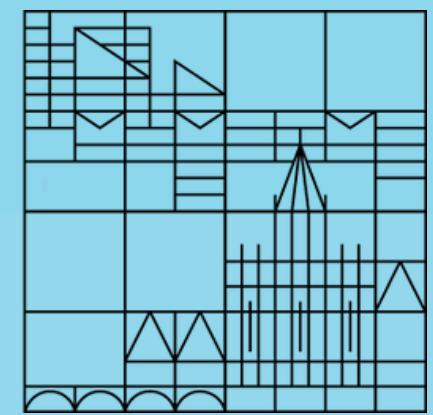


Introduction to Network Science

Network Science of
Socio-Economic Systems
Giordano De Marzo

Universität
Konstanz



About Me

- Postdoc at the Political Science department, University of Konstanz
- Junior Research Fellow at the Complexity Science Hub Vienna
- PhD in Physics at Sapienza University and Enrico Fermi Research Center (Rome)
- MSc and BSc in Theoretical Physics at Sapienza University



View from my room at Enrico Fermi Research Center

About Me

Research interests:

- Complex Digital Systems
- Social Networks
- Economic Complexity
- Artificial Neural Networks
- Large Language Models

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*View from my room at Enrico
Fermi Research Center*

Outline

1. About this Course

2. Complex Networks

3. Network Science

4. A Network Science Experiment



About this Course

Course Objectives

By the end of this course, students will understand key concepts in network science, be able to analyse and model real networks, and apply these techniques to socio-economic systems.

- Grasp fundamental **network theory** concepts
- Analyse and model **network growth** processes
- Detect **communities** within networks
- Utilize **network ensembles** theory
- Apply network science to the analysis of **social** and **economic** systems

Course Format

This course is structures as seminars and coding sessions
13 Theoretical seminars covering basics and advanced topics in
Network Science
8 Coding Sessions
1 Students presentation session

The coding sessions are optional but strongly recommended!

I will upload slides and code on my website before each lesson

giordano-demarzo.github.io/teaching/network-science/

Course Assessment

- Students select a published article or a dataset from those listed on the course website.
- The task is to replicate the analysis performed in the paper or apply network science to the analysis of the dataset.
- Results must be summarized in a report and discussed in a presentation.

The course grade is based on:

- the student **presentation** (35%)
- the **code** (15%)
- and on the **report** (50%)

Seminars Dates

October 28, 2024–Network Theory Basics

November 04, 2024–Random Graphs and Small World

November 11, 2024–Scale Free Networks

November 18, 2024–Measuring Nodes Centrality

November 25, 2024–Communities in Networks

December 2, 2024–Processes on Networks

December 9, 2024–Network Ensembles

December 16, 2024–Multilayer and Higher Order Networks

December 17, 2024–Economic and Financial Networks 1

January 13, 2025–Economic and Financial Networks 2

January 27, 2025–Social Networks

February 03, 2025–Advanced Topics in Network Science

February 04, 2025–Students Presentations

Coding Sessions Dates

October 29, 2024–Analysis of real world networks

November 12, 2024–Simulating network growth processes

November 19, 2024–Centrality measures

November 26, 2024–Community detection algorithms

December 3, 2024–Simulating processes on networks

December 10, 2024–Configuration models

January 14, 2025–Analysis of the world trading network

January 28, 2025–Analysis of social networks

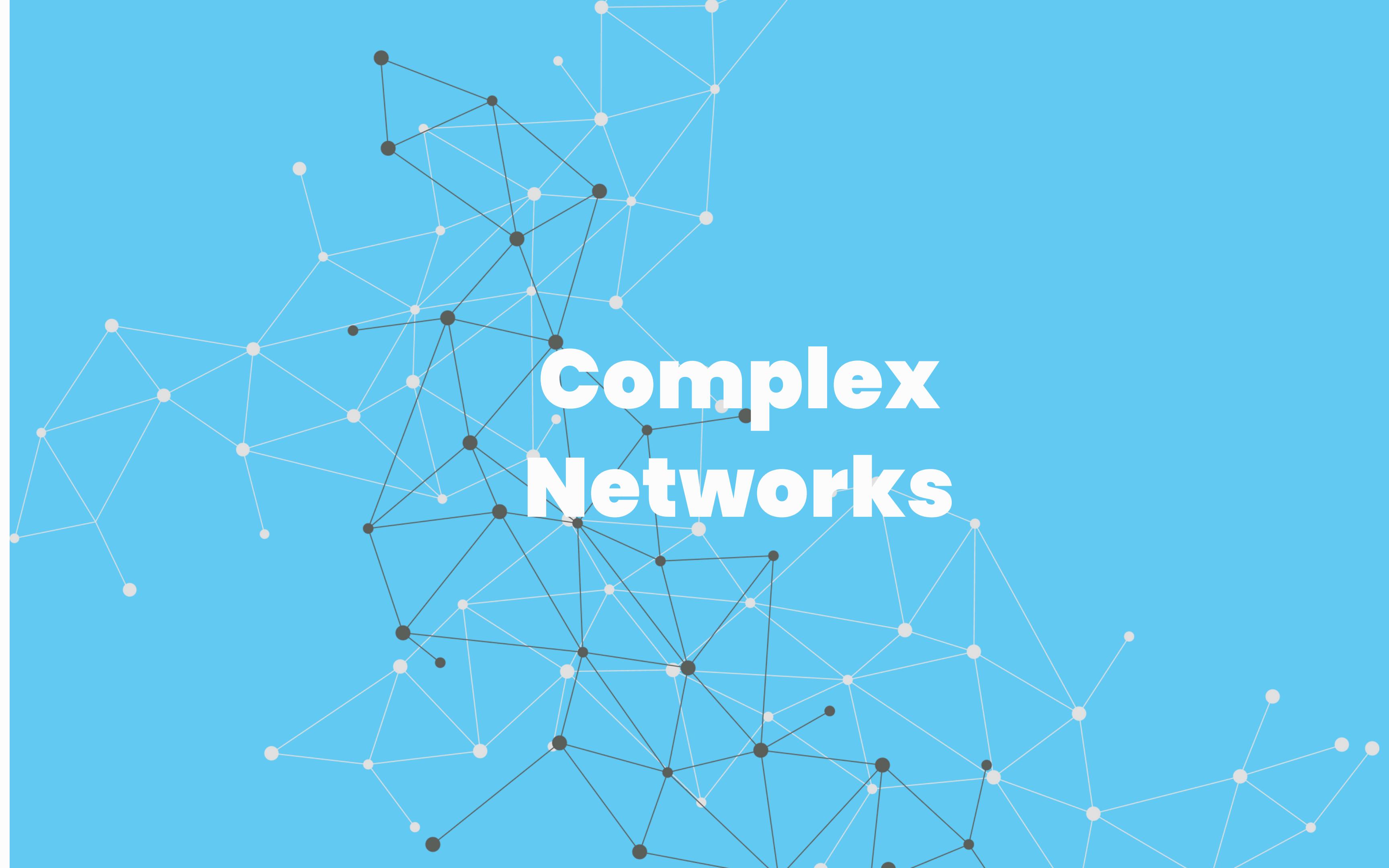
Final Report

I will upload datasets and papers on my website during the course

- the same dataset/paper can not be chosen by more than one person
- you will have to communicate your choice by 26/01
- first come first served, but there is plenty of choice for everybody

The report must be structured as a scientific paper and about **4/5 pages** long (including the bibliography). It must contain

- Abstract
- Introduction
- Results
- Discussion
- Methods
- References



A complex network graph is displayed against a light blue background. The graph consists of numerous small, semi-transparent grey dots representing nodes, connected by thin white lines representing edges. The nodes are densely packed in the center and become more sparse towards the periphery. A prominent feature is a large, roughly circular cluster of nodes in the middle-left area. Several other smaller clusters are scattered across the right side and bottom. The overall structure is organic and interconnected.

Complex Networks

What is a Network?

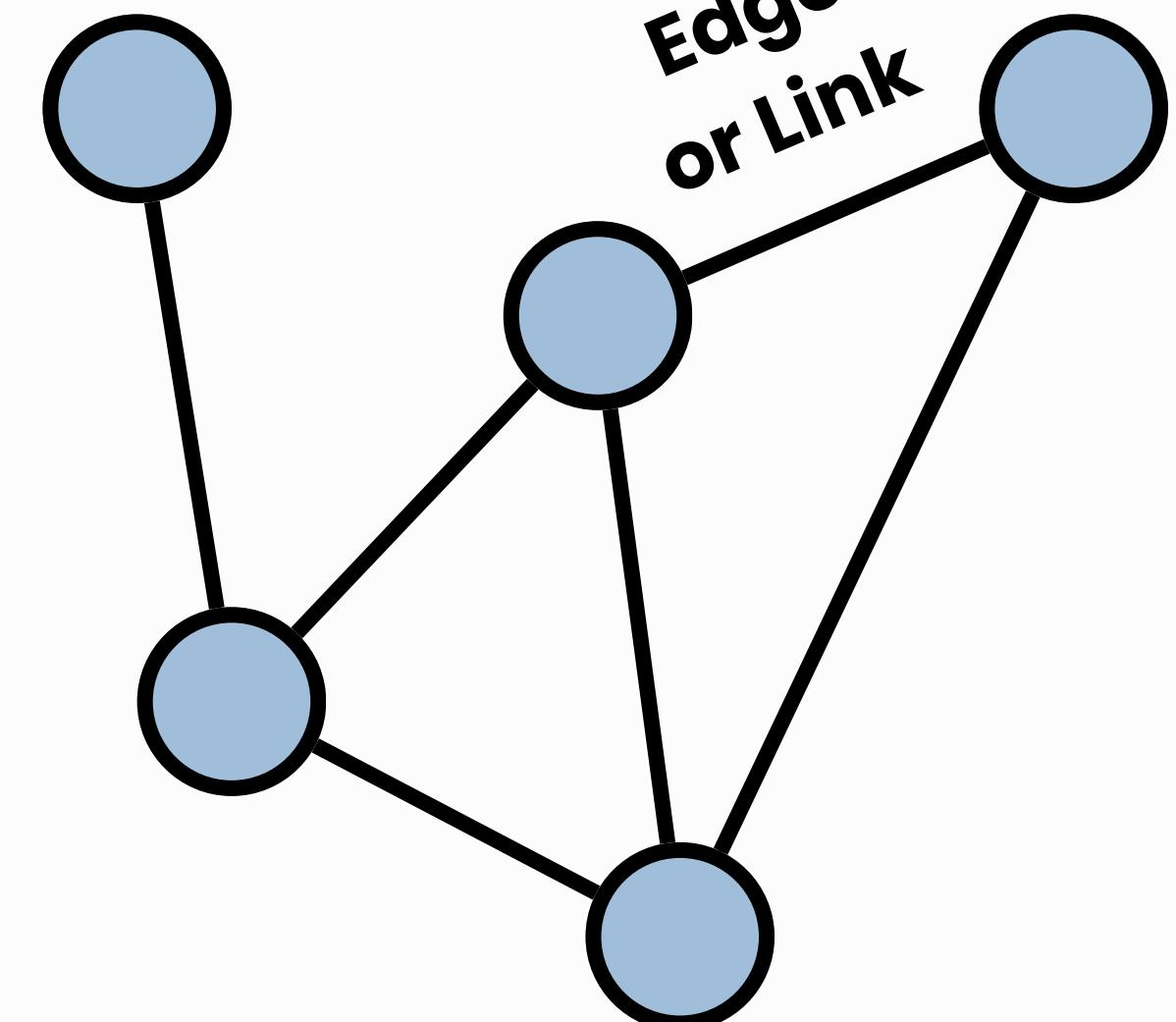
A Network or Graph $G(V, E)$ is a set of vertices or nodes V and edges or links E

