

$$\mathbf{B}_i^T \mathbf{M} \mathbf{B}_i \ddot{\mathbf{q}}_i = \mathbf{B}_i^T \mathbf{Q}_e - \mathbf{B}_i^T \mathbf{M} \gamma$$

State Space form

$$\begin{aligned} \dot{\mathbf{q}}_{1i} &= \mathbf{q}_{2i} \\ \dot{\mathbf{q}}_{2i} &= \mathbf{M}_i^{-1} \mathbf{B}_i^T \mathbf{Q}_e - \mathbf{M}_i^{-1} \mathbf{B}_i^T \mathbf{M} \gamma \end{aligned}$$

Initial Conditions for independent coordinates

$\mathbf{q}_{1i}(0), \mathbf{q}_{2i}(0)$ specified

Newton iteration

$$\begin{pmatrix} \mathbf{C}_q \\ \mathbf{I}_b \end{pmatrix} \Delta \mathbf{q}_1 = \begin{pmatrix} -\mathbf{C} \\ \mathbf{0} \end{pmatrix}$$

Form \mathbf{C}_q, \mathbf{C}

Assume $\mathbf{q}_{1d}(0)$

Converged $\mathbf{q}_{1d}(0)$

$$\begin{pmatrix} \mathbf{C}_q \\ \mathbf{I}_b \end{pmatrix} \mathbf{q}_2 = \begin{pmatrix} -\mathbf{C}_t \\ \mathbf{q}_{2i} \end{pmatrix}$$

Gives $\mathbf{q}_{2d}(0)$

Form \mathbf{B}_i

$$\mathbf{M}_i = \mathbf{B}_i^T \mathbf{M} \mathbf{B}_i$$

Form γ

\mathbf{I}_b Boolean matrix

$$\mathbf{M}_i^{-1} \mathbf{B}_i^T \mathbf{Q}_e, \mathbf{M}_i^{-1} \mathbf{B}_i^T \mathbf{M} \gamma$$

B

$\mathbf{q}_{1i}(\mathbf{h}), \mathbf{q}_{2i}(\mathbf{h})$

Numerical Integration Step

B

The steps in dotted box to be repeated for each subsequent time step; One can use the \mathbf{q}_{1d} from the previous time step as a guess for the Newton iteration