

# Topological Fractal Dimension of Networks of Protein–Protein Interaction Networks

Georgios Kalantzis<sup>a</sup> and Andrei Stoica<sup>a</sup>

<sup>a</sup>SABS, DTC

This manuscript was compiled on October 29, 2018

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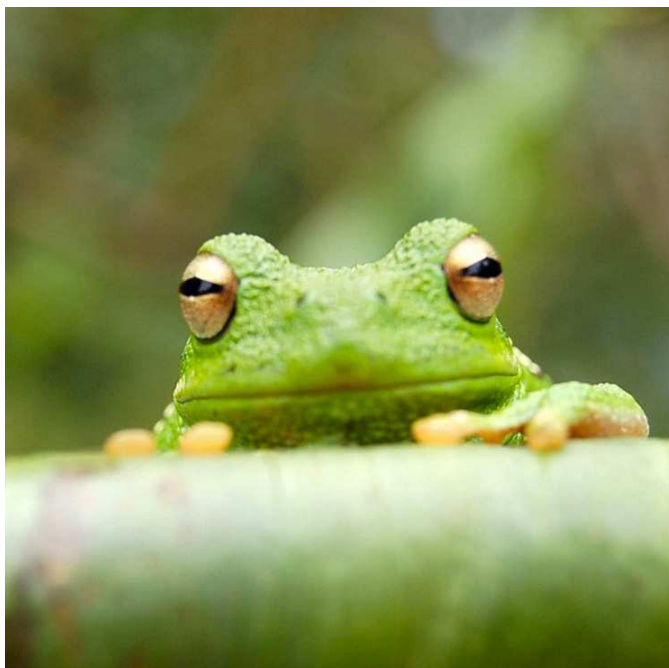
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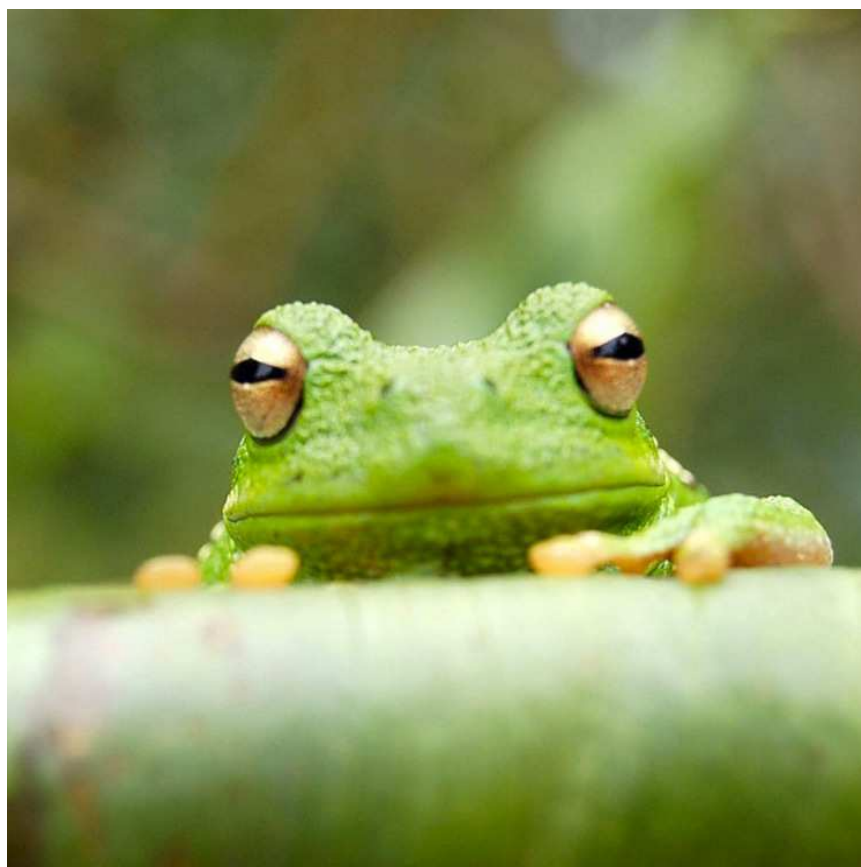


**Fig. 1.** Placeholder image of a frog with an example caption.

**Table 1. Comparison of the fitted potential energy surfaces and ab initio benchmark electronic energy calculations**

Species	CBS	CV	G3
1. Acetaldehyde	0.0	0.0	0.0
2. Vinyl alcohol	9.1	9.6	13.5
3. Hydroxyethylidene	50.8	51.2	54.0

nomenclature for the TSs refers to the numbered species in the table.



