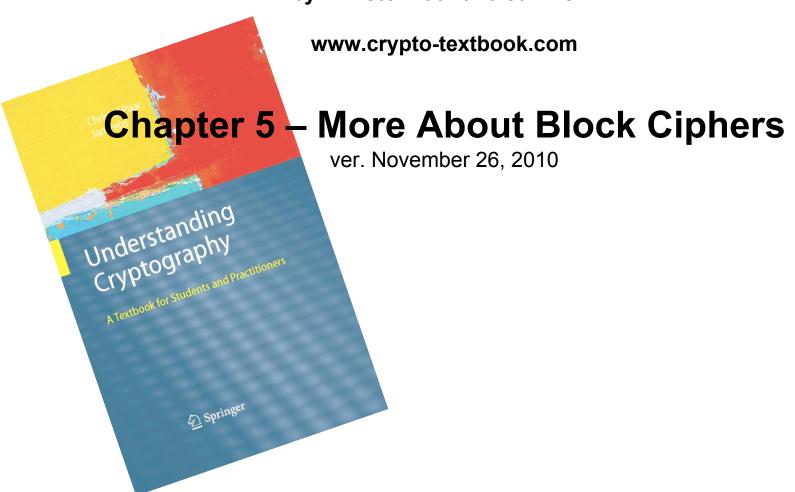
# Understanding Cryptography – A Textbook for Students and Practitioners

by Christof Paar and Jan Pelzl



These slides were prepared by Amir Moradi, Christof Paar and Jan Pelzl

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- Encryption with Block Ciphers: Modes of Operation
  - Electronic Code Book mode (ECB)
  - Cipher Block Chaining mode (CBC)
  - Output Feedback mode (OFB)
  - Cipher Feedback mode (CFB)
  - Counter mode (CTR)
  - Galois Counter Mode (GCM)
- Exhaustive Key Search Revisited
- Increasing the Security of Block Ciphers

#### Block Ciphers

- A block cipher is much more than just an encryption algorithm, it can be used ...
  - to build different types of block-based encryption schemes
  - to realize stream ciphers
  - to construct hash functions
  - to make message authentication codes
  - to build key establishment protocols
  - to make a pseudo-random number generator
  - ...
- The security of block ciphers also can be increased by
  - key whitening
  - multiple encryption

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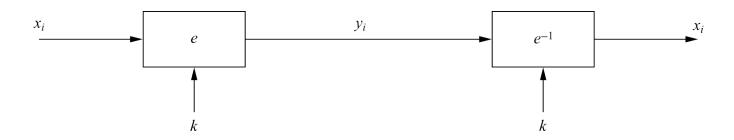
### Encryption with Block Ciphers

- There are several ways of encrypting long plaintexts, e.g., an e-mail or a computer file, with a block cipher ("modes of operation")
  - Electronic Code Book mode (ECB)
  - Cipher Block Chaining mode (CBC)
  - Output Feedback mode (OFB)
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- All of the 6 modes have one goal:
  - In addition to confidentiality, they provide authenticity and integrity:
    - Is the message really coming from the original sender? (authenticity)
    - Was the ciphertext altered during transmission? (integrity)

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### ■ Electronic Code Book mode (ECB)

- $e_k(x_i)$  denote the encryption of a *b*-bit plaintext block  $x_i$  with key k
- $e_k^{-1}(y_i)$  denote the decryption of b-bit ciphertext block  $y_i$  with key k
- Messages which exceed b bits are partitioned into b-bit blocks
- Each Block is encrypted separately



**Encryption**:  $y_i = e_k(x_i), i \ge 1$ 

**Decryption**:  $x_i = e_k^{-1}(y_i) = e_k^{-1}(e_k(x_i)), i \ge 1$ 

### ECB: advantages/disadvantages

- Advantages
  - no block synchronization between sender and receiver is required
  - bit errors caused by noisy channels only affect the corresponding block but not succeeding blocks
  - Block cipher operating can be parallelized
    - advantage for high-speed implementations
- Disadvantages
  - ECB encrypts highly deterministically
    - identical plaintexts result in identical ciphertexts
    - an attacker recognizes if the same message has been sent twice
    - plaintext blocks are encrypted independently of previous blocks
      - an attacker may reorder ciphertext blocks which results in valid plaintext

