the matrix is stored at (e.g. trying to call this method on a GPU matrix from the OMP results in a runtime error)

## 46.118.3.9 ell\_val\_at() [1/2]

Returns the idx-th non-zero element of the row-th row in the ell part.

#### **Parameters**

row	the row of the requested element
idx	the idx-th stored element of the row

## Note

the method has to be called on the same Executor the matrix is stored at (e.g. trying to call this method on a GPU matrix from the OMP results in a runtime error)

### 46.118.3.10 ell\_val\_at() [2/2]

Returns the idx-th non-zero element of the row-th row in the ell part.

#### **Parameters**

row	the row of the requested element
idx	the idx-th stored element of the row

#### Note

the method has to be called on the same Executor the matrix is stored at (e.g. trying to call this method on a GPU matrix from the OMP results in a runtime error)

### 46.118.3.11 extract\_diagonal()

```
template<typename ValueType = default_precision, typename IndexType = int32>
std::unique_ptr<Diagonal<ValueType> > gko::matrix::Hybrid< ValueType, IndexType >::extract
_diagonal ( ) const [override], [virtual]
```

Extracts the diagonal entries of the matrix into a vector.

#### **Parameters**

onal will be written	the vector into which the	diag	
----------------------	---------------------------	------	--

Implements gko::DiagonalExtractable < ValueType >.

## 46.118.3.12 get\_const\_coo\_col\_idxs()

```
template<typename ValueType = default_precision, typename IndexType = int32>
const index_type* gko::matrix::Hybrid< ValueType, IndexType >::get_const_coo_col_idxs ( )
const [inline], [noexcept]
```

Returns the column indexes of the coo part.

## Returns

the column indexes of the coo part.

### Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

#### 46.118.3.13 get\_const\_coo\_row\_idxs()

```
template<typename ValueType = default_precision, typename IndexType = int32>
const index_type* gko::matrix::Hybrid< ValueType, IndexType >::get_const_coo_row_idxs ( )
const [inline], [noexcept]
```

Returns the row indexes of the coo part.

#### Returns

the row indexes of the coo part.

#### Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

#### 46.118.3.14 get const coo values()

```
template<typename ValueType = default_precision, typename IndexType = int32>
const value_type* gko::matrix::Hybrid< ValueType, IndexType >::get_const_coo_values ( ) const
[inline], [noexcept]
```

Returns the values of the coo part.

#### Returns

the values of the coo part.

#### Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

## 46.118.3.15 get\_const\_ell\_col\_idxs()

```
template<typename ValueType = default_precision, typename IndexType = int32>
const index_type* gko::matrix::Hybrid< ValueType, IndexType >::get_const_ell_col_idxs ( )
const [inline], [noexcept]
```

Returns the column indexes of the ell part.

#### Returns

the column indexes of the ell part

## Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

### 46.118.3.16 get\_const\_ell\_values()

```
template<typename ValueType = default_precision, typename IndexType = int32>
const value_type* gko::matrix::Hybrid< ValueType, IndexType >::get_const_ell_values ( ) const
[inline], [noexcept]
```

Returns the values of the ell part.

#### Returns

the values of the ell part

#### Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

## 46.118.3.17 get\_coo()

```
template<typename ValueType = default_precision, typename IndexType = int32>
const coo_type* gko::matrix::Hybrid< ValueType, IndexType >::get_coo ( ) const [inline],
[noexcept]
```

Returns the matrix of the coo part.

## Returns

the matrix of the coo part

## 46.118.3.18 get\_coo\_col\_idxs()

```
template<typename ValueType = default_precision, typename IndexType = int32>
index_type* gko::matrix::Hybrid< ValueType, IndexType >::get_coo_col_idxs () [inline], [noexcept]
```

Returns the column indexes of the coo part.

#### Returns

the column indexes of the coo part.

## 46.118.3.19 get\_coo\_num\_stored\_elements()

```
template<typename ValueType = default_precision, typename IndexType = int32>
size_type gko::matrix::Hybrid< ValueType, IndexType >::get_coo_num_stored_elements ( ) const
[inline], [noexcept]
```

Returns the number of elements explicitly stored in the coo part.

#### Returns

the number of elements explicitly stored in the coo part

## 46.118.3.20 get\_coo\_row\_idxs()

```
template<typename ValueType = default_precision, typename IndexType = int32>
index_type* gko::matrix::Hybrid< ValueType, IndexType >::get_coo_row_idxs () [inline], [noexcept]
```

Returns the row indexes of the coo part.

#### Returns

the row indexes of the coo part.

## 46.118.3.21 get\_coo\_values()

```
template<typename ValueType = default_precision, typename IndexType = int32>
value_type* gko::matrix::Hybrid< ValueType, IndexType >::get_coo_values ( ) [inline], [noexcept]
```

Returns the values of the coo part.

## Returns

the values of the coo part.

## 46.118.3.22 get\_ell()

```
template<typename ValueType = default_precision, typename IndexType = int32>
const ell_type* gko::matrix::Hybrid< ValueType, IndexType >::get_ell ( ) const [inline],
[noexcept]
```

Returns the matrix of the ell part.

#### Returns

the matrix of the ell part

## 46.118.3.23 get\_ell\_col\_idxs()

```
template<typename ValueType = default_precision, typename IndexType = int32>
index_type* gko::matrix::Hybrid< ValueType, IndexType >::get_ell_col_idxs () [inline], [noexcept]
```

Returns the column indexes of the ell part.

#### Returns

the column indexes of the ell part

## 46.118.3.24 get\_ell\_num\_stored\_elements()

```
template<typename ValueType = default_precision, typename IndexType = int32>
size_type gko::matrix::Hybrid< ValueType, IndexType >::get_ell_num_stored_elements ( ) const
[inline], [noexcept]
```

Returns the number of elements explicitly stored in the ell part.

#### Returns

the number of elements explicitly stored in the ell part

## 46.118.3.25 get\_ell\_num\_stored\_elements\_per\_row()

```
template<typename ValueType = default_precision, typename IndexType = int32>
size_type gko::matrix::Hybrid< ValueType, IndexType >::get_ell_num_stored_elements_per_row ( )
const [inline], [noexcept]
```

Returns the number of stored elements per row of ell part.

## Returns

the number of stored elements per row of ell part

## 46.118.3.26 get ell stride()

```
template<typename ValueType = default_precision, typename IndexType = int32>
size_type gko::matrix::Hybrid< ValueType, IndexType >::get_ell_stride ( ) const [inline],
[noexcept]
```

Returns the stride of the ell part.

#### Returns

the stride of the ell part

## 46.118.3.27 get\_ell\_values()

```
template<typename ValueType = default_precision, typename IndexType = int32>
value_type* gko::matrix::Hybrid< ValueType, IndexType >::get_ell_values () [inline], [noexcept]
```

Returns the values of the ell part.

#### Returns

the values of the ell part

## 46.118.3.28 get\_num\_stored\_elements()

```
template<typename ValueType = default_precision, typename IndexType = int32>
size_type gko::matrix::Hybrid< ValueType, IndexType >::get_num_stored_elements ( ) const
[inline], [noexcept]
```

Returns the number of elements explicitly stored in the matrix.

#### Returns

the number of elements explicitly stored in the matrix

## 46.118.3.29 get\_strategy() [1/2]

```
template<typename ValueType = default_precision, typename IndexType = int32>
template<typename HybType >
std::shared_ptr<typename HybType::strategy_type> gko::matrix::Hybrid< ValueType, IndexType
>::get_strategy ( ) const
```

Returns the current strategy allowed in given hybrid format.

## **Template Parameters**

```
HybType hybrid type
```

#### Returns

the strategy

## 46.118.3.30 get\_strategy() [2/2]

```
template<typename ValueType = default_precision, typename IndexType = int32>
std::shared_ptr< typename HybType::strategy_type > gko::matrix::Hybrid< ValueType, IndexType
>::get_strategy ( ) const [inline], [noexcept]
```

Returns the strategy.

Returns

the strategy

## 46.118.3.31 operator=() [1/2]

Copy-assigns a Hybrid matrix.

Preserves the executor, copy-assigns the Ell and Coo matrices.

## 46.118.3.32 operator=() [2/2]

Move-assigns a Hybrid matrix.

Preserves the executor, move-assigns the Ell and Coo matrices. The moved-from matrix is empty (0x0 with empty Ell/Coo matrices).

## 46.118.3.33 read() [1/3]

Reads a matrix from a device matrix data structure.

#### **Parameters**

```
data the device_matrix_data structure.
```

Reimplemented from gko::ReadableFromMatrixData< ValueType, IndexType >.

## 46.118.3.34 read() [2/3]

Reads a matrix from a matrix\_data structure.

## **Parameters**

```
data the matrix_data structure
```

Implements gko::ReadableFromMatrixData< ValueType, IndexType >.

#### 46.118.3.35 read() [3/3]

Reads a matrix from a device\_matrix\_data structure.

The structure may be emptied by this function.

## **Parameters**

```
data the device_matrix_data structure.
```

Reimplemented from gko::ReadableFromMatrixData< ValueType, IndexType >.

## 46.118.3.36 write()

Writes a matrix to a matrix\_data structure.

## **Parameters**

```
data the matrix_data structure
```

Implements gko::WritableToMatrixData< ValueType, IndexType >.

The documentation for this class was generated from the following files:

- ginkgo/core/matrix/coo.hpp
- ginkgo/core/matrix/hybrid.hpp

# 46.119 gko::preconditioner::lc< LSolverType, IndexType > Class Template Reference

The Incomplete Cholesky (IC) preconditioner solves the equation  $LL^H*x=b$  for a given lower triangular matrix L and the right hand side b (can contain multiple right hand sides).

#include <ginkgo/core/preconditioner/ic.hpp>

#### **Public Member Functions**

std::shared\_ptr< const I\_solver\_type > get\_I\_solver () const

Returns the solver which is used for the provided L matrix.

std::shared\_ptr< const lh\_solver\_type > get\_lh\_solver () const

Returns the solver which is used for the  $L^{\wedge}H$  matrix.

• std::unique\_ptr< LinOp > transpose () const override

Returns a LinOp representing the transpose of the Transposable object.

• std::unique ptr< LinOp > conj transpose () const override

Returns a LinOp representing the conjugate transpose of the Transposable object.

• Ic & operator= (const Ic &other)

Copy-assigns an IC preconditioner.

Ic & operator= (Ic &&other)

Move-assigns an IC preconditioner.

Ic (const Ic &other)

Copy-constructs an IC preconditioner.

• Ic (Ic &&other)

Move-constructs an IC preconditioner.

## **Static Public Member Functions**

• static parameters\_type parse (const config::pnode &config, const config::registry &context, const config::type\_descriptor &td\_for\_child=config::make\_type\_descriptor < value\_type, index\_type >())

Create the parameters from the property\_tree.

## 46.119.1 Detailed Description

 $template < typename\ LSolverType = solver::LowerTrs <> \ , typename\ IndexType = int32 > class\ gko::preconditioner::lc < LSolverType, IndexType >$ 

The Incomplete Cholesky (IC) preconditioner solves the equation  $LL^H*x=b$  for a given lower triangular matrix L and the right hand side b (can contain multiple right hand sides).

It allows to set both the solver for L defaulting to solver::LowerTrs, which is a direct triangular solvers. The solver for  $L^{h}$  is the conjugate-transposed solver for L, ensuring that the preconditioner is symmetric and positive-definite. For this L solver, a factory can be provided (using with\_l\_solver) to have more control over their behavior. In particular, it is possible to use an iterative method for solving the triangular systems. The default parameters for an iterative triangluar solver are:

• reduction factor = 1e-4

• max iteration = <number of="" rows="" of="" the="" matrix="" given="" to="" the="" solver>=""> Solvers without such criteria can also be used, in which case none are set.

An object of this class can be created with a matrix or a gko::Composition containing two matrices. If created with a matrix, it is factorized before creating the solver. If a gko::Composition (containing two matrices) is used, the first operand will be taken as the L matrix, the second will be considered the L^H matrix, which helps to avoid the otherwise necessary transposition of L inside the solver. Parlc can be directly used, since it orders the factors in the correct way.

## Note

When providing a gko::Composition, the first matrix must be the lower matrix (L), and the second matrix must be its conjugate-transpose ( $L^H$ ). If they are swapped, solving might crash or return the wrong result.

Do not use symmetric solvers (like CG) for the L solver since both matrices (L and  $L^{\wedge}H$ ) are, by design, not symmetric.

This class is not thread safe (even a const object is not) because it uses an internal cache to accelerate multiple (sequential) applies. Using it in parallel can lead to segmentation faults, wrong results and other unwanted behavior.

#### **Template Parameters**

LSolverType	type of the solver used for the L matrix. Defaults to solver::LowerTrs
IndexType	type of the indices when Parlc is used to generate the L and $L^{\wedge}H$ factors. Irrelevant otherwise.

## 46.119.2 Constructor & Destructor Documentation

## 46.119.2.1 lc() [1/2]

Copy-constructs an IC preconditioner.

Inherits the executor, shallow-copies the solvers and parameters.

```
318 : Ic{other.get_executor()} { *this = other; }
```

 $References\ gko::PolymorphicObject::get\_executor().$ 

## 46.119.2.2 lc() [2/2]

Move-constructs an IC preconditioner.

Inherits the executor, moves the solvers and parameters. The moved-from object is empty (0x0 with nullptr solvers and default parameters)

References gko::PolymorphicObject::get\_executor().

## 46.119.3 Member Function Documentation

## 46.119.3.1 conj\_transpose()

```
template<typename LSolverType = solver::LowerTrs<>, typename IndexType = int32>
std::unique_ptr<LinOp> gko::preconditioner::Ic< LSolverType, IndexType >::conj_transpose ()
const [inline], [override], [virtual]
```

Returns a LinOp representing the conjugate transpose of the Transposable object.

#### Returns

a pointer to the new conjugate transposed object

Implements gko::Transposable.

References gko::PolymorphicObject::get\_executor(), gko::preconditioner::lc< LSolverType, IndexType >::get\_l \cdot \solver(), gko::preconditioner::lc< LSolverType, IndexType >::get\_lh\_solver(), gko::share(), and gko::transpose().

## 46.119.3.2 get\_l\_solver()

```
template<typename LSolverType = solver::LowerTrs<>, typename IndexType = int32> std::shared_ptr<const l_solver_type> gko::preconditioner::Ic< LSolverType, IndexType >::get← _l_solver ( ) const [inline]
```

Returns the solver which is used for the provided L matrix.

## Returns

the solver which is used for the provided L matrix

Referenced by gko::preconditioner::lc< LSolverType, IndexType >::conj\_transpose(), and gko::preconditioner::lc< LSolverType, IndexType >::transpose().

## 46.119.3.3 get\_lh\_solver()

```
template<typename LSolverType = solver::LowerTrs<>, typename IndexType = int32>
std::shared_ptr<const lh_solver_type> gko::preconditioner::Ic< LSolverType, IndexType >
::get_lh_solver ( ) const [inline]
```

Returns the solver which is used for the L^H matrix.

#### Returns

the solver which is used for the L^H matrix

Referenced by gko::preconditioner::lc< LSolverType, IndexType >::conj\_transpose(), and gko::preconditioner::lc< LSolverType, IndexType >::transpose().

#### 46.119.3.4 operator=() [1/2]

Copy-assigns an IC preconditioner.

Preserves the executor, shallow-copies the solvers and parameters. Creates a clone of the solvers if they are on the wrong executor.

References gko::clone(), and gko::PolymorphicObject::get\_executor().

## 46.119.3.5 operator=() [2/2]

Move-assigns an IC preconditioner.

Preserves the executor, moves the solvers and parameters. Creates a clone of the solvers if they are on the wrong executor. The moved-from object is empty (0x0 with nullptr solvers and default parameters)

References gko::clone(), and gko::PolymorphicObject::get\_executor().

## 46.119.3.6 parse()

Create the parameters from the property\_tree.

Because this is directly tied to the specific type, the value/index type settings within config are ignored and type\_ descriptor is only used for children configs.

#### **Parameters**

config	the property tree for setting	
context	the registry	
td for child	the type descriptor for children configs. The default uses the value/index type of this class.	

#### Returns

parameters

Note

only support the following for I solver: Ir, Gmres, LowerTrs, and LowerIsai

#### 46.119.3.7 transpose()

```
template<typename LSolverType = solver::LowerTrs<>, typename IndexType = int32>
std::unique_ptr<LinOp> gko::preconditioner::Ic< LSolverType, IndexType >::transpose ( ) const
[inline], [override], [virtual]
```

Returns a LinOp representing the transpose of the Transposable object.

Returns

a pointer to the new transposed object

Implements gko::Transposable.

References gko::PolymorphicObject::get\_executor(), gko::preconditioner::Ic< LSolverType, IndexType >::get\_l $_{\leftarrow}$  solver(), gko::preconditioner::Ic< LSolverType, IndexType >::get\_lh $_{\rightarrow}$ solver(), gko::share(), and gko::transpose().

The documentation for this class was generated from the following file:

• ginkgo/core/preconditioner/ic.hpp

## 46.120 gko::factorization::lc< ValueType, IndexType > Class Template Reference

Represents an incomplete Cholesky factorization (IC(0)) of a sparse matrix.

```
#include <ginkgo/core/factorization/ic.hpp>
```

## **Static Public Member Functions**

• static parameters\_type parse (const config::pnode &config, const config::registry &context, const config::type\_descriptor &td\_for\_child=config::make\_type\_descriptor < ValueType, IndexType >())

Create the parameters from the property\_tree.

## **Additional Inherited Members**

## 46.120.1 Detailed Description

template < typename ValueType = gko::default\_precision, typename IndexType = gko::int32 > class gko::factorization::lc < ValueType, IndexType >

Represents an incomplete Cholesky factorization (IC(0)) of a sparse matrix.

More specifically, it consists of a lower triangular factor L and its conjugate transpose  $L^H$  with sparsity pattern  $\mathcal{S}(L+L^H) = \mathcal{S}(A)$  fulfilling  $LL^H = A$  at every non-zero location of A.

## **Template Parameters**

ValueType	Type of the values of all matrices used in this class
IndexType	Type of the indices of all matrices used in this class

## 46.120.2 Member Function Documentation

## 46.120.2.1 parse()

Create the parameters from the property\_tree.

Because this is directly tied to the specific type, the value/index type settings within config are ignored and type\_ descriptor is only used for children configs.

## **Parameters**

config	the property tree for setting
context	the registry
td_for_child	the type descriptor for children configs. The default uses the value/index type of this class.

#### Returns

parameters

The documentation for this class was generated from the following file:

· ginkgo/core/factorization/ic.hpp

## 46.121 gko::matrix::Identity < ValueType > Class Template Reference

This class is a utility which efficiently implements the identity matrix (a linear operator which maps each vector to itself).

#include <ginkgo/core/matrix/identity.hpp>

## **Public Member Functions**

- std::unique\_ptr< LinOp > transpose () const override
   Returns a LinOp representing the transpose of the Transposable object.
- std::unique\_ptr< LinOp > conj\_transpose () const override

Returns a LinOp representing the conjugate transpose of the Transposable object.

## **Static Public Member Functions**

- static std::unique\_ptr< Identity > create (std::shared\_ptr< const Executor > exec, dim< 2 > size)
   Creates an Identity matrix of the specified size.
- static std::unique\_ptr< Identity > create (std::shared\_ptr< const Executor > exec, size\_type size=0)

  Creates an Identity matrix of the specified size.

## 46.121.1 Detailed Description

```
template<typename ValueType = default_precision> class gko::matrix::ldentity< ValueType >
```

This class is a utility which efficiently implements the identity matrix (a linear operator which maps each vector to itself).

Thus, objects of the Identity class always represent a square matrix, and don't require any storage for their values. The apply method is implemented as a simple copy (or a linear combination).

Note

This class is useful when composing it with other operators. For example, it can be used instead of a preconditioner in Krylov solvers, if one wants to run a "plain" solver, without using a preconditioner.

#### **Template Parameters**

ValueType	precision of matrix elements
-----------	------------------------------

## 46.121.2 Member Function Documentation

## 46.121.2.1 conj\_transpose()

```
template<typename ValueType = default_precision>
std::unique_ptr<LinOp> gko::matrix::Identity< ValueType >::conj_transpose ( ) const [override],
[virtual]
```

Returns a LinOp representing the conjugate transpose of the Transposable object.

#### Returns

a pointer to the new conjugate transposed object

Implements gko::Transposable.

## 46.121.2.2 create() [1/2]

Creates an Identity matrix of the specified size.

#### **Parameters**

```
size | size of the matrix (must be square)
```

## 46.121.2.3 create() [2/2]

Creates an Identity matrix of the specified size.

## **Parameters**

```
size size of the matrix
```

## 46.121.2.4 transpose()

```
template<typename ValueType = default_precision>
std::unique_ptr<LinOp> gko::matrix::Identity< ValueType >::transpose ( ) const [override],
[virtual]
```

Returns a LinOp representing the transpose of the Transposable object.

#### Returns

a pointer to the new transposed object

Implements gko::Transposable.

The documentation for this class was generated from the following file:

ginkgo/core/matrix/identity.hpp

## 46.122 gko::batch::matrix::ldentity< ValueType > Class Template Reference

The batch Identity matrix, which represents a batch of Identity matrices.

#include <ginkgo/core/matrix/batch\_identity.hpp>

## **Public Member Functions**

Identity \* apply (ptr\_param< const MultiVector< value\_type >> b, ptr\_param< MultiVector< value\_type >> x)

Apply the matrix to a multi-vector.

• Identity \* apply (ptr\_param< const MultiVector< value\_type >> alpha, ptr\_param< const MultiVector< value\_type >> b, ptr\_param< const MultiVector< value\_type >> beta, ptr\_param< MultiVector< value\_type >> x)

Apply the matrix to a multi-vector with a linear combination of the given input vector.

- const Identity \* apply (ptr\_param< const MultiVector< value\_type >> b, ptr\_param< MultiVector< value ←
   \_type >> x) const
- const Identity \* apply (ptr\_param< const MultiVector< value\_type >> alpha, ptr\_param< const MultiVector< value\_type >> b, ptr\_param< const MultiVector< value\_type >> beta, ptr\_param< MultiVector< value\_type >> x) const

## **Static Public Member Functions**

static std::unique\_ptr< Identity > create (std::shared\_ptr< const Executor > exec, const batch\_dim< 2 > &size=batch\_dim< 2 >{})

Creates an Identity matrix of the specified size.

## 46.122.1 Detailed Description

template<typename ValueType = default\_precision> class gko::batch::matrix::ldentity< ValueType >

The batch Identity matrix, which represents a batch of Identity matrices.

**Template Parameters** 

ValueType | precision of matrix elements

## 46.122.2 Member Function Documentation

## 46.122.2.1 apply() [1/4]

Apply the matrix to a multi-vector with a linear combination of the given input vector.

Represents the matrix vector multiplication, x = alpha \* I

• b + beta \* x, where x and b are both multi-vectors.

#### **Parameters**

alpha	the scalar to scale the matrix-vector product with
b	the multi-vector to be applied to
beta	the scalar to scale the x vector with
X	the output multi-vector

## 46.122.2.2 apply() [2/4]

#### 46.122.2.3 apply() [3/4]

Apply the matrix to a multi-vector.

Represents the matrix vector multiplication, x = I \* b, where x and b are both multi-vectors.

#### **Parameters**

	the multi-vector to be applied to
X	the output multi-vector

## 46.122.2.4 apply() [4/4]

## 46.122.2.5 create()

Creates an Identity matrix of the specified size.

#### **Parameters**

exec	Executor associated to the matrix
size	size of the batch matrices in a batch_dim object

## Returns

A smart pointer to the newly created matrix.

The documentation for this class was generated from the following file:

• ginkgo/core/matrix/batch\_identity.hpp

# 46.123 gko::matrix::ldentityFactory< ValueType > Class Template Reference

This factory is a utility which can be used to generate Identity operators.

#include <ginkgo/core/matrix/identity.hpp>

## Static Public Member Functions

static std::unique\_ptr< IdentityFactory > create (std::shared\_ptr< const Executor > exec)
 Creates a new Identity factory.

## **Additional Inherited Members**

## 46.123.1 Detailed Description

```
template<typename ValueType = default_precision> class gko::matrix::ldentityFactory< ValueType >
```

This factory is a utility which can be used to generate Identity operators.

The factory will generate the Identity matrix with the same dimension as the passed in operator. It will throw an exception if the operator is not square.

## **Template Parameters**

```
ValueType | precision of matrix elements
```

## 46.123.2 Member Function Documentation

## 46.123.2.1 create()

Creates a new Identity factory.

#### **Parameters**

```
exec the executor where the Identity operator will be stored
```

#### Returns

a unique pointer to the newly created factory

The documentation for this class was generated from the following file:

ginkgo/core/matrix/identity.hpp

## 46.124 gko::solver::ldr< ValueType > Class Template Reference

IDR(s) is an efficient method for solving large nonsymmetric systems of linear equations.

#include <ginkgo/core/solver/idr.hpp>

#### **Public Member Functions**

• std::unique ptr< LinOp > transpose () const override

Returns a LinOp representing the transpose of the Transposable object.

• std::unique\_ptr< LinOp > conj\_transpose () const override

Returns a LinOp representing the conjugate transpose of the Transposable object.

· bool apply\_uses\_initial\_guess () const override

Return true as iterative solvers use the data in x as an initial guess.

• size\_type get\_subspace\_dim () const

Gets the subspace dimension of the solver.

void set\_subspace\_dim (const size\_type other)

Sets the subspace dimension of the solver.

remove\_complex< ValueType > get\_kappa () const

Gets the kappa parameter of the solver.

void set\_kappa (const remove\_complex < ValueType > other)

Sets the kappa parameter of the solver.

· bool get deterministic () const

Gets the deterministic parameter of the solver.

void set\_deterministic (const bool other)

Sets the deterministic parameter of the solver.

bool get\_complex\_subspace () const

Gets the complex\_subspace parameter of the solver.

void set\_complex\_subpsace (const bool other)

Sets the complex\_subspace parameter of the solver.

void set complex subspace (const bool other)

Sets the complex\_subspace parameter of the solver.

## **Static Public Member Functions**

• static parameters\_type parse (const config::pnode &config, const config::registry &context, const config::type\_descriptor &td\_for\_child=config::make\_type\_descriptor < ValueType >())

Create the parameters from the property\_tree.

## 46.124.1 Detailed Description

template<typename ValueType = default\_precision> class gko::solver::ldr< ValueType >

IDR(s) is an efficient method for solving large nonsymmetric systems of linear equations.

The implemented version is the one presented in the paper "Algorithm 913: An elegant IDR(s) variant that efficiently exploits biorthogonality properties" by M. B. Van Gijzen and P. Sonneveld.

The method is based on the induced dimension reduction theorem which provides a way to construct subsequent residuals that lie in a sequence of shrinking subspaces. These subspaces are spanned by s vectors which are first generated randomly and then orthonormalized. They are stored in a dense matrix.

## **Template Parameters**

*ValueType* precision of the elements of the system matrix.

## 46.124.2 Member Function Documentation

## 46.124.2.1 apply\_uses\_initial\_guess()

```
template<typename ValueType = default_precision>
bool gko::solver::Idr< ValueType >::apply_uses_initial_guess ( ) const [inline], [override]
```

Return true as iterative solvers use the data in x as an initial guess.

#### Returns

true as iterative solvers use the data in x as an initial guess.

```
76 { return true; }
```

## 46.124.2.2 conj\_transpose()

```
template<typename ValueType = default_precision>
std::unique_ptr<LinOp> gko::solver::Idr< ValueType >::conj_transpose ( ) const [override],
[virtual]
```

Returns a LinOp representing the conjugate transpose of the Transposable object.

#### Returns

a pointer to the new conjugate transposed object

Implements gko::Transposable.

## 46.124.2.3 get\_complex\_subspace()

```
template<typename ValueType = default_precision>
bool gko::solver::Idr< ValueType >::get_complex_subspace ( ) const [inline]
```

Gets the complex\_subspace parameter of the solver.

#### Returns

the complex\_subspace parameter

## 46.124.2.4 get\_deterministic()

```
template<typename ValueType = default_precision>
bool gko::solver::Idr< ValueType >::get_deterministic ( ) const [inline]
```

Gets the deterministic parameter of the solver.

Returns

the deterministic parameter

## 46.124.2.5 get\_kappa()

```
template<typename ValueType = default_precision>
remove_complex<ValueType> gko::solver::Idr< ValueType >::get_kappa ( ) const [inline]
```

Gets the kappa parameter of the solver.

Returns

the kappa parameter

## 46.124.2.6 get\_subspace\_dim()

```
template<typename ValueType = default_precision>
size_type gko::solver::Idr< ValueType >::get_subspace_dim ( ) const [inline]
```

Gets the subspace dimension of the solver.

Returns

the subspace Dimension

## 46.124.2.7 parse()

Create the parameters from the property\_tree.

Because this is directly tied to the specific type, the value/index type settings within config are ignored and type\_ descriptor is only used for children configs.

#### **Parameters**

config	the property tree for setting	
context	the registry	
td_for_child	the type descriptor for children configs. The default uses the value type of this class.	

## Returns

parameters

## 46.124.2.8 set\_complex\_subpsace()

Sets the complex\_subspace parameter of the solver.

#### **Parameters**

other the new complex_su	bspace parameter
--------------------------	------------------

References gko::solver::ldr< ValueType >::set\_complex\_subspace().

## 46.124.2.9 set\_complex\_subspace()

Sets the complex\_subspace parameter of the solver.

#### **Parameters**

```
other the new complex_subspace parameter
```

## 46.124.2.10 set\_deterministic()

Sets the deterministic parameter of the solver.

#### **Parameters**

```
other the new deterministic parameter
```

## 46.124.2.11 set\_kappa()

Sets the kappa parameter of the solver.

#### **Parameters**

```
other the new kappa parameter
```

## 46.124.2.12 set\_subspace\_dim()

Sets the subspace dimension of the solver.

## **Parameters**

```
other the new subspace Dimension
```

## 46.124.2.13 transpose()

```
template<typename ValueType = default_precision>
std::unique_ptr<LinOp> gko::solver::Idr< ValueType >::transpose ( ) const [override], [virtual]
```

Returns a LinOp representing the transpose of the Transposable object.

#### Returns

a pointer to the new transposed object

Implements gko::Transposable.

The documentation for this class was generated from the following file:

• ginkgo/core/solver/idr.hpp

# 46.125 gko::preconditioner::llu< LSolverType, USolverType, ReverseApply, IndexType > Class Template Reference

The Incomplete LU (ILU) preconditioner solves the equation LUx = b for a given lower triangular matrix L, an upper triangular matrix U and the right hand side b (can contain multiple right hand sides).

#include <ginkgo/core/preconditioner/ilu.hpp>

#### **Public Member Functions**

- std::shared\_ptr< const l\_solver\_type > get\_l\_solver () const
- Returns the solver which is used for the provided L matrix.
- std::shared\_ptr< const u\_solver\_type > get\_u\_solver () const

Returns the solver which is used for the provided U matrix.

- std::unique\_ptr< LinOp > transpose () const override
  - Returns a LinOp representing the transpose of the Transposable object.
- std::unique\_ptr< LinOp > conj\_transpose () const override

Returns a LinOp representing the conjugate transpose of the Transposable object.

- Ilu & operator= (const Ilu &other)
  - Copy-assigns an ILU preconditioner.
- Ilu & operator= (Ilu &&other)

Move-assigns an ILU preconditioner.

• Ilu (const Ilu &other)

Copy-constructs an ILU preconditioner.

• Ilu (Ilu &&other)

Move-constructs an ILU preconditioner.

## **Static Public Member Functions**

• static parameters\_type parse (const config::pnode &config, const config::registry &context, const config::type descriptor &td for child=config::make type descriptor < value type, index type >())

Create the parameters from the property\_tree.

## 46.125.1 Detailed Description

template<typename LSolverType = solver::LowerTrs<>, typename USolverType = solver::UpperTrs<>, bool ReverseApply = false, typename IndexType = int32>

class gko::preconditioner::llu< LSolverType, USolverType, ReverseApply, IndexType >

The Incomplete LU (ILU) preconditioner solves the equation LUx=b for a given lower triangular matrix L, an upper triangular matrix U and the right hand side b (can contain multiple right hand sides).

It allows to set both the solver for L and the solver for U independently, while providing the defaults solver::LowerTrs and solver::UpperTrs, which are direct triangular solvers. For these solvers, a factory can be provided (with with—l\_solver and with\_u\_solver) to have more control over their behavior. In particular, it is possible to use an iterative method for solving the triangular systems. The default parameters for an iterative triangular solver are:

• reduction factor = 1e-4

• max iteration = <number of="" rows="" of="" the="" matrix="" given="" to="" the="" solver>=""> Solvers without such criteria can also be used, in which case none are set.

An object of this class can be created with a matrix or a gko::Composition containing two matrices. If created with a matrix, it is factorized before creating the solver. If a gko::Composition (containing two matrices) is used, the first operand will be taken as the L matrix, the second will be considered the U matrix. Parllu can be directly used, since it orders the factors in the correct way.

## Note

When providing a gko::Composition, the first matrix must be the lower matrix (L), and the second matrix must be the upper matrix (U). If they are swapped, solving might crash or return the wrong result.

Do not use symmetric solvers (like CG) for L or U solvers since both matrices (L and U) are, by design, not symmetric.

This class is not thread safe (even a const object is not) because it uses an internal cache to accelerate multiple (sequential) applies. Using it in parallel can lead to segmentation faults, wrong results and other unwanted behavior.

## **Template Parameters**

LSolverType	type of the solver used for the L matrix. Defaults to solver::LowerTrs
USolverType	type of the solver used for the U matrix Defaults to solver::UpperTrs
ReverseApply	default behavior (ReverseApply = false) is first to solve with L (Ly = b) and then with U (Ux = y). When set to true, it will solve first with U, and then with L.
IndexTypeParllu	Type of the indices when Parllu is used to generate both L and U factors. Irrelevant
	otherwise.

## 46.125.2 Constructor & Destructor Documentation

## 46.125.2.1 Ilu() [1/2]

Copy-constructs an ILU preconditioner.

Inherits the executor, shallow-copies the solvers and parameters.
365 : Ilu{other.get\_executor()} { \*this = other; }

References gko::PolymorphicObject::get executor().

## 46.125.2.2 Ilu() [2/2]

Move-constructs an ILU preconditioner.

Inherits the executor, moves the solvers and parameters. The moved-from object is empty (0x0 with nullptr solvers and default parameters)

References gko::PolymorphicObject::get executor().

## 46.125.3 Member Function Documentation

## 46.125.3.1 conj\_transpose()

```
template<typename LSolverType = solver::LowerTrs<>, typename USolverType = solver::Upper← Trs<>, bool ReverseApply = false, typename IndexType = int32> std::unique_ptr<LinOp> gko::preconditioner::Ilu< LSolverType, USolverType, ReverseApply, IndexType >::conj_transpose () const [inline], [override], [virtual]
```

Returns a LinOp representing the conjugate transpose of the Transposable object.

## Returns

a pointer to the new conjugate transposed object

Implements gko::Transposable.

References gko::PolymorphicObject::get\_executor(), gko::preconditioner::Ilu< LSolverType, USolverType, ReverseApply, IndexType >::get\_l\_solver(), gko::preconditioner::Ilu< LSolverType, USolverType, ReverseApply, IndexType >::get\_u\_solver(), gko::share(), and gko::transpose().

## 46.125.3.2 get I solver()

```
template<typename LSolverType = solver::LowerTrs<>, typename USolverType = solver::Upper←
Trs<>, bool ReverseApply = false, typename IndexType = int32>
std::shared_ptr<const l_solver_type> gko::preconditioner::Ilu< LSolverType, USolverType,
ReverseApply, IndexType >::get_l_solver () const [inline]
```

Returns the solver which is used for the provided L matrix.

#### Returns

the solver which is used for the provided L matrix

Referenced by gko::preconditioner::llu< LSolverType, USolverType, ReverseApply, IndexType >::conj\_transpose(), and gko::preconditioner::llu< LSolverType, USolverType, ReverseApply, IndexType >::transpose().

## 46.125.3.3 get\_u\_solver()

```
template<typename LSolverType = solver::LowerTrs<>, typename USolverType = solver::Upper←
Trs<>, bool ReverseApply = false, typename IndexType = int32>
std::shared_ptr<const u_solver_type> gko::preconditioner::Ilu< LSolverType, USolverType,
ReverseApply, IndexType >::get_u_solver () const [inline]
```

Returns the solver which is used for the provided U matrix.

#### Returns

the solver which is used for the provided U matrix

Referenced by gko::preconditioner::llu< LSolverType, USolverType, ReverseApply, IndexType >::conj\_transpose(), and gko::preconditioner::llu< LSolverType, USolverType, ReverseApply, IndexType >::transpose().

#### 46.125.3.4 operator=() [1/2]

Copy-assigns an ILU preconditioner.

Preserves the executor, shallow-copies the solvers and parameters. Creates a clone of the solvers if they are on the wrong executor.

References gko::clone(), and gko::PolymorphicObject::get\_executor().

## 46.125.3.5 operator=() [2/2]

Move-assigns an ILU preconditioner.

Preserves the executor, moves the solvers and parameters. Creates a clone of the solvers if they are on the wrong executor. The moved-from object is empty (0x0 with nullptr solvers and default parameters)

References gko::clone(), and gko::PolymorphicObject::get\_executor().

## 46.125.3.6 parse()

Create the parameters from the property\_tree.

Because this is directly tied to the specific type, the value/index type settings within config are ignored and type\_ descriptor is only used for children configs.

## **Parameters**

config	the property tree for setting
context	the registry
td_for_child	the type descriptor for children configs. The default uses the value/index type of this class.

#### Returns

parameters

#### Note

only support the following pairs for <l\_solver, u\_solver>: <lr> | Ir>, <Gmres, Gmres>, <LowerTrs, Upper</td> | Trs>, and <LowerIsai, UpperIsai>

## 46.125.3.7 transpose()

```
template<typename LSolverType = solver::LowerTrs<>, typename USolverType = solver::Upper
Trs<>, bool ReverseApply = false, typename IndexType = int32>
std::unique_ptr<LinOp> gko::preconditioner::Ilu< LSolverType, USolverType, ReverseApply,
IndexType >::transpose () const [inline], [override], [virtual]
```

Returns a LinOp representing the transpose of the Transposable object.

## Returns

a pointer to the new transposed object

Implements gko::Transposable.

References gko::PolymorphicObject::get\_executor(), gko::preconditioner::Ilu< LSolverType, USolverType, ReverseApply, IndexType >::get\_l\_solver(), gko::preconditioner::Ilu< LSolverType, USolverType, ReverseApply, IndexType >::get\_u\_solver(), gko::share(), and gko::transpose().

The documentation for this class was generated from the following file:

• ginkgo/core/preconditioner/ilu.hpp

## 46.126 gko::factorization::llu< ValueType, IndexType > Class Template Reference

Represents an incomplete LU factorization – ILU(0) – of a sparse matrix.

```
#include <ginkgo/core/factorization/ilu.hpp>
```

## **Static Public Member Functions**

• static parameters\_type parse (const config::pnode &config, const config::registry &context, const config::type\_descriptor &td\_for\_child=config::make\_type\_descriptor < ValueType, IndexType >())

Create the parameters from the property\_tree.

#### **Additional Inherited Members**

## 46.126.1 Detailed Description

```
template<typename ValueType = gko::default_precision, typename IndexType = gko::int32> class gko::factorization::llu< ValueType, IndexType >
```

Represents an incomplete LU factorization – ILU(0) – of a sparse matrix.

More specifically, it consists of a lower unitriangular factor L and an upper triangular factor U with sparsity pattern S(L+U) = S(A) fulfilling LU = A at every non-zero location of A.

## **Template Parameters**

ValueType	Type of the values of all matrices used in this class
IndexType	Type of the indices of all matrices used in this class

## 46.126.2 Member Function Documentation

## 46.126.2.1 parse()

Create the parameters from the property tree.

Because this is directly tied to the specific type, the value/index type settings within config are ignored and type\_ descriptor is only used for children configs.

#### **Parameters**

config	the property tree for setting
context	the registry
td_for_child	the type descriptor for children configs. The default uses the value/index type of this class.

## Returns

parameters

The documentation for this class was generated from the following file:

· ginkgo/core/factorization/ilu.hpp

# 46.127 gko::matrix::Hybrid< ValueType, IndexType >::imbalance bounded limit Class Reference

imbalance\_bounded\_limit is a strategy\_type which decides the number of stored elements per row of the ell part.

#include <ginkgo/core/matrix/hybrid.hpp>

## **Public Member Functions**

- imbalance\_bounded\_limit (double percent=0.8, double ratio=0.0001)
  - Creates a imbalance\_bounded\_limit strategy.
- size\_type compute\_ell\_num\_stored\_elements\_per\_row (array < size\_type > \*row\_nnz) const override
   Computes the number of stored elements per row of the ell part.
- · auto get percentage () const
  - Get the percent setting.
- auto get\_ratio () const

Get the ratio setting.

## 46.127.1 Detailed Description

template < typename ValueType = default\_precision, typename IndexType = int32 > class gko::matrix::Hybrid < ValueType, IndexType > ::imbalance\_bounded\_limit

imbalance\_bounded\_limit is a strategy\_type which decides the number of stored elements per row of the ell part.

It uses the imbalance\_limit and adds the upper bound of the number of ell's cols by the number of rows.

## 46.127.2 Member Function Documentation

## 46.127.2.1 compute\_ell\_num\_stored\_elements\_per\_row()

```
template<typename ValueType = default_precision, typename IndexType = int32> size_type gko::matrix::Hybrid< ValueType, IndexType >::imbalance_bounded_limit::compute_ell_← num_stored_elements_per_row (

array< size_type > * row_nnz ) const [inline], [override], [virtual]
```

Computes the number of stored elements per row of the ell part.

#### **Parameters**

row_nnz	the number of nonzeros of each row	l
---------	------------------------------------	---

## Returns

the number of stored elements per row of the ell part

Implements gko::matrix::Hybrid< ValueType, IndexType >::strategy\_type.

References gko::matrix::Hybrid< ValueType, IndexType >::imbalance\_limit::compute\_ell\_num\_stored\_elements -- \_\_per\_row(), and gko::array< ValueType >::get\_size().

Referenced by gko::matrix::Hybrid< ValueType, IndexType >::automatic::compute\_ell\_num\_stored\_elements\_ compute\_ell\_num\_stored\_elements.

## 46.127.2.2 get\_percentage()

```
template<typename ValueType = default_precision, typename IndexType = int32>
auto gko::matrix::Hybrid< ValueType, IndexType >::imbalance_bounded_limit::get_percentage ( )
const [inline]
```

Get the percent setting.

## Returns

percent

References gko::matrix::Hybrid< ValueType, IndexType >::imbalance\_limit::get\_percentage().

## 46.127.2.3 get\_ratio()

```
template<typename ValueType = default_precision, typename IndexType = int32>
auto gko::matrix::Hybrid< ValueType, IndexType >::imbalance_bounded_limit::get_ratio ( ) const
[inline]
```

Get the ratio setting.

## Returns

ratio

The documentation for this class was generated from the following file:

ginkgo/core/matrix/hybrid.hpp

## 46.128 gko::matrix::Hybrid< ValueType, IndexType >::imbalance\_limit Class Reference

imbalance\_limit is a strategy\_type which decides the number of stored elements per row of the ell part according to the percent.

#include <ginkgo/core/matrix/hybrid.hpp>

## **Public Member Functions**

- imbalance\_limit (double percent=0.8)
  - Creates a imbalance\_limit strategy.
- size\_type compute\_ell\_num\_stored\_elements\_per\_row (array < size\_type > \*row\_nnz) const override
   Computes the number of stored elements per row of the ell part.
- auto get\_percentage () const
   Get the percent setting.

## 46.128.1 Detailed Description

template<typename ValueType = default\_precision, typename IndexType = int32> class gko::matrix::Hybrid< ValueType, IndexType >::imbalance\_limit

imbalance\_limit is a strategy\_type which decides the number of stored elements per row of the ell part according to the percent.

It sorts the number of nonzeros of each row and takes the value at the position floor (percent \* num\_row) as the number of stored elements per row of the ell part. Thus, at least percent rows of all are in the ell part.

## 46.128.2 Constructor & Destructor Documentation

#### 46.128.2.1 imbalance limit()

Creates a imbalance\_limit strategy.

## **Parameters**

percent the row\_nnz[floor(num\_rows\*percent)] is the number of stored elements per row of the ell part

## 46.128.3 Member Function Documentation

## 46.128.3.1 compute\_ell\_num\_stored\_elements\_per\_row()

Computes the number of stored elements per row of the ell part.

#### **Parameters**

row	nnz	the number of nonzeros of each row
-----	-----	------------------------------------

#### Returns

the number of stored elements per row of the ell part

Implements gko::matrix::Hybrid< ValueType, IndexType >::strategy\_type.

References gko::array < ValueType >::get data(), and gko::array < ValueType >::get size().

Referenced by gko::matrix::Hybrid< ValueType, IndexType >::imbalance\_bounded\_limit::compute\_ell\_num\_ stored\_elements\_per\_row(), and gko::matrix::Hybrid< ValueType, IndexType >::minimal\_storage\_limit::compute \_ell\_num\_stored\_elements\_per\_row().

## 46.128.3.2 get\_percentage()

```
template<typename ValueType = default_precision, typename IndexType = int32>
auto gko::matrix::Hybrid< ValueType, IndexType >::imbalance_limit::get_percentage ( ) const
[inline]
```

Get the percent setting.

#### Returns

percent

Referenced by gko::matrix::Hybrid< ValueType, IndexType >::imbalance\_bounded\_limit::get\_percentage(), and gko::matrix::Hybrid< ValueType, IndexType >::minimal storage limit::get percentage().

The documentation for this class was generated from the following file:

ginkgo/core/matrix/hybrid.hpp

## 46.129 gko::stop::ImplicitResidualNorm< ValueType > Class Template Reference

The ImplicitResidualNorm class is a stopping criterion which stops the iteration process when the implicit residual norm is below a certain threshold relative to.

#include <ginkgo/core/stop/residual\_norm.hpp>

## 46.129.1 Detailed Description

template < typename ValueType = default\_precision > class gko::stop::ImplicitResidualNorm < ValueType >

The ImplicitResidualNorm class is a stopping criterion which stops the iteration process when the implicit residual norm is below a certain threshold relative to.

- the norm of the right-hand side, implicit\_resnorm ≤ < threshold \* norm(right\_hand\_side)</li>
- 2. the initial residual, implicit\_resnorm  $\leq$  threshold \* norm(initial\_residual) .
- $3. \ \ \text{one, implicit\_resnorm} \leq \text{threshold}.$

Note

To use this stopping criterion there are some dependencies. The constructor depends on either b or the initial\_residual in order to compute their norms. If this is not correctly provided, an exception ::gko ::NotSupported() is thrown.

The documentation for this class was generated from the following file:

· ginkgo/core/stop/residual\_norm.hpp

# 46.130 gko::experimental::distributed::index\_map < LocalIndexType, GlobalIndexType > Struct Template Reference

This class defines mappings between global and local indices.

#include <ginkgo/core/distributed/index\_map.hpp>

## **Public Member Functions**

array< LocalIndexType > map\_to\_local (const array< GlobalIndexType > &global\_ids, index\_space index
 —space\_v) const

Maps global indices to local indices.

· size\_type get\_global\_size () const

get size of index\_space::local

size\_type get\_local\_size () const

get size of index\_space::local

• size\_type get\_non\_local\_size () const

get size of index\_space::non\_local

index\_map (std::shared\_ptr< const Executor > exec, std::shared\_ptr< const partition\_type > partition,
 comm\_index\_type rank, const array
 GlobalIndexType > &recv\_connections)

Creates a new index map.

index\_map (std::shared\_ptr< const Executor > exec)

Creates an empty index map.

const segmented\_array< GlobalIndexType > & get\_remote\_global\_idxs () const

get the index set  $R_k$  for this rank.

const segmented\_array< LocalIndexType > & get\_remote\_local\_idxs () const

get the index set  $R_k$ , but mapped to their respective local index space.

const array< comm\_index\_type > & get\_remote\_target\_ids () const

get the rank ids which contain indices accessed by this rank.

- std::shared\_ptr< const Executor > get\_executor () const

get the associated executor.

## 46.130.1 Detailed Description

template<typename LocalIndexType, typename GlobalIndexType = int64> struct gko::experimental::distributed::index\_map< LocalIndexType, GlobalIndexType >

This class defines mappings between global and local indices.

Given an index space  $I=[0,\dots,N)$  that is partitioned into P disjoint subsets  $I_k, k=1,\dots,P$ , this class defines for each subset an extended global index set  $\hat{I}_k\supset I_K$ . The extended index set contains the global indices owned by part k, as well as remote indices  $R_k=\hat{I}_k\setminus I_k$ , which are also accessed by part k, but owned by parts  $l\neq k$ . At the core, this class provides mappings from the global index space I into different local index spaces. The combined local index space (index\_space::combined) is then defined as  $[0,\dots,|\hat{I}_k|)$ . Additionally, the combined index space can be separated into locally owned (index\_space::local) and non-locally owned (index\_space::non\_local). The locally owned indices are defined as  $[0,\dots,|I_k|)$ , and the non-locally owned as  $[0,\dots,|R_k|)$ . With these index sets, the following mappings are defined:

- $c_k: \hat{I}_k \mapsto [0, \dots, |\hat{I}_k|)$  which maps global indices into the combined/full local index space (denoted as index space::combined),
- $l_k:I_k\mapsto [0,\ldots,|I_k|)$  which maps global indices into the locally owned index space (denoted as index\_space::local),
- $r_k: R_k \mapsto [0, \dots, |R_k|)$  which maps global indices into the non-locally owned index space (denoted as index\_space::non\_local).

The required map can be selected by passing the appropriate type of an index\_space.

The index map for  $I_k$  has no knowledge about any other index maps for  $I_l$ ,  $l \neq k$ . In particular, any global index passed to the map\_to\_local map that is not part of the specified index space, will be mapped to an invalid\_index.

## **Template Parameters**

LocalIndexType	type for local indices
GlobalIndexType	type for global indices

## 46.130.2 Constructor & Destructor Documentation

## 46.130.2.1 index map()

Creates a new index map.

The passed in recv\_connections may contain duplicates, which will be filtered out.

#### **Parameters**

exec	the executor
partition	the partition of the global index set
rank	the id of the global index space subset
recv_connections	the global indices that are not owned by this rank, but accessed by it

## 46.130.3 Member Function Documentation

## 46.130.3.1 get\_remote\_global\_idxs()

```
template<typename LocalIndexType , typename GlobalIndexType = int64> const segmented_array<GlobalIndexType>& gko::experimental::distributed::index_map< Local↔ IndexType, GlobalIndexType >::get_remote_global_idxs ( ) const
```

get the index set  $R_k$  for this rank.

The indices are ordered by their owning rank and global index.

## 46.130.3.2 get\_remote\_local\_idxs()

```
template<typename LocalIndexType , typename GlobalIndexType = int64>
const segmented_array<LocalIndexType>& gko::experimental::distributed::index_map< Local←
IndexType, GlobalIndexType >::get_remote_local_idxs ( ) const
```

get the index set  $R_k$ , but mapped to their respective local index space.

The indices are grouped by their owning rank and sorted according to their global index within each group.

The set  $R_k = \hat{I}_k \setminus I_k$  can also be written as the union of the intersection of  $\hat{I}_k$  with other disjoint sets  $I_l, l \neq k$ , i.e.  $R_k = \bigcup_{j \neq k} \hat{I}_k \cap I_j = \bigcup_{j \neq k} R_{k,j}$ . The set  $R_{k,j}$  can then be mapped by  $l_j$  to get the local indices wrt. part j. The indices here are mapped by  $l_j$ .

#### 46.130.3.3 get remote target ids()

```
template<typename LocalIndexType , typename GlobalIndexType = int64>
const array<comm_index_type>& gko::experimental::distributed::index_map< LocalIndexType,
GlobalIndexType >::get_remote_target_ids ( ) const
```

get the rank ids which contain indices accessed by this rank.

The order matches the order of the sets in get\_remote\_global\_idxs and get\_remote\_local\_idxs.

#### 46.130.3.4 map\_to\_local()

Maps global indices to local indices.

## **Parameters**

global_ids	the global indices to map
index_space←	the index space in which the returned local indices are defined
_v	

#### Returns

the mapped local indices. Any global index that is not in the specified index space is mapped to invalid\_index.

The documentation for this struct was generated from the following file:

• ginkgo/core/distributed/index\_map.hpp

## 46.131 gko::index\_set< IndexType > Class Template Reference

An index set class represents an ordered set of intervals.

#include <ginkgo/core/base/index\_set.hpp>

## **Public Types**

using index\_type = IndexType

The type of elements stored in the index set.

#### **Public Member Functions**

• index\_set (std::shared\_ptr< const Executor > exec) noexcept

Creates an empty index\_set tied to the specified Executor.

index\_set (std::shared\_ptr< const gko::Executor > exec, std::initializer\_list< IndexType > init\_list, const bool
is\_sorted=false)

Creates an index set on the specified executor from the initializer list.

index\_set (std::shared\_ptr< const gko::Executor > exec, const index\_type size, const gko::array< index\_type</li>
 &indices, const bool is\_sorted=false)

Creates an index set on the specified executor and the given size.

index\_set (std::shared\_ptr< const Executor > exec, const index\_set &other)

Creates a copy of the input index\_set on a different executor.

• index set (const index set &other)

Creates a copy of the input index\_set.

index\_set (std::shared\_ptr< const Executor > exec, index\_set &&other)

Moves the input index\_set to a different executor.

index\_set (index\_set &&other)

Moves the input index\_set.

index\_set & operator= (const index\_set &other)

Copies data from another index set.

index\_set & operator= (index\_set &&other)

Moves data from another index\_set.

• void clear () noexcept

Deallocates all data used by the index\_set.

std::shared\_ptr< const Executor > get\_executor () const

Returns the executor of the index\_set.

