

APS

Fermat's Little Theorem

Course Code: 17ECSE309

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USN: 01FE15BEC021

Fermat's Little Theorem

- Intuition

→ It's a fundamental theorem in elementary number theory, which helps to compute powers of integers modulo prime numbers.

→ It finds great application in generation of pseudo-prime numbers' and in encryption for generating large prime factors

Fermat's Little Theorem

- Statement : It states that if p is a prime number, then for any integer a , the number $a^p - a$ is an integer multiple of p . In the notation of modular arithmetic, this is expressed as
- Equation: $a^p = a \pmod{p}$
- Example : If $a = 2$ and $p = 7$, then $2^7 = 128$, and $128 - 2 = 126 = 7 \times 18$ is thus a multiple of 7.

Applications

- The theorem finds many uses in
 1. Cryptography - in particular, underlies the computations used in the RSA public key encryption method.
 2. Pseudo – primes
 3. Number – theory
 4. Primality testing – using corollary, we can test whether the given no is prime or composite.

References:

- <https://brilliant.org/wiki/fermats-little-theorem/>
- [https://en.wikipedia.org/wiki/Fermat%27s little theorem](https://en.wikipedia.org/wiki/Fermat%27s_little_theorem)
- <https://www.quora.com/What-are-the-real-life-applications-of-Fermats-little-theorem>
- <http://mathworld.wolfram.com/FermatsLittleTheorem.html>
- <http://www.quanta-magazine.com/single-post/2017/08/31/Application-of-Fermats-Little-Theorem>

Thank you