#### Substitution Attack on ECB

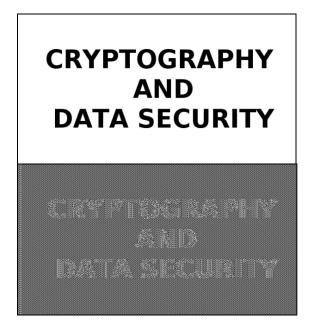
- Once a particular plaintext to ciphertext block mapping  $x_i \rightarrow y_i$  is known, a sequence of ciphertext blocks can easily be manipulated
- Suppose an electronic bank transfer

Block #	1	2	3	4	5
		Sending Account #		Receiving Account #	

- the encryption key between the two banks does not change too frequently
- The attacker sends \$1.00 transfers from his account at bank A to his account at bank B repeatedly
  - He can check for ciphertext blocks that repeat, and he stores blocks
     1,3 and 4 of these transfers
- He now simply replaces block 4 of other transfers with the block
   4 that he stored before
  - all transfers from some account of bank A to some account of bank B are redirected to go into the attacker's B account!

### ■ Example of encrypting bitmaps in ECB mode

Identical plaintexts are mapped to identical ciphertexts



Statistical properties in the plaintext are preserved in the ciphertext

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### Cipher Block Chaining mode (CBC)

