

# A Decision Support Methodology for the Design of Reconfigurable Assembly Systems

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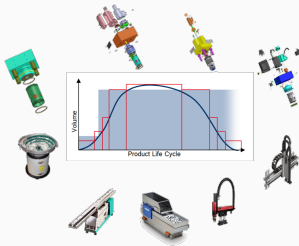
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## Introduction

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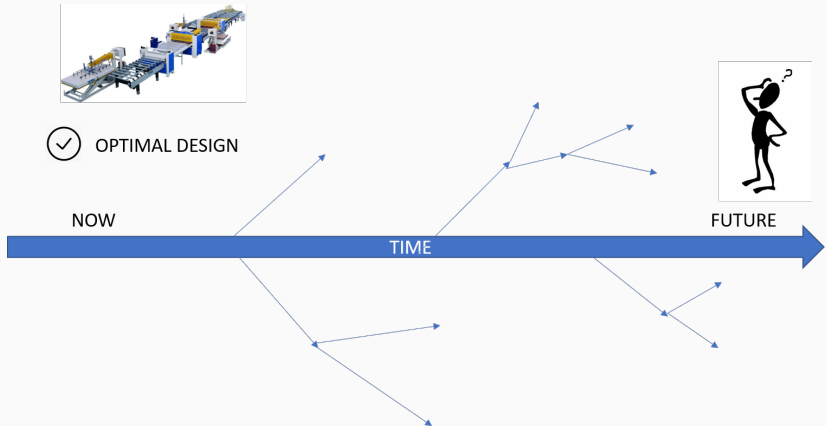
- Assembly for mass customization
- High number of product families
- Small lot sizes
- Short product life-cycles
- Changing product-mix and
- High demand fluctuations

The problem the manufacturers are facing is:



1. multi-period
2. multi-product
3. long-term
4. modular and complex system

# Industrial Relevance



- Some of the main problems concerning system design of large-scale production systems include
  - Assembly Line Balancing (Becker and Scholl, 2006)
  - Buffer Allocation (Demir et al., 2014)
  - Capacity estimation (Wazed et al., 2010).
- Solving methods include:
  - Stochastic approaches play a central role in system design (Tolio, 2008)
  - Analytical approaches (Shabanpour and Colledani, 2018; Colledani et al., 2015; Colledani, 2013; Colledani and Gershwin, 2013; Colledani et al., 2014)
  - Stochastic Programming (J. R. Birge and F. Louveaux., 1997) is based on the assumption that the fluctuation of model parameters is governed by their probability distribution.
  - Alternative methodologies to deal with uncertainty include robust approaches, such as the ones proposed in (Ben-Tal, A. and Nemirovski, A., 2000) and reviewed in (Bertsimas et al., 2011).

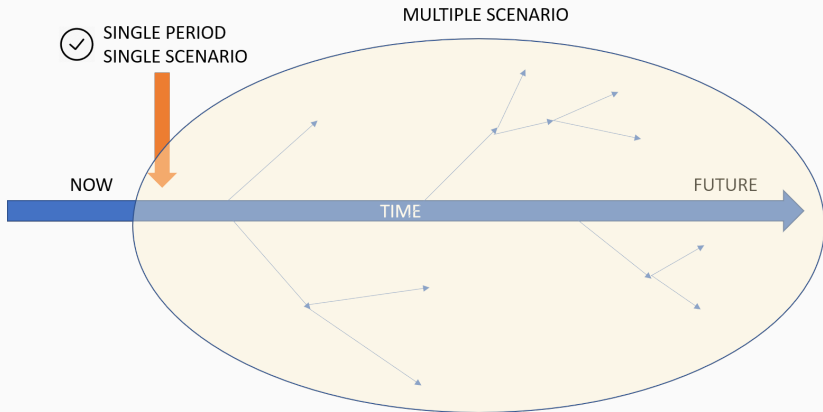
### In general

Methods applicable to real industrial problems characterized by complexity, multi-objective and multi-period decision making are not widely available.