- nodes represent entities in the system (eg. people on a social network)
- edges represent connections among the nodes (eg. friendship in a social network)

We denote by

- N the number of nodes
- E the number of links

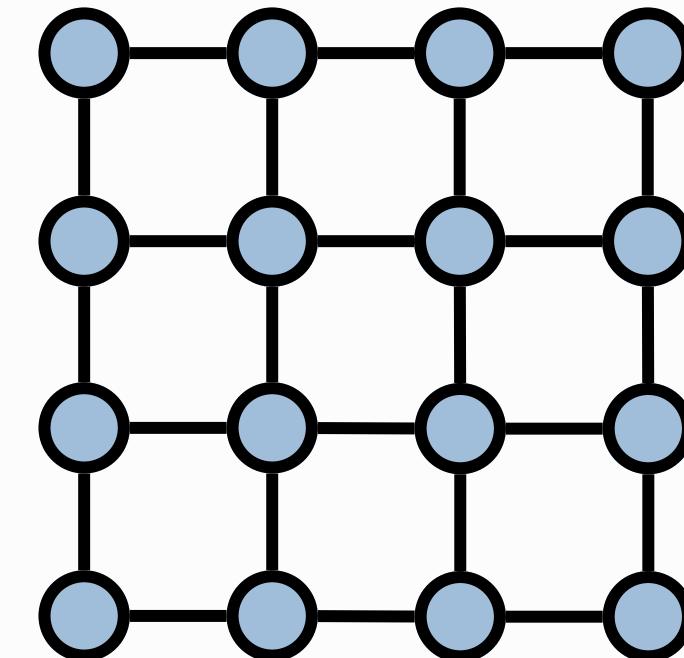
**Vertex
or Node**



What is a Complex Network?

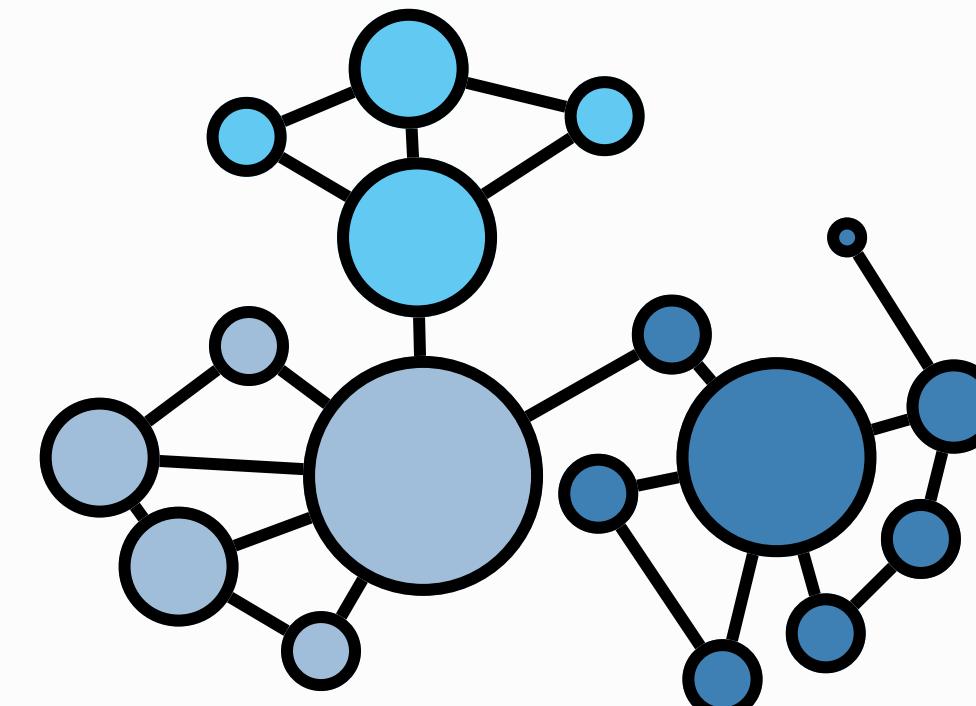
A grid or lattice is one of the simplest networks

- all nodes have the same degree
- no heterogeneity
- it repeats over and over without differences



Defining Complex Networks is not easy

- degrees tend to be very heterogeneous
- nodes tend to form communities and more sophisticated structures

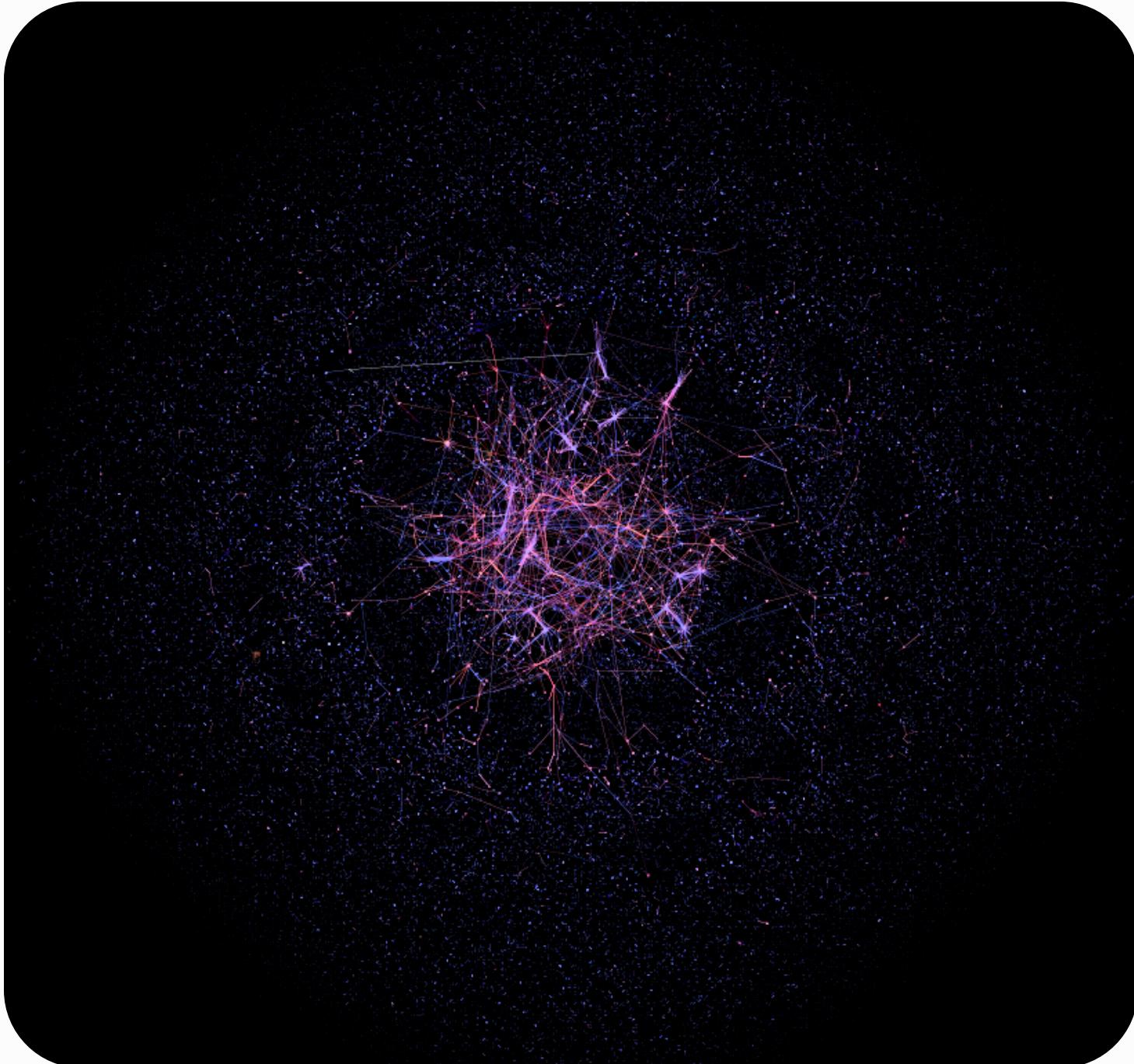


Social Networks

Human (online) societies can be described as a network

- nodes are individuals
- links represent some form of relation between the individuals
 - Facebook: friendship (undirected network)
 - Instagram: follow (directed network)

