

Giovanna Santana Pennisi - CTII 350

Lista de Exercícios - Aula 11

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1 - $(1 + 2x^2)^6$ / Coeficiente de $x^8 = ?$

↳ Linha 6: $\binom{6}{k} \cdot 1^{6-k} \cdot (2x^2)^k$

$\binom{6}{k} \cdot 1^{6-k} \cdot 2^k \cdot x^{2k}$

$2k = 8$
 $k = \frac{8}{2}$
 $k = 4$

$\binom{6}{4} \cdot 1^{6-4} \cdot 2^4 \cdot x^{2 \cdot 4}$

$\frac{6!}{4!(6-4)!} \cdot 1^2 \cdot 16 \cdot x^8$

Alternativa C $\textcircled{240} x^8$

$\frac{6 \cdot 5 \cdot 4!}{4! \cdot 2 \cdot 1} \cdot 16 x^8$
 $15 \cdot 16 x^8$
 $\textcircled{240} x^8$

2 - $(14x - 13y)^{237}$ / Soma de todos coeficientes = ? / $x=1$ / $y=1$

↳ $(14 - 13)^{237} \rightarrow 1^{237} \rightarrow \textcircled{1}$ Alternativa B.

$$3 - (x+a)^{11} / 1386 x^5 / a = ?$$

$$\hookrightarrow \text{linha 11: } \binom{11}{k} \cdot x^{11-k} \cdot a^k$$

$$11 - k = 5$$

$$k = 11 - 5$$

$$k = 6$$

$$\binom{11}{6} \cdot x^{11-6} \cdot a^6 = 1386 x^5$$

$$462 a^6 = 1386$$

$$a^6 = \frac{1386}{462}$$

$$a^6 = 3$$

$$a = \sqrt[6]{3}$$

Alternativa A.

$$\frac{11!}{6! (11-6)!} \cdot x^5 \cdot a^6 = 1386 x^5$$

$$\frac{11 \cdot 10 \cdot 9 \cdot 8 \cdot 7 \cdot 6!}{6! \cdot 5 \cdot 4 \cdot 3 \cdot 2 \cdot 1} \cdot x^5 \cdot a^6 = 1386 x^5$$

$$4 - \left(\frac{x+1}{x^2} \right)^9 / \text{termo independente} = ? \quad (x^0)$$

$$\hookrightarrow (x + x^{-2})^9$$

$$\binom{9}{0} x^{9-0} \cdot (x^{-2})^0 + \binom{9}{1} x^{9-1} \cdot (x^{-2})^1 + \binom{9}{2} x^{9-2} \cdot (x^{-2})^2 + \binom{9}{3} x^{9-3} \cdot (x^{-2})^3 + \dots$$

$$\binom{9}{0} x^9 \cdot x^0 + \binom{9}{1} x^8 \cdot x^{-2} + \binom{9}{2} x^7 \cdot x^{-4} + \binom{9}{3} x^6 \cdot x^{-6} + \dots$$

$$\binom{9}{0} x^9 + \binom{9}{1} x^6 + \binom{9}{2} x^3 + \binom{9}{3} x^0 \quad \text{termo independente } (x^0)$$

\hookrightarrow Alternativa D $\binom{9}{3}$

$$5 - \left(x + \frac{1}{x^2}\right)^n \quad / \quad n = ? \quad / \quad \text{tem termo independente}$$

$$(x + x^{-2})^n$$

Termo independente (x^0)

$$+ \text{linha } n: \binom{n}{k} \cdot x^{n-k} \cdot (x^{-2})^k$$

$$\binom{n}{k} \cdot x^{n-k} \cdot x^{-2k}$$

$$n - k - 2k = 0$$

$$n - 3k = 0$$

$$n = 3k$$

$$k = \frac{n}{3}$$

Como k , um número natural, é igual a n dividido por 3, logo podemos concluir que n é divisível por 3. → Alternativa C

Se n é divisível por 3.

$$6 - k = \left(3x^3 + \frac{2}{x^2}\right)^5 - \left(243x^{15} + 810x^{10} + 1080x^5 + 240 + \frac{32}{x^5}\right)$$

$$(3x^3 + 2x^{-2})^5 = \binom{5}{0} (3x^3)^5 (2x^{-2})^0 + \binom{5}{1} (3x^3)^4 (2x^{-2})^1 + \binom{5}{2} (3x^3)^3 (2x^{-2})^2 + \binom{5}{3} (3x^3)^2 (2x^{-2})^3 + \binom{5}{4} (3x^3)^1 (2x^{-2})^4 + \binom{5}{5} (3x^3)^0 (2x^{-2})^5$$

$$= 243x^{15} + 810x^{10} + 1080x^5 + 240 + \frac{240}{x^5} + \frac{32}{x^{10}}$$

$$+ 720 + \frac{240}{x^5} + \frac{32}{x^{10}}$$

$$k = 243x^{15} + 810x^{10} + 1080x^5 + 720 + \frac{240}{x^5} + \frac{32}{x^{10}} - \left(243x^{15} + 810x^{10} + 1080x^5 + 240 + \frac{240}{x^5} + \frac{32}{x^{10}}\right)$$

$$k = \cancel{243x^{15}} + \cancel{810x^{10}} + \cancel{1080x^5} + 720 + \frac{240}{x^5} + \frac{32}{x^{10}} - \cancel{243x^{15}} - \cancel{810x^{10}} - \cancel{1080x^5} - \frac{240}{x^5} - \frac{32}{x^{10}}$$

$$k = 720 \rightarrow \text{Alternativa E}$$

7- $(2x + y)^5$ / Soma coeficientes = ?

$x=1 / y=1$

$(2+1)^5 = 3^5 = 243$ Alternativa C