Since the refracted ray should be in the same plane as the incident ray and the normal we should be able to express it as:

$$\hat{r}_r = \alpha \hat{n} + \beta \hat{r}_i$$

 $\alpha$  and  $\beta$  can be obtained from the noting that  $\hat{r}_i$  is a unit vector and Snell's law:

$$\hat{r}_i \cdot \hat{r}_i = 1$$
$$(\alpha \hat{n} + \beta \hat{r}_i) \cdot (\alpha \hat{n} + \beta \hat{r}_i) = 1$$
$$\alpha^2 + \beta^2 + 2\alpha\beta(\hat{n} \cdot \hat{r}_i) = 1$$

and from Snell

$$n_i \sin \theta_i = n_r \sin \theta_r \Rightarrow \theta_r = \arcsin \left(\frac{n_i}{n_r} \sin \theta_i\right)$$

where

$$\cos \theta_i = -\hat{n} \cdot \hat{r}_i$$
$$\theta_i = \arccos(-\hat{n} \cdot \hat{r}_i)$$

And the expression for the angle on the refracted side:

$$-\hat{n} \cdot \hat{r}_r = \cos \theta_r$$

$$(-\hat{n}) \cdot (\alpha \hat{n} + \beta \hat{r}_i) = \cos \theta_r$$

$$-\alpha - \beta (\hat{n} \cdot \hat{r}_i) = \cos \theta_r$$

$$\alpha = -\cos \theta_r - \beta (n \cdot r_i)$$

replacing this in the first equation

$$(-\cos\theta_r - \beta(\hat{n}\cdot\hat{r}_i))^2 + \beta^2 + 2(-\cos\theta_r - \beta(\hat{n}\cdot\hat{r}_i))\beta(\hat{n}\cdot\hat{r}_i) = 1$$
$$(1 - (\hat{n}\cdot\hat{r}_i)^2)\beta^2 = 1 - \cos^2\theta_r$$
$$\beta = +\sqrt{\frac{1 - \cos^2\theta_r}{1 - (\hat{n}\cdot\hat{r}_i)^2}}$$