# CS451 (Distributed Algorithms): Lattice Agreement

#### 1 SYSTEM MODEL & PRELIMINARIES

Processes. We assume a static system  $\Psi = \{P_1, ..., P_n\}$  of n = 2f + 1 processes among which some processes can fail by *crashing*. A process that fails is said to be *faulty*; a non-faulty process is *correct*. We assume that at most f processes can fail. Processes communicate by exchanging messages over an authenticated point-to-point network. The communication network is *reliable*: if a correct process sends a message to a correct process, the message is eventually received.

Asynchrony. The processes are asynchronous: a process proceeds at its own arbitrary (and non-deterministic) speed. Moreover, the communication network is asynchronous: message delays are finite, but arbitrarily big. In other words, if a correct process sends a message to another correct process, it is not known when the message will be received; it is just known that the message will eventually be received.

Lattice agreement. Let  $\mathcal{V}$  denote the set of values. The lattice agreement problem allows processes to agree on "similar" decisions despite failures. The lattice agreement problem exposes the following interface:

- request propose( $I \subseteq \mathcal{V}$ ): a process proposes a set I.
- **indication** decide( $O \subseteq V$ ): a process decides a set O.

The proposal of a process  $P_i$  is denoted by  $I_i$ , whereas the decision of a process  $P_i$  is denoted by  $O_i$ .

The lattice agreement problem requires the following properties to be satisfied:

• *Validity:* Let a process  $P_i$  decide a set  $O_i$ . Then:

```
- I_i \subseteq O_i, \text{ and}
- O_i \subseteq \bigcup_{j \in [1,n]} I_j.
```

- Consistency: Let a process  $P_i$  decide a set  $O_i$  and let a process  $P_j$  decide a set  $O_j$ . Then,  $O_i \subseteq O_j$  or  $O_i \supset O_j$ .
- Termination: Every correct process eventually decides.

The validity property states that (1) the decided set must include the proposal set, and (2) the decided set includes the proposals of other processes (i.e., the decided set cannot include values which were not proposed). Consistency claims that decided values must be comparable. Finally, termination states that all correct processes eventually decide.

### 2 ALGORITHM

The algorithm considers two roles: proposers and acceptors. Every process plays *both* roles; the separation is included solely for the simplicity of the presentation.

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## **Algorithm 1** Lattice Agreement Algorithm: Pseudocode of proposer $P_i$

```
1: upon init:
 2:
          Boolean active_i = false
          Integer ack\_count_i = 0
 3:
          Integer nack\_count_i = 0
 4:
          Integer active\_proposal\_number_i = 0
 5:
          Set proposed\_value_i = \bot
 7: upon propose(Set proposal):
          proposed\_value_i \leftarrow proposal
 8:
          active_i \leftarrow true
 9:
          active\_proposal\_number_i \leftarrow active\_proposal\_number_i + 1
10:
          ack\_count_i \leftarrow 0
11:
12:
          nack\ count_i \leftarrow 0
          trigger beb.broadcast(\langle PROPOSAL, proposed\_value_i, active\_proposal\_number_i \rangle)
13:
14: upon reception of \( \text{ACK}, \text{ Integer } proposal_number \) \( \text{such that } proposal_number = active_proposal_number; \):
          ack\_count_i \leftarrow ack\_count_i + 1
15:
16: upon reception of \( \text{NACK}, \text{Integer } \text{proposal_number}, \text{Set } \text{value} \)
                                                                                             such that proposal_number
    active_proposal_number;:
          proposed\_value \leftarrow proposed\_value \cup value
          nack\_count_i \leftarrow nack\_count_i + 1
18:
19: upon nack\_count_i > 0 and ack\_count_i + nack\_count_i \ge f + 1 and active_i = true:
          active\_proposal\_number_i \leftarrow active\_proposal\_number_i + 1
21:
          ack\_count_i \leftarrow 0
22:
          nack\ count_i \leftarrow 0
          trigger beb.broadcast(\(\rangle \text{PROPOSAL}, \rangle roposed_value_i, \active_proposal_number_i \rangle)\)
23:
24: upon ack\_count_i \ge f + 1 and active_i = true:
          trigger decide(proposed value;)
          active_i \leftarrow false
26:
```

### **Algorithm 2** Lattice Agreement Algorithm: Pseudocode of acceptor $P_i$

```
    upon init:
    Set accepted_value<sub>i</sub> = ⊥
    upon reception of ⟨PROPOSAL, Set proposed_value, Integer proposal_number⟩ from proposer P<sub>j</sub> such that accepted_value<sub>i</sub> ⊆ proposed_value:
    accepted_value<sub>i</sub> ← proposed_value
    send ⟨ACK, proposal_number⟩ to P<sub>j</sub>
    upon reception of ⟨PROPOSAL, Set proposed_value, Integer proposal_number⟩ from proposer P<sub>j</sub> such that accepted_value<sub>i</sub> ⊈ proposed_value:
    accepted_value<sub>i</sub> ← accepted_value<sub>i</sub> ∪ proposed_value
    accepted_value<sub>i</sub> ← accepted_value<sub>i</sub> ∪ proposed_value
    send ⟨NACK, proposal_number, accepted_value<sub>i</sub>⟩ to P<sub>j</sub>
```