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Bubbles in a ferromagnetic superfluid

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- **Introduction:** What is a ferromagnetic superfluid?
- **Theoretical background:** Coherently coupled BEC spin-mixtures
- **Data analysis:** False Vacuum Decay bubbles
- **Conclusions**



The ideal Bose gas is a quantum system of N non-interacting bosons, described by statistical mechanics.

$$\langle n_i \rangle = \frac{1}{e^{\beta(\epsilon_i - \mu)} - 1}$$

The occupation number of the ground state $N_0 = \langle n_0 \rangle$ corresponds to the condensation. There is a phase transition at $T = T_c$.

$$\frac{N_0}{N} = 1 - \left(\frac{T}{T_c} \right)^\alpha \quad \text{for } T < T_c$$

In a finite box $\alpha = 3/2$, in harmonic confinement $\alpha = 3$.



A system of weakly-interacting bosons can be described by a single wavefunction by a mean-field approximation, yielding the GPE

$$i\hbar \frac{\partial \psi(x, t)}{\partial t} = \left[-\frac{\hbar^2}{2m} \nabla^2 + V(x, t) + g|\psi(x, t)|^2 \right] \psi(x, t)$$

In the stationary case

$$\left[-\frac{\hbar^2}{2m} \nabla^2 + V(x) + g|\psi(x)|^2 \right] \psi(x) = \mu \psi(x)$$

When the interaction dominates

$$n(x) = \frac{\mu - V(x)}{g}$$

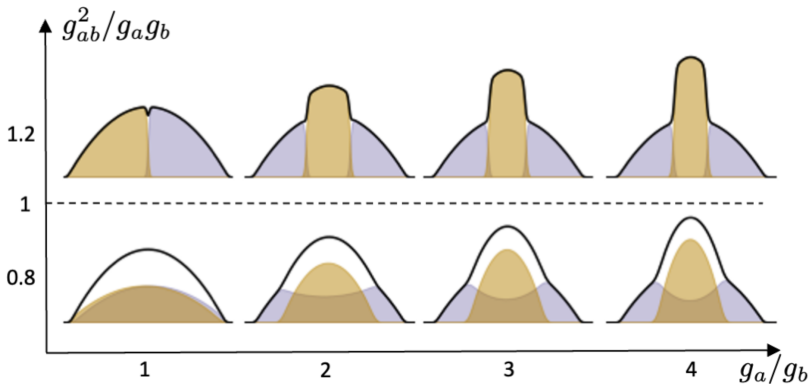


The GPEs are coupled because of the interspecies interaction constant

$$\left[-\frac{\hbar^2}{2m} \nabla^2 + V(x) + g_{aa} |\psi_a(x)|^2 + g_{ab} |\psi_b(x)|^2 \right] \psi_a(x) = \mu_a \psi_a(x)$$
$$\left[-\frac{\hbar^2}{2m} \nabla^2 + V(x) + g_{ab} |\psi_a(x)|^2 + g_{bb} |\psi_b(x)|^2 \right] \psi_b(x) = \mu_b \psi_b(x)$$

Depending on the values of g_{aa} , g_{bb} and g_{ab} , the system GS can behave in different manners

The mixture can be miscible or immiscible: buoyancy effect

















Thank you for the attention