- There are two main ideas behind the CBC mode:
  - The encryption of all blocks are "chained together"
    - ciphertext  $y_i$  depends not only on block  $x_i$  but on all previous plaintext blocks as well
  - The encryption is randomized by using an initialization vector (IV)

```
Encryption (first block): y_1 = e_k(x_1 \oplus IV)
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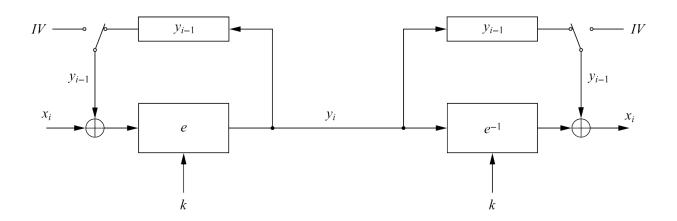
**Encryption** (general block):  $y_i = e_k(x_i \oplus y_{i-1}), i \ge 2$ 

**Decryption (first block)**:  $x_1 = e_k^{-1}(y_1) \oplus IV$ 

**Decryption (general block)**:  $x_i = e_k^{-1}(y_i) \oplus y_{i-1}, i \ge 2$ 

### Cipher Block Chaining mode (CBC)

- For the first plaintext block  $x_1$  there is no previous ciphertext
  - an IV is added to the first plaintext to make each CBC encryption nondeterministic
  - the first ciphertext  $y_1$  depends on plaintext  $x_1$  and the IV
- The second ciphertext  $y_2$  depends on the IV,  $x_1$  and  $x_2$
- The third ciphertext  $y_3$  depends on the IV and  $x_1$ ,  $x_2$  and  $x_3$ , and so on



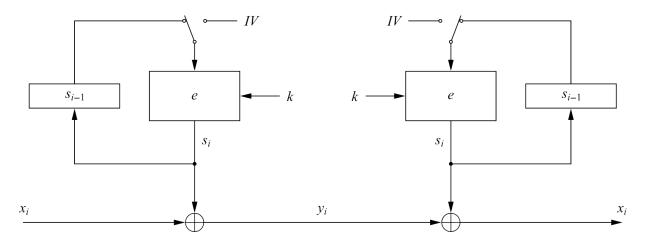
#### Substitution Attack on CBC

- Suppose the last example (electronic bank transfer)
- If the IV is properly chosen for every wire transfer, the attack will not work at all
- If the IV is kept the same for several transfers, the attacker would recognize the transfers from his account at bank A to back B
- If we choose a new IV every time we encrypt, the CBC mode becomes a probabilistic encryption scheme, i.e., two encryptions of the same plaintext look entirely different
- It is not needed to keep the IV secret!
- Typically, the IV should be a non-secret nonce (value used only once)

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### Output Feedback mode (OFB)

- It is used to build a synchronous stream cipher from a block cipher
- The key stream is not generated bitwise but instead in a blockwise fashion
- The output of the cipher gives us key stream bits  $S_i$  with which we can encrypt plaintext bits using the XOR operation



**Encryption (first block)**:  $s_1 = e_k(IV)$  and  $y_1 = s_1 \oplus x_1$ 

**Encryption (general block)**:  $s_i = e_k(s_{i-1})$  and  $y_i = s_i \oplus x_i$ ,  $i \ge 2$ 

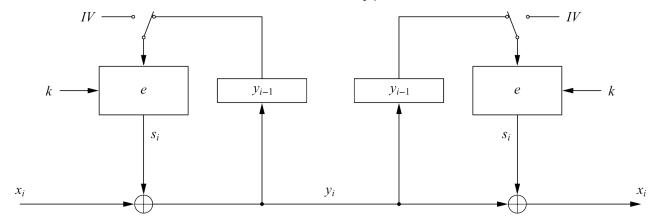
**Decryption (first block)**:  $s_1 = e_k(IV)$  and  $x_1 = s_1 \oplus y_1$ 

**Decryption (general block)**:  $s_i = e_k(s_{i-1})$  and  $x_i = s_i \oplus y_i$ ,  $i \ge 2$ 

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### Cipher Feedback mode (CFB)

- It uses a block cipher as a building block for an asynchronous stream cipher (similar to the OFB mode), more accurate name: "Ciphertext Feedback Mode"
- The key stream  $S_i$  is generated in a blockwise fashion and is also a function of the ciphertext
- As a result of the use of an IV, the CFB encryption is also nondeterministic



**Encryption (first block)**:  $y_1 = e_k(IV) \oplus x_1$ **Encryption (general block)**:  $y_i = e_k(y_{i-1}) \oplus x_i$ ,  $i \ge 2$ 

**Decryption (first block)**:  $x_1 = e_k(IV) \oplus y_1$ 

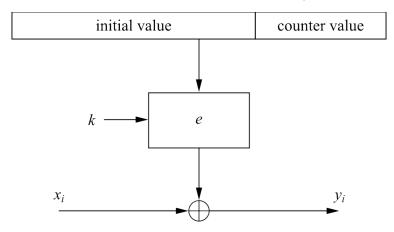
**Decryption (general block)**:  $x_i = e_k(y_{i-1}) \oplus y_i$ ,  $i \ge 2$ 

It can be used in situations where short plaintext blocks are to be encrypted

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### Counter mode (CTR)

- It uses a block cipher as a stream cipher (like the OFB and CFB modes)
- The key stream is computed in a blockwise fashion
- The input to the block cipher is a counter which assumes a different value every time the block cipher computes a new key stream block



- Unlike CFB and OFB modes, the CTR mode can be parallelized since the 2<sup>nd</sup> encryption can begin before the 1<sup>st</sup> one has finished
  - Desirable for high-speed implementations, e.g., in network routers

