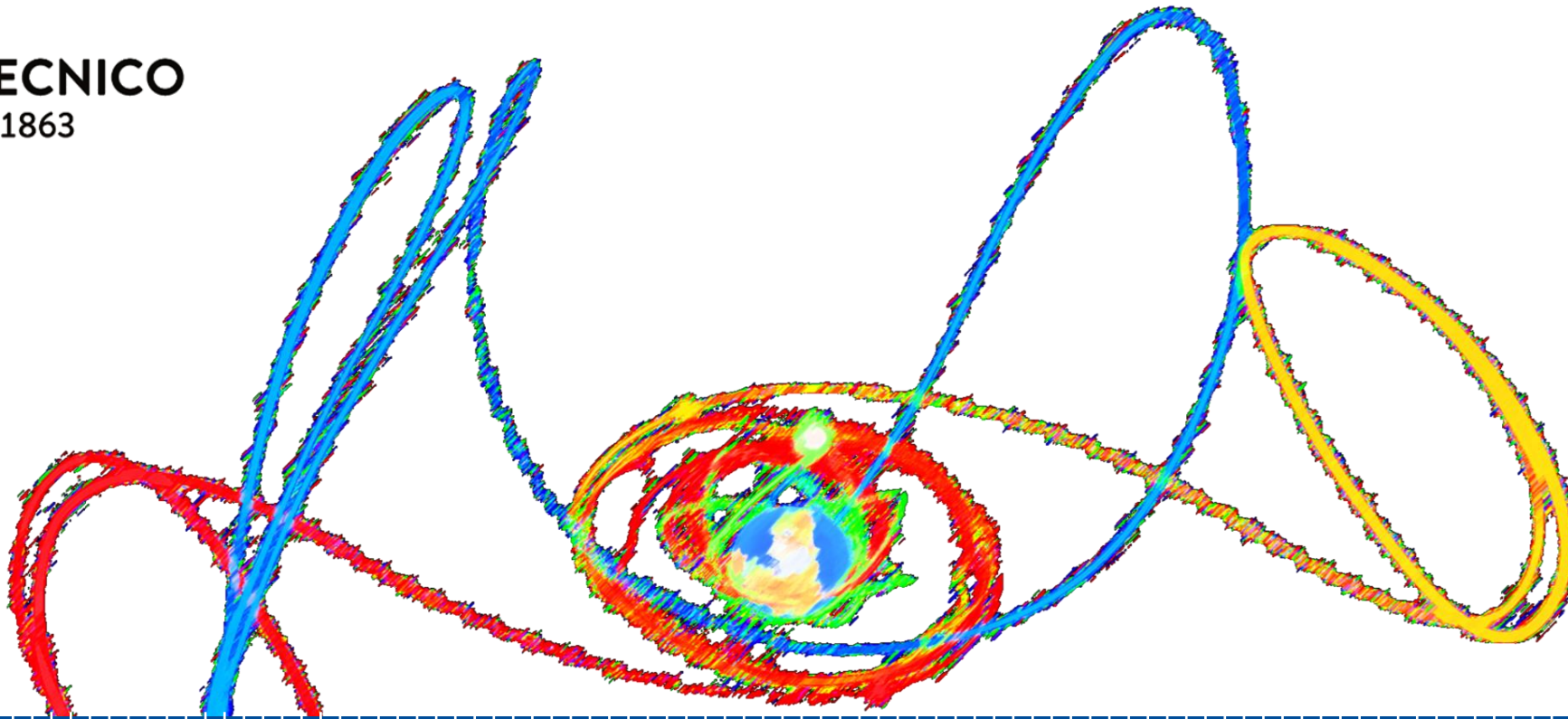




POLITECNICO
MILANO 1863



POLITECNICO
MILANO 1863



Orbital Mechanics

Module 0: Introduction & MATLAB fundamentals

Juan Luis GONZALO GOMEZ, Lorenzo GIUDICI, Camilla COLOMBO

Department of Aerospace Science and Technology, Politecnico di Milano

Academic year 2021/22

Introduction & MATLAB fundamentals

■ Project lab introduction

- Teaching staff
- Lab groups
- Project
- Past year students

■ MATLAB fundamentals

- MATLAB learning resources
- Code structuring
- Best coding practices
- Figures

Contacts

■ Camilla **Colombo**

- Email: camilla.colombo@polimi.it
- Meeting time: please arrange via email
- Tel: 8352

■ Juan Luis **Gonzalo Gomez**

- Email: juanluis.gonzalo@polimi.it
- Meeting time: please arrange via email
- Tel: 8401

■ Lorenzo **Giudici**

- Email: lorenzo1.giudici@polimi.it
- Meeting time: please arrange via email
- Tel: 8401

Teaching staff

Lorenzo Giudici



2018: BEng, Politecnico di Milano, Mechanical Engineering



2020: MEng, Politecnico di Milano, Space engineering



2021-present: PhD Candidate, Politecnico di Milano

- Extension of a debris population model based on the density of orbiting objects in the phase space of Keplerian elements, through an analogy with fluid dynamics.

Teaching staff

Juan Luis Gonzalo



Ingeniero Aeronáutico (equiv. to a laurea quinquennale in Aerospace Engineering),
Universidad Politécnica de Madrid



M.Sc. in Aerospace Engineering, Universidad Politécnica de Madrid



Ph.D. in Aerospace Engineering, Universidad Politécnica de Madrid

- Propagation and optimal control of space trajectories using perturbation methods



Visiting Ph.D. student at PoliMi, Department of Aerospace Science and technology

- Indirect optimization methods, applications to end-of-life de-orbiting



Postdoctoral research fellow at Politecnico di Milano, Department of Aerospace
Science and Technology

- Space Situational Awareness, asteroid orbit manipulation

Rules

- The lab project will be carried out in **teams**, with the following **rules**:
 - Each team should have **4 members**.
 - To promote diversity, each team **must** include at least one student who did not study the bachelor's degree at PoliMi.
 - **You can register your team using the activity available in WeBeep (section “Project lab”).**
 - The teams could be the same for the course of Spacecraft Attitude Dynamics.
- Also, please consider the following **recommendations**:
 - **Passing the assignment is a prerequisite to attend the final exam.** If you do not intend to do the assignment now, avoid teaming up with people that do.
 - **This is a team effort.** You can distribute the tasks, but everybody is responsible for the final result. At the oral presentation, **any member can be questioned about any part of the work.**

Teamwork

As in a **Mission Analysis team** at **ESA**, you will also work in a group:

- Members of the group must **cooperate**: you are advised to distribute the work among the team, but **everyone is responsible for all the work done in the project**.
- Make decisions towards design solutions based on numerical/analytical/physical evidence and analyses: you must always be able to **motivate your design choices**. *You are supposed to perform the preliminary mission analysis of a real mission.*
- During the final review (oral presentation), **any team member can be questioned about any part of the work**.

Contents

- The **project** consists of **2 assignments** based on the computer lab
 - Fly-by explorer mission
 - Planetary explorer mission
- Project evaluation includes **2 parts**:
 - **Deliverables** (1 submission per group)
 - **Project report**: A single PDF report on the assignments, of maximum 20 pages
 - **Presentation slides**
 - **Simulation codes and results**
 - **Oral presentation (final review)**
 - 15 minutes followed by questions about the assignments and the theory of the course
 - All team members must participate in the oral presentation
 - Any student can be questioned about any part of the work

Submission and deadlines

- The deliverables must be submitted through **WeBeep**
 - Submit a **single ZIP file** with all the deliverables (report, slides, and code), named "OrbitalMech_aaaaaaaa_group_nn.zip", where aaaaaaaaa is the academic year and nn the group number (e.g., OrbitalMech_20212022_group_42.zip).
 - Submission via email will not be considered.
 - **Changes to the deliverables after the deadline will not be considered.**
- Deadlines:
 - **Deliverables must be submitted by 7 January 2022.**
 - Delivering the project is a must condition for the oral presentation and attending the written exam.
 - **Oral presentation**
 - Dates will be available during the Winter, Summer and September exam sessions. They will be notified prior to each exam session.
 - Presentation to be done before or within the same exam session (winter/summer/autumn) when the written is done.