• index\_type get\_size () const

Returns the size of the index set space.

bool is\_contiguous () const

Returns if the index set is contiguous.

• index\_type get\_num\_elems () const

Return the actual number of indices stored in the index set.

• index\_type get\_global\_index (index\_type local\_index) const

Return the global index given a local index.

index\_type get\_local\_index (index\_type global\_index) const

Return the local index given a global index.

This is an array version of the scalar function above.

This is an array version of the scalar function above.

array< index\_type > to\_global\_indices () const

This function allows the user obtain a decompressed global\_indices array from the indices stored in the index set.

array < bool > contains (const array < index\_type > &global\_indices, const bool is\_sorted=false) const
 Checks if the individual global indeices exist in the index set.

bool contains (const index\_type global\_index) const

Checks if the global index exists in the index set.

index\_type get\_num\_subsets () const

Returns the number of subsets stored in the index set.

const index\_type \* get\_subsets\_begin () const

Returns a pointer to the beginning indices of the subsets.

const index type \* get subsets end () const

Returns a pointer to the end indices of the subsets.

const index\_type \* get\_superset\_indices () const

Returns a pointer to the cumulative indices of the superset of the subsets.

## 46.131.1 Detailed Description

```
template<typename IndexType = int32> class gko::index_set< IndexType >
```

An index set class represents an ordered set of intervals.

The index set contains subsets which store the starting and end points of a range, [a,b), storing the first index and one past the last index. As the index set only stores the end-points of ranges, it can be quite efficient in terms of storage.

This class is particularly useful in storing continuous ranges. For example, consider the index set (1, 2, 3, 4, 5, 6, 7, 8, 10, 11, 12, 18, 19, 20, 21, 42). Instead of storing the entire array of indices, one can store intervals ([1,9), [10,13), [18,22), [42,43)), thereby only using half the storage.

We store three arrays, one (subsets\_begin) with the starting indices of the subsets in the index set, another (subsets\_end) storing one index beyond the end indices of the subsets and the last (superset\_cumulative\_indices) storing the cumulative number of indices in the subsequent subsets with an initial zero which speeds up the querying. Additionally, the arrays conataining the range boundaries (subsets\_begin, subsets\_end) are stored in a sorted fashion.

Therefore the storage would look as follows

```
index_set = (1, 2, 3, 4, 5, 6, 7, 8, 10, 11, 12, 18, 19, 20, 21, 42) subsets_begin = \{1, 10, 18, 42\} subsets_end = \{9, 13, 22, 43\} superset_cumulative_indices = \{0, 8, 11, 15, 16\}
```

## **Template Parameters**

```
index_type type of the indices being stored in the index set.
```

#### 46.131.2 Constructor & Destructor Documentation

#### 46.131.2.1 index\_set() [1/7]

```
template<typename IndexType = int32>
gko::index_set< IndexType >::index_set (
```

```
std::shared_ptr< const Executor > exec ) [inline], [explicit], [noexcept]
```

Creates an empty index\_set tied to the specified Executor.

#### **Parameters**

```
exec the Executor where the index_set data is allocated
```

#### 46.131.2.2 index\_set() [2/7]

Creates an index set on the specified executor from the initializer list.

#### **Parameters**

exec     the Executor where the index set data will be allocated       init_list     the indices that the index set should hold in an initializer_list.       is_sorted     a parameter that specifies if the indices array is sorted or not. true if so	
--	--

## 46.131.2.3 index\_set() [3/7]

Creates an index set on the specified executor and the given size.

exec	the Executor where the index set data will be allocated	
size	the maximum index the index set it allowed to hold. This is the size of the index space.	
indices	the indices that the index set should hold.	
is_sorted	a parameter that specifies if the indices array is sorted or not. true if sorted.	

References gko::array< ValueType >::get\_size().

#### 46.131.2.4 index\_set() [4/7]

Creates a copy of the input index\_set on a different executor.

#### **Parameters**

exec	the executor where the new index_set will be created
other	the index_set to copy from

## 46.131.2.5 index\_set() [5/7]

Creates a copy of the input index\_set.

#### **Parameters**

other	the index_set to copy from
-------	----------------------------

## 46.131.2.6 index\_set() [6/7]

Moves the input index\_set to a different executor.

exec	the executor where the new index_set will be moved to
other	the index_set to move from

#### 46.131.2.7 index\_set() [7/7]

Moves the input index\_set.

#### **Parameters**

other	the index_set to move from
-------	----------------------------

## 46.131.3 Member Function Documentation

## 46.131.3.1 clear()

```
template<typename IndexType = int32>
void gko::index_set< IndexType >::clear ( ) [inline], [noexcept]
```

Deallocates all data used by the index\_set.

The index\_set is left in a valid, but empty state, so the same index\_set can be used to allocate new memory. Calls to index\_set::get\_subsets\_begin() will return a nullptr.

References gko::array< ValueType >::clear().

## 46.131.3.2 contains() [1/2]

Checks if the individual global indeices exist in the index set.

global_indices	the indices to check.
is_sorted	a parameter that specifies if the query array is sorted or not. true if sorted.

#### Returns

the array that contains element wise whether the corresponding global index in the index set or not.

#### 46.131.3.3 contains() [2/2]

Checks if the global index exists in the index set.

#### **Parameters**

global_index	the index to check.
--------------	---------------------

#### Returns

whether the element exists in the index set.

#### Warning

This single entry query can have significant kernel launch overheads and should be avoided if possible.

## 46.131.3.4 get\_executor()

```
template<typename IndexType = int32>
std::shared_ptr<const Executor> gko::index_set< IndexType >::get_executor ( ) const [inline]
```

Returns the executor of the index set.

#### Returns

the executor.

## 46.131.3.5 get\_global\_index()

Return the global index given a local index.

Consider the set  $idx\_set = (0, 1, 2, 4, 6, 7, 8, 9)$ . This function returns the element at the global index k stored in the index set. For example,  $idx\_set.get\_global\_index(0) == 0 idx\_set.get\_global\_index(3) == 4 and <math>idx\_set.get\_global\_index(7) == 9$ 

#### Note

This function returns a scalar value and needs a scalar value. For repeated queries, it is more efficient to use the array functions that take and return arrays which allow for more throughput.

#### **Parameters**

local index	the local index.

#### Returns

the global index from the index set.

#### Warning

This single entry query can have significant kernel launch overheads and should be avoided if possible.

#### 46.131.3.6 get\_local\_index()

Return the local index given a global index.

Consider the set  $idx_set = (0, 1, 2, 4, 6, 7, 8, 9)$ . This function returns the local index in the index set of the provided index set. For example,  $idx_set_get_local_index(0) == 0 idx_set_get_local_index(4) == 3 and <math>idx_set_get_local_index(6) == 4$ .

## Note

This function returns a scalar value and needs a scalar value. For repeated queries, it is more efficient to use the array functions that take and return arrays which allow for more throughput.

#### **Parameters**

global_index	the global index.
--------------	-------------------

#### Returns

the local index of the element in the index set.

#### Warning

This single entry query can have significant kernel launch overheads and should be avoided if possible.

## 46.131.3.7 get\_num\_elems()

```
template<typename IndexType = int32>
index_type gko::index_set< IndexType >::get_num_elems ( ) const [inline]
```

Return the actual number of indices stored in the index set.

#### Returns

number of indices stored in the index set

## 46.131.3.8 get\_num\_subsets()

```
template<typename IndexType = int32>
index_type gko::index_set< IndexType >::get_num_subsets ( ) const [inline]
```

Returns the number of subsets stored in the index set.

#### Returns

the number of stored subsets.

References gko::array< ValueType >::get size().

Referenced by gko::index\_set< IndexType >::is\_contiguous().

## 46.131.3.9 get\_size()

```
template<typename IndexType = int32>
index_type gko::index_set< IndexType >::get_size ( ) const [inline]
```

Returns the size of the index set space.

#### Returns

the size of the index set space.

## 46.131.3.10 get\_subsets\_begin()

```
template<typename IndexType = int32>
const index_type* gko::index_set< IndexType >::get_subsets_begin ( ) const [inline]
```

Returns a pointer to the beginning indices of the subsets.

#### Returns

a pointer to the beginning indices of the subsets.

References gko::array < ValueType >::get\_const\_data().

## 46.131.3.11 get\_subsets\_end()

```
template<typename IndexType = int32>
const index_type* gko::index_set< IndexType >::get_subsets_end ( ) const [inline]
```

Returns a pointer to the end indices of the subsets.

Returns

a pointer to the end indices of the subsets.

References gko::array< ValueType >::get const data().

## 46.131.3.12 get superset indices()

```
template<typename IndexType = int32>
const index_type* gko::index_set< IndexType >::get_superset_indices ( ) const [inline]
```

Returns a pointer to the cumulative indices of the superset of the subsets.

Returns

a pointer to the cumulative indices of the superset of the subsets.

References gko::array< ValueType >::get\_const\_data().

## 46.131.3.13 is\_contiguous()

```
template<typename IndexType = int32>
bool gko::index_set< IndexType >::is_contiguous ( ) const [inline]
```

Returns if the index set is contiguous.

Returns

if the index set is contiguous.

References gko::index\_set< IndexType >::get\_num\_subsets().

## 46.131.3.14 map\_global\_to\_local()

This is an array version of the scalar function above.

#### **Parameters**

global_indices	the global index array.
is_sorted	a parameter that specifies if the query array is sorted or not. true if sorted.

#### Returns

the local index array from the index set.

#### Note

Whenever possible, passing a sorted array is preferred as the queries can be significantly faster.

## 46.131.3.15 map\_local\_to\_global()

This is an array version of the scalar function above.

#### **Parameters**

local_indices	the local index array.
is_sorted	a parameter that specifies if the query array is sorted or not. $\verb true $ if sorted .

### Returns

the global index array from the index set.

## Note

Whenever possible, passing a sorted array is preferred as the queries can be significantly faster. Passing local indices from [0, size) is equivalent to using the @to\_global\_indices function.

## 46.131.3.16 operator=() [1/2]

Copies data from another index\_set.

The executor of this is preserved. In case this does not have an assigned executor, it will inherit the executor of other.

#### **Parameters**

#### Returns

this

## 46.131.3.17 operator=() [2/2]

Moves data from another index\_set.

The executor of this is preserved. In case this does not have an assigned executor, it will inherit the executor of other.

#### **Parameters**

other	the index	set to move from	
-------	-----------	------------------	--

## Returns

this

## 46.131.3.18 to\_global\_indices()

```
template<typename IndexType = int32>
array<index_type> gko::index_set< IndexType >::to_global_indices ( ) const
```

This function allows the user obtain a decompressed global\_indices array from the indices stored in the index set.

## Returns

the decompressed set of indices.

The documentation for this class was generated from the following file:

ginkgo/core/base/index\_set.hpp

# 46.132 gko::InvalidStateError Class Reference

Exception thrown if an object is in an invalid state.

```
#include <ginkgo/core/base/exception.hpp>
```

## **Public Member Functions**

InvalidStateError (const std::string &file, int line, const std::string &func, const std::string &clarification)
 Initializes an invalid state error.

## 46.132.1 Detailed Description

Exception thrown if an object is in an invalid state.

## 46.132.2 Constructor & Destructor Documentation

#### 46.132.2.1 InvalidStateError()

Initializes an invalid state error.

#### **Parameters**

file	The name of the offending source file
line	The source code line number where the error occurred
func	The function name where the error occurred
clarification	A message describing the invalid state

The documentation for this class was generated from the following file:

• ginkgo/core/base/exception.hpp

# 46.133 gko::solver::lr< ValueType > Class Template Reference

Iterative refinement (IR) is an iterative method that uses another coarse method to approximate the error of the current solution via the current residual.

```
#include <ginkgo/core/solver/ir.hpp>
```

#### **Public Member Functions**

• std::unique\_ptr< LinOp > transpose () const override

Returns a LinOp representing the transpose of the Transposable object.

std::unique\_ptr< LinOp > conj\_transpose () const override

Returns a LinOp representing the conjugate transpose of the Transposable object.

· bool apply\_uses\_initial\_guess () const override

Return true as iterative solvers use the data in x as an initial guess.

std::shared ptr< const LinOp > get solver () const

Returns the solver operator used as the inner solver.

void set\_solver (std::shared\_ptr< const LinOp > new\_solver)

Sets the solver operator used as the inner solver.

Ir & operator= (const Ir &)

Copy-assigns an IR solver.

Ir & operator= (Ir &&)

Move-assigns an IR solver.

Ir (const Ir &)

Copy-constructs an IR solver.

• Ir (Ir &&)

Move-constructs an IR solver.

#### **Static Public Member Functions**

• static parameters\_type parse (const config::pnode &config, const config::registry &context, const config::type\_descriptor &td\_for\_child=config::make\_type\_descriptor < ValueType >())

Create the parameters from the property\_tree.

## 46.133.1 Detailed Description

```
template < typename ValueType = default_precision > class gko::solver::lr < ValueType >
```

Iterative refinement (IR) is an iterative method that uses another coarse method to approximate the error of the current solution via the current residual.

Moreover, it can be also considered as preconditioned Richardson iteration with relaxation factor = 1.

For any approximation of the solution solution to the system Ax = b, the residual is defined as: residual = b - A solution. The error in solution, e = x - solution (with x being the exact solution) can be obtained as the solution to the residual equation Ae = residual, since Ae = Ax - A solution = b - A solution = residual. Then, the real solution is computed as  $x = relaxation_factor * solution + e$ . Instead of accurately solving the residual equation Ae = residual, the solution of the system e can be approximated to obtain the approximation error using a coarse method solver, which is used to update solution, and the entire process is repeated with the updated solution. This yields the iterative refinement method:

```
solution = initial_guess
while not converged:
    residual = b - A solution
    error = solver(A, residual)
    solution = solution + relaxation_factor * error
```

With relaxation\_factor equal to 1 (default), the solver is Iterative Refinement, with relaxation\_factor equal to a value other than 1, the solver is a Richardson iteration, with possibility for additional preconditioning.

Assuming that solver has accuracy c, i.e., | e - error | <= c | e |, iterative refinement will converge with a convergence rate of c. Indeed, from e - error = x - solution - error = x - solution\* (where solution\* denotes the value stored in solution after the update) and <math>e = inv(A) residual = inv(A)b - inv(A) A solution = x - solution it follows that | x - solution\* | <= c | x - solution |.

Unless otherwise specified via the solver factory parameter, this implementation uses the identity operator (i.e. the solver that approximates the solution of a system Ax = b by setting x := b) as the default inner solver. Such a setting results in a relaxation method known as the Richardson iteration with parameter 1, which is guaranteed to converge for matrices whose spectrum is strictly contained within the unit disc around 1 (i.e., all its eigenvalues lambda have to satisfy the equation '|relaxation\_factor \* lambda - 1| < 1).

#### **Template Parameters**

ValueType	precision of matrix elements
-----------	------------------------------

## 46.133.2 Constructor & Destructor Documentation

## 46.133.2.1 Ir() [1/2]

Copy-constructs an IR solver.

Inherits the executor, shallow-copies inner solver, stopping criterion and system matrix.

## 46.133.2.2 Ir() [2/2]

Move-constructs an IR solver.

Preserves the executor, moves inner solver, stopping criterion and system matrix. The moved-from object is empty (0x0 and nullptr inner solver, stopping criterion and system matrix)

## 46.133.3 Member Function Documentation

#### 46.133.3.1 apply\_uses\_initial\_guess()

```
template<typename ValueType = default_precision>
bool gko::solver::Ir< ValueType >::apply_uses_initial_guess ( ) const [inline], [override]
```

Return true as iterative solvers use the data in x as an initial guess.

#### Returns

true as iterative solvers use the data in x as an initial guess.

References gko::solver::provided.

#### 46.133.3.2 conj\_transpose()

```
template<typename ValueType = default_precision>
std::unique_ptr<LinOp> gko::solver::Ir< ValueType >::conj_transpose ( ) const [override],
[virtual]
```

Returns a LinOp representing the conjugate transpose of the Transposable object.

#### Returns

a pointer to the new conjugate transposed object

Implements gko::Transposable.

## 46.133.3.3 get\_solver()

```
template<typename ValueType = default_precision>
std::shared_ptr<const LinOp> gko::solver::Ir< ValueType >::get_solver ( ) const [inline]
```

Returns the solver operator used as the inner solver.

## Returns

the solver operator used as the inner solver

## 46.133.3.4 operator=() [1/2]

Copy-assigns an IR solver.

Preserves the executor, shallow-copies inner solver, stopping criterion and system matrix. If the executors mismatch, clones inner solver, stopping criterion and system matrix onto this executor.

#### 46.133.3.5 operator=() [2/2]

Move-assigns an IR solver.

Preserves the executor, moves inner solver, stopping criterion and system matrix. If the executors mismatch, clones inner solver, stopping criterion and system matrix onto this executor. The moved-from object is empty (0x0 and nullptr inner solver, stopping criterion and system matrix)

#### 46.133.3.6 parse()

Create the parameters from the property\_tree.

Because this is directly tied to the specific type, the value/index type settings within config are ignored and type\_ descriptor is only used for children configs.

#### **Parameters**

config	the property tree for setting
context	the registry
td_for_child	the type descriptor for children configs. The default uses the value type of this class.

#### Returns

parameters

## 46.133.3.7 set\_solver()

Sets the solver operator used as the inner solver.

new solver	the new inner solver
TIEW SOIVE	LITE HEW HITEL SOIVE

#### 46.133.3.8 transpose()

```
template<typename ValueType = default_precision>
std::unique_ptr<LinOp> gko::solver::Ir< ValueType >::transpose ( ) const [override], [virtual]
```

Returns a LinOp representing the transpose of the Transposable object.

#### Returns

a pointer to the new transposed object

Implements gko::Transposable.

The documentation for this class was generated from the following file:

• ginkgo/core/solver/ir.hpp

# 46.134 gko::preconditioner::lsai< lsaiType, ValueType, IndexType > Class Template Reference

The Incomplete Sparse Approximate Inverse (ISAI) Preconditioner generates an approximate inverse matrix for a given square matrix A, lower triangular matrix L, upper triangular matrix U or symmetric positive (spd) matrix B.

```
#include <ginkgo/core/preconditioner/isai.hpp>
```

#### **Public Member Functions**

std::shared\_ptr< const typename std::conditional< IsaiType==isai\_type::spd, Comp, Csr >::type > get approximate inverse () const

Returns the approximate inverse of the given matrix (either a CSR matrix for IsaiType general, upper or lower or a composition of two CSR matrices for IsaiType spd).

Isai & operator= (const Isai & other)

Copy-assigns an ISAI preconditioner.

• Isai & operator= (Isai &&other)

Move-assigns an ISAI preconditioner.

Isai (const Isai &other)

Copy-constructs an ISAI preconditioner.

· Isai (Isai &&other)

Move-constructs an ISAI preconditioner.

std::unique\_ptr< LinOp > transpose () const override

Returns a LinOp representing the transpose of the Transposable object.

• std::unique\_ptr< LinOp > conj\_transpose () const override

Returns a LinOp representing the conjugate transpose of the Transposable object.

#### **Static Public Member Functions**

• static parameters\_type parse (const config::pnode &config, const config::registry &context, const config::type\_descriptor &td\_for\_child=config::make\_type\_descriptor < ValueType, IndexType >())

Create the parameters from the property\_tree.

## 46.134.1 Detailed Description

```
template<isai_type | saiType, typename | ValueType, typename | IndexType> class gko::preconditioner::lsai< | IsaiType, ValueType, IndexType>
```

The Incomplete Sparse Approximate Inverse (ISAI) Preconditioner generates an approximate inverse matrix for a given square matrix A, lower triangular matrix L, upper triangular matrix U or symmetric positive (spd) matrix B.

Using the preconditioner computes aiA\*x, aiU\*x, aiL\*x or  $aiC^T*aiC*x$  (depending on the type of the Isai) for a given vector x (may have multiple right hand sides). aiA, aiU and aiL are the approximate inverses for A, U and L respectively. aiC is an approximation to C, the exact Cholesky factor of B (This is commonly referred to as a Factorized Sparse Approximate Inverse, short FSPAI).

The sparsity pattern used for the approximate inverse of A, L and U is the same as the sparsity pattern of the respective matrix. For B, the sparsity pattern used for the approximate inverse is the same as the sparsity pattern of the lower triangular half of B.

Note that, except for the spd case, for a matrix A generally  $ISAI(A)^T = ISAI(A^T)$ .

For more details on the algorithm, see the paper Incomplete Sparse Approximate Inverses for Parallel Preconditioning, which is the basis for this work.

#### Note

GPU implementations can only handle the vector unit width width (warp size for CUDA) as number of elements per row in the sparse matrix. If there are more than width elements per row, the remaining elements will be ignored.

## **Template Parameters**

IsaiType	determines if the ISAI is generated for a general square matrix, a lower triangular matrix, an upper triangular matrix or an spd matrix
ValueType	precision of matrix elements
IndexType	precision of matrix indexes

## 46.134.2 Constructor & Destructor Documentation

#### 46.134.2.1 Isai() [1/2]

Copy-constructs an ISAI preconditioner.

Inherits the executor, shallow-copies the matrix and parameters.

## 46.134.2.2 Isai() [2/2]

Move-constructs an ISAI preconditioner.

Inherits the executor, moves the matrix and parameters. The moved-from object is empty (0x0 with nullptr matrix and default parameters)

#### 46.134.3 Member Function Documentation

## 46.134.3.1 conj\_transpose()

```
template<isai_type IsaiType, typename ValueType , typename IndexType >
std::unique_ptr<LinOp> gko::preconditioner::Isai< IsaiType, ValueType, IndexType >::conj_
transpose ( ) const [override], [virtual]
```

Returns a LinOp representing the conjugate transpose of the Transposable object.

#### Returns

a pointer to the new conjugate transposed object

Implements gko::Transposable.

## 46.134.3.2 get\_approximate\_inverse()

```
template<isai_type IsaiType, typename ValueType , typename IndexType >
std::shared_ptr<const typename std::conditional<IsaiType == isai_type::spd, Comp, Csr>::type>
gko::preconditioner::Isai< IsaiType, ValueType, IndexType >::get_approximate_inverse ( ) const
[inline]
```

Returns the approximate inverse of the given matrix (either a CSR matrix for IsaiType general, upper or lower or a composition of two CSR matrices for IsaiType spd).

## Returns

the generated approximate inverse

References gko::as().

#### 46.134.3.3 operator=() [1/2]

Copy-assigns an ISAI preconditioner.

Preserves the executor, shallow-copies the matrix and parameters. Creates a clone of the matrix if it is on the wrong executor.

#### 46.134.3.4 operator=() [2/2]

Move-assigns an ISAI preconditioner.

Preserves the executor, moves the matrix and parameters. Creates a clone of the matrix if it is on the wrong executor. The moved-from object is empty (0x0 with nullptr matrix and default parameters)

#### 46.134.3.5 parse()

Create the parameters from the property\_tree.

Because this is directly tied to the specific type, the value/index type settings within config are ignored and type\_ descriptor is only used for children configs.

#### **Parameters**

config	the property tree for setting
context	the registry
td_for_child	the type descriptor for children configs. The default uses the value/index type of this class.

## Returns

parameters

#### 46.134.3.6 transpose()

```
{\tt template}{<} {\tt isai\_type} \  \, {\tt IsaiType}, \  \, {\tt typename} \  \, {\tt ValueType} \  \, , \  \, {\tt typename} \  \, {\tt IndexType} \  \, > \\
```

```
std::unique_ptr<LinOp> gko::preconditioner::Isai< IsaiType, ValueType, IndexType >::transpose
( ) const [override], [virtual]
```

Returns a LinOp representing the transpose of the Transposable object.

Returns

a pointer to the new transposed object

Implements gko::Transposable.

The documentation for this class was generated from the following file:

· ginkgo/core/preconditioner/isai.hpp

## 46.135 gko::stop::Iteration Class Reference

The Iteration class is a stopping criterion which stops the iteration process after a preset number of iterations.

```
#include <ginkgo/core/stop/iteration.hpp>
```

## 46.135.1 Detailed Description

The Iteration class is a stopping criterion which stops the iteration process after a preset number of iterations.

Note

to use this stopping criterion, it is required to update the iteration count for the ::check() method.

The documentation for this class was generated from the following file:

• ginkgo/core/stop/iteration.hpp

## 46.136 gko::log::iteration\_complete\_data Struct Reference

Struct representing iteration complete related data.

```
#include <ginkgo/core/log/record.hpp>
```

## 46.136.1 Detailed Description

Struct representing iteration complete related data.

The documentation for this struct was generated from the following file:

• ginkgo/core/log/record.hpp

## 46.137 gko::solver::IterativeBase Class Reference

A LinOp implementing this interface stores a stopping criterion factory.

```
#include <ginkgo/core/solver_base.hpp>
```

#### **Public Member Functions**

- std::shared\_ptr< const stop::CriterionFactory > get\_stop\_criterion\_factory () const Gets the stopping criterion factory of the solver.
- virtual void set\_stop\_criterion\_factory (std::shared\_ptr< const stop::CriterionFactory > new\_stop\_factory)

  Sets the stopping criterion of the solver.

## 46.137.1 Detailed Description

A LinOp implementing this interface stores a stopping criterion factory.

#### 46.137.2 Member Function Documentation

## 46.137.2.1 get\_stop\_criterion\_factory()

```
std::shared_ptr<const stop::CriterionFactory> gko::solver::IterativeBase::get_stop_criterion←
_factory ( ) const [inline]
```

Gets the stopping criterion factory of the solver.

Returns

the stopping criterion factory

Referenced by gko::solver::EnableIterativeBase< Bicg< ValueType > >::operator=().

#### 46.137.2.2 set\_stop\_criterion\_factory()

Sets the stopping criterion of the solver.

#### **Parameters**

other	the new stopping criterion factory
-------	------------------------------------

```
Reimplemented in gko::solver::EnableIterativeBase< DerivedType >, gko::solver::EnableIterativeBase< Bicgstab< ValueType >>, gko::solver::EnableIterativeBase< Multigrid >, gko::solver::EnableIterativeBase< Gmres< ValueType >>, gko::solver::EnableIterativeBase< Ir< ValueType >>, gko::solver::EnableIterativeBase< Ir< ValueType >>, gko::solver::EnableIterativeBase< Ir< ValueType >>, gko::solver::EnableIterativeBase< Idr< ValueType >>, gko::solver::EnableIterativeBase< Gcr< ValueType >>, gko::solver::EnableIterativeBase< Gcr< ValueType >>, gko::solver::EnableIterativeBase< Gcr< ValueType >>, gko::solver::EnableIterativeBase< Gcr< ValueType >>, gko::solver::EnableIterativeBase< Bicg< ValueType >>.
```

Referenced by gko::solver::EnableIterativeBase< Bicg< ValueType > >::set\_stop\_criterion\_factory().

The documentation for this class was generated from the following file:

• ginkgo/core/solver/solver\_base.hpp

# 46.138 gko::batch::preconditioner::Jacobi < ValueType, IndexType > Class Template Reference

A block-Jacobi preconditioner is a block-diagonal linear operator, obtained by inverting the diagonal blocks (stored in a dense row major fashion) of the source operator.

```
#include <ginkgo/core/preconditioner/batch_jacobi.hpp>
```

## **Public Member Functions**

- const index\_type \* get\_const\_block\_pointers () const noexcept
   Returns the block pointers.
- const index\_type \* get\_const\_map\_block\_to\_row () const noexcept

Returns the mapping between the blocks and the row id.

const index\_type \* get\_const\_blocks\_cumulative\_offsets () const noexcept

Returns the cumulative blocks storage array.

uint32 get\_max\_block\_size () const noexcept

Returns the max block size.

size\_type get\_num\_blocks () const noexcept

Returns the number of blocks in an individual batch entry.

const value\_type \* get\_const\_blocks () const noexcept

Returns the pointer to the memory used for storing the block data.

size\_type get\_num\_stored\_elements () const noexcept

Returns the number of elements explicitly stored in the dense blocks.

## 46.138.1 Detailed Description

template<typename ValueType = default\_precision, typename IndexType = int32> class gko::batch::preconditioner::Jacobi< ValueType, IndexType >

A block-Jacobi preconditioner is a block-diagonal linear operator, obtained by inverting the diagonal blocks (stored in a dense row major fashion) of the source operator.

With the batched preconditioners, it is required that all items in the batch have the same sparsity pattern. The detection of the blocks and the block pointers require that the sparsity pattern of all the items be the same. Other cases is undefined behaviour. The input batch matrix must be in batch::Csr matrix format or must be convertible to batch::Csr matrix format. The block detection algorithm and the conversion to dense blocks kernels require this assumption.

#### Note

In a fashion similar to the non-batched Jacobi preconditioner, the maximum possible size of the diagonal blocks is equal to the maximum warp size on the device (32 for NVIDIA GPUs, 64 for AMD GPUs).

## **Template Parameters**

ValueType	value precision of matrix elements
IndexType	index precision of matrix elements

## 46.138.2 Member Function Documentation

## 46.138.2.1 get\_const\_block\_pointers()

```
template<typename ValueType = default_precision, typename IndexType = int32> const index_type* gko::batch::preconditioner::Jacobi< ValueType, IndexType >::get_const_← block_pointers ( ) const [inline], [noexcept]
```

Returns the block pointers.

#### Note

Returns nullptr in case of a scalar jacobi preconditioner (max\_block\_size = 1).

#### Returns

## the block pointers

```
68 {
69          return block_pointers_.get_const_data();
70    }
```

References gko::array< ValueType >::get const data().

### 46.138.2.2 get\_const\_blocks()

```
template<typename ValueType = default_precision, typename IndexType = int32>
const value_type* gko::batch::preconditioner::Jacobi< ValueType, IndexType >::get_const_blocks
( ) const [inline], [noexcept]
```

Returns the pointer to the memory used for storing the block data.

Element (i, j) of the block, which belongs to the batch entry with index = "batch\_id" and has local id = "block—id" within its batch entry is stored at the address = get\_const\_blocks() + detail::get\_global\_block\_offset(batch\_id, num\_blocks, block\_id, cumulative\_blocks\_storage) + i \* detail::get\_stride(block\_id, block\_pointers) + j

Note

Returns nullptr in case of a scalar jacobi preconditioner (max\_block\_size = 1). The blocks array is empty in case of scalar jacobi preconditioner as the preconditioner is generated inside the batched solver kernel.

#### Returns

the pointer to the memory used for storing the block data

References gko::array < ValueType >::get\_const\_data().

#### 46.138.2.3 get const blocks cumulative offsets()

```
template<typename ValueType = default_precision, typename IndexType = int32>
const index_type* gko::batch::preconditioner::Jacobi< ValueType, IndexType >::get_const_
blocks_cumulative_offsets ( ) const [inline], [noexcept]
```

Returns the cumulative blocks storage array.

Note

Returns nullptr in case of a scalar jacobi preconditioner (max block size = 1).

References gko::array< ValueType >::get\_const\_data().

#### 46.138.2.4 get const map block to row()

```
template<typename ValueType = default_precision, typename IndexType = int32>
const index_type* gko::batch::preconditioner::Jacobi< ValueType, IndexType >::get_const_map_
block_to_row ( ) const [inline], [noexcept]
```

Returns the mapping between the blocks and the row id.

Note

Returns nullptr in case of a scalar jacobi preconditioner (max\_block\_size = 1).

References gko::array< ValueType >::get\_const\_data().

#### 46.138.2.5 get\_max\_block\_size()

```
template<typename ValueType = default_precision, typename IndexType = int32>
uint32 gko::batch::preconditioner::Jacobi< ValueType, IndexType >::get_max_block_size ( )
const [inline], [noexcept]
```

Returns the max block size.

#### Returns

the max block size

### 46.138.2.6 get\_num\_blocks()

```
template<typename ValueType = default_precision, typename IndexType = int32>
size_type gko::batch::preconditioner::Jacobi< ValueType, IndexType >::get_num_blocks ( ) const
[inline], [noexcept]
```

Returns the number of blocks in an individual batch entry.

#### Returns

the number of blocks in an individual batch entry.

## 46.138.2.7 get\_num\_stored\_elements()

```
template<typename ValueType = default_precision, typename IndexType = int32>
size_type gko::batch::preconditioner::Jacobi< ValueType, IndexType >::get_num_stored_elements
( ) const [inline], [noexcept]
```

Returns the number of elements explicitly stored in the dense blocks.

#### Note

Returns 0 in case of scalar jacobi preconditioner as the preconditioner is generated inside the batched solver kernels, hence, blocks array storage is not required.

## Returns

the number of elements explicitly stored in the dense blocks.

References gko::array< ValueType >::get\_size().

The documentation for this class was generated from the following file:

ginkgo/core/preconditioner/batch\_jacobi.hpp

# 46.139 gko::preconditioner::Jacobi < ValueType, IndexType > Class Template Reference

A block-Jacobi preconditioner is a block-diagonal linear operator, obtained by inverting the diagonal blocks of the source operator.

#include <ginkgo/core/preconditioner/jacobi.hpp>

#### **Public Member Functions**

• size\_type get\_num\_blocks () const noexcept

Returns the number of blocks of the operator.

const block\_interleaved\_storage\_scheme < index\_type > & get\_storage\_scheme () const noexcept

Returns the storage scheme used for storing Jacobi blocks.

const value\_type \* get\_blocks () const noexcept

Returns the pointer to the memory used for storing the block data.

const remove\_complex< value\_type > \* get\_conditioning () const noexcept

Returns an array of 1-norm condition numbers of the blocks.

• size\_type get\_num\_stored\_elements () const noexcept

Returns the number of elements explicitly stored in the matrix.

void convert\_to (matrix::Dense< value\_type > \*result) const override

Converts the implementer to an object of type result\_type.

void move\_to (matrix::Dense< value\_type > \*result) override

Converts the implementer to an object of type result\_type by moving data from this object.

• void write (mat\_data &data) const override

Writes a matrix to a matrix\_data structure.

std::unique\_ptr< LinOp > transpose () const override

Returns a LinOp representing the transpose of the Transposable object.

std::unique\_ptr< LinOp > conj\_transpose () const override

Returns a LinOp representing the conjugate transpose of the Transposable object.

Jacobi & operator= (const Jacobi & other)

Copy-assigns a Jacobi preconditioner.

Jacobi & operator= (Jacobi &&other)

Move-assigns a Jacobi preconditioner.

• Jacobi (const Jacobi &other)

Copy-constructs a Jacobi preconditioner.

Jacobi (Jacobi &&other)

Move-assigns a Jacobi preconditioner.

## **Static Public Member Functions**

• static parameters\_type parse (const config::pnode &config, const config::registry &context, const config::type\_descriptor &td\_for\_child=config::make\_type\_descriptor < ValueType, IndexType >())

Create the parameters from the property\_tree.

## 46.139.1 Detailed Description

template<typename ValueType = default\_precision, typename IndexType = int32> class gko::preconditioner::Jacobi< ValueType, IndexType >

A block-Jacobi preconditioner is a block-diagonal linear operator, obtained by inverting the diagonal blocks of the source operator.

The Jacobi class implements the inversion of the diagonal blocks using Gauss-Jordan elimination with column pivoting, and stores the inverse explicitly in a customized format.

If the diagonal blocks of the matrix are not explicitly set by the user, the implementation will try to automatically detect the blocks by first finding the natural blocks of the matrix, and then applying the supervariable agglomeration procedure on them. However, if problem-specific knowledge regarding the block diagonal structure is available, it is usually beneficial to explicitly pass the starting rows of the diagonal blocks, as the block detection is merely a heuristic and cannot perfectly detect the diagonal block structure. The current implementation supports blocks of up to 32 rows / columns.

The implementation also includes an improved, adaptive version of the block-Jacobi preconditioner, which can store some of the blocks in lower precision and thus improve the performance of preconditioner application by reducing the amount of memory transfers. This variant can be enabled by setting the Jacobi::Factory's storage optimization parameter. Refer to the documentation of the parameter for more details.

#### **Template Parameters**

ValueType	precision of matrix elements
IndexType	integral type used to store pointers to the start of each block

#### Note

The current implementation supports blocks of up to 32 rows / columns.

When using the adaptive variant, there may be a trade-off in terms of slightly longer preconditioner generation due to extra work required to detect the optimal precision of the blocks.

When the max\_block\_size is set to 1, specialized kernels are used, both for generation (inverting the diagonals) and application (diagonal scaling) to reduce the overhead involved in the usual (adaptive) block case.

#### 46.139.2 Constructor & Destructor Documentation

#### 46.139.2.1 Jacobi() [1/2]

Copy-constructs a Jacobi preconditioner.

Inherits executor, copies all data and parameters.

#### 46.139.2.2 Jacobi() [2/2]

Move-assigns a Jacobi preconditioner.

Inherits executor, moves all data and parameters. The moved-from object will be empty (0x0 and default parameters).

## 46.139.3 Member Function Documentation

#### 46.139.3.1 conj\_transpose()

```
template<typename ValueType = default_precision, typename IndexType = int32>
std::unique_ptr<LinOp> gko::preconditioner::Jacobi< ValueType, IndexType >::conj_transpose (
) const [override], [virtual]
```

Returns a LinOp representing the conjugate transpose of the Transposable object.

#### Returns

a pointer to the new conjugate transposed object

Implements gko::Transposable.

#### 46.139.3.2 convert\_to()

Converts the implementer to an object of type result type.

#### **Parameters**

result the object used to store the result of the conversion

Implements gko::ConvertibleTo< matrix::Dense< ValueType >>.

### 46.139.3.3 get\_blocks()

```
template<typename ValueType = default_precision, typename IndexType = int32>
const value_type* gko::preconditioner::Jacobi< ValueType, IndexType >::get_blocks ( ) const
[inline], [noexcept]
```

Returns the pointer to the memory used for storing the block data.

Element (i, j) of block b is stored in position (get\_block\_pointers() [b] + i) \* stride + j of the array.

#### Returns

the pointer to the memory used for storing the block data

References gko::array< ValueType >::get\_const\_data().

### 46.139.3.4 get conditioning()

```
template<typename ValueType = default_precision, typename IndexType = int32>
const remove_complex<value_type>* gko::preconditioner::Jacobi< ValueType, IndexType >::get_
conditioning ( ) const [inline], [noexcept]
```

Returns an array of 1-norm condition numbers of the blocks.

#### Returns

an array of 1-norm condition numbers of the blocks

#### Note

This value is valid only if adaptive precision variant is used, and implementations of the standard non-adaptive variant are allowed to omit the calculation of condition numbers.

References gko::array< ValueType >::get\_const\_data().

#### 46.139.3.5 get\_num\_blocks()

```
template<typename ValueType = default_precision, typename IndexType = int32>
size_type gko::preconditioner::Jacobi< ValueType, IndexType >::get_num_blocks ( ) const [inline],
[noexcept]
```

Returns the number of blocks of the operator.

#### Returns

the number of blocks of the operator

#### 46.139.3.6 get\_num\_stored\_elements()

```
template<typename ValueType = default_precision, typename IndexType = int32>
size_type gko::preconditioner::Jacobi< ValueType, IndexType >::get_num_stored_elements ( )
const [inline], [noexcept]
```

Returns the number of elements explicitly stored in the matrix.

#### Returns

the number of elements explicitly stored in the matrix

References gko::array< ValueType >::get\_size().

## 46.139.3.7 get\_storage\_scheme()

```
template<typename ValueType = default_precision, typename IndexType = int32>
const block_interleaved_storage_scheme<index_type>& gko::preconditioner::Jacobi< ValueType,
IndexType >::get_storage_scheme ( ) const [inline], [noexcept]
```

Returns the storage scheme used for storing Jacobi blocks.

#### Returns

the storage scheme used for storing Jacobi blocks

#### 46.139.3.8 move\_to()

Converts the implementer to an object of type result\_type by moving data from this object.

This method is used when the implementer is a temporary object, and move semantics can be used.

#### **Parameters**

```
result | the object used to emplace the result of the conversion
```

#### Note

ConvertibleTo::move\_to can be implemented by simply calling ConvertibleTo::convert\_to. However, this operation can often be optimized by exploiting the fact that implementer's data can be moved to the result.

Implements gko::ConvertibleTo< matrix::Dense< ValueType >>.

### 46.139.3.9 operator=() [1/2]

Copy-assigns a Jacobi preconditioner.

Preserves executor, copies all data and parameters.

## 46.139.3.10 operator=() [2/2]

Move-assigns a Jacobi preconditioner.

Preserves executor, moves all data and parameters. The moved-from object will be empty (0x0 and default parameters).

#### 46.139.3.11 parse()

Create the parameters from the property\_tree.

Because this is directly tied to the specific type, the value/index type settings within config are ignored and type\_ descriptor is only used for children configs.

#### **Parameters**

config	the property tree for setting
context	the registry
td_for_child	the type descriptor for children configs. The default uses the value/index type of this class.

## Returns

parameters

## Note

Jacobi does not support block\_pointers and storage\_optimization array.

#### 46.139.3.12 transpose()

```
template<typename ValueType = default_precision, typename IndexType = int32>
std::unique_ptr<LinOp> gko::preconditioner::Jacobi< ValueType, IndexType >::transpose ( )
const [override], [virtual]
```

Returns a LinOp representing the transpose of the Transposable object.

#### Returns

a pointer to the new transposed object

Implements gko::Transposable.

#### 46.139.3.13 write()

Writes a matrix to a matrix\_data structure.

#### **Parameters**

```
data the matrix_data structure
```

Implements gko::WritableToMatrixData< ValueType, IndexType >.

The documentation for this class was generated from the following file:

• ginkgo/core/preconditioner/jacobi.hpp

# 46.140 gko::KernelNotFound Class Reference

KernelNotFound is thrown if Ginkgo cannot find a kernel which satisfies the criteria imposed by the input arguments.

```
#include <ginkgo/core/base/exception.hpp>
```

## **Public Member Functions**

KernelNotFound (const std::string &file, int line, const std::string &func)
 Initializes a KernelNotFound error.

## 46.140.1 Detailed Description

KernelNotFound is thrown if Ginkgo cannot find a kernel which satisfies the criteria imposed by the input arguments.

## 46.140.2 Constructor & Destructor Documentation

## 46.140.2.1 KernelNotFound()

Initializes a KernelNotFound error.

#### **Parameters**

file	The name of the offending source file
line	The source code line number where the error occurred
func	The name of the function where the error occurred

The documentation for this class was generated from the following file:

• ginkgo/core/base/exception.hpp

# 46.141 gko::log::linop\_data Struct Reference

Struct representing LinOp related data.

```
#include <ginkgo/core/log/record.hpp>
```

## 46.141.1 Detailed Description

Struct representing LinOp related data.

The documentation for this struct was generated from the following file:

• ginkgo/core/log/record.hpp

# 46.142 gko::log::linop\_factory\_data Struct Reference

Struct representing LinOp factory related data.

#include <ginkgo/core/log/record.hpp>

## 46.142.1 Detailed Description

Struct representing LinOp factory related data.

The documentation for this struct was generated from the following file:

· ginkgo/core/log/record.hpp

# 46.143 gko::LinOpFactory Class Reference

A LinOpFactory represents a higher order mapping which transforms one linear operator into another.

#include <ginkgo/core/base/lin\_op.hpp>

#### Additional Inherited Members

## 46.143.1 Detailed Description

A LinOpFactory represents a higher order mapping which transforms one linear operator into another.

In Ginkgo, every linear solver is viewed as a mapping. For example, given an s.p.d linear system Ax=b, the solution  $x=A^{-1}b$  can be computed using the CG method. This algorithm can be represented in terms of linear operators and mappings between them as follows:

- A Cg::Factory is a higher order mapping which, given an input operator A, returns a new linear operator  $A^{-1}$  stored in "CG format"
- Storing the operator  $A^{-1}$  in "CG format" means that the data structure used to store the operator is just a simple pointer to the original matrix A. The application  $x=A^{-1}b$  of such an operator can then be implemented by solving the linear system Ax=b using the CG method. This is achieved in code by having a special class for each of those "formats" (e.g. the "Cg" class defines such a format for the CG solver).

Another example of a LinOpFactory is a preconditioner. A preconditioner for a linear operator A is a linear operator  $M^{-1}$ , which approximates  $A^{-1}$ . In addition, it is stored in a way such that both the data of  $M^{-1}$  is cheap to compute from A, and the operation  $x=M^{-1}b$  can be computed quickly. These operators are useful to accelerate the convergence of Krylov solvers. Thus, a preconditioner also fits into the LinOpFactory framework:

- The factory maps a linear operator A into a preconditioner  $M^{-1}$  which is stored in suitable format (e.g. as a product of two factors in case of ILU preconditioners).
- The resulting linear operator implements the application operation  $x = M^{-1}b$  depending on the format the preconditioner is stored in (e.g. as two triangular solves in case of ILU)

#### 46.143.1.1 Example: using CG in Ginkgo

```
{c++}
// Suppose A is a matrix, b a rhs vector, and x an initial guess
// Create a CG which runs for at most 1000 iterations, and stops after
// reducing the residual norm by 6 orders of magnitude
auto cg_factory = solver::Cg<>::build()
    .with_max_iters(1000)
    .with_rel_residual_goal(1e-6)
    .on(cuda);
// create a linear operator which represents the solver
auto cg = cg_factory->generate(A);
// solve the system
cg->apply(b, x);
```

The documentation for this class was generated from the following file:

• ginkgo/core/base/lin\_op.hpp

# 46.144 gko::matrix::Csr< ValueType, IndexType >::load\_balance Class Reference

load\_balance is a strategy\_type which uses the load balance algorithm.

```
#include <ginkgo/core/matrix/csr.hpp>
```

#### **Public Member Functions**

• load\_balance ()

Creates a load\_balance strategy.

load\_balance (std::shared\_ptr< const CudaExecutor > exec)

Creates a load\_balance strategy with CUDA executor.

load\_balance (std::shared\_ptr< const HipExecutor > exec)

Creates a load\_balance strategy with HIP executor.

load\_balance (std::shared\_ptr< const DpcppExecutor > exec)

Creates a load\_balance strategy with DPCPP executor.

- load\_balance (int64\_t nwarps, int warp\_size=32, bool cuda\_strategy=true, std::string strategy\_name="none")
   Creates a load\_balance strategy with specified parameters.
- void process (const array < index\_type > &mtx\_row\_ptrs, array < index\_type > \*mtx\_srow) override
   Computes srow according to row pointers.
- int64\_t clac\_size (const int64\_t nnz) override

Computes the srow size according to the number of nonzeros.

-  $std::shared\_ptr < strategy\_type > copy$  () override

Copy a strategy.

## 46.144.1 Detailed Description

template < typename ValueType = default\_precision, typename IndexType = int32 > class gko::matrix::Csr < ValueType, IndexType >::load\_balance

load\_balance is a strategy\_type which uses the load balance algorithm.

# 46.144.2 Constructor & Destructor Documentation

# 46.144.2.1 load\_balance() [1/5]

```
template<typename ValueType = default_precision, typename IndexType = int32>
gko::matrix::Csr< ValueType, IndexType >::load_balance::load_balance ( ) [inline]
```

Creates a load balance strategy.

#### Warning

this is deprecated! Please rely on the new automatic strategy instantiation or use one of the other constructors.

# 46.144.2.2 load\_balance() [2/5]

Creates a load balance strategy with CUDA executor.

## **Parameters**

```
exec the CUDA executor
```

# 46.144.2.3 load\_balance() [3/5]

Creates a load\_balance strategy with HIP executor.

## **Parameters**

```
exec the HIP executor
```

#### 46.144.2.4 load\_balance() [4/5]

```
template<typename ValueType = default_precision, typename IndexType = int32>
```

Creates a load\_balance strategy with DPCPP executor.

#### **Parameters**

```
exec the DPCPP executor
```

Note

TODO: porting - we hardcode the subgroup size is 32

# 46.144.2.5 load\_balance() [5/5]

Creates a load\_balance strategy with specified parameters.

#### **Parameters**

nwarps	the number of warps in the executor	
warp_size	the warp size of the executor	
cuda_strategy	whether the cuda_strategy needs to be used.	

Note

The warp\_size must be the size of full warp. When using this constructor, set\_strategy needs to be called with correct parameters which is replaced during the conversion.

# 46.144.3 Member Function Documentation

# 46.144.3.1 clac\_size()

Computes the srow size according to the number of nonzeros.

#### **Parameters**

```
nnz the number of nonzeros
```

#### Returns

the size of srow

Implements gko::matrix::Csr< ValueType, IndexType >::strategy\_type.

References gko::ceildiv(), and gko::min().

#### 46.144.3.2 copy()

```
template<typename ValueType = default_precision, typename IndexType = int32>
std::shared_ptr<strategy_type> gko::matrix::Csr< ValueType, IndexType >::load_balance::copy (
) [inline], [override], [virtual]
```

#### Copy a strategy.

This is a workaround until strategies are revamped, since strategies like automatical do not work when actually shared.

Implements gko::matrix::Csr< ValueType, IndexType >::strategy\_type.

## 46.144.3.3 process()

Computes srow according to row pointers.

#### **Parameters**

mtx_row_ptrs	the row pointers of the matrix
mtx_srow	the srow of the matrix

Implements gko::matrix::Csr< ValueType, IndexType >::strategy\_type.

References gko::ceildiv(), gko::array < ValueType >::get\_const\_data(), gko::array < ValueType >::get\_data(), gko::array < ValueType >::get\_executor(), and gko::array < ValueType >::get\_size().

The documentation for this class was generated from the following file:

• ginkgo/core/matrix/csr.hpp

# 46.145 gko::log::Loggable Class Reference

Loggable class is an interface which should be implemented by classes wanting to support logging.

```
#include <ginkgo/core/log/logger.hpp>
```

#### **Public Member Functions**

virtual void add logger (std::shared ptr< const Logger > logger)=0

Adds a new logger to the list of subscribed loggers.

• virtual void remove\_logger (const Logger \*logger)=0

Removes a logger from the list of subscribed loggers.

virtual const std::vector< std::shared\_ptr< const Logger >> & get\_loggers () const =0

Returns the vector containing all loggers registered at this object.

• virtual void clear\_loggers ()=0

Remove all loggers registered at this object.

# 46.145.1 Detailed Description

Loggable class is an interface which should be implemented by classes wanting to support logging.

For most cases, one can rely on the EnableLogging mixin which provides a default implementation of this interface.

# 46.145.2 Member Function Documentation

#### 46.145.2.1 add\_logger()

Adds a new logger to the list of subscribed loggers.

#### **Parameters**

```
logger to add
```

Implemented in gko::Executor.

# 46.145.2.2 get\_loggers()

```
virtual const std::vector<std::shared_ptr<const Logger> >& gko::log::Loggable::get_loggers (
) const [pure virtual]
```

Returns the vector containing all loggers registered at this object.

#### Returns

the vector containing all registered loggers.

# 46.145.2.3 remove\_logger()

Removes a logger from the list of subscribed loggers.

#### **Parameters**

logger	the logger to remove
--------	----------------------

#### Note

The comparison is done using the logger's object unique identity. Thus, two loggers constructed in the same way are not considered equal.

Implemented in gko::Executor.

The documentation for this class was generated from the following file:

· ginkgo/core/log/logger.hpp

# 46.146 gko::log::Record::logged\_data Struct Reference

Struct storing the actually logged data.

```
#include <ginkgo/core/log/record.hpp>
```

# 46.146.1 Detailed Description

Struct storing the actually logged data.

The documentation for this struct was generated from the following file:

• ginkgo/core/log/record.hpp

# 46.147 gko::solver::LowerTrs< ValueType, IndexType > Class Template Reference

LowerTrs is the triangular solver which solves the system L x = b, when L is a lower triangular matrix.

#include <ginkgo/core/solver/triangular.hpp>

#### **Public Member Functions**

std::unique\_ptr< LinOp > transpose () const override

Returns a LinOp representing the transpose of the Transposable object.

• std::unique\_ptr< LinOp > conj\_transpose () const override

Returns a LinOp representing the conjugate transpose of the Transposable object.

• LowerTrs (const LowerTrs &)

Copy-assigns a triangular solver.

• LowerTrs (LowerTrs &&)

Move-assigns a triangular solver.

LowerTrs & operator= (const LowerTrs &)

Copy-constructs a triangular solver.

LowerTrs & operator= (LowerTrs &&)

Move-constructs a triangular solver.

#### Static Public Member Functions

• static parameters\_type parse (const config::pnode &config, const config::registry &context, const config::type\_descriptor &td\_for\_child=config::make\_type\_descriptor < ValueType, IndexType >())

Create the parameters from the property\_tree.

# 46.147.1 Detailed Description

template<typename ValueType = default\_precision, typename IndexType = int32> class gko::solver::LowerTrs< ValueType, IndexType >

LowerTrs is the triangular solver which solves the system L x = b, when L is a lower triangular matrix.

It works best when passing in a matrix in CSR format. If the matrix is not in CSR, then the generate step converts it into a CSR matrix. The generation fails if the matrix is not convertible to CSR.

Note

As the constructor uses the copy and convert functionality, it is not possible to create a empty solver or a solver with a matrix in any other format other than CSR, if none of the executor modules are being compiled with.

# **Template Parameters**

ValueType	precision of matrix elements
IndexType	precision of matrix indices

# 46.147.2 Constructor & Destructor Documentation

### 46.147.2.1 LowerTrs() [1/2]

Copy-assigns a triangular solver.

Preserves the executor, shallow-copies the system matrix. If the executors mismatch, clones system matrix onto this executor. Solver analysis information will be regenerated.

# 46.147.2.2 LowerTrs() [2/2]

Move-assigns a triangular solver.

Preserves the executor, moves the system matrix. If the executors mismatch, clones system matrix onto this executor and regenerates solver analysis information. Moved-from object is empty (0x0 and nullptr system matrix)

## 46.147.3 Member Function Documentation

# 46.147.3.1 conj\_transpose()

```
template<typename ValueType = default_precision, typename IndexType = int32>
std::unique_ptr<LinOp> gko::solver::LowerTrs< ValueType, IndexType >::conj_transpose ( )
const [override], [virtual]
```

Returns a LinOp representing the conjugate transpose of the Transposable object.

