

# Queues

1

## The Queue ADT

- The Queue ADT stores arbitrary objects
- Insertions and deletions follow the first-in first-out scheme
- Insertions are at the rear of the queue and removals are at the front of the queue
- Main queue operations:
  - `enqueue(object)`: inserts an element at the end of the queue
  - `object dequeue()`: removes and returns the element at the front of the queue
- Auxiliary queue operations:
  - `object first()`: returns the element at the front without removing it
  - `integer size()`: returns the number of elements stored
  - `boolean isEmpty()`: indicates whether no elements are stored
- Boundary cases:
  - Attempting the execution of `dequeue` or `first` on an empty queue returns `null`

2

## Example

Operation		Output	Q
enqueue(5)	–	(5)	
enqueue(3)	–	(5, 3)	
dequeue()	5	(3)	
enqueue(7)	–	(3, 7)	
dequeue()	3	(7)	
first()	7	(7)	
dequeue()	7	()	
dequeue()	null	()	
isEmpty()	true	()	
enqueue(9)	–	(9)	
enqueue(7)	–	(9, 7)	
size()	2	(9, 7)	
enqueue(3)	–	(9, 7, 3)	
enqueue(5)	–	(9, 7, 3, 5)	
dequeue()	9	(7, 3, 5)	

3

## Applications of Queues

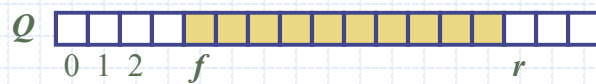
- Direct applications
  - Waiting lists, bureaucracy
  - Access to shared resources (e.g., printer)
  - Multiprogramming
- Indirect applications
  - Auxiliary data structure for algorithms
  - Component of other data structures

4

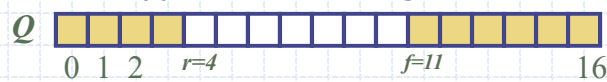
## Array-based Queue

- Use an array of size  $N$  in a circular fashion
- Two variables keep track of the front and size
  - $f$  index of the front element
  - $sz$  number of stored elements
- When the queue has fewer than  $N$  elements, array location  $r = (f + sz) \bmod N$  is the first empty slot past the rear of the queue

normal configuration



wrapped-around configuration



5

## Queue Operations

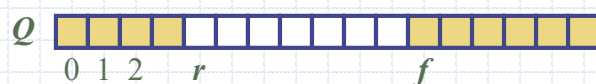
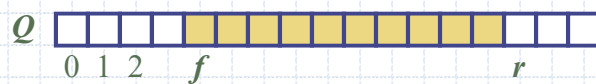
- We use the modulo operator (remainder of division)

Algorithm **size()**

return  $sz$

Algorithm **isEmpty()**

return  $(sz == 0)$



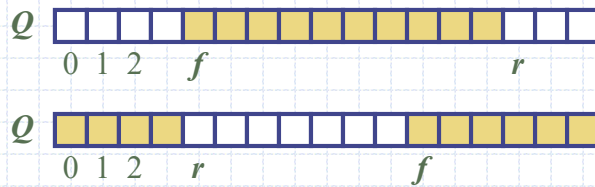
6

## Queue Operations (cont.)

- Operation **enqueue** throws an exception if the array is full
- This exception is implementation-dependent

```

Algorithm enqueue(o)
if size() = N then
    throw IllegalStateException
else
     $r \leftarrow (f + sz) \bmod N$ 
     $Q[r] \leftarrow o$ 
     $sz \leftarrow (sz + 1)$ 
    
```



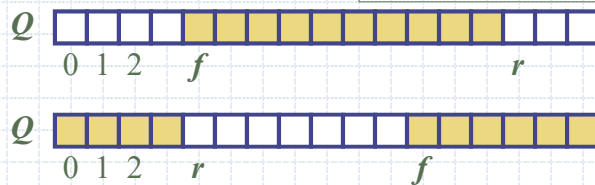
7

## Queue Operations (cont.)

- Note that operation **dequeue** returns null if the queue is empty

```

Algorithm dequeue()
if isEmpty() then
    return null
else
     $o \leftarrow Q[f]$ 
     $f \leftarrow (f + 1) \bmod N$ 
     $sz \leftarrow (sz - 1)$ 
    return o
    
```



8

## Queue Interface in Java

- Java interface corresponding to our Queue ADT
- Assumes that `first()` and `dequeue()` return null if queue is empty

```
public interface Queue<E> {  
    int size();  
    boolean isEmpty();  
    E first();  
    void enqueue(E e);  
    E dequeue();  
}
```