- **Single PDF of maximum 20 pages for both assignments.**
- Include a **front page** with:
 - Title,
 - Group number, academic year,
 - For each member: full name, matriculation number, and person code.
- The report should contain **explanations, data, figures, and tables supporting your design process and final solution.**
 - You may follow the structure from the lab slides.
 - **Properly indicate the units of all numerical data.**
 - **Include labels, legends and titles/captions in all figures.**
 - There is no need to include theory, but properly introduce/reference all the formulas and models you use.
 - Include a 'references' section with a list of all the sources you consulted, and cite them in the text where appropriate.
 - Properly credit all images taken from other sources.

- The submission must include **two different folders** with the codes of each assignment:
 - **Assignment 1:** Folder named **Assignment1** containing:
 - **PlanetaryMission_group_N.m**: main script that reproduces your result.
 - **Assignment1\functions**: subfolder with **all the other functions you developed**.
 - **Assignment 2:** Folder named **Assignment2** containing:
 - **InterplanetaryMission_group_N.m** : main script that reproduces your results.
 - **Assignment2\functions**: subfolder with **all the other functions you developed**.
- No need to upload the functions we provide to you in WeBeep, unless you modified them.

Code headers

- Each code file must include a **header** detailing:
 - Inputs and outputs (specify dimensions and units),
 - Authors,
 - Basic usage information

```
function dy = ode_2bp( t, y, muP )
%ode_2bp ODE system for the two-body problem (Keplerian motion)
%
% PROTOTYPE:
%   dy = ode_2bp( t, y, mu )
%
% INPUT:
%   t[1]           Time (can be omitted, as the system is autonomous) [T]
%   y[6x1]         Cartesian state of the body ( rx, ry, rz, vx, vy, vz ) [ L, L/T ]
%   muP[1]         Gravitational parameter of the primary [L^3/T^2]
%
% OUTPUT:
%   dy[6x1]        Derivative of the state [ L/T^2, L/T^3 ]
%
% CONTRIBUTORS:
%   Student 1
%   Student 2
%
% VERSIONS
%   2020-11-19: First version
%
```

Auxiliar functions available in Beep

- For the assignments, you may use the auxiliar MATLAB functions **available in WeBeep**:
 - `astroConstants`: Use it to retrieve common astrodynamic constants (both assignments).
 - `lambertMR`: Use it for solving each Lambert arc (Assignment 1).
 - `uplanet`: Planets' ephemeris (**don't propagate the planets' orbits yourself**).
 - `ephMoon`: Analytical ephemeris of the Moon.
 - `ephNEO`: Ephemerides of several Near-Earth Objects.
 - **timeConversion.zip**: Compressed folder with several time conversion routines

- Project marks of past years are valid if you:
 - presented a report,
 - performed an oral presentation, and
 - received a mark for the assignments.

- Past students who do not fulfil these 3 conditions (incomplete assignments) can either:
 1. Join a group and start the project anew this academic year.
 2. Complete their project from past year and deliver it with the same rules presented before. If several past students of the same project group want to follow this option, they have to maintain the group



POLITECNICO
MILANO 1863

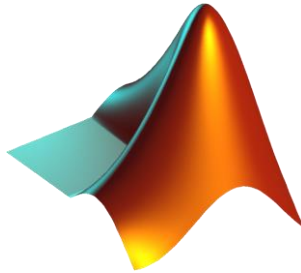


POLITECNICO
MILANO 1863

MATLAB FUNDAMENTALS

Before we begin...

- We will use **MATLAB** for the lab classes
 - You need to know the basics to follow the lab!






- PoliMi has a **Campus License**, giving access to the software and many resources:

<https://www.software.polimi.it/mathworks-matlab/>

Servizi ICT di Ateneo


Servizi Online





ICT SERVICES
SOFTWARE

All software from A to ZTeaching staffStudentPhDTechnical and administrative staffContacts

Mathworks Matlab

Teachings adopting this software

Availability in classroom

Accessible on Virtual Desktop





Mathworks Matlab

Matlab is an interactive language and environment for numerical computation, data analysis and visualization, and programming. It allows you to analyze data, develop algorithms, create models and applications.


- Operating system: Windows, Linux, macOS
- [System requirements](#)

How to get the software

Licenses, recipients, request and download methods

 Teaching staff
 Students
 PhD students
 Technical and administrative staff

Tags: [Analysis](#), [Computation](#)



Educational licenses

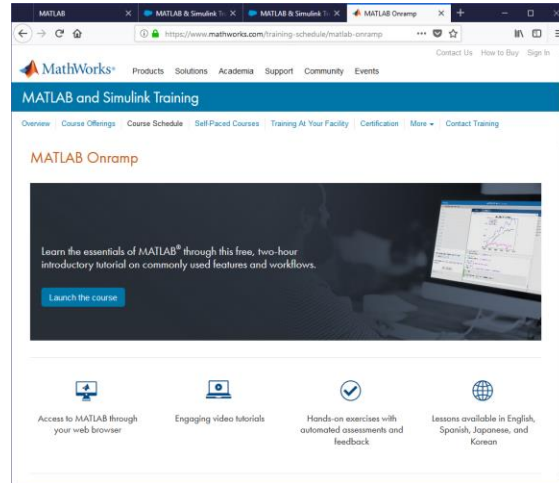
The licenses are "educational" editions, the use of the application packages is strictly limited to the University's institutional activities, thus excluding any use for personal, professional purposes and for profit.

[Help us improve this page](#)

© Copyright - [University software service](#) - [Enfold Theme by Kriesi](#)

MATLAB learning resources

Mathworks online courses



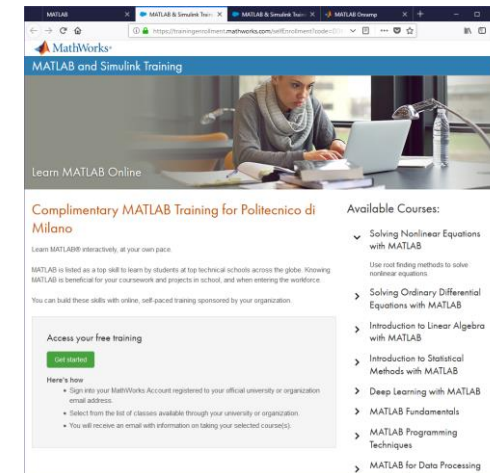
For those with little or no MATLAB experience, it is **strongly recommended** to follow the **MATLAB Onramp** online course (approx. 2 hours)

<https://www.mathworks.com/training-schedule/matlab-onramp>



Visit the courses in MATLAB Academy (included in the Campus license) to improve your MATLAB competencies

<https://trainingenrollment.mathworks.com/selfEnrollment?code=D3M4TB3KDGIC>



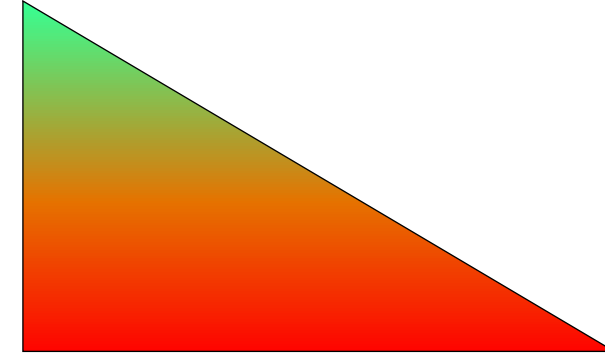
MATLAB learning resources

MATLAB functions: too many things to remember

MATLAB has:

- **Thousands** of included functions and toolsets
 - Most of them with multiple inputs and outputs
 - To be provided in a given way (can affect behaviour)
 - Many are optional, with pre-set default values

Effort to remember it all:



Impossible to remember/know them all!