#### Returns

a pointer to the new conjugate transposed object

Implements gko::Transposable.

#### 46.147.3.2 operator=() [1/2]

Copy-constructs a triangular solver.

Preserves the executor, shallow-copies the system matrix. Solver analysis information will be regenerated.

## 46.147.3.3 operator=() [2/2]

Move-constructs a triangular solver.

Preserves the executor, moves the system matrix and solver analysis information. Moved-from object is empty (0x0 and nullptr system matrix)

#### 46.147.3.4 parse()

Create the parameters from the property\_tree.

Because this is directly tied to the specific type, the value/index type settings within config are ignored and type\_ descriptor is only used for children configs.

#### **Parameters**

config	the property tree for setting	
context	the registry	
td_for_child	the type descriptor for children configs. The default uses the value/index type of this class.	

# Returns

parameters

#### 46.147.3.5 transpose()

```
template<typename ValueType = default_precision, typename IndexType = int32>
std::unique_ptr<LinOp> gko::solver::LowerTrs< ValueType, IndexType >::transpose ( ) const
[override], [virtual]
```

Returns a LinOp representing the transpose of the Transposable object.

## Returns

a pointer to the new transposed object

Implements gko::Transposable.

The documentation for this class was generated from the following file:

• ginkgo/core/solver/triangular.hpp

# 46.148 gko::experimental::factorization::Lu< ValueType, IndexType > Class Template Reference

Computes an LU factorization of a sparse matrix.

#include <ginkgo/core/factorization/lu.hpp>

# **Public Member Functions**

- const parameters\_type & get\_parameters ()
  - Returns the parameters used to construct the factory.

Returns the parameters used to construct the factory.

- const parameters\_type & get\_parameters () const
- std::unique\_ptr< factorization\_type > generate (std::shared\_ptr< const LinOp > system\_matrix) const

#### Static Public Member Functions

- static parameters\_type build ()
  - Creates a new parameter\_type to set up the factory.
- static parameters\_type parse (const config::pnode &config, const config::registry &context, const config::type\_descriptor &td\_for\_child=config::make\_type\_descriptor < ValueType, IndexType >())

Create the parameters from the property\_tree.

# 46.148.1 Detailed Description

template<typename ValueType, typename IndexType> class gko::experimental::factorization::Lu< ValueType, IndexType>

Computes an LU factorization of a sparse matrix.

This LinOpFactory returns a Factorization storing the L and U factors for the provided system matrix in matrix::Csr format. If no symbolic factorization is provided, it will be computed first.

# **Template Parameters**

ValueType	the type used to store values of the system matrix
IndexType	the type used to store sparsity pattern indices of the system matrix

## 46.148.2 Member Function Documentation

# 46.148.2.1 generate()

template<typename ValueType , typename IndexType >
std::unique\_ptr<factorization\_type> gko::experimental::factorization::Lu< ValueType, Index↔

#### Note

This function overrides the default LinOpFactory::generate to return a Factorization instead of a generic LinOp, which would need to be cast to Factorization again to access its factors. It is only necessary because smart pointers aren't covariant.

## 46.148.2.2 get\_parameters() [1/2]

```
template<typename ValueType , typename IndexType >
const parameters_type& gko::experimental::factorization::Lu< ValueType, IndexType >::get_←
parameters ( ) [inline]
```

Returns the parameters used to construct the factory.

#### Returns

the parameters used to construct the factory.

```
107 { return parameters_; }
```

## 46.148.2.3 get parameters() [2/2]

```
template<typename ValueType , typename IndexType >
const parameters_type& gko::experimental::factorization::Lu< ValueType, IndexType >::get_←
parameters ( ) const [inline]
```

Returns the parameters used to construct the factory.

## Returns

the parameters used to construct the factory.

# 46.148.2.4 parse()

Create the parameters from the property\_tree.

Because this is directly tied to the specific type, the value/index type settings within config are ignored and type\_ descriptor is only used for children configs.

#### **Parameters**

config	the property tree for setting	
context	the registry	
td_for_child	the type descriptor for children configs. The default uses the value/index type of this class.	

#### Returns

parameters

The documentation for this class was generated from the following file:

• ginkgo/core/factorization/lu.hpp

# 46.149 gko::machine\_topology Class Reference

The machine topology class represents the hierarchical topology of a machine, including NUMA nodes, cores and PCI Devices.

#include <ginkgo/core/base/machine\_topology.hpp>

# **Public Member Functions**

- void bind\_to\_cores (const std::vector< int > &ids, const bool singlify=true) const
   Bind the calling process to the CPU cores associated with the ids.
- void bind\_to\_core (const int &id) const

Bind to a single core.

void bind\_to\_pus (const std::vector< int > &ids, const bool singlify=true) const

Bind the calling process to PUs associated with the ids.

• void bind\_to\_pu (const int &id) const

Bind to a Processing unit (PU)

const normal\_obj\_info \* get\_pu (size\_type id) const

Get the object of type PU associated with the id.

• const normal\_obj\_info \* get\_core (size\_type id) const

Get the object of type core associated with the id.

const io\_obj\_info \* get\_pci\_device (size\_type id) const

Get the object of type pci device associated with the id.

const io\_obj\_info \* get\_pci\_device (const std::string &pci\_bus\_id) const

Get the object of type pci device associated with the PCI bus id.

• size\_type get\_num\_pus () const

Get the number of PU objects stored in this Topology tree.

• size\_type get\_num\_cores () const

Get the number of core objects stored in this Topology tree.

size\_type get\_num\_pci\_devices () const

Get the number of PCI device objects stored in this Topology tree.

size\_type get\_num\_numas () const

Get the number of NUMA objects stored in this Topology tree.

#### **Static Public Member Functions**

static machine\_topology \* get\_instance ()
 Returns an instance of the machine topology object.

# 46.149.1 Detailed Description

The machine topology class represents the hierarchical topology of a machine, including NUMA nodes, cores and PCI Devices.

Various information of the machine are gathered with the help of the Hardware Locality library (hwloc).

This class also provides functionalities to bind objects in the topology to the execution objects. Binding can enhance performance by allowing data to be closer to the executing object.

See the hwloc documentation ( https://www.open-mpi.org/projects/hwloc/doc/) for more detailed information on topology detection and binding interfaces.

Note

A global object of machine\_topology type is created in a thread safe manner and only destroyed at the end of the program. This means that any subsequent queries will be from the same global object and hence use an extra atomic read.

# 46.149.2 Member Function Documentation

# 46.149.2.1 bind\_to\_core()

Bind to a single core.

# **Parameters**

```
ids The ids of the core to be bound to the calling process.
```

References bind\_to\_cores(), and get\_instance().

# 46.149.2.2 bind\_to\_cores()

Bind the calling process to the CPU cores associated with the ids.

#### **Parameters**

ids	The ids of cores to be bound.
singlify	The ids of PUs are singlified to prevent possibly expensive migrations by the OS. This means that the
	binding is performed for only one of the ids in the set of ids passed in. See hwloc doc for
	singlify

Referenced by bind\_to\_core().

# 46.149.2.3 bind to pu()

Bind to a Processing unit (PU)

#### **Parameters**

References bind\_to\_pus(), and get\_instance().

# 46.149.2.4 bind\_to\_pus()

Bind the calling process to PUs associated with the ids.

# **Parameters**

ids	The ids of PUs to be bound.
singlify	The ids of PUs are singlified to prevent possibly expensive migrations by the OS. This means that the
	binding is performed for only one of the ids in the set of ids passed in. See hwloc doc for
	singlify

Referenced by bind\_to\_pu().

# 46.149.2.5 get\_core()

Get the object of type core associated with the id.

#### **Parameters**

```
id The id of the core
```

#### Returns

the core object struct.

# 46.149.2.6 get\_instance()

```
static machine_topology* gko::machine_topology::get_instance ( ) [inline], [static]
```

Returns an instance of the machine\_topology object.

#### Returns

the machine\_topology instance

Referenced by bind\_to\_core(), and bind\_to\_pu().

#### 46.149.2.7 get\_num\_cores()

```
size_type gko::machine_topology::get_num_cores ( ) const [inline]
```

Get the number of core objects stored in this Topology tree.

# Returns

the number of cores.

# 46.149.2.8 get\_num\_numas()

```
size_type gko::machine_topology::get_num_numas ( ) const [inline]
```

Get the number of NUMA objects stored in this Topology tree.

# Returns

the number of NUMA objects.

# 46.149.2.9 get\_num\_pci\_devices()

```
size_type gko::machine_topology::get_num_pci_devices ( ) const [inline]
```

Get the number of PCI device objects stored in this Topology tree.

#### Returns

the number of PCI devices.

# 46.149.2.10 get\_num\_pus()

```
size_type gko::machine_topology::get_num_pus ( ) const [inline]
```

Get the number of PU objects stored in this Topology tree.

#### Returns

the number of PUs.

# 46.149.2.11 get\_pci\_device() [1/2]

Get the object of type pci device associated with the PCI bus id.

# Parameters

pci_bus⊷	The PCI bus id of the pci device
_id	

#### Returns

the PCI object struct.

# 46.149.2.12 get\_pci\_device() [2/2]

Get the object of type pci device associated with the id.

#### **Parameters**

id The id of the pci device

#### Returns

the PCI object struct.

#### 46.149.2.13 get\_pu()

Get the object of type PU associated with the id.

#### **Parameters**

id The id of the PU

#### Returns

the PU object struct.

The documentation for this class was generated from the following file:

• ginkgo/core/base/machine\_topology.hpp

# 46.150 gko::experimental::distributed::Matrix< ValueType, LocalIndexType, GlobalIndexType > Class Template Reference

The Matrix class defines a (MPI-)distributed matrix.

```
#include <ginkgo/core/distributed/matrix.hpp>
```

# **Public Member Functions**

void read\_distributed (const device\_matrix\_data< value\_type, global\_index\_type > &data, std::shared\_ptr<
const Partition< local\_index\_type, global\_index\_type >> partition)

Reads a square matrix from the device\_matrix\_data structure and a global partition.

 void read\_distributed (const matrix\_data< value\_type, global\_index\_type > &data, std::shared\_ptr< const Partition< local\_index\_type, global\_index\_type >> partition)

Reads a square matrix from the matrix\_data structure and a global partition.

void read\_distributed (const device\_matrix\_data< value\_type, global\_index\_type > &data, std::shared\_ptr<
 const Partition< local\_index\_type, global\_index\_type >> row\_partition, std::shared\_ptr< const Partition<
 local\_index\_type, global\_index\_type >> col\_partition)

Reads a matrix from the device\_matrix\_data structure, a global row partition, and a global column partition.

 void read\_distributed (const matrix\_data< value\_type, global\_index\_type > &data, std::shared\_ptr< const Partition< local\_index\_type, global\_index\_type >> row\_partition, std::shared\_ptr< const Partition< local—index\_type, global\_index\_type >> col\_partition)

Reads a matrix from the matrix data structure, a global row partition, and a global column partition.

std::shared\_ptr< const LinOp > get\_local\_matrix () const

Get read access to the stored local matrix.

std::shared\_ptr< const LinOp > get\_non\_local\_matrix () const

Get read access to the stored non-local matrix.

Matrix (const Matrix & other)

Copy constructs a Matrix.

Matrix (Matrix &&other) noexcept

Move constructs a Matrix.

Matrix & operator= (const Matrix & other)

Copy assigns a Matrix.

Matrix & operator= (Matrix &&other)

Move assigns a Matrix.

void col\_scale (ptr\_param< const global\_vector\_type > scaling\_factors)

Scales the columns of the matrix by the respective entries of the vector.

void row\_scale (ptr\_param< const global\_vector\_type > scaling\_factors)

Scales the rows of the matrix by the respective entries of the vector.

#### **Static Public Member Functions**

- static std::unique\_ptr< Matrix > create (std::shared\_ptr< const Executor > exec, mpi::communicator comm)

  Creates an empty distributed matrix.
- template<typename MatrixType , typename = std::enable\_if\_t<detail::is\_matrix\_type\_builder< MatrixType, ValueType, LocalIndex← Type>::value>>

static std::unique\_ptr< Matrix > create (std::shared\_ptr< const Executor > exec, mpi::communicator comm, MatrixType matrix template)

Creates an empty distributed matrix with specified type for local matrices.

• template<typename LocalMatrixType , typename NonLocalMatrixType , typename = std::enable\_if\_t< detail::is\_matrix\_type\_← builder<LocalMatrixType, ValueType, LocalIndexType>::value && detail::is\_matrix\_type\_builder<NonLocalMatrixType, ValueType, LocalIndexType>::value>>

static std::unique\_ptr< Matrix > create (std::shared\_ptr< const Executor > exec, mpi::communicator comm, LocalMatrixType local\_matrix\_template, NonLocalMatrixType non\_local\_matrix\_template)

Creates an empty distributed matrix with specified types for the local matrix and the non-local matrix.

• static std::unique\_ptr< Matrix > create (std::shared\_ptr< const Executor > exec, mpi::communicator comm, ptr\_param< const LinOp > matrix\_template)

Creates an empty distributed matrix with specified type for local matrices.

 static std::unique\_ptr< Matrix > create (std::shared\_ptr< const Executor > exec, mpi::communicator comm, ptr\_param< const LinOp > local\_matrix\_template, ptr\_param< const LinOp > non\_local\_matrix\_template)

Creates an empty distributed matrix with specified types for the local matrix and the non-local matrix.

 static std::unique\_ptr< Matrix > create (std::shared\_ptr< const Executor > exec, mpi::communicator comm, dim< 2 > size, std::shared\_ptr< LinOp > local\_linop)

Creates a local-only distributed matrix with existent LinOp.

static std::unique\_ptr< Matrix > create (std::shared\_ptr< const Executor > exec, mpi::communicator comm, dim< 2 > size, std::shared\_ptr< LinOp > local\_linop, std::shared\_ptr< LinOp > non\_local\_linop, std::shared\_ptr< LinOp > non\_local\_linop, std::vector< comm\_index\_type > recv\_offsets, array< local\_tindex\_type > recv\_gather\_idxs)

Creates distributed matrix with existent local and non-local LinOp and the corresponding mapping to collect the non-local data from the other ranks.

# 46.150.1 Detailed Description

template < typename ValueType = default\_precision, typename LocalIndexType = int32, typename GlobalIndexType = int64 > class gko::experimental::distributed::Matrix < ValueType, LocalIndexType, GlobalIndexType >

The Matrix class defines a (MPI-)distributed matrix.

The matrix is stored in a row-wise distributed format. Each process owns a specific set of rows, where the assignment of rows is defined by a row Partition. The following depicts the distribution of global rows according to their assigned part-id (which will usually be the owning process id):

The local rows are further split into two matrices on each process. One matrix, called local, contains only entries from columns that are also owned by the process, while the other one, called  $non_local$ , contains entries from columns that are not owned by the process. The non-local matrix is stored in a compressed format, where empty columns are discarded and the remaining columns are renumbered. This splitting is depicted in the following:

```
Part-Id Global
                                                   Non-Local
                                          Local
                                                      1
         | 3 4 ! . . . ! . .
0
                                                 3 4 |
                                  . .
         | .. 5 ! 6 .. ! 7 .. | .. . ! ..
                                     | ----> | 6 .. | | 5 7 .. |
9 | ----> | 8 .. | | .. .. 9 |
1
1
2
              .. ! .. 10 ! 11 12 |
                                              | 11 12 | | ...
                                                | 14 .. | | 13 ..
         | 13 .. ! .. .. ! 14 ..
```

This uses the same ownership of the columns as for the rows. Additionally, the ownership of the columns may be explicitly defined with an second column partition. If that is not provided, the same row partition will be used for the columns. Using a column partition also allows to create non-square matrices, like the one below:

```
Part-Id Global
                            Local
                                     Non-Local
P R/P C
         2 2
       | .. 1 2 ..
| 3 4 .. ..
                             | 2 |
                                       | 1
                                       3 4
                             1 .. 1
                    ----|
       j .. 5 6 ..
1
                    | ----> | ..
                                 - 1
                                       | 6 5 |
1
               .. 8 | ----> | 8
                                  | .. ..
       |----|
           .. .. 10 |
                                   .. | | 10 |
       | 13 .. ..
                              | 13 .. | | .. |
```

Here P\_R denotes the row partition and P\_C denotes the column partition.

The Matrix should be filled using the read\_distributed method, e.g.

```
auto part = Partition<...>::build_from_mapping(...);
auto mat = Matrix<...>::create(exec, comm);
mat->read_distributed(matrix_data, part);
```

or if different partitions for the rows and columns are used:

```
auto row_part = Partition<...>::build_from_mapping(...);
auto col_part = Partition<...>::build_from_mapping(...);
auto mat = Matrix<...>::create(exec, comm);
mat->read_distributed(matrix_data, row_part, col_part);
```

This will set the dimensions of the global and local matrices automatically by deducing the sizes from the partitions.

By default the Matrix type uses Csr for both stored matrices. It is possible to explicitly change the datatype for the stored matrices, with the constraint that the new type should implement the LinOp and ReadableFromMatrixData interface. The type can be set by:

```
auto mat = Matrix<ValueType, LocalIndexType[, ...]>::create(
  exec, comm,
  Ell<ValueType, LocalIndexType>::create(exec).get(),
  Coo<ValueType, LocalIndexType>::create(exec).get());
```

Alternatively, the helper function with\_matrix\_type can be used:

```
auto mat = Matrix<ValueType, LocalIndexType>::create(
  exec, comm,
  with_matrix_type<Ell>(),
  with_matrix_type<Coo>());
```

See also

with\_matrix\_type

# The Matrix LinOp supports the following operations:

```
experimental::distributed::Matrix *A;  // distributed matrix experimental::distributed::Vector *b, *x;  // distributed multi-vectors matrix::Dense *alpha, *beta;  // scalars of dimension 1x1  // Applying to distributed multi-vectors computes an SpMV/SpMM product A->apply(b, x)  // x = A*b A->apply(alpha, b, beta, x) // x = alpha*A*b + beta*x
```

#### **Template Parameters**

ValueType	The underlying value type.
LocalIndexType	The index type used by the local matrices.
GlobalIndexType	The type for global indices.

## 46.150.2 Constructor & Destructor Documentation

# 46.150.2.1 Matrix() [1/2]

Copy constructs a Matrix.

#### **Parameters**

other	Matrix to copy from.
-------	----------------------

# 46.150.2.2 Matrix() [2/2]

Move constructs a Matrix.

#### **Parameters**

- 41	Manufacture and account for a second
otner	Matrix to move from.

#### 46.150.3 Member Function Documentation

# 46.150.3.1 col\_scale()

Scales the columns of the matrix by the respective entries of the vector.

The vector's row partition has to be the same as the matrix's column partition. The scaling is done in-place.

#### **Parameters**

g_factors The vector containing the scaling factors.
--

#### 46.150.3.2 create() [1/7]

Creates an empty distributed matrix.

#### **Parameters**

exec	Executor associated with this matrix.
comm	Communicator associated with this matrix. The default is the MPI_COMM_WORLD.

# Returns

A smart pointer to the newly created matrix.

Referenced by gko::experimental::distributed::Matrix < ValueType, LocalIndexType, GlobalIndexType >::create().

## 46.150.3.3 create() [2/7]

```
template<typename ValueType = default_precision, typename LocalIndexType = int32, typename
GlobalIndexType = int64>
```

Creates a local-only distributed matrix with existent LinOp.

#### Note

It use the input to build up the distributed matrix

#### **Parameters**

exec	Executor associated with this matrix.
comm	Communicator associated with this matrix.
size	the global size
local_linop	the local linop

#### Returns

A smart pointer to the newly created matrix.

#### 46.150.3.4 create() [3/7]

Creates distributed matrix with existent local and non-local LinOp and the corresponding mapping to collect the non-local data from the other ranks.

#### Note

It use the input to build up the distributed matrix

### **Parameters**

exec	Executor associated with this matrix.
comm	Communicator associated with this matrix.
size	the global size

#### **Parameters**

local_linop	the local linop
non_local_linop	the non-local linop
recv_sizes	the size of non-local receiver
recv_offset	the offset of non-local receiver
recv_gather_idxs	the gathering index of non-local receiver

#### Returns

A smart pointer to the newly created matrix.

#### 46.150.3.5 create() [4/7]

Creates an empty distributed matrix with specified types for the local matrix and the non-local matrix.

# Note

This is mainly a convenience wrapper for Matrix(std::shared\_ptr<const Executor>, mpi::communicator, const LinOp\*, const LinOp\*)

# **Template Parameters**

LocalMatrixType	A type that has a create <valuetype, indextype="">(exec) function to create a</valuetype,>
	smart pointer of a type derived from LinOp and ReadableFromMatrixData.

## See also

with\_matrix\_type

#### **Template Parameters**

NonLocalMatrixType	A (possible different) type with the same constraints as LocalMatrixType.
--------------------	---

#### **Parameters**

exec	Executor associated with this matrix.
comm	Communicator associated with this matrix.
local_matrix_template	the local matrix will be constructed with the same type as create returns. It should be the return value of make_matrix_template.
non_local_matrix_template	the non-local matrix will be constructed with the same type as create returns. It should be the return value of make_matrix_template.

### Returns

A smart pointer to the newly created matrix.

References gko::experimental::distributed::Matrix< ValueType, LocalIndexType, GlobalIndexType >::create().

# 46.150.3.6 create() [5/7]

Creates an empty distributed matrix with specified type for local matrices.

#### Note

This is mainly a convenience wrapper for Matrix(std::shared\_ptr<const Executor>, mpi::communicator, const LinOp\*)

# **Template Parameters**

MatrixType	A type that has a create <valuetype, indextype="">(exec) function to create a smart</valuetype,>	
	pointer of a type derived from LinOp and ReadableFromMatrixData.	

## See also

with\_matrix\_type

# **Parameters**

exec	Executor associated with this matrix.
comm	Communicator associated with this matrix.
matrix_template	the local matrices will be constructed with the same type as create returns. It should be the return value of make_matrix_template.

#### Returns

A smart pointer to the newly created matrix.

References gko::experimental::distributed::Matrix< ValueType, LocalIndexType, GlobalIndexType >::create().

# 46.150.3.7 create() [6/7]

Creates an empty distributed matrix with specified types for the local matrix and the non-local matrix.

#### Note

It internally clones the passed in local\_matrix\_template and non\_local\_matrix\_template. Therefore, those LinOps should be empty.

## **Parameters**

exec	Executor associated with this matrix.
comm	Communicator associated with this matrix.
local_matrix_template	the local matrix will be constructed with the same runtime type.
non_local_matrix_template	the non-local matrix will be constructed with the same runtime type.

#### Returns

A smart pointer to the newly created matrix.

## 46.150.3.8 create() [7/7]

Creates an empty distributed matrix with specified type for local matrices.

# Note

It internally clones the passed in matrix template. Therefore, the LinOp should be empty.

#### **Parameters**

exec	Executor associated with this matrix.
comm	Communicator associated with this matrix.
matrix_template	the local matrices will be constructed with the same runtime type.

#### Returns

A smart pointer to the newly created matrix.

#### 46.150.3.9 get\_local\_matrix()

```
template<typename ValueType = default_precision, typename LocalIndexType = int32, typename
GlobalIndexType = int64>
std::shared_ptr<const LinOp> gko::experimental::distributed::Matrix< ValueType, LocalIndex
Type, GlobalIndexType >::get_local_matrix ( ) const [inline]
```

Get read access to the stored local matrix.

#### Returns

Shared pointer to the stored local matrix

# 46.150.3.10 get\_non\_local\_matrix()

```
template<typename ValueType = default_precision, typename LocalIndexType = int32, typename
GlobalIndexType = int64>
std::shared_ptr<const LinOp> gko::experimental::distributed::Matrix< ValueType, LocalIndex
Type, GlobalIndexType >::get_non_local_matrix ( ) const [inline]
```

Get read access to the stored non-local matrix.

#### Returns

Shared pointer to the stored non-local matrix

# 46.150.3.11 operator=() [1/2]

Copy assigns a Matrix.

#### **Parameters**

other Matrix to copy from, has to have a communicator of the same size as this.

Returns

this.

## 46.150.3.12 operator=() [2/2]

Move assigns a Matrix.

#### **Parameters**

other | Matrix to move from, has to have a communicator of the same size as this.

## Returns

this.

#### 46.150.3.13 read\_distributed() [1/4]

Reads a square matrix from the device\_matrix\_data structure and a global partition.

The global size of the final matrix is inferred from the size of the partition. Both the number of rows and columns of the device\_matrix\_data are ignored.

#### Note

The matrix data can contain entries for rows other than those owned by the process. Entries for those rows are discarded.

#### **Parameters**

data	The device_matrix_data structure.
partition	The global row and column partition.

#### Returns

the index\_map induced by the partitions and the matrix structure

## 46.150.3.14 read\_distributed() [2/4]

Reads a matrix from the device\_matrix\_data structure, a global row partition, and a global column partition.

The global size of the final matrix is inferred from the size of the row partition and the size of the column partition. Both the number of rows and columns of the device matrix data are ignored.

# Note

The matrix data can contain entries for rows other than those owned by the process. Entries for those rows are discarded.

#### **Parameters**

data	The device_matrix_data structure.
row_partition	The global row partition.
col_partition	The global col partition.

## Returns

the index\_map induced by the partitions and the matrix structure

# 46.150.3.15 read\_distributed() [3/4]

```
template<typename ValueType = default_precision, typename LocalIndexType = int32, typename
GlobalIndexType = int64>
```

Reads a square matrix from the matrix\_data structure and a global partition.

See also

read distributed

Note

For efficiency it is advised to use the device matrix data overload.

#### 46.150.3.16 read distributed() [4/4]

Reads a matrix from the matrix\_data structure, a global row partition, and a global column partition.

See also

read distributed

Note

For efficiency it is advised to use the <a href="device\_matrix\_data">device\_matrix\_data</a> overload.

# 46.150.3.17 row\_scale()

Scales the rows of the matrix by the respective entries of the vector.

The vector and the matrix have to have the same row partition. The scaling is done in-place.

#### **Parameters**

scaling_factors   The vector containing the scaling factors.
--

The documentation for this class was generated from the following file:

· ginkgo/core/distributed/matrix.hpp

# 46.151 gko::matrix\_assembly\_data< ValueType, IndexType > Class Template Reference

This structure is used as an intermediate type to assemble a sparse matrix.

#include <ginkgo/core/base/matrix\_assembly\_data.hpp>

#### **Public Member Functions**

- void add\_value (index\_type row, index\_type col, value\_type val)
   Sets the matrix value at (row, col).
- void set\_value (index\_type row, index\_type col, value\_type val)

  Sets the matrix value at (row, col).
- value\_type get\_value (index\_type row, index\_type col)
   Gets the matrix value at (row, col).
- bool contains (index\_type row, index\_type col)

Returns true iff the matrix contains an entry at (row, col).

- dim< 2 > get\_size () const noexcept
- size\_type get\_num\_stored\_elements () const noexcept
- matrix\_data< ValueType, IndexType > get\_ordered\_data () const

# 46.151.1 Detailed Description

template<typename ValueType = default\_precision, typename IndexType = int32> class gko::matrix\_assembly\_data< ValueType, IndexType >

This structure is used as an intermediate type to assemble a sparse matrix.

The matrix is stored as a set of nonzero elements, where each element is a triplet of the form (row\_index, column 
\_index, value).

New values can be added by using the matrix\_assembly\_data::add\_value or matrix\_assembly\_data::set\_value

# **Template Parameters**

ValueType	type of matrix values stored in the structure
IndexType	type of matrix indexes stored in the structure

# 46.151.2 Member Function Documentation

# 46.151.2.1 add\_value()

Sets the matrix value at (row, col).

If there is an existing value, it will be set to the sum of the existing and new value, otherwise the value will be inserted.

#### **Parameters**

row	the row where the value should be added
col	the column where the value should be added
val	the value to be added to (row, col)

```
79 {
80      auto ind = std::make_pair(row, col);
81      nonzeros_[ind] += val;
82 }
```

# 46.151.2.2 contains()

Returns true iff the matrix contains an entry at (row, col).

# Parameters

row	the row index	
col	the column index	

#### Returns

true if the value at (row, col) exists, false otherwise

#### 46.151.2.3 get\_num\_stored\_elements()

```
template<typename ValueType = default_precision, typename IndexType = int32>
size_type gko::matrix_assembly_data< ValueType, IndexType >::get_num_stored_elements ( ) const
[inline], [noexcept]
```

#### Returns

the number of non-zeros in the (partially) assembled matrix

## 46.151.2.4 get\_ordered\_data()

```
template<typename ValueType = default_precision, typename IndexType = int32>
matrix_data<ValueType, IndexType> gko::matrix_assembly_data< ValueType, IndexType >::get_←
ordered_data ( ) const [inline]
```

#### Returns

a matrix\_data instance containing the assembled non-zeros in row-major order to be used by all matrix formats.

Referenced by gko::ReadableFromMatrixData< ValueType, int32 >::read().

## 46.151.2.5 get\_size()

```
template<typename ValueType = default_precision, typename IndexType = int32>
dim<2> gko::matrix_assembly_data< ValueType, IndexType >::get_size ( ) const [inline], [noexcept]
```

#### Returns

the dimensions of the matrix being assembled

#### 46.151.2.6 get value()

Gets the matrix value at (row, col).

#### **Parameters**

row the row index	
col	the column index

#### Returns

the value at (row, col) or 0 if it doesn't exist.

# 46.151.2.7 set\_value()

Sets the matrix value at (row, col).

If there is an existing value, it will be overwritten by the new value.

#### **Parameters**

row	the row index
col	the column index
val	the value to be written to (row, col)

The documentation for this class was generated from the following file:

• ginkgo/core/base/matrix\_assembly\_data.hpp

# 46.152 gko::matrix\_data< ValueType, IndexType > Struct Template Reference

This structure is used as an intermediate data type to store a sparse matrix.

```
#include <ginkgo/core/base/matrix_data.hpp>
```

#### **Public Member Functions**

- matrix\_data (dim< 2 > size\_=dim< 2 >{}, ValueType value=zero< ValueType >())
   Initializes a matrix filled with the specified value.
- template<typename RandomDistribution, typename RandomEngine >
   matrix\_data (dim< 2 > size\_, RandomDistribution &&dist, RandomEngine &&engine)
   Initializes a matrix with random values from the specified distribution.

matrix\_data (std::initializer\_list< std::initializer\_list< ValueType >> values)

List-initializes the structure from a matrix of values.

Initializes the structure from a list of nonzeros.

matrix\_data (dim< 2 > size\_, const matrix\_data &block)

Initializes a matrix out of a matrix block via duplication.

• template<typename Accessor >

matrix\_data (const range< Accessor > &data)

Initializes a matrix from a range.

void sort row major ()

Sorts the nonzero vector so the values follow row-major order.

void ensure\_row\_major\_order ()

Sorts the nonzero vector so the values follow row-major order.

• void remove zeros ()

Remove entries with value zero from the matrix data.

• void sum\_duplicates ()

Sum up all values that refer to the same matrix entry.

#### **Static Public Member Functions**

static matrix\_data diag (dim< 2 > size\_, ValueType value)

Initializes a diagonal matrix.

static matrix\_data diag (dim< 2 > size\_, std::initializer\_list< ValueType > nonzeros\_)

Initializes a diagonal matrix using a list of diagonal elements.

static matrix\_data diag (dim< 2 > size\_, const matrix\_data &block)

Initializes a block-diagonal matrix.

 $\bullet \ \ \text{template}{<} \text{typename ForwardIterator} >$ 

static matrix\_data diag (ForwardIterator begin, ForwardIterator end)

Initializes a block-diagonal matrix from a list of diagonal blocks.

static matrix\_data diag (std::initializer\_list< matrix\_data > blocks)

Initializes a block-diagonal matrix from a list of diagonal blocks.

template<typename RandomDistribution, typename RandomEngine >
 static matrix\_data cond (size\_type size, remove\_complex< ValueType > condition\_number, Random
 Distribution &&dist, RandomEngine &&engine, size\_type num\_reflectors)

Initializes a random dense matrix with a specific condition number.

template<typename RandomDistribution, typename RandomEngine >
 static matrix\_data cond (size\_type size, remove\_complex< ValueType > condition\_number, Random
 Distribution &&dist, RandomEngine &&engine)

Initializes a random dense matrix with a specific condition number.

# **Public Attributes**

dim< 2 > size

Size of the matrix.

• std::vector< nonzero\_type > nonzeros

A vector of tuples storing the non-zeros of the matrix.

# 46.152.1 Detailed Description

template<typename ValueType = default\_precision, typename IndexType = int32> struct gko::matrix\_data< ValueType, IndexType >

This structure is used as an intermediate data type to store a sparse matrix.

The matrix is stored as a sequence of nonzero elements, where each element is a triple of the form (row\_index, column\_index, value).

#### Note

All Ginkgo functions returning such a structure will return the nonzeros sorted in row-major order.

All Ginkgo functions that take this structure as input expect that the nonzeros are sorted in row-major order and that the index pair (row\_index, column\_index) of each nonzero is unique.

This structure is not optimized for usual access patterns and it can only exist on the CPU. Thus, it should only be used for utility functions which do not have to be optimized for performance.

### **Template Parameters**

ValueType	type of matrix values stored in the structure
IndexType	type of matrix indexes stored in the structure

# 46.152.2 Constructor & Destructor Documentation

# 46.152.2.1 matrix\_data() [1/6]

Initializes a matrix filled with the specified value.

#### **Parameters**

<i>size</i> ⊷ –	dimensions of the matrix
value	value used to fill the elements of the matrix

```
148 }
149 }
```

# 46.152.2.2 matrix\_data() [2/6]

Initializes a matrix with random values from the specified distribution.

# **Template Parameters**

RandomDistribution	random distribution type
RandomEngine	random engine type

#### **Parameters**

size⊷	dimensions of the matrix	
_		
dist	random distribution of the elements of the matrix	
engine	random engine used to generate random values	

## 46.152.2.3 matrix\_data() [3/6]

List-initializes the structure from a matrix of values.

## **Parameters**

```
values a 2D braced-init-list of matrix values.
```

### 46.152.2.4 matrix\_data() [4/6]

```
template<typename ValueType = default_precision, typename IndexType = int32>
gko::matrix_data< ValueType, IndexType >::matrix_data (
```

Initializes the structure from a list of nonzeros.

#### **Parameters**

size_	dimensions of the matrix
nonzeros⇔	list of nonzero elements
_	

# 46.152.2.5 matrix\_data() [5/6]

Initializes a matrix out of a matrix block via duplication.

#### **Parameters**

size	size of the block-matrix (in blocks)
diag_block	matrix block used to fill the complete matrix

# 46.152.2.6 matrix\_data() [6/6]

Initializes a matrix from a range.

# **Template Parameters**

Accessor   accessor type of the input range	Accessor
---	----------

#### **Parameters**

data	range used to initialize the matrix
------	-------------------------------------

References gko::range < Accessor >::length().

# 46.152.3 Member Function Documentation

# 46.152.3.1 cond() [1/2]

Initializes a random dense matrix with a specific condition number.

The matrix is generated by applying a series of random Hausholder reflectors to a diagonal matrix with diagonal entries uniformly distributed between sqrt (condition\_number) and 1/sqrt (condition\_number).

This version of the function applies size - 1 reflectors to each side of the diagonal matrix.

#### **Template Parameters**

RandomDistribution	the type of the random distribution
RandomEngine	the type of the random engine

# Parameters

size	number of rows and columns of the matrix
condition_number	condition number of the matrix
dist	random distribution used to generate reflectors
engine	random engine used to generate reflectors

## Returns

the dense matrix with the specified condition number

References gko::matrix\_data < ValueType, IndexType >::cond(), and gko::matrix\_data < ValueType, IndexType > ∴ ::size.

# 46.152.3.2 cond() [2/2]

```
template<typename ValueType = default_precision, typename IndexType = int32>
template<typename RandomDistribution , typename RandomEngine >
```

Initializes a random dense matrix with a specific condition number.

The matrix is generated by applying a series of random Hausholder reflectors to a diagonal matrix with diagonal entries uniformly distributed between sqrt (condition\_number) and 1/sqrt (condition\_number).

#### **Template Parameters**

RandomDistribution	the type of the random distribution
RandomEngine	the type of the random engine

## **Parameters**

size	number of rows and columns of the matrix
condition_number	condition number of the matrix
dist	random distribution used to generate reflectors
engine	random engine used to generate reflectors
num_reflectors	number of reflectors to apply from each side

# Returns

the dense matrix with the specified condition number

References gko::matrix\_data< ValueType, IndexType >::size.

Referenced by gko::matrix\_data < ValueType, IndexType >::cond().

# 46.152.3.3 diag() [1/5]

Initializes a block-diagonal matrix.

size_	the size of the matrix
diag_block	matrix used to fill diagonal blocks

#### Returns

the block-diagonal matrix

References gko::matrix\_data< ValueType, IndexType >::nonzeros, and gko::matrix\_data< ValueType, IndexType >::size.

## 46.152.3.4 diag() [2/5]

Initializes a diagonal matrix using a list of diagonal elements.

#### **Parameters**

size_	dimensions of the matrix
nonzeros⊷	list of diagonal elements
_	

# Returns

the diagonal matrix

References gko::matrix\_data< ValueType, IndexType >::nonzeros.

# 46.152.3.5 diag() [3/5]

Initializes a diagonal matrix.

#### **Parameters**

size⊷	dimensions of the matrix
value	value used to fill the elements of the matrix

# Returns

the diagonal matrix

References gko::is\_nonzero(), and gko::matrix\_data< ValueType, IndexType >::nonzeros.

Referenced by gko::matrix\_data< ValueType, IndexType >::diag().

## 46.152.3.6 diag() [4/5]

Initializes a block-diagonal matrix from a list of diagonal blocks.

## **Template Parameters**

ForwardIterator	type of list iterator
-----------------	-----------------------

#### **Parameters**

begin	the first iterator of the list
end	the last iterator of the list

# Returns

the block-diagonal matrix with diagonal blocks set to the blocks between begin (inclusive) and end (exclusive)

References gko::matrix\_data< ValueType, IndexType >::nonzeros.

# 46.152.3.7 diag() [5/5]

Initializes a block-diagonal matrix from a list of diagonal blocks.

# **Parameters**

blocks	a list of blocks to initialize from
--------	-------------------------------------

## Returns

the block-diagonal matrix with diagonal blocks set to the blocks passed in blocks

References gko::matrix\_data< ValueType, IndexType >::diag().

## 46.152.3.8 sum\_duplicates()

```
template<typename ValueType = default_precision, typename IndexType = int32>
void gko::matrix_data< ValueType, IndexType >::sum_duplicates () [inline]
```

Sum up all values that refer to the same matrix entry.

The result is sorted in row-major order.

References gko::matrix\_data< ValueType, IndexType >::nonzeros, and gko::matrix\_data< ValueType, IndexType >::sort\_row\_major().

#### 46.152.4 Member Data Documentation

# 46.152.4.1 nonzeros

```
template<typename ValueType = default_precision, typename IndexType = int32>
std::vector<nonzero_type> gko::matrix_data< ValueType, IndexType >::nonzeros
```

A vector of tuples storing the non-zeros of the matrix.

The first two elements of the tuple are the row index and the column index of a matrix element, and its third element is the value at that position.

Referenced by gko::matrix\_data < ValueType, IndexType >::diag(), gko::matrix\_data < ValueType, IndexType >::remove\_zeros(), gko::matrix\_data < ValueType, IndexType >::sort\_row\_major(), and gko::matrix\_data < Value  $\leftarrow$  Type, IndexType >::sum\_duplicates().

The documentation for this struct was generated from the following file:

ginkgo/core/base/matrix\_data.hpp

# 46.153 gko::matrix\_data\_entry< ValueType, IndexType > Struct Template Reference

Type used to store nonzeros.

#include <ginkgo/core/base/matrix\_data.hpp>

# 46.153.1 Detailed Description

template<typename ValueType, typename IndexType>
struct gko::matrix\_data\_entry< ValueType, IndexType>

Type used to store nonzeros.

The documentation for this struct was generated from the following file:

• ginkgo/core/base/matrix\_data.hpp

# 46.154 gko::experimental::reorder::Mc64< ValueType, IndexType > Class Template Reference

MC64 is an algorithm for permuting large entries to the diagonal of a sparse matrix.

```
#include <ginkgo/core/reorder/mc64.hpp>
```

### **Public Member Functions**

- const parameters\_type & get\_parameters () const
   Returns the parameters used to construct the factory.
- $\bullet \ \, \text{std::unique\_ptr} < \overline{\text{result\_type}} > \underline{\text{generate}} \ \, (\text{std::shared\_ptr} < \overline{\text{const LinOp}} > \underline{\text{system\_matrix}}) \ \, \overline{\text{const LinOp}} > \underline{\text{const LinOp}} > \underline{\text$

#### Static Public Member Functions

static parameters\_type build ()
 Creates a new parameter\_type to set up the factory.

# 46.154.1 Detailed Description

template<typename ValueType = default\_precision, typename IndexType = int32> class gko::experimental::reorder::Mc64< ValueType, IndexType >

MC64 is an algorithm for permuting large entries to the diagonal of a sparse matrix.

This approach can increase numerical stability of e.g. an LU factorization without pivoting. Under the assumption of working on a nonsingular square matrix, the algorithm computes a minimum weight perfect matching on a weighted edge bipartite graph of the matrix. It is described in detail in "On Algorithms for Permuting Large Entries to the Diagonal of a Sparse Matrix" (Duff, Koster, 2001, DOI: 10.1137/S0895479899358443). There are two strategies for choosing the weights supported:

- Maximizing the product of the absolute values on the diagonal. For this strategy, the weights are computed as  $c(i,j) = \log_2(a_i) \log_2(|a(i,j)|)$  if  $a(i,j) \neq 0$  and  $c(i,j) = \infty$  otherwise. Here, a\_i is the maximum absolute value in row i of the matrix A. In this case, the implementation computes a row permutation P and row and column scaling coefficients L and R such that the matrix P\*L\*A\*R has values with unity absolute value on the diagonal and smaller or equal entries everywhere else.
- Maximizing the sum of the absolute values on the diagonal. For this strategy, the weights are computed as  $c(i,j)=a_i-|a(i,j)|$  if  $a(i,j)\neq 0$  and  $c(i,j)=\infty$  otherwise. In this case, no scaling coefficients are computed.

This class creates a Combination of two ScaledPermutations representing the row and column permutation and scaling factors computed by this algorithm.

## **Template Parameters**

ValueType	Type of the values of all matrices used in this class
IndexType	Type of the indices of all matrices used in this class

# 46.154.2 Member Function Documentation

#### 46.154.2.1 generate()

#### Note

This function overrides the default LinOpFactory::generate to return a Permutation instead of a generic LinOp, which would need to be cast to ScaledPermutation again to access its indices. It is only necessary because smart pointers aren't covariant.

## 46.154.2.2 get\_parameters()

```
template<typename ValueType = default_precision, typename IndexType = int32>
const parameters_type& gko::experimental::reorder::Mc64< ValueType, IndexType >::get_parameters
( ) const [inline]
```

Returns the parameters used to construct the factory.

## Returns

the parameters used to construct the factory.

The documentation for this class was generated from the following file:

• ginkgo/core/reorder/mc64.hpp

# 46.155 gko::matrix::Csr< ValueType, IndexType >::merge\_path Class Reference

merge\_path is a strategy\_type which uses the merge\_path algorithm.

#include <ginkgo/core/matrix/csr.hpp>

## **Public Member Functions**

• merge\_path ()

Creates a merge\_path strategy.

void process (const array < index\_type > &mtx\_row\_ptrs, array < index\_type > \*mtx\_srow) override
 Computes srow according to row pointers.

• int64\_t clac\_size (const int64\_t nnz) override

Computes the srow size according to the number of nonzeros.

 std::shared\_ptr< strategy\_type > copy () override Copy a strategy.

# 46.155.1 Detailed Description

```
template<typename ValueType = default_precision, typename IndexType = int32> class gko::matrix::Csr< ValueType, IndexType >::merge_path
```

merge\_path is a strategy\_type which uses the merge\_path algorithm.

merge\_path is according to Merrill and Garland: Merge-Based Parallel Sparse Matrix-Vector Multiplication

### 46.155.2 Member Function Documentation

## 46.155.2.1 clac size()

Computes the srow size according to the number of nonzeros.

# **Parameters**

```
nnz the number of nonzeros
```

# Returns

the size of srow

Implements gko::matrix::Csr< ValueType, IndexType >::strategy type.

### 46.155.2.2 copy()

```
template<typename ValueType = default_precision, typename IndexType = int32>
std::shared_ptr<strategy_type> gko::matrix::Csr< ValueType, IndexType >::merge_path::copy ( )
[inline], [override], [virtual]
```

Copy a strategy.

This is a workaround until strategies are revamped, since strategies like automatical do not work when actually shared.

Implements gko::matrix::Csr< ValueType, IndexType >::strategy\_type.

#### 46.155.2.3 process()

Computes srow according to row pointers.

#### **Parameters**

mtx_row_ptrs	the row pointers of the matrix
mtx_srow	the srow of the matrix

Implements gko::matrix::Csr< ValueType, IndexType >::strategy\_type.

The documentation for this class was generated from the following file:

· ginkgo/core/matrix/csr.hpp

# 46.156 gko::MetisError Class Reference

MetisError is thrown when METIS routine throws an error code.

```
#include <ginkgo/core/base/exception.hpp>
```

## **Public Member Functions**

MetisError (const std::string &file, int line, const std::string &func, const std::string &error)
 Initializes a METIS error.

# 46.156.1 Detailed Description

MetisError is thrown when METIS routine throws an error code.

# 46.156.2 Constructor & Destructor Documentation

# 46.156.2.1 MetisError()

Initializes a METIS error.

## **Parameters**

file	The name of the offending source file	
line	The source code line number where the error occurred	
func	The name of the METIS routine that failed	
error	The resulting METIS error name	

The documentation for this class was generated from the following file:

· ginkgo/core/base/exception.hpp

# 46.157 gko::matrix::Hybrid< ValueType, IndexType >::minimal\_storage\_limit Class Reference

minimal\_storage\_limit is a strategy\_type which decides the number of stored elements per row of the ell part.

```
#include <ginkgo/core/matrix/hybrid.hpp>
```

# **Public Member Functions**

- minimal\_storage\_limit ()
   Creates a minimal\_storage\_limit strategy.
- size\_type compute\_ell\_num\_stored\_elements\_per\_row (array< size\_type > \*row\_nnz) const override
   Computes the number of stored elements per row of the ell part.
- auto get\_percentage () const

Get the percent setting.

# 46.157.1 Detailed Description

```
template<typename ValueType = default_precision, typename IndexType = int32> class gko::matrix::Hybrid< ValueType, IndexType >::minimal_storage_limit
```

minimal\_storage\_limit is a strategy\_type which decides the number of stored elements per row of the ell part.

It is determined by the size of ValueType and IndexType, the storage is the minimum among all partition.

## 46.157.2 Member Function Documentation

# 46.157.2.1 compute\_ell\_num\_stored\_elements\_per\_row()

```
template<typename ValueType = default_precision, typename IndexType = int32> size_type gko::matrix::Hybrid< ValueType, IndexType >::minimal_storage_limit::compute_ell_← num_stored_elements_per_row (

array< size_type > * row_nnz ) const [inline], [override], [virtual]
```

Computes the number of stored elements per row of the ell part.

#### **Parameters**

row_nnz	the number of nonzeros of each row
---------	------------------------------------

#### Returns

the number of stored elements per row of the ell part

Implements gko::matrix::Hybrid< ValueType, IndexType >::strategy\_type.

References gko::matrix::Hybrid< ValueType, IndexType >::imbalance\_limit::compute\_ell\_num\_stored\_elements ← \_per\_row().

# 46.157.2.2 get\_percentage()

```
template<typename ValueType = default_precision, typename IndexType = int32>
auto gko::matrix::Hybrid< ValueType, IndexType >::minimal_storage_limit::get_percentage ( )
const [inline]
```

Get the percent setting.

# Returns

percent

References gko::matrix::Hybrid < ValueType, IndexType >::imbalance limit::get percentage().

The documentation for this class was generated from the following file:

ginkgo/core/matrix/hybrid.hpp

# 46.158 gko::MpiError Class Reference

MpiError is thrown when a MPI routine throws a non-zero error code.

#include <ginkgo/core/base/exception.hpp>

# **Public Member Functions**

MpiError (const std::string &file, int line, const std::string &func, int64 error\_code)
 Initializes a MPI error.

# 46.158.1 Detailed Description

MpiError is thrown when a MPI routine throws a non-zero error code.

## 46.158.2 Constructor & Destructor Documentation

# 46.158.2.1 MpiError()

Initializes a MPI error.

# **Parameters**

file	The name of the offending source file
line	The source code line number where the error occurred
func	The name of the MPI routine that failed
error_code	The resulting MPI error code

The documentation for this class was generated from the following file:

· ginkgo/core/base/exception.hpp

# 46.159 gko::solver::Multigrid Class Reference

Multigrid methods have a hierarchy of many levels, whose corase level is a subset of the fine level, of the problem.

```
#include <ginkgo/core/solver/multigrid.hpp>
```

# **Public Member Functions**

- · bool apply\_uses\_initial\_guess () const override
  - Return true as iterative solvers use the data in x as an initial guess or false if multigrid always set the input as zero.
- $\bullet \ \, \text{std::vector} < \text{std::shared\_ptr} < \text{const gko::multigrid::} \\ \text{MultigridLevel} >> \text{get\_mg\_level\_list () const} \\$

Gets the list of MultigridLevel operators.

- std::vector< std::shared\_ptr< const LinOp >> get\_pre\_smoother\_list () const
  - Gets the list of pre-smoother operators.
- std::vector< std::shared\_ptr< const LinOp >> get\_mid\_smoother\_list () const
  - Gets the list of mid-smoother operators.
- std::vector< std::shared\_ptr< const LinOp > > get\_post\_smoother\_list () const
  - Gets the list of post-smoother operators.
- std::shared\_ptr< const LinOp > get\_coarsest\_solver () const
  - Gets the operator at the coarsest level.
- multigrid::cycle get\_cycle () const
  - Get the cycle of multigrid.
- void set\_cycle (multigrid::cycle cycle)
  - Set the cycle of multigrid.

## **Static Public Member Functions**

• static parameters\_type parse (const config::pnode &config, const config::registry &context, const config::type\_descriptor &td\_for\_child=config::make\_type\_descriptor<>())

Create the parameters from the property tree.

# 46.159.1 Detailed Description

Multigrid methods have a hierarchy of many levels, whose corase level is a subset of the fine level, of the problem.

The coarse level solves the system on the residual of fine level and fine level will use the coarse solution to correct its own result. Multigrid solves the problem by relatively cheap step in each level and refining the result when prolongating back.

The main step of each level

- · Presmooth (solve on the fine level)
- · Calculate residual
- Restrict (reduce the problem dimension)
- · Solve residual in next level
- · Prolongate (return to the fine level size)
- Postsmooth (correct the answer in fine level)

Ginkgo uses the index from 0 for finest level (original problem size)  $\sim$  N for the coarsest level (the coarsest solver), and its level counts is N (N multigrid level generation).

# 46.159.2 Member Function Documentation

## 46.159.2.1 apply\_uses\_initial\_guess()

```
bool gko::solver::Multigrid::apply_uses_initial_guess ( ) const [inline], [override]
```

Return true as iterative solvers use the data in x as an initial guess or false if multigrid always set the input as zero.

Returns

bool it is related to parameters variable zero\_guess

References gko::solver::provided.

## 46.159.2.2 get\_coarsest\_solver()

```
std::shared_ptr<const LinOp> gko::solver::Multigrid::get_coarsest_solver ( ) const [inline]
```

Gets the operator at the coarsest level.

Returns

the coarsest operator

# 46.159.2.3 get\_cycle()

```
multigrid::cycle gko::solver::Multigrid::get_cycle ( ) const [inline]
```

Get the cycle of multigrid.

Returns

the multigrid::cycle

# 46.159.2.4 get\_mg\_level\_list()

```
std::vector < std::shared_ptr < const gko::multigrid::MultigridLevel >> gko::solver::Multigrid \\ ::get_mg_level_list ( ) const [inline]
```

Gets the list of MultigridLevel operators.

Returns

the list of MultigridLevel operators

# 46.159.2.5 get\_mid\_smoother\_list()

```
std::vector<std::shared_ptr<const LinOp> > gko::solver::Multigrid::get_mid_smoother_list ( )
const [inline]
```

Gets the list of mid-smoother operators.

#### Returns

the list of mid-smoother operators

## 46.159.2.6 get\_post\_smoother\_list()

```
std::vector<std::shared_ptr<const LinOp> > gko::solver::Multigrid::get_post_smoother_list ( )
const [inline]
```

Gets the list of post-smoother operators.

#### Returns

the list of post-smoother operators

# 46.159.2.7 get\_pre\_smoother\_list()

```
std::vector<std::shared_ptr<const LinOp> > gko::solver::Multigrid::get_pre_smoother_list ( )
const [inline]
```

Gets the list of pre-smoother operators.

# Returns

the list of pre-smoother operators

# 46.159.2.8 parse()

Create the parameters from the property\_tree.

Because this is directly tied to the specific type, the value/index type settings within config are ignored and type\_ descriptor is only used for children configs.

#### **Parameters**

config	the property tree for setting
context	the registry
td_for_child	the type descriptor for children configs

## **Returns**

parameters

#### Note

Multigrid does not support the selector option in file config

# 46.159.2.9 set\_cycle()

Set the cycle of multigrid.