## Problem Statement

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# Problem



### Single-period

- Design solutions satisfying requirements defined within each scenario
- It is a greenfield design problem,
- Single-period problems can be solved independently
- It consists of:
  1. Multi-product Assembly Line Balancing (MALB)
  2. Buffer Allocation Problem (BAP)

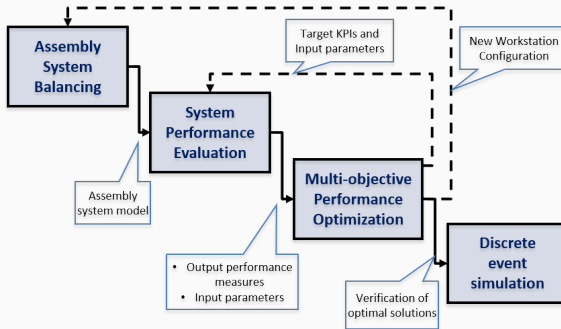
### Multiple-period

- System configurations taking into account **all** the possible paths along scenarios that the system might have to face



## The RecaM Approach

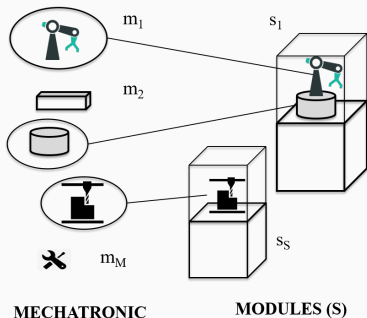
- The methodology is developed in the ReCaM project.
- Part of a software platform that supports engineers in the green field design phase of assembly systems.
- Composed of interconnected software building blocks that exchange information with both product and resource catalogues and the Manufacturing Execution Systems (MES).



# The ReCaM Approach

## Resources

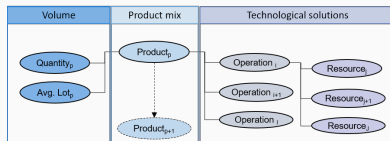
Modular and programmable resources called Mechatronic Objects (MOs) provide the processing capabilities required by the products.



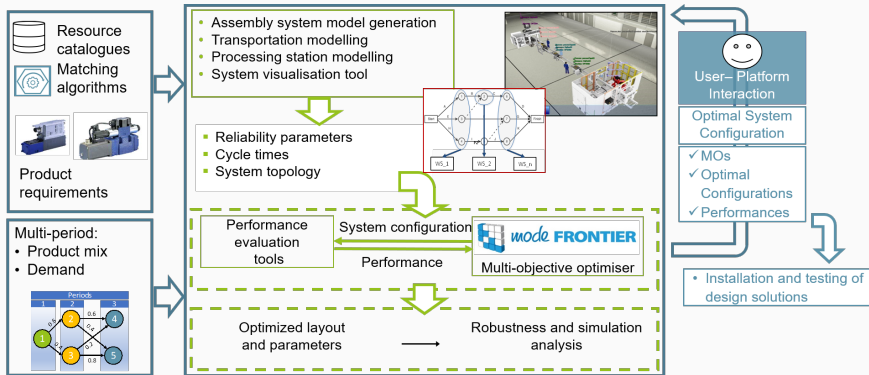
## Products

The input information consist of long term forecasts:

- Product mix
- Production volumes
- Expected volume changes
- Average lot sizes



# The ReCaM Approach



## Methodology

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Define:

$v \in V$  Set of discrete and finite time windows (i.e. periods)

$o \in O$  Scenarios Set of production forecast *scenarios*;

$p \in P$  Set of *product* variants to be produced over the entire planning horizon;

$i \in I$  Tasks of *tasks* to be executed (among all product  $p \in P$ );

$m \in M$  Set of *Mechatronic Objects* that can supply a certain set of capabilities;