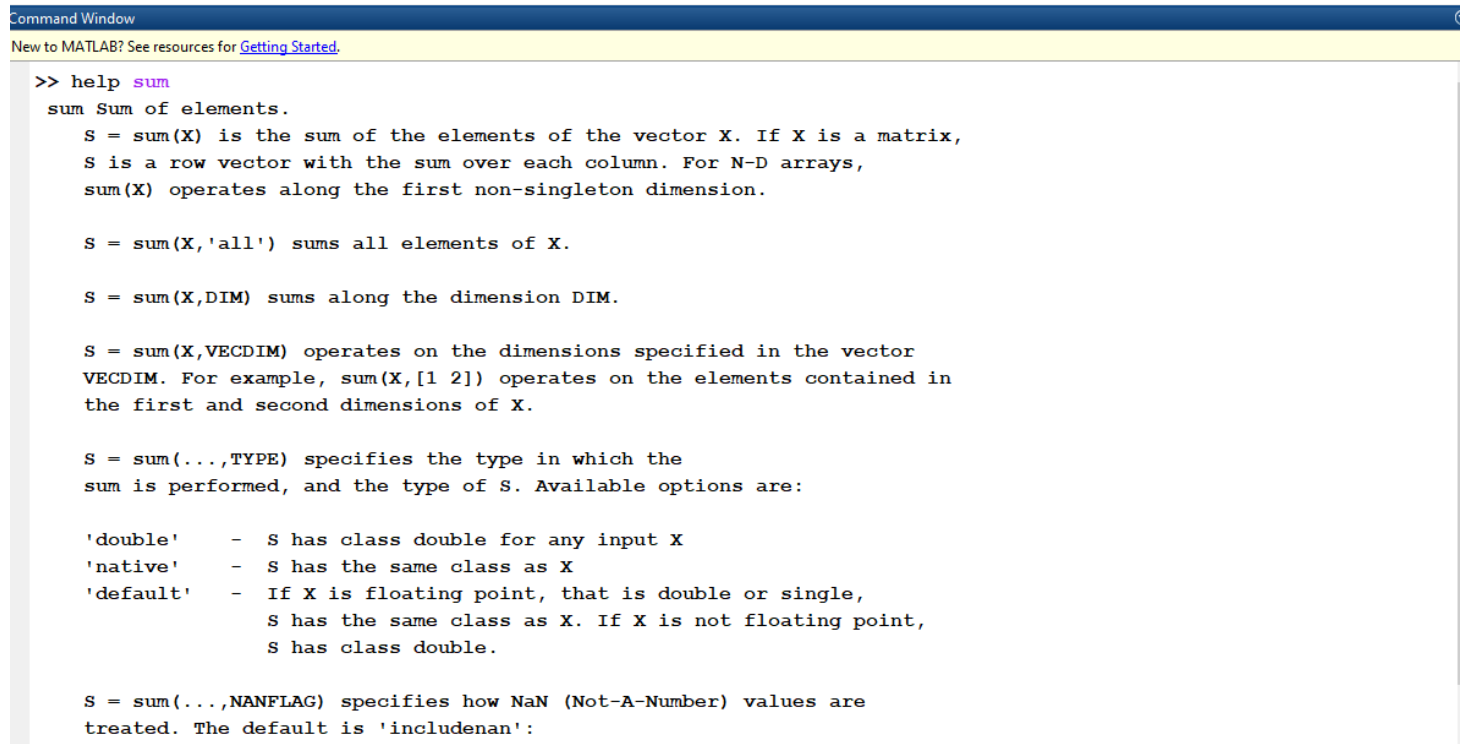


But it is easy remembering to check MATLAB's documentation (even the pros use it)

MATLAB's help command

MATLAB's `help` command is run from the command window, and provides usage information about a given function:

```
>> help name_of_function
```



```
Command Window
New to MATLAB? See resources for Getting Started.

>> help sum
sum Sum of elements.
  S = sum(X) is the sum of the elements of the vector X. If X is a matrix,
  S is a row vector with the sum over each column. For N-D arrays,
  sum(X) operates along the first non-singleton dimension.

  S = sum(X,'all') sums all elements of X.

  S = sum(X,DIM) sums along the dimension DIM.

  S = sum(X,VECDIM) operates on the dimensions specified in the vector
  VECDIM. For example, sum(X,[1 2]) operates on the elements contained in
  the first and second dimensions of X.

  S = sum(...,TYPE) specifies the type in which the
  sum is performed, and the type of S. Available options are:

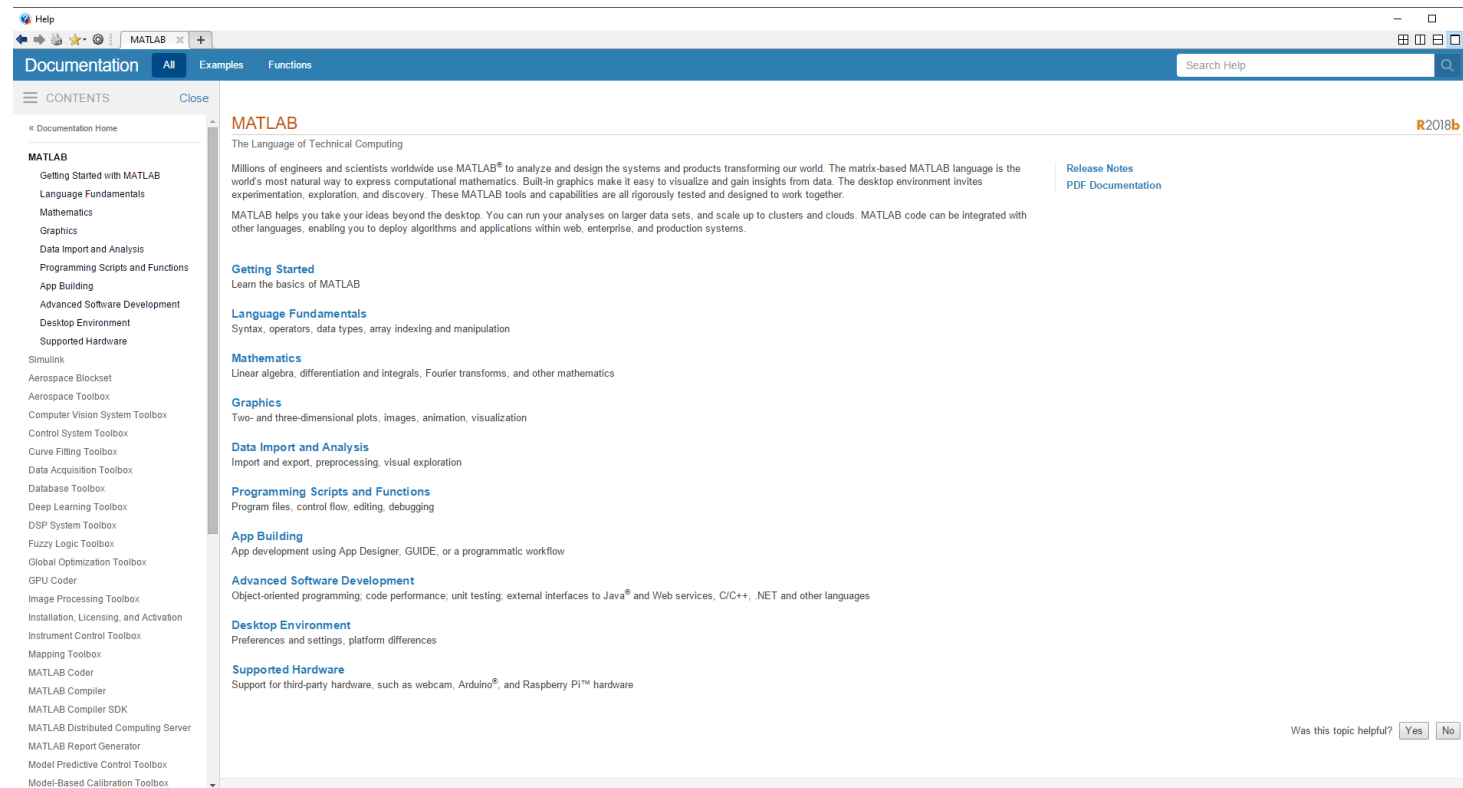
  'double' - S has class double for any input X
  'native' - S has the same class as X
  'default' - If X is floating point, that is double or single,
              S has the same class as X. If X is not floating point,
              S has class double.

  S = sum(...,NANFLAG) specifies how NaN (Not-A-Number) values are
  treated. The default is 'includenan':
```