## **Parameters**

multigrid::cycle	the new cycle
------------------	---------------

The documentation for this class was generated from the following file:

• ginkgo/core/solver/multigrid.hpp

# 46.160 gko::multigrid::MultigridLevel Class Reference

This class represents two levels in a multigrid hierarchy.

```
#include <ginkgo/core/multigrid/multigrid_level.hpp>
```

## **Public Member Functions**

- virtual std::shared\_ptr< const LinOp > get\_fine\_op () const =0
   Returns the operator on fine level.
- virtual std::shared\_ptr< const LinOp > get\_restrict\_op () const =0
   Returns the restrict operator.
- virtual std::shared\_ptr< const LinOp > get\_coarse\_op () const =0
   Returns the operator on coarse level.
- virtual std::shared\_ptr< const LinOp > get\_prolong\_op () const =0
   Returns the prolong operator.

# 46.160.1 Detailed Description

This class represents two levels in a multigrid hierarchy.

The MultigridLevel is an interface that allows to get the individual components of multigrid level. Each implementation of a multigrid level should inherit from this interface. Use EnableMultigridLevel<ValueType> to implement this interface with composition by default.

## 46.160.2 Member Function Documentation

# 46.160.2.1 get\_coarse\_op()

virtual std::shared\_ptr<const LinOp> gko::multigrid::MultigridLevel::get\_coarse\_op ( ) const
[pure virtual]

Returns the operator on coarse level.

Returns

the operator on coarse level.

Implemented in gko::multigrid::EnableMultigridLevel< ValueType >.

# 46.160.2.2 get\_fine\_op()

virtual std::shared\_ptr<const LinOp> gko::multigrid::MultigridLevel::get\_fine\_op ( ) const
[pure virtual]

Returns the operator on fine level.

Returns

the operator on fine level.

Implemented in gko::multigrid::EnableMultigridLevel < ValueType >.

# 46.160.2.3 get\_prolong\_op()

virtual std::shared\_ptr<const LinOp> gko::multigrid::MultigridLevel::get\_prolong\_op ( ) const
[pure virtual]

Returns the prolong operator.

Returns

the prolong operator.

 $Implemented \ in \ gko::multigrid::Enable Multigrid Level < Value Type >.$ 

# 46.160.2.4 get\_restrict\_op()

virtual std::shared\_ptr<const LinOp> gko::multigrid::MultigridLevel::get\_restrict\_op ( ) const
[pure virtual]

Returns the restrict operator.

#### Returns

the restrict operator.

Implemented in gko::multigrid::EnableMultigridLevel< ValueType >.

The documentation for this class was generated from the following file:

• ginkgo/core/multigrid/multigrid\_level.hpp

# 46.161 gko::batch::MultiVector < ValueType > Class Template Reference

MultiVector stores multiple vectors in a batched fashion and is useful for batched operations.

```
#include <ginkgo/core/base/batch_multi_vector.hpp>
```

# **Public Member Functions**

- std::unique\_ptr< unbatch\_type > create\_view\_for\_item (size\_type item\_id)
  - Creates a mutable view (of matrix::Dense type) of one item of the Batch MultiVector object.
- std::unique\_ptr< const unbatch\_type > create\_const\_view\_for\_item (size\_type item\_id) const
  - Creates a mutable view (of matrix::Dense type) of one item of the Batch MultiVector object.
- batch\_dim< 2 > get\_size () const
  - Returns the batch size.
- size\_type get\_num\_batch\_items () const
  - Returns the number of batch items.
- dim< 2 > get\_common\_size () const
  - Returns the common size of the batch items.
- value type \* get values () noexcept
  - Returns a pointer to the array of values of the multi-vector.
- const value\_type \* get\_const\_values () const noexcept
  - Returns a pointer to the array of values of the multi-vector.
- value\_type \* get\_values\_for\_item (size\_type batch\_id) noexcept
  - Returns a pointer to the array of values of the multi-vector for a specific batch item.
- const value\_type \* get\_const\_values\_for\_item (size\_type batch\_id) const noexcept
  - Returns a pointer to the array of values of the multi-vector for a specific batch item.
- size\_type get\_num\_stored\_elements () const noexcept
  - Returns the number of elements explicitly stored in the batch matrix, cumulative across all the batch items.
- size\_type get\_cumulative\_offset (size\_type batch\_id) const
  - Get the cumulative storage size offset.
- value\_type & at (size\_type batch\_id, size\_type row, size\_type col)

Returns a single element for a particular batch item.

value\_type at (size\_type batch\_id, size\_type row, size\_type col) const

Returns a single element for a particular batch item.

ValueType & at (size\_type batch\_id, size\_type idx) noexcept

Returns a single element for a particular batch item.

ValueType at (size\_type batch\_id, size\_type idx) const noexcept

Returns a single element for a particular batch item.

void scale (ptr\_param< const MultiVector< ValueType >> alpha)

Scales the vector with a scalar (aka: BLAS scal).

void add\_scaled (ptr\_param< const MultiVector< ValueType >> alpha, ptr\_param< const MultiVector< ValueType >> b)

Adds b scaled by alpha to the vector (aka: BLAS axpy).

void compute\_dot (ptr\_param< const MultiVector< ValueType >> b, ptr\_param< MultiVector< ValueType >> result) const

Computes the column-wise dot product of each multi-vector in this batch and its corresponding entry in b.

void compute\_conj\_dot (ptr\_param< const MultiVector< ValueType >> b, ptr\_param< MultiVector< ValueType >> result) const

Computes the column-wise conjugate dot product of each multi-vector in this batch and its corresponding entry in b.

void compute\_norm2 (ptr\_param< MultiVector< remove\_complex< ValueType >>> result) const

Computes the Euclidean ( $L^2$ ) norm of each multi-vector in this batch.

void fill (ValueType value)

Fills the input MultiVector with a given value.

## Static Public Member Functions

 $\bullet \ \ static \ std::unique\_ptr< \ \ MultiVector> create\_with\_config\_of \ (ptr\_param< const \ \ MultiVector> other)\\$ 

Creates a MultiVector with the configuration of another MultiVector.

static std::unique\_ptr< MultiVector > create (std::shared\_ptr< const Executor > exec, const batch\_dim< 2 > &size=batch\_dim< 2 > {})

Creates an uninitialized multi-vector of the specified size.

static std::unique\_ptr< MultiVector > create (std::shared\_ptr< const Executor > exec, const batch\_dim< 2
 <ul>
 &size, array< value\_type > values)

Creates a MultiVector from an already allocated (and initialized) array.

template<typename InputValueType >

 $static\ std::unique\_ptr< \ MultiVector> create\ (std::shared\_ptr< const\ Executor> exec,\ const\ batch\_dim<2\\ > \&size,\ std::initializer\_list< InputValueType> values)$ 

create(std::shared\_ptr<const</pre>

static std::unique\_ptr< const MultiVector > create\_const (std::shared\_ptr< const Executor > exec, const batch\_dim< 2 > &sizes, gko::detail::const\_array\_view< ValueType > &&values)

Creates a constant (immutable) batch multi-vector from a constant array.

# 46.161.1 Detailed Description

```
template<typename ValueType = default_precision> class gko::batch::MultiVector< ValueType >
```

MultiVector stores multiple vectors in a batched fashion and is useful for batched operations.

For example, if you want to store two batch items with multi-vectors of size (3 x 2) given below:

```
[12;3412;3412;34]
```

In memory, they would be stored as a single array: [1 2 1 2 1 2 3 4 3 4 3 4].

Access functions @at can help access individual item if necessary.

The values of the different batch items are stored consecutively and in each batch item, the multi-vectors are stored in a row-major fashion.

# **Template Parameters**

ValueType precision of multi-vector ele	ents
---	------

# 46.161.2 Member Function Documentation

# 46.161.2.1 add\_scaled()

Adds b scaled by alpha to the vector (aka: BLAS axpy).

#### **Parameters**

alpha	the scalar
b	a multi-vector of the same dimension as this

## Note

If alpha is 1x1 MultiVector matrix, the entire multi-vector (all batches) is scaled by alpha. If it is a MultiVector row vector of values, then i-th column of the vector is scaled with the i-th element of alpha (the number of columns of alpha has to match the number of columns of the multi-vector).

# 46.161.2.2 at() [1/4]

Returns a single element for a particular batch item.

batch⊷ _id	the batch item index to be queried
row	the row of the requested element
col	the column of the requested element

Note

the method has to be called on the same Executor the vector is stored at (e.g. trying to call this method on a GPU multi-vector from the OMP results in a runtime error)

```
249 {
250          return values_.get_const_data()[linearize_index(batch_id, idx)];
251    }
```

References gko::array< ValueType >::get\_const\_data().

# 46.161.2.3 at() [2/4]

Returns a single element for a particular batch item.

Useful for iterating across all elements of the vector. However, it is less efficient than the two-parameter variant of this method.

## **Parameters**

batch⊷	the batch item index to be queried
_id	
idx	a linear index of the requested element

#### Note

the method has to be called on the same Executor the vector is stored at (e.g. trying to call this method on a GPU multi-vector from the OMP results in a runtime error)

References gko::array< ValueType >::get\_data().

# 46.161.2.4 at() [3/4]

Returns a single element for a particular batch item.

batch⊷	the batch item index to be queried
_id	
row	the row of the requested element
Generated by D	the column of the requested element

#### Note

the method has to be called on the same Executor the vector is stored at (e.g. trying to call this method on a GPU multi-vector from the OMP results in a runtime error)

References gko::array< ValueType >::get\_data(), and gko::batch::MultiVector< ValueType >::get\_num\_batch\_← items().

## 46.161.2.5 at() [4/4]

Returns a single element for a particular batch item.

#### **Parameters**

batch⊷ _id	the batch item index to be queried
row	the row of the requested element
col	the column of the requested element

## Note

the method has to be called on the same Executor the vector is stored at (e.g. trying to call this method on a GPU multi-vector from the OMP results in a runtime error)

 $References\ gko::array<\ ValueType>::get\_const\_data(),\ and\ gko::batch::MultiVector<\ ValueType>::get\_num\_{\hookleftarrow}\ batch\_items().$ 

# 46.161.2.6 compute\_conj\_dot()

Computes the column-wise conjugate dot product of each multi-vector in this batch and its corresponding entry in b.

If the vector has complex value\_type, then the conjugate of this is taken.

b	a MultiVector of same dimension as this	
result	a MultiVector row vector, used to store the dot product (the number of column in the vector must match	
	the number of columns of this)  Generated by Doxygen	

# 46.161.2.7 compute\_dot()

Computes the column-wise dot product of each multi-vector in this batch and its corresponding entry in b.

#### **Parameters**

b	a MultiVector of same dimension as this
result	a MultiVector row vector, used to store the dot product

# 46.161.2.8 compute\_norm2()

Computes the Euclidean ( $L^{\wedge}2$ ) norm of each multi-vector in this batch.

# Parameters

```
result a MultiVector, used to store the norm (the number of columns in the vector must match the number of columns of this)
```

# 46.161.2.9 create() [1/3]

Creates a MultiVector from an already allocated (and initialized) array.

exec	Executor associated to the vector
size	sizes of the batch matrices in a batch_dim object
values	array of values

#### Note

If values is not an rvalue, not an array of ValueType, or is on the wrong executor, an internal copy will be created, and the original array data will not be used in the vector.

## 46.161.2.10 create() [2/3]

create(std::shared\_ptr<const executor>="">, const batch\_dim<2>&, array<value\_type>)

References gko::batch::MultiVector< ValueType >::create().

# 46.161.2.11 create() [3/3]

Creates an uninitialized multi-vector of the specified size.

# **Parameters**

exec	Executor associated to the vector
size	size of the batch multi vector

# Returns

A smart pointer to the newly created matrix.

Referenced by gko::batch::MultiVector< ValueType >::create().

# 46.161.2.12 create\_const()

```
template<trypename ValueType = default_precision>
static std::unique_ptr<const MultiVector> gko::batch::MultiVector< ValueType >::create_const
```

```
(
    std::shared_ptr< const Executor > exec,
    const batch_dim< 2 > & sizes,
    gko::detail::const_array_view< ValueType > && values ) [static]
```

Creates a constant (immutable) batch multi-vector from a constant array.

#### **Parameters**

exec	the executor to create the vector on
size	the dimensions of the vector
values	the value array of the vector
stride	the row-stride of the vector

#### Returns

A smart pointer to the constant multi-vector wrapping the input array (if it resides on the same executor as the vector) or a copy of the array on the correct executor.

# 46.161.2.13 create\_const\_view\_for\_item()

Creates a mutable view (of matrix::Dense type) of one item of the Batch MultiVector object.

Does not perform any deep copies, but only returns a view of the data.

#### **Parameters**

	The final and the decade factor
item⊷	The index of the batch item
id	

#### Returns

a matrix::Dense object with the data from the batch item at the given index.

## 46.161.2.14 create\_view\_for\_item()

Creates a mutable view (of matrix::Dense type) of one item of the Batch MultiVector object.

Does not perform any deep copies, but only returns a view of the data.

#### **Parameters**

item⊷	The index of the batch item
_id	

#### Returns

a matrix::Dense object with the data from the batch item at the given index.

# 46.161.2.15 create\_with\_config\_of()

Creates a MultiVector with the configuration of another MultiVector.

#### **Parameters**

#### 46.161.2.16 fill()

Fills the input MultiVector with a given value.

# **Parameters**

```
value the value to be filled
```

# 46.161.2.17 get\_common\_size()

```
template<typename ValueType = default_precision>
dim<2> gko::batch::MultiVector< ValueType >::get_common_size ( ) const [inline]
```

Returns the common size of the batch items.

#### Returns

the common size stored

References gko::batch\_dim< Dimensionality, DimensionType >::get\_common\_size().

Referenced by gko::batch::MultiVector< ValueType >::get cumulative offset().

# 46.161.2.18 get\_const\_values()

```
template<typename ValueType = default_precision>
const value_type* gko::batch::MultiVector< ValueType >::get_const_values ( ) const [inline],
[noexcept]
```

Returns a pointer to the array of values of the multi-vector.

#### Returns

the pointer to the array of values

## Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

References gko::array< ValueType >::get\_const\_data().

# 46.161.2.19 get\_const\_values\_for\_item()

Returns a pointer to the array of values of the multi-vector for a specific batch item.

#### **Parameters**

batch⊷	the id of the batch item.
id	

# Returns

the pointer to the array of values

#### Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

References gko::array< ValueType >::get\_const\_data(), gko::batch::MultiVector< ValueType >::get\_cumulative offset(), and gko::batch::MultiVector< ValueType >::get num batch items().

#### 46.161.2.20 get cumulative offset()

Get the cumulative storage size offset.

#### **Parameters**

batch⊷	the batch id
_id	

#### Returns

the cumulative offset

References gko::batch::MultiVector< ValueType >::get\_common\_size().

# 46.161.2.21 get\_num\_batch\_items()

```
template<typename ValueType = default_precision>
size_type gko::batch::MultiVector< ValueType >::get_num_batch_items ( ) const [inline]
```

Returns the number of batch items.

# Returns

the number of batch items

References gko::batch\_dim< Dimensionality, DimensionType >::get\_num\_batch\_items().

Referenced by gko::batch::MultiVector< ValueType >::at(), gko::batch::MultiVector< ValueType >::get\_const\_ values for item(), and gko::batch::MultiVector< ValueType >::get values for item().

# 46.161.2.22 get\_num\_stored\_elements()

```
template<typename ValueType = default_precision>
size_type gko::batch::MultiVector< ValueType >::get_num_stored_elements ( ) const [inline],
[noexcept]
```

Returns the number of elements explicitly stored in the batch matrix, cumulative across all the batch items.

#### Returns

the number of elements explicitly stored in the vector, cumulative across all the batch items

References gko::array< ValueType >::get\_size().

### 46.161.2.23 get\_size()

```
template<typename ValueType = default_precision>
batch_dim<2> gko::batch::MultiVector< ValueType >::get_size ( ) const [inline]
```

Returns the batch size.

#### Returns

the batch size

#### 46.161.2.24 get\_values()

```
template<typename ValueType = default_precision>
value_type* gko::batch::MultiVector< ValueType >::get_values ( ) [inline], [noexcept]
```

Returns a pointer to the array of values of the multi-vector.

#### Returns

the pointer to the array of values

References gko::array< ValueType >::get\_data().

# 46.161.2.25 get\_values\_for\_item()

Returns a pointer to the array of values of the multi-vector for a specific batch item.

#### **Parameters**

batch←	the id of the batch item.
_id	

#### Returns

the pointer to the array of values

References gko::batch::MultiVector< ValueType >::get\_cumulative\_offset(), gko::array< ValueType >::get\_data(), and gko::batch::MultiVector< ValueType >::get\_num\_batch\_items().

## 46.161.2.26 scale()

Scales the vector with a scalar (aka: BLAS scal).

#### **Parameters**

alpha the scalar	
------------------	--

# Note

If alpha is 1x1 MultiVector matrix, the entire multi-vector (all batches) is scaled by alpha. If it is a MultiVector row vector of values, then i-th column of the vector is scaled with the i-th element of alpha (the number of columns of alpha has to match the number of columns of the multi-vector). If it is a MultiVector of the same size as this, then an element wise scaling is performed.

The documentation for this class was generated from the following file:

ginkgo/core/base/batch\_multi\_vector.hpp

# 46.162 gko::log::ProfilerHook::NestedSummaryWriter Class Reference

Receives the results from ProfilerHook::create\_nested\_summary().

```
#include <ginkgo/core/log/profiler_hook.hpp>
```

# **Public Member Functions**

virtual void write\_nested (const nested\_summary\_entry &root, std::chrono::nanoseconds overhead)=0
 Callback to write out the summary results.

# 46.162.1 Detailed Description

Receives the results from ProfilerHook::create\_nested\_summary().

# 46.162.2 Member Function Documentation

# 46.162.2.1 write\_nested()

Callback to write out the summary results.

#### **Parameters**

root	the root range with runtime and count.
overhead	an estimate of the profiler overhead

Implemented in gko::log::ProfilerHook::TableSummaryWriter.

The documentation for this class was generated from the following file:

• ginkgo/core/log/profiler\_hook.hpp

# 46.163 gko::NotCompiled Class Reference

NotCompiled is thrown when attempting to call an operation which is a part of a module that was not compiled on the system.

```
#include <ginkgo/core/base/exception.hpp>
```

# **Public Member Functions**

NotCompiled (const std::string &file, int line, const std::string &func, const std::string &module)
 Initializes a NotCompiled error.

# 46.163.1 Detailed Description

NotCompiled is thrown when attempting to call an operation which is a part of a module that was not compiled on the system.

# 46.163.2 Constructor & Destructor Documentation

# 46.163.2.1 NotCompiled()

Initializes a NotCompiled error.

#### **Parameters**

file	The name of the offending source file
line	The source code line number where the error occurred
func	The name of the function that has not been compiled
module	The name of the module which contains the function

The documentation for this class was generated from the following file:

· ginkgo/core/base/exception.hpp

# 46.164 gko::NotImplemented Class Reference

NotImplemented is thrown in case an operation has not yet been implemented (but will be implemented in the future).

```
#include <ginkgo/core/base/exception.hpp>
```

# **Public Member Functions**

• NotImplemented (const std::string &file, int line, const std::string &func) Initializes a NotImplemented error.

# 46.164.1 Detailed Description

NotImplemented is thrown in case an operation has not yet been implemented (but will be implemented in the future).

# 46.164.2 Constructor & Destructor Documentation

# 46.164.2.1 NotImplemented()

Initializes a NotImplemented error.

#### **Parameters**

file	The name of the offending source file
line	The source code line number where the error occurred
func	The name of the not-yet implemented function

The documentation for this class was generated from the following file:

• ginkgo/core/base/exception.hpp

# 46.165 gko::NotSupported Class Reference

NotSupported is thrown in case it is not possible to perform the requested operation on the given object type.

```
#include <ginkgo/core/base/exception.hpp>
```

# **Public Member Functions**

NotSupported (const std::string &file, int line, const std::string &func, const std::string &obj\_type)
 Initializes a NotSupported error.

# 46.165.1 Detailed Description

NotSupported is thrown in case it is not possible to perform the requested operation on the given object type.

# 46.165.2 Constructor & Destructor Documentation

# 46.165.2.1 NotSupported()

Initializes a NotSupported error.

#### **Parameters**

file	The name of the offending source file
line	The source code line number where the error occurred
func	The name of the function where the error occurred
obj_type	The object type on which the requested operation cannot be performed.

The documentation for this class was generated from the following file:

• ginkgo/core/base/exception.hpp

# 46.166 gko::null\_deleter< T > Class Template Reference

This is a deleter that does not delete the object.

```
#include <ginkgo/core/base/utils_helper.hpp>
```

# **Public Member Functions**

• void operator() (pointer) const noexcept Deletes the object.

# 46.166.1 Detailed Description

```
template<typename T> class gko::null_deleter< T >
```

This is a deleter that does not delete the object.

It is useful where the object has been allocated elsewhere and will be deleted manually.

# 46.166.2 Member Function Documentation

# 46.166.2.1 operator()()

Deletes the object.

#### **Parameters**

ptr pointer to the object being deleted

The documentation for this class was generated from the following file:

• ginkgo/core/base/utils\_helper.hpp

# 46.167 gko::nvidia device Class Reference

nvidia\_device handles the number of executor on Nvidia devices and have the corresponding recursive\_mutex.

#include <ginkgo/core/base/device.hpp>

# 46.167.1 Detailed Description

nvidia\_device handles the number of executor on Nvidia devices and have the corresponding recursive\_mutex.

The documentation for this class was generated from the following file:

· ginkgo/core/base/device.hpp

# 46.168 gko::OmpExecutor Class Reference

This is the Executor subclass which represents the OpenMP device (typically CPU).

#include <ginkgo/core/base/executor.hpp>

# **Public Member Functions**

- std::shared\_ptr< Executor > get\_master () noexcept override
  - Returns the master OmpExecutor of this Executor.
- std::shared\_ptr< const Executor > get\_master () const noexcept override

Returns the master OmpExecutor of this Executor.

· void synchronize () const override

Synchronize the operations launched on the executor with its master.

- std::string get\_description () const override
- virtual void run (const Operation &op) const=0

Runs the specified Operation using this Executor.

template<typename ClosureOmp, typename ClosureCuda, typename ClosureHip, typename ClosureDpcpp > void run (const ClosureOmp &op\_omp, const ClosureCuda &op\_cuda, const ClosureHip &op\_hip, const ClosureDpcpp &op\_dpcpp) const

Runs one of the passed in functors, depending on the Executor type.

template < typename ClosureReference , typename ClosureOmp , typename ClosureCuda , typename ClosureHip , typename Closure
 —
 —
 Dpcpp >

void run (std::string name, const ClosureReference &op\_ref, const ClosureOmp &op\_omp, const Closure← Cuda &op\_cuda, const ClosureHip &op\_hip, const ClosureDpcpp &op\_dpcpp) const

Runs one of the passed in functors, depending on the Executor type.

# **Static Public Member Functions**

static std::shared\_ptr< OmpExecutor > create (std::shared\_ptr< CpuAllocatorBase > alloc=std::make\_←
 shared< CpuAllocator >())

Creates a new OmpExecutor.

# 46.168.1 Detailed Description

This is the Executor subclass which represents the OpenMP device (typically CPU).

# 46.168.2 Member Function Documentation

## 46.168.2.1 get\_description()

```
std::string gko::OmpExecutor::get_description ( ) const [override], [virtual]
```

## Returns

a textual representation of the executor and its device.

Implements gko::Executor.

Reimplemented in gko::ReferenceExecutor.

# 46.168.2.2 get\_master() [1/2]

```
std::shared_ptr<const Executor> gko::OmpExecutor::get_master ( ) const [override], [virtual],
[noexcept]
```

Returns the master OmpExecutor of this Executor.

# Returns

the master OmpExecutor of this Executor.

Implements gko::Executor.

## 46.168.2.3 get\_master() [2/2]

```
std::shared_ptr<Executor> gko::OmpExecutor::get_master ( ) [override], [virtual], [noexcept]
```

Returns the master OmpExecutor of this Executor.

#### Returns

the master OmpExecutor of this Executor.

Implements gko::Executor.

## 46.168.2.4 run() [1/3]

Runs one of the passed in functors, depending on the Executor type.

## **Template Parameters**

ClosureOmp	type of op_omp
ClosureCuda	type of op_cuda
ClosureHip	type of op_hip
ClosureDpcpp	type of op_dpcpp

## **Parameters**

op_omp	functor to run in case of a OmpExecutor or ReferenceExecutor
op_cuda	functor to run in case of a CudaExecutor
op_hip	functor to run in case of a HipExecutor
op_dpcpp	functor to run in case of a DpcppExecutor

## 46.168.2.5 run() [2/3]

```
virtual void gko::Executor::run
```

Runs the specified Operation using this Executor.

#### **Parameters**

```
op the operation to run
```

## 46.168.2.6 run() [3/3]

Runs one of the passed in functors, depending on the Executor type.

## **Template Parameters**

ClosureReference	type of op_ref
ClosureOmp	type of op_omp
ClosureCuda	type of op_cuda
ClosureHip	type of op_hip
ClosureDpcpp	type of op_dpcpp

#### **Parameters**

name	the name of the operation
op_ref	functor to run in case of a ReferenceExecutor
op_omp	functor to run in case of a OmpExecutor
op_cuda	functor to run in case of a CudaExecutor
op_hip	functor to run in case of a HipExecutor
op_dpcpp	functor to run in case of a DpcppExecutor

The documentation for this class was generated from the following file:

• ginkgo/core/base/executor.hpp

# 46.169 gko::Operation Class Reference

Operations can be used to define functionalities whose implementations differ among devices.

#include <ginkgo/core/base/executor.hpp>

#### **Public Member Functions**

 virtual const char \* get\_name () const noexcept
 Returns the operation's name.

## 46.169.1 Detailed Description

Operations can be used to define functionalities whose implementations differ among devices.

This is done by extending the Operation class and implementing the overloads of the Operation::run() method for all Executor types. When invoking the Executor::run() method with the Operation as input, the library will select the Operation::run() overload corresponding to the dynamic type of the Executor instance.

Consider an overload of operator<< for Executors, which prints some basic device information (e.g. device type and id) of the Executor to a C++ stream:

```
std::ostream& operator«(std::ostream &os, const gko::Executor &exec);
```

One possible implementation would be to use RTTI to find the dynamic type of the Executor, However, using the Operation feature of Ginkgo, there is a more elegant approach which utilizes polymorphism. The first step is to define an Operation that will print the desired information for each Executor type.

```
class DeviceInfoPrinter : public gko::Operation {
public:
    explicit DeviceInfoPrinter(std::ostream &os) : os_(os) {}
    void run(const gko::OmpExecutor *)const override { os_ « "OMP"; }
    void run(const gko::CudaExecutor *exec)const override
{ os_ « "CUDA(" « exec->get_device_id() « ")"; }
    void run(const gko::HipExecutor *exec)const override
{ os_ « "HIP(" « exec->get_device_id() « ")"; }
    void run(const gko::DpcpExecutor *exec)const override
{ os_ « "DPC++(" « exec->get_device_id() « ")"; }
    // This is optional, if not overloaded, defaults to OmpExecutor overload
    void run(const gko::ReferenceExecutor *)const override
{ os_ « "Reference CPU"; }
private:
    std::ostream &os_;
};
```

Using DeviceInfoPrinter, the implementation of operator<< is as simple as calling the run() method of the executor.

```
std::ostream& operator«(std::ostream &os, const gko::Executor &exec)
{
    DeviceInfoPrinter printer(os);
    exec.run(printer);
    return os;
}
```

Now it is possible to write the following code:

which produces the expected output:

```
OMP
CUDA(0)
HIP(0)
DPC++(0)
Reference CPU
```

One might feel that this code is too complicated for such a simple task. Luckily, there is an overload of the Executor::run() method, which is designed to facilitate writing simple operations like this one. The method takes four closures as input: one which is run for OMP, one for CUDA executors, one for HIP executors, and the last one for DPC++ executors. Using this method, there is no need to implement an Operation subclass:

```
std::ostream& operator«(std::ostream &os, const gko::Executor &exec)
{
    exec.run(
        [&]() { os « "OMP"; }, // OMP closure
```

Using this approach, however, it is impossible to distinguish between a OmpExecutor and ReferenceExecutor, as both of them call the OMP closure.

## 46.169.2 Member Function Documentation

## 46.169.2.1 get\_name()

```
virtual const char* gko::Operation::get_name ( ) const [virtual], [noexcept]
```

Returns the operation's name.

Returns

the operation's name

The documentation for this class was generated from the following file:

• ginkgo/core/base/executor.hpp

## 46.170 gko::log::operation\_data Struct Reference

Struct representing Operator related data.

```
#include <ginkgo/core/log/record.hpp>
```

## 46.170.1 Detailed Description

Struct representing Operator related data.

The documentation for this struct was generated from the following file:

ginkgo/core/log/record.hpp

## 46.171 gko::OutOfBoundsError Class Reference

OutOfBoundsError is thrown if a memory access is detected to be out-of-bounds.

```
#include <ginkgo/core/base/exception.hpp>
```

#### **Public Member Functions**

• OutOfBoundsError (const std::string &file, int line, size\_type index, size\_type bound)

Initializes an OutOfBoundsError.

## 46.171.1 Detailed Description

OutOfBoundsError is thrown if a memory access is detected to be out-of-bounds.

## 46.171.2 Constructor & Destructor Documentation

#### 46.171.2.1 OutOfBoundsError()

Initializes an OutOfBoundsError.

#### **Parameters**

file	The name of the offending source file
line	The source code line number where the error occurred
index	The position that was accessed
bound	The first out-of-bound index

The documentation for this class was generated from the following file:

· ginkgo/core/base/exception.hpp

## 46.172 gko::OverflowError Class Reference

OverflowError is thrown when an index calculation for storage requirements overflows.

```
#include <ginkgo/core/base/exception.hpp>
```

## **Public Member Functions**

• OverflowError (const std::string &file, const int line, const std::string &index\_type)

## 46.172.1 Detailed Description

OverflowError is thrown when an index calculation for storage requirements overflows.

This most likely means that the index type is too small.

## 46.172.2 Constructor & Destructor Documentation

#### 46.172.2.1 OverflowError()

#### **Parameters**

file	The name of the offending source file
line	The source code line number where the error occurred
index_type	The integer type that overflowed

The documentation for this class was generated from the following file:

• ginkgo/core/base/exception.hpp

## 46.173 gko::log::Papi< ValueType > Class Template Reference

Papi is a Logger which logs every event to the PAPI software.

```
#include <ginkgo/core/log/papi.hpp>
```

## **Public Member Functions**

- const std::string get\_handle\_name () const
  - Returns the unique name of this logger, which can be used in the PAPI\_read() call.
- const papi\_handle\_t get\_handle () const

Returns the corresponding papi\_handle\_t for this logger.

#### Static Public Member Functions

 static std::shared\_ptr< Papi > create (std::shared\_ptr< const gko::Executor >, const Logger::mask\_type &enabled\_events=Logger::all\_events\_mask)

Creates a Papi Logger.

static std::shared\_ptr< Papi > create (const Logger::mask\_type &enabled\_events=Logger::all\_events\_←
mask)

Creates a Papi Logger.

## 46.173.1 Detailed Description

```
template<typename ValueType = default_precision> class gko::log::Papi< ValueType >
```

Papi is a Logger which logs every event to the PAPI software.

Thanks to this logger, applications which interface with PAPI can access Ginkgo internal data through PAPI. For an example of usage, see examples/papi\_logging/papi\_logging.cpp

The logged values for each event are the following:

- · all allocation events: number of bytes per executor
- · all free events: number of calls per executor
- copy\_started: number of bytes per executor from (to), in copy\_started\_from (respectively copy\_started\_to).
- copy\_completed: number of bytes per executor from (to), in copy\_completed\_from (respectively copy\_

   completed\_to).
- all polymorphic objects and operation events: number of calls per executor
- all apply events: number of calls per LinOp (argument "A").
- · all factory events: number of calls per factory
- · criterion check completed event: the residual norm is stored in a record (per criterion)
- iteration complete event: the number of iteration is counted (per solver)

## **Template Parameters**

```
ValueType the type of values stored in the class (e.g. residuals)
```

#### 46.173.2 Member Function Documentation

## 46.173.2.1 create() [1/2]

```
template<trypename ValueType = default_precision>
static std::shared_ptr<Papi> gko::log::Papi< ValueType >::create (
```

```
const Logger::mask_type & enabled_events = Logger::all_events_mask ) [inline],
[static]
```

Creates a Papi Logger.

enabled\_events

**Parameters** 

200 201

the events enabled for this Logger

References gko::log::Papi< ValueType >::get\_handle().

## 46.173.2.2 create() [2/2]

Creates a Papi Logger.

#### **Parameters**

```
enabled_events the events enabled for this Logger
```

#### 46.173.2.3 get\_handle()

```
template<typename ValueType = default_precision>
const papi_handle_t gko::log::Papi< ValueType >::get_handle ( ) const [inline]
```

Returns the corresponding papi handle t for this logger.

Returns

the corresponding papi\_handle\_t for this logger

Referenced by gko::log::Papi< ValueType >::create().

## 46.173.2.4 get\_handle\_name()

```
template<typename ValueType = default_precision>
const std::string gko::log::Papi< ValueType >::get_handle_name ( ) const [inline]
```

Returns the unique name of this logger, which can be used in the PAPI\_read() call.

#### Returns

the unique name of this logger

The documentation for this class was generated from the following file:

ginkgo/core/log/papi.hpp

# 46.174 gko::factorization::Parlc< ValueType, IndexType > Class Template Reference

ParIC is an incomplete Cholesky factorization which is computed in parallel.

#include <ginkgo/core/factorization/par\_ic.hpp>

#### **Static Public Member Functions**

• static parameters\_type parse (const config::pnode &config, const config::registry &context, const config::type\_descriptor &td\_for\_child=config::make\_type\_descriptor < ValueType, IndexType >())

Create the parameters from the property\_tree.

#### **Additional Inherited Members**

## 46.174.1 Detailed Description

template<typename ValueType = default\_precision, typename IndexType = int32> class gko::factorization::Parlc< ValueType, IndexType >

ParIC is an incomplete Cholesky factorization which is computed in parallel.

L is a lower triangular matrix, which approximates a given matrix A with  $A \approx LL^H$ . Here,  $L + L^H$  has the same sparsity pattern as A, which is also called IC(0).

The ParlC algorithm generates the incomplete factors iteratively, using a fixed-point iteration of the form

$$F(L) = \begin{cases} \sqrt{a_{ii} - \sum_{k=1}^{i-1} |l_{ik}|^2}, & i == j \\ a_{ij} - \sum_{k=1}^{i-1} l_{ik} u_{kj}, & i < j \end{cases}$$

In general, the entries of L can be iterated in parallel and in asynchronous fashion, the algorithm asymptotically converges to the incomplete factors L and  $L^H$  fulfilling  $\left(R=A-L\cdot L^H\right)|_{\mathcal{S}}=0|_{\mathcal{S}}$  where  $\mathcal{S}$  is the pre-defined sparsity pattern (in case of IC(0) the sparsity pattern of the system matrix A). The number of ParlC sweeps needed for convergence depends on the parallelism level: For sequential execution, a single sweep is sufficient, for fine-grained parallelism, the number of sweeps necessary to get a good approximation of the incomplete factors depends heavily on the problem. On the OpenMP executor, 3 sweeps usually give a decent approximation in our experiments, while GPU executors can take 10 or more iterations.

The ParIC algorithm in Ginkgo follows the design of E. Chow and A. Patel, Fine-grained Parallel Incomplete LU Factorization, SIAM Journal on Scientific Computing, 37, C169-C193 (2015).

## **Template Parameters**

ValueType	Type of the values of all matrices used in this class
IndexType	Type of the indices of all matrices used in this class

## 46.174.2 Member Function Documentation

#### 46.174.2.1 parse()

Create the parameters from the property\_tree.

Because this is directly tied to the specific type, the value/index type settings within config are ignored and type\_ descriptor is only used for children configs.

## **Parameters**

config	the property tree for setting	
context	the registry	
td_for_child	the type descriptor for children configs. The default uses the value/index type of this class.	

## Returns

parameters

The documentation for this class was generated from the following file:

• ginkgo/core/factorization/par\_ic.hpp

# 46.175 gko::factorization::ParIct< ValueType, IndexType > Class Template Reference

ParICT is an incomplete threshold-based Cholesky factorization which is computed in parallel.

#include <ginkgo/core/factorization/par\_ict.hpp>

#### Static Public Member Functions

• static parameters\_type parse (const config::pnode &config, const config::registry &context, const config::type\_descriptor &td\_for\_child=config::make\_type\_descriptor < ValueType, IndexType >())

Create the parameters from the property\_tree.

#### **Additional Inherited Members**

## 46.175.1 Detailed Description

template<typename ValueType = default\_precision, typename IndexType = int32> class gko::factorization::Parlct< ValueType, IndexType >

ParICT is an incomplete threshold-based Cholesky factorization which is computed in parallel.

L is a lower triangular matrix which approximates a given symmetric positive definite matrix A with  $A \approx LL^T$ . Here, L has a sparsity pattern that is improved iteratively based on its element-wise magnitude. The initial sparsity pattern is chosen based on the lower triangle of A.

One iteration of the ParICT algorithm consists of the following steps:

- 1. Calculating the residual  $R = A LL^T$
- 2. Adding new non-zero locations from R to L. The new non-zero locations are initialized based on the corresponding residual value.
- 3. Executing a fixed-point iteration on L according to  $F(L) = \begin{cases} \frac{1}{l_{jj}} \left( a_{ij} \sum_{k=1}^{j-1} l_{ik} l_{jk} \right), & i \neq j \\ \sqrt{a_{ij} \sum_{k=1}^{j-1} l_{ik} l_{jk}}, & i = j \end{cases}$
- 4. Removing the smallest entries (by magnitude) from L
- 5. Executing a fixed-point iteration on the (now sparser) L

This ParICT algorithm thus improves the sparsity pattern and the approximation of L simultaneously.

The implementation follows the design of H. Anzt et al., ParlLUT - A Parallel Threshold ILU for GPUs, 2019 IEEE International Parallel and Distributed Processing Symposium (IPDPS), pp. 231–241.

#### **Template Parameters**

ValueType	Type of the values of all matrices used in this class
IndexType	Type of the indices of all matrices used in this class

#### 46.175.2 Member Function Documentation

#### 46.175.2.1 parse()

Create the parameters from the property\_tree.

Because this is directly tied to the specific type, the value/index type settings within config are ignored and type\_ descriptor is only used for children configs.

#### **Parameters**

config	the property tree for setting	
context	the registry	
td_for_child	the type descriptor for children configs. The default uses the value/index type of this class.	

#### Returns

parameters

The documentation for this class was generated from the following file:

• ginkgo/core/factorization/par\_ict.hpp

# 46.176 gko::factorization::Parllu< ValueType, IndexType > Class Template Reference

ParILU is an incomplete LU factorization which is computed in parallel.

```
#include <ginkgo/core/factorization/par_ilu.hpp>
```

## **Static Public Member Functions**

• static parameters\_type parse (const config::pnode &config, const config::registry &context, const config::type\_descriptor &td\_for\_child=config::make\_type\_descriptor < ValueType, IndexType >())

Create the parameters from the property\_tree.

#### **Additional Inherited Members**

## 46.176.1 Detailed Description

template<typename ValueType = default\_precision, typename IndexType = int32> class gko::factorization::ParIlu< ValueType, IndexType >

ParILU is an incomplete LU factorization which is computed in parallel.

L is a lower unitriangular, while U is an upper triangular matrix, which approximate a given matrix A with  $A \approx LU$ . Here, L and U have the same sparsity pattern as A, which is also called ILU(0).

The ParILU algorithm generates the incomplete factors iteratively, using a fixed-point iteration of the form

$$F(L,U) = \begin{cases} \frac{1}{u_{jj}} \left( a_{ij} - \sum_{k=1}^{j-1} l_{ik} u_{kj} \right), & i > j \\ a_{ij} - \sum_{k=1}^{i-1} l_{ik} u_{kj}, & i \leq j \end{cases}$$

In general, the entries of L and U can be iterated in parallel and in asynchronous fashion, the algorithm asymptotically converges to the incomplete factors L and U fulfilling  $(R=A-L\cdot U)\,|_{\mathcal{S}}=0|_{\mathcal{S}}$  where  $\mathcal{S}$  is the pre-defined sparsity pattern (in case of ILU(0) the sparsity pattern of the system matrix A). The number of ParlLU sweeps needed for convergence depends on the parallelism level: For sequential execution, a single sweep is sufficient, for fine-grained parallelism, the number of sweeps necessary to get a good approximation of the incomplete factors depends heavily on the problem. On the OpenMP executor, 3 sweeps usually give a decent approximation in our experiments, while GPU executors can take 10 or more iterations.

The ParlLU algorithm in Ginkgo follows the design of E. Chow and A. Patel, Fine-grained Parallel Incomplete LU Factorization, SIAM Journal on Scientific Computing, 37, C169-C193 (2015).

## **Template Parameters**

ValueType	Type of the values of all matrices used in this class
IndexType	Type of the indices of all matrices used in this class

## 46.176.2 Member Function Documentation

## 46.176.2.1 parse()

Create the parameters from the property tree.

Because this is directly tied to the specific type, the value/index type settings within config are ignored and type\_ descriptor is only used for children configs.

#### **Parameters**

config	the property tree for setting	
context	the registry	
td_for_child	the type descriptor for children configs. The default uses the value/index type of this class.	

#### Returns

parameters

The documentation for this class was generated from the following file:

• ginkgo/core/factorization/par\_ilu.hpp

# 46.177 gko::factorization::Parllut< ValueType, IndexType > Class Template Reference

ParILUT is an incomplete threshold-based LU factorization which is computed in parallel.

#include <ginkgo/core/factorization/par\_ilut.hpp>

#### **Static Public Member Functions**

static parameters\_type parse (const config::pnode &config, const config::registry &context, const config::type\_descriptor &td\_for\_child=config::make\_type\_descriptor < ValueType, IndexType >())

Create the parameters from the property\_tree.

#### **Additional Inherited Members**

#### 46.177.1 Detailed Description

template<typename ValueType = default\_precision, typename IndexType = int32> class gko::factorization::Parllut< ValueType, IndexType >

ParILUT is an incomplete threshold-based LU factorization which is computed in parallel.

L is a lower unitriangular, while U is an upper triangular matrix, which approximate a given matrix A with  $A \approx LU$ . Here, L and U have a sparsity pattern that is improved iteratively based on their element-wise magnitude. The initial sparsity pattern is chosen based on the ILU(0) factorization of A.

One iteration of the ParlLUT algorithm consists of the following steps:

- 1. Calculating the residual R = A LU
- 2. Adding new non-zero locations from R to L and U. The new non-zero locations are initialized based on the corresponding residual value.
- 3. Executing a fixed-point iteration on L and U according to  $F(L,U) = \begin{cases} \frac{1}{u_{jj}} \left( a_{ij} \sum_{k=1}^{j-1} l_{ik} u_{kj} \right), & i > j \\ a_{ij} \sum_{k=1}^{i-1} l_{ik} u_{kj}, & i \leq j \end{cases}$  For a more detailed description of the fixed-point iteration, see Parllu.
- 4. Removing the smallest entries (by magnitude) from  ${\cal L}$  and  ${\cal U}$
- 5. Executing a fixed-point iteration on the (now sparser) L and U

This ParlLUT algorithm thus improves the sparsity pattern and the approximation of L and U simultaneously.

The implementation follows the design of H. Anzt et al., ParlLUT - A Parallel Threshold ILU for GPUs, 2019 IEEE International Parallel and Distributed Processing Symposium (IPDPS), pp. 231–241.

## **Template Parameters**

ValueType	Type of the values of all matrices used in this class
IndexType	Type of the indices of all matrices used in this class

## 46.177.2 Member Function Documentation

#### 46.177.2.1 parse()

Create the parameters from the property\_tree.

Because this is directly tied to the specific type, the value/index type settings within config are ignored and type\_ descriptor is only used for children configs.

## **Parameters**

config	the property tree for setting	
context	the registry	
td_for_child	the type descriptor for children configs. The default uses the value/index type of this class.	

## Returns

parameters

The documentation for this class was generated from the following file:

• ginkgo/core/factorization/par\_ilut.hpp

# 46.178 gko::experimental::distributed::Partition< LocalIndexType, GlobalIndexType > Class Template Reference

Represents a partition of a range of indices [0, size) into a disjoint set of parts.

#include <ginkgo/core/distributed/partition.hpp>

#### **Public Member Functions**

· size\_type get\_size () const

Returns the total number of elements represented by this partition.

size\_type get\_num\_ranges () const noexcept

Returns the number of ranges stored by this partition.

comm\_index\_type get\_num\_parts () const noexcept

Returns the number of parts represented in this partition.

• comm\_index\_type get\_num\_empty\_parts () const noexcept

Returns the number of empty parts within this partition.

const global index type \* get range bounds () const noexcept

Returns the ranges boundary array stored by this partition.

const comm\_index\_type \* get\_part\_ids () const noexcept

Returns the part IDs of the ranges in this partition.

const local index type \* get range starting indices () const noexcept

Returns the part-local starting index for each range in this partition.

const local\_index\_type \* get\_part\_sizes () const noexcept

Returns the part size array.

· local index type get part size (comm index type part) const

Returns the size of a part given by its part ID.

· bool has connected parts () const

Checks if each part has no more than one contiguous range.

· bool has ordered parts () const

Checks if the ranges are ordered by their part index.

## **Static Public Member Functions**

• static std::unique\_ptr< Partition > build\_from\_mapping (std::shared\_ptr< const Executor > exec, const array< comm\_index\_type > &mapping, comm\_index\_type num\_parts)

Builds a partition from a given mapping global\_index -> part\_id.

static std::unique\_ptr< Partition > build\_from\_contiguous (std::shared\_ptr< const Executor > exec, const array< global\_index\_type > &ranges, const array< comm\_index\_type > &part\_ids={})

Builds a partition consisting of contiguous ranges, one for each part.

• static std::unique\_ptr< Partition > build\_from\_global\_size\_uniform (std::shared\_ptr< const Executor > exec, comm\_index\_type num\_parts, global\_index\_type global\_size)

Builds a partition by evenly distributing the global range.

## 46.178.1 Detailed Description

template<typename LocalIndexType = int32, typename GlobalIndexType = int64> class gko::experimental::distributed::Partition< LocalIndexType, GlobalIndexType >

Represents a partition of a range of indices [0, size) into a disjoint set of parts.

The partition is stored as a set of consecutive ranges [begin, end) with an associated part ID and local index (number of indices in this part before begin). Global indices are stored as 64 bit signed integers (int64), part-local indices use LocalIndexType, Part IDs use 32 bit signed integers (int).

For example, consider the interval [0, 13) that is partitioned into the following ranges: [0,3), [3,6), [6,8), [8,10), [10,13).

These ranges are distributed on three part with:

```
p_0 = [0, 3) + [6, 8) + [10, 13),

p_1 = [3, 6),

p_2 = [8, 10).
```

The part ids can be queried from the get\_part\_ids array, and the ranges are represented as offsets, accessed by get\_range\_bounds, leading to the offset array:

```
r = [0, 3, 6, 8, 10, 13]
```

so that individual ranges are given by [r[i], r[i+1]). Since each part may be associated with multiple ranges, it is possible to get the starting index for each range that is local to the owning part, see get\_range\_starting\_indices. These indices can be used to easily iterate over part local data. For example, the above partition has the following starting indices

```
starting_index[0] = 0,
starting_index[1] = 0,
starting_index[2] = 3,  // second range of part 0
starting_index[3] = 0,
starting_index[4] = 5,  // third range of part 0
```

which you can use to iterate only over the the second range of part 0 (the third global range) with

```
for(int i = 0; i < r[3] - r[2]; ++i){
  data[starting_index[2] + i] = val;
}</pre>
```

#### **Template Parameters**

LocalIndexType	The index type used for part-local indices. To prevent overflows, no single part's size ma exceed this index type's maximum value.	
GlobalIndexType	The index type used for the global indices. Needs to be at least as large a type as LocalIndexType.	

## 46.178.2 Member Function Documentation

## 46.178.2.1 build\_from\_contiguous()

Builds a partition consisting of contiguous ranges, one for each part.

#### **Parameters**

exec	the Executor on which the partition should be built
ranges	the boundaries of the ranges representing each part. Part part_id[i] contains the indices [ranges[i], ranges[i + 1]). Has to contain at least one element. The first element has to be 0.
part_ids	the part ids of the provided ranges. If empty, then it will assume range i belongs to part i.

#### Returns

a Partition representing the given contiguous partitioning.

## 46.178.2.2 build\_from\_global\_size\_uniform()

Builds a partition by evenly distributing the global range.

#### **Parameters**

ехес	the Executor on which the partition should be built
num_parts	the number of parst used in this partition
global_size	the global size of this partition

#### Returns

```
a Partition where each range has either floor(global_size/num_parts) or floor(global_↔ size/num_parts) + 1 indices.
```

## 46.178.2.3 build\_from\_mapping()

Builds a partition from a given mapping global\_index -> part\_id.

## **Parameters**

exec	the Executor on which the partition should be built
mapping	the mapping from global indices to part IDs.
num_parts	the number of parts used in the mapping.

#### Returns

a Partition representing the given mapping as a set of ranges

## 46.178.2.4 get\_num\_empty\_parts()

```
template<typename LocalIndexType = int32, typename GlobalIndexType = int64>
comm_index_type gko::experimental::distributed::Partition< LocalIndexType, GlobalIndexType >←
::get_num_empty_parts () const [inline], [noexcept]
```

Returns the number of empty parts within this partition.

#### Returns

number of empty parts.

```
126 {
127          return num_empty_parts_;
128 }
```

#### 46.178.2.5 get num parts()

```
template<typename LocalIndexType = int32, typename GlobalIndexType = int64>
comm_index_type gko::experimental::distributed::Partition< LocalIndexType, GlobalIndexType >
::get_num_parts ( ) const [inline], [noexcept]
```

Returns the number of parts represented in this partition.

## Returns

number of parts.

#### 46.178.2.6 get num ranges()

```
template<typename LocalIndexType = int32, typename GlobalIndexType = int64>
size_type gko::experimental::distributed::Partition< LocalIndexType, GlobalIndexType >::get_
num_ranges ( ) const [inline], [noexcept]
```

Returns the number of ranges stored by this partition.

This size refers to the data returned by <a href="mailto:get\_range\_bounds">get\_range\_bounds</a>().

#### Returns

number of ranges.

References gko::array< ValueType >::get\_size().

#### 46.178.2.7 get\_part\_ids()

```
template<typename LocalIndexType = int32, typename GlobalIndexType = int64>
const comm_index_type* gko::experimental::distributed::Partition< LocalIndexType, Global←
IndexType >::get_part_ids ( ) const [inline], [noexcept]
```

Returns the part IDs of the ranges in this partition.

For each range from get\_range\_bounds(), it stores the part ID in the interval [0, get\_num\_parts() - 1].

Returns

part ID array.

References gko::array< ValueType >::get\_const\_data().

#### 46.178.2.8 get\_part\_size()

Returns the size of a part given by its part ID.

Warning

Triggers a copy from device to host.

#### **Parameters**

```
part the part ID.
```

Returns

size of part.

## 46.178.2.9 get\_part\_sizes()

```
template<typename LocalIndexType = int32, typename GlobalIndexType = int64>
const local_index_type* gko::experimental::distributed::Partition< LocalIndexType, Global←
IndexType >::get_part_sizes ( ) const [inline], [noexcept]
```

Returns the part size array.

part\_sizes[p] stores the total number of indices in part p.

Returns

part size array.

References gko::array< ValueType >::get\_const\_data().

## 46.178.2.10 get\_range\_bounds()

```
template<typename LocalIndexType = int32, typename GlobalIndexType = int64>
const global_index_type* gko::experimental::distributed::Partition< LocalIndexType, Global←
IndexType >::get_range_bounds ( ) const [inline], [noexcept]
```

Returns the ranges boundary array stored by this partition.

 $range\_bounds[i]$  is the beginning (inclusive) and  $range\_bounds[i+1]$  is the end (exclusive) of the ith range.

#### Returns

range boundaries array.

References gko::array< ValueType >::get\_const\_data().

#### 46.178.2.11 get\_range\_starting\_indices()

```
template<typename LocalIndexType = int32, typename GlobalIndexType = int64>
const local_index_type* gko::experimental::distributed::Partition< LocalIndexType, Global←
IndexType >::get_range_starting_indices ( ) const [inline], [noexcept]
```

Returns the part-local starting index for each range in this partition.

```
Consider the partition on [0, 10) with p_1 = [0-4) + [7-10), p_2 = [4-7).
```

Then range\_starting\_indices[0] = 0, range\_starting\_indices[1] = 0, range\_ $\leftarrow$  starting\_indices[2] = 4.

#### Returns

part-local starting index array.

References gko::array< ValueType >::get const data().

## 46.178.2.12 get\_size()

```
template<typename LocalIndexType = int32, typename GlobalIndexType = int64>
size_type gko::experimental::distributed::Partition< LocalIndexType, GlobalIndexType >::get_
size () const [inline]
```

Returns the total number of elements represented by this partition.

#### Returns

number elements.

#### 46.178.2.13 has\_connected\_parts()

```
template<typename LocalIndexType = int32, typename GlobalIndexType = int64>
bool gko::experimental::distributed::Partition< LocalIndexType, GlobalIndexType >::has_←
connected_parts ( ) const
```

Checks if each part has no more than one contiguous range.

#### Returns

true if each part has no more than one contiguous range.

#### 46.178.2.14 has\_ordered\_parts()

```
template<typename LocalIndexType = int32, typename GlobalIndexType = int64>
bool gko::experimental::distributed::Partition< LocalIndexType, GlobalIndexType >::has_←
ordered_parts ( ) const
```

Checks if the ranges are ordered by their part index.

Implies that the partition is connected.

#### Returns

true if the ranges are ordered by their part index.

The documentation for this class was generated from the following files:

- · ginkgo/core/distributed/matrix.hpp
- · ginkgo/core/distributed/partition.hpp

## 46.179 gko::log::PerformanceHint Class Reference

PerformanceHint is a Logger which analyzes the performance of the application and outputs hints for unnecessary copies and allocations.

```
#include <ginkgo/core/log/performance_hint.hpp>
```

## **Public Member Functions**

· void print status () const

Writes out the cross-executor writes and allocations that have been stored so far.