**Encryption**: 
$$y_i = e_k(\text{IV} || \text{CTR}_i) \oplus x_i, \quad i \ge 1$$
  
**Decryption**:  $x_i = e_k(\text{IV} || \text{CTR}_i) \oplus y_i, \quad i \ge 1$ 

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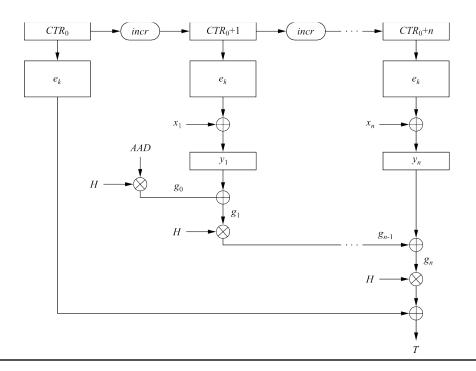
### ■ Galois Counter Mode (GCM)

- It also computes a message authentication code (MAC), i.e., a cryptographic checksum is computed for a message (for more information see Chapter 12 in Understanding Cryptography)
- By making use of GCM, two additional services are provided:
  - Message Authentication
    - the receiver can make sure that the message was really created by the original sender
  - Message Integrity
    - the receiver can make sure that nobody tampered with the ciphertext during transmission

### Galois Counter Mode (GCM)

- For encryption
  - An initial counter is derived from an IV and a serial number
  - The initial counter value is incremented then encrypted and XORed with the first plaintext block
  - For subsequent plaintexts, the counter is incremented and then encrypted
- For authentication
  - A chained Galois field multiplication is performed (for more information Galois field see Chapter 4.3 in *Understanding Cryptography*)
  - For every plaintext an intermediate authentication parameter  $g_i$  is derived
    - $g_i$  is computed as the XOR of the current ciphertext and the last  $g_{i-1}$ , and multiplied by the constant H
      - H is generated by encryption of the zero input with the block cipher
  - All multiplications are in the 128-bit Galois field  $GF(2^{128})$

#### Galois Counter Mode (GCM)



#### **Encryption**:

- a. Derive a counter value  $CTR_0$  from the IV and compute  $CTR_1 = CTR_0 + 1$
- b. Compute ciphertext:  $y_i = e_k(CTR_i) \oplus x_i$ ,  $i \ge 1$

#### Authentication:

- a. Generate authentication subkey  $H = e_k(0)$
- b. Compute  $g_0 = AAD \times H$  (Galois field multiplication)
- c. Compute  $g_i = (g_{i-1} \oplus y_i) \times H$ ,  $1 \le i \le n$  (Galois field multiplication)
- d. Final authentication tag:  $T = (g_n \times H) \oplus e_k(CTR_0)$

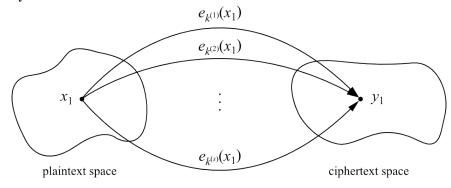
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#### Exhaustive Key Search Revisited

• A simple exhaustive search for a DES key knowing one pair  $(x_1,y_1)$ :

$$DES_k^{(i)}(x_1) \stackrel{?}{=} y_1, \quad i = 0, 1, \dots, 2^{56}-1$$

- However, for most other block ciphers a key search is somewhat more complicated
- A brute-force attack can produce false positive results
  - keys  $k_i$  that are found are not the one used for the encryption



- The likelihood of this is related to the relative size of the key space and the plaintext space
- A brute-force attack is still possible, but several pairs of plaintext—ciphertext are needed

### An Exhaustive Key Search Example

- Assume a cipher with a block width of 64 bit and a key size of 80 bit
- If we encrypt  $x_1$  under all possible  $2^{80}$  keys, we obtain  $2^{80}$  ciphertexts
  - However, there exist only 2<sup>64</sup> different ones
- If we run through all keys for a given plaintext–ciphertext pair, we find on average  $2^{80}/2^{64} = 2^{16}$  keys that perform the mapping  $e_k(x_1) = y_1$

Given a block cipher with a key length of k bits and block size of n bits, as well as t plaintext–ciphertext pairs  $(x_1, y_1), \ldots, (x_t, y_t)$ , the expected number of *false* keys which encrypt all plaintexts to the corresponding ciphertexts is:

$$2^{k-tn}$$

In this example assuming two plaintext-ciphertext pairs, the likelihood is

$$2^{80-2.64}=2^{-48}$$

 for almost all practical purposes two plaintext-ciphertext pairs are sufficient

- Encryption with Block Ciphers: Modes of Operation
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  - Double Encryption and Meet-in-the-Middle Attack
  - Triple Encryption
  - Key Whitening