MATLAB learning resources

MATLAB documentation center

- The **documentation center** provides:
 - **Detailed information on functions** (usage, inputs/outputs, examples, etc.)
 - **General and specific information about how to use MATLAB**
 - **Practical examples and tutorials**

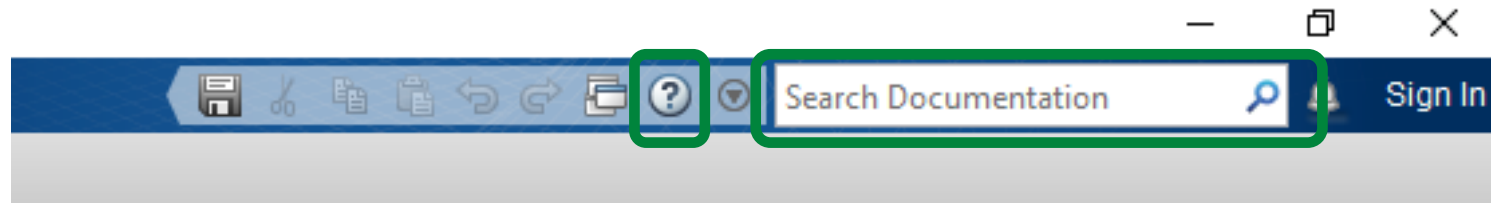


MATLAB documentation center

- You can access the **documentation center** in several ways:
 - Running command `doc` from the command window
 - If you use command `doc name_of_function`, you will go directly to the documentation page for that function

```
>> doc  
>> doc name_of_function
```

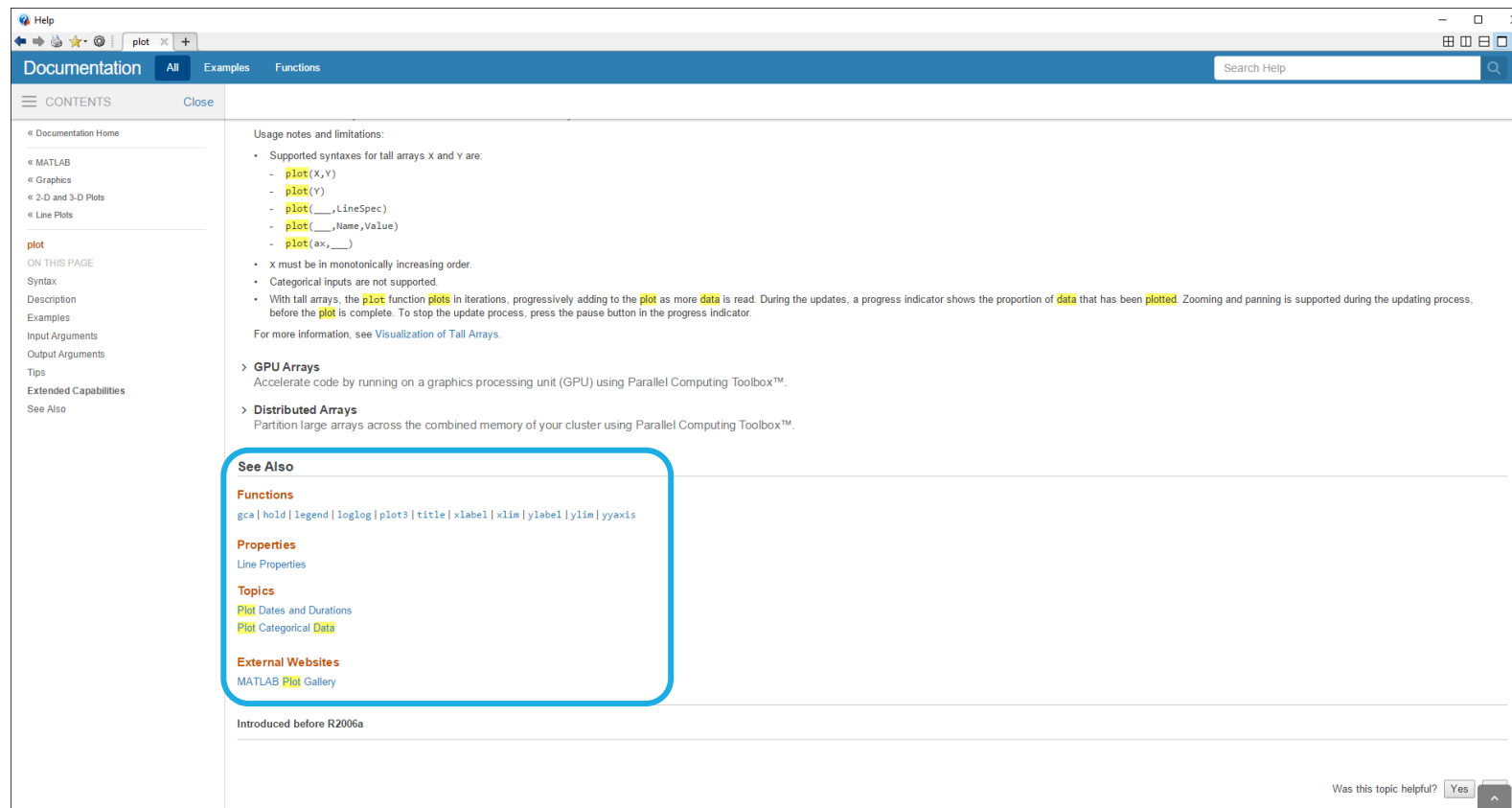
- Using the **help button** or the **Search Documentation** box in the toolbar:



- Pressing **F1** on your keyboard

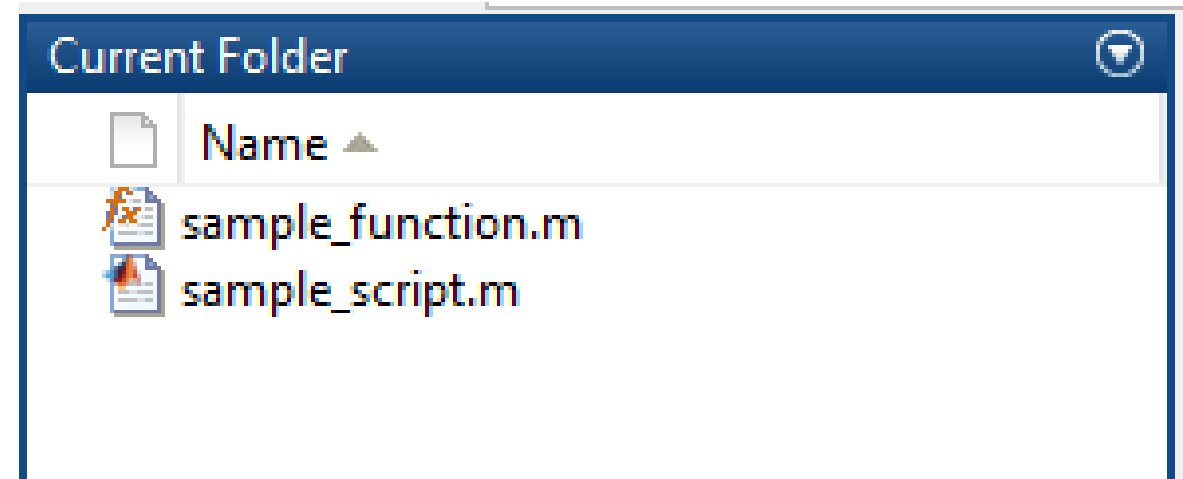
MATLAB documentation center

- Many times MATLAB already has the functionality you need:
 - Search the **documentation center** before implementing new functions
 - At the end of each documentation page, you will find a list of **related functions and topics** that can be very handy



Scripts and functions

- MATLAB code is organized in **scripts** and **functions**
 - Both have file extension `.m`
 - They get different icons in MATLAB file explorer
 - **Scripts** should be the top-level part of your code, where you organize the whole program.
 - **Functions** should correspond to specific tasks.



