

# Data Structures Assignment-4

## B) Jack and Railways

Jack arrives at the first stop of the railway line. The railway line has  $N$  stops and Jack wants to reach the last stop ( $N^{th}$  stop). It takes 1 minute to travel from one stop to its adjacent stop.

To make the travel cheaper, there are multiple travel passes available. Each travel pass has cost  $p$  and support distance  $r$ . A travel pass with support distance  $r$  can be used to travel at most  $r$  stops. So, if you enter at stop  $i$  and use travel pass with support distance  $r$  you can exit at any stop from  $i$  to  $i + r$ . To exit and reenter the stop  $i$ , it takes  $d_i$  minutes. There is no time spent on entering the first stop and exiting the last stop.

As Jack has  $t$  time available, he wants to choose the cheapest travel pass that would allow him to complete the journey within time  $t$ .

### Input

First line contains two integers  $N$  and  $t$ , the number of stops and time that is available.

The second line contains  $N - 1$  integers (for  $i = 1$  to  $N - 1$ ),  $p_i$  cost of travel pass with support distance  $i$ .

The third line contains  $N - 2$  integers (for  $i = 2$  to  $N - 2$ ),  $d_i$ , number of minutes required to reenter at stop  $i$ .

### Output

Output a single integer which is the cheapest cost that allows Jack to travel within time  $t$ .

### Constraints

$1 \leq N \leq 50000$ , number of stops

$N - 1 \leq t \leq 10^9$

$1 \leq p[i] \leq 10^6$

$1 \leq d[i] \leq 10^5$

### Sample Input 1

```
4 4
1 2 3
1 4
```

### Sample Output 1

```
2
```

### Sample Explanation 1

For  $r = 1$ , optimal path would be 1-2-3-4. so time taken is 8 minutes. But as it is greater than 4 minutes, you can't use  $r$  as 1.

For  $r = 2$ , optimal path would be 1-2-4. so time taken is 4. So you can use  $r = 2$ . Its price is 2.

For  $r = 3$ , optimal path would be 1-4. so time taken is 3. So you can use  $r = 3$ . Its price is 3.

Hence, it is better to use  $r = 2$ , travel pass as it allows you to travel in time  $t = 4$  minutes and is cheapest.

## Limits

Time: 2 second

Memory: 256 MB