The image shows a network representation of 500M users on Twitter

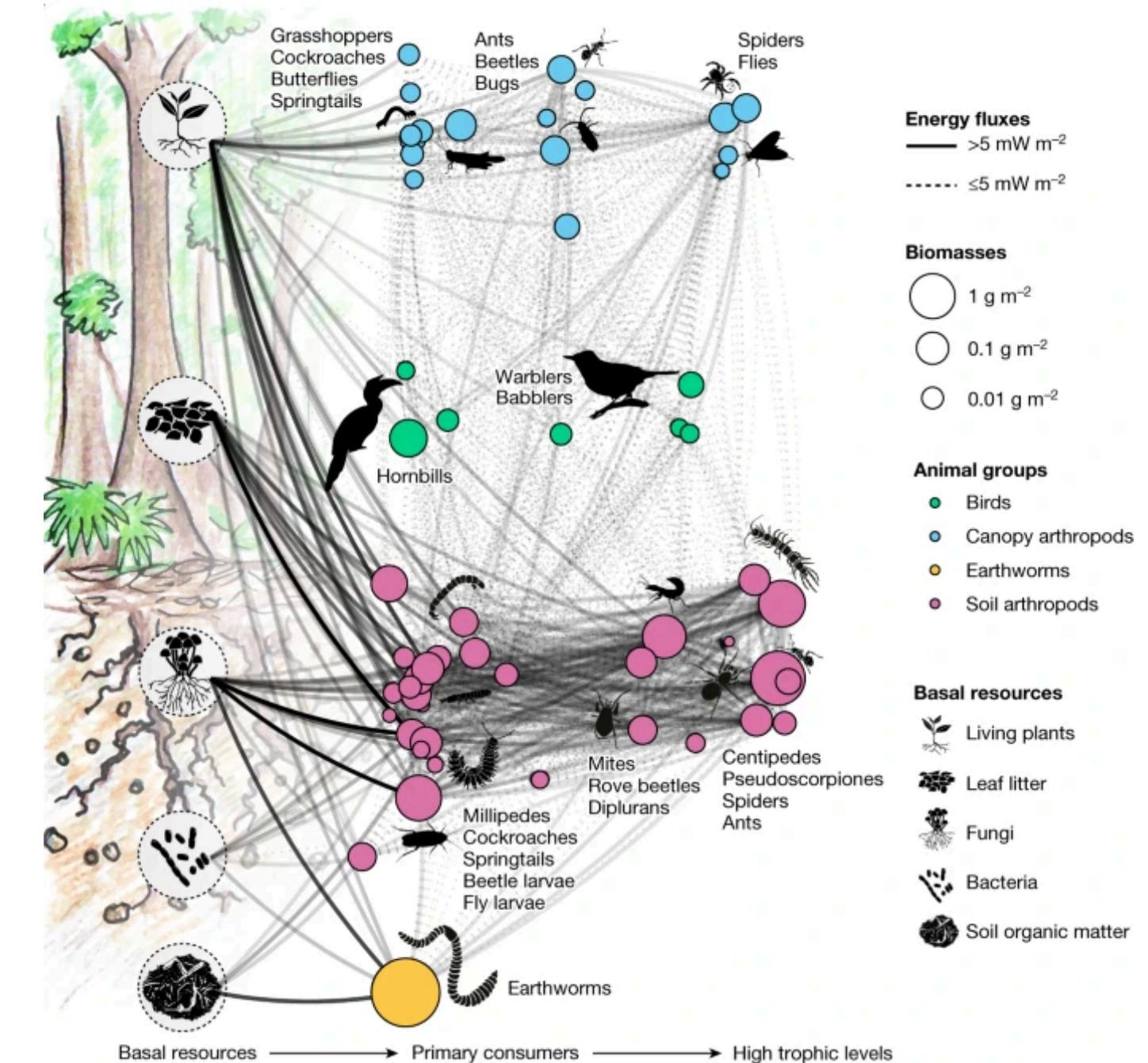


<https://dhs.stanford.edu/gephi-workshop/twitter-network-gallery/>

Food Webs

Networks can be used to describe prey-predator relations, obtaining the so called food-webs

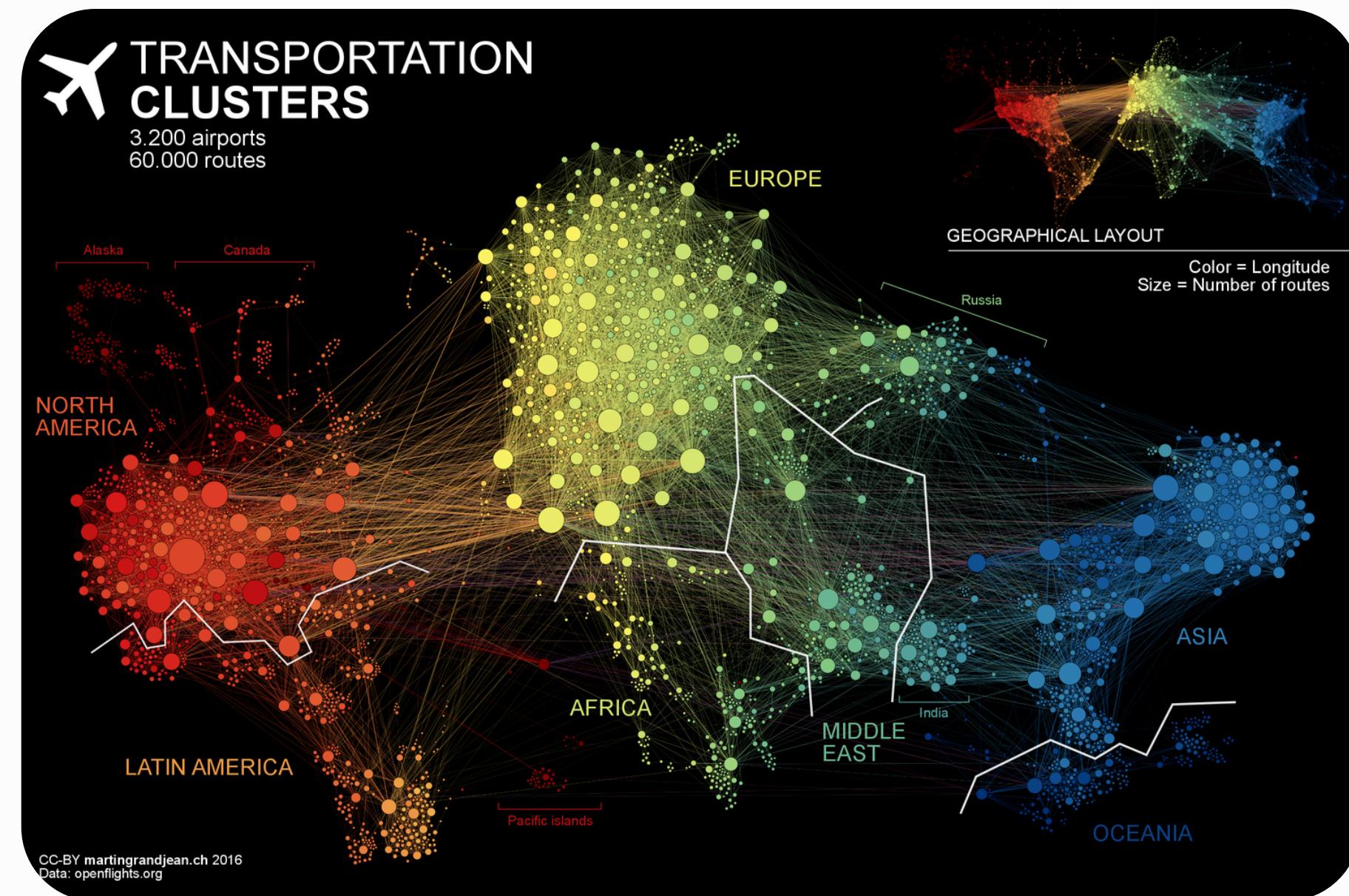
- nodes are animals or plants
- links represent who eats who relations
- the network is directed and can be weighted by the carbon transfer between the two species



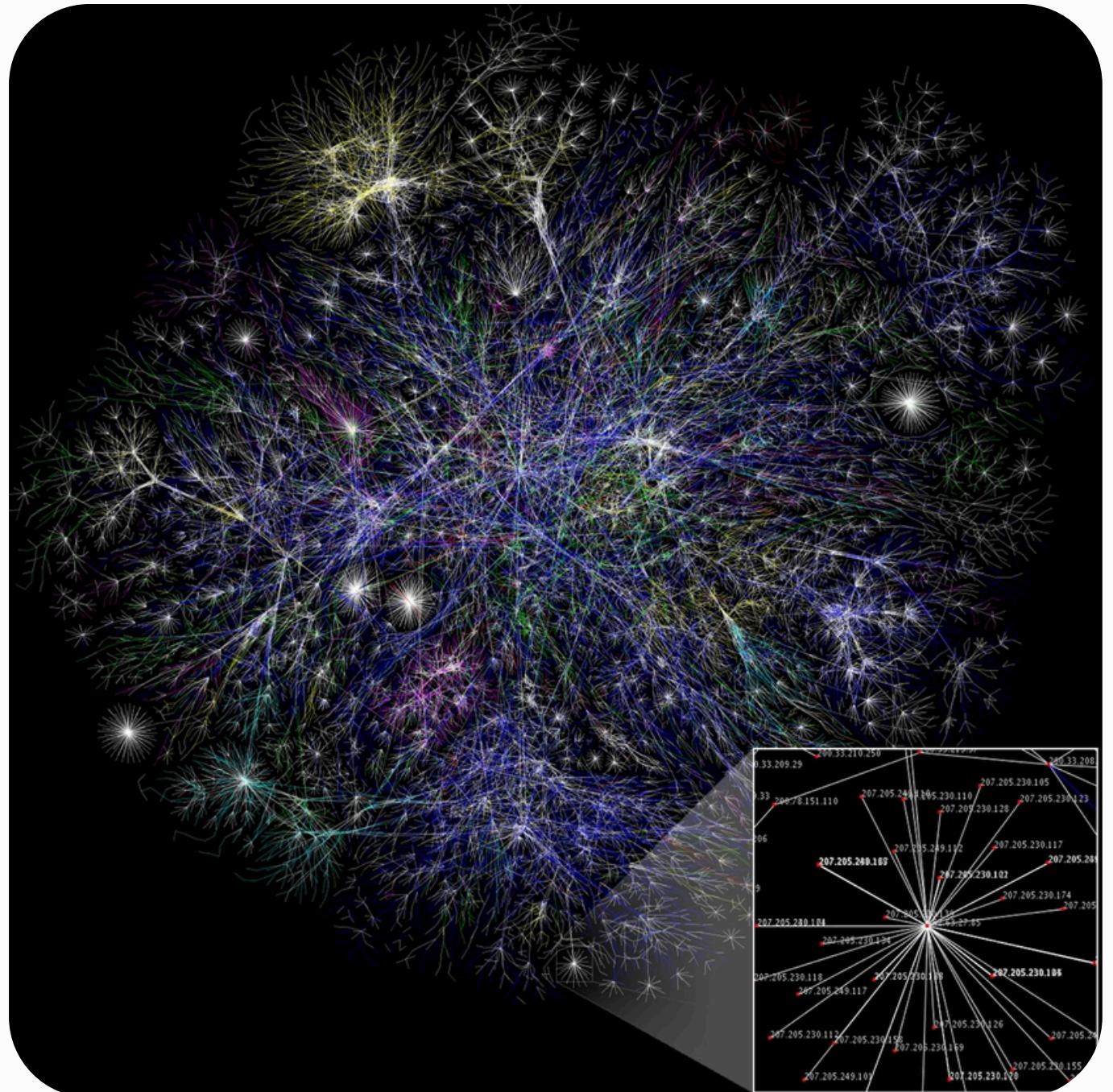
Potapov, A.M. et al. Rainforest transformation reallocates energy from green to brown food webs. *Nature* 627, 116–122 (2024).