Scripts

TestCode.m

Mission1.m

Mission2.m

Functions

convert_coordinates.m

propagate_orbit.m

compute_flyby.m

planet_ephemeris.m

time_conversion.m

Code structuring

Scripts

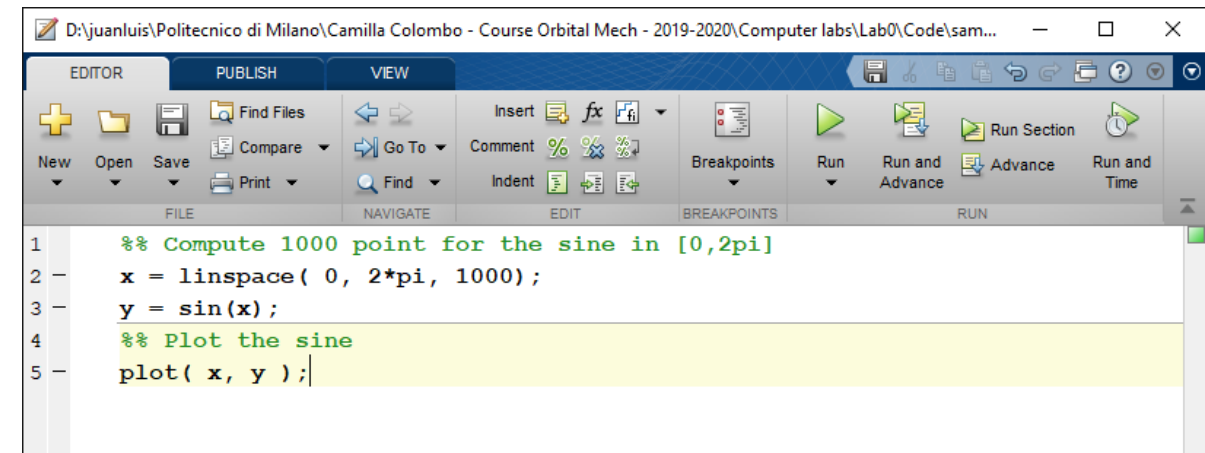
Scripts are the top-level files of your code.
They can be **executed directly**:

- From the **editor**, using the toolbar or the keyboard
- From the command window, typing the name of the script (without file extension)
- You can also define **sections**, to execute your scripts part by part
 - New sections are created typing **%%**
 - The current section is the one containing the cursor, and is highlighted in yellow



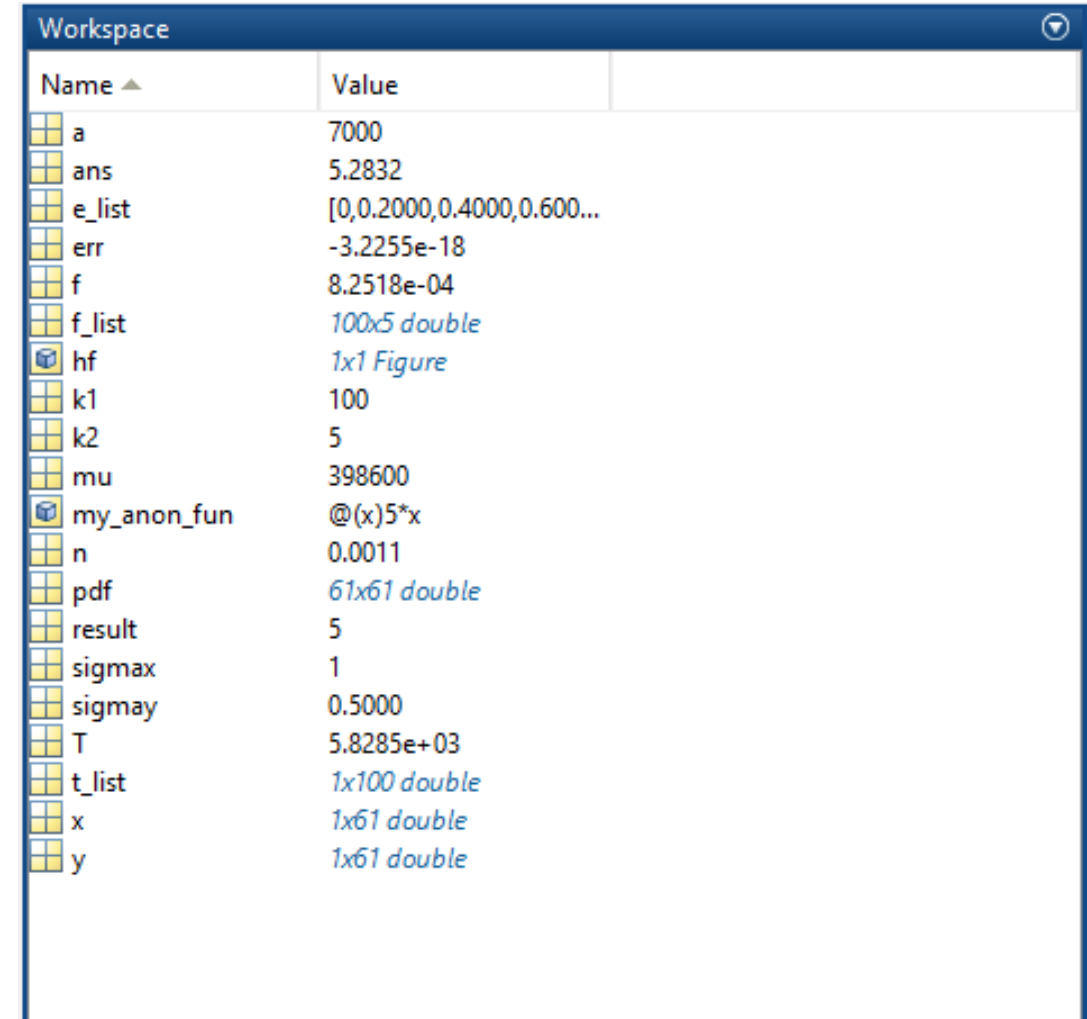
Keep your cursor over a button in the toolbar to see the keyboard shortcut

```
>> sample_script
```



Scripts

- **Scripts** use the **global memory workspace**:
 - They can access any variable previously defined in the workspace. This includes variables created by other scripts or in the command line
 - They can add new variables to the workspace
- **This is very dangerous when calling scripts from scripts**. Because they share the workspace, if they accidentally use the same name for different variables, they will overwrite each other:
 - **Very difficult to debug**
 - You have better control calling **functions** instead



Name ▲	Value
a	7000
ans	5.2832
e_list	[0,0.2000,0.4000,0.600...
err	-3.2255e-18
f	8.2518e-04
f_list	100x5 double
hf	1x1 Figure
k1	100
k2	5
mu	398600
my_anon_fun	@(x)5*x
n	0.0011
pdf	61x61 double
result	5
sigmax	1
sigmay	0.5000
T	5.8285e+03
t_list	1x100 double
x	1x61 double
y	1x61 double

Functions

- **Functions** can be called from the **command window**, **scripts**, or **other functions**:

```
>> [output1,output2] = sample_function(input1,input2)
```

- **Functions** should focus on **performing specific tasks**:
 - Breaking code into small pieces makes it easier to **test**, **develop** and **maintain**
 - Try making them as general as possible, so that they can be **reused**
- **Functions** have their own **memory workspace**:
 - They don't "see" variables created outside of their workspace, except for those defined as **global** (**strongly discouraged**)
 - Data exchange is controlled through **input/output variables**
 - Their internal variable names will not conflict with other scripts/functions
 - All internal variables are erased when the function ends, unless they are defined as **persistent** (be careful when using them)