$s \in S$  Set of *stations* that are instantiated;

$b \in B$  Buffer types (technological choice of buffer system)

$\Delta v$  Period length [h]

$\pi_{o_i, o_j}$  Transition probability between scenarios

$CMinv_m$  cost of module  $m$

$CBinv_b$  Cost of buffer  $b$

$CMbusy_m$  working Cost

$CMidle_m$  starving and blocking cost

$CMfail_m$  Failure Cost

$CF_m$  Cost per failure event

$CBhold_{p,k}$  Inventory Cost

$CMstock_m$  Inventory Cost

$CMinstall_m$  Installation Cost of MO

type  $m$  at a certain station.

$CMuninstall_m$  Uninstallation Cost

$CBinstall_b$  Installation Cost of  
buffer-type  $b$

# Single-period problem

**Objective:** minimize: single-period objective function  $Z_o$

## Decision variables

- Tasks-stations assignments ( $x_{i,p,s,o}$ )
- MOs-stations assignments ( $\xi_{m,s,o}$ )
- Instances of MO type  $m$  assigned ( $Nline_{m,o}$ )
- Capacity of  $k$ -th buffer ( $\beta_{b,k,o}$ )
- Buffer slots of type  $b$  installed ( $n_{b,k,o}$ )

## Constraints

- Demand satisfaction constraints (i.e. minimum throughput)
- Line Balancing constraints (e.g. precedences)
- Buffers-related constraints (e.g. maximum capacity)

## Some quantities in the model are non-linear

- The throughput of the assembly system in scenario  $o$  ( $TH^o$ )
- The utilization of each MO associated to a station in scenario  $o$  ( $u_{s,m,o}$ )
- The probability of failure for a MO in a station in scenario  $o$  ( $f_{s,m,o}$ )
- The average inventory of product  $p$  in the buffer  $k$  in scenario  $o$  ( $WIP_{p,k,o}$ )

# Objective Function $Z_o$ - Single-period

The objective function  $Z_o$  includes:

## Operating costs

$$CMbusy_m \cdot \bar{u}_{s,m,o}$$

## Failures costs

$$CMfail_m \cdot \bar{f}_{s,m,o}$$

## Idle times costs

$$CMidle_m \cdot (1 - \bar{u}_{s,m,o} - \bar{f}_{s,m,o})$$

## Inventory costs

$$\sum_{p \in P} \sum_{k \in K} CBhold_{p,k} \cdot \bar{WIP}_{p,k,o}$$

## Investment costs of MOs

$$\sum_{m \in M} (CMinv_m + CMinstall_m) \cdot (Nline_{m,o})$$

## Investment costs of buffers

$$\sum_{k \in K} \sum_{b \in B} (CBinv_b + CBininstall_b) \cdot n_{b,k,o}$$

## Failures costs (events)

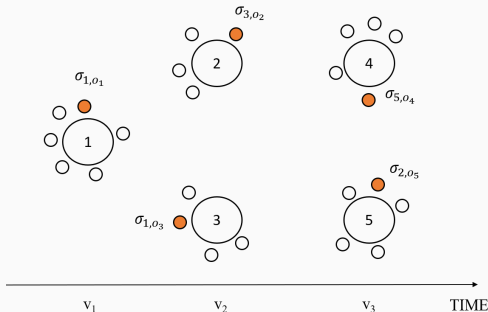
$$\sum_{m \in M} \sum_{s \in S} CF_m \cdot NF_{m,s}$$

# Objective Function - Multiple-period

## Notation

- $\sigma_{r,o} \in \Sigma$ :  $r^{th}$  solution found for the single-period, single-scenario problem for scenario  $o \in O$ .
- $\Psi$ : set of all the permutations of feasible solutions.
- $\gamma \in \Gamma(\psi_i)$  is a path through a set of solutions. It represents a feasible sequence over time periods for the  $i$ -th permutation  $\psi_i$ .