Air Transportation Network

Airlines connect airports forming the air transportation network: nodes are airports, (directed) links represent flights between airports



Internet Backbone



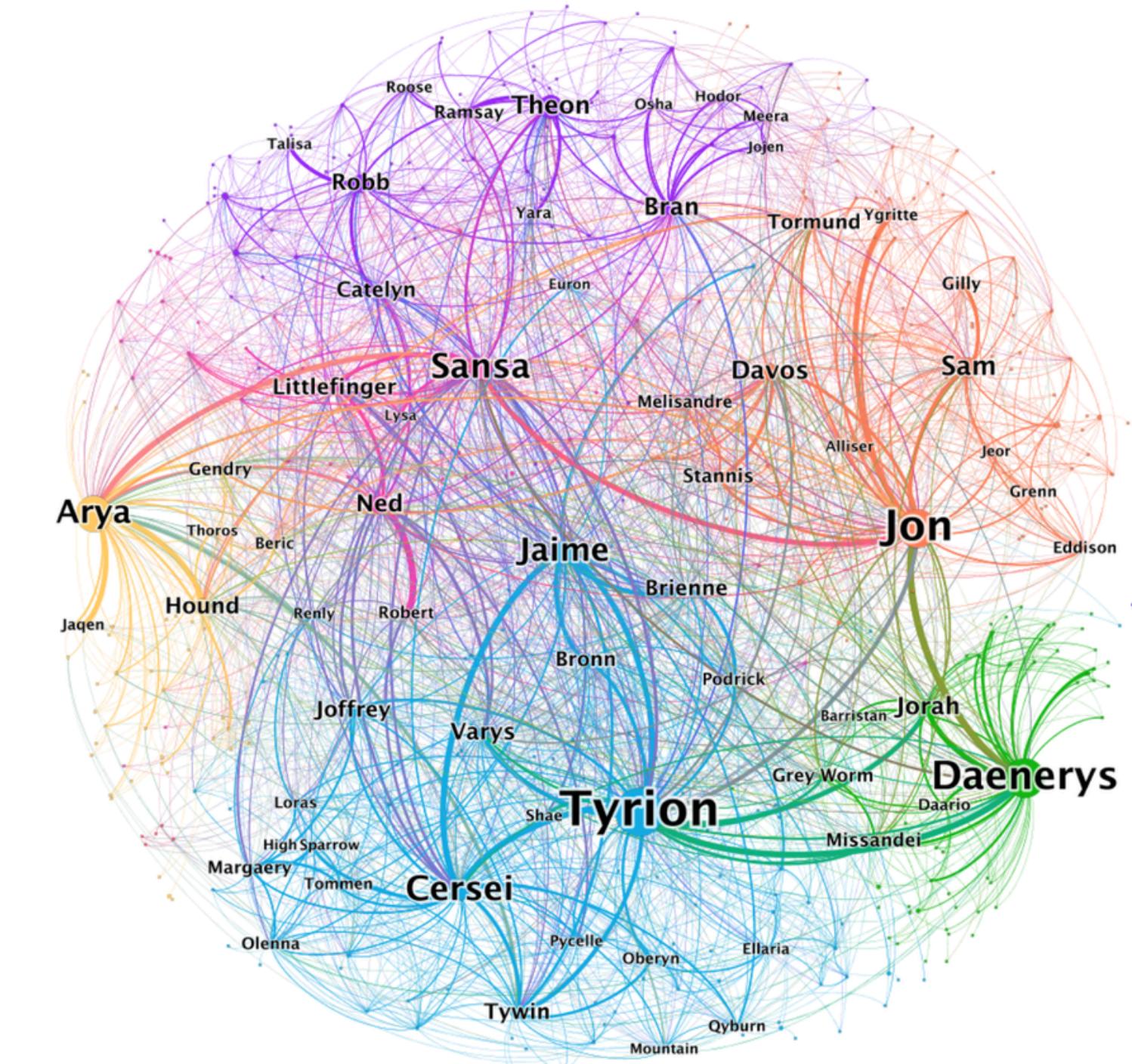
The global structure of the internet can be described as a network.

- Nodes are internet routers, data centers, servers
- Links are physical or logical connections (fiber optics, satellite links, etc.) that transfer data
- The network is directed
- The links can be weighted by bandwidth capacity or latency

Network of Thrones

We can build a network more or less out of everything. For instance we can visualize Game of Thrones as a network

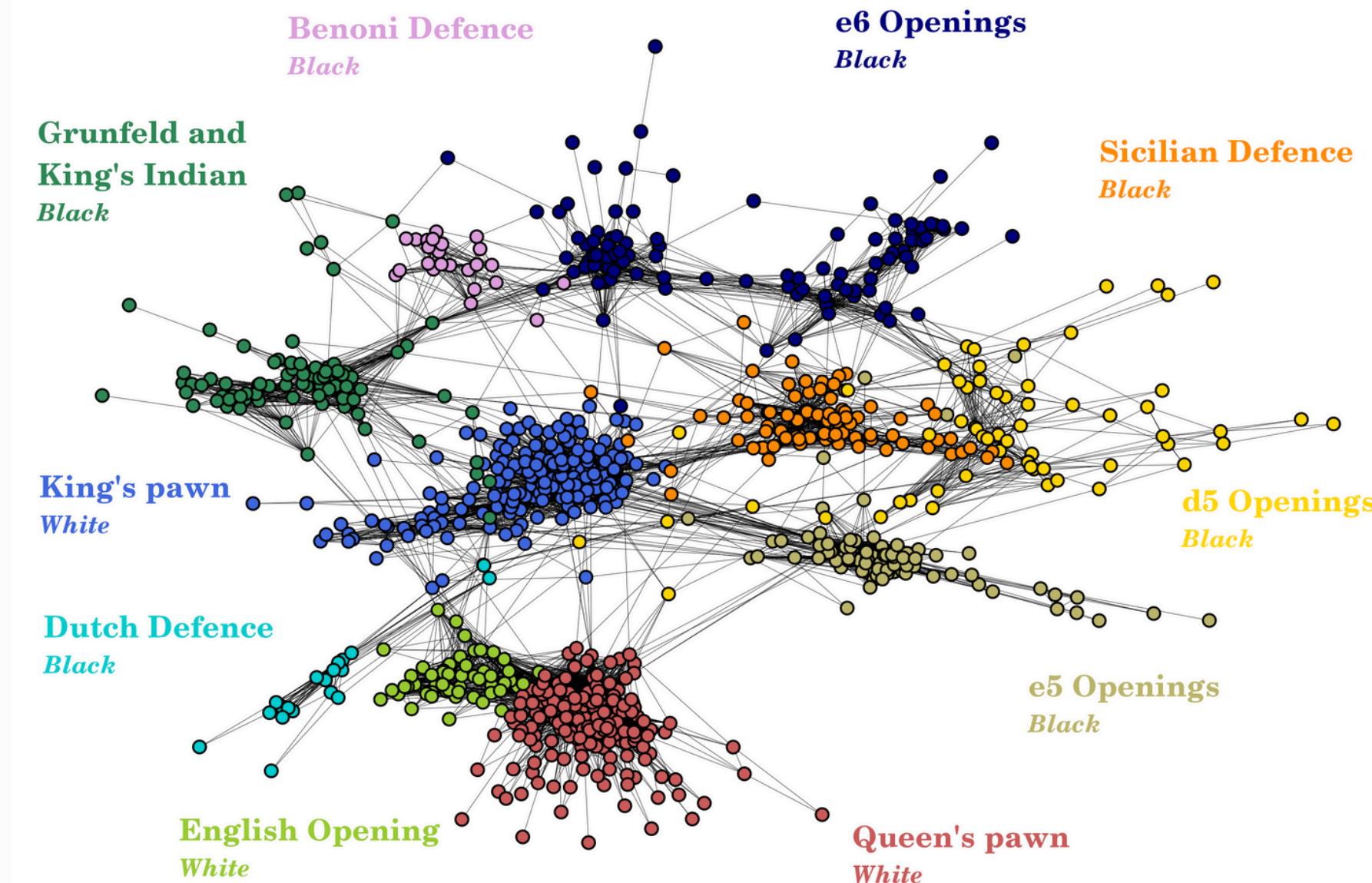
- nodes are characters
 - links represent who co-appearances of two characters
 - the weight gives the number of times two characters appeared together