Functions

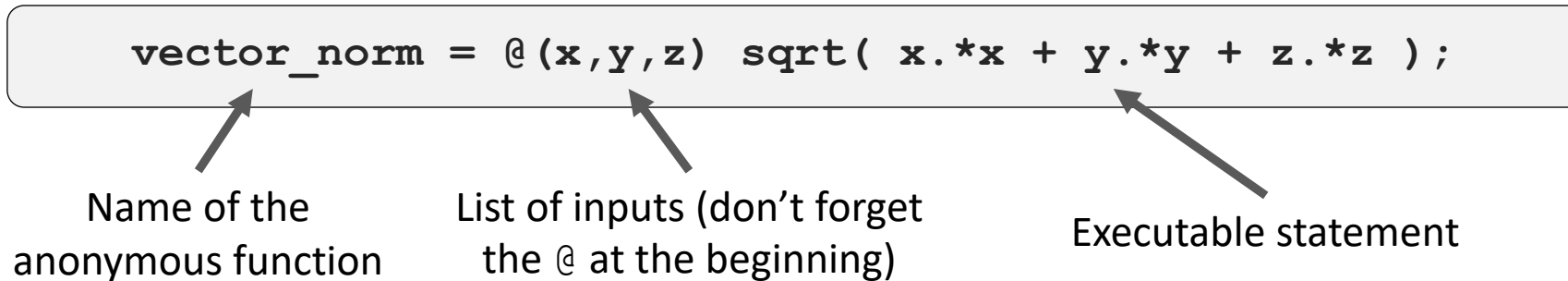
```
function n = mean_motion( a, mu )
% mean_motion Mean motion of a Keplerian orbit
%
% Function to compute the mean motion of an orbit. This is a very simple
% example to put in the slides of the lab
%
% PROTOTYPE
%   n = mean_motion( a, mu )
%
% INPUT:
%   a [1]      Semimajor axis [L]
%   mu [1]     Gravitational parameter of the primary [L^3/T^2]
%
% OUTPUT:
%   n [1]      Orbit mean motion [1/T]
%
% CONTRIBUTORS:
%   Juan Luis Gonzalo Gomez
%
% VERSIONS
%   2018-09-26: First version
%
n = sqrt( mu/a^3 );

end
```

Anonymous functions

- An **anonymous function** is a function that is not written in a separate file, but defined directly as a variable inside another function/script
 - They can have several inputs and outputs, as a normal **function**
 - But they can only contain a single executable statement
 - You can define them inside **scripts**, **functions**, or in the command line
- **Anonymous functions** are created as follows:

```
vector_norm = @(x,y,z) sqrt( x.*x + y.*y + z.*z );
```



Name of the anonymous function

List of inputs (don't forget the @ at the beginning)

Executable statement

- **Anonymous functions** are called as any normal **function**

Anonymous functions

- **Anonymous functions** are normally used to:
 - Define small auxiliary functions within a **function** or **script**, without the need of creating a new file
 - Adapt the **interface** (inputs/outputs) of another function. Example:

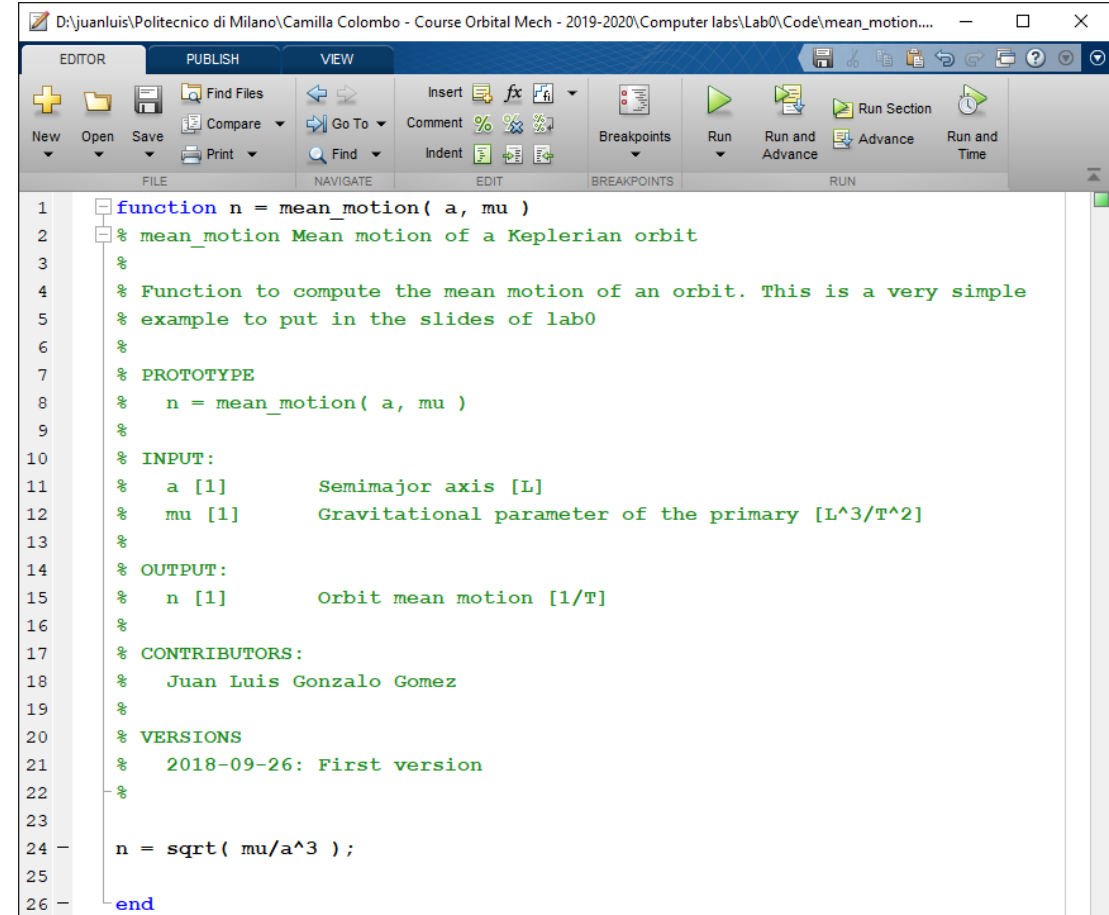
```
% MATLAB's 'integral' function can be used to perform the  
% numeric integral of a 1D function. 'integral' expects  
% a function with a single input variable.  
% I want to perform the integral of function my_fun  
% between 0 and 1, but it has 2 inputs (the second one  
% is a parameter, of value 5 for this example).  
% I can solve this using an anonymous function:
```

```
my_anon_fun = @(x) my_fun( x, 5 );  
result = integral( my_anon_fun, 0, 1 );
```

Documentation

■ Document your code!

- Software is normally developed by **teams**; others must be able to understand/use your code
- Not just for others, also **for the future you**
- Use easily identifiable names for functions and variables
- Include a header with:
 - Usage of the function
 - List of inputs and outputs (with physical units)
 - Authors and dates
 - Version log
 - External dependencies



```
1 function n = mean_motion( a, mu )
2 % mean_motion Mean motion of a Keplerian orbit
3 %
4 % Function to compute the mean motion of an orbit. This is a very simple
5 % example to put in the slides of lab0
6 %
7 % PROTOTYPE
8 %     n = mean_motion( a, mu )
9 %
10 % INPUT:
11 %     a [1]      Semimajor axis [L]
12 %     mu [1]     Gravitational parameter of the primary [L^3/T^2]
13 %
14 % OUTPUT:
15 %     n [1]      Orbit mean motion [1/T]
16 %
17 % CONTRIBUTORS:
18 %     Juan Luis Gonzalo Gomez
19 %
20 % VERSIONS
21 %     2018-09-26: First version
22 %
23
24 n = sqrt( mu/a^3 );
25
26 end
```



Comments in MATLAB begin with symbol `%`

They can begin at any point of the line (e.g., after a command)

Testing

■ Test your code as you go!

- No large code is bug-free (empirically demonstrated)
- **Unit testing**: test each function independently as you program them
 - If you only debug the whole program at the end, it is very difficult to identify the source of each problem
- Breaking up your code into small **functions** eases validation
- One great way of validation is to check if the code reproduces **known results** (analytic solutions for particular cases, conservation principles, etc.)