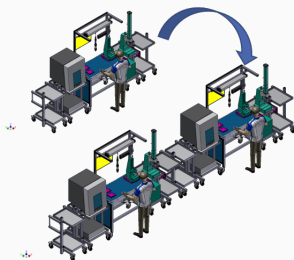
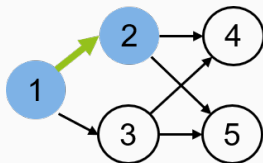
$$\phi_i = \{\sigma_{1,o_1}, \sigma_{3,o_2}, \sigma_{1,o_3}, \sigma_{5,o_4}, \sigma_{2,o_5}\}$$





## Objective Function - Multiple-period

Suppose to go from scenario  $\sigma_1$  to  $\sigma_2$  from period  $v$  to  $v + 1$ .

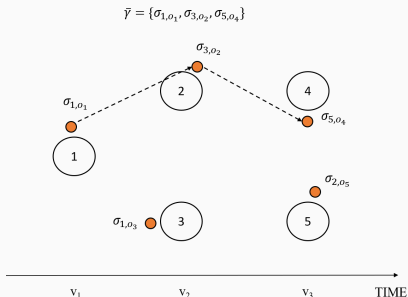


Reconfiguration actions may be taken:

- **Buy** a new module  $m$  on a station  $s$ ;
- **Move** a module  $m$  from one station to another;
- **Store** a module  $m$  in a warehouse/stock;
- **Move back** module  $m$  from stock to the system.

# Objective Function - Multiple-period

→ The total cost  $Z_{tot, \psi_i}$  depends on the particular permutation of solutions:



## Total cost

$$Z_{tot, \psi_i} = \sum_{\gamma \in \Gamma(\psi_i)} Z_{\gamma} \cdot \pi_{\gamma}$$

$$Z_{\gamma} = \sum_{o \in \gamma} Z_o$$

$$\pi_{\gamma} = \prod_{\{i\} \in \Gamma(\psi_i)} \pi_{i, i+1}$$

→ The multi-period, multi-scenario problem becomes:

$$\min_{\psi_i \in \Psi} Z_{tot, \psi_i}$$

That is, finding the permutation of solutions  $\psi_i$  that minimizes the total system cost, satisfying all the problem's constraints.

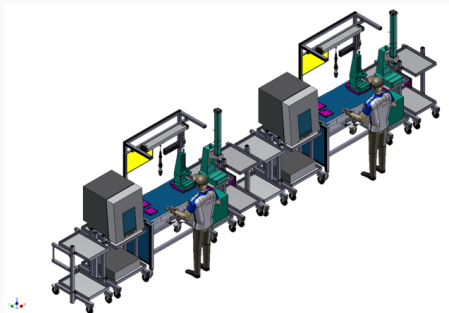
- The solution method is heuristic (complete enumeration).
- Each scenario is solved independently as single-period problem, and a certain number (user-specified) of near-optimal solutions are generated .
- By sampling one solution from each single scenario, a permutation of solutions at the scenario level is generated. The result is a set of solutions  $\Sigma$ , and the corresponding set of permutations  $\Psi$ .
- From this point, the heuristic follows an exhaustive enumeration over all the  $\psi_i \in \Psi$ .
  - a) List all the permutations  $\psi_i \in \Psi$ .
  - b) Calculate the set of feasible paths for each permutation  $\Gamma(\psi_i)$ .
  - c) For each permutation, calculate the solution of single-scenario problems for all the scenarios along the feasible paths.
  - d) For all the feasible paths, evaluate the expected total cost.
  - e) Solve the global minimization problem.
  - f) Enumerate the cost of solutions found and select the minimum ones.

