Topological Fractal Dimension of Networks of Protein–Protein Interaction Networks

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Fig. 1. Placeholder image of a frog with an example caption.

Table 1. Comparison of the fitted potential energy surfaces and ab initio benchmark electronic energy calculations

Species	CBS	CV	G3
1. Acetaldehyde	0.0	0.0	0.0
2. Vinyl alcohol	9.1	9.6	13.5
3. Hydroxyethylidene	50.8	51.2	54.0

nomenclature for the TSs refers to the numbered species in the table.

Fig. 2. This caption would be placed at the side of the figure, rather than below it.

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Table 2. Basic Information about PPINs

Organism	# Nodes	# Edges	Avg Degree	ConComps	Largest
Anopheles gambiae PEST	2	1	1.00	1	2
Apis mellifera	2	1	1.00	1	2
Arabidopsis thaliana Columbia	9626	36091	7.50	134	9389
Bacillus subtilis 168	3	2	1.33	2	2
Bos taurus	439	412	1.88	75	71
Caenorhabditis elegans	3954	8051	4.07	93	3753
*Candida albicans SC*5314	726	886	2.44	43	637
Canis familiaris	53	35	1.32	21	7
Cavia porcellus	9	5	1.11	4	3
Chlamydomonas reinhardtii	19	16	1.68	4	12
Chlorocebus sabaeus	11	7	1.27	4	3
Cricetulus griseus	32	24	1.50	8	16
Danio rerio	247	255	2.06	39	99
*Dictyostelium discoideum AX*4	24	20	1.67	6	5
Drosophila melanogaster	9197	55350	12.04	43	9113
*Emericella nidulans FGSC A*4	64	62	1.94	6	45
Equus caballus	4	2	1.00	2	2
*Escherichia coli K*12	2	1	1.00	1	2
*Escherichia coli K*12 *MC*4100 *BW*2952	10	9	1.80	2	8
*Escherichia coli K*12 *MG*1655	150	133	1.77	25	91
*Escherichia coli K*12 *W*3110	4063	181621	89.40	1	4063
Gallus gallus	391	421	2.15	42	230
Glycine max	45	40	1.78	8	14
Hepatitus C Virus	131	129	1.97	2	129
Homo sapiens	22840	321550	28.16	28	22798
Human Herpesvirus 1	174	195	2.24	1	174
Human Herpesvirus 2	7	4	1.14	3	3
Human Herpesvirus 3	4	2	1.00	2	2
Human Herpesvirus 4	240	235	1.96	7	185
Human Herpesvirus 5	91	80	1.76	12	35
Human Herpesvirus 6*A*	11	7	1.27	4	4
Human Herpesvirus 6*B*	7	4	1.14	3	3
Human Herpesvirus 7	2	1	1.00	1	2
Human Herpesvirus 8	714	689	1.93	45	378
Human Immunodeficiency Virus 1	1121	1306	2.33	1	1121
Human Immunodeficiency Virus 2	16	12	1.50	4	8
Human papillomavirus 16	14	12	1.71	2	12
Macaca mulatta	15	13	1.73	3	11
Meleagris gallopavo	2	2	2.00	1	2
Mus musculus	13021	38893	5.97	107	12793
*Mycobacterium tuberculosis H*37*Rv*	11	9	1.64	2	9
*Neurospora crassa OR*74*A*	12	10	1.67	2	8
Nicotiana tomentosiformis	2	2	2.00	1	2
Oryctolagus cuniculus	283	278	1.96	33	142
Oryza sativa Japonica	75	94	2.51	19	26
Ovis aries	2	1	1.00	1	2
Pan troglodytes	10	5	1.00	5	2
Pediculus humanus	2	1	1.00	1	2
Plasmodium falciparum 3*D*7	1227	2508	4.09	26	1179
Rattus norvegicus	3718	5282	2.84	123	3407
Ricinus communis	3	2	1.33	1	3
*Saccharomyces cerevisiae S*288*c*	7158	535782	149.70	1	7158
Schizosaccharomyces pombe 972*h*	4318	58739	27.21	33	4279
Selaginella moellendorffii	6	8	2.67	1	6
Simian Immunodeficiency Virus	19	16	1.68	4	8
Simian Virus 40	6	5	1.67	1	6
Solanum lycopersicum	45	109	4.84	7	21
Solanum tuberosum	5	3	1.20	3	2
Strongylocentrotus purpuratus	17	16	1.88	1	17
Sus scrofa	94	79	1.68	23	22
Tobacco Mosaic Virus	3	2	1.33	1	3
Ustilago maydis 521	4	4	2.00	1	4
Vaccinia Virus	8	6	1.50	3	3
Vitis vinifera	2	1	1.00	1	2
Xenopus laevis	1128	1223	2.17	61	959
Zea mays	21	13	1.24	10	3

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