networkofthrones.com

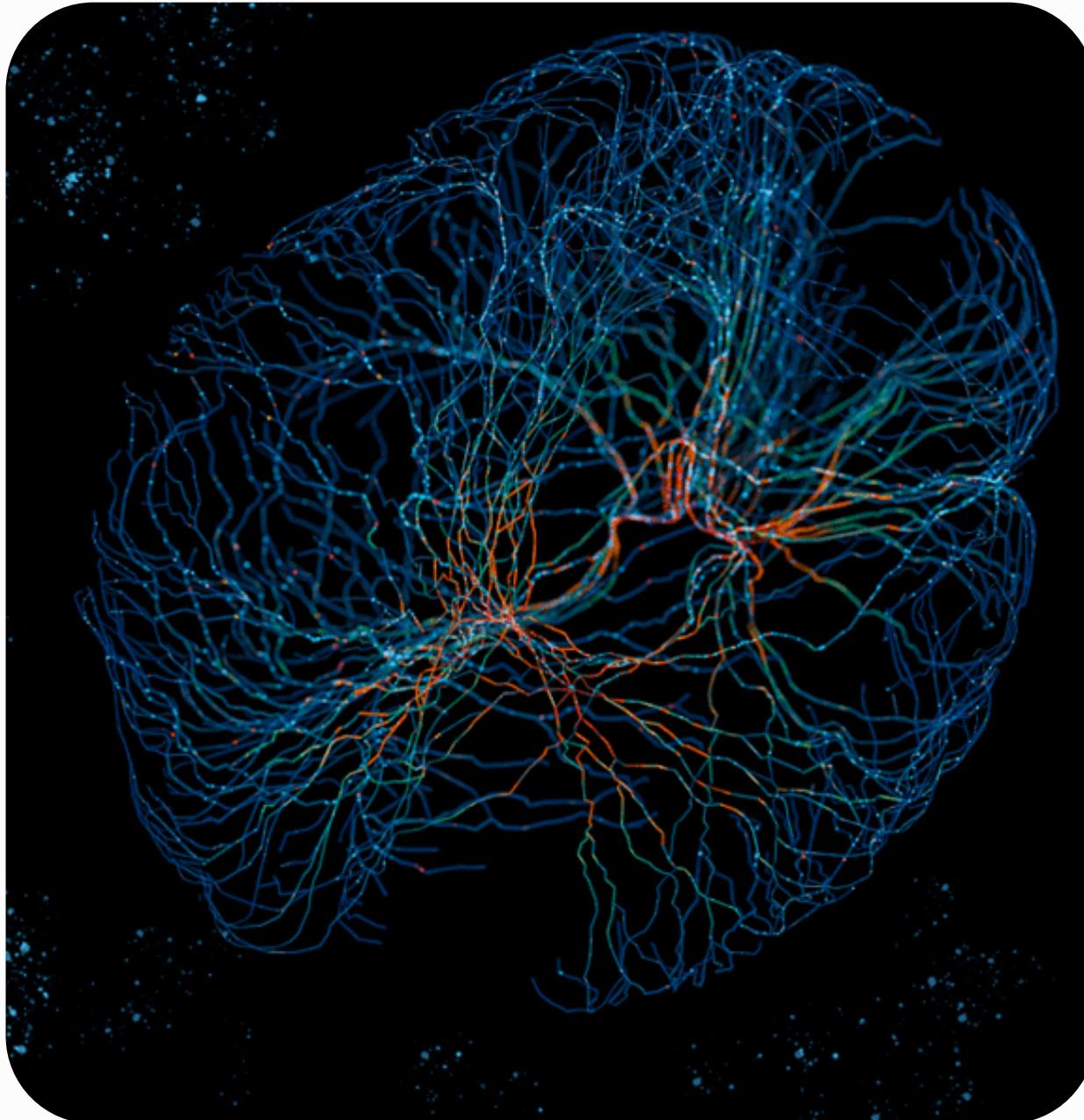
Chess Openings Network

Each dot is a specific chess opening, while (undirected) links represent similarity relations between these openings



De Marzo, Giordano, and Vito DP Servedio. "Quantifying the complexity and similarity of chess openings using online chess community data." *Scientific Reports* 13.1 (2023): 5327.

Neural Networks



Networks describe both biological and artificial neural networks

- Nodes are neurons (in biological networks) or artificial neurons (in artificial networks).
- Links are Synapses or weighted connections
- In both cases, the network is directed and weighted

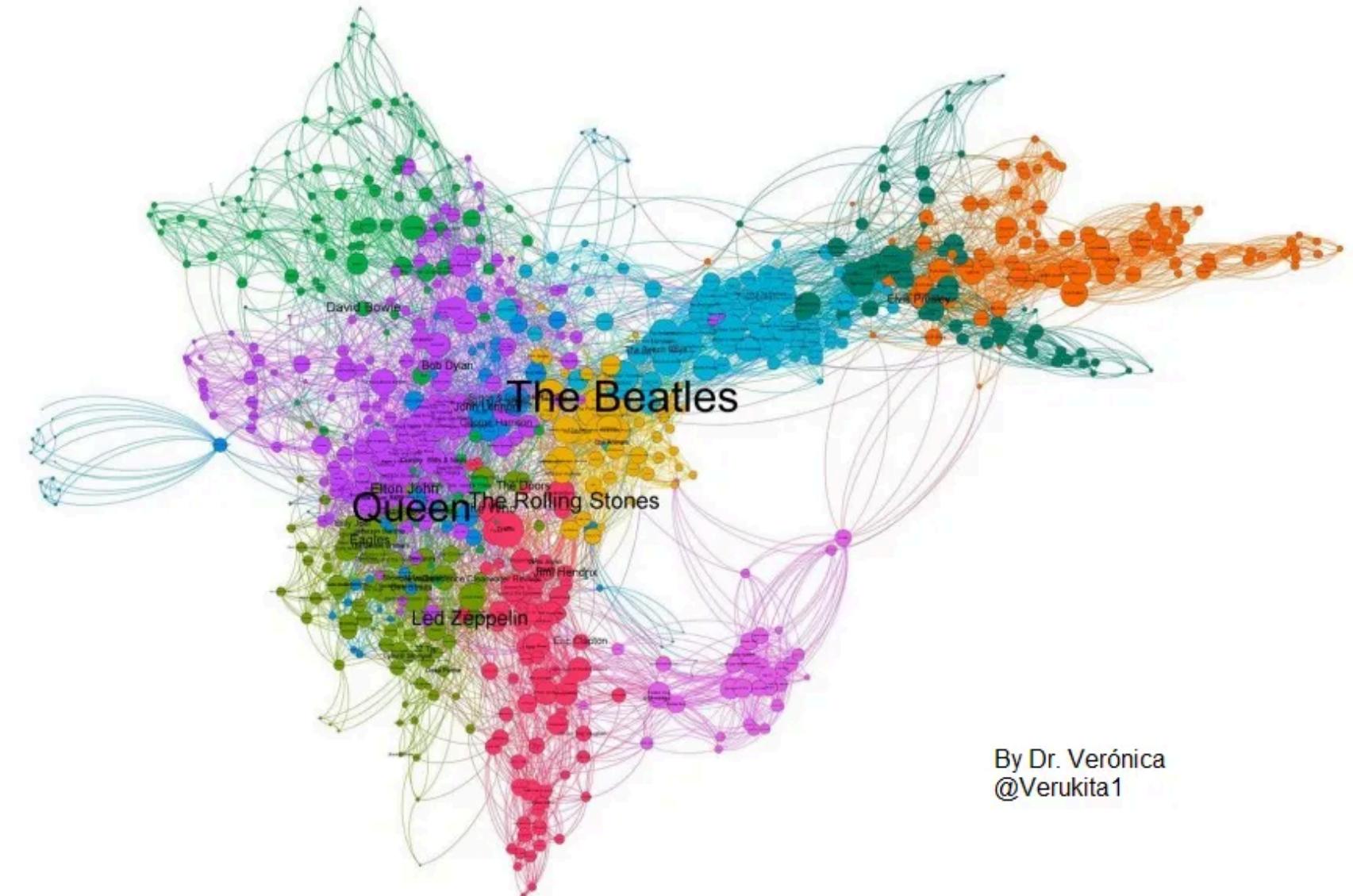
<https://news.mit.edu/2022/neural-networks-brain-function-1102>

Network of Spotify Artists

We can use network science to study music on Spotify

- nodes are artists
- links represent similarity between artists
- the weight gives the similarity score between them

You can try it with your favorite artist



[https://labs.polsys.net/playground/
spotify/.com](https://labs.polsys.net/playground/spotify/.com)

Network Science



What is Network Science?

Network Science is an interdisciplinary field that studies complex systems through their network structures

- Bridges mathematics, physics, computer science, sociology, biology, and economics
- focuses on the relationships between components (nodes) rather than individual components themselves
- analyzes both the topology (structure) and the processes (information flow, influence, etc.) occurring over networks

Research Questions

Network Dynamics

How do networks form and evolve over time? What are the processes leading to particular networks structures?

Processes on Networks

How does the network topology influences the process taking place on it? Examples can be epidemic spreading or opinion dynamics

Analysis of Real Networks

Which are the most influential nodes within a network? How resilient is a social or economic network? Which are the communities within a social network?

