## BF

The brainfuck language uses a simple machine model consisting of the program and instruction pointer, as well as an array of at least 30,000 byte cells initialized to zero; a movable data pointer (initialized to point to the leftmost byte of the array); and two streams of bytes for input and output (most often connected to a keyboard and a monitor respectively, and using the ASCII character encoding).

## MODULE BF-SYNTAX

The syntax of the language consists in eight commands: ><+-., []

 $SYNTAX \quad \textit{Ignore} ::= [onlyLabel(onlyLabel()), regex(regex([^\b\\\]+\\])]$ 

SYNTAX Instruction ::= > , [onlyLabel( onlyLabel())] [Instructions] Ignore

A Brainfuck program consists in a list of commands. Brainfuck ignores all characters except the eight commands +-<>[],. so no special syntax for comments is needed. Unfortunately, because of K parsing issues, we assume that programs contain only the language instructions.

SYNTAX  $Instructions ::= List\{Instruction, ````\}$ 

END MODULE

MODULE BF

The configuration of the language contains the K cell for Brainfuck programs, an array cell containing the byte array, a cell ptr for the instruction pointer and I/O streams.

CONFIGURATION:

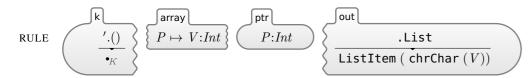


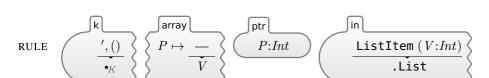
Unroll intructions into KList.

 ${\tt RULE} \quad I{:}Instruction \ Is{:}Instructions$ 

 $RULE \quad \bullet_{Instructions}$ 

Output the byte at the data pointer.

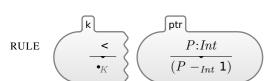




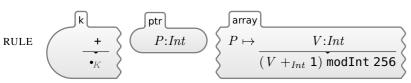
Increment the data pointer.

RULE 
$$\left\langle \begin{array}{c} k \\ \hline \\ \bullet_{K} \end{array} \right\rangle \left\langle \begin{array}{c} P:Int \\ \hline (P+I_{Int} \ 1) \end{array} \right\rangle$$

Decrement the data pointer.



Increment the byte at the data pointer



## Decrement the byte at the data pointer

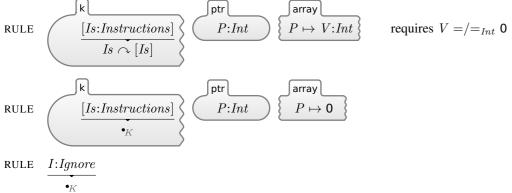
RULE 
$$\left\{\begin{array}{c} k \\ \hline \\ \bullet_{K} \end{array}\right\}$$
  $\left\{\begin{array}{c} P:Int \\ P:Int \end{array}\right\}$   $\left\{\begin{array}{c} P\mapsto V:Int \\ \hline (V-_{Int}\ 1)\ \mathsf{modInt}\ 256 \end{array}\right\}$ 

array

 $M{:}Map$  .Map

 $I\mapsto 0$ 

Brainfuck jumps ('[' and ']') are considered to be loops. Whenever the byte at the data pointer is not zero, execute the loops instructions.



[ptr]

 $\text{requires} \lnot_{Bool}(I \text{ in keys } (M)) \land_{Bool} (I \ge_{Int} \mathbf{0})$ 

[structural( structural())]