9

## Array-based Implementation

```
1  /** Implementation of the queue ADT using a fixed-length array. */  
2  public class ArrayQueue<E> implements Queue<E> {  
3      // instance variables  
4      private E[] data;           // generic array used for storage  
5      private int f = 0;          // index of the front element  
6      private int sz = 0;         // current number of elements  
7  
8      // constructors  
9      public ArrayQueue() {this(CAPACITY);} // constructs queue with default capacity  
10     public ArrayQueue(int capacity) {      // constructs queue with given capacity  
11         data = (E[]) new Object[capacity]; // safe cast; compiler may give warning  
12     }  
13  
14     // methods  
15     /** Returns the number of elements in the queue. */  
16     public int size() { return sz; }  
17  
18     /** Tests whether the queue is empty. */  
19     public boolean isEmpty() { return (sz == 0); }  
20 }
```

10

## Array-based Implementation (2)

```
21  /** Inserts an element at the rear of the queue. */
22  public void enqueue(E e) throws IllegalStateException {
23      if (sz == data.length) throw new IllegalStateException("Queue is full");
24      int avail = (f + sz) % data.length; // use modular arithmetic
25      data[avail] = e;
26      sz++;
27  }
28
29  /** Returns, but does not remove, the first element of the queue (null if empty). */
30  public E first() {
31      if (isEmpty()) return null;
32      return data[f];
33  }
34
35  /** Removes and returns the first element of the queue (null if empty). */
36  public E dequeue() {
37      if (isEmpty()) return null;
38      E answer = data[f];
39      data[f] = null; // dereference to help garbage collection
40      f = (f + 1) % data.length;
41      sz--;
42      return answer;
43  }
```

Se siamo in fondo devo tornare all'inizio

11

## Linked\_List-based Queue in Java

```
public class LinkedListQueue<E> implements Queue<E> {
    private SinglyLinkedList<E> list = new SinglyLinkedList<>();
    /** Constructs an initially empty queue. */
    public LinkedListQueue() {}
    public int size() { return list.size(); }
    public boolean isEmpty() { return list.isEmpty(); }
    public void enqueue(E element) { list.addLast(element); }
    public E first() { return list.first(); }
    public E dequeue() { return list.removeFirst(); }
}
```

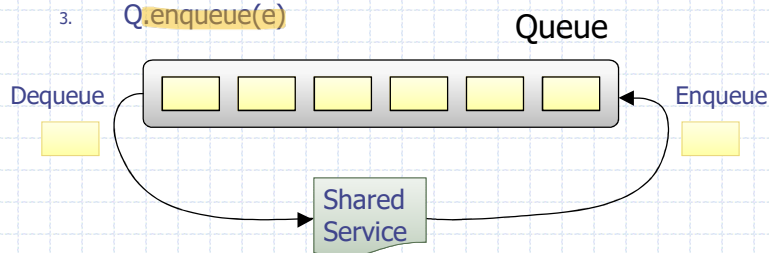
12



## Application: Round Robin Schedulers

- We can implement a round robin scheduler using a queue *Q* by repeatedly performing the following steps:

1. *e* = *Q.dequeue()*
2. Service element *e*
3. *Q.enqueue(e)*



13

## Deque Interface in Java

```
public interface Deque<E> {  
    /**  
     * Returns the number of elements in the deque.  
     * @return number of elements in the deque  
     */  
    int size();  
    /**  
     * Tests whether the deque is empty.  
     * @return true if the deque is empty, false otherwise  
     */  
    boolean isEmpty();  
    /**  
     * Returns (but does not remove) the first element of the deque.  
     * @return first element of the deque (or null if empty)  
     */  
    E first();  
    /**  
     * Returns (but does not remove) the last element of the deque.  
     * @return last element of the deque (or null if empty)  
     */  
    E last();  
    /**  
     * Inserts an element at the front of the deque.  
     * @param e the new element  
     */  
    void addFirst(E e);  
    /**  
     * Inserts an element at the back of the deque.  
     * @param e the new element  
     */  
    void addLast(E e);  
    /**  
     * Removes and returns the first element of the deque.  
     * @return element removed (or null if empty)  
     */  
    E removeFirst();  
    /**  
     * Removes and returns the last element of the deque.  
     * @return element removed (or null if empty)  
     */  
    E removeLast();  
}
```

14

# Deque implementation

```
public class DoublyLinkedList<E> implements Deque<E> {
```

Nothing to add!!!!

```
}
```