Network Dynamics

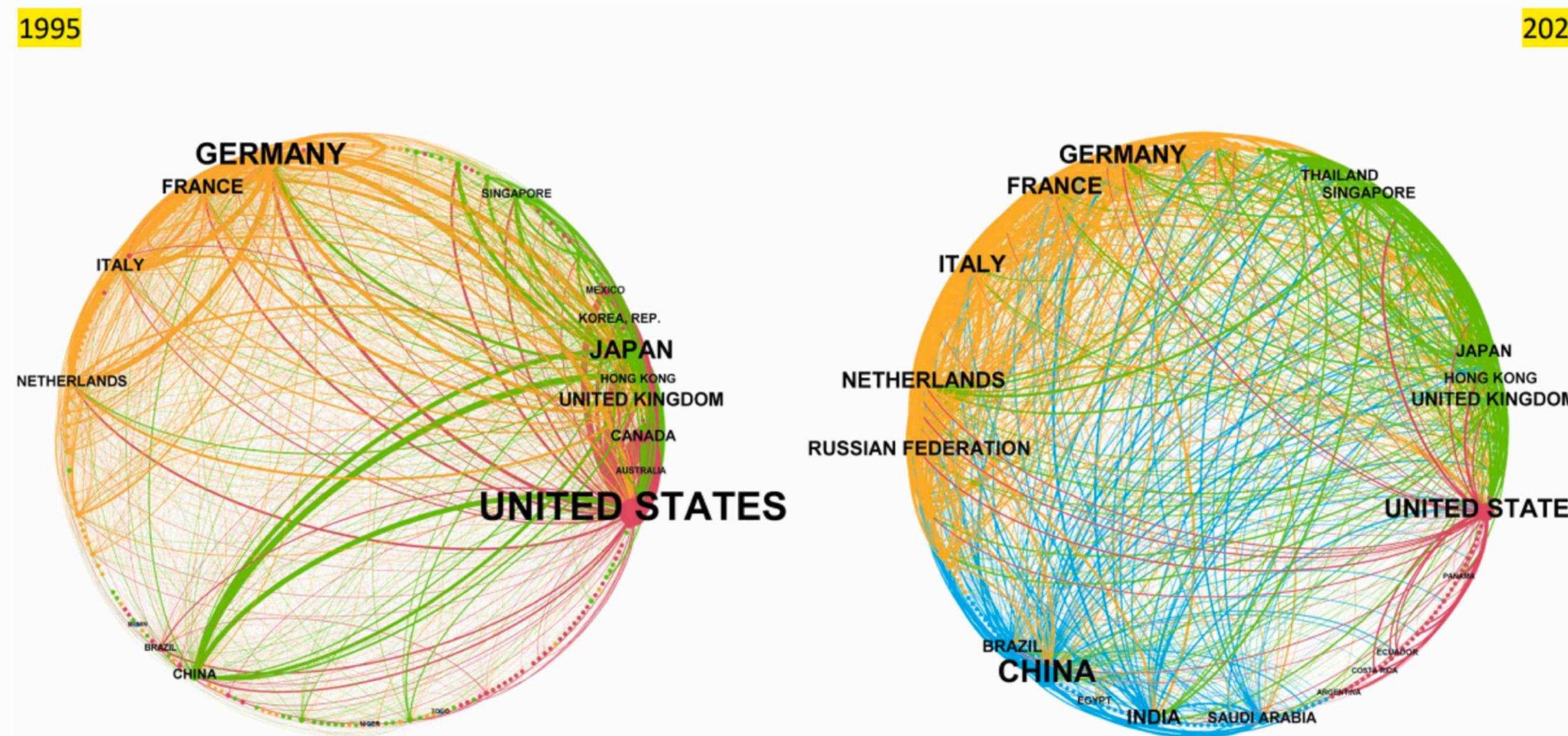
One of the main areas of network science is the study of Networks formation and dynamics

- many real world network from very different systems show similar statistical properties
- which are the growing mechanisms leading to many networks sharing similar characteristics?
- how do extremely complex structures like the internet can form from simple, pairwise interactions?

We will cover the main network growth processes in lectures 3 and 4

Network Dynamics

Evolution of the world trade network from 1995 to 2021



<https://doi.org/10.1016/j.joitmc.2023.100009>

Processes on Networks

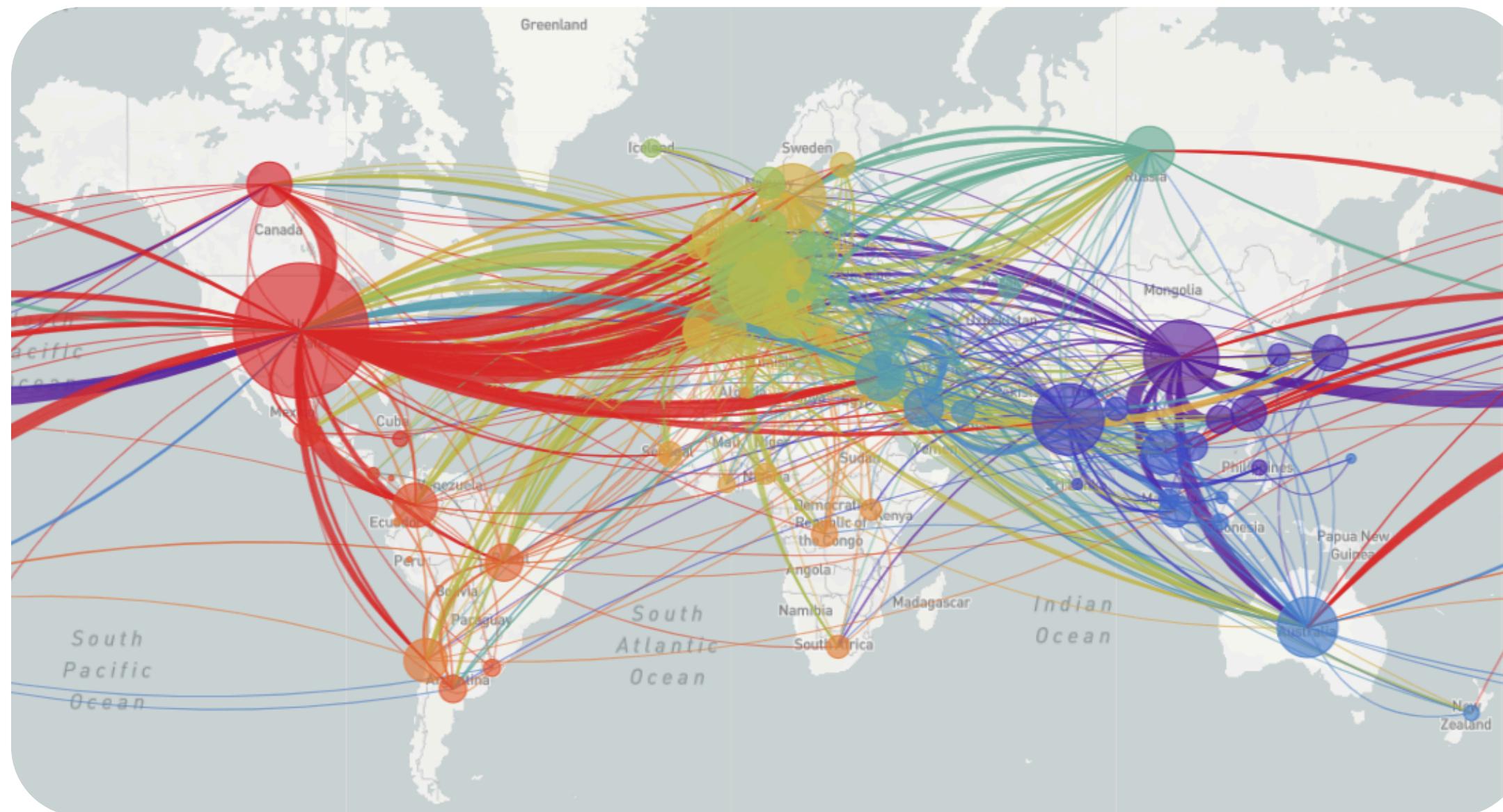
Not only a network can evolve, but processes can also take place on it, potentially shaping its growth process

- most interesting phenomena take place over network structures
- epidemic spreading is governed by transportation networks
- opinion dynamics take place on (online) social networks
- a process on a network can influence the network itself, for instance opinion dynamics may lead to the formation of a clustered social network

We will cover the main network processes in lecture 7

Processes on Networks

COVID-19 transmission network as of May 30, 2020



<https://gwips.ucc.ie/covid19.html>

Analysis of Real Networks

Network science can also be used to study and characterize real world networks and their components

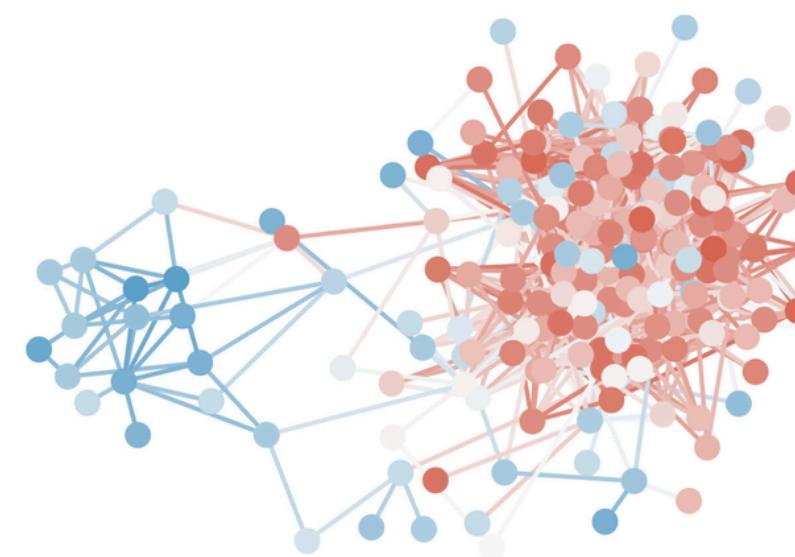
- centrality measures can help identify the most influential actors within a network
- community detection can spot groups within networks
- network based techniques can be used to understand the preferences and tastes of users
- the most significant links can be individuated and the resilience of an entire network can be computed

