

Properties of inner products

5/5 points (100.00%)

Quiz, 5 questions

✓

Congratulations! You passed!

Next Item



1 / 1
points

Properties of inner products

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Quiz, 5 questions

1.
The function

$$\beta(\mathbf{x}, \mathbf{y}) = \mathbf{x}^T \begin{bmatrix} 2 & -1 \\ -1 & 1 \end{bmatrix} \mathbf{y}$$

is

☐

symmetric

Correct
Yes: $\beta(\mathbf{x}, \mathbf{y}) = \beta(\mathbf{y}, \mathbf{x})$

☐

not positive definite

Un-selected is correct

☐

not bilinear

Un-selected is correct

☐

an inner product

Correct
It's symmetric, bilinear and positive definite. Therefore, it is a valid inner product.

☐

bilinear

Correct
Yes:

- β is symmetric. Therefore, we only need to show linearity in one argument.
- For any $\lambda \in \mathbb{R}$ it holds that $\beta(\mathbf{x} + \lambda \mathbf{z}, \mathbf{y}) = \beta(\mathbf{x}, \mathbf{y}) + \lambda \beta(\mathbf{z}, \mathbf{y})$. This holds because of the rules for vector-matrix multiplication and addition



1 / 1
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2.
The function

$$\beta(\mathbf{x}, \mathbf{y}) = \mathbf{x}^T \begin{bmatrix} 1 & -1 \\ -1 & 1 \end{bmatrix} \mathbf{y}$$

is

☐

 symmetric

Correct
Correct: $\beta(\mathbf{x}, \mathbf{y}) = \beta(\mathbf{y}, \mathbf{x})$

☐

 not an inner product

Correct
Correct: Since β is not positive definite, it cannot be an inner product.

☐

 not positive definite

Correct
With $x = [1, 1]^T$ we get $\beta(\mathbf{x}, \mathbf{x}) = 0$. Therefore β is not positive definite.

☐

 an inner product

Un-selected is correct

☐

 not symmetric

Un-selected is correct

☐

 bilinear

Correct



1 / 1
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3.
The function

$$\beta(\mathbf{x}, \mathbf{y}) = \mathbf{x}^T \begin{bmatrix} 2 & 1 \\ -1 & 1 \end{bmatrix} \mathbf{y}$$

is

☐ symmetric

Un-selected is correct

☐ not symmetric

Correct
Correct: If we take $\mathbf{x} = [1, 1]^T$ and $\mathbf{y} = [2, -1]^T$ then $\beta(\mathbf{x}, \mathbf{y}) = 0$ but $\beta(\mathbf{y}, \mathbf{x}) = 6$. Therefore, β is not symmetric.

☐ bilinear

Correct
Correct.

☐ not bilinear

Un-selected is correct

☐ an inner product

Un-selected is correct

☐ not an inner product

Correct
Correct: Symmetry is violated.



1 / 1
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4.
The function

$$\beta(\mathbf{x}, \mathbf{y}) = \mathbf{x}^T \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \mathbf{y}$$

is

☐

 positive definite

Correct
It is the dot product, which we know already. Therefore, it is positive definite.

☐

 symmetric

Correct
It is the dot product, which we know already. Therefore, it is symmetric.

☐

 not positive definite

Un-selected is correct

☐

 bilinear

Correct
It is the dot product, which we know already. Therefore, it is positive bilinear.

☐

 an inner product

Correct
It is the dot product, which we know already. Therefore, it is also an inner product.

Properties of inner products



1 / 1

points

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5.

For any two vectors $\mathbf{x}, \mathbf{y} \in \mathbb{R}^2$ write a short piece of code that defines a valid inner product.

```
1 import numpy as np
2
3 def dot(a, b):
4     """Compute dot product between a and b.
5     Args:
6         a, b: (2,) ndarray as R^2 vectors
7
8     Returns:
9         a number which is the dot product between a, b
10    """
11
12    dot_product = a[0]*b[0]+a[1]*b[1]
13
14    return dot_product
15
16 # Test your code before you submit.
17 a = np.array([1,0])
18 b = np.array([0,1])
19 print(dot(a,b))
```

Run

Reset

Correct Response

Good job!