## Case-study

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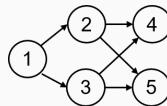
## Case-study

The use case involves an assembly line for the production of hydraulic valves:



### Data

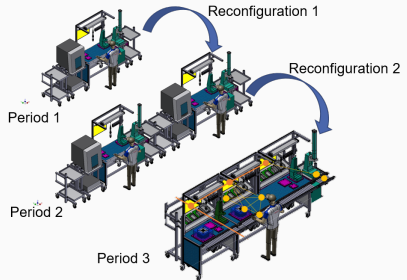
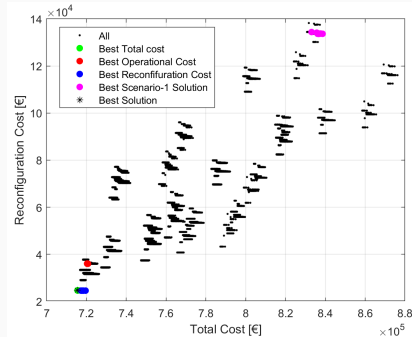
- 6 product types
- 19 modules
- 3 years horizon
- 5 scenarios



- 11 solutions have been drawn for each of the 5 single-scenario sub-problems, for a total of  $|\Psi| = 161051$  permutations.
- Each of these solutions represent the configuration of an assembly line.
- The complete enumeration algorithm took around 10 minutes to be solved on a DELL XPS13 laptop with 8 GB memory and INTEL 2.3-GHz, i7 processor.

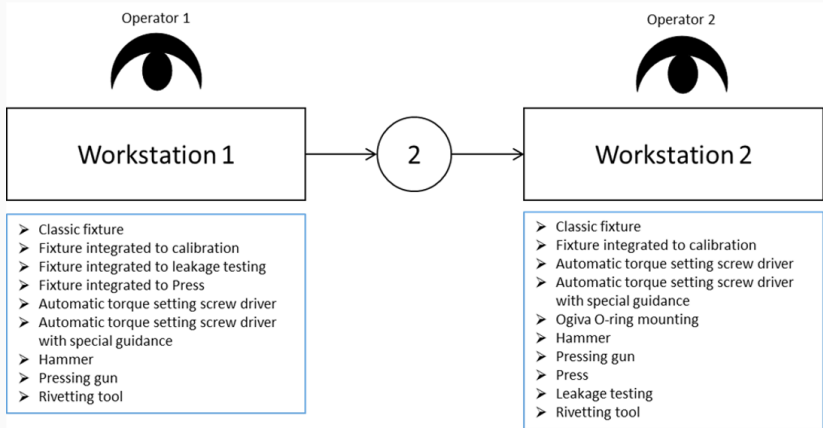
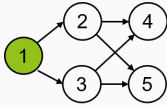
# Case-study

→ Each point in the solution list corresponds to a specific system design and reconfiguration throughout the system lifecycle.



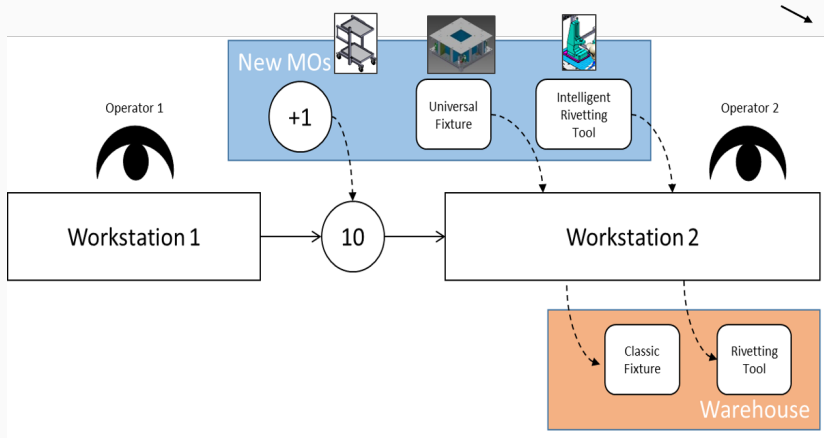
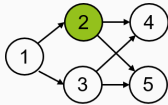
| Cost Category   | Total expected Cost [€] |
|---|-------------------------|
| Best Reconfigurable Solution                              | 715,430                 |
| Flexible Solution for all scenarios                       | + 35 %                  |
| Solution that minimizes costs only for the initial period | + 23 %                  |