## **Static Public Member Functions**

static std::unique\_ptr< PerformanceHint > create (std::ostream &os=std::cerr, size\_type allocation\_size\_
 — limit=16, size\_type copy\_size\_limit=16, size\_type histogram\_max\_size=1024)

Creates a PerformanceHint logger.

## 46.179.1 Detailed Description

PerformanceHint is a Logger which analyzes the performance of the application and outputs hints for unnecessary copies and allocations.

The specific patterns it checks for are:

- · repeated cross-executor copies from or to the same pointer
- · repeated allocation/free pairs of the same size

## 46.179.2 Member Function Documentation

#### 46.179.2.1 create()

```
static std::unique_ptr<PerformanceHint> gko::log::PerformanceHint::create (
    std::ostream & os = std::cerr,
    size_type allocation_size_limit = 16,
    size_type copy_size_limit = 16,
    size_type histogram_max_size = 1024 ) [inline], [static]
```

Creates a PerformanceHint logger.

This dynamically allocates the memory, constructs the object and returns an std::unique\_ptr to this object.

#### **Parameters**

os	the stream used for this logger	
allocation_size_limit   ignore allocations below this limit (bytes)		
copy_size_limit	ignore copies below this limit (bytes)	
histogram_max_size	how many allocation sizes and/or pointers to keep track of at most?	

#### Returns

an std::unique\_ptr to the the constructed object

The documentation for this class was generated from the following file:

• ginkgo/core/log/performance\_hint.hpp

## 46.180 gko::Permutable < IndexType > Class Template Reference

Linear operators which support permutation should implement the Permutable interface.

```
#include <ginkgo/core/base/lin_op.hpp>
```

#### **Public Member Functions**

- virtual std::unique\_ptr< LinOp > permute (const array< IndexType > \*permutation\_indices) const Returns a LinOp representing the symmetric row and column permutation of the Permutable object.
- virtual std::unique\_ptr< LinOp > inverse\_permute (const array< IndexType > \*permutation\_indices) const Returns a LinOp representing the symmetric inverse row and column permutation of the Permutable object.
- virtual std::unique\_ptr< LinOp > row\_permute (const array< IndexType > \*permutation\_indices) const =0

  Returns a LinOp representing the row permutation of the Permutable object.
- virtual std::unique\_ptr< LinOp > column\_permute (const array< IndexType > \*permutation\_indices) const
   =0

Returns a LinOp representing the column permutation of the Permutable object.

virtual std::unique\_ptr< LinOp > inverse\_row\_permute (const array< IndexType > \*permutation\_indices)
 const =0

Returns a LinOp representing the row permutation of the inverse permuted object.

virtual std::unique\_ptr< LinOp > inverse\_column\_permute (const array< IndexType > \*permutation\_← indices) const =0

Returns a LinOp representing the row permutation of the inverse permuted object.

## 46.180.1 Detailed Description

```
template < typename IndexType > class gko::Permutable < IndexType >
```

Linear operators which support permutation should implement the Permutable interface.

It provides functions to permute the rows and columns of a LinOp, independently or symmetrically, and with a regular or inverted permutation.

After a regular row permutation with permutation array perm the row i in the output LinOp contains the row perm[i] from the input LinOp. After an inverse row permutation, the row perm[i] in the output LinOp contains the row i from the input LinOp. Equivalently, after a column permutation, the output stores in column i the column perm[i] from the input, and an inverse column permutation stores in column perm[i] the column i from the input. A symmetric permutation is functionally equivalent to calling as<Permutable>(A->row\_ $\leftarrow$  permute (perm)) ->column\_permute (perm), but the implementation can provide better performance due to kernel fusion.

## 46.180.1.1 Example: Permuting a Csr matrix:

```
{c++}
//Permuting an object of LinOp type.
//The object you want to permute.
auto op = matrix::Csr::create(exec);
//Permute the object by first converting it to a Permutable type.
auto perm = op->row_permute(permutation_indices);
```

## 46.180.2 Member Function Documentation

## 46.180.2.1 column\_permute()

Returns a LinOp representing the column permutation of the Permutable object.

In the resulting LinOp, the column i contains the input column perm[i].

From the linear algebra perspective, with  $P_{ij} = \delta_{i\pi(i)}$ , this represents the operation  $AP^T$ .

## **Parameters**

normutation indicas	the array of indices containing the permutation order we are
permutation_indices	the array of indices containing the permutation order perm.

#### Returns

a pointer to the new column permuted object

Implemented in gko::matrix::Dense < ValueType >, gko::matrix::Dense < value\_type >, gko::matrix::Dense < ValueType >, gko::matrix::Dense < ValueType >, and gko::matrix::Csr < ValueType, IndexType >.

#### 46.180.2.2 inverse column permute()

Returns a LinOp representing the row permutation of the inverse permuted object.

In the resulting LinOp, the column perm[i] contains the input column i.

From the linear algebra perspective, with  $P_{ij} = \delta_{i\pi(i)}$ , this represents the operation  $AP^{-T}$ .

#### **Parameters**

	permutation_indices	the array of indices containing the permutation order perm.	
--	---------------------	---	--

#### Returns

a pointer to the new inverse permuted object

Implemented in gko::matrix::Dense < ValueType >, gko::matrix::Dense < value\_type >, gko::matrix::Dense < ValueType >, gko::matrix::Dense < ValueType >, and gko::matrix::Csr < ValueType, IndexType >.

#### 46.180.2.3 inverse\_permute()

Returns a LinOp representing the symmetric inverse row and column permutation of the Permutable object.

In the resulting LinOp, the entry at location (perm[i], perm[j]) contains the input value (i, j).

From the linear algebra perspective, with  $P_{ij} = \delta_{i\pi(i)}$ , this represents the operation  $P^{-1}AP^{-T}$ .

#### **Parameters**

permutation_indices	the array of indices containing the permutation order.
---------------------	--

#### Returns

a pointer to the new permuted object

## 46.180.2.4 inverse\_row\_permute()

Returns a LinOp representing the row permutation of the inverse permuted object.

In the resulting LinOp, the row perm[i] contains the input row i.

From the linear algebra perspective, with  $P_{ij} = \delta_{i\pi(i)}$ , this represents the operation  $P^{-1}A$ .

#### **Parameters**

	permutation_indices	the array of indices containing the permutation order perm.
--	---------------------	---

#### Returns

a pointer to the new inverse permuted object

Implemented in gko::matrix::Dense < ValueType >, gko::matrix::Dense < value\_type >, gko::matrix::Dense < ValueType >, gko::matrix::Dense < ValueType >, and gko::matrix::Csr < ValueType, IndexType >.

## 46.180.2.5 permute()

Returns a LinOp representing the symmetric row and column permutation of the Permutable object.

In the resulting LinOp, the entry at location (i,j) contains the input value (perm[i],perm[j]).

From the linear algebra perspective, with  $P_{ij} = \delta_{i\pi(i)}$ , this represents the operation  $PAP^T$ .

#### **Parameters**

permutation_ir	ndices	the array of indices containing the permutation order.

#### Returns

a pointer to the new permuted object

Reimplemented in gko::matrix::Dense < ValueType >, gko::matrix::Dense < value\_type >, gko::matrix::Dense < ValueType >, gko::matrix::Dense < ValueType >, and gko::matrix::Csr < ValueType, IndexType >.

## 46.180.2.6 row\_permute()

Returns a LinOp representing the row permutation of the Permutable object.

In the resulting LinOp, the row i contains the input row perm[i].

From the linear algebra perspective, with  $P_{ij} = \delta_{i\pi(i)}$ , this represents the operation PA.

#### **Parameters**

	permutation_indices	the array of indices containing the permutation order.	
--	---------------------	--	--

#### Returns

a pointer to the new permuted object

Implemented in gko::matrix::Dense < ValueType >, gko::matrix::Dense < value\_type >, gko::matrix::Dense < ValueType >, gko::matrix::Dense < ValueType >, and gko::matrix::Csr < ValueType, IndexType >.

The documentation for this class was generated from the following file:

• ginkgo/core/base/lin\_op.hpp

# 46.181 gko::matrix::Permutation < IndexType > Class Template Reference

Permutation is a matrix format that represents a permutation matrix, i.e.

```
#include <ginkgo/core/matrix/permutation.hpp>
```

## **Public Member Functions**

index\_type \* get\_permutation () noexcept

Returns a pointer to the array of permutation.

const index type \* get const permutation () const noexcept

Returns a pointer to the array of permutation.

size\_type get\_permutation\_size () const noexcept

Returns the number of elements explicitly stored in the permutation array.

• std::unique\_ptr< Permutation > compute\_inverse () const

Returns the inverse permutation.

std::unique\_ptr< Permutation > compose (ptr\_param< const Permutation > other) const

Composes this permutation with another permutation.

void write (gko::matrix\_data< value\_type, index\_type > &data) const override

Writes a matrix to a matrix\_data structure.

#### Static Public Member Functions

- static std::unique\_ptr< Permutation > create (std::shared\_ptr< const Executor > exec, size\_type size=0)

  Creates an uninitialized Permutation arrays on the specified executor.
- static std::unique\_ptr< Permutation > create (std::shared\_ptr< const Executor > exec, array< IndexType > permutation\_indices)

Creates a Permutation matrix from an already allocated (and initialized) row and column permutation arrays.

• static std::unique\_ptr< const Permutation > create\_const (std::shared\_ptr< const Executor > exec, size\_type size, gko::detail::const\_array\_view< IndexType > &&perm\_idxs, mask\_type enabled\_const\_permute=row permute)

Creates a constant (immutable) Permutation matrix from a constant array.

static std::unique\_ptr< const Permutation > create\_const (std::shared\_ptr< const Executor > exec, gko
 ::detail::const\_array\_view< IndexType > &&perm\_idxs)

Creates a constant (immutable) Permutation matrix from a constant array.

## 46.181.1 Detailed Description

```
template < typename IndexType = int32 > class gko::matrix::Permutation < IndexType >
```

Permutation is a matrix format that represents a permutation matrix, i.e.

a matrix where each row and column has exactly one entry. The matrix can only be applied to Dense inputs, where it represents a row permutation: A' = PA means A'(i, j) = A(p[i], j).

**Template Parameters** 

```
IndexType precision of permutation array indices.
```

#### 46.181.2 Member Function Documentation

## 46.181.2.1 compose()

Composes this permutation with another permutation.

The resulting permutation fulfills result[i] = this[other[i]] or result = other \* this from the matrix perspective, which is equivalent to first permuting by this and then by other: Combining permutations  $P_1$  and  $P_2$  with P = P\_1.combine(P\_2) performs the operation permute(A, P) = permute(permute(A, P\_1), P\_2).

#### **Parameters**

other	the other permutation
-------	-----------------------

#### Returns

the combined permutation

## 46.181.2.2 compute\_inverse()

```
template<typename IndexType = int32>
std::unique_ptr<Permutation> gko::matrix::Permutation< IndexType >::compute_inverse ( ) const
```

Returns the inverse permutation.

#### Returns

a newly created Permutation object storing the inverse permutation of this Permutation.

## 46.181.2.3 create() [1/2]

Creates a Permutation matrix from an already allocated (and initialized) row and column permutation arrays.

## **Parameters**

exec	Executor associated to the matrix
size	size of the permutation array.
permutation_indices	array of permutation array
enabled_permute	mask for the type of permutation to apply.

## Note

If permutation\_indices is not an rvalue, not an array of IndexType, or is on the wrong executor, an internal copy will be created, and the original array data will not be used in the matrix.

## Returns

A smart pointer to the newly created matrix.

#### 46.181.2.4 create() [2/2]

Creates an uninitialized Permutation arrays on the specified executor.

#### **Parameters**

```
exec Executor associated to the LinOp
```

#### Returns

A smart pointer to the newly created matrix.

## 46.181.2.5 create\_const() [1/2]

Creates a constant (immutable) Permutation matrix from a constant array.

#### **Parameters**

exec	the executor to create the matrix on
size	the size of the square matrix
perm_idxs	the permutation index array of the matrix
enabled_permute	the mask describing the type of permutation

## Returns

A smart pointer to the constant matrix wrapping the input array (if it resides on the same executor as the matrix) or a copy of the array on the correct executor.

#### 46.181.2.6 create\_const() [2/2]

```
size_type size,
gko::detail::const_array_view< IndexType > && perm_idxs,
mask_type enabled_permute = row_permute ) [static]
```

Creates a constant (immutable) Permutation matrix from a constant array.

#### **Parameters**

exec	the executor to create the matrix on
size	the size of the square matrix
perm_idxs	the permutation index array of the matrix
enabled_permute	the mask describing the type of permutation

#### Returns

A smart pointer to the constant matrix wrapping the input array (if it resides on the same executor as the matrix) or a copy of the array on the correct executor.

#### 46.181.2.7 get\_const\_permutation()

```
template<typename IndexType = int32>
const index_type* gko::matrix::Permutation < IndexType >::get_const_permutation ( ) const [inline],
[noexcept]
```

Returns a pointer to the array of permutation.

## Returns

the pointer to the row permutation array.

## Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

References gko::array< ValueType >::get\_const\_data().

### 46.181.2.8 get\_permutation()

```
template<typename IndexType = int32>
index_type* gko::matrix::Permutation< IndexType >::get_permutation ( ) [inline], [noexcept]
```

Returns a pointer to the array of permutation.

## Returns

the pointer to the row permutation array.

References gko::array< ValueType >::get\_data().

#### 46.181.2.9 get\_permutation\_size()

```
template<typename IndexType = int32>
size_type gko::matrix::Permutation< IndexType >::get_permutation_size ( ) const [noexcept]
```

Returns the number of elements explicitly stored in the permutation array.

#### Returns

the number of elements explicitly stored in the permutation array.

#### 46.181.2.10 write()

Writes a matrix to a matrix\_data structure.

#### **Parameters**

```
data the matrix_data structure
```

Implements gko::WritableToMatrixData< default\_precision, IndexType >.

The documentation for this class was generated from the following file:

• ginkgo/core/matrix/permutation.hpp

# 46.182 gko::Perturbation < ValueType > Class Template Reference

The Perturbation class can be used to construct a LinOp to represent the operation (identity + scalar \* basis \* projector).

```
#include <ginkgo/core/base/perturbation.hpp>
```

#### **Public Member Functions**

- const std::shared ptr< const LinOp > get basis () const noexcept
  - Returns the basis of the perturbation.
- const std::shared\_ptr< const LinOp > get\_projector () const noexcept

Returns the projector of the perturbation.

const std::shared\_ptr< const LinOp > get\_scalar () const noexcept

Returns the scalar of the perturbation.

#### Static Public Member Functions

• static std::unique\_ptr< Perturbation > create (std::shared\_ptr< const Executor > exec)

Creates an empty perturbation operator (0x0 operator).

static std::unique\_ptr< Perturbation > create (std::shared\_ptr< const LinOp > scalar, std::shared\_ptr< const LinOp > basis)

Creates a perturbation with scalar and basis by setting projector to the conjugate transpose of basis.

static std::unique\_ptr< Perturbation > create (std::shared\_ptr< const LinOp > scalar, std::shared\_ptr< const LinOp > basis, std::shared\_ptr< const LinOp > projector)

Creates a perturbation of scalar, basis and projector.

## 46.182.1 Detailed Description

```
template<typename ValueType = default_precision> class gko::Perturbation< ValueType >
```

The Perturbation class can be used to construct a LinOp to represent the operation (identity + scalar \* basis \* projector).

This operator adds a movement along a direction constructed by basis and projector on the LinOp. projector gives the coefficient of basis to decide the direction.

For example, the Householder matrix can be represented with the Perturbation operator as follows. If u is the Householder factor then we can generate the Householder transformation, H = (I - 2 u u\*). In this case, the parameters of Perturbation class are scalar = -2, basis = u, and projector = u\*.

#### **Template Parameters**

Note

the apply operations of Perturbation class are not thread safe

#### 46.182.2 Member Function Documentation

## 46.182.2.1 create() [1/3]

Creates an empty perturbation operator (0x0 operator).

#### **Parameters**

*exec* | Executor associated to the perturbation

#### Returns

A smart pointer to the newly created perturbation.

## 46.182.2.2 create() [2/3]

Creates a perturbation with scalar and basis by setting projector to the conjugate transpose of basis.

Basis must be transposable. Perturbation will throw gko::NotSupported if basis is not transposable.

#### **Parameters**

scalar	scaling of the movement
basis	the direction basis

#### Returns

A smart pointer to the newly created perturbation.

## 46.182.2.3 create() [3/3]

Creates a perturbation of scalar, basis and projector.

#### **Parameters**

scalar	scaling of the movement
basis	the direction basis
projector	decides the coefficient of basis

#### Returns

A smart pointer to the newly created perturbation.

#### 46.182.2.4 get\_basis()

```
template<typename ValueType = default_precision>
const std::shared_ptr<const LinOp> gko::Perturbation< ValueType >::get_basis ( ) const [inline],
[noexcept]
```

Returns the basis of the perturbation.

#### Returns

the basis of the perturbation

## 46.182.2.5 get\_projector()

```
template<typename ValueType = default_precision>
const std::shared_ptr<const LinOp> gko::Perturbation< ValueType >::get_projector ( ) const
[inline], [noexcept]
```

Returns the projector of the perturbation.

## Returns

the projector of the perturbation

## 46.182.2.6 get\_scalar()

```
template<typename ValueType = default_precision>
const std::shared_ptr<const LinOp> gko::Perturbation< ValueType >::get_scalar ( ) const [inline],
[noexcept]
```

Returns the scalar of the perturbation.

#### Returns

the scalar of the perturbation

The documentation for this class was generated from the following file:

ginkgo/core/base/perturbation.hpp

# 46.183 gko::multigrid::Pgm< ValueType, IndexType > Class Template Reference

Parallel graph match (Pgm) is the aggregate method introduced in the paper M.

#include <ginkgo/core/multigrid/pgm.hpp>

# **Public Member Functions**

- std::shared\_ptr< const LinOp > get\_system\_matrix () const Returns the system operator (matrix) of the linear system.
- IndexType \* get\_agg () noexcept
   Returns the aggregate group.
- const IndexType \* get\_const\_agg () const noexcept
   Returns the aggregate group.

#### **Static Public Member Functions**

static parameters\_type parse (const config::pnode &config, const config::registry &context, const config::type\_descriptor &td\_for\_child=config::make\_type\_descriptor < ValueType, IndexType >())

Create the parameters from the property\_tree.

# 46.183.1 Detailed Description

template<typename ValueType = default\_precision, typename IndexType = int32> class gko::multigrid::Pgm< ValueType, IndexType >

Parallel graph match (Pgm) is the aggregate method introduced in the paper M.

Naumov et al., "AmgX: A Library for GPU Accelerated Algebraic Multigrid and Preconditioned Iterative Methods". Current implementation only contains size = 2 version.

Pgm creates the aggregate group according to the matrix value not the structure. Pgm gives two steps (one-phase handshaking) to group the elements. 1: get the strongest neighbor of each unaggregated element. 2: group the elements whose strongest neighbor is each other. repeating until reaching the given conditions. After that, the un-aggregated elements are assigned to an aggregated group or are left alone.

#### **Template Parameters**

ValueType	precision of matrix elements	
IndexType	precision of matrix indexes	

#### 46.183.2 Member Function Documentation

### 46.183.2.1 get\_agg()

```
template<typename ValueType = default_precision, typename IndexType = int32>
IndexType* gko::multigrid::Pgm< ValueType, IndexType >::get_agg ( ) [inline], [noexcept]
```

Returns the aggregate group.

Aggregate group whose size is same as the number of rows. Stores the mapping information from row index to coarse row index. i.e., agg[row idx] = coarse row idx.

#### Returns

the aggregate group.

```
79 { return agg_.get_data(); }
```

References gko::array< ValueType >::get\_data().

#### 46.183.2.2 get const agg()

```
template<typename ValueType = default_precision, typename IndexType = int32>
const IndexType* gko::multigrid::Pgm< ValueType, IndexType >::get_const_agg ( ) const [inline],
[noexcept]
```

Returns the aggregate group.

Aggregate group whose size is same as the number of rows. Stores the mapping information from row index to coarse row index. i.e., agg[row\_idx] = coarse\_row\_idx.

#### Returns

the aggregate group.

#### Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

References gko::array< ValueType >::get\_const\_data().

#### 46.183.2.3 get\_system\_matrix()

```
template<typename ValueType = default_precision, typename IndexType = int32>
std::shared_ptr<const LinOp> gko::multigrid::Pgm< ValueType, IndexType >::get_system_matrix (
) const [inline]
```

Returns the system operator (matrix) of the linear system.

# Returns

the system operator (matrix)

#### 46.183.2.4 parse()

Create the parameters from the property\_tree.

Because this is directly tied to the specific type, the value/index type settings within config are ignored and type\_ descriptor is only used for children configs.

#### **Parameters**

config	the property tree for setting	
context	the registry	
td_for_child	the type descriptor for children configs. The default uses the value/index type of this class.	

#### Returns

parameters

The documentation for this class was generated from the following files:

- · ginkgo/core/distributed/matrix.hpp
- ginkgo/core/multigrid/pgm.hpp

# 46.184 gko::config::pnode Class Reference

pnode describes a tree of properties.

```
#include <ginkgo/core/config/property_tree.hpp>
```

# **Public Types**

· enum tag\_t

tag\_t is the indicator for the current node storage.

#### **Public Member Functions**

• pnode ()

Default constructor: create an empty node.

• pnode (bool boolean)

Constructor for bool.

template<typename T, std::enable\_if\_t< std::is\_integral< T >::value > \* = nullptr>
pnode (T integer)

Constructor for integer with all integer type.

• pnode (const std::string &str)

Constructor for string.

• pnode (const char \*str)

Constructor for char\* (otherwise, it will use bool)

• pnode (double real)

Constructor for double (and also float)

• pnode (const array type & array)

Constructor for array.

• pnode (const map\_type &map)

Constructor for map.

• operator bool () const noexcept

bool conversion.

tag\_t get\_tag () const

Get the current node tag.

• const array\_type & get\_array () const

Access the array stored in this property node.

const map\_type & get\_map () const

Access the map stored in this property node.

• bool get\_boolean () const

Access the boolean value stored in this property node.

- std::int64\_t get\_integer () const
- · double get real () const

Access the real floating point value stored in this property node.

const std::string & get\_string () const

Access the string stored in this property node.

· const pnode & get (const std::string &key) const

This function is to access the data under the map.

· const pnode & get (int index) const

This function is to access the data under the array.

# 46.184.1 Detailed Description

pnode describes a tree of properties.

A pnode can either be empty, hold a value (a string, integer, real, or bool), contain an array of pnode., or contain a mapping between strings and pnodes.

# 46.184.2 Constructor & Destructor Documentation

#### 46.184.2.1 pnode() [1/7]

Constructor for bool.

**Parameters** 

```
boolean the bool type value
```

# 46.184.2.2 pnode() [2/7]

Constructor for integer with all integer type.

# **Template Parameters**

```
T input type
```

#### **Parameters**

```
integer the integer type value
```

# 46.184.2.3 pnode() [3/7]

Constructor for string.

## **Parameters**

```
str string type value
```

# 46.184.2.4 pnode() [4/7]

Constructor for char\* (otherwise, it will use bool)

**Parameters** 

```
str | the string like "..."
```

# 46.184.2.5 pnode() [5/7]

Constructor for double (and also float)

#### **Parameters**

```
real the floating point type value
```

# 46.184.2.6 pnode() [6/7]

Constructor for array.

# **Parameters**

```
array an pnode array
```

#### 46.184.2.7 pnode() [7/7]

Constructor for map.

#### **Parameters**

<i>map</i>   a (string, pnode)-ma <sub>l</sub>	р
--	---

# 46.184.3 Member Function Documentation

# 46.184.3.1 get() [1/2]

This function is to access the data under the map.

It will throw error when it does not hold a map. When access non-existent key in the map, it will return an empty node.

#### **Parameters**

key	the key for the node of the map
-----	---------------------------------

# Returns

node. If the map does not have the key, return an empty node.

# 46.184.3.2 get() [2/2]

This function is to access the data under the array.

It will throw error when it does not hold an array or access out-of-bound index.

# **Parameters**

index	the node index in array
-------	-------------------------

# Returns

node.

#### 46.184.3.3 get\_array()

```
const array_type& gko::config::pnode::get_array ( ) const
```

Access the array stored in this property node.

Throws gko::InvalidStateError if the property node does not store an array.

Returns

the array

# 46.184.3.4 get\_boolean()

```
bool gko::config::pnode::get_boolean ( ) const
```

Access the boolean value stored in this property node.

Throws gko::InvalidStateError if the property node does not store a boolean value.

Returns

the boolean value

#### 46.184.3.5 get\_integer()

```
std::int64_t gko::config::pnode::get_integer ( ) const
```

• Access the integer value stored in this property node. Throws gko::InvalidStateError if the property node does not store an integer value.

Returns

the integer value

# 46.184.3.6 get\_map()

```
const map_type& gko::config::pnode::get_map ( ) const
```

Access the map stored in this property node.

Throws gko::InvalidStateError if the property node does not store a map.

Returns

the map

### 46.184.3.7 get\_real()

```
double gko::config::pnode::get_real ( ) const
```

Access the real floating point value stored in this property node.

Throws gko::InvalidStateError if the property node does not store a real value

Returns

the real floating point value

# 46.184.3.8 get\_string()

```
const std::string& gko::config::pnode::get_string ( ) const
```

Access the string stored in this property node.

Throws gko::InvalidStateError if the property node does not store a string.

Returns

the string

# 46.184.3.9 get\_tag()

```
tag_t gko::config::pnode::get_tag ( ) const
```

Get the current node tag.

Returns

the tag

# 46.184.3.10 operator bool()

```
gko::config::pnode::operator bool ( ) const [explicit], [noexcept]
```

bool conversion.

It's true if and only if it is not empty.

The documentation for this class was generated from the following file:

• ginkgo/core/config/property\_tree.hpp

# 46.185 gko::log::polymorphic object data Struct Reference

Struct representing PolymorphicObject related data.

#include <ginkgo/core/log/record.hpp>

# 46.185.1 Detailed Description

Struct representing PolymorphicObject related data.

The documentation for this struct was generated from the following file:

· ginkgo/core/log/record.hpp

# 46.186 gko::PolymorphicObject Class Reference

A PolymorphicObject is the abstract base for all "heavy" objects in Ginkgo that behave polymorphically.

```
#include <ginkgo/core/base/polymorphic_object.hpp>
```

#### **Public Member Functions**

- std::unique\_ptr< PolymorphicObject > create\_default (std::shared\_ptr< const Executor > exec) const Creates a new "default" object of the same dynamic type as this object.
- std::unique\_ptr< PolymorphicObject > create\_default () const

Creates a new "default" object of the same dynamic type as this object.

- std::unique\_ptr< PolymorphicObject > clone (std::shared\_ptr< const Executor > exec) const
   Creates a clone of the object.
- std::unique\_ptr< PolymorphicObject > clone () const

Creates a clone of the object.

• PolymorphicObject \* copy\_from (const PolymorphicObject \*other)

Copies another object into this object.

• template<typename Derived , typename Deleter >

 $std::enable\_if\_t < std::is\_base\_of < PolymorphicObject, std::decay\_t < Derived > >::value, PolymorphicObject > * copy\_from (std::unique\_ptr < Derived, Deleter > &&other)$ 

Moves another object into this object.

• template<typename Derived , typename Deleter >

 $std::enable\_if\_t < std::is\_base\_of < PolymorphicObject, std::decay\_t < Derived > >::value, PolymorphicObject > * copy\_from (const std::unique\_ptr < Derived, Deleter > &other)$ 

Copies another object into this object.

PolymorphicObject \* copy\_from (const std::shared\_ptr< const PolymorphicObject > &other)

Copies another object into this object.

PolymorphicObject \* move\_from (ptr\_param< PolymorphicObject > other)

Moves another object into this object.

PolymorphicObject \* clear ()

Transforms the object into its default state.

std::shared\_ptr< const Executor > get\_executor () const noexcept

Returns the Executor of the object.

# 46.186.1 Detailed Description

A PolymorphicObject is the abstract base for all "heavy" objects in Ginkgo that behave polymorphically.

It defines the basic utilities (copying moving, cloning, clearing the objects) for all such objects. It takes into account that these objects are dynamically allocated, managed by smart pointers, and used polymorphically. Additionally, it assumes their data can be allocated on different executors, and that they can be copied between those executors.

Note

Most of the public methods of this class should not be overridden directly, and are thus not virtual. Instead, there are equivalent protected methods (ending in <method\_name>\_impl) that should be overridden instead. This allows polymorphic objects to implement default behavior around virtual methods (parameter checking, type casting).

See also

EnablePolymorphicObject if you wish to implement a concrete polymorphic object and have sensible defaults generated automatically. EnableAbstractPolymorphicObject if you wish to implement a new abstract polymorphic object, and have the return types of the methods updated to your type (instead of having them return PolymorphicObject).

#### 46.186.2 Member Function Documentation

# 46.186.2.1 clear()

```
PolymorphicObject* gko::PolymorphicObject::clear ( ) [inline]
```

Transforms the object into its default state.

Equivalent to this->copy\_from(this->create\_default()).

See also

clear\_impl() when implementing this method

Returns

this

### 46.186.2.2 clone() [1/2]

```
std::unique_ptr<PolymorphicObject> gko::PolymorphicObject::clone ( ) const [inline]
```

Creates a clone of the object.

This is a shorthand for clone(std::shared\_ptr<const Executor>) that uses the executor of this object to construct the new object.

#### Returns

A clone of the LinOp.

# 46.186.2.3 clone() [2/2]

Creates a clone of the object.

This is the polymorphic equivalent of the *executor copy constructor* decltype (\*this) (exec, this).

#### **Parameters**

```
exec the executor where the clone will be created
```

# Returns

A clone of the LinOp.

References create\_default().

# 46.186.2.4 copy\_from() [1/4]

Copies another object into this object.

This is the polymorphic equivalent of the copy assignment operator.

# See also

```
copy_from_impl(const PolymorphicObject *)
```

#### **Parameters**

other	the object to copy
-------	--------------------

Returns

this

Referenced by copy\_from().

# 46.186.2.5 copy\_from() [2/4]

Copies another object into this object.

This is the polymorphic equivalent of the copy assignment operator.

See also

copy\_from\_impl(const PolymorphicObject \*)

# **Parameters**

other the object to cop	y
-------------------------	---

Returns

this

References copy\_from().

# 46.186.2.6 copy\_from() [3/4]

Copies another object into this object.

This is the polymorphic equivalent of the copy assignment operator.

See also

copy\_from\_impl(const PolymorphicObject \*)

#### **Parameters**

# Returns

this

# **Template Parameters**

De	erived	the actual pointee type of the parameter, it needs to be derived from PolymorphicObject.
D	eleter	the deleter of the unique_ptr parameter

References copy\_from().

# 46.186.2.7 copy\_from() [4/4]

Moves another object into this object.

This is the polymorphic equivalent of the move assignment operator.

#### See also

copy\_from\_impl(std::unique\_ptr<PolymorphicObject>)

#### **Parameters**

other the object to mov
-------------------------

#### Returns

this

# **Template Parameters**

	Derived	the actual pointee type of the parameter, it needs to be derived from PolymorphicObject.
Ī	Deleter	the deleter of the unique_ptr parameter

# 46.186.2.8 create\_default() [1/2]

```
std::unique_ptr<PolymorphicObject> gko::PolymorphicObject::create_default ( ) const [inline]
```

Creates a new "default" object of the same dynamic type as this object.

This is a shorthand for create\_default(std::shared\_ptr<const Executor>) that uses the executor of this object to construct the new object.

#### Returns

a polymorphic object of the same type as this

Referenced by clone().

# 46.186.2.9 create\_default() [2/2]

Creates a new "default" object of the same dynamic type as this object.

This is the polymorphic equivalent of the executor default constructor decltype (\*this) (exec);.

#### **Parameters**

```
exec the executor where the object will be created
```

#### Returns

a polymorphic object of the same type as this

### 46.186.2.10 get\_executor()

```
std::shared_ptr<const Executor> gko::PolymorphicObject::get_executor ( ) const [inline],
[noexcept]
```

Returns the Executor of the object.

#### Returns

**Executor** of the object

Referenced by gko::preconditioner::lc< LSolverType, IndexType >::conj\_transpose(), gko::preconditioner::llu< LSolverType, USolverType, ReverseApply, IndexType >::conj\_transpose(), gko::preconditioner::lc< LSolver Type, IndexType >::lc(), gko::preconditioner::llu< LSolverType, USolverType, ReverseApply, IndexType >:: LSolverType, IndexType >::coperator=(), gko::preconditioner::lc< LSolverType, IndexType >::coperator=(), gko::preconditioner::llu< LSolverType, USolverType, ReverseApply, IndexType >::coperator=(), gko::matrix::Csr< ValueType, IndexType >::scale(), gko::preconditioner::lc< LSolverType, IndexType >::transpose(), and gko::preconditioner::llu< LSolverType, USolverType, ReverseApply, IndexType >::transpose().

### 46.186.2.11 move\_from()

Moves another object into this object.

This is the polymorphic equivalent of the move assignment operator.

See also

```
move_from_impl(PolymorphicObject *)
```

#### **Parameters**

other	the object to move from
-------	-------------------------

#### Returns

this

References gko::ptr\_param< T >::get().

The documentation for this class was generated from the following file:

· ginkgo/core/base/polymorphic object.hpp

# 46.187 gko::precision\_reduction Class Reference

This class is used to encode storage precisions of low precision algorithms.

```
#include <ginkgo/core/base/types.hpp>
```

# **Public Types**

using storage\_type = uint8

The underlying datatype used to store the encoding.

#### **Public Member Functions**

constexpr precision\_reduction () noexcept

Creates a default precision\_reduction encoding.

- constexpr precision\_reduction (storage\_type preserving, storage\_type nonpreserving) noexcept Creates a precision\_reduction encoding with the specified number of conversions.
- · constexpr operator storage\_type () const noexcept

Extracts the raw data of the encoding.

constexpr storage\_type get\_preserving () const noexcept

Returns the number of preserving conversions in the encoding.

constexpr storage\_type get\_nonpreserving () const noexcept

Returns the number of non-preserving conversions in the encoding.

#### Static Public Member Functions

- constexpr static precision\_reduction autodetect () noexcept
   Returns a special encoding which instructs the algorithm to automatically detect the best precision.
- constexpr static precision\_reduction common (precision\_reduction x, precision\_reduction y) noexcept

  Returns the common encoding of input encodings.

# 46.187.1 Detailed Description

This class is used to encode storage precisions of low precision algorithms.

Some algorithms in Ginkgo can improve their performance by storing parts of the data in lower precision, while doing computation in full precision. This class is used to encode the precisions used to store the data. From the user's perspective, some algorithms can provide a parameter for fine-tuning the storage precision. Commonly, the special value returned by <a href="mailto:precision\_reduction::autodetect">precision\_reduction::autodetect</a>() should be used to allow the algorithm to automatically choose an appropriate value, though manually selected values can be used for fine-tuning.

In general, a lower precision floating point value can be obtained by either dropping some of the insignificant bits of the significand (keeping the same number of exponent bits, and thus preserving the range of representable values) or using one of the hardware or software supported conversions between IEEE formats, such as double to float or float to half (reducing both the number of exponent, as well as significand bits, and thus decreasing the range of representable values).

The precision\_reduction class encodes the lower precision format relative to the base precision used and the algorithm in question. The encoding is done by specifying the amount of range non-preserving conversions and the amount of range preserving conversions that should be done on the base precision to obtain the lower precision format. For example, starting with a double precision value (11 exp, 52 sig. bits), the encoding specifying 1 non-preserving conversion and 1 preserving conversion would first use a hardware-supported non-preserving conversion to obtain a single precision value (8 exp, 23 sig. bits), followed by a preserving bit truncation to obtain a value with 8 exponent and 7 significand bits. Note that non-preserving conversion are always done first, as preserving conversions usually result in datatypes that are not supported by builtin conversions (thus, it is generally not possible to apply a non-preserving conversion to the result of a preserving conversion).

If the specified conversion is not supported by the algorithm, it will most likely fall back to using full precision for storing the data. Refer to the documentation of specific algorithms using this class for details about such special cases.

#### 46.187.2 Constructor & Destructor Documentation

# 46.187.2.1 precision\_reduction() [1/2]

```
constexpr gko::precision_reduction::precision_reduction ( ) [inline], [constexpr], [noexcept]
```

Creates a default precision reduction encoding.

This encoding represents the case where no conversions are performed.

Referenced by common().

## 46.187.2.2 precision\_reduction() [2/2]

Creates a precision\_reduction encoding with the specified number of conversions.

#### **Parameters**

preserving	the number of range preserving conversion
nonpreserving	the number of range non-preserving conversions

# 46.187.3 Member Function Documentation

#### 46.187.3.1 autodetect()

```
constexpr static precision_reduction gko::precision_reduction::autodetect ( ) [inline], [static],
[constexpr], [noexcept]
```

Returns a special encoding which instructs the algorithm to automatically detect the best precision.

#### Returns

a special encoding instructing the algorithm to automatically detect the best precision.

#### 46.187.3.2 common()

Returns the common encoding of input encodings.

The common encoding is defined as the encoding that does not have more preserving, nor non-preserving conversions than the input encodings.

# **Parameters**

X	an encoding
У	an encoding

## Returns

the common encoding of x and y

References precision\_reduction().

#### 46.187.3.3 get\_nonpreserving()

```
constexpr storage_type gko::precision_reduction::get_nonpreserving ( ) const [inline], [constexpr],
[noexcept]
```

Returns the number of non-preserving conversions in the encoding.

#### Returns

the number of non-preserving conversions in the encoding.

# 46.187.3.4 get\_preserving()

```
constexpr storage_type gko::precision_reduction::get_preserving ( ) const [inline], [constexpr],
[noexcept]
```

Returns the number of preserving conversions in the encoding.

#### Returns

the number of preserving conversions in the encoding.

#### 46.187.3.5 operator storage\_type()

```
constexpr gko::precision_reduction::operator storage_type ( ) const [inline], [constexpr],
[noexcept]
```

Extracts the raw data of the encoding.

# Returns

the raw data of the encoding

The documentation for this class was generated from the following file:

· ginkgo/core/base/types.hpp

# 46.188 gko::Preconditionable Class Reference

A LinOp implementing this interface can be preconditioned.

```
#include <ginkgo/core/base/lin_op.hpp>
```

#### **Public Member Functions**

- virtual std::shared\_ptr< const LinOp > get\_preconditioner () const
   Returns the preconditioner operator used by the Preconditionable.
- virtual void set\_preconditioner (std::shared\_ptr< const LinOp > new\_precond)

Sets the preconditioner operator used by the Preconditionable.

# 46.188.1 Detailed Description

A LinOp implementing this interface can be preconditioned.

#### 46.188.2 Member Function Documentation

#### 46.188.2.1 get\_preconditioner()

```
virtual std::shared_ptr<const LinOp> gko::Preconditionable::get_preconditioner ( ) const
[inline], [virtual]
```

Returns the preconditioner operator used by the Preconditionable.

# Returns

the preconditioner operator used by the Preconditionable

Referenced by gko::solver::EnablePreconditionable< Bicg< ValueType > >::operator=().

# 46.188.2.2 set\_preconditioner()

Sets the preconditioner operator used by the Preconditionable.

## **Parameters**

```
new_precond the new preconditioner operator used by the Preconditionable
```

The documentation for this class was generated from the following file:

ginkgo/core/base/lin\_op.hpp

# 46.189 gko::log::ProfilerHook Class Reference

This Logger can be used to annotate the execution of Ginkgo functionality with profiler-specific ranges.

#include <ginkgo/core/log/profiler\_hook.hpp>

#### Classes

· class NestedSummaryWriter

Receives the results from ProfilerHook::create\_nested\_summary().

class SummaryWriter

Receives the results from ProfilerHook::create\_summary().

class TableSummaryWriter

Writes the results from ProfilerHook::create\_summary() and ProfilerHook::create\_nested\_summary() to a ASCII table in Markdown format.

#### **Public Member Functions**

void set\_object\_name (ptr\_param < const PolymorphicObject > obj, std::string name)

Sets the name for an object to be profiled.

void set synchronization (bool synchronize)

Should the events call executor->synchronize on operations and copy/allocation? This leads to a certain overhead, but makes the execution timeline of kernels synchronous.

profiling\_scope\_guard user\_range (const char \*name) const

Creates a scope guard for a user-defined range to be included in the profile.

#### Static Public Member Functions

static std::shared ptr< ProfilerHook > create tau (bool initialize=true)

Creates a logger annotating Ginkgo events with TAU ranges via PerfStubs.

static std::shared\_ptr< ProfilerHook > create\_vtune ()

Creates a logger annotating Ginkgo events with VTune ITT ranges.

static std::shared\_ptr< ProfilerHook > create\_nvtx (uint32 color\_argb=color\_yellow\_argb)

Creates a logger annotating Ginkgo events with NVTX ranges for CUDA.

static std::shared\_ptr< ProfilerHook > create\_roctx ()

Creates a logger annotating Ginkgo events with ROCTX ranges for HIP.

static std::shared\_ptr< ProfilerHook > create\_for\_executor (std::shared\_ptr< const Executor > exec)

Creates a logger annotating Ginkgo events with the most suitable backend for the given executor: NVTX for NSight Systems in CUDA, ROCTX for rocprof in HIP, TAU for everything else.

static std::shared\_ptr< ProfilerHook > create\_summary (std::shared\_ptr< Timer > timer=std::make\_←
 shared< CpuTimer >(), std::unique\_ptr< SummaryWriter > writer=std::make\_unique< TableSummaryWriter
 >(), bool debug\_check\_nesting=false)

Creates a logger measuring the runtime of Ginkgo events and printing a summary when it is destroyed.

static std::shared\_ptr< ProfilerHook > create\_nested\_summary (std::shared\_ptr< Timer > timer=std
 ::make\_shared< CpuTimer >(), std::unique\_ptr< NestedSummaryWriter > writer=std::make\_unique
 TableSummaryWriter >(), bool debug\_check\_nesting=false)

Creates a logger measuring the runtime of Ginkgo events in a nested fashion and printing a summary when it is destroyed.

static std::shared\_ptr< ProfilerHook > create\_custom (hook\_function begin, hook\_function end)

Creates a logger annotating Ginkgo events with a custom set of functions for range begin and end.

#### **Static Public Attributes**

constexpr static uint32 color\_yellow\_argb = 0xFFFCB05U
 The Ginkgo yellow background color as packed 32 bit ARGB value.

# 46.189.1 Detailed Description

This Logger can be used to annotate the execution of Ginkgo functionality with profiler-specific ranges.

It currently supports TAU, VTune, NSightSystems (NVTX) and rocPROF(ROCTX) and custom profiler hooks.

The Logger should be attached to the Executor that is being used to run the application for a full, program-wide annotation, or to individual objects to only highlight events caused directly by them (not operations and memory allocations though)

#### 46.189.2 Member Function Documentation

#### 46.189.2.1 create nested summary()

Creates a logger measuring the runtime of Ginkgo events in a nested fashion and printing a summary when it is destroyed.

# Parameters

timer	The timer used to record time points.
writer	The NestedSummaryWriter to receive the performance results.
debug_check_nesting	Enable this flag if the output looks like it might contain incorrect nesting. This increases the overhead slightly, but recognizes mismatching push/pop pairs on the range stack.

# Note

For this logger to provide reliable GPU timings, either use Timer::create\_for\_executor or enable synchronization via set\_synchronization (true).

#### 46.189.2.2 create nvtx()

Creates a logger annotating Ginkgo events with NVTX ranges for CUDA.

#### **Parameters**

color_argb	The color of the NVTX ranges in the NSight Systems output. It has to be a 32 bit packed ARGB	]
	value.	

#### 46.189.2.3 create\_summary()

Creates a logger measuring the runtime of Ginkgo events and printing a summary when it is destroyed.

#### **Parameters**

timer	The timer used to record time points.
writer	The SummaryWriter to receive the performance results.
debug_check_nesting	Enable this flag if the output looks like it might contain incorrect nesting. This increases the overhead slightly, but recognizes mismatching push/pop pairs on the range stack.

#### Note

For this logger to provide reliable GPU timings, either use Timer::create\_for\_executor or enable synchronization via set\_synchronization (true).

#### 46.189.2.4 create\_tau()

Creates a logger annotating Ginkgo events with TAU ranges via PerfStubs.

# **Parameters**

initialize Should we call TAU's initialization and finalization functions, or does the application take care of it? The initialization will happen immediately, the finalization at program exit.

# 46.189.2.5 set\_object\_name()

Sets the name for an object to be profiled.

Every instance of that object in the profile will be replaced by the name instead of its runtime type.

#### **Parameters**

obj	the object
name	its name

# 46.189.2.6 user\_range()

Creates a scope guard for a user-defined range to be included in the profile.

#### **Parameters**

name	the name of the range
------	-----------------------

#### Returns

the scope guard. It will begin a range immediately and end it at the end of its scope.

The documentation for this class was generated from the following file:

• ginkgo/core/log/profiler\_hook.hpp

# 46.190 gko::log::profiling\_scope\_guard Class Reference

Scope guard that annotates its scope with the provided profiler hooks.

```
#include <ginkgo/core/log/profiler_hook.hpp>
```

# **Public Member Functions**

• profiling\_scope\_guard ()

Creates an empty (moved-from) scope guard.

• profiling\_scope\_guard (const char \*name, profile\_event\_category category, ProfilerHook::hook\_function begin, ProfilerHook::hook\_function end)

Creates the scope guard.

~profiling\_scope\_guard ()

Calls the range end function if the scope guard was not moved from.

# 46.190.1 Detailed Description

Scope guard that annotates its scope with the provided profiler hooks.

# 46.190.2 Constructor & Destructor Documentation

# 46.190.2.1 profiling\_scope\_guard()

Creates the scope guard.

#### **Parameters**

name	the name of the profiler range
category	the category of the profiler range
begin	the hook function to begin a range
end	the hook function to end a range

The documentation for this class was generated from the following file:

• ginkgo/core/log/profiler\_hook.hpp

# 46.191 gko::ptr\_param< T > Class Template Reference

This class is used for function parameters in the place of raw pointers.

```
#include <ginkgo/core/base/utils_helper.hpp>
```

#### **Public Member Functions**

```
    ptr_param (T *ptr)
        Initializes the ptr_param from a raw pointer.
```

```
• template<typename U , std::enable_if_t< std::is_base_of< T, U >::value > * = nullptr> ptr_param (const std::shared_ptr< U > &ptr)
```

Initializes the ptr\_param from a shared\_ptr.

template<typename U , typename Deleter , std::enable\_if\_t< std::is\_base\_of< T, U >::value > \* = nullptr> ptr\_param (const std::unique\_ptr< U, Deleter > &ptr)

Initializes the ptr\_param from a unique\_ptr.

```
    template < typename U , std::enable_if_t < std::is_base_of < T, U >::value > * = nullptr>
    ptr_param (const ptr_param < U > &ptr)
    Initializes the ptr_param from a ptr_param of a derived type.
```

- T & operator\* () const
- T \* operator-> () const
- T \* get () const
- · operator bool () const

# 46.191.1 Detailed Description

```
template < typename T> class gko::ptr_param < T>
```

This class is used for function parameters in the place of raw pointers.

Pointer parameters should be used for everything that does not involve transfer of ownership. It can be converted to from raw pointers, shared pointers and unique pointers of the specified type or any derived type. This allows functions to be called without having to use gko::lend or calling .get() for every pointer argument. It probably has no use outside of function parameters, as it is immutable.

## **Template Parameters**

```
T the pointed-to type
```

## 46.191.2 Member Function Documentation

#### 46.191.2.1 get()

```
template<typename T>
T* gko::ptr_param< T >::get ( ) const [inline]
```

## Returns

the underlying pointer.

Referenced by gko::as(), gko::Executor::copy\_from(), gko::matrix::Diagonal < ValueType >::inverse\_apply(), gko::PolymorphicObject::move\_from(), gko::ptr\_param < T >::ptr\_param(), and gko::matrix::Diagonal < ValueType >  $\leftarrow$  ::rapply().

# 46.191.2.2 operator bool()

```
template<typename T>
gko::ptr_param< T >::operator bool ( ) const [inline], [explicit]
```

#### Returns

true iff the underlying pointer is non-null.

#### 46.191.2.3 operator\*()

```
template<typename T>
T& gko::ptr_param< T >::operator* ( ) const [inline]
```

#### Returns

a reference to the underlying pointee.

#### 46.191.2.4 operator->()

```
template<typename T>
T* gko::ptr_param< T >::operator-> ( ) const [inline]
```

#### Returns

the underlying pointer.

The documentation for this class was generated from the following file:

ginkgo/core/base/utils\_helper.hpp

# 46.192 gko::range< Accessor > Class Template Reference

A range is a multidimensional view of the memory.

```
#include <ginkgo/core/base/range.hpp>
```

# **Public Types**

• using accessor = Accessor

The type of the underlying accessor.

# **Public Member Functions**

∼range ()=default

Use the default destructor.

template<typename... AccessorParams, typename = std::enable\_if\_t< sizeof...(AccessorParams) != 1 || !std::is\_same< range, std
 ::decay<detail::head\_t<AccessorParams...>>>::value>>
 constexpr range (AccessorParams &&... params)

Creates a new range.

• template<typename... DimensionTypes>

constexpr auto operator() (DimensionTypes &&... dimensions) const -> decltype(std::declval< accessor >()(std::forward< DimensionTypes >(dimensions)...))

Returns a value (or a sub-range) with the specified indexes.

• template<typename OtherAccessor >

const range & operator= (const range< OtherAccessor > &other) const

• const range & operator= (const range &other) const

Assigns another range to this range.

• constexpr size\_type length (size\_type dimension) const

Returns the length of the specified dimension of the range.

• constexpr const accessor \* operator-> () const noexcept

Returns a pointer to the accessor.

· constexpr const accessor & get\_accessor () const noexcept

`Returns a reference to the accessor.

#### **Static Public Attributes**

• static constexpr size\_type dimensionality = accessor::dimensionality

The number of dimensions of the range.

# 46.192.1 Detailed Description

```
template<typename Accessor> class gko::range< Accessor>
```

A range is a multidimensional view of the memory.

The range does not store any of its values by itself. Instead, it obtains the values through an accessor (e.g. accessor::row\_major) which describes how the indexes of the range map to physical locations in memory.

There are several advantages of using ranges instead of plain memory pointers:

- 1. Code using ranges is easier to read and write, as there is no need for index linearizations.
- 2. Code using ranges is safer, as it is impossible to accidentally miscalculate an index or step out of bounds, since range accessors perform bounds checking in debug builds. For performance, this can be disabled in release builds by defining the NDEBUG flag.
- 3. Ranges enable generalized code, as algorithms can be written independent of the memory layout. This does not impede various optimizations based on memory layout, as it is always possible to specialize algorithms for ranges with specific memory layouts.
- 4. Ranges have various pointwise operations predefined, which reduces the amount of loops that need to be written.

# 46.192.1.1 Range operations

Ranges define a complete set of pointwise unary and binary operators which extend the basic arithmetic operators in C++, as well as a few pointwise operations and mathematical functions useful in ginkgo, and a couple of non-pointwise operations. Compound assignment (+=, \*=, etc.) is not yet supported at this moment. Here is a complete list of operations:

- standard unary operations: +, -, !,  $\sim$
- standard binary operations: +, \* (this is pointwise, not matrix multiplication), /, %, <, >, <=, >=, ==, !=, ||, & &, |, &, ^, <<, >>
- useful unary functions: zero, one, abs, real, imag, conj, squared\_norm
- useful binary functions: min, max

All binary pointwise operations also work as expected if one of the operands is a scalar and the other is a range. The scalar operand will have the effect as if it was a range of the same size as the other operand, filled with the specified scalar.

Two "global" functions transpose and mmul are also supported. transpose transposes the first two dimensions of the range (i.e. transpose (r) (i, j, ...) == r(j, i, ...)). mmul performs a (batched) matrix multiply of the ranges - the first two dimensions represent the matrices, while the rest represent the batch. For example, given the ranges r1 and r2 of dimensions (3, 2, 3) and (2, 4, 3), respectively, mmul (r1, r2) will return a range of dimensions (3, 4, 3), obtained by multiplying the 3 frontal slices of the range, and stacking the result back vertically.

#### 46.192.1.2 Compound operations

Multiple range operations can be combined into a single expression. For example, an "axpy" operation can be obtained using y = alpha \* x + y, where x an y are ranges, and alpha is a scalar. Range operations are optimized for memory access, and the above code does not allocate additional storage for intermediate ranges alpha \* x or alpha \* x + y. In fact, the entire computation is done during the assignment, and the results of operations + and \* only register the data, and the types of operations that will be computed once the results are needed.

It is possible to store and reuse these intermediate expressions. The following example will overwrite the range  $\mathbf{x}$  with it's 4th power:

```
{c++} auto square = x * x; // this is range constructor, not range assignment! x = \text{square}; // overwrites x with x*x (this is range assignment) x = \text{square}; // overwrites new x (x*x) with (x*x)*(x*x) (as is this)
```

#### 46.192.1.3 Caveats

\_mmul is not a highly-optimized BLAS-3 version of the matrix multiplication.\_\_ The current design of ranges and accessors prevents that, so if you need a high-performance matrix multiplication, you should use one of the libraries that provide that, or implement your own (you can use pointwise range operations to help simplify that). However, range design might get improved in the future to allow efficient implementations of BLAS-3 kernels.

Aliasing the result range in mmul and transpose is not allowed. Constructs like A = transpose(A), A = mmul(A, A), or A = mmul(A, A) + C lead to undefined behavior. However, aliasing input arguments is allowed: C = mmul(A, A), and even C = mmul(A, A) + C is valid code (in the last example, only pointwise operations are aliased). C = mmul(A, A + C) is not valid though.

