

10 discs

How many moves are needed to move all the discs?

$$2^{10} - 1 = 1023 \checkmark$$

Probability

$$P(E) = \frac{\text{No. of favorable outcomes}}{\text{Total no. of outcomes}}$$

Sample space \rightarrow list of all possible outcomes

$$P(\text{Head}) = \frac{1}{2} = P(\text{Tail})$$

$$S = \{H, T\}$$

BlackJack

A deck contains 52 cards

4 suits \rightarrow Clubs, Diamond, Heart, Spade

13 cards in each suit

Cards \rightarrow A 2 3 4 5 6 7 8 9 10 J Q K

A \rightarrow 1 or 11

10, J, Q, K \rightarrow 10

When do we have a blackjack?

10, A	A, 10
J, A	or J, A
Q, A	Q, A
K, A	K, A

What is the probability of a BlackJack in the first 2 cards drawn from a deck of 52 cards?

$$P(\text{Blackjack}) = \begin{matrix} \checkmark & \text{Face card/10} & \text{and} & \text{Ace in} \\ & \text{in first draw} & & \text{second draw} \end{matrix}$$

OR

$$\begin{matrix} \checkmark & \text{Ace is first} & \text{and} & \text{Face card/10} \\ & \text{drawn} & & \text{in second draw} \end{matrix}$$

$$\left(\frac{4 \times 4}{52} \times \frac{4}{51} \right) + \left(\frac{4}{52} \times \frac{5}{51} \right)$$
$$\left(\frac{16}{52} \times \frac{4}{51} \right) + \left(\frac{4}{52} \times \frac{5}{51} \right)$$

$$\frac{64 + 20}{52 \times 51} = \frac{84}{52 \times 51} = \frac{21}{13 \times 52} = \frac{21}{663} = 3.16\%$$

What is the probability of getting a (20) in first two draws of 52-card deck?

Card 1
10
10
10
K
Q
J
10
Q
K
Q
K
Q
K
Q
A
9

Card 2
J
Q
K
10
10
10
J
Q
Q
K
K
Q
Q
A

Card 1 Facecard or 10 and Card 2 Facecard or 10
or A and 9
or 9 and A

$$\begin{aligned} & \frac{4 \times 4}{52} \times \frac{15}{51} \\ & + \frac{4}{52} \times \frac{4}{51} \\ & + \frac{4}{52} \times \frac{4}{51} \\ & = \frac{(16 \times 15) + 16 + 16}{52 \times 51} \\ & = \frac{240 + 32}{52 \times 51} = \frac{272}{52 \times 51} = \frac{10.25\%}{2} \end{aligned}$$

How many arrangements of a 52-card deck are possible?

$$52! = 52 \times 51 \times 50 \times \dots \times 1 = 8.067 \times 10^{67}$$

□ □ □ ... □

Pair of Dice (Die)

Roll a pair of dice. What is the probability of getting an ~~even~~ number as the sum on the dice?
odd number

1) \boxed{e} \boxed{e}
2) $\boxed{10}$ $\boxed{0}$

$e + e = \text{even}$
 $0 + 0 = \text{even}$

$$\begin{aligned} 1) \frac{3}{6} \times \frac{3}{6} &= \frac{1}{4} & 2) \frac{3}{6} \times \frac{3}{6} &= \frac{1}{4} \\ \frac{1}{4} + \frac{1}{4} &= \frac{1}{2} \end{aligned}$$

$S = \{ \underline{(1,1)}, \underline{(1,2)}, \underline{(1,3)}, \underline{(1,4)}, \underline{(1,5)}, \underline{(1,6)}, \underline{(2,1)}, \underline{(2,2)}, \underline{(2,3)}, \underline{(2,4)}, \underline{(2,5)}, \underline{(2,6)}, \dots, \underline{(6,1)}, \underline{(6,2)}, \underline{(6,3)}, \underline{(6,4)}, \underline{(6,5)}, \underline{(6,6)} \}$

$$|S| = 6 \times 6 = 36$$

$$\text{Even sum} = 3 \times 6 = 18$$

$$P(\text{Even sum}) = \frac{18}{36} = \frac{1}{2}$$

Prime number \rightarrow is a number that has exactly two factors

i) The number itself

ii) 1

4 \rightarrow 2, 2, 4 (Composite num.)

7 \rightarrow 1, 7 (prime number)

2 \rightarrow 1, 2

2 is the smallest prime number.

What is the probability of getting a prime number on a die?

2, 3, 5

$$P(\text{prime}) = \frac{3}{6} = \frac{1}{2} = 50\%$$

13

A Face card - including 10

$$\frac{1}{13} \text{ and } \frac{4}{12}$$

$$\frac{1}{13} \times \frac{4}{12} = \frac{4}{13 \times 12} - \textcircled{A}$$

OR

Face card including 10

A

$$\frac{4}{13}$$

$$\frac{1}{12}$$

$$\frac{4}{13} \times \frac{1}{12} = \frac{4}{13 \times 12} - \textcircled{B}$$

2

$$\frac{\cancel{8}}{13 \times \cancel{12}_3}$$

$$= \frac{2}{39} = 5.13\%$$