# Problem A. Score analysis

Input file: standard input
Output file: standard output

Time limit: 3 seconds
Memory limit: 256 megabytes

MSAI teaches continue to analyse results of this year courses. And again, they can't do without your help!

This time number of students was  $0 \le N \le 100000$ , and teachers want to check if courses were too easy or too difficult. To do that they need to check number of students whose average score is within given range:  $l \le score \le r$ .

Please, help the teachers and write the program which can process such requests fast. The number of requests teachers prepared for you is  $0 \le M \le 100000$ .

#### Input

First line contains two integer numbers divided by space character:  $0 \le N, M \le 100000$  — number of students and requests respectively. Second line contains N numbers divided by space character: scores of students.  $0 \le s_i \le 10^9$ . Each of the following M lines contains two integer numbers:  $l_j, r_j$ , divided by space character:  $0 \le l_i \le r_j \le 10^9$ 

#### Output

For each request  $(l_j, r_j)$  print one integer number on separate line: number of students who got score within requested range:  $|\{i: l_j \leq s_i \leq r_j\}|$ .

#### **Examples**

standard input	standard output
6 6	2
1 1 2 2 2 3	3
1 1	1
2 2	5
3 3	4
1 2	6
2 3	
1 3	
2 3	0
1 1	2
0 0	0
0 100000000	
5 10	
2 3	1
1 1000000000	1
0 10	2
10 1000000000	
0 100000000	

#### Note

You can use sorted() and list.sort() in this week home assignments.

# Problem B. Sigma-trimpasation 1

Input file: standard input
Output file: standard output

Time limit: 7 seconds
Memory limit: 256 megabytes

After graduating from MIPT you've decided to apply your knowledge in AI to Physics. You've become a world-wide famous physicist due to your deep knowledge of AI which you get on MSAI program. And now you are working on a innovational quantum process research: sigma-trimpazation\*. Your research is definitely going to change the world!

Your experiment is in progress. Quantum sensors are installed and send you data permanently. You've found a regularity in this data. And now you are going to analyse it using python. What you need – is to get this data in sorted order.

Your process is initialized with three parameters:  $0 \le N \le 10^7$ ,  $0 < M \le 10^4$ ,  $0 < q_0 < 2^{31}$ . The process is the following: your data sequence x is generated from quantum data sequence q. You are given  $q_0$  value and next items are generated using the following rule\*\* (this process is already implemented for you):

$$q_i = (q_{i-1} * 7^5) \bmod (2^{31} - 1)$$

The data you need to analyze is calculated from quantum data:  $x_i = (q_i \mod M) - M//2$ 

Let's denote sorted data sequence as  $x_s = sorted(x)$ . You need to calculate the following value:

$$y = \sum_{i=1}^{N} (i * x_s[i-1]) = 1 * x_s[0] + 2 * x_s[1] + 3 * x_s[2] + \dots + N * x_s[N-1]$$

You've tried to use built-it python sorting algorithm but it takes too much time (your code is here: <a href="https://bit.ly/34vIxb2">https://bit.ly/34vIxb2</a>). You need to implement something faster. Try to optimize it somehow. No time to obtain TL verdict! Research must go on!

#### Input

The only line in input file contains 3 integer numbers divided by space character and followed by line break:  $0 \le N \le 10^7$ ,  $0 < M \le 10^4$ ,  $0 < q_0 < 2^{31}$  — parameters of your process.

### Output

Print the only integer number -y value for your process.

## **Examples**

standard input	standard output
3 5 1	<pre>5 # array generated: # [-1, 0, 5] # result: # -1 * 1 + 0 * 2 + 5 * 2 = 5</pre>
5 10 7	# array generated: # [2, 4, -2, 1, 0] # sorted: # [-2, 0, 1, 2, 4] # result: # -2 * 1 + 0 * 2 + 1 * 3 + # 2 * 4 + 4 * 5 = 29
10000000 10000 1	83287854395709985

#### Note

A. and B. Strugatsky (1962). Noon: XXII century (translated by Patrick L.McGuire). ISBN:0-02-615150-2.

\*\* This process of «quantum» data generation is a Lehmer pseudo-random numbers generator:  $\frac{\texttt{https://en.wikipedia.org/wiki/Lehmer\_random\_number\_generator}}{\texttt{generator}}, \text{ and } q[0] - \text{it's random seed. This generator} \text{ is used here not to slow your program down with reading a lot of data from text file (that will be really slow)}.}$ 

<sup>\*</sup>Trimpazation — joking name of space warp process in book of famous russian sci-fiction writers — the Strugatsky brothers (original: тирьямпампация).

# Problem C. No cheating

Input file: standard input
Output file: standard output

Time limit: 1 second Memory limit: 256 megabytes

MSAI teachers are organizing an exam in another university and they are worried about cheating possibility. Of course, this exam is not in MSAI and not in MIPT, because MIPT students do not cheat. Usually:)

So, teachers decided to prepare sitting places for examinees on a straight line, to be able to see them all. Also, to minimize possibility of using each other's solutions, teachers want to maximize minimum distance between students. Help them, please!

Classroom has  $2 \le N \le 10000$  sitting places, which are situated on a straight line. Their coordinates are  $0 \le x_i \le 10^9$ . You need to assign M students to seats (choose M seats:  $x_{k_1}, x_{k_2}, ..., x_{k_M}$ ) so that minimum distance between students is as much as possible:

$$\min_{i \neq j} |x_{k_i} - x_{k_j}| \to \max$$

Write a program which will do that.

#### Input

First line contains 2 integer numbers N, M divided by space character:  $2 \le N \le 10000$ ,  $2 \le M \le N$  — number of sitting places and students respectively.

Next line contains N integer numbers  $0 \le x_i \le 10^9$  — coordinates of sitting places.

# Output

Print single integer number — desired maximized minimum distance:  $\min_{i \neq j} |x_{k_i} - x_{k_j}|$ 

## **Examples**

standard input	standard output
5 5	1
1 2 3 4 5	
7 3	7
8 9 4 7 12 15 1	
6 4	11
1000000000 0 1 10 11 100	