## 46.192.1.4 Examples

The range unit tests in core/test/base/range.cpp contain lots of simple 1-line examples of range operations. The accessor unit tests in core/test/base/range.cpp show how to use ranges with concrete accessors, and how to use range slices using spans as arguments to range function call operator. Finally, examples/range contains a complete example where ranges are used to implement a simple version of the right-looking LU factorization.

**Template Parameters** 

```
Accessor underlying accessor of the range
```

#### 46.192.2 Constructor & Destructor Documentation

#### 46.192.2.1 range()

Creates a new range.

# **Template Parameters**

#### **Parameters**

params	parameters forwarded to Accessor constructor.	
329 330 {}	: accessor_{std::forward <accessorparams>(params)</accessorparams>	. }

# 46.192.3 Member Function Documentation

# 46.192.3.1 get\_accessor()

```
template<typename Accessor>
constexpr const accessor& gko::range< Accessor >::get_accessor ( ) const [inline], [constexpr],
[noexcept]
```

`Returns a reference to the accessor.

#### Returns

reference to the accessor

Referenced by gko::range < Accessor >::operator=().

# 46.192.3.2 length()

Returns the length of the specified dimension of the range.

# **Parameters**

dimension	the dimensions whose length is returned
aimension	the dimensions whose length is returned

#### Returns

the length of the  ${\tt dimension}\text{-th}$  dimension of the range

Referenced by gko::matrix\_data< ValueType, IndexType >::matrix\_data().

#### 46.192.3.3 operator()()

Returns a value (or a sub-range) with the specified indexes.

#### **Template Parameters**

DimensionTypes	The types of indexes. Supported types depend on the underlying accessor, but are usually
	either integer types or spans. If at least one index is a span, the returned value will be a
	sub-range.

#### **Parameters**

dimensions	the indexes of the values.
------------	----------------------------

#### Returns

```
a value on position (dimensions...).
```

References gko::range < Accessor >::dimensionality.

# 46.192.3.4 operator->()

```
template<typename Accessor>
constexpr const accessor* gko::range< Accessor >::operator-> ( ) const [inline], [constexpr],
[noexcept]
```

Returns a pointer to the accessor.

Can be used to access data and functions of a specific accessor.

## Returns

pointer to the accessor

#### 46.192.3.5 operator=() [1/2]

Assigns another range to this range.

The order of assignment is defined by the accessor of this range, thus the memory access will be optimized for the resulting range, and not for the other range. If the sizes of two ranges do not match, the result is undefined. Sizes of the ranges are checked at runtime in debug builds.

#### Note

Temporary accessors are allowed to define the implementation of the assignment as deleted, so do not expect r1 \* r2 = r2 to work.

#### **Parameters**

other	the range to copy the data from
-------	---------------------------------

References gko::range < Accessor >::get\_accessor().

# 46.192.3.6 operator=() [2/2]

This is a version of the function which allows to copy between ranges of different accessors.

# **Template Parameters**

OtherAccessor   accessor of the other range
---

The documentation for this class was generated from the following file:

• ginkgo/core/base/range.hpp

# 46.193 gko::syn::range< Start, End, Step > Struct Template Reference

range records start, end, step in template

#include <ginkgo/core/synthesizer/containers.hpp>

# 46.193.1 Detailed Description

```
template<int Start, int End, int Step = 1>
struct gko::syn::range< Start, End, Step >
```

range records start, end, step in template

# **Template Parameters**

Start	start of range
End	end of range
Step	step of range. default is 1

The documentation for this struct was generated from the following file:

ginkgo/core/synthesizer/containers.hpp

# 46.194 gko::experimental::reorder::Rcm< IndexType > Class Template Reference

Rcm (Reverse Cuthill-McKee) is a reordering algorithm minimizing the bandwidth of a matrix.

#include <ginkgo/core/reorder/rcm.hpp>

#### **Public Member Functions**

- const parameters\_type & get\_parameters ()
   Returns the parameters used to construct the factory.
- std::unique\_ptr< permutation\_type > generate (std::shared\_ptr< const LinOp > system\_matrix) const

#### Static Public Member Functions

static parameters\_type build ()
 Creates a new parameter\_type to set up the factory.

# 46.194.1 Detailed Description

template < typename IndexType = int32 > class gko::experimental::reorder::Rcm < IndexType >

Rcm (Reverse Cuthill-McKee) is a reordering algorithm minimizing the bandwidth of a matrix.

Such a reordering typically also significantly reduces fill-in, though usually not as effective as more complex algorithms, specifically AMD and nested dissection schemes. The advantage of this algorithm is its low runtime.

The class is a LinOpFactory generating a Permutation matrix out of a Csr system matrix, to be used with Csrc::permute(...).

There are two "starting strategies" currently available: minimum degree and pseudo-peripheral. These strategies control how a starting vertex for a connected component is chosen, which is then renumbered as first vertex in the component, starting the algorithm from there. In general, the bandwidths obtained by choosing a pseudo-peripheral vertex are slightly smaller than those obtained from choosing a vertex of minimum degree. On the other hand, this strategy is much more expensive, relatively. The algorithm for finding a pseudo-peripheral vertex as described in "Computer Solution of Sparse Linear Systems" (George, Liu, Ng, Oak Ridge National Laboratory, 1994) is implemented here.

#### **Template Parameters**

IndexType Type of the indices of all matrices used in this class

#### 46.194.2 Member Function Documentation

#### 46.194.2.1 generate()

#### Note

This function overrides the default LinOpFactory::generate to return a Permutation instead of a generic LinOp, which would need to be cast to Permutation again to access its indices. It is only necessary because smart pointers aren't covariant.

#### 46.194.2.2 get\_parameters()

```
template<typename IndexType = int32>
const parameters_type& gko::experimental::reorder::Rcm< IndexType >::get_parameters ( ) [inline]
```

Returns the parameters used to construct the factory.

#### Returns

the parameters used to construct the factory.

```
205 { return parameters_; }
```

The documentation for this class was generated from the following file:

· ginkgo/core/reorder/rcm.hpp

# 46.195 gko::reorder::Rcm< ValueType, IndexType > Class Template Reference

Rcm (Reverse Cuthill-McKee) is a reordering algorithm minimizing the bandwidth of a matrix.

```
#include <ginkgo/core/reorder/rcm.hpp>
```

# **Public Member Functions**

- ${\sf std::shared\_ptr} < {\sf const} \ {\sf PermutationMatrix} > {\sf get\_permutation} \ () \ {\sf const}$
- std::shared\_ptr< const PermutationMatrix > get\_inverse\_permutation () const

Gets the inverse permutation (permutation matrix, output of the algorithm) of the linear operator.

Gets the permutation (permutation matrix, output of the algorithm) of the linear operator.

# 46.195.1 Detailed Description

template<typename ValueType = default\_precision, typename IndexType = int32> class gko::reorder::Rcm< ValueType, IndexType >

Rcm (Reverse Cuthill-McKee) is a reordering algorithm minimizing the bandwidth of a matrix.

Such a reordering typically also significantly reduces fill-in, though usually not as effective as more complex algorithms, specifically AMD and nested dissection schemes. The advantage of this algorithm is its low runtime. It requires the input matrix to be structurally symmetric.

#### Note

This class is derived from polymorphic object but is not a LinOp as it does not make sense for this class to implement the apply methods. The objective of this class is to generate a reordering/permutation vector (in the form of the Permutation matrix), which can be used to apply to reorder a matrix as required.

There are two "starting strategies" currently available: minimum degree and pseudo-peripheral. These strategies control how a starting vertex for a connected component is chosen, which is then renumbered as first vertex in the component, starting the algorithm from there. In general, the bandwidths obtained by choosing a pseudo-peripheral vertex are slightly smaller than those obtained from choosing a vertex of minimum degree. On the other hand, this strategy is much more expensive, relatively. The algorithm for finding a pseudo-peripheral vertex as described in "Computer Solution of Sparse Linear Systems" (George, Liu, Ng, Oak Ridge National Laboratory, 1994) is implemented here.

#### **Template Parameters**

ValueType	Type of the values of all matrices used in this class
IndexType	Type of the indices of all matrices used in this class

# 46.195.2 Member Function Documentation

#### 46.195.2.1 get inverse permutation()

```
template<typename ValueType = default_precision, typename IndexType = int32> std::shared_ptr<const PermutationMatrix> gko::reorder::Rcm< ValueType, IndexType >::get_← inverse_permutation ( ) const [inline]
```

Gets the inverse permutation (permutation matrix, output of the algorithm) of the linear operator.

#### Returns

the inverse permutation (permutation matrix)

### 46.195.2.2 get\_permutation()

```
template<typename ValueType = default_precision, typename IndexType = int32>
std::shared_ptr<const PermutationMatrix> gko::reorder::Rcm< ValueType, IndexType >::get_
permutation ( ) const [inline]
```

Gets the permutation (permutation matrix, output of the algorithm) of the linear operator.

#### Returns

the permutation (permutation matrix)

The documentation for this class was generated from the following file:

• ginkgo/core/reorder/rcm.hpp

# 46.196 gko::ReadableFromMatrixData< ValueType, IndexType > Class Template Reference

A LinOp implementing this interface can read its data from a matrix data structure.

```
#include <ginkgo/core/base/lin_op.hpp>
```

#### **Public Member Functions**

- virtual void read (const matrix\_data < ValueType, IndexType > &data)=0
   Reads a matrix from a matrix\_data structure.
- void read (const matrix\_assembly\_data< ValueType, IndexType > &data)

Reads a matrix from a matrix\_assembly\_data structure.

virtual void read (const device\_matrix\_data < ValueType, IndexType > &data)

Reads a matrix from a device\_matrix\_data structure.

virtual void read (device\_matrix\_data < ValueType, IndexType > &&data)

Reads a matrix from a device\_matrix\_data structure.

# 46.196.1 Detailed Description

```
template<typename ValueType, typename IndexType> class gko::ReadableFromMatrixData< ValueType, IndexType>
```

A LinOp implementing this interface can read its data from a matrix\_data structure.

# 46.196.2 Member Function Documentation

# 46.196.2.1 read() [1/4]

Reads a matrix from a device matrix data structure.

#### **Parameters**

```
data the device_matrix_data structure.
```

Reimplemented in gko::matrix::Csr< ValueType, IndexType >, gko::matrix::Hybrid< ValueType, IndexType >, gko::matrix::Fbcsr< ValueType, IndexType >, gko::matrix::Fbcsr< ValueType, IndexType >, gko::matrix::Coo< ValueType, IndexType > gko::matrix::Sellp< ValueType, IndexType >, and gko::matrix::SparsityCsr< ValueType, IndexType >.

### 46.196.2.2 read() [2/4]

Reads a matrix from a matrix\_assembly\_data structure.

#### **Parameters**

data the matrix\_assembly\_data structure

#### 46.196.2.3 read() [3/4]

Reads a matrix from a matrix data structure.

#### **Parameters**

```
data the matrix_data structure
```

Implemented in gko::matrix::Csr< ValueType, IndexType >, gko::matrix::Hybrid< ValueType, IndexType >, gko::matrix::Fbcsr< ValueType, IndexType >, gko::matrix::Ell< ValueType, IndexType >, gko::matrix::Coo< ValueType, IndexType > gko::matrix::Sellp< ValueType, IndexType >, and gko::matrix::SparsityCsr< ValueType, IndexType >.

### 46.196.2.4 read() [4/4]

Reads a matrix from a device\_matrix\_data structure.

The structure may be emptied by this function.

#### **Parameters**

data the device\_matrix\_data structure.

Reimplemented in gko::matrix::Csr< ValueType, IndexType >, gko::matrix::Hybrid< ValueType, IndexType >, gko::matrix::Fbcsr< ValueType, IndexType >, gko::matrix::Ell< ValueType, IndexType >, gko::matrix::Coo< ValueType, IndexType > gko::matrix::Sellp< ValueType, IndexType >, and gko::matrix::SparsityCsr< ValueType, IndexType >.

The documentation for this class was generated from the following file:

• ginkgo/core/base/lin\_op.hpp

### 46.197 gko::log::Record Class Reference

Record is a Logger which logs every event to an object.

#include <ginkgo/core/log/record.hpp>

### **Classes**

· struct logged\_data

Struct storing the actually logged data.

### **Public Member Functions**

- const logged\_data & get () const noexcept
   Returns the logged data.
- logged\_data & get () noexcept

### **Static Public Member Functions**

 static std::unique\_ptr< Record > create (std::shared\_ptr< const Executor > exec, const mask\_type &enabled\_events=Logger::all\_events\_mask, size\_type max\_storage=1)

Creates a Record logger.

static std::unique\_ptr< Record > create (const mask\_type &enabled\_events=Logger::all\_events\_mask, size\_type max\_storage=1)

Creates a Record logger.

### 46.197.1 Detailed Description

Record is a Logger which logs every event to an object.

The object can then be accessed at any time by asking the logger to return it.

Note

Please note that this logger can have significant memory and performance overhead. In particular, when logging events such as the <code>check</code> events, all parameters are cloned. If it is sufficient to clone one parameter, consider implementing a specific logger for this. In addition, it is advised to tune the history size in order to control memory overhead.

### 46.197.2 Member Function Documentation

### 46.197.2.1 create() [1/2]

Creates a Record logger.

This dynamically allocates the memory, constructs the object and returns an std::unique\_ptr to this object.

### **Parameters**

exec	the executor
enabled_events	the events enabled for this logger. By default all events.
max_storage	the size of storage (i.e. history) wanted by the user. By default 0 is used, which means unlimited storage. It is advised to control this to reduce memory overhead of this logger.

### Returns

an std::unique\_ptr to the the constructed object

### 46.197.2.2 create() [2/2]

Creates a Record logger.

This dynamically allocates the memory, constructs the object and returns an std::unique\_ptr to this object.

### **Parameters**

exec	the executor
enabled_events	the events enabled for this logger. By default all events.
max_storage	the size of storage (i.e. history) wanted by the user. By default 0 is used, which means unlimited storage. It is advised to control this to reduce memory overhead of this logger.

#### Returns

an std::unique\_ptr to the the constructed object

### 46.197.2.3 get() [1/2]

```
const logged_data& gko::log::Record::get ( ) const [inline], [noexcept]
```

Returns the logged data.

#### Returns

the logged data

### 46.197.2.4 get() [2/2]

```
logged_data& gko::log::Record::get ( ) [inline], [noexcept]
```

The documentation for this class was generated from the following file:

· ginkgo/core/log/record.hpp

### 46.198 gko::ReferenceExecutor Class Reference

This is a specialization of the OmpExecutor, which runs the reference implementations of the kernels used for debugging purposes.

#include <ginkgo/core/base/executor.hpp>

### **Public Member Functions**

- std::string get\_description () const override
- void run (const Operation &op) const override

Runs the specified Operation using this Executor.

• virtual void run (const Operation &op) const=0

Runs the specified Operation using this Executor.

template < typename ClosureOmp, typename ClosureCuda, typename ClosureHip, typename ClosureDpcpp > void run (const ClosureOmp & op\_omp, const ClosureCuda & op\_cuda, const ClosureHip & op\_hip, const ClosureDpcpp & op\_dpcpp) const

Runs one of the passed in functors, depending on the Executor type.

template < typename ClosureReference , typename ClosureOmp , typename ClosureCuda , typename ClosureHip , typename Closure ← Dpcpp >

void run (std::string name, const ClosureReference &op\_ref, const ClosureOmp &op\_omp, const Closure ← Cuda &op\_cuda, const ClosureHip &op\_hip, const ClosureDpcpp &op\_dpcpp) const

Runs one of the passed in functors, depending on the Executor type.

### **Additional Inherited Members**

### 46.198.1 Detailed Description

This is a specialization of the OmpExecutor, which runs the reference implementations of the kernels used for debugging purposes.

### 46.198.2 Member Function Documentation

### 46.198.2.1 get\_description()

```
std::string gko::ReferenceExecutor::get_description ( ) const [inline], [override], [virtual]
```

### Returns

a textual representation of the executor and its device.

Reimplemented from gko::OmpExecutor.

### 46.198.2.2 run() [1/4]

Runs one of the passed in functors, depending on the Executor type.

### **Template Parameters**

ClosureOmp	type of op_omp
ClosureCuda	type of op_cuda
ClosureHip	type of op_hip
ClosureDpcpp	type of op_dpcpp

### **Parameters**

op_omp	functor to run in case of a OmpExecutor or ReferenceExecutor	
op_cuda	functor to run in case of a CudaExecutor	
op_hip	hip functor to run in case of a HipExecutor	
op_dpcpp	functor to run in case of a DpcppExecutor	

### 46.198.2.3 run() [2/4]

Runs the specified Operation using this Executor.

#### **Parameters**

```
op the operation to run
```

Implements gko::Executor.

### 46.198.2.4 run() [3/4]

```
virtual void gko::Executor::run
```

Runs the specified Operation using this Executor.

### **Parameters**

```
op the operation to run
```

### 46.198.2.5 run() [4/4]

Runs one of the passed in functors, depending on the Executor type.

### **Template Parameters**

ClosureReference	type of op_ref
ClosureOmp	type of op_omp
ClosureCuda	type of op_cuda
ClosureHip	type of op_hip
ClosureDpcpp	type of op_dpcpp

#### **Parameters**

name	the name of the operation	
op_ref	functor to run in case of a ReferenceExecutor	
op_omp	functor to run in case of a OmpExecutor	
op_cuda	op_cuda functor to run in case of a CudaExecutor	
op_hip	functor to run in case of a HipExecutor	
op_dpcpp	functor to run in case of a DpcppExecutor	

The documentation for this class was generated from the following file:

· ginkgo/core/base/executor.hpp

### 46.199 gko::config::registry Class Reference

This class stores additional context for creating Ginkgo objects from configuration files.

```
#include <ginkgo/core/config/registry.hpp>
```

### **Public Member Functions**

- registry (const configuration\_map &additional\_map={})
   registry constructor
- registry (const std::unordered\_map< std::string, detail::allowed\_ptr > &stored\_map, const configuration\_
   map &additional\_map={})

registry constructor

• template<typename T >

bool emplace (std::string key, std::shared\_ptr< T > data)

Store the data with the key.

### 46.199.1 Detailed Description

This class stores additional context for creating Ginkgo objects from configuration files.

The context can contain user-provided objects that derive from the following base types:

- LinOp
- LinOpFactory
- CriterionFactory

Additionally, users can provide mappings from a configuration (provided as a pnode) to user-defined types that are derived from LinOpFactory

#### 46.199.2 Constructor & Destructor Documentation

### 46.199.2.1 registry() [1/2]

registry constructor

### **Parameters**

additional_map	the additional map to dispatch the class base. Users can extend the map to fit their own
	LinOpFactory. We suggest using "usr::" as the prefix in the key to simply avoid conflict with
	ginkgo's map.

### 46.199.2.2 registry() [2/2]

### registry constructor

### **Parameters**

stored_map	the map stores the shared pointer of users' objects. It can hold any type whose base type is LinOp/LinOpFactory/CriterionFactory.
additional_map	the additional map to dispatch the class base. Users can extend the map to fit their own LinOpFactory. We suggest using "usr::" as the prefix in the key to simply avoid conflict with ginkgo's map.

### 46.199.3 Member Function Documentation

### 46.199.3.1 emplace()

Store the data with the key.

### **Template Parameters**

```
T the type
```

### **Parameters**

key	the unique key string
data	the shared pointer of the object

```
236 {
237     auto it = stored_map_.emplace(key, data);
```

```
238     return it.second;
239 }
```

The documentation for this class was generated from the following file:

· ginkgo/core/config/registry.hpp

## 46.200 gko::stop::RelativeResidualNorm< ValueType > Class Template Reference

The RelativeResidualNorm class is a stopping criterion which stops the iteration process when the residual norm is below a certain threshold relative to the norm of the right-hand side, i.e.

```
#include <ginkgo/core/stop/residual_norm.hpp>
```

### 46.200.1 Detailed Description

```
template<typename ValueType = default_precision> class gko::stop::RelativeResidualNorm< ValueType >
```

The RelativeResidualNorm class is a stopping criterion which stops the iteration process when the residual norm is below a certain threshold relative to the norm of the right-hand side, i.e.

when norm(residual) / norm(right\_hand\_side) < threshold. For better performance, the checks are run thanks to kernels on the executor where the algorithm is executed.

Note

To use this stopping criterion there are some dependencies. The constructor depends on b in order to compute the norm of the right-hand side. If this is not correctly provided, an exception ::gko::NotSupported() is thrown.

The documentation for this class was generated from the following file:

• ginkgo/core/stop/residual norm.hpp

## 46.201 gko::reorder::ReorderingBase< IndexType > Class Template Reference

The ReorderingBase class is a base class for all the reordering algorithms.

```
#include <ginkgo/core/reorder/reordering_base.hpp>
```

### **Additional Inherited Members**

### 46.201.1 Detailed Description

template<typename IndexType = int32> class gko::reorder::ReorderingBase< IndexType >

The ReorderingBase class is a base class for all the reordering algorithms.

It contains a factory to instantiate the reorderings. It is up to each specific reordering to decide what to do with the data that is passed to it.

The documentation for this class was generated from the following file:

ginkgo/core/reorder/reordering base.hpp

### 46.202 gko::reorder::ReorderingBaseArgs Struct Reference

This struct is used to pass parameters to the EnableDefaultReorderingBaseFactory::generate() method.

#include <ginkgo/core/reorder/reordering\_base.hpp>

### 46.202.1 Detailed Description

This struct is used to pass parameters to the EnableDefaultReorderingBaseFactory::generate() method.

It is the ComponentsType of ReorderingBaseFactory.

The documentation for this struct was generated from the following file:

• ginkgo/core/reorder/reordering\_base.hpp

### 46.203 gko::experimental::mpi::request Class Reference

The request class is a light, move-only wrapper around the MPI Request handle.

#include <ginkgo/core/base/mpi.hpp>

### **Public Member Functions**

• request ()

The default constructor.

MPI\_Request \* get ()

Get a pointer to the underlying MPI\_Request handle.

• status wait ()

Allows a rank to wait on a particular request handle.

### 46.203.1 Detailed Description

The request class is a light, move-only wrapper around the MPI\_Request handle.

### 46.203.2 Constructor & Destructor Documentation

#### 46.203.2.1 request()

```
gko::experimental::mpi::request::request ( ) [inline]
```

The default constructor.

It creates a null MPI\_Request of MPI\_REQUEST\_NULL type.

### 46.203.3 Member Function Documentation

#### 46.203.3.1 get()

```
MPI_Request* gko::experimental::mpi::request::get () [inline]
```

Get a pointer to the underlying MPI\_Request handle.

#### Returns

a pointer to MPI\_Request handle

Referenced by gko::experimental::mpi::communicator::i\_all\_gather(), gko::experimental::mpi::communicator::i  $\leftarrow$  \_all\_reduce(), gko::experimental::mpi::communicator::i\_all\_to\_all(), gko::experimental::mpi::communicator::i  $\leftarrow$  \_all\_to\_all\_v(), gko::experimental::mpi::communicator::i\_broadcast(), gko::experimental::mpi::communicator::i  $\leftarrow$  \_recv(), gko::experimental::mpi::communicator::i\_gather\_v(), gko::experimental::mpi::communicator::i\_scan(), gko::experimental::mpi::communicator::i\_scan(), gko::experimental::mpi::communicator::i\_scan(), gko::experimental::mpi::communicator::i\_scan(), gko::experimental::mpi::communicator::i\_scan(), gko::experimental::mpi::communicator::i\_scan(), gko::experimental::mpi::communicator::i\_scan(), gko::experimental::mpi::window< ValueType >::r\_accumulate(), gko::experimental::mpi::window< ValueType >::r\_get\_ $\leftarrow$  accumulate(), and gko::experimental::mpi::window< ValueType >::r\_get\_ $\leftarrow$  accumulate().

#### 46.203.3.2 wait()

```
status gko::experimental::mpi::request::wait ( ) [inline]
```

Allows a rank to wait on a particular request handle.

#### **Parameters**

req	The request to wait on.	
status	The status variable that can be queried.	

References gko::experimental::mpi::status::get().

The documentation for this class was generated from the following file:

· ginkgo/core/base/mpi.hpp

## 46.204 gko::stop::ResidualNorm< ValueType > Class Template Reference

The ResidualNorm class is a stopping criterion which stops the iteration process when the actual residual norm is below a certain threshold relative to.

#include <ginkgo/core/stop/residual\_norm.hpp>

### 46.204.1 Detailed Description

template<typename ValueType = default\_precision> class gko::stop::ResidualNorm< ValueType >

The ResidualNorm class is a stopping criterion which stops the iteration process when the actual residual norm is below a certain threshold relative to.

- 1. the norm of the right-hand side, norm(residual)  $\leq$  < threshold \* norm(right\_hand\_side).
- 2. the initial residual,  $norm(residual) \le threshold * norm(initial\_residual)$ .
- 3. one,  $norm(residual) \le threshold$ .

For better performance, the checks are run on the executor where the algorithm is executed.

### Note

To use this stopping criterion there are some dependencies. The constructor depends on either b or the  $initial\_residual$  in order to compute their norms. If this is not correctly provided, an exception ::gko $\leftarrow$ ::NotSupported() is thrown.

The documentation for this class was generated from the following file:

ginkgo/core/stop/residual\_norm.hpp

## 46.205 gko::stop::ResidualNormBase< ValueType > Class Template Reference

The ResidualNormBase class provides a framework for stopping criteria related to the residual norm.

```
#include <ginkgo/core/stop/residual_norm.hpp>
```

### 46.205.1 Detailed Description

```
template<typename ValueType>
class gko::stop::ResidualNormBase< ValueType >
```

The ResidualNormBase class provides a framework for stopping criteria related to the residual norm.

These criteria differ in the way they initialize starting\_tau\_, so in the value they compare the residual norm against. The provided check impl uses the actual residual to check for convergence.

The documentation for this class was generated from the following file:

· ginkgo/core/stop/residual\_norm.hpp

## 46.206 gko::stop::ResidualNormReduction < ValueType > Class Template Reference

The ResidualNormReduction class is a stopping criterion which stops the iteration process when the residual norm is below a certain threshold relative to the norm of the initial residual, i.e.

```
#include <ginkgo/core/stop/residual_norm.hpp>
```

### 46.206.1 Detailed Description

```
template<typename ValueType = default_precision> class gko::stop::ResidualNormReduction< ValueType >
```

The ResidualNormReduction class is a stopping criterion which stops the iteration process when the residual norm is below a certain threshold relative to the norm of the initial residual, i.e.

when norm(residual) / norm(initial\_residual) < threshold. For better performance, the checks are run thanks to kernels on the executor where the algorithm is executed.

Note

To use this stopping criterion there are some dependencies. The constructor depends on <code>initial\_constitual</code> in order to compute the first relative residual norm. The check method depends on either the <code>residual\_norm</code> or the <code>residual\_being</code> set. When any of those is not correctly provided, an exception <code>::gko::NotSupported()</code> is thrown.

The documentation for this class was generated from the following file:

ginkgo/core/stop/residual\_norm.hpp

## 46.207 gko::accessor::row\_major< ValueType, Dimensionality > Class Template Reference

A row\_major accessor is a bridge between a range and the row-major memory layout.

#include <ginkgo/core/base/range\_accessors.hpp>

### **Public Types**

using value type = ValueType

Type of values returned by the accessor.

using data\_type = value\_type \*

Type of underlying data storage.

#### **Public Member Functions**

• constexpr value\_type & operator() (size\_type row, size\_type col) const

Returns the data element at position (row, col)

constexpr range < row\_major > operator() (const span &rows, const span &cols) const

Returns the sub-range spanning the range (rows, cols)

constexpr size type length (size type dimension) const

Returns the length in dimension dimension.

template<typename OtherAccessor >

void copy\_from (const OtherAccessor &other) const

Copies data from another accessor.

#### **Public Attributes**

const data\_type data

Reference to the underlying data.

const std::array< const size\_type, dimensionality > lengths

An array of dimension sizes.

· const size type stride

Distance between consecutive rows.

### **Static Public Attributes**

• static constexpr size\_type dimensionality = 2

Number of dimensions of the accessor.

### 46.207.1 Detailed Description

template<typename ValueType, size\_type Dimensionality> class gko::accessor::row\_major< ValueType, Dimensionality >

A row\_major accessor is a bridge between a range and the row-major memory layout.

You should never try to explicitly create an instance of this accessor. Instead, supply it as a template parameter to a range, and pass the constructor parameters for this class to the range (it will forward it to this class).

Warning

The current implementation is incomplete, and only allows for 2-dimensional ranges.

### **Template Parameters**

ValueType	type of values this accessor returns
Dimensionality	number of dimensions of this accessor (has to be 2)

### 46.207.2 Member Function Documentation

### 46.207.2.1 copy\_from()

Copies data from another accessor.

### Warning

Do not use this function since it is not optimized for a specific executor. It will always be performed sequentially. Please write an optimized version (adjusted to the architecture) by iterating through the values yourself.

#### **Template Parameters**

OtherAccessor	type of the other accessor
---------------	----------------------------

other accessor

### **Parameters**

141	{	
142		<pre>for (size_type i = 0; i &lt; lengths[0]; ++i) {</pre>
143		<pre>for (size_type j = 0; j &lt; lengths[1]; ++j) {</pre>
144		(*this)(i, j) = other(i, j);
145		}
146		}
147	}	

References gko::accessor::row\_major< ValueType, Dimensionality >::lengths.

### 46.207.2.2 length()

Returns the length in dimension dimension.

#### **Parameters**

dimension a dimension inde
----------------------------

### Returns

length in dimension dimension

References gko::accessor::row\_major< ValueType, Dimensionality >::lengths.

### 46.207.2.3 operator()() [1/2]

Returns the sub-range spanning the range (rows, cols)

#### **Parameters**

rows	row span
cols	column span

### Returns

sub-range spanning the range (rows, cols)

References gko::span::begin, gko::accessor::row\_major< ValueType, Dimensionality >::data, gko::span::end, gko::span::is\_valid(), gko::accessor::row\_major< ValueType, Dimensionality >::lengths, and gko::accessor::row—major< ValueType, Dimensionality >::stride.

### 46.207.2.4 operator()() [2/2]

Returns the data element at position (row, col)

#### **Parameters**

row	row index
col	column index

Returns

data element at (row, col)

References gko::accessor::row\_major< ValueType, Dimensionality >::data, gko::accessor::row\_major< Value ← Type, Dimensionality >::lengths, and gko::accessor::row major< ValueType, Dimensionality >::stride.

The documentation for this class was generated from the following file:

ginkgo/core/base/range accessors.hpp

## 46.208 gko::matrix::RowGatherer< IndexType > Class Template Reference

RowGatherer is a matrix "format" which stores the gather indices arrays which can be used to gather rows to another matrix.

#include <ginkgo/core/matrix/row\_gatherer.hpp>

### **Public Member Functions**

index\_type \* get\_row\_idxs () noexcept

Returns a pointer to the row index array for gathering.

const index\_type \* get\_const\_row\_idxs () const noexcept

Returns a pointer to the row index array for gathering.

### **Static Public Member Functions**

static std::unique\_ptr< RowGatherer > create (std::shared\_ptr< const Executor > exec, const dim< 2 > &size={})

Creates uninitialized RowGatherer arrays of the specified size.

static std::unique\_ptr< RowGatherer > create (std::shared\_ptr< const Executor > exec, const dim< 2 > &size, array< index\_type > row\_idxs)

Creates a RowGatherer matrix from an already allocated (and initialized) row gathering array.

static std::unique\_ptr< const RowGatherer > create\_const (std::shared\_ptr< const Executor > exec, const dim< 2 > &size, gko::detail::const\_array\_view< IndexType > &&row\_idxs)

Creates a constant (immutable) RowGatherer matrix from a constant array.

### 46.208.1 Detailed Description

template<typename IndexType = int32> class gko::matrix::RowGatherer< IndexType >

RowGatherer is a matrix "format" which stores the gather indices arrays which can be used to gather rows to another matrix.

### **Template Parameters**

IndexType	precision of rowgatherer array indices.
-----------	---

### Note

This format is used mainly to allow for an abstraction of the rowgatherer and provides the user with an apply method which calls the respective Dense rowgatherer operation. As such it only stores an array of the rowgatherer indices.

### 46.208.2 Member Function Documentation

### 46.208.2.1 create() [1/2]

Creates a RowGatherer matrix from an already allocated (and initialized) row gathering array.

### **Parameters**

exec	Executor associated to the matrix
size	size of the rowgatherer array.
row_idxs	array of rowgatherer array

### Note

If row\_idxs is not an rvalue, not an array of IndexType, or is on the wrong executor, an internal copy will be created, and the original array data will not be used in the matrix.

### Returns

A smart pointer to the newly created matrix.

### 46.208.2.2 create() [2/2]

Creates uninitialized RowGatherer arrays of the specified size.

#### **Parameters**

exec	Executor associated to the matrix
size	size of the RowGatherable matrix

#### Returns

A smart pointer to the newly created matrix.

### 46.208.2.3 create\_const()

Creates a constant (immutable) RowGatherer matrix from a constant array.

#### **Parameters**

exec	the executor to create the matrix on
size	the dimensions of the matrix
row_idxs	the gathered row indices of the matrix

### Returns

A smart pointer to the constant matrix wrapping the input arrays (if they reside on the same executor as the matrix) or a copy of the arrays on the correct executor.

### 46.208.2.4 get\_const\_row\_idxs()

```
template<typename IndexType = int32>
const index_type* gko::matrix::RowGatherer< IndexType >::get_const_row_idxs ( ) const [inline],
[noexcept]
```

Returns a pointer to the row index array for gathering.

### Returns

the pointer to the row index array for gathering.

Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

```
64 {
65          return row_idxs_.get_const_data();
66 }
```

References gko::array< ValueType >::get\_const\_data().

### 46.208.2.5 get\_row\_idxs()

```
template<typename IndexType = int32>
index_type* gko::matrix::RowGatherer< IndexType >::get_row_idxs ( ) [inline], [noexcept]
```

Returns a pointer to the row index array for gathering.

#### Returns

the pointer to the row index array for gathering.

References gko::array< ValueType >::get\_data().

The documentation for this class was generated from the following file:

ginkgo/core/matrix/row\_gatherer.hpp

### 46.209 gko::ScaledIdentityAddable Class Reference

Adds the operation M <- a I + b M for matrix M, identity operator I and scalars a and b, where M is the calling object.

```
#include <ginkgo/core/base/lin_op.hpp>
```

### **Public Member Functions**

void add\_scaled\_identity (ptr\_param< const LinOp > const a, ptr\_param< const LinOp > const b)
 Scales this and adds another scalar times the identity to it.

### 46.209.1 Detailed Description

Adds the operation M < a I + b M for matrix M, identity operator I and scalars a and b, where M is the calling object.

### 46.209.2 Member Function Documentation

### 46.209.2.1 add scaled identity()

Scales this and adds another scalar times the identity to it.

#### **Parameters**

а	Scalar to multiply the identity operator before adding.
b	Scalar to multiply this before adding the scaled identity to it.

References gko::make\_temporary\_clone().

The documentation for this class was generated from the following file:

· ginkgo/core/base/lin\_op.hpp

## 46.210 gko::matrix::ScaledPermutation < ValueType, IndexType > Class Template Reference

ScaledPermutation is a matrix combining a permutation with scaling factors.

#include <ginkgo/core/matrix/scaled\_permutation.hpp>

### **Public Member Functions**

value type \* get scaling factors () noexcept

Returns a pointer to the scaling factors.

• const value\_type \* get\_const\_scaling\_factors () const noexcept

Returns a pointer to the scaling factors.

index\_type \* get\_permutation () noexcept

Returns a pointer to the permutation indices.

const index\_type \* get\_const\_permutation () const noexcept

Returns a pointer to the permutation indices.

• std::unique\_ptr< ScaledPermutation > compute\_inverse () const

Returns the inverse of this operator as a scaled permutation.

• std::unique\_ptr< ScaledPermutation > compose (ptr\_param< const ScaledPermutation > other) const

Composes this scaled permutation with another scaled permutation.

void write (gko::matrix\_data< value\_type, index\_type > &data) const override

Writes a matrix to a matrix\_data structure.

### **Static Public Member Functions**

static std::unique\_ptr< ScaledPermutation > create (std::shared\_ptr< const Executor > exec, size\_type size=0)

Creates an uninitialized ScaledPermutation matrix.

static std::unique\_ptr< ScaledPermutation > create (ptr\_param< const Permutation< IndexType >> permutation)

Create a ScaledPermutation from a Permutation.

static std::unique\_ptr< ScaledPermutation > create (std::shared\_ptr< const Executor > exec, array< value\_type > scaling\_factors, array< index\_type > permutation\_indices)

Creates a ScaledPermutation matrix from already allocated arrays.

static std::unique\_ptr< const ScaledPermutation > create\_const (std::shared\_ptr< const Executor > exec, gko::detail::const\_array\_view< value\_type > &&scale, gko::detail::const\_array\_view< index\_type > &&perm\_idxs)

Creates a constant (immutable) ScaledPermutation matrix from constant arrays.

### 46.210.1 Detailed Description

template<typename ValueType = default\_precision, typename IndexType = int32> class gko::matrix::ScaledPermutation< ValueType, IndexType >

ScaledPermutation is a matrix combining a permutation with scaling factors.

It is a combination of Diagonal and Permutation, and can be read as  $SP = P \cdot S$ , i.e. the scaling gets applied before the permutation.

### **Template Parameters**

IndexType	index type of permutation indices
ValueType	value type of the scaling factors

### 46.210.2 Member Function Documentation

### 46.210.2.1 compose()

Composes this scaled permutation with another scaled permutation.

This means result = other \* this from the matrix perspective, which is equivalent to first scaling and permuting by this and then by other.

#### **Parameters**

other	the other permutation

### Returns

the combined permutation

### 46.210.2.2 compute\_inverse()

```
template<typename ValueType = default_precision, typename IndexType = int32> std::unique_ptr<ScaledPermutation> gko::matrix::ScaledPermutation< ValueType, IndexType > ← ::compute_inverse ( ) const
```

Returns the inverse of this operator as a scaled permutation.

It is computed via  $(PS)^{-1} = P^{-1}(PSP^{-1})$ .

#### Returns

a newly created ScaledPermutation object storing the inverse of the permutation and scaling factors of this ScaledPermutation.

### 46.210.2.3 create() [1/3]

Create a ScaledPermutation from a Permutation.

The permutation will be copied, the scaling factors are all set to 1.0.

#### **Parameters**

permutation	the permutation
-------------	-----------------

#### Returns

A smart pointer to the newly created matrix.

### 46.210.2.4 create() [2/3]

Creates a ScaledPermutation matrix from already allocated arrays.

#### **Parameters**

exec	Executor associated to the matrix
permutation_indices	array of permutation indices
scaling_factors	array of scaling factors

#### Returns

A smart pointer to the newly created matrix.

### 46.210.2.5 create() [3/3]

Creates an uninitialized ScaledPermutation matrix.

### **Parameters**

ехес	Executor associated to the matrix
size	dimensions of the (square) scaled permutation matrix

#### Returns

A smart pointer to the newly created matrix.

### 46.210.2.6 create const()

Creates a constant (immutable) ScaledPermutation matrix from constant arrays.

### **Parameters**

exec	the executor to create the object on
perm_idxs	the permutation index array of the matrix
scale	the scaling factor array

#### Returns

A smart pointer to the constant matrix wrapping the input arrays (if it resides on the same executor as the matrix) or a copy of the arrays on the correct executor.

### 46.210.2.7 get\_const\_permutation()

```
template<typename ValueType = default_precision, typename IndexType = int32>
const index_type* gko::matrix::ScaledPermutation
ValueType, IndexType >::get_const_permutation
( ) const [inline], [noexcept]
```

Returns a pointer to the permutation indices.

#### Returns

the pointer to the permutation indices.

#### Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

```
79 {
80     return permutation_.get_const_data();
81 }
```

References gko::array< ValueType >::get\_const\_data().

### 46.210.2.8 get\_const\_scaling\_factors()

```
template<typename ValueType = default_precision, typename IndexType = int32>
const value_type* gko::matrix::ScaledPermutation< ValueType, IndexType >::get_const_scaling_←
factors ( ) const [inline], [noexcept]
```

Returns a pointer to the scaling factors.

#### Returns

the pointer to the scaling factors.

### Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

References gko::array< ValueType >::get\_const\_data().

### 46.210.2.9 get\_permutation()

```
template<typename ValueType = default_precision, typename IndexType = int32>
index_type* gko::matrix::ScaledPermutation< ValueType, IndexType >::get_permutation ( ) [inline],
[noexcept]
```

Returns a pointer to the permutation indices.

#### Returns

the pointer to the permutation indices.

References gko::array< ValueType >::get\_data().

### 46.210.2.10 get\_scaling\_factors()

```
template<typename ValueType = default_precision, typename IndexType = int32>
value_type* gko::matrix::ScaledPermutation< ValueType, IndexType >::get_scaling_factors ( )
[inline], [noexcept]
```

Returns a pointer to the scaling factors.

Returns

the pointer to the scaling factors.

References gko::array< ValueType >::get\_data().

### 46.210.2.11 write()

Writes a matrix to a matrix\_data structure.

#### **Parameters**

```
data the matrix_data structure
```

Implements gko::WritableToMatrixData< ValueType, IndexType >.

The documentation for this class was generated from the following file:

ginkgo/core/matrix/scaled\_permutation.hpp

## 46.211 gko::experimental::reorder::ScaledReordered< ValueType, IndexType > Class Template Reference

Provides an interface to wrap reorderings like Rcm and diagonal scaling like equilibration around a LinOp like e.g.

```
#include <ginkgo/core/reorder/scaled_reordered.hpp>
```

### **Additional Inherited Members**

### 46.211.1 Detailed Description

template<typename ValueType = default\_precision, typename IndexType = int32> class gko::experimental::reorder::ScaledReordered< ValueType, IndexType >

Provides an interface to wrap reorderings like Rcm and diagonal scaling like equilibration around a LinOp like e.g.

a sparse direct solver.

Reorderings can be useful for reducing fill-in in the numerical factorization phase of direct solvers, diagonal scaling can help improve the numerical stability by reducing the condition number of the system matrix.

With a permutation matrix P, a row scaling R and a column scaling C, the inner operator is applied to the system matrix  $P*R*A*C*P^{\wedge}T$  instead of A. Instead of A\*x = b, the inner operator attempts to solve the equivalent linear system  $P*R*A*C*P^{\wedge}T*y = P*R*b$  and retrieves the solution  $x = C*P^{\wedge}T*y$ . Note: The inner system matrix is computed from a clone of A, so the original system matrix is not changed.

#### **Template Parameters**

ValueType	Type of the values of all matrices used in this class
IndexType	Type of the indices of all matrices used in this class

The documentation for this class was generated from the following file:

• ginkgo/core/reorder/scaled\_reordered.hpp

# 46.212 gko::experimental::distributed::preconditioner::Schwarz < ValueType, LocalIndexType, GlobalIndexType > Class Template Reference

A Schwarz preconditioner is a simple domain decomposition preconditioner that generalizes the Block Jacobi preconditioner, incorporating options for different local subdomain solvers and overlaps between the subdomains.

#include <ginkgo/core/distributed/preconditioner/schwarz.hpp>

#### Static Public Member Functions

• static parameters\_type parse (const config::pnode &config, const config::registry &context, const config::type\_descriptor &td\_for\_child=config::make\_type\_descriptor < ValueType, LocalIndexType, Global← IndexType >())

Create the parameters from the property\_tree.

### **Additional Inherited Members**

### 46.212.1 Detailed Description

template < typename ValueType = default\_precision, typename LocalIndexType = int32, typename GlobalIndexType = int64 > class gko::experimental::distributed::preconditioner::Schwarz < ValueType, LocalIndexType, GlobalIndexType >

A Schwarz preconditioner is a simple domain decomposition preconditioner that generalizes the Block Jacobi preconditioner, incorporating options for different local subdomain solvers and overlaps between the subdomains.

See Iterative Methods for Sparse Linear Systems (Y. Saad) for a general treatment and variations of the method.

Note

Currently overlap and coarse grid correction are not supported (TODO).

### **Template Parameters**

ValueType precision of matrix element	
LocalIndexType	local integer type of the matrix
GlobalIndexType	global integer type of the matrix

### 46.212.2 Member Function Documentation

### 46.212.2.1 parse()

Create the parameters from the property\_tree.

Because this is directly tied to the specific type, the value/index type settings within config are ignored and type\_ descriptor is only used for children objects.

### **Parameters**

config	the property tree for setting
context	the registry
td_for_child	the type descriptor for children objects. The default uses the value/local/global index type of this class.

### Returns

parameters

The documentation for this class was generated from the following file:

• ginkgo/core/distributed/preconditioner/schwarz.hpp

### 46.213 gko::scoped\_device\_id\_guard Class Reference

This move-only class uses RAII to set the device id within a scoped block, if necessary.

#include <ginkgo/core/base/scoped\_device\_id\_guard.hpp>

#### **Public Member Functions**

• scoped\_device\_id\_guard (const ReferenceExecutor \*exec, int device\_id)

Create a scoped device id from an Reference.

scoped\_device\_id\_guard (const OmpExecutor \*exec, int device\_id)

Create a scoped device id from an OmpExecutor.

scoped\_device\_id\_guard (const CudaExecutor \*exec, int device\_id)

Create a scoped device id from an CudaExecutor.

• scoped\_device\_id\_guard (const HipExecutor \*exec, int device\_id)

Create a scoped device id from an HipExecutor.

scoped\_device\_id\_guard (const DpcppExecutor \*exec, int device\_id)

Create a scoped device id from an DpcppExecutor.

### 46.213.1 Detailed Description

This move-only class uses RAII to set the device id within a scoped block, if necessary.

The class behaves similar to std::scoped\_lock. The scoped guard will make sure that the device code is run on the correct device within one scoped block, when run with multiple devices. Depending on the executor it will record the current device id and set the device id to the one being passed in. After the scope has been exited, the destructor sets the device\_id back to the one before entering the scope. The OmpExecutor and DpcppExecutor don't require setting an device id, so in those cases, the class is a no-op.

The device id scope has to be constructed from a executor with concrete type (not plain Executor) and a device id. Only the type of the executor object is relevant, so the pointer will not be accessed, and may even be a nullptr. From the executor type the correct derived class of detail::generic\_scoped\_device\_id\_guard is picked. The following illustrates the usage of this class:

```
{
    scoped_device_id_guard g{static_cast<CudaExecutor>(nullptr), 1};
    // now the device id is set to 1
}
// now the device id is reverted again
```

### 46.213.2 Constructor & Destructor Documentation

### 46.213.2.1 scoped\_device\_id\_guard() [1/5]

Create a scoped device id from an Reference.

The resulting object will be a noop.

#### **Parameters**

exec	Not used.
device←	Not used.
_id	

### 46.213.2.2 scoped\_device\_id\_guard() [2/5]

Create a scoped device id from an OmpExecutor.

The resulting object will be a noop.

### **Parameters**

exec	Not used.
device⊷	Not used.
_id	

### 46.213.2.3 scoped\_device\_id\_guard() [3/5]

Create a scoped device id from an CudaExecutor.

The resulting object will set the cuda device id accordingly.

### **Parameters**

exec	Not used.
device⊷	The device id to use within the scope.
id	

### 46.213.2.4 scoped\_device\_id\_guard() [4/5]

Create a scoped device id from an HipExecutor.

The resulting object will set the hip device id accordingly.

#### **Parameters**

exec	Not used.
device⊷	The device id to use within the scope.
_id	

### 46.213.2.5 scoped device id guard() [5/5]

Create a scoped device id from an DpcppExecutor.

The resulting object will be a noop.

### **Parameters**

exec	Not used.
device⊷	Not used.
_id	

The documentation for this class was generated from the following file:

• ginkgo/core/base/scoped\_device\_id\_guard.hpp

### 46.214 gko::segmented\_array< T > Struct Template Reference

A minimal interface for a segmented array.

```
#include <ginkgo/core/base/segmented_array.hpp>
```

### **Public Member Functions**

- $\bullet \ \ segmented\_array \ (std::shared\_ptr{< const} \ \ \mathsf{Executor} > \mathsf{exec})$ 
  - Create an empty segmented array.
- segmented\_array (std::shared\_ptr< const Executor > exec, const segmented\_array &other)

Copies a segmented array to a different executor.

- segmented\_array (std::shared\_ptr< const Executor > exec, segmented\_array &&other)
  - Moves a segmented array to a different executor.
- size\_type get\_size () const
  - Get the total size of the stored buffer.
- size\_type get\_segment\_count () const
  - Get the number of segments.
- T \* get\_flat\_data ()

Access to the flat buffer.

const T \* get\_const\_flat\_data () const

Const-access to the flat buffer.

const gko::array< int64 > & get\_offsets () const

Access to the segment offsets.

• std::shared\_ptr< const Executor > get\_executor () const

Access the executor.

### **Static Public Member Functions**

static segmented\_array create\_from\_sizes (const gko::array< int64 > &sizes)

Creates an uninitialized segmented array with predefined segment sizes.

• static segmented\_array create\_from\_sizes (gko::array< T > buffer, const gko::array< int64 > &sizes)

Creates a segmented array from a flat buffer and segment sizes.

static segmented\_array create\_from\_offsets (gko::array< int64 > offsets)

Creates an uninitialized segmented array from offsets.

static segmented\_array create\_from\_offsets (gko::array < T > buffer, gko::array < int64 > offsets)

Creates a segmented array from a flat buffer and offsets.

### 46.214.1 Detailed Description

```
template<typename T> struct gko::segmented_array< T>
```

A minimal interface for a segmented array.

The segmented array is stored as a flat buffer with an offsets array. The segment i contains the index range [offset[i], offset[i+1]) of the flat buffer.

**Template Parameters** 

```
T | value type stored in the arrays
```

#### 46.214.2 Constructor & Destructor Documentation

### 46.214.2.1 segmented\_array() [1/3]

Create an empty segmented array.

#### **Parameters**

exec	executor for storage arrays
------	-----------------------------

### 46.214.2.2 segmented\_array() [2/3]

Copies a segmented array to a different executor.

#### **Parameters**

exec	the executor to copy to
other	the segmented array to copy from

### 46.214.2.3 segmented\_array() [3/3]

Moves a segmented array to a different executor.

### **Parameters**

exec	the executor to move to
other	the segmented array to move from

### 46.214.3 Member Function Documentation

### 46.214.3.1 create\_from\_offsets() [1/2]

Creates an uninitialized segmented array from offsets.

### **Parameters**

### 46.214.3.2 create\_from\_offsets() [2/2]

Creates a segmented array from a flat buffer and offsets.

#### **Parameters**

buffe	the flat buffer whose size has to match the last element of offsets	
offse	the index offsets for each segment, and the total size of the buffer as last element	1

### 46.214.3.3 create\_from\_sizes() [1/2]

Creates an uninitialized segmented array with predefined segment sizes.

### **Parameters**

exec	executor for storage arrays
sizes	the sizes of each segment

### 46.214.3.4 create\_from\_sizes() [2/2]

```
template<typename T> static segmented_array gko::segmented_array< T >::create_from_sizes ( gko::array< T > buffer, const gko::array< int64 > & sizes ) [static]
```

Creates a segmented array from a flat buffer and segment sizes.

### **Parameters**

buffer	the flat buffer whose size has to match the sum of sizes
sizes the sizes of each segment	

### 46.214.3.5 get\_const\_flat\_data()

```
template<typename T>
const T* gko::segmented_array< T >::get_const_flat_data ( ) const
```

Const-access to the flat buffer.

### Returns

the flat buffer

### 46.214.3.6 get\_executor()

```
template<typename T>
std::shared_ptr<const Executor> gko::segmented_array< T >::get_executor ( ) const
```

Access the executor.

### Returns

the executor

### 46.214.3.7 get\_flat\_data()

```
template<typename T>
T* gko::segmented_array< T >::get_flat_data ( )
```

Access to the flat buffer.

### Returns

the flat buffer

### 46.214.3.8 get\_offsets()

```
template<typename T>
const gko::array<int64>& gko::segmented_array< T >::get_offsets ( ) const
```

Access to the segment offsets.

Returns

the segment offsets

### 46.214.3.9 get\_segment\_count()

```
template<typename T>
size_type gko::segmented_array< T >::get_segment_count ( ) const
```

Get the number of segments.

Returns

the number of segments

### 46.214.3.10 get\_size()

```
template<typename T>
size_type gko::segmented_array< T >::get_size ( ) const
```

Get the total size of the stored buffer.

Returns

the total size of the stored buffer.

The documentation for this struct was generated from the following file:

• ginkgo/core/base/segmented\_array.hpp

## 46.215 gko::matrix::Sellp< ValueType, IndexType > Class Template Reference

SELL-P is a matrix format similar to ELL format.

#include <ginkgo/core/matrix/sellp.hpp>

#### **Public Member Functions**

void read (const mat\_data &data) override

Reads a matrix from a matrix data structure.

· void read (const device mat data &data) override

Reads a matrix from a device\_matrix\_data structure.

• void read (device\_mat\_data &&data) override

Reads a matrix from a device\_matrix\_data structure.

· void write (mat data &data) const override

Writes a matrix to a matrix\_data structure.

• std::unique\_ptr< Diagonal< ValueType > > extract\_diagonal () const override

Extracts the diagonal entries of the matrix into a vector.

std::unique\_ptr< absolute\_type > compute\_absolute () const override

Gets the AbsoluteLinOp.

void compute\_absolute\_inplace () override

Compute absolute inplace on each element.

value\_type \* get\_values () noexcept

Returns the values of the matrix.

const value\_type \* get\_const\_values () const noexcept

Returns the values of the matrix.

index\_type \* get\_col\_idxs () noexcept

Returns the column indexes of the matrix.

const index\_type \* get\_const\_col\_idxs () const noexcept

Returns the column indexes of the matrix.

size\_type \* get\_slice\_lengths () noexcept

Returns the lengths(columns) of slices.

const size\_type \* get\_const\_slice\_lengths () const noexcept

Returns the lengths(columns) of slices.

size\_type \* get\_slice\_sets () noexcept

Returns the offsets of slices.

const size type \* get const slice sets () const noexcept

Returns the offsets of slices.

size\_type get\_slice\_size () const noexcept

Returns the size of a slice.

size\_type get\_stride\_factor () const noexcept

Returns the stride factor(t) of SELL-P.

size\_type get\_total\_cols () const noexcept

Returns the total column number.

size\_type get\_num\_stored\_elements () const noexcept

Returns the number of elements explicitly stored in the matrix.