We will cover the main network processes in lectures 2, 5 and 6

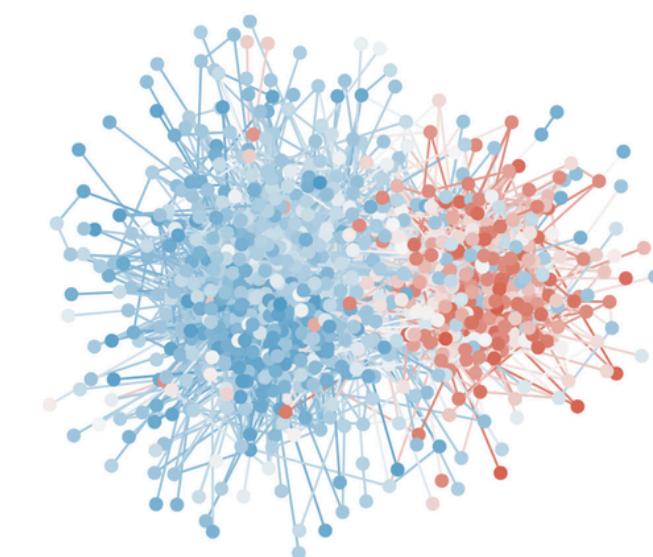
Analysis of Real Networks

Debates networks happening on Twitter in the mid-2010s

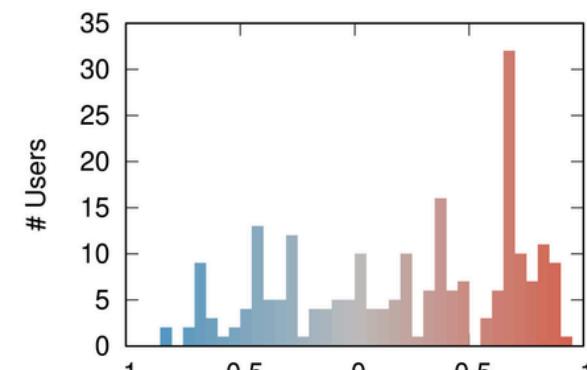
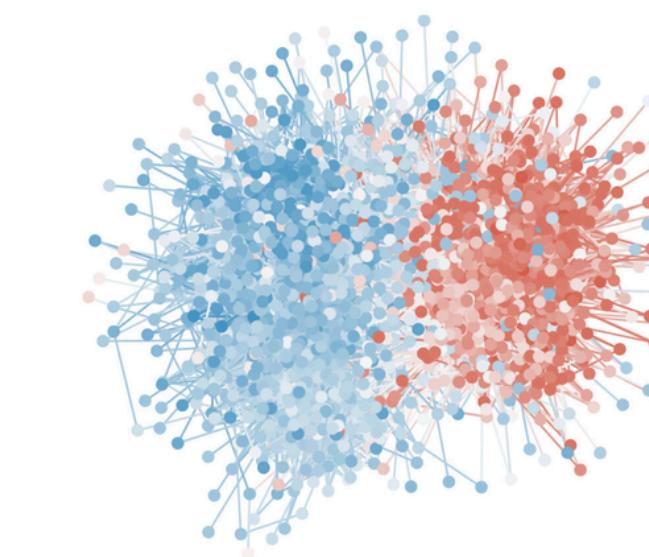
Obamacare



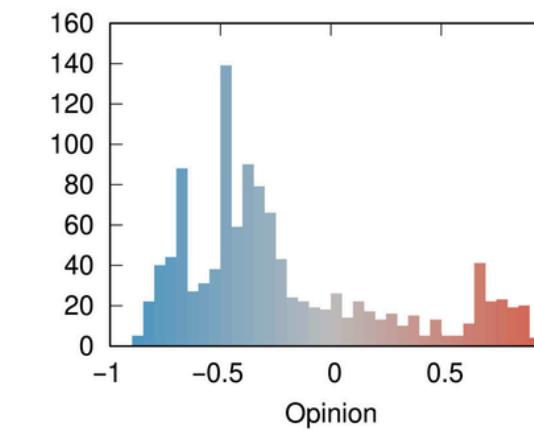
Gun control



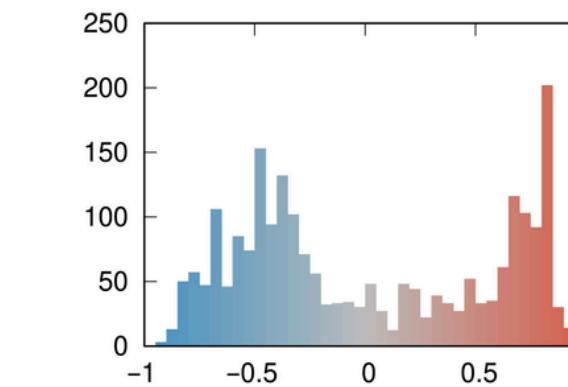
Abortion



9.44

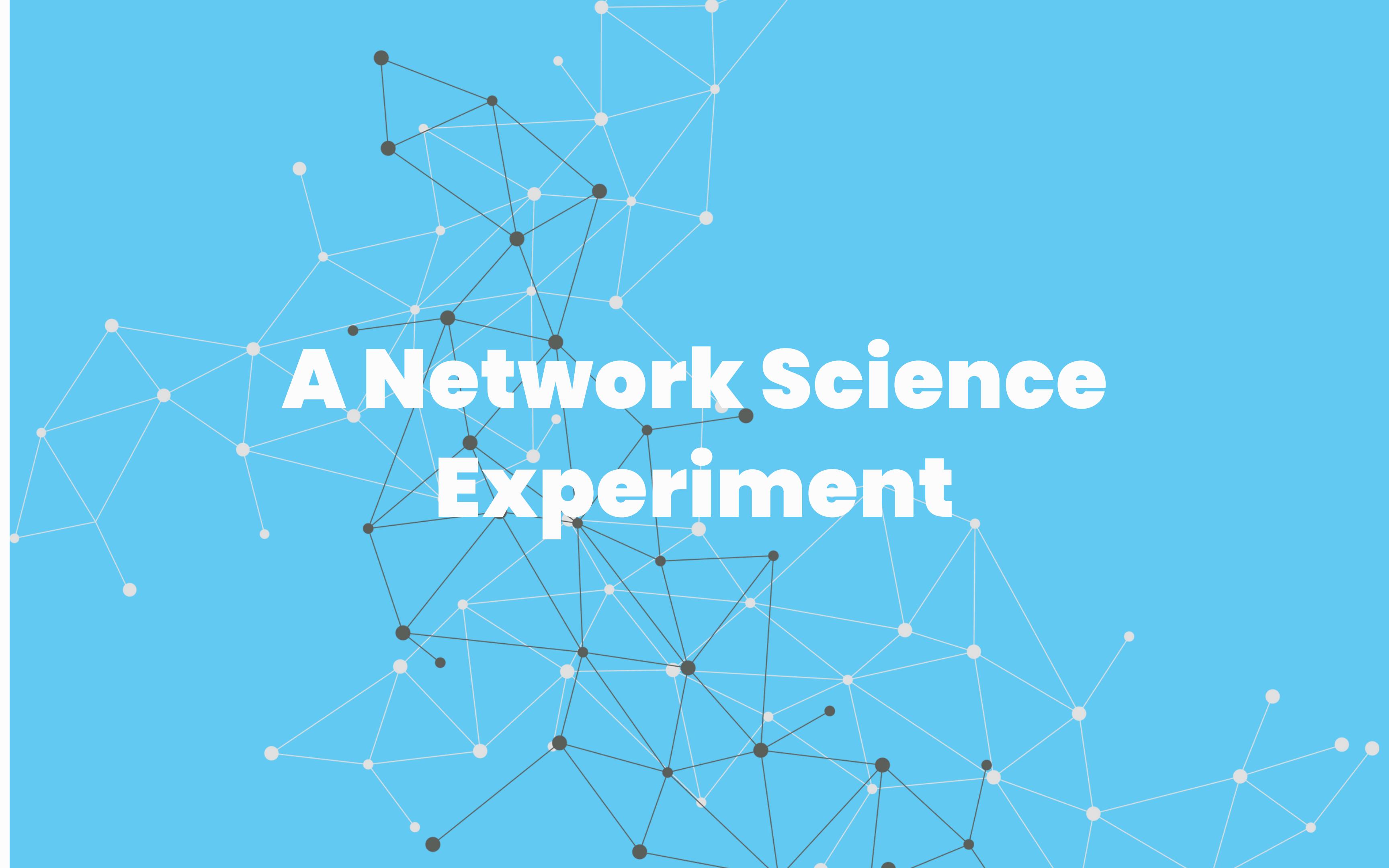


11.17



16.71

<https://doi.org/10.1126/sciadv.abq2044>



A Network Science Experiment

The Research Question

**Can we use network theory to understand which cocktails
are closer to individuals' tastes?**

Cocktail Project: a social experiment to validate network theory-based
recommendations of cocktails

Giordano De Marzo^{1,2,3,4}, Vito D. P. Servedio³, et al.³

¹*Centro Ricerche Enrico Fermi, Piazza del Viminale, 1, I-00184 Rome, Italy*

²*Dipartimento di Fisica, Sapienza Università di Roma, Roma, Italy.*

³*Complexity Science Hub Vienna, Josefstadtter Strasse 39, 1080, Vienna, Austria.*

⁴*Sapienza School for Advanced Studies, “Sapienza”, P.le A. Moro, 2, I-00185 Rome, Italy.*

Cocktails Data



We use the thecocktailedb.com dataset.