# Results



Solution A – first period design

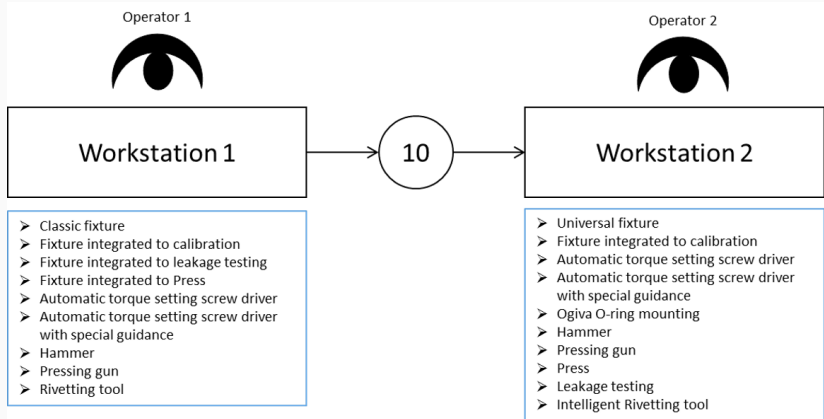
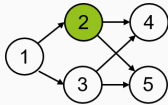
# Results



Solution A – reconfiguration 1-2

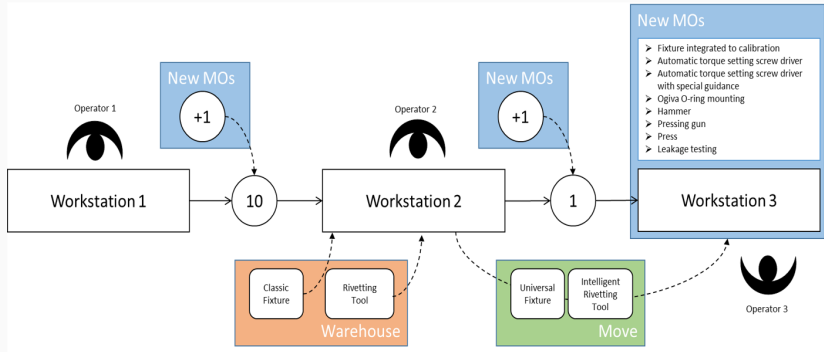
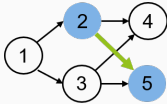


# Results



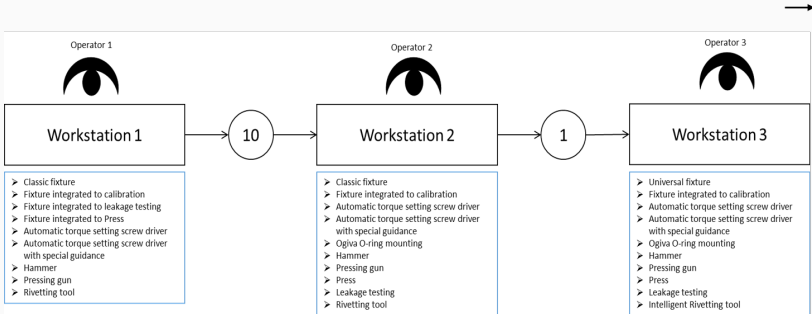
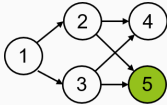
Solution A – second period design (scenario 2)

# Results



Solution A – reconfiguration 2-5

# Results



Solution A – third period design (scenario 5)

## Conclusions

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- A methodology for supporting the green-field design of reconfigurable assembly systems by considering a multi-period problem, characterized by uncertain product-mix and demand scenarios.
- The system configuration decisions taken at the initial design phase can consider possible future system modifications that might be needed within the planning horizon.
- The approach identifies optimal designs capable of quickly and efficiently adapting towards product variant and production quantity changes.
- The optimal solution is not always the one that minimizes the total cost over a certain time horizon, but the system configuration that is more adaptable to the anticipated future changes.