• value\_type & val\_at (size\_type row, size\_type slice\_set, size\_type idx) noexcept

Returns the idx-th non-zero element of the row-th row with slice\_set slice set.

value\_type val\_at (size\_type row, size\_type slice\_set, size\_type idx) const noexcept

Returns the idx-th non-zero element of the row-th row with  $slice\_set$  slice set.

• index\_type & col\_at (size\_type row, size\_type slice\_set, size\_type idx) noexcept

Returns the idx-th column index of the row-th row with slice\_set slice set.

• index\_type col\_at (size\_type row, size\_type slice\_set, size\_type idx) const noexcept

Returns the idx-th column index of the row-th row with slice\_set slice set.

Sellp & operator= (const Sellp &)

Copy-assigns a Sellp matrix.

Sellp & operator= (Sellp &&)

Move-assigns a Sellp matrix.

• Sellp (const Sellp &)

Copy-assigns a Sellp matrix.

• Sellp (Sellp &&)

Move-assigns a Sellp matrix.

# **Static Public Member Functions**

static std::unique\_ptr< Sellp > create (std::shared\_ptr< const Executor > exec, const dim< 2 > &size={}, size\_type total\_cols=0)

Creates an uninitialized Sellp matrix of the specified size.

static std::unique\_ptr< Sellp > create (std::shared\_ptr< const Executor > exec, const dim< 2 > &size, size\_type slice\_size, size\_type stride\_factor, size\_type total\_cols)

Creates an uninitialized Sellp matrix of the specified size.

## 46.215.1 Detailed Description

```
template<typename ValueType = default_precision, typename IndexType = int32> class gko::matrix::Sellp< ValueType, IndexType >
```

SELL-P is a matrix format similar to ELL format.

The difference is that SELL-P format divides rows into smaller slices and store each slice with ELL format.

This implementation uses the column index value invalid\_index<IndexType>() to mark padding entries that are not part of the sparsity pattern.

## **Template Parameters**

ValueType	precision of matrix elements
IndexType	precision of matrix indexes

#### 46.215.2 Constructor & Destructor Documentation

## 46.215.2.1 Sellp() [1/2]

Copy-assigns a Sellp matrix.

Inherits the executor, copies the data and parameters.

#### 46.215.2.2 Sellp() [2/2]

Move-assigns a Sellp matrix.

Inherits the executor, moves the data and parameters. The moved-from object is empty (0x0 with valid slice\_sets and unchanged parameters).

# 46.215.3 Member Function Documentation

#### 46.215.3.1 col\_at() [1/2]

Returns the idx-th column index of the row-th row with slice\_set slice set.

#### **Parameters**

row	the row of the requested element in the slice
slice_set	the slice set of the slice
idx	the idx-th stored element of the row in the slice

#### Note

the method has to be called on the same Executor the matrix is stored at (e.g. trying to call this method on a GPU matrix from the CPU results in a runtime error)

```
268 {
269     return this
270          ->get_const_col_idxs()[this->linearize_index(row, slice_set, idx)];
271 }
```

#### 46.215.3.2 col\_at() [2/2]

Returns the idx-th column index of the row-th row with slice\_set slice set.

#### **Parameters**

row	the row of the requested element in the slice
slice_set	the slice set of the slice
idx	the idx-th stored element of the row in the slice

#### Note

the method has to be called on the same Executor the matrix is stored at (e.g. trying to call this method on a GPU matrix from the CPU results in a runtime error)

References gko::matrix::Sellp< ValueType, IndexType >::get\_col\_idxs().

#### 46.215.3.3 compute\_absolute()

```
template<typename ValueType = default_precision, typename IndexType = int32>
std::unique_ptr<absolute_type> gko::matrix::Sellp< ValueType, IndexType >::compute_absolute (
) const [override], [virtual]
```

Gets the AbsoluteLinOp.

#### Returns

a pointer to the new absolute object

Implements gko::EnableAbsoluteComputation< remove\_complex< Sellp< ValueType, IndexType >>>.

#### 46.215.3.4 create() [1/2]

Creates an uninitialized Sellp matrix of the specified size.

## **Parameters**

exec	Executor associated to the matrix
size	size of the matrix
slice_size	number of rows in each slice
stride_factor	factor for the stride in each slice (strides should be multiples of the stride_factor)
total_cols	number of the sum of all cols in every slice.

#### Returns

A smart pointer to the newly created matrix.

# 46.215.3.5 create() [2/2]

Creates an uninitialized Sellp matrix of the specified size.

(The slice\_size and stride\_factor are set to the default values.)

#### **Parameters**

exec	Executor associated to the matrix
size	size of the matrix
total_cols	number of the sum of all cols in every slice.

#### Returns

A smart pointer to the newly created matrix.

#### 46.215.3.6 extract diagonal()

```
template<typename ValueType = default_precision, typename IndexType = int32>
std::unique_ptr<Diagonal<ValueType> > gko::matrix::Sellp< ValueType, IndexType >::extract_
diagonal () const [override], [virtual]
```

Extracts the diagonal entries of the matrix into a vector.

## **Parameters**

```
diag the vector into which the diagonal will be written
```

Implements gko::DiagonalExtractable< ValueType >.

# 46.215.3.7 get\_col\_idxs()

```
template<typename ValueType = default_precision, typename IndexType = int32>
index_type* gko::matrix::Sellp< ValueType, IndexType >::get_col_idxs () [inline], [noexcept]
```

Returns the column indexes of the matrix.

#### Returns

the column indexes of the matrix.

References gko::array< ValueType >::get\_data().

Referenced by gko::matrix::Sellp< ValueType, IndexType >::col\_at().

## 46.215.3.8 get\_const\_col\_idxs()

```
template<typename ValueType = default_precision, typename IndexType = int32>
const index_type* gko::matrix::Sellp< ValueType, IndexType >::get_const_col_idxs ( ) const
[inline], [noexcept]
```

Returns the column indexes of the matrix.

#### Returns

the column indexes of the matrix.

#### Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

References gko::array< ValueType >::get\_const\_data().

## 46.215.3.9 get\_const\_slice\_lengths()

```
template<typename ValueType = default_precision, typename IndexType = int32>
const size_type* gko::matrix::Sellp< ValueType, IndexType >::get_const_slice_lengths ( ) const
[inline], [noexcept]
```

Returns the lengths(columns) of slices.

#### Returns

the lengths(columns) of slices.

#### Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

References gko::array< ValueType >::get\_const\_data().

## 46.215.3.10 get\_const\_slice\_sets()

```
template<typename ValueType = default_precision, typename IndexType = int32>
const size_type* gko::matrix::Sellp< ValueType, IndexType >::get_const_slice_sets ( ) const
[inline], [noexcept]
```

Returns the offsets of slices.

#### Returns

the offsets of slices.

#### Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

References gko::array< ValueType >::get const data().

#### 46.215.3.11 get\_const\_values()

```
template<typename ValueType = default_precision, typename IndexType = int32>
const value_type* gko::matrix::Sellp< ValueType, IndexType >::get_const_values ( ) const [inline],
[noexcept]
```

Returns the values of the matrix.

#### Returns

the values of the matrix.

## Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

References gko::array< ValueType >::get\_const\_data().

## 46.215.3.12 get\_num\_stored\_elements()

```
template<typename ValueType = default_precision, typename IndexType = int32>
size_type gko::matrix::Sellp< ValueType, IndexType >::get_num_stored_elements ( ) const [inline],
[noexcept]
```

Returns the number of elements explicitly stored in the matrix.

#### Returns

the number of elements explicitly stored in the matrix

References gko::array< ValueType >::get\_size().

#### 46.215.3.13 get\_slice\_lengths()

```
template<typename ValueType = default_precision, typename IndexType = int32>
size_type* gko::matrix::Sellp< ValueType, IndexType >::get_slice_lengths ( ) [inline], [noexcept]
```

Returns the lengths(columns) of slices.

#### Returns

the lengths(columns) of slices.

References gko::array< ValueType >::get\_data().

# 46.215.3.14 get\_slice\_sets()

```
template<typename ValueType = default_precision, typename IndexType = int32>
size_type* gko::matrix::Sellp< ValueType, IndexType >::get_slice_sets () [inline], [noexcept]
```

Returns the offsets of slices.

#### Returns

the offsets of slices.

# 46.215.3.15 get\_slice\_size()

```
template<typename ValueType = default_precision, typename IndexType = int32>
size_type gko::matrix::Sellp< ValueType, IndexType >::get_slice_size ( ) const [inline],
[noexcept]
```

Returns the size of a slice.

#### Returns

the size of a slice.

#### 46.215.3.16 get\_stride\_factor()

```
template<typename ValueType = default_precision, typename IndexType = int32>
size_type gko::matrix::Sellp< ValueType, IndexType >::get_stride_factor ( ) const [inline],
[noexcept]
```

Returns the stride factor(t) of SELL-P.

#### Returns

the stride factor(t) of SELL-P.

#### 46.215.3.17 get\_total\_cols()

```
template<typename ValueType = default_precision, typename IndexType = int32>
size_type gko::matrix::Sellp< ValueType, IndexType >::get_total_cols ( ) const [inline],
[noexcept]
```

Returns the total column number.

Returns

the total column number.

References gko::array< ValueType >::get\_size().

## 46.215.3.18 get\_values()

```
template<typename ValueType = default_precision, typename IndexType = int32>
value_type* gko::matrix::Sellp< ValueType, IndexType >::get_values () [inline], [noexcept]
```

Returns the values of the matrix.

Returns

the values of the matrix.

References gko::array< ValueType >::get\_data().

# 46.215.3.19 operator=() [1/2]

Copy-assigns a Sellp matrix.

Preserves the executor, copies the data and parameters.

## 46.215.3.20 operator=() [2/2]

Move-assigns a Sellp matrix.

Preserves the executor, moves the data and parameters. The moved-from object is empty (0x0 with valid slice\_sets and unchanged parameters).

# 46.215.3.21 read() [1/3]

Reads a matrix from a device\_matrix\_data structure.

#### **Parameters**

```
data the device_matrix_data structure.
```

Reimplemented from gko::ReadableFromMatrixData< ValueType, IndexType >.

## 46.215.3.22 read() [2/3]

Reads a matrix from a matrix\_data structure.

#### **Parameters**

```
data the matrix_data structure
```

Implements gko::ReadableFromMatrixData< ValueType, IndexType >.

## 46.215.3.23 read() [3/3]

Reads a matrix from a device\_matrix\_data structure.

The structure may be emptied by this function.

#### **Parameters**

```
data the device_matrix_data structure.
```

Reimplemented from gko::ReadableFromMatrixData< ValueType, IndexType >.

## 46.215.3.24 val\_at() [1/2]

Returns the idx-th non-zero element of the row-th row with slice\_set slice set.

#### **Parameters**

row	the row of the requested element in the slice
slice_set	the slice set of the slice
idx	the idx-th stored element of the row in the slice

#### Note

the method has to be called on the same Executor the matrix is stored at (e.g. trying to call this method on a GPU matrix from the CPU results in a runtime error)

References gko::array< ValueType >::get\_const\_data().

#### 46.215.3.25 val\_at() [2/2]

Returns the idx-th non-zero element of the row-th row with slice\_set slice set.

#### **Parameters**

row	the row of the requested element in the slice
slice_set	the slice set of the slice
idx	the idx-th stored element of the row in the slice

#### Note

the method has to be called on the same Executor the matrix is stored at (e.g. trying to call this method on a GPU matrix from the CPU results in a runtime error)

References gko::array< ValueType >::get\_data().

## 46.215.3.26 write()

Writes a matrix to a matrix data structure.

#### **Parameters**

```
data the matrix_data structure
```

Implements gko::WritableToMatrixData< ValueType, IndexType >.

The documentation for this class was generated from the following files:

- ginkgo/core/matrix/csr.hpp
- · ginkgo/core/matrix/sellp.hpp

# 46.216 gko::log::SolverProgress Class Reference

This Logger outputs the value of all scalar values (and potentially vectors) stored internally by the solver after each iteration.

```
#include <ginkgo/core/log/solver_progress.hpp>
```

#### **Static Public Member Functions**

static std::shared\_ptr< SolverProgress > create\_scalar\_table\_writer (std::ostream &output, int precision=6, int column width=12)

Creates a logger printing the value for all scalar values in the solver after each iteration in an ASCII table.

static std::shared\_ptr< SolverProgress > create\_scalar\_csv\_writer (std::ostream &output, int precision=6, char separator=',')

Creates a logger printing the value for all scalar values in the solver after each iteration in a CSV table.

Creates a logger storing all vectors and scalar values in the solver after each iteration on disk.

# 46.216.1 Detailed Description

This Logger outputs the value of all scalar values (and potentially vectors) stored internally by the solver after each iteration.

It needs to be attached to the solver being inspected.

## 46.216.2 Member Function Documentation

## 46.216.2.1 create\_scalar\_csv\_writer()

Creates a logger printing the value for all scalar values in the solver after each iteration in a CSV table.

If the solver is applied to multiple right-hand sides, only the first right-hand side gets printed.

#### **Parameters**

output	the stream to write the output to.
precision	the number of digits of precision to print
separator	the character separating columns from each other

# 46.216.2.2 create\_scalar\_table\_writer()

Creates a logger printing the value for all scalar values in the solver after each iteration in an ASCII table.

If the solver is applied to multiple right-hand sides, only the first right-hand side gets printed.

#### **Parameters**

output	the stream to write the output to.
precision	the number of digits of precision to print
column_width	the number of characters an output column is wide

#### 46.216.2.3 create vector storage()

Creates a logger storing all vectors and scalar values in the solver after each iteration on disk.

This logger can handle multiple right-hand sides, in contrast to create\_scalar\_table\_writer or create\_scalar\_csv\_← writer.

#### **Parameters**

output	the path and file name prefix used to generate the output file names.
precision	the number of digits of precision to print when outputting matrices in text format
binary	if true, write data in Ginkgo's own binary format (lossless), if false write data in the MatrixMarket format (potentially lossy)

The documentation for this class was generated from the following file:

ginkgo/core/log/solver\_progress.hpp

# 46.217 gko::span Struct Reference

A span is a lightweight structure used to create sub-ranges from other ranges.

```
#include <ginkgo/core/base/range.hpp>
```

#### **Public Member Functions**

• constexpr span (size\_type point) noexcept

Creates a span representing a point point.

constexpr span (size\_type begin, size\_type end) noexcept

Creates a span.

• constexpr bool is\_valid () const

Checks if a span is valid.

constexpr size\_type length () const

Returns the length of a span.

#### **Public Attributes**

const size\_type begin

Beginning of the span.const size\_type end

End of the span.

# 46.217.1 Detailed Description

A span is a lightweight structure used to create sub-ranges from other ranges.

A span s represents a contiguous set of indexes in one dimension of the range, starting on index s.begin (inclusive) and ending at index s.end (exclusive). A span is only valid if its starting index is smaller than its ending index.

Spans can be compared using the == and != operators. Two spans are identical if both their begin and end values are identical.

Spans also have two distinct partial orders defined on them:

```
1. x < y (y > x) if and only if x.end < y.begin
```

2. 
$$x \ll y (y \gg x)$$
 if and only if x.end  $\ll y$ .begin

Note that the orders are in fact partial - there are spans x and y for which none of the following inequalities holds: x < y, x > y, x == y, x <= y, x >= y. An example are spans  $span\{0, 2\}$  and  $span\{1, 3\}$ .

In addition, <= is a distinct order from <, and not just an extension of the strict order to its weak equivalent. Thus, x <= y is not equivalent to  $x < y \mid \mid x == y$ .

#### 46.217.2 Constructor & Destructor Documentation

```
46.217.2.1 span() [1/2]
```

Creates a span representing a point point.

The begin of this span is set to point, and the end to point + 1.

#### **Parameters**

point	the point which the span represents
-------	-------------------------------------

## 46.217.2.2 span() [2/2]

Creates a span.

#### **Parameters**

begin	the beginning of the span
end	the end of the span

References begin.

## 46.217.3 Member Function Documentation

## 46.217.3.1 is\_valid()

```
constexpr bool gko::span::is_valid ( ) const [inline], [constexpr]
```

Checks if a span is valid.

Returns

```
true if and only if this->begin <= this->end
```

References begin, and end.

Referenced by gko::accessor::row\_major< ValueType, Dimensionality >::operator()().

## 46.217.3.2 length()

```
constexpr size_type gko::span::length ( ) const [inline], [constexpr]
```

Returns the length of a span.

Returns

```
this->end - this->begin
```

References begin, and end.

The documentation for this struct was generated from the following file:

• ginkgo/core/base/range.hpp

# 46.218 gko::matrix::Csr< ValueType, IndexType >::sparselib Class Reference

sparselib is a strategy\_type which uses the sparselib csr.

```
#include <ginkgo/core/matrix/csr.hpp>
```

#### **Public Member Functions**

• sparselib ()

Creates a sparselib strategy.

- void process (const array < index\_type > &mtx\_row\_ptrs, array < index\_type > \*mtx\_srow) override
   Computes srow according to row pointers.
- int64\_t clac\_size (const int64\_t nnz) override

Computes the srow size according to the number of nonzeros.

-  $std::shared\_ptr < strategy\_type > copy$  () override

Copy a strategy.

# 46.218.1 Detailed Description

```
template < typename ValueType = default_precision, typename IndexType = int32 > class gko::matrix::Csr < ValueType, IndexType >::sparselib
```

sparselib is a strategy\_type which uses the sparselib csr.

Note

Uses cusparse in cuda and hipsparse in hip.

## 46.218.2 Member Function Documentation

## 46.218.2.1 clac\_size()

Computes the srow size according to the number of nonzeros.

#### **Parameters**

nnz the number of nonzeros

#### Returns

the size of srow

Implements gko::matrix::Csr< ValueType, IndexType >::strategy type.

## 46.218.2.2 copy()

```
template<typename ValueType = default_precision, typename IndexType = int32>
std::shared_ptr<strategy_type> gko::matrix::Csr< ValueType, IndexType >::sparselib::copy ( )
[inline], [override], [virtual]
```

Copy a strategy.

This is a workaround until strategies are revamped, since strategies like automatical do not work when actually shared.

Implements gko::matrix::Csr< ValueType, IndexType >::strategy\_type.

#### 46.218.2.3 process()

Computes srow according to row pointers.

#### **Parameters**

mtx_row_ptrs	the row pointers of the matrix
mtx_srow	the srow of the matrix

Implements gko::matrix::Csr< ValueType, IndexType >::strategy\_type.

The documentation for this class was generated from the following file:

• ginkgo/core/matrix/csr.hpp

# 46.219 gko::matrix::SparsityCsr< ValueType, IndexType > Class Template Reference

SparsityCsr is a matrix format which stores only the sparsity pattern of a sparse matrix by compressing each row of the matrix (compressed sparse row format).

#include <ginkgo/core/matrix/sparsity\_csr.hpp>

#### **Public Member Functions**

void read (const mat\_data &data) override

Reads a matrix from a matrix data structure.

void read (const device\_mat\_data &data) override

Reads a matrix from a device\_matrix\_data structure.

void read (device\_mat\_data &&data) override

Reads a matrix from a device\_matrix\_data structure.

void write (mat\_data &data) const override

Writes a matrix to a matrix\_data structure.

• std::unique\_ptr< LinOp > transpose () const override

Returns a LinOp representing the transpose of the Transposable object.

std::unique\_ptr< LinOp > conj\_transpose () const override

Returns a LinOp representing the conjugate transpose of the Transposable object.

• std::unique\_ptr< SparsityCsr > to\_adjacency\_matrix () const

Transforms the sparsity matrix to an adjacency matrix.

void sort\_by\_column\_index ()

Sorts each row by column index.

index\_type \* get\_col\_idxs () noexcept

Returns the column indices of the matrix.

• const index\_type \* get\_const\_col\_idxs () const noexcept

Returns the column indices of the matrix.

index\_type \* get\_row\_ptrs () noexcept

Returns the row pointers of the matrix.

const index\_type \* get\_const\_row\_ptrs () const noexcept

Returns the row pointers of the matrix.

value\_type \* get\_value () noexcept

Returns the value stored in the matrix.

const value\_type \* get\_const\_value () const noexcept

Returns the value stored in the matrix.

• size\_type get\_num\_nonzeros () const noexcept

Returns the number of elements explicitly stored in the matrix.

SparsityCsr & operator= (const SparsityCsr &)

Copy-assigns a SparsityCsr matrix.

SparsityCsr & operator= (SparsityCsr &&)

Move-assigns a SparsityCsr matrix.

SparsityCsr (const SparsityCsr &)

Copy-constructs a SparsityCsr matrix.

SparsityCsr (SparsityCsr &&)

Move-constructs a SparsityCsr matrix.

## **Static Public Member Functions**

static std::unique\_ptr< SparsityCsr > create (std::shared\_ptr< const Executor > exec, const dim< 2 > &size=dim< 2 >{}, size\_type num\_nonzeros={})

Creates an uninitialized SparsityCsr matrix of the specified size.

static std::unique\_ptr< SparsityCsr > create (std::shared\_ptr< const Executor > exec, const dim< 2 > &size, array< index\_type > col\_idxs, array< index\_type > row\_ptrs, value\_type value=one< ValueType >())

Creates a SparsityCsr matrix from already allocated (and initialized) row pointer and column index arrays.

template<typename CollndexType, typename RowPtrType >
 static std::unique\_ptr< SparsityCsr > create (std::shared\_ptr< const Executor > exec, const dim< 2 >
 &size, std::initializer\_list< CollndexType > col\_idxs, std::initializer\_list< RowPtrType > row\_ptrs, value\_type
 value=one< ValueType >())

create(std::shared\_ptr<const

static std::unique\_ptr< SparsityCsr > create (std::shared\_ptr< const Executor > exec, std::shared\_ptr< const LinOp > matrix)

Creates a Sparsity matrix from an existing matrix.

static std::unique\_ptr< const SparsityCsr > create\_const (std::shared\_ptr< const Executor > exec, const dim< 2 > &size, gko::detail::const\_array\_view< IndexType > &&col\_idxs, gko::detail::const\_array\_view< IndexType > &&row\_ptrs, ValueType value=one< ValueType >())

Creates a constant (immutable) SparsityCsr matrix from constant arrays.

## 46.219.1 Detailed Description

```
template<typename ValueType = default_precision, typename IndexType = int32> class gko::matrix::SparsityCsr< ValueType, IndexType >
```

SparsityCsr is a matrix format which stores only the sparsity pattern of a sparse matrix by compressing each row of the matrix (compressed sparse row format).

The values of the nonzero elements are stored as a value array of length 1. All the values in the matrix are equal to this value. By default, this value is set to 1.0. A row pointer array also stores the linearized starting index of each row. An additional column index array is used to identify the column where a nonzero is present.

#### **Template Parameters**

ValueType	precision of vectors in apply
IndexType	precision of matrix indexes

#### 46.219.2 Constructor & Destructor Documentation

#### 46.219.2.1 SparsityCsr() [1/2]

Copy-constructs a SparsityCsr matrix.

Inherits executor, strategy and data.

#### 46.219.2.2 SparsityCsr() [2/2]

Move-constructs a SparsityCsr matrix.

Inherits executor, moves the data and leaves the moved-from object in an empty state (0x0 LinOp with unchanged executor, no nonzeros and valid row pointers).

## 46.219.3 Member Function Documentation

## 46.219.3.1 conj\_transpose()

```
template<typename ValueType = default_precision, typename IndexType = int32>
std::unique_ptr<LinOp> gko::matrix::SparsityCsr< ValueType, IndexType >::conj_transpose ( )
const [override], [virtual]
```

Returns a LinOp representing the conjugate transpose of the Transposable object.

#### Returns

a pointer to the new conjugate transposed object

Implements gko::Transposable.

## 46.219.3.2 create() [1/4]

Creates a SparsityCsr matrix from already allocated (and initialized) row pointer and column index arrays.

## **Template Parameters**

ColldxsArray	type of col_idxs array
RowPtrsArray	type of row_ptrs array

#### Parameters

exec	Executor associated to the matrix
size	size of the matrix
col_idxs	array of column indexes
row_ptrs	array of row pointers
value	value stored. (same value for all matrix elements)

Note

If one of row\_ptrs or col\_idxs is not an rvalue, not an array of IndexType and IndexType respectively, or is on the wrong executor, an internal copy of that array will be created, and the original array data will not be used in the matrix.

## 46.219.3.3 create() [2/4]

create(std::shared\_ptr<const

create(std::shared\_ptr<const executor>="">, const dim<2>&, array<index\_type>, array<index\_type>, value <--

References gko::matrix::SparsityCsr< ValueType, IndexType >::create().

# 46.219.3.4 create() [3/4]

Creates an uninitialized SparsityCsr matrix of the specified size.

#### **Parameters**

exec	Executor associated to the matrix	
size	size of the matrix	
num_nonzeros	number of nonzeros	

 $\label{lem:conditional} Referenced \ by \ gko::matrix::SparsityCsr< \ ValueType, \ IndexType >::create().$ 

#### 46.219.3.5 create() [4/4]

Creates a Sparsity matrix from an existing matrix.

Uses the copy\_and\_convert\_to functionality.

#### **Parameters**

exec	Executor associated to the matrix
matrix	The input matrix

#### 46.219.3.6 create\_const()

Creates a constant (immutable) SparsityCsr matrix from constant arrays.

## Parameters

exec	the executor to create the matrix on
size	the dimensions of the matrix
values	the value array of the matrix
col_idxs	the column index array of the matrix
row_ptrs	the row pointer array of the matrix
strategy	the strategy the matrix uses for SpMV operations

## Returns

A smart pointer to the constant matrix wrapping the input arrays (if they reside on the same executor as the matrix) or a copy of these arrays on the correct executor.

#### 46.219.3.7 get\_col\_idxs()

```
template<typename ValueType = default_precision, typename IndexType = int32>
index_type* gko::matrix::SparsityCsr< ValueType, IndexType >::get_col_idxs ( ) [inline],
[noexcept]
```

Returns the column indices of the matrix.

#### Returns

the column indices of the matrix.

References gko::array< ValueType >::get\_data().

#### 46.219.3.8 get\_const\_col\_idxs()

```
template<typename ValueType = default_precision, typename IndexType = int32>
const index_type* gko::matrix::SparsityCsr< ValueType, IndexType >::get_const_col_idxs ( )
const [inline], [noexcept]
```

Returns the column indices of the matrix.

#### Returns

the column indices of the matrix.

#### Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

References gko::array< ValueType >::get\_const\_data().

#### 46.219.3.9 get\_const\_row\_ptrs()

```
template<typename ValueType = default_precision, typename IndexType = int32>
const index_type* gko::matrix::SparsityCsr< ValueType, IndexType >::get_const_row_ptrs ( )
const [inline], [noexcept]
```

Returns the row pointers of the matrix.

#### Returns

the row pointers of the matrix.

## Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

References gko::array< ValueType >::get\_const\_data().

## 46.219.3.10 get\_const\_value()

```
template<typename ValueType = default_precision, typename IndexType = int32>
const value_type* gko::matrix::SparsityCsr< ValueType, IndexType >::get_const_value ( ) const
[inline], [noexcept]
```

Returns the value stored in the matrix.

#### Returns

the value of the matrix.

#### Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

References gko::array< ValueType >::get\_const\_data().

## 46.219.3.11 get\_num\_nonzeros()

```
template<typename ValueType = default_precision, typename IndexType = int32>
size_type gko::matrix::SparsityCsr< ValueType, IndexType >::get_num_nonzeros ( ) const [inline],
[noexcept]
```

Returns the number of elements explicitly stored in the matrix.

## Returns

the number of elements explicitly stored in the matrix

References gko::array< ValueType >::get\_size().

## 46.219.3.12 get\_row\_ptrs()

```
template<typename ValueType = default_precision, typename IndexType = int32>
index_type* gko::matrix::SparsityCsr< ValueType, IndexType >::get_row_ptrs ( ) [inline],
[noexcept]
```

Returns the row pointers of the matrix.

## Returns

the row pointers of the matrix.

References gko::array< ValueType >::get\_data().

#### 46.219.3.13 get\_value()

```
template<typename ValueType = default_precision, typename IndexType = int32>
value_type* gko::matrix::SparsityCsr< ValueType, IndexType >::get_value ( ) [inline], [noexcept]
```

Returns the value stored in the matrix.

#### Returns

the value of the matrix.

References gko::array< ValueType >::get\_data().

#### 46.219.3.14 operator=() [1/2]

Copy-assigns a SparsityCsr matrix.

Preserves executor, copies everything else.

#### 46.219.3.15 operator=() [2/2]

Move-assigns a SparsityCsr matrix.

Preserves executor, moves the data and leaves the moved-from object in an empty state (0x0 LinOp with unchanged executor, no nonzeros and valid row pointers).

## 46.219.3.16 read() [1/3]

Reads a matrix from a device\_matrix\_data structure.

#### **Parameters**

```
data the device matrix data structure.
```

 $\label{lem:lemented_from_gko::ReadableFromMatrixData} Reimplemented from gko:: ReadableFromMatrixData < ValueType, IndexType >.$ 

#### 46.219.3.17 read() [2/3]

Reads a matrix from a matrix\_data structure.

#### **Parameters**

```
data the matrix_data structure
```

Implements gko::ReadableFromMatrixData< ValueType, IndexType >.

#### 46.219.3.18 read() [3/3]

Reads a matrix from a device\_matrix\_data structure.

The structure may be emptied by this function.

#### **Parameters**

```
data the device_matrix_data structure.
```

 $\label{lem:lemented$ 

## 46.219.3.19 to\_adjacency\_matrix()

```
template<typename ValueType = default_precision, typename IndexType = int32> std::unique_ptr<SparsityCsr> gko::matrix::SparsityCsr< ValueType, IndexType >::to_adjacency← _matrix ( ) const
```

Transforms the sparsity matrix to an adjacency matrix.

As the adjacency matrix has to be square, the input SparsityCsr matrix for this function to work has to be square.

Note

The adjacency matrix in this case is the sparsity pattern but with the diagonal ones removed. This is mainly used for the reordering/partitioning as taken in by graph libraries such as METIS.

#### 46.219.3.20 transpose()

```
template<typename ValueType = default_precision, typename IndexType = int32>
std::unique_ptr<LinOp> gko::matrix::SparsityCsr< ValueType, IndexType >::transpose ( ) const
[override], [virtual]
```

Returns a LinOp representing the transpose of the Transposable object.

#### Returns

a pointer to the new transposed object

Implements gko::Transposable.

#### 46.219.3.21 write()

Writes a matrix to a matrix\_data structure.

#### **Parameters**

```
data the matrix_data structure
```

Implements gko::WritableToMatrixData< ValueType, IndexType >.

The documentation for this class was generated from the following files:

- · ginkgo/core/matrix/csr.hpp
- ginkgo/core/matrix/sparsity\_csr.hpp

# 46.220 gko::experimental::mpi::status Struct Reference

The status struct is a light wrapper around the MPI\_Status struct.

```
#include <ginkgo/core/base/mpi.hpp>
```

#### **Public Member Functions**

• status ()

The default constructor.

• MPI\_Status \* get ()

Get a pointer to the underlying MPI\_Status object.

• template<typename T >

```
int get_count (const T *data) const
```

Get the count of the number of elements received by the communication call.

# 46.220.1 Detailed Description

The status struct is a light wrapper around the MPI\_Status struct.

# 46.220.2 Constructor & Destructor Documentation

# 46.220.2.1 status()

```
gko::experimental::mpi::status::status ( ) [inline]
```

The default constructor.

It creates an empty MPI\_Status

## 46.220.3 Member Function Documentation

## 46.220.3.1 get()

```
MPI_Status* gko::experimental::mpi::status::get ( ) [inline]
```

Get a pointer to the underlying MPI\_Status object.

Returns

a pointer to MPI\_Status object

Referenced by gko::experimental::mpi::communicator::recv(), and gko::experimental::mpi::request::wait().

#### 46.220.3.2 get\_count()

```
\label{template} $$ template < typename T > $$ int gko::experimental::mpi::status::get_count ( $$ const T * data ) const [inline] $$
```

Get the count of the number of elements received by the communication call.

**Template Parameters** 

 $T \mid$  The datatype of the object that was received.

#### **Parameters**

data The data object of type T that was received.

#### Returns

the count

The documentation for this struct was generated from the following file:

• ginkgo/core/base/mpi.hpp

# 46.221 gko::stopping\_status Class Reference

This class is used to keep track of the stopping status of one vector.

#include <ginkgo/core/stop/stopping\_status.hpp>

#### **Public Member Functions**

· bool has stopped () const noexcept

Check if any stopping criteria was fulfilled.

bool has\_converged () const noexcept

Check if convergence was reached.

· bool is\_finalized () const noexcept

Check if the corresponding vector stores the finalized result.

• uint8 get\_id () const noexcept

Get the id of the stopping criterion which caused the stop.

· void reset () noexcept

Clear all flags.

· void stop (uint8 id, bool set finalized=true) noexcept

Call if a stop occurred due to a hard limit (and convergence was not reached).

void converge (uint8 id, bool set\_finalized=true) noexcept

Call if convergence occurred.

· void finalize () noexcept

Set the result to be finalized (it needs to be stopped or converged first).

#### **Friends**

• bool operator== (const stopping\_status &x, const stopping\_status &y) noexcept

• bool operator!= (const stopping\_status &x, const stopping\_status &y) noexcept

# 46.221.1 Detailed Description

This class is used to keep track of the stopping status of one vector.

Checks if two stopping statuses are equivalent.

Checks if two stopping statuses are different.

# 46.221.2 Member Function Documentation

# 46.221.2.1 converge()

Call if convergence occurred.

#### **Parameters**

id	id of the stopping criteria.
set_finalized	Controls if the current version should count as finalized (set to true) or not (set to false).

References has\_stopped().

## 46.221.2.2 get\_id()

```
uint8 gko::stopping_status::get_id ( ) const [inline], [noexcept]
```

Get the id of the stopping criterion which caused the stop.

## Returns

Returns the id of the stopping criterion which caused the stop.

Referenced by has\_stopped().

## 46.221.2.3 has\_converged()

```
bool gko::stopping_status::has_converged ( ) const [inline], [noexcept]
```

Check if convergence was reached.

## Returns

Returns true if convergence was reached.

#### 46.221.2.4 has\_stopped()

```
bool gko::stopping_status::has_stopped ( ) const [inline], [noexcept]
```

Check if any stopping criteria was fulfilled.

#### Returns

Returns true if any stopping criteria was fulfilled.

References get\_id().

Referenced by converge(), finalize(), and stop().

## 46.221.2.5 is\_finalized()

```
bool gko::stopping_status::is_finalized ( ) const [inline], [noexcept]
```

Check if the corresponding vector stores the finalized result.

#### Returns

Returns true if the corresponding vector stores the finalized result.

#### 46.221.2.6 stop()

Call if a stop occurred due to a hard limit (and convergence was not reached).

## **Parameters**

id	id of the stopping criteria.
set_finalized	Controls if the current version should count as finalized (set to true) or not (set to false).

References has\_stopped().

# 46.221.3 Friends And Related Function Documentation

## 46.221.3.1 operator"!=

Checks if two stopping statuses are different.

#### **Parameters**

X	a stopping status
У	a stopping status

#### Returns

```
true if and only if ! (x == y)
```

## 46.221.3.2 operator==

Checks if two stopping statuses are equivalent.

#### **Parameters**

X	a stopping status
V	a stopping status

#### Returns

true if and only if both  $\boldsymbol{x}$  and  $\boldsymbol{y}$  have the same mask and converged and finalized state

The documentation for this class was generated from the following file:

• ginkgo/core/stop/stopping\_status.hpp

# 46.222 gko::matrix::Csr< ValueType, IndexType >::strategy\_type Class Reference

strategy\_type is to decide how to set the csr algorithm.

```
#include <ginkgo/core/matrix/csr.hpp>
```

#### **Public Member Functions**

• strategy\_type (std::string name)

Creates a strategy\_type.

• std::string get\_name ()

Returns the name of strategy.

- virtual void process (const array< index\_type > &mtx\_row\_ptrs, array< index\_type > \*mtx\_srow)=0
   Computes srow according to row pointers.
- virtual int64\_t clac\_size (const int64\_t nnz)=0

Computes the srow size according to the number of nonzeros.

virtual std::shared\_ptr< strategy\_type > copy ()=0
 Copy a strategy.

# 46.222.1 Detailed Description

```
template<typename ValueType = default_precision, typename IndexType = int32> class gko::matrix::Csr< ValueType, IndexType >::strategy_type
```

strategy\_type is to decide how to set the csr algorithm.

The practical strategy method should inherit strategy\_type and implement its process,  $clac_size$  function and the corresponding device kernel.

#### 46.222.2 Constructor & Destructor Documentation

# 46.222.2.1 strategy\_type()

Creates a strategy\_type.

### **Parameters**

```
name the name of strategy
```

## 46.222.3 Member Function Documentation

#### 46.222.3.1 clac\_size()

```
template<typename ValueType = default_precision, typename IndexType = int32>
virtual int64_t gko::matrix::Csr< ValueType, IndexType >::strategy_type::clac_size (
```

```
const int64_t nnz ) [pure virtual]
```

Computes the srow size according to the number of nonzeros.

#### **Parameters**

```
nnz the number of nonzeros
```

#### Returns

the size of srow

Implemented in gko::matrix::Csr< ValueType, IndexType >::load\_balance, gko::matrix::Csr< ValueType, IndexType >::sparselib, gko::matrix::Csr< ValueType, IndexType >::cusparse, gko::matrix::Csr< ValueType, IndexType >::merge\_path, and gko::matrix::Csr< ValueType, IndexType >::classical.

#### 46.222.3.2 copy()

```
template<typename ValueType = default_precision, typename IndexType = int32>
virtual std::shared_ptr<strategy_type> gko::matrix::Csr< ValueType, IndexType >::strategy_\times
type::copy ( ) [pure virtual]
```

#### Copy a strategy.

This is a workaround until strategies are revamped, since strategies like automatical do not work when actually shared.

Implemented in gko::matrix::Csr< ValueType, IndexType >::load\_balance, gko::matrix::Csr< ValueType, IndexType >::sparselib, gko::matrix::Csr< ValueType, IndexType >::cusparse, gko::matrix::Csr< ValueType, IndexType >::merge\_path, and gko::matrix::Csr< ValueType, IndexType >::classical.

#### 46.222.3.3 get name()

```
template<typename ValueType = default_precision, typename IndexType = int32>
std::string gko::matrix::Csr< ValueType, IndexType >::strategy_type::get_name () [inline]
```

Returns the name of strategy.

#### Returns

the name of strategy

## 46.222.3.4 process()

Computes srow according to row pointers.

#### **Parameters**

mtx_row_ptrs	the row pointers of the matrix
mtx_srow	the srow of the matrix

Implemented in gko::matrix::Csr< ValueType, IndexType >::load\_balance, gko::matrix::Csr< ValueType, IndexType >::sparselib, gko::matrix::Csr< ValueType, IndexType >::cusparse, gko::matrix::Csr< ValueType, IndexType >::merge\_path, and gko::matrix::Csr< ValueType, IndexType >::classical.

The documentation for this class was generated from the following file:

· ginkgo/core/matrix/csr.hpp

# 46.223 gko::matrix::Hybrid< ValueType, IndexType >::strategy\_type Class Reference

strategy\_type is to decide how to set the hybrid config.

#include <qinkgo/core/matrix/hybrid.hpp>

#### **Public Member Functions**

• strategy\_type ()

Creates a strategy\_type.

void compute\_hybrid\_config (const array < size\_type > &row\_nnz, size\_type \*ell\_num\_stored\_elements\_←
per\_row, size\_type \*coo\_nnz)

Computes the config of the Hybrid matrix (ell\_num\_stored\_elements\_per\_row and coo\_nnz).

• size\_type get\_ell\_num\_stored\_elements\_per\_row () const noexcept

Returns the number of stored elements per row of the ell part.

• size\_type get\_coo\_nnz () const noexcept

Returns the number of nonzeros of the coo part.

• virtual size\_type compute\_ell\_num\_stored\_elements\_per\_row (array< size\_type > \*row\_nnz) const =0

Computes the number of stored elements per row of the ell part.

# 46.223.1 Detailed Description

template<typename ValueType = default\_precision, typename IndexType = int32> class gko::matrix::Hybrid< ValueType, IndexType >::strategy\_type

strategy\_type is to decide how to set the hybrid config.

It computes the number of stored elements per row of the ell part and then set the number of residual nonzeros as the number of nonzeros of the coo part.

The practical strategy method should inherit strategy\_type and implement its  $compute_ell_num_stored\_\leftarrow elements\_per\_row function$ .

#### 46.223.2 Member Function Documentation

### 46.223.2.1 compute\_ell\_num\_stored\_elements\_per\_row()

Computes the number of stored elements per row of the ell part.

#### **Parameters**

row	nnz	the number of nonzeros of each row
-----	-----	------------------------------------

#### Returns

the number of stored elements per row of the ell part

Implemented in gko::matrix::Hybrid< ValueType, IndexType >::automatic, gko::matrix::Hybrid< ValueType, IndexType >::minimal\_stagko::matrix::Hybrid< ValueType, IndexType >::imbalance\_bounded\_limit, gko::matrix::Hybrid< ValueType, IndexType >::imbalance\_and gko::matrix::Hybrid< ValueType, IndexType >::column\_limit.

Referenced by gko::matrix::Hybrid < ValueType, IndexType >::strategy type::compute hybrid config().

## 46.223.2.2 compute\_hybrid\_config()

Computes the config of the Hybrid matrix (ell\_num\_stored\_elements\_per\_row and coo\_nnz).

For now, it copies row nnz to the reference executor and performs all operations on the reference executor.

#### **Parameters**

row_nnz	the number of nonzeros of each row
ell_num_stored_elements_per_row	the output number of stored elements per row of the ell part
coo_nnz	the output number of nonzeros of the coo part

References gko::matrix::Hybrid< ValueType, IndexType >::strategy\_type::compute\_ell\_num\_stored\_elements\_ per\_row(), gko::array< ValueType >::get\_executor(), and gko::array< ValueType >::get\_size().

## 46.223.2.3 get\_coo\_nnz()

```
template<typename ValueType = default_precision, typename IndexType = int32>
size_type gko::matrix::Hybrid< ValueType, IndexType >::strategy_type::get_coo_nnz ( ) const
[inline], [noexcept]
```

Returns the number of nonzeros of the coo part.

#### Returns

the number of nonzeros of the coo part

#### 46.223.2.4 get\_ell\_num\_stored\_elements\_per\_row()

```
template<typename ValueType = default_precision, typename IndexType = int32>
size_type gko::matrix::Hybrid< ValueType, IndexType >::strategy_type::get_ell_num_stored_←
elements_per_row ( ) const [inline], [noexcept]
```

Returns the number of stored elements per row of the ell part.

#### Returns

the number of stored elements per row of the ell part

The documentation for this class was generated from the following file:

ginkgo/core/matrix/hybrid.hpp

# 46.224 gko::log::Stream < ValueType > Class Template Reference

Stream is a Logger which logs every event to a stream.

```
#include <ginkgo/core/log/stream.hpp>
```

# **Static Public Member Functions**

- - Creates a Stream logger.
- static std::unique\_ptr < Stream > create (const Logger::mask\_type &enabled\_events=Logger::all\_events\_
   — mask, std::ostream &os=std::cerr, bool verbose=false)

Creates a Stream logger.

# 46.224.1 Detailed Description

```
template<typename ValueType = default_precision> class gko::log::Stream< ValueType >
```

Stream is a Logger which logs every event to a stream.

This can typically be used to log to a file or to the console.

# **Template Parameters**

ValueType	the type of values stored in the class (i.e. ValueType template parameter of the concrete Loggable	1
	this class will log)	

# 46.224.2 Member Function Documentation

# 46.224.2.1 create() [1/2]

# Creates a Stream logger.

This dynamically allocates the memory, constructs the object and returns an std::unique\_ptr to this object.

#### **Parameters**

exec	the executor
enabled_events	the events enabled for this logger. By default all events.
os	the stream used for this logger
verbose	whether we want detailed information or not. This includes always printing residuals and other information which can give a large output.

#### Returns

an std::unique\_ptr to the the constructed object

```
195 {
196     return std::unique_ptr<Stream>(new Stream(enabled_events, os, verbose));
197 }
```

# 46.224.2.2 create() [2/2]

# Creates a Stream logger.

This dynamically allocates the memory, constructs the object and returns an std::unique\_ptr to this object.

#### **Parameters**

exec	the executor
enabled_events	the events enabled for this logger. By default all events.
os	the stream used for this logger
verbose	whether we want detailed information or not. This includes always printing residuals and other information which can give a large output.

## Returns

an std::unique\_ptr to the the constructed object

The documentation for this class was generated from the following file:

• ginkgo/core/log/stream.hpp

# 46.225 gko::StreamError Class Reference

StreamError is thrown if accessing a stream failed.

```
#include <ginkgo/core/base/exception.hpp>
```

# **Public Member Functions**

• StreamError (const std::string &file, int line, const std::string &func, const std::string &message)

Initializes a file access error.

# 46.225.1 Detailed Description

StreamError is thrown if accessing a stream failed.

# 46.225.2 Constructor & Destructor Documentation

# 46.225.2.1 StreamError()

Initializes a file access error.

#### **Parameters**

file	The name of the offending source file
line	The source code line number where the error occurred
func	The name of the function that tried to access the file
message	The error message

The documentation for this class was generated from the following file:

• ginkgo/core/base/exception.hpp

# 46.226 gko::log::ProfilerHook::SummaryWriter Class Reference

Receives the results from ProfilerHook::create\_summary().

```
#include <ginkgo/core/log/profiler_hook.hpp>
```

#### **Public Member Functions**

virtual void write (const std::vector< summary\_entry > &entries, std::chrono::nanoseconds overhead)=0
 Callback to write out the summary results.

# 46.226.1 Detailed Description

Receives the results from ProfilerHook::create\_summary().

# 46.226.2 Member Function Documentation

# 46.226.2.1 write()

Callback to write out the summary results.

#### **Parameters**

entries	the vector of ranges with runtime and count.
overhead	an estimate of the profiler overhead

Implemented in gko::log::ProfilerHook::TableSummaryWriter.

The documentation for this class was generated from the following file:

• ginkgo/core/log/profiler\_hook.hpp

# 46.227 gko::log::ProfilerHook::TableSummaryWriter Class Reference

Writes the results from ProfilerHook::create\_summary() and ProfilerHook::create\_nested\_summary() to a ASCII table in Markdown format.

```
#include <ginkgo/core/log/profiler_hook.hpp>
```

# **Public Member Functions**

- TableSummaryWriter (std::ostream &output=std::cerr, std::string header="Runtime summary")

  Constructs a writer on an output stream.
- void write (const std::vector< summary\_entry > &entries, std::chrono::nanoseconds overhead) override Callback to write out the summary results.
- void write\_nested (const nested\_summary\_entry &root, std::chrono::nanoseconds overhead) override
   Callback to write out the summary results.

# 46.227.1 Detailed Description

Writes the results from ProfilerHook::create\_summary() and ProfilerHook::create\_nested\_summary() to a ASCII table in Markdown format.

# 46.227.2 Constructor & Destructor Documentation

## 46.227.2.1 TableSummaryWriter()

Constructs a writer on an output stream.

#### **Parameters**

output	the output stream to write the table to.
header	the header to write above the table.

# 46.227.3 Member Function Documentation

# 46.227.3.1 write()

Callback to write out the summary results.

#### **Parameters**

entries	the vector of ranges with runtime and count.
overhead	an estimate of the profiler overhead

Implements gko::log::ProfilerHook::SummaryWriter.

# 46.227.3.2 write\_nested()

Callback to write out the summary results.

# **Parameters**

root	the root range with runtime and count.
overhead	an estimate of the profiler overhead

 $Implements\ gko:: log:: Profiler Hook:: Nested Summary Writer.$ 

The documentation for this class was generated from the following file:

• ginkgo/core/log/profiler\_hook.hpp

# 46.228 gko::stop::Time Class Reference

The Time class is a stopping criterion which stops the iteration process after a certain amount of time has passed.

```
#include <ginkgo/core/stop/time.hpp>
```

# 46.228.1 Detailed Description

The Time class is a stopping criterion which stops the iteration process after a certain amount of time has passed.

The documentation for this class was generated from the following file:

· ginkgo/core/stop/time.hpp

# 46.229 gko::time point Class Reference

An opaque wrapper for a time point generated by a timer.

#include <ginkgo/core/base/timer.hpp>

# 46.229.1 Detailed Description

An opaque wrapper for a time point generated by a timer.

The documentation for this class was generated from the following file:

· ginkgo/core/base/timer.hpp

# 46.230 gko::Timer Class Reference

Represents a generic timer that can be used to record time points and measure time differences on host or device streams.

#include <ginkgo/core/base/timer.hpp>

## **Public Member Functions**

• time\_point create\_time\_point ()

Returns a newly created time point.

virtual void record (time\_point &time)=0

Records a time point at the current time.

• virtual void wait (time\_point &time)=0

Waits until all kernels in-process when recording the time point are finished.

std::chrono::nanoseconds difference (time\_point &start, time\_point &stop)

Computes the difference between the two time points in nanoseconds.

• virtual std::chrono::nanoseconds difference\_async (const time\_point &start, const time\_point &stop)=0

Computes the difference between the two time points in nanoseconds.

# **Static Public Member Functions**

static std::unique\_ptr < Timer > create\_for\_executor (std::shared\_ptr < const Executor > exec)
 Creates the timer type most suitable for recording accurate timings of kernels on the given executor.

# 46.230.1 Detailed Description

Represents a generic timer that can be used to record time points and measure time differences on host or device streams.

To keep the runtime overhead of timing minimal, time points need to be allocated beforehand using Timer::create\_time\_point:

```
auto begin = timer->create_time_point();
auto end = timer->create_time_point();
// ...
timer->record(begin);
run_expensive_operation();
timer->record(end);
auto elapsed = timer->difference(begin, end);
```

#### 46.230.2 Member Function Documentation

## 46.230.2.1 create\_for\_executor()

Creates the timer type most suitable for recording accurate timings of kernels on the given executor.

#### **Parameters**

```
exec the executor to create a Timer for
```

#### Returns

CpuTimer for ReferenceExecutor and OmpExecutor, CudaTimer for CudaExecutor, HipTimer for HipExecutor or DpcppExecutor.

#### 46.230.2.2 create\_time\_point()

```
time_point gko::Timer::create_time_point ( )
```

Returns a newly created time point.

Time points may only be used with the timer they were created with.

#### 46.230.2.3 difference()

Computes the difference between the two time points in nanoseconds.

The function synchronizes with stop before computing the difference.

#### **Parameters**

start	the first time point (earlier)
end	the second time point (later)

#### Returns

the difference between the time points in nanoseconds.

#### 46.230.2.4 difference\_async()

Computes the difference between the two time points in nanoseconds.

This asynchronous version does not synchronize itself, so the time points need to have been synchronized with, i.e. timer->wait(stop) needs to have been called. The version is intended for more advanced users who want to measure the overhead of timing functionality separately.

#### **Parameters**

start	the first time point (earlier)
end	the second time point (later)

#### Returns

the difference between the time points in nanoseconds.

Implemented in gko::DpcppTimer, gko::HipTimer, gko::CudaTimer, and gko::CpuTimer.

The documentation for this class was generated from the following file:

• ginkgo/core/base/timer.hpp

# 46.231 gko::Transposable Class Reference

Linear operators which support transposition should implement the Transposable interface.

```
#include <ginkgo/core/base/lin_op.hpp>
```

# **Public Member Functions**

virtual std::unique\_ptr< LinOp > transpose () const =0

Returns a LinOp representing the transpose of the Transposable object.

virtual std::unique\_ptr< LinOp > conj\_transpose () const =0

Returns a LinOp representing the conjugate transpose of the Transposable object.

# 46.231.1 Detailed Description

Linear operators which support transposition should implement the Transposable interface.

It provides two functionalities, the normal transpose and the conjugate transpose.

The normal transpose returns the transpose of the linear operator without changing any of its elements representing the operation,  $B = A^T$ .

The conjugate transpose returns the conjugate of each of the elements and additionally transposes the linear operator representing the operation,  $B = A^H$ .

#### 46.231.1.1 Example: Transposing a Csr matrix:

```
{c++}
//Transposing an object of LinOp type.
//The object you want to transpose.
auto op = matrix::Crs::create(exec);
//Transpose the object by first converting it to a transposable type.
auto trans = op->transpose();
```

#### 46.231.2 Member Function Documentation

#### 46.231.2.1 conj\_transpose()

```
virtual std::unique_ptr<LinOp> gko::Transposable::conj_transpose ( ) const [pure virtual]
```

Returns a LinOp representing the conjugate transpose of the Transposable object.

# Returns

a pointer to the new conjugate transposed object

Implemented in gko::matrix::Csr< ValueType, IndexType >, gko::matrix::Dense< ValueType >, gko::matrix::Dense< value\_type >, gko::preconditioner::Ilu< LSolverType, USolverType, ReverseApply, IndexType >, gko::preconditioner::Jacobi< ValueType, IndexType gko::matrix::Fft3, gko::preconditioner::Ic< LSolverType, IndexType >, gko::solver::UpperTrs< ValueType, IndexType >, gko::preconditioner::Isai< IsaiType, ValueType, IndexType >, gko::matrix::Fbcsr< ValueType, IndexType >, gko::matrix::Fft2, gko::solver::Ir< ValueType >, gko::matrix::SparsityCsr< ValueType, IndexType >, gko::solver::Gmres< ValueType gko::solver::LowerTrs< ValueType, IndexType >, gko::matrix::Diagonal< ValueType >, gko::solver::Idr< ValueType >, gko::solver::Fcg< ValueType ygko::matrix::Fft, gko::Composition< ValueType >, gko::solver::Gcr< ValueType >, gko::solver::Cg< Va

#### 46.231.2.2 transpose()

```
virtual std::unique_ptr<LinOp> gko::Transposable::transpose ( ) const [pure virtual]
```

Returns a LinOp representing the transpose of the Transposable object.