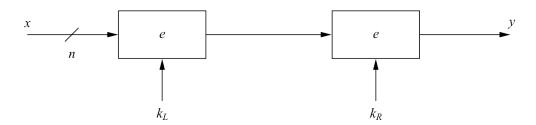
### Increasing the Security of Block Ciphers

- In some situations we wish to increase the security of block ciphers, e.g., if a cipher such as DES is available in hardware or software for legacy reasons in a given application
- Two approaches are possible
  - Multiple encryption
    - theoretically much more secure, but sometimes in practice increases the security very little
  - Key whitening

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#### Double Encryption

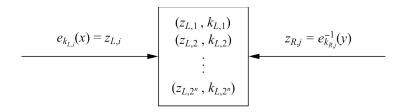
• A plaintext x is first encrypted with a key  $k_L$ , and the resulting ciphertext is encrypted again using a second key  $k_R$ 



• Assuming a key length of k bits, an exhaustive key search would require  $2^{k} \cdot 2^{k} = 2^{2k}$  encryptions or decryptions

#### Meet-in-the-Middle Attack

• A Meet-in-the-Middle attack requires  $2^{k}+2^{k}=2^{k+1}$  operations!



- **Phase I**: for the given  $(x_1, y_1)$  the **left** encryption is brute-forced for all  $k_{L,i}$ ,  $i=1,2,...,2^k$  and a lookup table with  $2^k$  entry (each n+k bits wide) is computed
  - the lookup table should be ordered by the result of the encryption  $(z_{L,i})$
- **Phase II**: the **right** encryption is brute-forced (using decryption) and for each  $z_{R,i}$  it is checked whether  $z_{R,i}$  is equal to any  $z_{L,i}$  value in the table of the first phase
- Computational Complexity
  number of encryptions and decryptions =  $2^k + 2^k = 2^{k+1}$ number of storage locations =  $2^k$
- Double encryption is not much more secure then single encryption!

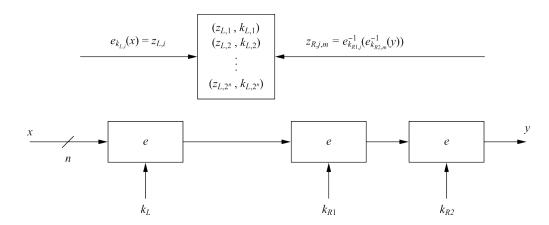
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### Triple Encryption

- The encryption of a block three times  $y = e_{k3} (e_{k2} (e_{k1} (x)))$
- In practice a variant scheme is often used EDE (encryption-decryption-encryption)

$$y = e_{k3} (e^{-1}_{k2} (e_{k1} (x)))$$

- Advantage: choosing k1=k2=k3 performs single DES encryption
- Still we can perform a meet-in-the middle attack, and it reduces the *effective key* length of triple encryption from 3K to 2K!
  - The attacker must run 2<sup>112</sup> tests in the case of 3DES

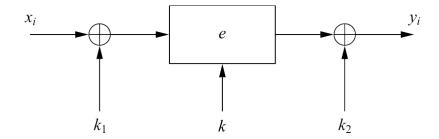


Triple encryption effectively doubles the key length

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### Key Whitening

- Makes block ciphers such as DES much more resistant against brute-force attacks
- In addition to the regular cipher key k, two whitening keys  $k_1$  and  $k_2$  are used to XOR-mask the plaintext and ciphertext



- It does not strengthen block ciphers against most analytical attacks such as linear and differential cryptanalysis
- It is not a "cure" for inherently weak ciphers
- The additional computational load is negligible
- Its main application is ciphers that are relatively strong against analytical attacks but possess too short a key space especially DES
  - a variant of DES which uses key whitening is called DESX

#### Lessons Learned

- There are many different ways to encrypt with a block cipher. Each mode of operation has some advantages and disadvantages
- Several modes turn a block cipher into a stream cipher
- There are modes that perform encryption together together with authentication, i.e., a cryptographic checksum protects against message manipulation
- The straightforward ECB mode has security weaknesses, independent of the underlying block cipher
- The counter mode allows parallelization of encryption and is thus suited for high speed implementations
- Double encryption with a given block cipher only marginally improves the resistance against brute-force attacks
- Triple encryption with a given block cipher roughly doubles the key length
- Triple DES (3DES) has an effective key length of 112 bits
- Key whitening enlarges the DES key length without much computational overhead.