### Future research

- Extend the formulation to include spatial constraints, product routing constraints, layout constraints, as well as specific user-defined constraints.
- Efficient and faster solution techniques are needed. Candidates are genetic algorithms, branch-and-bound algorithms, and neural networks.



[recam-project.eu](http://recam-project.eu)

## References

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- Becker, C., and A. Scholl. 2006. "A survey on problems and methods in generalized assembly line balancing". *European Journal of Operational Research* 168(3):694 – 715. Balancing Assembly and Transfer lines.
- Ben-Tal, A. and Nemirovski, A. 2000. "Robust solutions of Linear Programming problems contaminated with uncertain data".
- Bertsimas, D., D. Brown, and C. Caramanis. 2011. "Theory and applications of robust optimization". *SIAM Review* 53(3):464–501.
- J. R. Birge and F. Louveaux. 1997. "Introduction to Stochastic Programming".
- Colledani, M. 2013. "A Decomposition Method for the Analysis of Long Buffered Production Systems with Discrete General Markovian Machines". *IFAC Proceedings Volumes* 46(9):1644 – 1649. 7th IFAC Conference on Manufacturing Modelling, Management, and Control.
- Colledani, M., and S. B. Gershwin. 2013, Oct. "A decomposition method for approximate evaluation of continuous flow multi-stage lines with general Markovian machines". *Annals of Operations Research* 209(1):5–40.
- Colledani, M., A. Ratti, and C. Senanayake. 2015. "An Approximate Analytical Method to Evaluate the Performance of Multi-product Assembly Manufacturing Systems". *Procedia CIRP* 33:357 – 363. 9th CIRP Conference on Intelligent Computation in Manufacturing Engineering - CIRP ICME '14.



Colledani, M., T. Tolio, A. Fischer, B. lung, G. Lanza, R. Schmitt, and J. Váncza. 2014. "Design and management of manufacturing systems for production quality". *CIRP Annals* 63(2):773 – 796.

Demir, L., S. Tunali, and D. Eliiyi. 2014. "The state of the art on buffer allocation problem: A comprehensive survey". *Journal of Intelligent Manufacturing* 25(3):371–392.

Shabanpour, N., and M. Colledani. 2018. "Integrated Workstation Design and Buffer Allocation in Disassembly Systems for Remanufacturing". *Procedia CIRP* 69:921 – 926. 25th CIRP Life Cycle Engineering (LCE) Conference, 30 April – 2 May 2018, Copenhagen, Denmark.

Tolio, T. 2008. *Design of flexible production systems*. Springer.

Wazed, M. A., S. Ahmed, and Y. Nukman. 2010. "A review of manufacturing resources planning models under different uncertainties: State-of-the-art and future directions". *South African Journal of Industrial Engineering* 21(1):17–34.

# Assumptions

- It is assumed that the set of *scenarios* are finite and describe possible forecasts of product-mix and quantities.
- All reconfiguration actions happen only between two consecutive periods, and include:
  1. the **upgrade** of a station in terms of installation/uninstallation of resources,
  2. the **purchase** of a new resource
  3. the **storing** of a resource in a warehouse because it is not required for production.
- once an instance of a certain resource (MO, buffer) is uninstalled from the layout, it is moved to a warehouse to be stored.
- The reconfiguration costs are considered as the costs of reconfiguring the system between two scenarios in sequential periods
- Unused MOs are stored in a warehouse.