#### Returns

a pointer to the new transposed object

Implemented in gko::matrix::Csr< ValueType, IndexType >, gko::matrix::Dense< ValueType >, gko::matrix::Dense< value\_type >, gko::preconditioner::Jacobi< ValueType, IndexType gko::preconditioner::Jacobi< ValueType, IndexType yko::preconditioner::Jacobi< ValueType, IndexType yko::preconditioner::Jacobi< ValueType, IndexType >, gko::preconditioner::Jacobi< ValueType, IndexType >, gko::matrix::Fbcsr< ValueType, IndexType >, gko::matrix::Fbcsr< ValueType, IndexType >, gko::solver::Gmres< ValueType gko::matrix::Fft2, gko::solver::Jacobi< ValueType >, gko::solver::Jacobi< ValueType >, gko::solver::Jacobi< ValueType >, gko::solver::Gg< ValueType >, gko::solver::Jacobi< ValueType >, gko::s

The documentation for this class was generated from the following file:

• ginkgo/core/base/lin\_op.hpp

# 46.232 gko::config::type descriptor Class Reference

This class describes the value and index types to be used when building a Ginkgo type from a configuration file.

```
#include <ginkgo/core/config/type_descriptor.hpp>
```

#### **Public Member Functions**

type\_descriptor (std::string value\_typestr="float64", std::string index\_typestr="int32", std::string global\_
index\_typestr="int64")

type\_descriptor constructor.

const std::string & get\_value\_typestr () const

Get the value type string.

const std::string & get\_index\_typestr () const

Get the index type string.

• const std::string & get\_local\_index\_typestr () const

Get the local index type string, which gives the same result as <a href="mailto:get\_index\_typestr">get\_index\_typestr</a>()

const std::string & get\_global\_index\_typestr () const

Get the global index type string.

# 46.232.1 Detailed Description

This class describes the value and index types to be used when building a Ginkgo type from a configuration file.

A type\_descriptor is passed in order to define the parse function defines which template parameters, in terms of value\_type and/or index\_type, the created object will have. For example, a CG solver created like this:

auto cg = parse(config, context, type\_descriptor("float64", "int32"));

will have the value type float64 and the index type int32. Any Ginkgo object that does not require one of these types will just ignore it. In value\_type, one additional value void can be used to specify that no default type is provided. In this case, the configuration has to provide the necessary template types.

```
If the configuration specifies one field (only allow value_type now): value_type: "some_value_type"
```

this type will take precedence over the type descriptor.

# 46.232.2 Constructor & Destructor Documentation

# 46.232.2.1 type\_descriptor()

type descriptor constructor.

There is free function make\_type\_descriptor to create the object by template.

#### **Parameters**

value_typestr	the value type string. "void" means no default.
index_typestr	the (local) index type string.
global_index_typestr	the global index type string.

## Note

there is no way to call the constructor with explicit template, so we create another free function to handle it.

The documentation for this class was generated from the following file:

ginkgo/core/config/type descriptor.hpp

# 46.233 gko::experimental::mpi::type\_impl< T > Struct Template Reference

A struct that is used to determine the MPI\_Datatype of a specified type.

```
#include <ginkgo/core/base/mpi.hpp>
```

# 46.233.1 Detailed Description

template < typename T > struct gko::experimental::mpi::type\_impl < T >

A struct that is used to determine the MPI\_Datatype of a specified type.

**Template Parameters** 

T | type of which the MPI\_Datatype should be inferred.

Note

any specialization of this type hast to provide a static function <code>get\_type()</code> that returns an MPI\_Datatype

The documentation for this struct was generated from the following file:

• ginkgo/core/base/mpi.hpp

# 46.234 gko::syn::type\_list< Types > Struct Template Reference

type\_list records several types in template

#include <ginkgo/core/synthesizer/containers.hpp>

# 46.234.1 Detailed Description

template<typename... Types> struct gko::syn::type\_list< Types >

type\_list records several types in template

**Template Parameters** 

Types the types in the list

The documentation for this struct was generated from the following file:

• ginkgo/core/synthesizer/containers.hpp

# 46.235 gko::UnsupportedMatrixProperty Class Reference

Exception throws if a matrix does not have a property required by a numerical method.

#include <ginkgo/core/base/exception.hpp>

# **Public Member Functions**

UnsupportedMatrixProperty (const std::string &file, const int line, const std::string &msg)
 Initializes the UnsupportedMatrixProperty error.

# 46.235.1 Detailed Description

Exception throws if a matrix does not have a property required by a numerical method.

Currently, a message is specified at the call-site manually.

# 46.235.2 Constructor & Destructor Documentation

#### 46.235.2.1 UnsupportedMatrixProperty()

Initializes the UnsupportedMatrixProperty error.

#### **Parameters**

file	The name of the offending source file
line	The source code line number where the error occurred
msg	A message describing the property required.

The documentation for this class was generated from the following file:

• ginkgo/core/base/exception.hpp

# 46.236 gko::stop::Criterion::Updater Class Reference

The Updater class serves for convenient argument passing to the Criterion's check function.

```
#include <ginkgo/core/stop/criterion.hpp>
```

# **Public Member Functions**

• Updater (const Updater &)=delete

Prevent copying and moving the object This is to enforce the use of argument passing and calling check at the same time.

bool check (uint8 stopping\_id, bool set\_finalized, array< stopping\_status > \*stop\_status, bool \*one\_← changed) const

Calls the parent Criterion object's check method.

# 46.236.1 Detailed Description

The Updater class serves for convenient argument passing to the Criterion's check function.

The pattern used is a Builder, except Updater builds a function's arguments before calling the function itself, and does not build an object. This allows calling a Criterion's check in the form of: stop\_criterion->update() .num\_iterations(num\_iterations) .ignore\_residual\_check(ignore\_residual\_check) .residual\_norm(residual\_norm) .implicit sq residual norm(implicit sq residual norm) .residual(residual) .solution(solution) .check(converged);

If there is a need for a new form of data to pass to the Criterion, it should be added here.

#### 46.236.2 Member Function Documentation

#### 46.236.2.1 check()

Calls the parent Criterion object's check method.

References gko::stop::Criterion::check().

The documentation for this class was generated from the following file:

· ginkgo/core/stop/criterion.hpp

# 46.237 gko::solver::UpperTrs< ValueType, IndexType > Class Template Reference

UpperTrs is the triangular solver which solves the system U x = b, when U is an upper triangular matrix.

```
#include <ginkgo/core/solver/triangular.hpp>
```

# **Public Member Functions**

• std::unique ptr< LinOp > transpose () const override

Returns a LinOp representing the transpose of the Transposable object.

std::unique\_ptr< LinOp > conj\_transpose () const override

Returns a LinOp representing the conjugate transpose of the Transposable object.

UpperTrs (const UpperTrs &)

Copy-assigns a triangular solver.

UpperTrs (UpperTrs &&)

Move-assigns a triangular solver.

UpperTrs & operator= (const UpperTrs &)

Copy-constructs a triangular solver.

UpperTrs & operator= (UpperTrs &&)

Move-constructs a triangular solver.

#### Static Public Member Functions

• static parameters\_type parse (const config::pnode &config, const config::registry &context, const config::type\_descriptor &td\_for\_child=config::make\_type\_descriptor < ValueType, IndexType >())

Create the parameters from the property\_tree.

## 46.237.1 Detailed Description

```
template<typename ValueType = default_precision, typename IndexType = int32> class gko::solver::UpperTrs< ValueType, IndexType >
```

UpperTrs is the triangular solver which solves the system U x = b, when U is an upper triangular matrix.

It works best when passing in a matrix in CSR format. If the matrix is not in CSR, then the generate step converts it into a CSR matrix. The generation fails if the matrix is not convertible to CSR.

Note

As the constructor uses the copy and convert functionality, it is not possible to create a empty solver or a solver with a matrix in any other format other than CSR, if none of the executor modules are being compiled with.

#### **Template Parameters**

ValueType	precision of matrix elements
IndexType	precision of matrix indices

#### 46.237.2 Constructor & Destructor Documentation

## 46.237.2.1 UpperTrs() [1/2]

Copy-assigns a triangular solver.

Preserves the executor, shallow-copies the system matrix. If the executors mismatch, clones system matrix onto this executor. Solver analysis information will be regenerated.

# 46.237.2.2 UpperTrs() [2/2]

Move-assigns a triangular solver.

Preserves the executor, moves the system matrix. If the executors mismatch, clones system matrix onto this executor and regenerates solver analysis information. Moved-from object is empty (0x0 and nullptr system matrix)

#### 46.237.3 Member Function Documentation

## 46.237.3.1 conj\_transpose()

```
template<typename ValueType = default_precision, typename IndexType = int32>
std::unique_ptr<LinOp> gko::solver::UpperTrs< ValueType, IndexType >::conj_transpose ( )
const [override], [virtual]
```

Returns a LinOp representing the conjugate transpose of the Transposable object.

Returns

a pointer to the new conjugate transposed object

Implements gko::Transposable.

#### 46.237.3.2 operator=() [1/2]

Copy-constructs a triangular solver.

Preserves the executor, shallow-copies the system matrix. Solver analysis information will be regenerated.

#### 46.237.3.3 operator=() [2/2]

Move-constructs a triangular solver.

Preserves the executor, moves the system matrix and solver analysis information. Moved-from object is empty (0x0 and nullptr system matrix)

#### 46.237.3.4 parse()

Create the parameters from the property\_tree.

Because this is directly tied to the specific type, the value/index type settings within config are ignored and type\_ descriptor is only used for children configs.

#### **Parameters**

config	the property tree for setting	
context	the registry	
td_for_child	the type descriptor for children configs. The default uses the value/index type of this class.	

#### Returns

parameters

#### 46.237.3.5 transpose()

```
template<typename ValueType = default_precision, typename IndexType = int32>
std::unique_ptr<LinOp> gko::solver::UpperTrs< ValueType, IndexType >::transpose ( ) const
[override], [virtual]
```

Returns a LinOp representing the transpose of the Transposable object.

#### Returns

a pointer to the new transposed object

Implements gko::Transposable.

The documentation for this class was generated from the following file:

• ginkgo/core/solver/triangular.hpp

# 46.238 gko::UseComposition < ValueType > Class Template Reference

The UseComposition class can be used to store the composition information in LinOp.

```
#include <ginkgo/core/base/composition.hpp>
```

# **Public Member Functions**

- std::shared\_ptr< Composition< ValueType >> get\_composition () const
   Returns the composition operators.
- std::shared\_ptr< const LinOp > get\_operator\_at (size\_type index) const Returns the operator at index-th position of composition.

# 46.238.1 Detailed Description

```
template<typename ValueType = default_precision> class gko::UseComposition< ValueType >
```

The UseComposition class can be used to store the composition information in LinOp.

#### **Template Parameters**

ValueType	precision of input and result vectors
-----------	---------------------------------------

#### 46,238.2 Member Function Documentation

# 46.238.2.1 get\_composition()

```
template<typename ValueType = default_precision>
std::shared_ptr<Composition<ValueType> > gko::UseComposition< ValueType >::get_composition (
) const [inline]
```

Returns the composition operators.

#### Returns

composition

# 46.238.2.2 get\_operator\_at()

Returns the operator at index-th position of composition.

## Returns

index-th operator

# Note

when this composition is not set, this function always returns nullptr. However, when this composition is set, it will throw exception when exceeding index.

#### **Exceptions**

```
std::out_of_range | if index is out of bound when composition is existed.
```

Referenced by gko::multigrid::EnableMultigridLevel < ValueType >::get\_coarse\_op(), gko::multigrid::Enable  $\leftarrow$  MultigridLevel < ValueType >::get\_prolong\_op(), and gko::multigrid::EnableMultigridLevel < ValueType >::get\_ $\leftarrow$  restrict\_op().

The documentation for this class was generated from the following file:

• ginkgo/core/base/composition.hpp

# 46.239 gko::syn::value\_list< T, Values > Struct Template Reference

value list records several values with the same type in template.

#include <ginkgo/core/synthesizer/containers.hpp>

# 46.239.1 Detailed Description

```
template<typename T, T... Values>
struct gko::syn::value_list< T, Values>
```

value\_list records several values with the same type in template.

#### **Template Parameters**

Т	the value type of the list
Values	the values in the list

The documentation for this struct was generated from the following file:

· ginkgo/core/synthesizer/containers.hpp

# 46.240 gko::ValueMismatch Class Reference

ValueMismatch is thrown if two values are not equal.

#include <ginkgo/core/base/exception.hpp>

## **Public Member Functions**

• ValueMismatch (const std::string &file, int line, const std::string &func, size\_type val1, size\_type val2, const std::string &clarification)

Initializes a value mismatch error.

# 46.240.1 Detailed Description

ValueMismatch is thrown if two values are not equal.

# 46.240.2 Constructor & Destructor Documentation

#### 46.240.2.1 ValueMismatch()

Initializes a value mismatch error.

#### **Parameters**

file	The name of the offending source file
line	The source code line number where the error occurred
func	The function name where the error occurred
val1	The first value to be compared.
val2	The second value to be compared.
clarification	An additional message further describing the error

The documentation for this class was generated from the following file:

· ginkgo/core/base/exception.hpp

# 46.241 gko::experimental::distributed::Vector< ValueType > Class Template Reference

Vector is a format which explicitly stores (multiple) distributed column vectors in a dense storage format.

```
#include <ginkgo/core/distributed/vector.hpp>
```

## **Public Member Functions**

void read\_distributed (const device\_matrix\_data< ValueType, int64 > &data, ptr\_param< const Partition< int64, int64 >> partition)

Reads a vector from the device\_matrix\_data structure and a global row partition.

void read\_distributed (const matrix\_data< ValueType, int64 > &data, ptr\_param< const Partition< int64, int64 >> partition)

Reads a vector from the matrix\_data structure and a global row partition.

- std::unique\_ptr< absolute\_type > compute\_absolute () const override
   Gets the AbsoluteLinOp.
- void compute\_absolute\_inplace () override

Compute absolute inplace on each element.

std::unique\_ptr< complex\_type > make\_complex () const

Creates a complex copy of the original vectors.

void make\_complex (ptr\_param < complex\_type > result) const

Writes a complex copy of the original vectors to given complex vectors.

std::unique\_ptr< real\_type > get\_real () const

Creates new real vectors and extracts the real part of the original vectors into that.

void get real (ptr param < real type > result) const

Extracts the real part of the original vectors into given real vectors.

std::unique\_ptr< real\_type > get\_imag () const

Creates new real vectors and extracts the imaginary part of the original vectors into that.

void get\_imag (ptr\_param < real\_type > result) const

Extracts the imaginary part of the original vectors into given real vectors.

void fill (ValueType value)

Fill the distributed vectors with a given value.

void scale (ptr\_param< const LinOp > alpha)

Scales the vectors with a scalar (aka: BLAS scal).

void inv\_scale (ptr\_param< const LinOp > alpha)

Scales the vectors with the inverse of a scalar.

void add\_scaled (ptr\_param< const LinOp > alpha, ptr\_param< const LinOp > b)

Adds b scaled by alpha to the vectors (aka: BLAS axpy).

void sub\_scaled (ptr\_param< const LinOp > alpha, ptr\_param< const LinOp > b)

Subtracts b scaled by alpha from the vectors (aka: BLAS axpy).

void compute\_dot (ptr\_param< const LinOp > b, ptr\_param< LinOp > result) const

Computes the column-wise dot product of this (multi-)vector and b using a global reduction.

• void compute\_dot (ptr\_param< const LinOp > b, ptr\_param< LinOp > result, array< char > &tmp) const Computes the column-wise dot product of this (multi-)vector and b using a global reduction.

void compute\_conj\_dot (ptr\_param< const LinOp > b, ptr\_param< LinOp > result) const

Computes the column-wise dot product of this (multi-)vector and conj(b) using a global reduction.

void compute\_conj\_dot (ptr\_param< const LinOp > b, ptr\_param< LinOp > result, array< char > &tmp)
 const

Computes the column-wise dot product of this (multi-)vector and conj (b) using a global reduction.

void compute\_squared\_norm2 (ptr\_param< LinOp > result) const

Computes the square of the column-wise Euclidean ( $L^2$ ) norm of this (multi-)vector using a global reduction.

void compute squared norm2 (ptr param < LinOp > result, array < char > &tmp) const

Computes the square of the column-wise Euclidean (  $L^2$  ) norm of this (multi-)vector using a global reduction.

void compute\_norm2 (ptr\_param< LinOp > result) const

Computes the Euclidean ( $L^{\wedge}$ 2) norm of this (multi-)vector using a global reduction.

void compute\_norm2 (ptr\_param < LinOp > result, array < char > &tmp) const

Computes the Euclidean ( $L^{\wedge}$ 2) norm of this (multi-)vector using a global reduction.

void compute norm1 (ptr param< LinOp > result) const

Computes the column-wise ( $L^{\wedge}$ 1) norm of this (multi-)vector.

void compute\_norm1 (ptr\_param < LinOp > result, array < char > &tmp) const

Computes the column-wise ( $L^{\wedge}$ 1) norm of this (multi-)vector using a global reduction.

void compute mean (ptr param< LinOp > result) const

Computes the column-wise mean of this (multi-)vector using a global reduction.

void compute\_mean (ptr\_param< LinOp > result, array< char > &tmp) const

Computes the column-wise arithmetic mean of this (multi-)vector using a global reduction.

• value type & at local (size type row, size type col) noexcept

Returns a single element of the multi-vector.

value\_type at\_local (size\_type row, size\_type col) const noexcept

ValueType & at\_local (size\_type idx) noexcept

Returns a single element of the multi-vector.

- ValueType at\_local (size\_type idx) const noexcept
- value type \* get local values ()

Returns a pointer to the array of local values of the multi-vector.

const value\_type \* get\_const\_local\_values () const

Returns a pointer to the array of local values of the multi-vector.

const local\_vector\_type \* get\_local\_vector () const

Direct (read) access to the underlying local local vector type vectors.

std::unique\_ptr< const real\_type > create\_real\_view () const

Create a real view of the (potentially) complex original multi-vector.

std::unique\_ptr< real\_type > create\_real\_view ()

Create a real view of the (potentially) complex original multi-vector.

#### **Static Public Member Functions**

static std::unique\_ptr< Vector > create\_with\_config\_of (ptr\_param< const Vector > other)

Creates a distributed Vector with the same size and stride as another Vector.

static std::unique\_ptr< Vector > create\_with\_type\_of (ptr\_param< const Vector > other, std::shared\_ptr< const Executor > exec)

Creates an empty Vector with the same type as another Vector, but on a different executor.

static std::unique\_ptr< Vector > create\_with\_type\_of (ptr\_param< const Vector > other, std::shared\_ptr< const Executor > exec, const dim< 2 > &global\_size, const dim< 2 > &local\_size, size\_type stride)

Creates an Vector with the same type as another Vector, but on a different executor and with a different size.

 static std::unique\_ptr< Vector > create (std::shared\_ptr< const Executor > exec, mpi::communicator comm, dim< 2 > global\_size, dim< 2 > local\_size, size\_type stride)

Creates an empty distributed vector with a specified size.

static std::unique\_ptr< Vector > create (std::shared\_ptr< const Executor > exec, mpi::communicator comm, dim< 2 > global\_size={}, dim< 2 > local\_size={})

Creates an empty distributed vector with a specified size.

 static std::unique\_ptr< Vector > create (std::shared\_ptr< const Executor > exec, mpi::communicator comm, dim< 2 > global\_size, std::unique\_ptr< local\_vector\_type > local\_vector)

Creates a distributed vector from local vectors with a specified size.

• static std::unique\_ptr< Vector > create (std::shared\_ptr< const Executor > exec, mpi::communicator comm, std::unique\_ptr< local\_vector\_type > local\_vector)

Creates a distributed vector from local vectors.

 static std::unique\_ptr< const Vector > create\_const (std::shared\_ptr< const Executor > exec, mpi::communicator comm, dim< 2 > global\_size, std::unique\_ptr< const local\_vector\_type > local\_computer

Creates a constant (immutable) distributed Vector from a constant local vector.

 static std::unique\_ptr< const Vector > create\_const (std::shared\_ptr< const Executor > exec, mpi::communicator comm, std::unique\_ptr< const local\_vector\_type > local\_vector)

Creates a constant (immutable) distributed Vector from a constant local vector.

# 46.241.1 Detailed Description

```
template<typename ValueType = double>
class gko::experimental::distributed::Vector< ValueType >
```

Vector is a format which explicitly stores (multiple) distributed column vectors in a dense storage format.

The (multi-)vector is distributed by row, which is described by a

#### See also

Partition. The local vectors are stored using the

Dense format. The vector should be filled using the read\_distributed method, e.g. auto part = Partition<...>::build\_from\_mapping(...); auto vector = Vector<...>::create(exec, comm); vector->read\_distributed(matrix\_data, part);

Using this approach the size of the global vectors, as well as the size of the local vectors, will be automatically inferred. It is possible to create a vector with specified global and local sizes and fill the local vectors using the accessor get local vector.

#### Note

Operations between two vectors (axpy, dot product, etc.) are only valid if both vectors where created using the same partition.

#### **Template Parameters**

e The precision of vector elements.	ValueType
-------------------------------------	-----------

# 46.241.2 Member Function Documentation

# 46.241.2.1 add\_scaled()

Adds b scaled by alpha to the vectors (aka: BLAS axpy).

#### **Parameters**

alpha	If alpha is 1x1 Dense matrix, the all vectors of b are scaled by alpha. If it is a Dense row vector of values, then i-th column vector of b is scaled with the i-th element of alpha (the number of columns of alpha has to match the number of vectors).
b	a (multi-)vector of the same dimension as this

#### 46.241.2.2 at\_local() [1/4]

## 46.241.2.3 at\_local() [2/4]

Returns a single element of the multi-vector.

Useful for iterating across all elements of the multi-vector. However, it is less efficient than the two-parameter variant of this method.

#### **Parameters**

```
idx a linear index of the requested element (ignoring the stride)
```

#### Note

the method has to be called on the same Executor the matrix is stored at (e.g. trying to call this method on a GPU matrix from the OMP results in a runtime error)

#### 46.241.2.4 at\_local() [3/4]

# 46.241.2.5 at\_local() [4/4]

Returns a single element of the multi-vector.

# **Parameters**

row	the local row of the requested element
col	the local column of the requested element

#### Note

the method has to be called on the same Executor the multi-vector is stored at (e.g. trying to call this method on a GPU multi-vector from the OMP results in a runtime error)

## 46.241.2.6 compute\_absolute()

```
template<typename ValueType = double>
std::unique_ptr<absolute_type> gko::experimental::distributed::Vector< ValueType >::compute←
   _absolute ( ) const [override], [virtual]
```

Gets the AbsoluteLinOp.

#### Returns

a pointer to the new absolute object

Implements gko::EnableAbsoluteComputation< remove\_complex< Vector< ValueType >> >.

#### 46.241.2.7 compute\_conj\_dot() [1/2]

Computes the column-wise dot product of this (multi-)vector and conj (b) using a global reduction.

# **Parameters**

b	a (multi-)vector of same dimension as this
result	a Dense row matrix, used to store the dot product (the number of column in result must match the
	number of columns of this)

# 46.241.2.8 compute\_conj\_dot() [2/2]

Computes the column-wise dot product of this (multi-)vector and conj (b) using a global reduction.

# Parameters

b	a (multi-)vector of same dimension as this
result	a Dense row matrix, used to store the dot product (the number of column in result must match the number of columns of this)
tmp	the temporary storage to use for partial sums during the reduction computation. It may be resized and/or reset to the correct executor.

# 46.241.2.9 compute\_dot() [1/2]

Computes the column-wise dot product of this (multi-)vector and b using a global reduction.

#### **Parameters**

b	a (multi-)vector of same dimension as this
result	a Dense row matrix, used to store the dot product (the number of column in result must match the
	number of columns of this)

# 46.241.2.10 compute\_dot() [2/2]

Computes the column-wise dot product of this (multi-)vector and b using a global reduction.

#### **Parameters**

b	a (multi-)vector of same dimension as this
result	a Dense row matrix, used to store the dot product (the number of column in result must match the number of columns of this)
tmp	the temporary storage to use for partial sums during the reduction computation. It may be resized and/or reset to the correct executor.

# 46.241.2.11 compute\_mean() [1/2]

Computes the column-wise mean of this (multi-)vector using a global reduction.

#### **Parameters**

result
--------

a Dense row matrix, used to store the mean (the number of columns in result must match the number of columns of this)

# 46.241.2.12 compute\_mean() [2/2]

Computes the column-wise arithmetic mean of this (multi-)vector using a global reduction.

#### **Parameters**

result	a Dense row matrix, used to store the mean (the number of columns in result must match the number of columns of this)
tmp	the temporary storage to use for partial sums during the reduction computation. It may be resized and/or reset to the correct executor.

# 46.241.2.13 compute\_norm1() [1/2]

Computes the column-wise ( $L^{\wedge}1$ ) norm of this (multi-)vector.

#### **Parameters**

result	a Dense row matrix, used to store the norm (the number of columns in result must match the number
	of columns of this)

# 46.241.2.14 compute\_norm1() [2/2]

Computes the column-wise  $(L^{\wedge}1)$  norm of this (multi-)vector using a global reduction.

#### **Parameters**

result	a Dense row matrix, used to store the norm (the number of columns in result must match the number of columns of this)
tmp	the temporary storage to use for partial sums during the reduction computation. It may be resized
	and/or reset to the correct executor.

# 46.241.2.15 compute\_norm2() [1/2]

Computes the Euclidean ( $L^2$ ) norm of this (multi-)vector using a global reduction.

#### **Parameters**

result	a Dense row matrix, used to store the norm (the number of columns in result must match the number
	of columns of this)

# 46.241.2.16 compute\_norm2() [2/2]

Computes the Euclidean ( $L^2$ ) norm of this (multi-)vector using a global reduction.

#### **Parameters**

result	a Dense row matrix, used to store the norm (the number of columns in result must match the number of columns of this)
tmp	the temporary storage to use for partial sums during the reduction computation. It may be resized
	and/or reset to the correct executor.

# 46.241.2.17 compute\_squared\_norm2() [1/2]

Computes the square of the column-wise Euclidean ( $L^2$ ) norm of this (multi-)vector using a global reduction.

#### **Parameters**

a Dense row vector, used to store the norm (the number of columns in the vector must match the number of columns of this)

# 46.241.2.18 compute\_squared\_norm2() [2/2]

Computes the square of the column-wise Euclidean ( $L^2$ ) norm of this (multi-)vector using a global reduction.

#### **Parameters**

result	a Dense row vector, used to store the norm (the number of columns in the vector must match the number of columns of this)
tmp	the temporary storage to use for partial sums during the reduction computation. It may be resized and/or reset to the correct executor.

# 46.241.2.19 create() [1/4]

Creates an empty distributed vector with a specified size.

#### **Parameters**

exec	Executor associated with vector
comm	Communicator associated with vector
global_size	Global size of the vector
local_size	Processor-local size of the vector
stride	Stride of the local vector.

#### Returns

A smart pointer to the newly created vector.

#### 46.241.2.20 create() [2/4]

Creates a distributed vector from local vectors with a specified size.

#### Note

The data form the local\_vector will be moved into the new distributed vector. You could either move in a std ::unique\_ptr directly, copy a local vector with gko::clone, or create a unique non-owining view of a given local vector with gko::make\_dense\_view.

#### **Parameters**

exec	Executor associated with this vector
comm	Communicator associated with this vector
global_size	The global size of the vector
local_vector	The underlying local vector, the data will be moved into this

#### Returns

A smart pointer to the newly created vector.

# 46.241.2.21 create() [3/4]

Creates an empty distributed vector with a specified size.

#### **Parameters**

exec	Executor associated with vector
comm	Communicator associated with vector
global_size	Global size of the vector
local_size	Processor-local size of the vector, uses local_size[1] as the stride

#### Returns

A smart pointer to the newly created vector.

# 46.241.2.22 create() [4/4]

Creates a distributed vector from local vectors.

The global size will be deduced from the local sizes, which will incur a collective communication.

#### Note

The data form the local\_vector will be moved into the new distributed vector. You could either move in a std :: unique\_ptr directly, copy a local vector with gko::clone, or create a unique non-owining view of a given local vector with gko::make\_dense\_view.

#### **Parameters**

exec	Executor associated with this vector
comm	Communicator associated with this vector
local_vector	The underlying local vector, the data will be moved into this.

#### Returns

A smart pointer to the newly created vector.

# 46.241.2.23 create\_const() [1/2]

Creates a constant (immutable) distributed Vector from a constant local vector.

#### **Parameters**

exec	Executor associated with this vector	
comm	Communicator associated with this vector	
global_size	The global size of the vector	
local_vector	The underlying local vector, of which a view is created	

#### Returns

A smart pointer to the newly created vector.

#### 46.241.2.24 create\_const() [2/2]

Creates a constant (immutable) distributed Vector from a constant local vector.

The global size will be deduced from the local sizes, which will incur a collective communication.

#### **Parameters**

exec	Executor associated with this vector
comm	Communicator associated with this vector
local_vector	The underlying local vector, of which a view is created

#### Returns

A smart pointer to the newly created vector.

#### 46.241.2.25 create real\_view() [1/2]

```
template<typename ValueType = double>
std::unique_ptr<real_type> gko::experimental::distributed::Vector< ValueType >::create_real
_view ( )
```

Create a real view of the (potentially) complex original multi-vector.

If the original vector is real, nothing changes. If the original vector is complex, the result is created by viewing the complex vector with as real with a reinterpret\_cast with twice the number of columns and double the stride.

## 46.241.2.26 create\_real\_view() [2/2]

```
template<typename ValueType = double>
std::unique_ptr<const real_type> gko::experimental::distributed::Vector< ValueType >::create
_real_view ( ) const
```

Create a real view of the (potentially) complex original multi-vector.

If the original vector is real, nothing changes. If the original vector is complex, the result is created by viewing the complex vector with as real with a reinterpret\_cast with twice the number of columns and double the stride.

#### 46.241.2.27 create\_with\_config\_of()

Creates a distributed Vector with the same size and stride as another Vector.

#### **Parameters**

# 46.241.2.28 create\_with\_type\_of() [1/2]

Creates an empty Vector with the same type as another Vector, but on a different executor.

#### **Parameters**

other	The other multi-vector whose type we target.
exec	The executor of the new multi-vector.

# Note

The new multi-vector uses the same communicator as other.

#### Returns

an empty Vector with the type of other.

# 46.241.2.29 create\_with\_type\_of() [2/2]

Creates an Vector with the same type as another Vector, but on a different executor and with a different size.

#### **Parameters**

other	The other multi-vector whose type we target.
exec	The executor of the new multi-vector.
global_size	The global size of the multi-vector.
local_size	The local size of the multi-vector.
stride	The stride of the new multi-vector.

# Returns

a Vector of specified size with the type of other.

# 46.241.2.30 fill()

Fill the distributed vectors with a given value.

#### **Parameters**

the value to be filled	value
------------------------	-------

# 46.241.2.31 get\_const\_local\_values()

```
template<typename ValueType = double>
const value_type* gko::experimental::distributed::Vector< ValueType >::get_const_local_values
( ) const
```

Returns a pointer to the array of local values of the multi-vector.

## Returns

the pointer to the array of local values

#### Note

This is the constant version of the function, which can be significantly more memory efficient than the non-constant version, so always prefer this version.

## 46.241.2.32 get\_local\_values()

```
template<typename ValueType = double>
value_type* gko::experimental::distributed::Vector< ValueType >::get_local_values ( )
```

Returns a pointer to the array of local values of the multi-vector.

#### Returns

the pointer to the array of local values

#### 46.241.2.33 get\_local\_vector()

```
template<typename ValueType = double>
const local_vector_type* gko::experimental::distributed::Vector< ValueType >::get_local_vector
( ) const
```

Direct (read) access to the underlying local local\_vector\_type vectors.

#### Returns

a constant pointer to the underlying local\_vector\_type vectors

#### 46.241.2.34 inv\_scale()

Scales the vectors with the inverse of a scalar.

#### **Parameters**

alpha

If alpha is 1x1 Dense matrix, the all vectors are scaled by 1 / alpha. If it is a Dense row vector of values, then i-th column vector is scaled with the inverse of the i-th element of alpha (the number of columns of alpha has to match the number of vectors).

#### 46.241.2.35 make\_complex() [1/2]

```
template<typename ValueType = double>
std::unique_ptr<complex_type> gko::experimental::distributed::Vector< ValueType >::make_←
complex ( ) const
```

Creates a complex copy of the original vectors.

If the original vectors were real, the imaginary part of the result will be zero.

## 46.241.2.36 make\_complex() [2/2]

Writes a complex copy of the original vectors to given complex vectors.

If the original vectors were real, the imaginary part of the result will be zero.

# 46.241.2.37 read\_distributed() [1/2]

Reads a vector from the device\_matrix\_data structure and a global row partition.

The number of rows of the matrix data is ignored, only its number of columns is relevant. Both the number of local and global rows are inferred from the row partition.

## Note

The matrix data can contain entries for rows other than those owned by the process. Entries for those rows are discarded.

## **Parameters**

data	The device_matrix_data structure	
partition	The global row partition	

## 46.241.2.38 read\_distributed() [2/2]

Reads a vector from the matrix\_data structure and a global row partition.

See @read\_distributed

## Note

For efficiency it is advised to use the device\_matrix\_data overload.

## 46.241.2.39 scale()

```
template<typename ValueType = double>
void gko::experimental::distributed::Vector< ValueType >::scale (
    ptr_param< const LinOp > alpha )
```

Scales the vectors with a scalar (aka: BLAS scal).

## **Parameters**

alpha	If alpha is 1x1 Dense matrx, the all vectors are scaled by alpha. If it is a Dense row vector of values,	
	then i-th column vector is scaled with the i-th element of alpha (the number of columns of alpha has	
	match the number of vectors).	

# 46.241.2.40 sub\_scaled()

Subtracts b scaled by alpha from the vectors (aka: BLAS axpy).

# Parameters

alpha	If alpha is 1x1 Dense matrix, the all vectors of b are scaled by alpha. If it is a Dense row vector of values, then i-th column vector of b is scaled with the i-th element of alpha (the number of c	
b	a (multi-)vector of the same dimension as this	

The documentation for this class was generated from the following files:

- · ginkgo/core/distributed/matrix.hpp
- ginkgo/core/distributed/vector.hpp

# 46.242 gko::version Struct Reference

This structure is used to represent versions of various Ginkgo modules.

```
#include <ginkgo/core/base/version.hpp>
```

# **Public Attributes**

· const uint64 major

The major version number.

· const uint64 minor

The minor version number.

const uint64 patch

The patch version number.

· const char \*const tag

Addition tag string that describes the version in more detail.

# 46.242.1 Detailed Description

This structure is used to represent versions of various Ginkgo modules.

Version structures can be compared using the usual relational operators.

## 46.242.2 Member Data Documentation

## 46.242.2.1 tag

```
const char* const gko::version::tag
```

Addition tag string that describes the version in more detail.

It does not participate in comparisons.

Referenced by gko::operator<<().

The documentation for this struct was generated from the following file:

• ginkgo/core/base/version.hpp

# 46.243 gko::version\_info Class Reference

Ginkgo uses version numbers to label new features and to communicate backward compatibility guarantees:

```
#include <ginkgo/core/base/version.hpp>
```

# **Static Public Member Functions**

static const version\_info & get ()
 Returns an instance of version\_info.

## **Public Attributes**

· version header\_version

Contains version information of the header files.

version core\_version

Contains version information of the core library.

version reference\_version

Contains version information of the reference module.

version omp\_version

Contains version information of the OMP module.

version cuda\_version

Contains version information of the CUDA module.

version hip\_version

Contains version information of the HIP module.

version dpcpp\_version

Contains version information of the DPC++ module.

# 46.243.1 Detailed Description

Ginkgo uses version numbers to label new features and to communicate backward compatibility guarantees:

1. Versions with different major version number have incompatible interfaces (parts of the earlier interface may not be present anymore, and new interfaces can appear).

- 2. Versions with the same major number X, but different minor numbers Y1 and Y2 numbers keep the same interface as version X.0.0, but additions to the interface in X.0.0 present in X.Y1.0 may not be present in X.Y2.0 and vice versa.
- 3. Versions with the same major an minor version numbers, but different patch numbers have exactly the same interface, but the functionality may be different (something that is not implemented or has a bug in an earlier version may have this implemented or fixed in a later version).

This structure provides versions of different parts of Ginkgo: the headers, the core and the kernel modules (reference, OpenMP, CUDA, HIP, DPCPP). To obtain an instance of version\_info filled with information about the current version of Ginkgo, call the version\_info::get() static method.

## 46.243.2 Member Function Documentation

# 46.243.2.1 get()

```
static const version_info& gko::version_info::get ( ) [inline], [static]
```

Returns an instance of version\_info.

## Returns

an instance of version info

# 46.243.3 Member Data Documentation

## 46.243.3.1 core version

```
version gko::version_info::core_version
```

Contains version information of the core library.

This is the version of the static/shared library called "ginkgo".

## 46.243.3.2 cuda\_version

```
version gko::version_info::cuda_version
```

Contains version information of the CUDA module.

This is the version of the static/shared library called "ginkgo cuda".

# 46.243.3.3 dpcpp\_version

```
version gko::version_info::dpcpp_version
```

Contains version information of the DPC++ module.

This is the version of the static/shared library called "ginkgo dpcpp".

# 46.243.3.4 hip\_version

```
version gko::version_info::hip_version
```

Contains version information of the HIP module.

This is the version of the static/shared library called "ginkgo\_hip".

## 46.243.3.5 omp version

```
version gko::version_info::omp_version
```

Contains version information of the OMP module.

This is the version of the static/shared library called "ginkgo\_omp".

## 46.243.3.6 reference\_version

```
version gko::version_info::reference_version
```

Contains version information of the reference module.

This is the version of the static/shared library called "ginkgo\_reference".

The documentation for this class was generated from the following file:

• ginkgo/core/base/version.hpp

# 46.244 gko::experimental::mpi::window< ValueType > Class Template Reference

This class wraps the MPI\_Window class with RAII functionality.

```
#include <ginkgo/core/base/mpi.hpp>
```

# **Public Types**

· enum create\_type

The create type for the window object.

enum lock\_type

The lock type for passive target synchronization of the windows.

## **Public Member Functions**

• window ()

The default constructor.

• window (window &&other)

The move constructor.

window & operator= (window &&other)

The move assignment operator.

window (std::shared\_ptr< const Executor > exec, ValueType \*base, int num\_elems, const communicator &comm, const int disp\_unit=sizeof(ValueType), MPI\_Info input\_info=MPI\_INFO\_NULL, create\_type c\_
 type=create\_type::create)

Create a window object with a given data pointer and type.

MPI\_Win get\_window () const

Get the underlying window object of MPI\_Win type.

• void fence (int assert=0) const

The active target synchronization using MPI\_Win\_fence for the window object.

• void lock (int rank, lock\_type lock\_t=lock\_type::shared, int assert=0) const

Create an epoch using MPI\_Win\_lock for the window object.

· void unlock (int rank) const

Close the epoch using MPI\_Win\_unlock for the window object.

void lock\_all (int assert=0) const

Create the epoch on all ranks using MPI\_Win\_lock\_all for the window object.

void unlock\_all () const

Close the epoch on all ranks using MPI\_Win\_unlock\_all for the window object.

· void flush (int rank) const

Flush the existing RDMA operations on the target rank for the calling process for the window object.

void flush\_local (int rank) const

Flush the existing RDMA operations on the calling rank from the target rank for the window object.

· void flush\_all () const

Flush all the existing RDMA operations for the calling process for the window object.

· void flush\_all\_local () const

Flush all the local existing RDMA operations on the calling rank for the window object.

· void sync () const

Synchronize the public and private buffers for the window object.

~window ()

The deleter which calls MPI\_Win\_free when the window leaves its scope.

 $\bullet \ \ \text{template}{<} \text{typename PutType}>$ 

void put (std::shared\_ptr< const Executor > exec, const PutType \*origin\_buffer, const int origin\_count, const int target\_rank, const unsigned int target\_disp, const int target\_count) const

Put data into the target window.

• template<typename PutType >

request r\_put (std::shared\_ptr< const Executor > exec, const PutType \*origin\_buffer, const int origin\_count, const int target\_rank, const unsigned int target\_disp, const int target\_count) const

Put data into the target window.

template<typename PutType >
 void accumulate (std::shared\_ptr< const Executor > exec, const PutType \*origin\_buffer, const int origin\_
 count, const int target rank, const unsigned int target disp, const int target count, MPI Op operation) const

Accumulate data into the target window.

template<typename PutType >
 request r\_accumulate (std::shared\_ptr< const Executor > exec, const PutType \*origin\_buffer, const int origin\_count, const int target\_rank, const unsigned int target\_disp, const int target\_count, MPI\_Op opera-

(Non-blocking) Accumulate data into the target window.

template<typename GetType >
 void get (std::shared\_ptr< const Executor > exec, GetType \*origin\_buffer, const int origin\_count, const int target rank, const unsigned int target disp, const int target count) const

Get data from the target window.

tion) const

template<typename GetType >
 request r\_get (std::shared\_ptr< const Executor > exec, GetType \*origin\_buffer, const int origin\_count, const
 int target\_rank, const unsigned int target\_disp, const int target\_count) const

Get data (with handle) from the target window.

template<typename GetType >
 void get\_accumulate (std::shared\_ptr< const Executor > exec, GetType \*origin\_buffer, const int origin\_
 count, GetType \*result\_buffer, const int result\_count, const int target\_rank, const unsigned int target\_disp, const int target\_count, MPI\_Op operation) const

Get Accumulate data from the target window.

template < typename GetType >
 request r\_get\_accumulate (std::shared\_ptr < const Executor > exec, GetType \*origin\_buffer, const int origin\_count, GetType \*result\_buffer, const int result\_count, const int target\_rank, const unsigned int target ← disp, const int target\_count, MPI\_Op operation) const

(Non-blocking) Get Accumulate data (with handle) from the target window.

template<typename GetType >
 void fetch\_and\_op (std::shared\_ptr< const Executor > exec, GetType \*origin\_buffer, GetType \*result\_buffer,
 const int target\_rank, const unsigned int target\_disp, MPI\_Op operation) const

Fetch and operate on data from the target window (An optimized version of Get\_accumulate).

# 46.244.1 Detailed Description

template<typename ValueType>
class gko::experimental::mpi::window< ValueType >

This class wraps the MPI Window class with RAII functionality.

Different create and lock type methods are setup with enums.

MPI\_Window is primarily used for one sided communication and this class provides functionalities to fence, lock, unlock and flush the communication buffers.

## 46.244.2 Constructor & Destructor Documentation

# 46.244.2.1 window() [1/3]

```
template<typename ValueType >
gko::experimental::mpi::window< ValueType >::window ( ) [inline]
```

The default constructor.

It creates a null window of MPI WIN NULL type.

# 46.244.2.2 window() [2/3]

The move constructor.

Move the other object and replace it with MPI WIN NULL

## **Parameters**

other	the window object to be moved.
Ottion	The Window object to be moved.

## 46.244.2.3 window() [3/3]

```
template<typename ValueType >
gko::experimental::mpi::window< ValueType >::window (
    std::shared_ptr< const Executor > exec,
    ValueType * base,
    int num_elems,
    const communicator & comm,
    const int disp_unit = sizeof(ValueType),
    MPI_Info input_info = MPI_INFO_NULL,
    create_type c_type = create_type::create ) [inline]
```

Create a window object with a given data pointer and type.

A collective operation.

## **Parameters**

exec	The executor, on which the base pointer is located.
base	the base pointer for the window object.
num_elems	the num_elems of type ValueType the window points to.
comm	the communicator whose ranks will have windows created.
disp_unit	the displacement from base for the window object.
input_info	the MPI_Info object used to set certain properties.
c_type	the type of creation method to use to create the window.

References gko::experimental::mpi::communicator::get().

# 46.244.3 Member Function Documentation

# 46.244.3.1 accumulate()

```
template<typename ValueType >
template<typename PutType >
void gko::experimental::mpi::window< ValueType >::accumulate (
    std::shared_ptr< const Executor > exec,
    const PutType * origin_buffer,
    const int origin_count,
    const int target_rank,
    const unsigned int target_disp,
    const int target_count,
    MPI_Op operation ) const [inline]
```

Accumulate data into the target window.

## **Parameters**

exec	The executor, on which the message buffer is located.
origin_buffer	the buffer to send
origin_count	the number of elements to put
target_rank	the rank to put the data to
target_disp	the displacement at the target window
target_count	the request handle for the send call
operation	the reduce operation. See @MPI_Op

References gko::experimental::mpi::window< ValueType >::get\_window().

# 46.244.3.2 fence()

The active target synchronization using MPI\_Win\_fence for the window object.

This is called on all associated ranks.

## **Parameters**

assert	the optimization level. 0 is always valid.

## 46.244.3.3 fetch and op()

```
template<typename ValueType >
template<typename GetType >
void gko::experimental::mpi::window< ValueType >::fetch_and_op (
    std::shared_ptr< const Executor > exec,
    GetType * origin_buffer,
    GetType * result_buffer,
    const int target_rank,
    const unsigned int target_disp,
    MPI_Op operation ) const [inline]
```

Fetch and operate on data from the target window (An optimized version of Get\_accumulate).

## **Parameters**

exec	The executor, on which the message buffer is located.	
origin_buffer	the buffer to send	
target_rank	the rank to get the data from	
target_disp	the displacement at the target window	
operation	the reduce operation. See @MPI_Op	

References gko::experimental::mpi::window< ValueType >::get\_window().

# 46.244.3.4 flush()

Flush the existing RDMA operations on the target rank for the calling process for the window object.

## **Parameters**

```
rank the target rank.
```

# 46.244.3.5 flush\_local()

Flush the existing RDMA operations on the calling rank from the target rank for the window object.

## **Parameters**

```
rank the target rank.
```

## 46.244.3.6 get()

```
template<typename ValueType >
template<typename GetType >
void gko::experimental::mpi::window< ValueType >::get (
    std::shared_ptr< const Executor > exec,
    GetType * origin_buffer,
    const int origin_count,
    const int target_rank,
    const unsigned int target_disp,
    const int target_count ) const [inline]
```

Get data from the target window.

## **Parameters**

exec	The executor, on which the message buffer is located.
origin_buffer	the buffer to send
origin_count	the number of elements to get
target_rank	the rank to get the data from
target_disp	the displacement at the target window
target_count	the request handle for the send call

References gko::experimental::mpi::window< ValueType >::get\_window().

# 46.244.3.7 get\_accumulate()

Get Accumulate data from the target window.

## **Parameters**

exec	The executor, on which the message buffers are located.
origin_buffer	the buffer to send
origin_count	the number of elements to get
result_buffer	the buffer to receive the target data
result_count	the number of elements to get
target_rank	the rank to get the data from
target_disp	the displacement at the target window
target_count	the request handle for the send call
operation	the reduce operation. See @MPI_Op

References gko::experimental::mpi::window< ValueType >::get\_window().

## 46.244.3.8 get window()

```
template<typename ValueType >
MPI_Win gko::experimental::mpi::window< ValueType >::get_window ( ) const [inline]
```

Get the underlying window object of MPI\_Win type.

## Returns

the underlying window object.

Referenced by gko::experimental::mpi::window< ValueType >::accumulate(), gko::experimental::mpi::window< ValueType >::fetch\_and\_op(), gko::experimental::mpi::window< ValueType >::get(), gko::experimental:-:mpi::window< ValueType >::get\_accumulate(), gko::experimental::mpi::window< ValueType >::put(), gko::experimental::mpi::window< ValueType >::r\_accumulate(), gko::experimental::mpi::window< ValueType >::r\_cet(), gko::experimental::mpi::window< ValueType >::r\_get\_accumulate(), and gko::experimental::mpi::window< ValueType >::r\_put().

## 46.244.3.9 lock()

```
template<typename ValueType >
void gko::experimental::mpi::window< ValueType >::lock (
    int rank,
    lock_type lock_t = lock_type::shared,
    int assert = 0 ) const [inline]
```

Create an epoch using MPI\_Win\_lock for the window object.

## **Parameters**

rank	the target rank.	
lock⊷	the type of the lock: shared or exclusive	
_t		
assert	the optimization level. 0 is always valid.	

## 46.244.3.10 lock all()

Create the epoch on all ranks using MPI\_Win\_lock\_all for the window object.

## **Parameters**

assert the optimization level. 0 is	always valid.
-------------------------------------	---------------

# 46.244.3.11 operator=()

The move assignment operator.

Move the other object and replace it with MPI WIN NULL

## **Parameters**

```
other the window object to be moved.
```

# 46.244.3.12 put()

Put data into the target window.

## **Parameters**

exec	The executor, on which the message buffer is located.
origin_buffer	the buffer to send

## **Parameters**

origin_count	the number of elements to put
target_rank	the rank to put the data to
target_disp	the displacement at the target window
target_count	the request handle for the send call

References gko::experimental::mpi::window< ValueType >::get\_window().

# 46.244.3.13 r\_accumulate()

```
template<typename ValueType >
template<typename PutType >
request gko::experimental::mpi::window< ValueType >::r_accumulate (
    std::shared_ptr< const Executor > exec,
    const PutType * origin_buffer,
    const int origin_count,
    const int target_rank,
    const unsigned int target_disp,
    const int target_count,
    MPI_Op operation ) const [inline]
```

(Non-blocking) Accumulate data into the target window.

## **Parameters**

exec	The executor, on which the message buffer is located.
origin_buffer	the buffer to send
origin_count	the number of elements to put
target_rank	the rank to put the data to
target_disp	the displacement at the target window
target_count	the request handle for the send call
operation	the reduce operation. See @MPI_Op

# Returns

the request handle for the send call

References gko::experimental::mpi::request::get(), and gko::experimental::mpi::window< ValueType >::get $\_\leftarrow$  window().

# 46.244.3.14 r\_get()

```
template<typename ValueType >
template<typename GetType >
```

Get data (with handle) from the target window.

## **Parameters**

exec	The executor, on which the message buffer is located.
origin_buffer	the buffer to send
origin_count	the number of elements to get
target_rank	the rank to get the data from
target_disp	the displacement at the target window
target_count	the request handle for the send call

## Returns

the request handle for the send call

References gko::experimental::mpi::request::get(), and gko::experimental::mpi::window< ValueType >::get\_ $\leftarrow$  window().

## 46.244.3.15 r\_get\_accumulate()

(Non-blocking) Get Accumulate data (with handle) from the target window.

## **Parameters**

exec	The executor, on which the message buffers are located.
origin_buffer	the buffer to send
origin_count	the number of elements to get
result_buffer	the buffer to receive the target data
result_count	the number of elements to get
target_rank	the rank to get the data from
target disp Generated by Doxyge	the displacement at the target window
target_count	the request handle for the send call
operation	the reduce operation. See @MPI_Op

## Returns

the request handle for the send call

References gko::experimental::mpi::request::get(), and gko::experimental::mpi::window< ValueType >::get\_ $\leftarrow$  window().

# 46.244.3.16 r\_put()

```
template<typename ValueType >
template<typename PutType >
request gko::experimental::mpi::window< ValueType >::r_put (
    std::shared_ptr< const Executor > exec,
    const PutType * origin_buffer,
    const int origin_count,
    const int target_rank,
    const unsigned int target_disp,
    const int target_count ) const [inline]
```

Put data into the target window.

## **Parameters**

exec	The executor, on which the message buffer is located.
origin_buffer	the buffer to send
origin_count	the number of elements to put
target_rank	the rank to put the data to
target_disp	the displacement at the target window
target_count	the request handle for the send call

## Returns

the request handle for the send call

References gko::experimental::mpi::request::get(), and gko::experimental::mpi::window< ValueType >::get\_ $\leftarrow$  window().

# 46.244.3.17 unlock()

Close the epoch using MPI\_Win\_unlock for the window object.

#### **Parameters**

rank the target rank.

The documentation for this class was generated from the following file:

· ginkgo/core/base/mpi.hpp

# 46.245 gko::solver::workspace\_traits< Solver > Struct Template Reference

Traits class providing information on the type and location of workspace vectors inside a solver.

```
#include <ginkgo/core/solver/solver_base.hpp>
```

# 46.245.1 Detailed Description

```
template < typename Solver > struct gko::solver::workspace_traits < Solver >
```

Traits class providing information on the type and location of workspace vectors inside a solver.

The documentation for this struct was generated from the following file:

ginkgo/core/solver/solver\_base.hpp

# 46.246 gko::WritableToMatrixData< ValueType, IndexType > Class Template Reference

A LinOp implementing this interface can write its data to a matrix\_data structure.

```
#include <ginkgo/core/base/lin_op.hpp>
```

# **Public Member Functions**

virtual void write (matrix\_data < ValueType, IndexType > &data) const =0
 Writes a matrix to a matrix\_data structure.

# 46.246.1 Detailed Description

```
template<typename ValueType, typename IndexType> class gko::WritableToMatrixData< ValueType, IndexType >
```

A LinOp implementing this interface can write its data to a matrix\_data structure.

# 46.246.2 Member Function Documentation

## 46.246.2.1 write()

Writes a matrix to a matrix\_data structure.

## **Parameters**

data the matrix\_data structure

Implemented in gko::matrix::Fft3, gko::matrix::Fft4, gko::matrix::Fft4, gko::matrix::Fft5, gko::matrix::Fft5

The documentation for this class was generated from the following file:

• ginkgo/core/base/lin\_op.hpp

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