

Department of Mechanical Engineering
Indian Institute of Technology Madras
ME 5233 Multi-body Dynamics & Applications
Assignment 2

Due on: **September 30, 2023**

1. For the system shown in Fig. 1a, let $F = 10$ N, $M^2 = 3$ Nm, $M^3 = 3$ Nm, $\theta^2 = 45^\circ$, and $\theta^3 = 30^\circ$. Determine the generalized forces associated with the generalized coordinates θ^2 and θ^3 . Include the effect of gravity in your calculations.
2. Use the principle of virtual work in dynamics to determine the joint torques M^2 and M^3 for the system shown in Fig. 1a. Use the following data: $\theta^2 = 45^\circ$, $\theta^3 = 30^\circ$, $\dot{\theta}^2 = 70$ rad/s ACW, $\dot{\theta}^3 = 40$ rad/s ACW, $\ddot{\theta}^2 = 120$ rad/s² ACW, $\ddot{\theta}^3 = 180$ rad/s² ACW, and $F = 10$ N. Assume that the two links shown in the figure are uniform slender rods. Consider the effect of gravity.
3. The system shown in Fig. 1b consists of a slider block of mass m^2 and a uniform slender rod of mass m^3 , length l^3 , and mass moment of inertia about its center of mass J^3 . The slider block is connected to the ground by a spring that has a stiffness coefficient k . The slider block is subjected to the force $F(t)$, while the rod is subjected to the moment $M(t)$. Obtain the differential equations of motion of this two-degree-of-freedom system using Lagrange's equation.

Figures are from: A. A. Shabana, 2010, **Computational Dynamics**, Third Edition, John Wiley & Sons.

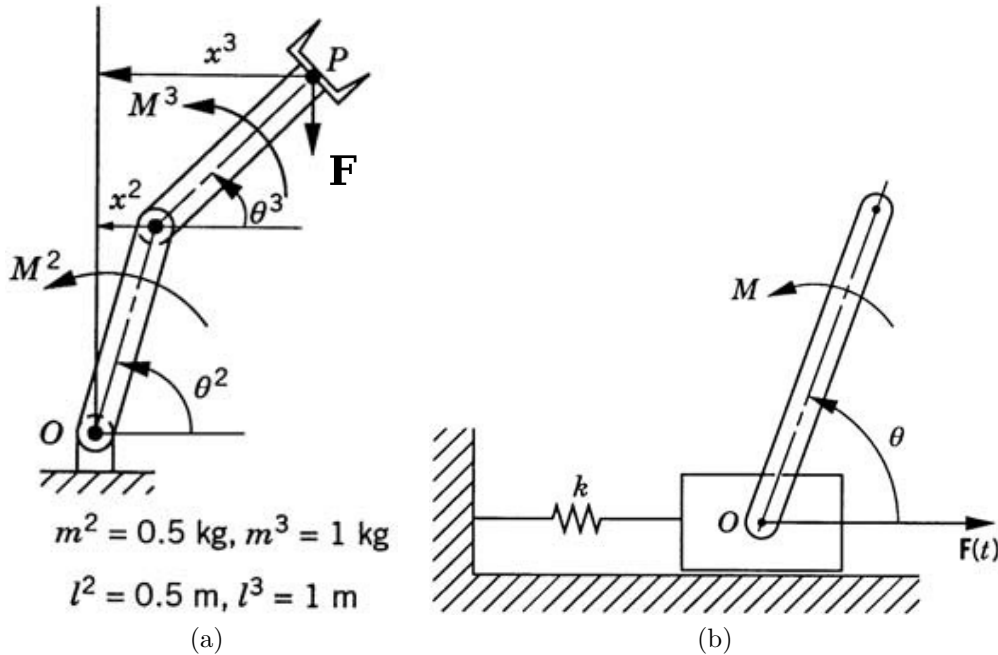


Figure 1: Figures for Problems.