**Fig. 2.** This caption would be placed at the side of the figure, rather than below it.

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Table 2. Basic Information about PPINs

Organism	# Nodes	# Edges	Avg Degree	ConComps	Largest
<i>Anopheles gambiae</i> PEST	2	1	1.00	1	2
<i>Apis mellifera</i>	2	1	1.00	1	2
<i>Arabidopsis thaliana</i> Columbia	9626	36091	7.50	134	9389
<i>Bacillus subtilis</i> 168	3	2	1.33	2	2
<i>Bos taurus</i>	439	412	1.88	75	71
<i>Caenorhabditis elegans</i>	3954	8051	4.07	93	3753
<i>Candida albicans</i> SC5314	726	886	2.44	43	637
<i>Canis familiaris</i>	53	35	1.32	21	7
<i>Cavia porcellus</i>	9	5	1.11	4	3
<i>Chlamydomonas reinhardtii</i>	19	16	1.68	4	12
<i>Chlorocebus sabaeus</i>	11	7	1.27	4	3
<i>Cricetulus griseus</i>	32	24	1.50	8	16
<i>Danio rerio</i>	247	255	2.06	39	99
<i>Dictyostelium discoideum</i> AX4	24	20	1.67	6	5
<i>Drosophila melanogaster</i>	9197	55350	12.04	43	9113
<i>Emericella nidulans</i> FGSC A4	64	62	1.94	6	45
<i>Equus caballus</i>	4	2	1.00	2	2
<i>Escherichia coli</i> K12	2	1	1.00	1	2
<i>Escherichia coli</i> K12 MC4100 BW2952	10	9	1.80	2	8
<i>Escherichia coli</i> K12 MG1655	150	133	1.77	25	91
<i>Escherichia coli</i> K12 W3110	4063	181621	89.40	1	4063
<i>Gallus gallus</i>	391	421	2.15	42	230
<i>Glycine max</i>	45	40	1.78	8	14
Hepatitis C Virus	131	129	1.97	2	129
<i>Homo sapiens</i>	22840	321550	28.16	28	22798
Human Herpesvirus 1	174	195	2.24	1	174
Human Herpesvirus 2	7	4	1.14	3	3
Human Herpesvirus 3	4	2	1.00	2	2
Human Herpesvirus 4	240	235	1.96	7	185
Human Herpesvirus 5	91	80	1.76	12	35
Human Herpesvirus 6A	11	7	1.27	4	4
Human Herpesvirus 6B	7	4	1.14	3	3
Human Herpesvirus 7	2	1	1.00	1	2
Human Herpesvirus 8	714	689	1.93	45	378
Human Immunodeficiency Virus 1	1121	1306	2.33	1	1121
Human Immunodeficiency Virus 2	16	12	1.50	4	8
Human papillomavirus 16	14	12	1.71	2	12
<i>Macaca mulatta</i>	15	13	1.73	3	11
<i>Meleagris gallopavo</i>	2	2	2.00	1	2
<i>Mus musculus</i>	13021	38893	5.97	107	12793
<i>Mycobacterium tuberculosis</i> H37Rv	11	9	1.64	2	9
<i>Neurospora crassa</i> OR74A	12	10	1.67	2	8
<i>Nicotiana tomentosiformis</i>	2	2	2.00	1	2
<i>Oryctolagus cuniculus</i>	283	278	1.96	33	142
<i>Oryza sativa</i> Japonica	75	94	2.51	19	26
<i>Ovis aries</i>	2	1	1.00	1	2
<i>Pan troglodytes</i>	10	5	1.00	5	2
<i>Pediculus humanus</i>	2	1	1.00	1	2
<i>Plasmodium falciparum</i> 3D7	1227	2508	4.09	26	1179
<i>Rattus norvegicus</i>	3718	5282	2.84	123	3407
<i>Ricinus communis</i>	3	2	1.33	1	3
<i>Saccharomyces cerevisiae</i> S288c	7158	535782	149.70	1	7158
<i>Schizosaccharomyces pombe</i> 972h	4318	58739	27.21	33	4279
<i>Selaginella moellendorffii</i>	6	8	2.67	1	6
Simian Immunodeficiency Virus	19	16	1.68	4	8
Simian Virus 40	6	5	1.67	1	6
<i>Solanum lycopersicum</i>	45	109	4.84	7	21
<i>Solanum tuberosum</i>	5	3	1.20	3	2
<i>Strongylocentrotus purpuratus</i>	17	16	1.88	1	17
<i>Sus scrofa</i>	94	79	1.68	23	22
Tobacco Mosaic Virus	3	2	1.33	1	3
<i>Ustilago maydis</i> 521	4	4	2.00	1	4
<i>Vaccinia</i> Virus	8	6	1.50	3	3
<i>Vitis vinifera</i>	2	1	1.00	1	2
<i>Xenopus laevis</i>	1128	1223	2.17	61	959
<i>Zea mays</i>	21	13	1.24	10	3

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