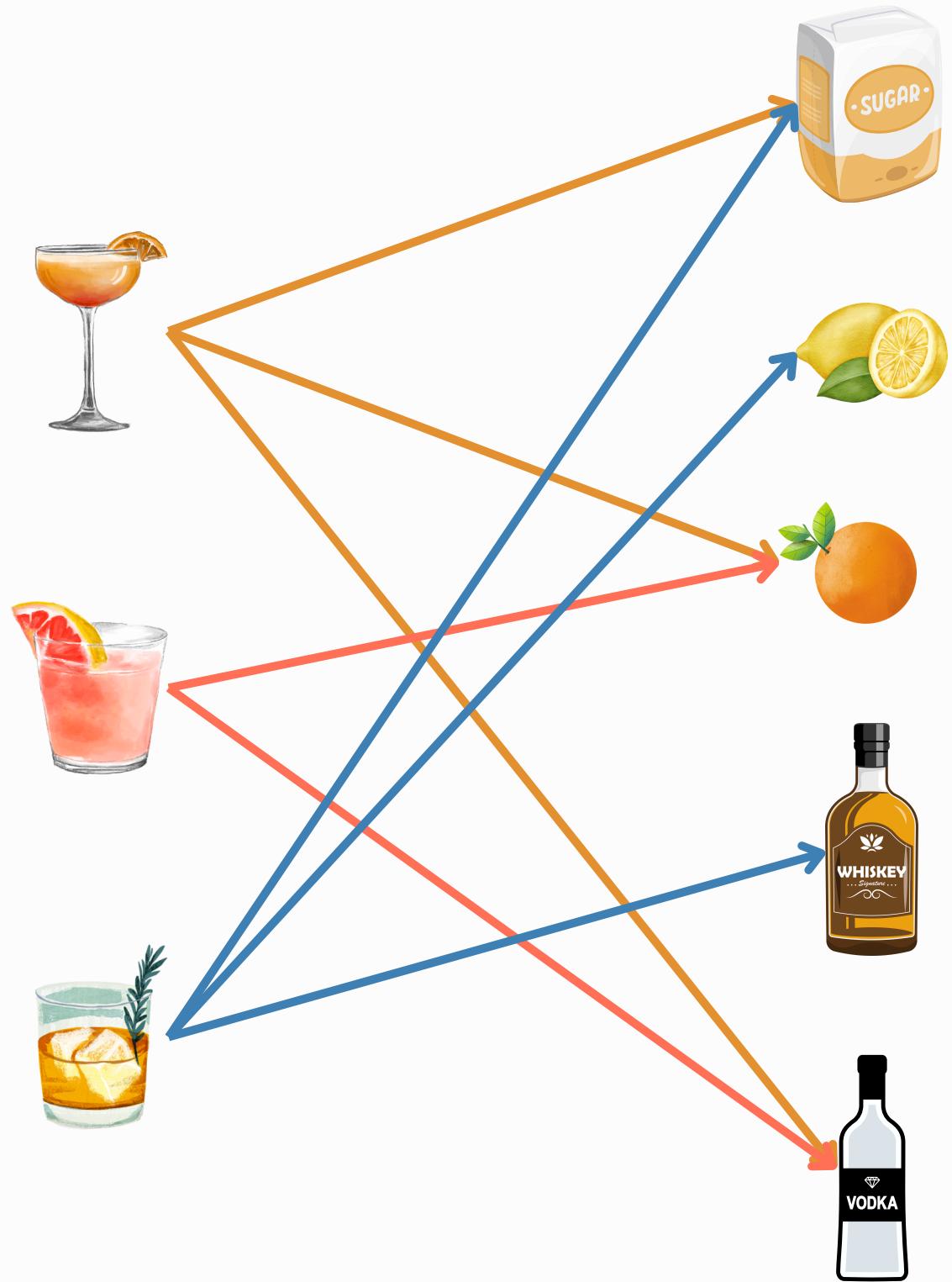
It provides

- ingredients
- procedure
- glass to be used
- cocktail image

A Bipartite Network

Recipes can be described as a bipartite network:

- one layer contains all drinks
- the other layer contains all ingredients
- arrows connect cocktails to ingredients



Bipartite Network Projection

Starting from the bipartite network we can build a cocktail network by projecting it:

- cocktails sharing many cooccurrences are similar
- ingredients used in many cocktails carry less information

Cocktail Network
Matrix

$$M_{ck} = \frac{1}{d_k} \sum_i \frac{B_{ci} \cdot B_{ki}}{u_i}$$

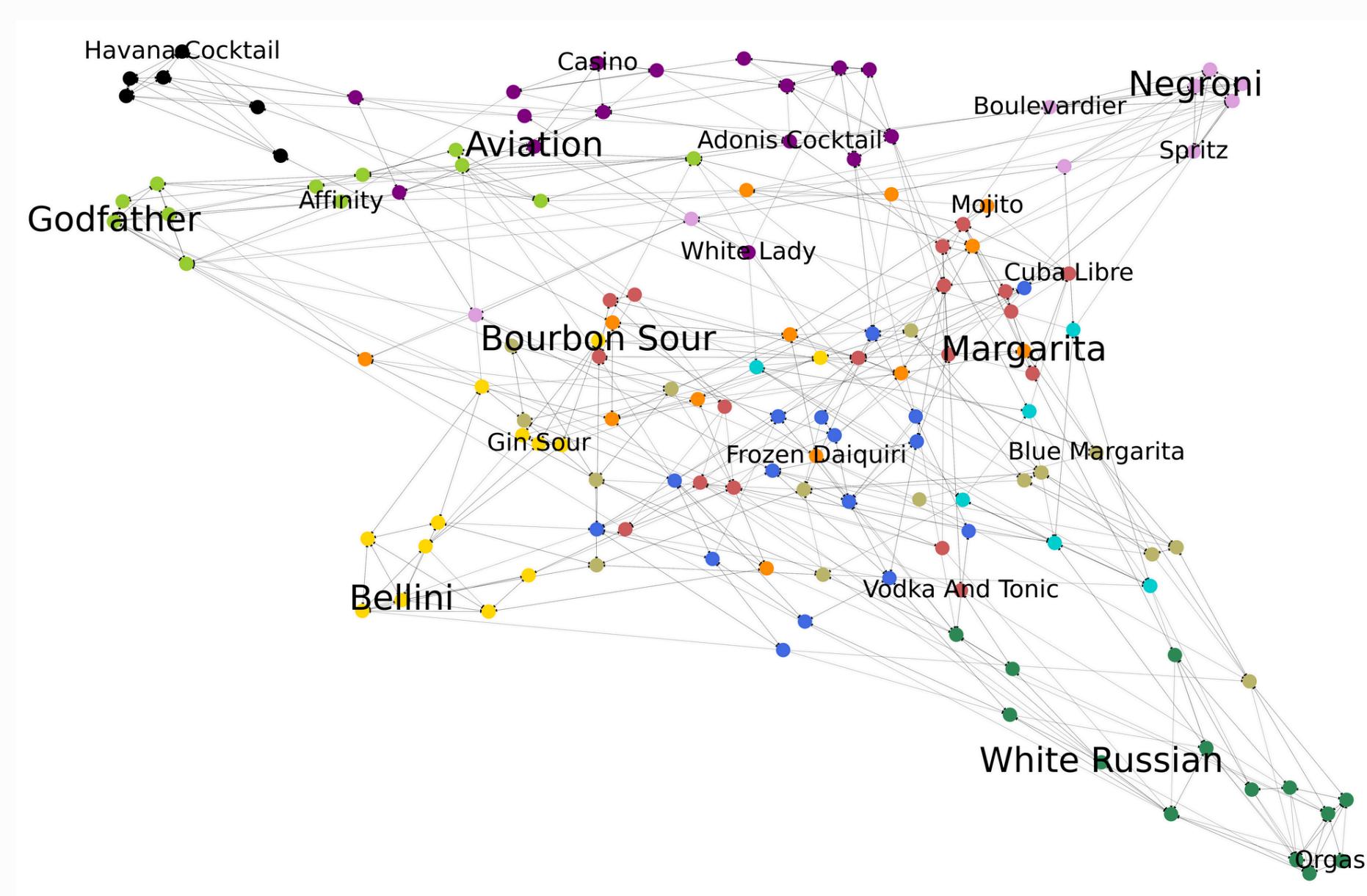
Cocktail k
diversification

Cocktail-Ingredient
bipartite matrix

Ingredient i
ubiquity

Network of Cocktails

Cocktails that are close on the network have similar ingredients and thus similar taste



The Experiment

In order to understand if the cocktail network is meaningful we have to validate it.

We devised a social experiment where users drink cocktails based on the position on the network.



Initial Survey

Users fill an initial survey to asses their level of knowledge about cocktails



Initial Cocktails Rating

All users initially taste and rate the same five cocktails as a starting point for the recommendation algorithm

We also collect additional information to look for patterns in the network



Cocktails Recommendations

Next, cocktails are automatically assigned to users by means of a network based recommendation algorithm

Data Analysis and Dataset

After the experiment we analyze the data and we curate a dataset on cocktail ratings

Web App

Cocktail Orders

Orders are digitally managed and collected



Data Collection

Users rate cocktails directly on the app



Cocktail Recommendations

Recommendations are fully automatized

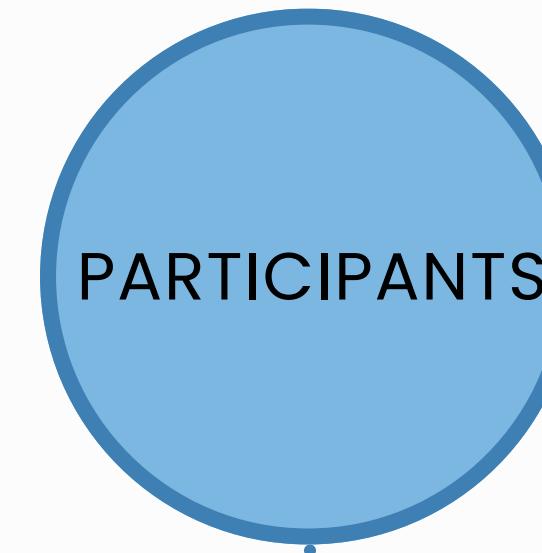
```
self.check_catch()
check_catch(self):
    """ Check if catch balls. """
    for ball in self.overlapping_sprites:
        self.score.value += 10
        ball.handle_caught()
    """ Change game level. """
    if self.score.value == 200:
        self.level.value += 1
    """ Next level game. """
    if self.level.value == games.size:
        games.level = games.size + 1
```

Some Numbers

We already performed four experimental sessions in the past years



Around 250
different cocktails



More than 100
participants



Around 750 ratings

Conclusions

Course Program

The first half of the course covers the main basic topics in network science. In the second half we will study more advanced topics with a focus on social and economic networks

Exam

Individual report and presentation. You can either reproduce a paper or analyze a network among those available on my website

Network Science

Network Science studies the dynamics of networks, the processes taking place on networks and the properties of nodes, links and structures within networks