MATLAB includes very useful **debugging tools**:

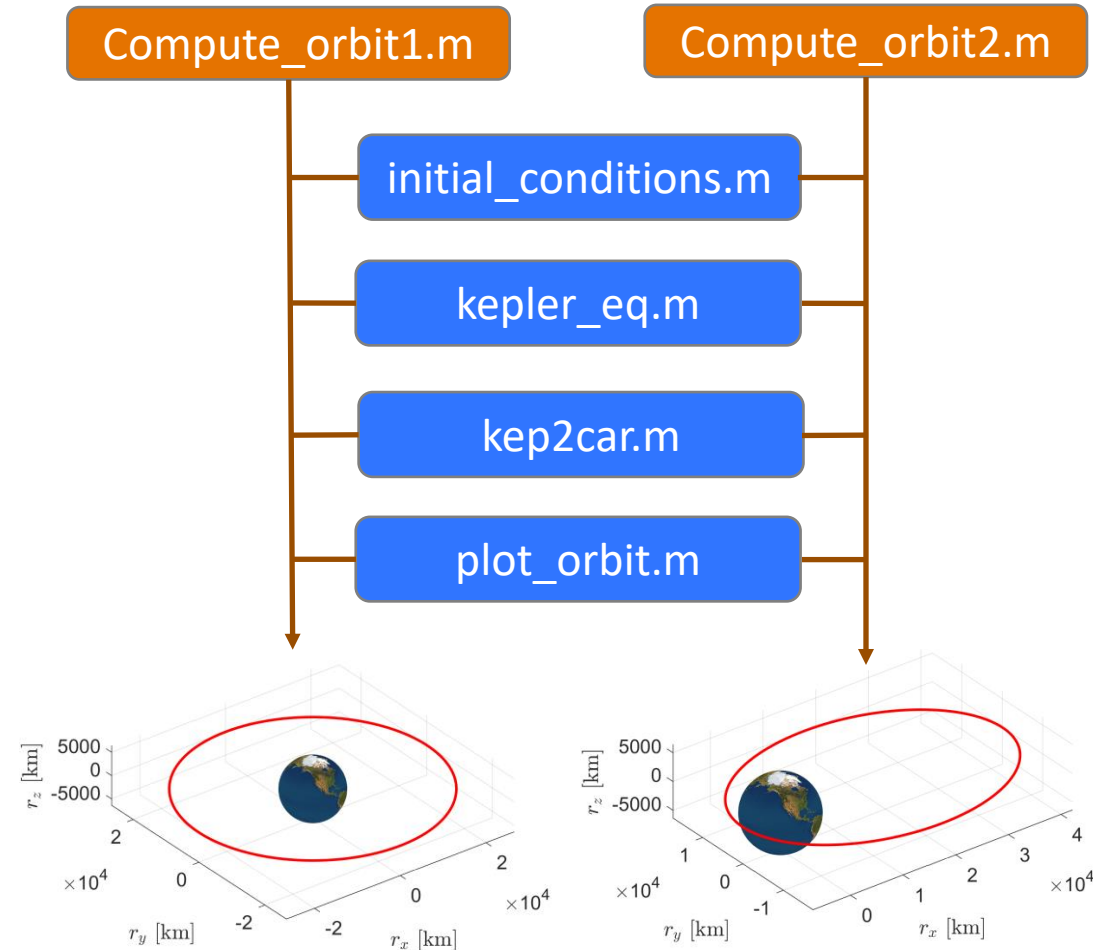
- Pause the execution and advance line by line,
- Check the memory workspace of each function,
- And much more.

Read the documentation page **“Debug a MATLAB Program”** to learn more!

Best coding practices

Reusability

- **Reuse as much as possible!**
 - Break your code into small, single-task **functions** with general inputs, so that they can be reused
 - This is not the same as copy-pasting blocks of code
 - This eases development and testing



By writing small, task-specific, reusable **functions** you will have less code to write, test and maintain

Are they really important?

- **Figures** (plots, graphs, charts, etc.) are a **key component of scientific and technical communication**
 - Good figures **convey a lot of information in a clear and concise way**
- A good figure should:
 - Have its axes clearly labelled, including physical units
 - Include a caption, placed below the figure, presenting its contents
 - If more than one data set is represented, include a legend and use different colours and markers/line styles
 - Use a font size clearly readable
 - Be self-contained (i.e. should be understandable even without reading the whole document)



Badly presented figures in the reports will be harshly punished

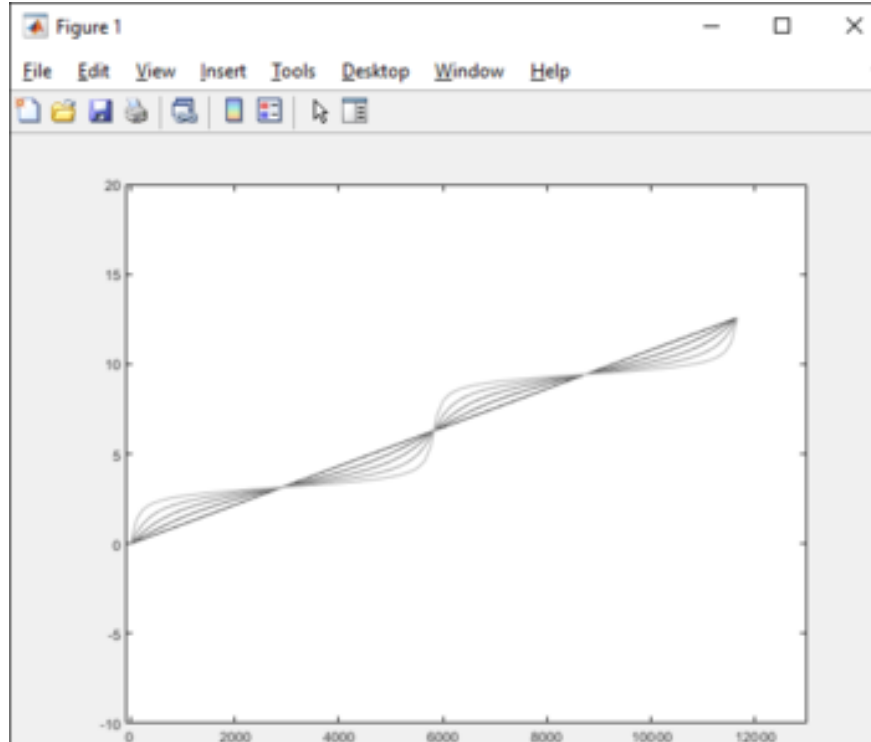
Figures

This is a BAD figure

It is just a low-resolution screenshot

Font is too small to read

I don't know what the axes represents, or their physical units



Very difficult to distinguish the lines

I don't know the meaning of each line

Plenty of wasted blank space

Without a title or a caption, I cannot know what is being represented in the plot

Figures

This is a GOOD figure

Good-quality image

Font size is similar to
the text of the slide

The variable
represented in each
axis is indicated,
along with its units

The unit of time
(orbital period) is
chosen to get
numerical values
easy to understand

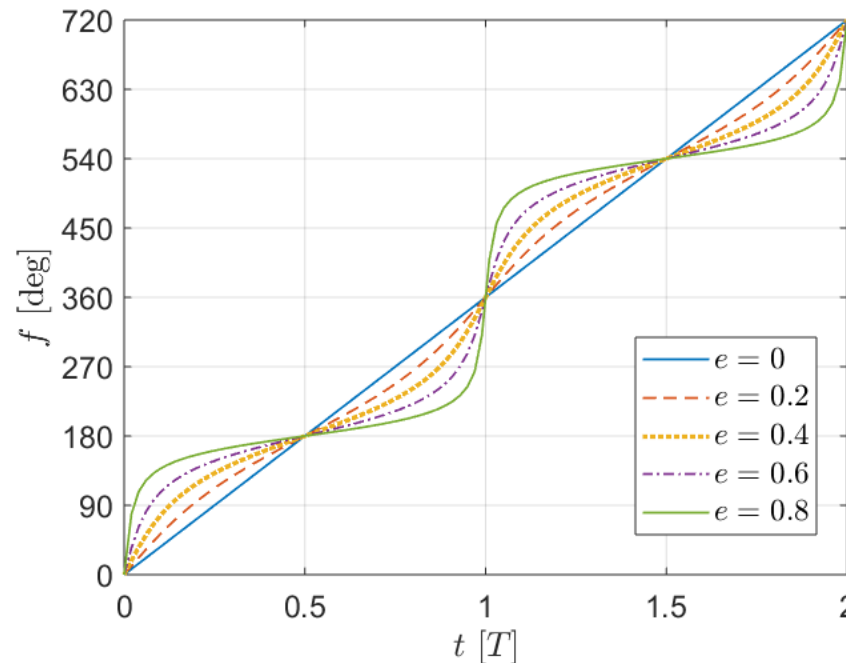


Figure 1. Evolution of true anomaly with time for several orbits with $a = 7000$ km, $\mu = 398600$ km³/s², and different e

Lines are set apart
using different colors
and line styles

A legend is included

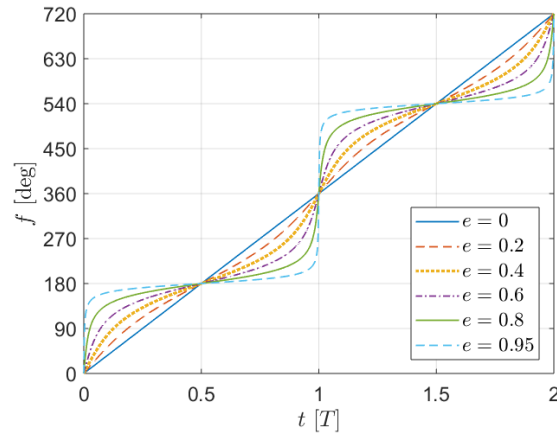
A grid is included to
improve readability

Ranges are set to
make use of all
available space

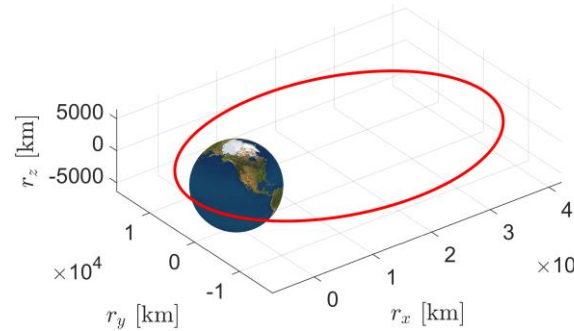
Figure contents are clearly introduced in a caption, together with a number to reference the figure

Plotting in MATLAB

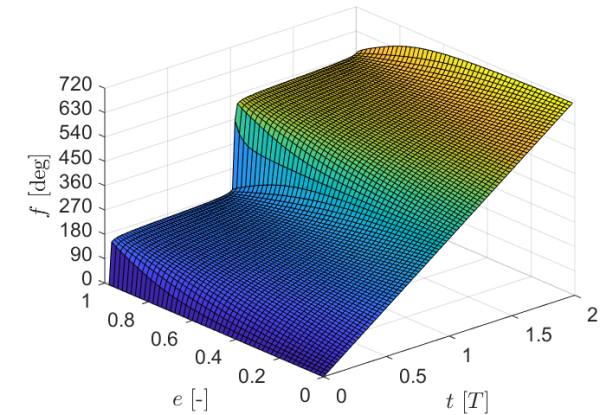
- MATLAB can represent many types of figures (check the [documentation center](#) to learn how to use them)



plot



plot3



surface

- Other types of MATLAB plots:
 - `quiver` and `quiver3`: 2D and 3D vector field plots
 - `comet` and `comet3`: animations in 2D and 3D plots
 - `sphere`: Generates a sphere
 - `mesh`: 3D surface plots

Customizing plots in MATLAB

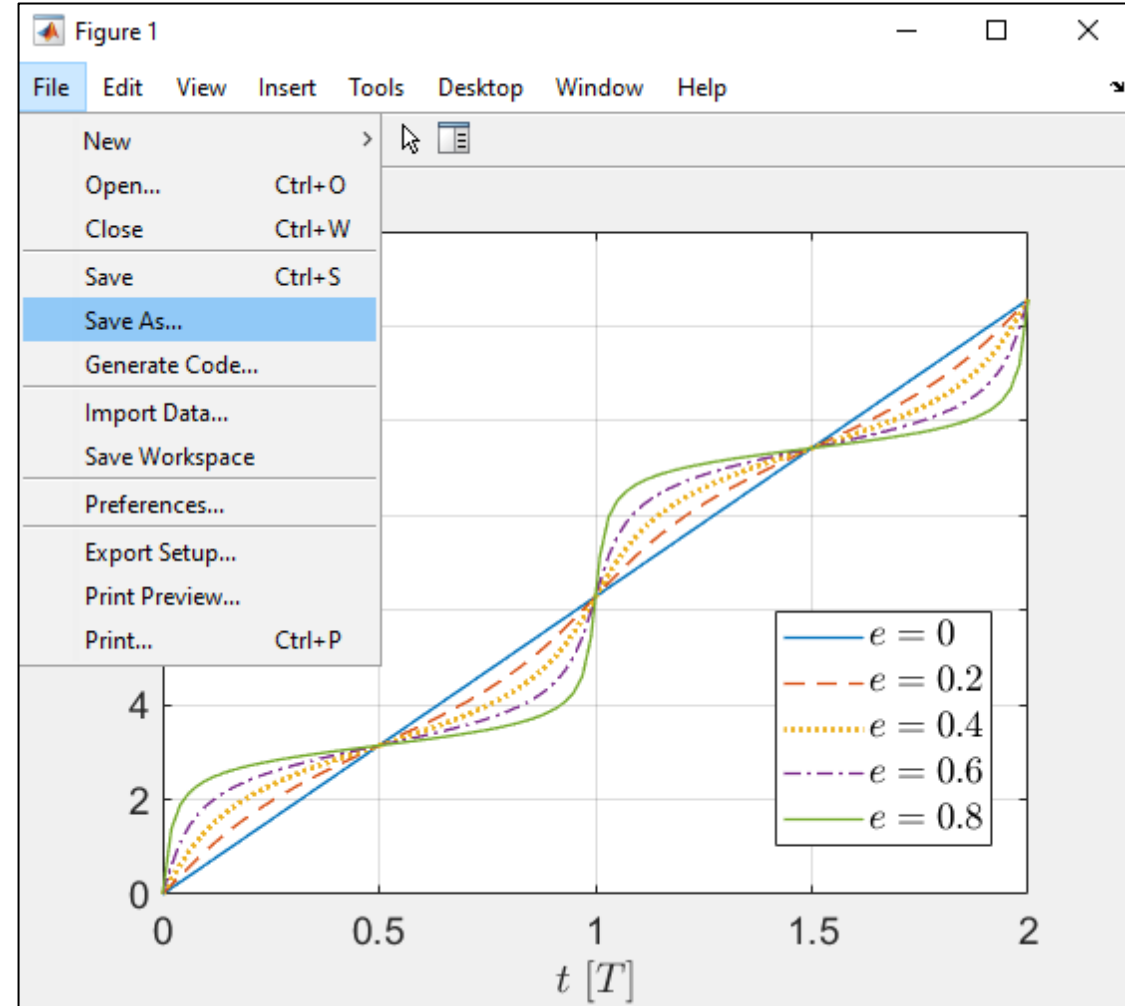
- Properties of plots can be adjusted from the graphical interface or using commands:
 - `xlabel`, `ylabel`, and `zlabel`: Set labels for x, y, and z axes
 - `xlim`, `ylim`, and `zlim`: Set the plotting range for each axis
 - `title`: Set the title of the plot
 - `legend`: Add a legend to the plot
 - `grid on`: Add a grid to the plot
 - `hold on`: Hold the plot, so new lines can be added
 - `axis equal`: Use equal unit length along all axes
 - and many more



Check the [documentation page](#) for each kind of plot to discover all the available options and related commands

Saving figures in MATLAB

- MATLAB uses its own format (`.fig`) to save figures
 - You can open fig files in MATLAB to edit them
- You can export figures to common formats (png, jpg, eps, etc), to use them in the report and presentation
 - Menu “File > Save as...”
 - MATLAB cannot edit these formats after exporting
- You can also save figures from code using commands such as `saveas` and `print`



Screenshots are not a good way to include figures in the report or presentation